# 2D-OOB: Attributing Data Contribution through Joint Valuation Framework

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# **Abstract**

Data valuation has emerged as a powerful framework to quantify the contribution of each datum to the training of a particular machine learning model. However, it is crucial to recognize that the quality of various *cells* within a single data point can vary greatly in practice. For example, even in the case of an abnormal data point, not all cells are necessarily noisy. The single scalar valuation assigned by existing methods blurs the distinction between noisy and clean cells of a data point, thereby compromising the interpretability of the valuation. In this paper, we propose 2D–00B, an out-of-bag estimation framework for jointly determining helpful (or detrimental) samples, as well as the particular cells that drive them. Our comprehensive experiments demonstrate that 2D–00B achieves state-of-the-art performance across multiple use cases, while being exponentially faster. 2D–00B excels in detecting and rectifying fine-grained outliers at the cell level, as well as localizing backdoor triggers in data poisoning attacks.

# 1 Introduction

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From customer behavior prediction and medical image analysis to autonomous driving and policy 15 making, machine learning (ML) systems process ever increasing amounts of data. In such data-rich 16 regimes, a fraction of the samples is often noisy, incorrect annotations are likely to occur, and uniform 17 data quality standards become difficult to enforce. To address these challenges, data valuation emerges 18 as a research field receiving increasing attention, focusing on properly assessing the contribution of each datum to ML training [12]. These methods have proven useful in identifying low-quality 20 samples that can be detrimental to model performance, as well as selecting subsets of data that are 21 representative of enhanced model performance [23, 48, 27]. Furthermore, they are widely applicable 22 in data marketplace for fair revenue allocation and incentive design [51, 45, 40]. 23

Nevertheless, existing data valuation methods assign a scalar score to each datum, thereby failing to 24 account for the varied roles of individual cells. This leaves the valuation rationale unclear and can be 25 unsatisfactory and sub-optimal in various practical scenarios. Firstly, whenever a score is assigned 27 to a data point by a particular data valuation method, it is crucial to understand the underlying justifications to ensure transparency and reliability, especially in high-stakes decision making [39]. 28 Secondly, it is important to recognize the fact that even if a data point is of low quality, it is rarely the 29 case that all the cells within this data point are noisy [37, 26, 43]. The absence of detailed insights into 30 how individual cells contribute to ML training inevitably leads to discarding entire data points. This 31 can result in substantial data waste, particularly when only a few cells are noisy and data acquisition 32 is expensive. Finally, in data markets, different cells within a data point may originate from different data sellers [3, 10]. Consequently, a singular valuation for the entire point fails to offer equitable compensation to all contributing parties.

Age	Income	Experience	Education
25	50000	3	4
34	62000	10	6
45	-1	20	8
29	35000	5	5
40	80000	15	100

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(a) Data valuation

(b) Joint valuation

low valuation scores

Figure 1: **Comparison of data valuation and joint valuation.** (a) Data valuation evaluates the quality of individual data points, whereas (b) joint valuation evaluates the quality of individual cells. Both panels illustrate the same hypothetical dataset, and the darker colors overlaid represent the higher quality or importance. Joint valuation provides a finer level of attributions than data valuation and aims to describe how features affect data values. As panel (b) illustrates, the joint valuation framework can identify outlier cells highlighted with blue boxes (i.e., -1 in "Income" and 100 in "Education") and provide quantitative interpretations of data values.

**Our contributions** In this paper, we propose 2D-00B, a powerful and efficient joint valuation framework that can attribute a data point's value to its individual features. 2D-00B quantifies the importance of each cell in a dataset, as illustrated in Figure 1, providing interpretable insights into which cells are associated with influential data points. Our method is computationally efficient as well as theoretically supported by its connections with Data-00B [23]. Moreover, our extensive empirical experiments demonstrate the practical effectiveness of 2D-00B in various use cases. 2D-00B accurately identifies cell outliers and pinpoints which cells to fix to improve model performance. 2D-00B enables inspection of data poisoning attacks by precisely localizing the backdoor trigger, an artifact inserted into a training sample to induce malicious model behavior [13, 5]. 2D-00B is on average 200 times faster than state-of-the-art methods across all datasets examined.

# 46 2 Preliminaries

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Notations Throughout this paper, we focus on supervised learning settings. For  $d \in \mathbb{N}$ , we denote an input space and an output space by  $\mathcal{X} \subseteq \mathbb{R}^d$  and  $\mathcal{Y} \subseteq \mathbb{R}$ , respectively. We denote a training dataset with n data points by  $\mathcal{D} = \{(x_i, y_i)\}_{i=1}^n$  where  $(x_i, y_i)$  is the i-th pair of the input covariates  $x_i \in \mathcal{X}$  and its output label  $y_i \in \mathcal{Y}$ . For an event A, an indicator function  $\mathbb{1}(A)$  is 1 if A is true, otherwise 0. For  $j \in \mathbb{N}$ , we set  $[j] := \{1, \ldots, j\}$ . For a set S, we denote its power set by  $2^S$  and its cardinality by |S|.

DataShapley The primary goal of data valuation is to quantify the contribution of individual data points to a model's performance. Leveraging the Shapley value in cooperative game theory [38], DataShapley [12] measures the average change in a utility function  $U: 2^{\mathcal{D}} \to \mathbb{R}$  when a data point is removed. For  $i \in [n]$ , DataShapley of i-th datum is defined as follows.

$$\phi_i^{\text{Shap}} := \frac{1}{n} \sum_{k=1}^n \frac{1}{\binom{n-1}{k-1}} \sum_{S \subset \mathcal{D}_k^{(i)}} [U(S \cup \{(x_i, y_i)\}) - U(S)] \tag{1}$$

where  $\mathcal{D}_k^{(i)}:=\{S\subseteq\mathcal{D}|(x_i,y_i)\notin S,|S|=k-1\}$ . DataShapley  $\phi_i^{\mathrm{Shap}}$  in (1) considers every set  $S\in\mathcal{D}_k^{(i)}$  and computes the average difference in utility  $U(S\cup\{(x_i,y_i)\})-U(S)$ . It characterizes the impact of a data point, but its computation requires evaluating U for all possible subsets of  $\mathcal{D}$ , rendering precise calculations infeasible. Many efficient computation algorithms have been studied [15, 25, 50], and in these studies, Shapley-based methods have demonstrated better effectiveness in detecting low-quality samples than standard attribution approaches, such as leave-one-out and influence function methods [20, 9].

Data-OOB As an alternative efficient data valuation method, Kwon and Zou [23] propose Data-OOB, which leverages a bagging model and measures the similarity between a nominal label and weak learners' predictions. To be more specific, we suppose a bagging model consists of B weak learners, where for  $b \in [B]$ , the b-th weak learner  $\hat{h}_b$  is given as a minimizer of the weighted empirical risk,

$$\hat{h}_b := \operatorname{argmin}_h \sum_{i=1}^n w_{bi} \ell(y_i, h(x_i)),$$

where  $\ell: \mathcal{Y} \times \mathcal{Y} \to \mathbb{R}$  is a loss function and  $w_{bi} \in \mathbb{N}$  is the number of times the *i*-th datum  $(x_i, y_i)$  is selected by the *b*-th bootstrap dataset. Let  $\mathbf{w}_b$  be a weight vector  $\mathbf{w}_b := (w_{b1}, \dots, w_{bn})$  for all  $b \in [B]$ . For  $i \in [n]$  and  $\{(\mathbf{w}_b, \hat{h}_b)\}_{b=1}^B$ , Data-00B of the *i*-th datum is defined as follows.

$$\phi_i^{\text{OOB}} := \frac{\sum_{b=1}^B \mathbb{1}(w_{bi} = 0) T(y_i, \hat{h}_b(x_i))}{\sum_{b=1}^B \mathbb{1}(w_{bi} = 0)},$$
(2)

where  $T(y_i, \hat{h}_b(x_i))$  is a score function evaluated at  $(x_i, y_i)$ . We assume that the higher T, the better the prediction. In classification settings, a common choice for T is  $\mathbb{1}(y_i = \hat{h}_b(x_i))$ , and in this case, Data-OOB  $\phi_i^{\text{OOB}}$  measures the average similarity between a nominal label  $y_i$  and weak learners' 73 74 predictions  $\hat{h}_b(x_i)$  when a datum  $(x_i, y_i)$  is *not* sampled in a bootstrap dataset. It intuitively captures the quality of a data point. For instance, when  $(x_i, y_i)$  is a mislabeled sample or an outlier, the label 75 76  $y_i$  is likely to differ from  $\hat{h}_b(x_i)$ , resulting in  $\phi_i^{\rm OOB}$  being close to zero. 77 It is noteworthy that Data-00B in (2) can be computed by training a single bagging model, making 78 it computationally efficient. Kwon and Zou [23] show that Data-OOB can easily scale to millions 79 of data points, but for DataShapley this is often very impractical. In addition, Data-OOB is often 80 81 comparable to or even more effective than DataShapley in detecting mislabeled data points and

# 3 Attributing Data Contribution through Joint Valuation Framework

selecting helpful data points [23, 16].

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Data valuation quantifies desiderata of data points, however, it does not describe what features contribute and how much to those specific data values. For instance, in anomaly detection tasks, data valuation methods can be deployed to detect anomalous data points, but they do not explain why they are abnormal, which is not generally desirable in practice. To address this challenge, we consider a joint valuation framework and assess a cell score for each feature of a data point. Here, a cell score is designed to quantify how a feature affects the value of an individual data point, attributing a data value to features.

To the best of the author's knowledge, Liu et al. [29] first consider a concept of the joint valuation in literature and introduce 2D-Shapley to quantitatively interpret DataShapley. To this end, we denote a 2D utility function by  $u:[n] \times [d] \to \mathbb{R}$ , which takes as input a subset of data points  $S \subseteq [n]$  and a subset of features  $F \subseteq [d]$ , and measure the utility of a fragment of the given dataset consisting of cells  $\{(i,j)\}_{i\in S,j\in F}$ , where a tuple (i,j) denotes a cell at the i-th datum and the j-th column. Then, 2D-Shapley is defined as

$$\psi_{ij}^{\text{2D-Shap}} := \frac{1}{nd} \sum_{k=1}^{n} \sum_{l=1}^{d} \frac{1}{\binom{n-1}{k-1} \binom{d-1}{l-1}} \sum_{(S,F) \subset \mathcal{D}_{k,l}^{(i,j)}} M_u^{i,j}(S,F)$$
(3)

where  $\mathcal{D}_{k,l}^{(i,j)}:=\{(S,F)|S\subseteq[n]\backslash\{i\},F\subseteq[d]\backslash\{j\},|S|=k-1,|F|=l-1\}$  and

$$M_u^{i,j}(S,F) = u(S \cup \{i\}, F \cup \{j\}) + u(S,F) - u(S \cup \{i\}, F) - u(S,F \cup \{j\}).$$

The function  $M_u^{i,j}$  allows us to quantify how much removing a specific cell at (i,j) from a given set  $(S \cup \{i\}, F \cup \{j\})$  affects the overall utility, and 2D-Shapley  $\psi_{ij}^{\text{2D-Shap}}$  evaluates the average  $M_u^{i,j}$  across all possible data fragments  $(S,F) \subset \mathcal{D}_{k,l}^{(i,j)}$ .

Similar to DataShapley, the permutation of all rows and columns required for exact 2D-Shapley calculations presents significant computational challenges. To address this, Liu et al. [29] develop

2D-KNN, which utilizes k-nearest-neighbors models as surrogates to approximate 2D-Shapley val-103 ues. However, the approximation methods can compromise the accuracy of valuations [23, 16]. 104 Additionally, 2D-KNN still faces challenges scaling to large-scale datasets and high-dimensional 105 settings. 106

We propose 2D-00B, an efficient and model-agnostic joint valuation framework that leverages out-107 of-bag estimation to attribute data contribution. We further illustrate how 2D-00B is connected to 108 Data-00B, thereby facilitating sample-wise interpretation for data valuation in Section 3.2. 109

#### 3.1 2D-OOB: an efficient joint valuation framework

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Our idea builds upon the subset bagging model [14], which is well recognized as an earlier version 111 of Breiman's random forest model [4]. A key distinction from a standard bagging model is that a 112 weak learner in a subset bagging model is trained on a randomly selected subset of features. For  $b \in [B]$ , we denote the b-th random feature subset by  $S_b \subseteq [d]$ . Then, the b-th weak learner of a 114 subset bagging model is given as follows.

$$\hat{f}_b := \operatorname{argmin}_f \sum_{i=1}^n w_{bi} \ell(y_i, f(x_{i,S_b})),$$

where  $x_{i,S_b}$  is a subvector of  $x_i$  that only takes elements in a subset  $S_b$ . This difference enables us to assess the impact of which features are more influential: if  $S_b$  includes a helpful (or detrimental) 117 feature, we can expect the out-of-bag prediction  $\hat{f}(x_{i,S_b})$  to be good (or poor). We formalize this intuition and propose 2D-00B. For  $i \in [n], j \in [d]$  and  $\{(w_b, S_b, \hat{f}_b)\}_{b=1}^B$ , the 2D-00B for the j-th 119 cell of the i-th data point is defined as follows, 120

$$\psi_{ij}^{\text{2D-OOB}} := \frac{\sum_{b=1}^{B} \mathbb{1}(w_{bi} = 0, j \in S_b) T(y_i, \hat{f}_b(x_{i,S_b}))}{\sum_{b=1}^{B} \mathbb{1}(w_{bi} = 0, j \in S_b)}, \tag{4}$$

where  $T: \mathcal{Y} \times \mathcal{Y} \to \mathbb{R}$  is a utility function that scores the performance of the weak learner  $\hat{f}_b(x_{i,S_b})$ 121 on the *i*-th datum  $(x_i, y_i)$ . Specifically, for binary or multi-class classification problems, we can 122 adopt  $T(y_i, \hat{f}_b(x_{i,S_b})) = \mathbb{1}(y_i = \hat{f}_b(x_{i,S_b}))$ . In this case, 2D-00B measures the average accuracy score of out-of-bag predictions (specifically, when the *i*-th data point is out-of-bag) if a cell j is used 123 124 in training  $\hat{f}_b$ . For regression problems, we can use the negative squared error loss function, defined 125 as  $T(y_i, \hat{f}_b(x_{i,S_b})) = -(y_i - \hat{f}_b(x_{i,S_b}))^2$ . In practice,  $\mathcal{X}$  could also be incorporated into T to suit the specific use case. 126 127

While Data-00B in (2) aims to assess the impact of the i-th datum, 2D-00B in (4) provides inter-128 pretable insights by evaluating the data point with various combinations of features, revealing which 129 cells are influential to model performance. Leveraging subset bagging scheme, 2D-00B requires a single training of the bagging model, and thus it is computational efficiency. 131

#### 3.2 Connection to Data-OOB 132

We now present interpretable expressions of how 2D-00B connects to Data-00B in the following 133 proposition. To begin with, we denote a set of subsets of [d] by  $S := \{S \subseteq [d]\}$ . With  $\{(\mathbf{w}_b, \hat{f}_b)\}_{b=1}^B$ , 134 we define the *i*-th Data-OOB when a particular subset S is used as follows and denote it by  $\phi_i^{OOB}(S)$ .

$$\phi_i^{\text{OOB}}(S) := \frac{\sum_{b=1}^B \mathbb{1}(w_{bi} = 0)T(y_i, \hat{f}_b(x_{i,S}))}{\sum_{b=1}^B \mathbb{1}(w_{bi} = 0)}.$$
**Proposition 3.1.** For all  $i \in [n]$  and  $j \in [d]$ ,  $\psi_{ij}^{\text{2D-OOB}}$  can be expressed as follows.

$$\psi_{ij}^{\text{2D-OOB}} = \mathbb{E}_{\hat{F}_S}[\phi_i^{\text{OOB}}(S) \mid j \in S],$$

where  $\hat{F}_S$  is an empirical distribution with respect to S induced by the sampling process. 137

A proof is given in the Appendix C. Proposition 3.1 shows that 2D-00B  $\psi_{ij}^{\rm 2D-OOB}$  can be expressed as a conditional empirical expectation of Data-00B provided that the j-th feature is used in Data-00B computation. It provides intuitive interpretations: for a fixed i and  $j \neq k$ ,  $\psi_{ij}^{\rm 2D-OOB} > \psi_{ik}^{\rm 2D-OOB}$  implies that the cell  $x_{ij}$  is more helpful to achieve the high OOB score, which serves as an indicator 138 of model performance, than the cell  $x_{ik}$ .

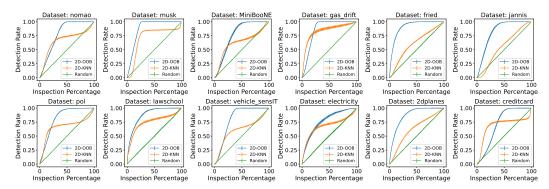


Figure 2: Cell-level outlier detection rate curves for 2D-00B, 2D-KNN, and Random. The x-axis represents the percentage of inspected cells. The y-axis represents the detection rate, defined as the ratio of the number of detected outlier cells to the total number of outlier cells present in a dataset. The error bars show a 95% confidence interval based on 30 independent experiments. We examine the cells in ascending order, starting from those with the lowest values, and thus a curve closer to the left-top corner indicates better performance. 2D-00B efficiently detects the majority of outlier cells by examining only a small fraction of the total cells, while 2D-KNN and Random require scanning nearly all the cells.

# 143 4 Experiments

In this section, we empirically show the effectiveness of 2D-00B across multiple use cases of the joint valuation: *cell-level outlier detection*, *cell fixation*, and *backdoor trigger detection*. As a summary, 2D-00B can precisely identify anomalous cells that should be prioritized for examination and subsequent fixation to improve model performance. In the context of backdoor trigger detection, 2D-00B demonstrates its efficacy by accurately identifying different types of triggers within poisoned data, showcasing its proficiency in detecting non-random, targeted anomalies. Our method also exhibits high computational efficiency through run-time comparison.

Throughout all of our experiments, 2D-00B uses a subset bagging model with B=1000 decision trees. We randomly select a fixed ratio of features to build each decision tree. Unless otherwise specified, we utilize half of the features for each weak learner and set  $T(y_i, \hat{f}(x_{i,S_b})) = \mathbb{1}(y_i = \hat{f}(x_{i,S_b}))$ . The run time is measured on a single Intel Xeon Gold 6226 2.9 Ghz CPU processor.

# 4.1 Cell-level outlier detection

**Experimental setting** In practical situations, even when dealing with abnormal data points, it is not always the case that all cells are noisy [37, 29, 21]. To simulate more realistic settings, we introduce noise to certain *cells* in the following two-step process: First, we randomly select 20% rows for each dataset. We then select 20% columns uniformly at random, allowing each selected row to have a different set of perturbed cells. We inject noises sampled from the low-probability region into these cells, following Du et al. [8] and Liu et al. [29]. Details on the outlier injection process can be found in Appendix A.3.

We use 12 publicly accessible binary classification datasets from OpenML, encompassing a range of both low and high-dimensional datasets, which have been widely used in the literature [12, 22, 23]. Details on these datasets are presented in Appendix A.1. For each dataset, 1000 and 3000 data points are randomly sampled for training and test datasets, respectively. For the baseline method, we consider 2D-KNN, a fast and performant variant of 2D-Shapley [29]. We incorporate a distance regularization term in the utility function T for enhanced performance.

**Results** We calculate the valuations for each cell using our joint valuation framework. Ideally, the outlier cells should receive a low valuation. We then arrange the cell valuations in *ascending* order and inspect those cells with the lowest values first.

Table 1: **Cell-level outlier detection results.** AUC and run-time comparison between 2D-00B and 2D-KNN across the twelve datasets. The average and standard error of the AUC and run-time (in seconds) based on 30 independent experiments are denoted by "average  $\pm$  standard error". Bold numbers denote the best method. The AUC value for the Random method consistently remains at 0.5 across all datasets. Overall, 2D-00B achieves a significantly higher AUC while being orders of magnitude faster than 2D-KNN.

Dataset	AU	C↑	Run-time $\downarrow$		
Dataset	2D-00B (ours)	2D-KNN	2D-00B (ours)	2D-KNN	
lawschool	0.88± 0.0027	$0.75\pm0.0011$	$\textbf{3.33} \pm \textbf{0.06}$	$177.56 \pm 1.92$	
electricity	$0.77 \pm 0.0072$	$0.68 \pm 0.0014$	$\textbf{3.39} \pm \textbf{0.07}$	$191.38 \pm 2.60$	
fried	$0.91 \pm 0.0015$	$0.61 \pm 0.0005$	$\textbf{3.97} \pm \textbf{0.10}$	$322.79 \pm 2.98$	
2dplanes	$0.87 \pm 0.0015$	$0.62 \pm 0.0005$	$\textbf{3.46} \pm \textbf{0.05}$	$295.25 \pm 2.37$	
creditcard	$0.72 \pm 0.0028$	$0.69 \pm 0.0011$	$\textbf{4.56} \pm \textbf{0.10}$	$662.34 \pm 7.12$	
pol	$0.82 \pm 0.0014$	$0.67 \pm 0.0006$	$\textbf{4.34} \pm \textbf{0.05}$	$759.33 \pm 4.37$	
MiniBooNE	$0.77 \pm 0.0058$	$0.63 \pm 0.0019$	$\textbf{7.46} \pm \textbf{0.06}$	$1507.83 \pm 14.50$	
jannis	$0.83 \pm 0.0042$	$0.55 \pm 0.0004$	$\textbf{7.98} \pm \textbf{0.07}$	$1753.10 \pm 12.35$	
nomao	$0.79 \pm 0.0021$	$0.67 \pm 0.0009$	$\textbf{7.69} \!\pm \textbf{0.11}$	$2564.58 \pm 23.11$	
vehicle_sensIT	$0.81 \pm 0.0014$	$0.61 \pm 0.0005$	$\textbf{9.87} \pm \textbf{0.08}$	$3113.65 \pm 24.54$	
gas_drift	$0.86 \pm 0.0010$	$0.84 \pm 0.0017$	$11.28 \pm 0.10$	$3878.31 \pm 40.72$	
musk	$0.88 \pm 0.0008$	$0.71 \pm 0.0006$	$\textbf{14.09} \pm \textbf{0.11}$	$4415.45 \pm 22.96$	
Average	0.83	0.67	6.78	1636.80	

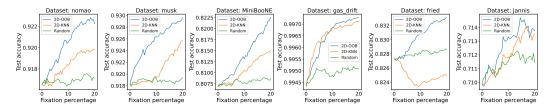


Figure 3: Cell fixation experiment results (test accuracy curves) for 2D-00B, 2D-KNN, and Random. We replace cells with their corresponding ground-truth annotations, starting with those cells assigned the lowest valuations. The results from 6 datasets are presented, and additional results are provided in Appendix B.2. We conduct 30 independent trials and report the average results. A higher curve indicates better performance. 2D-00B demonstrates a superior capability in accurately identifying and rectifying cell-level outliers.

The detection rate curve of inserted outlier is shown in Figure 2. For all datasets, 2D-00B successfully identifies over 90% of the outlier cells by inspecting only 30% of the bottom cells. In comparison, 2D-KNN requires examining nearly 90% of the cells to achieve the same detection level.

We also evaluate the area under the curve (AUC) as a quantitative metric and the run-time. As Table 1 shows, 2D-00B achieves an average AUC of 0.83 across 12 datasets, compared to 0.67 for 2D-KNN, while being significantly faster. For high-dimensional datasets such as the musk dataset, which comprises 166 features, 2D-KNN would take more than an hour to process, while 2D-00B can finish in seconds. Furthermore, we present additional results on **multi-class classification** datasets in Appendix B.1, demonstrating the consistently superior performance and efficiency of 2D-00B.

# 4.2 Cell fixation experiment

**Experimental setting** A naive strategy to handle cell-level outliers is to eliminate data points that contain outliers. This method, however, risks substantial data loss, particularly when outliers are scattered and data points are costly to collect. We instead consider a cell fixation experiment, where we assume that the ground-truth annotations of outlier cells can be restored with external expert knowledge. At each step, we "fix" a certain number of cells by substituting them with their ground-truth annotations, prioritizing cells that have the lowest valuations. Then we fit a logistic model and evaluate the model's performance with a test set of 3000 samples. It is important to note that correcting normal cells has no effect, whereas fixing outlier cells is expected to enhance the model's performance. We adopt the same datasets and implementations as in Section 4.1.

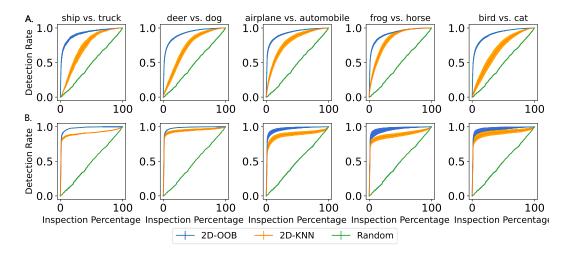


Figure 4: **Backdoor trigger detection rate curve for** 2D-00B, 2D-KNN, **and** Random. The panels A. and B. correspond to Trojan square and BadNets square, respectively. We prioritize cells within each poisoned sample, ranking from highest to lowest based on their valuations. The detection rate curve shows the average detection rate across all poisoned samples, and error bars represent a 95% confidence interval based on 15 independent runs. 2D-00B demonstrates superior performance in detecting the cells implanted with triggers.

**Results** Figure 3 illustrates the anticipated trend in the performance of 2D-00B, validating our method's capability to accurately identify and prioritize the most impactful outliers for correction. As cells with the lowest valuations are progressively fixed, 2D-00B demonstrates a consistent improvement in model accuracy. In contrast, when applying the same procedure with 2D-KNN, such notable performance enhancements are not observed.

Additionally, we investigate a scenario where ground-truth annotations remain unavailable. We adopt the setup from Liu et al. [29], where we replace the outlier cells with the average of other cells in the same feature column. 2D-00B uniformly demonstrates significant superiority over its counterparts. Results are provided in Appendix B.2.

# 4.3 Backdoor trigger detection

A common strategy of data poisoning attacks involves inserting a predefined trigger (e.g., a specific pixel pattern in an image) into a few training data [13, 5, 28]. These malicious manipulations can be challenging to detect as they only infect targeted samples. Even when poisoned data are present, it could be difficult to discern the cause of attacks since manually reviewing the images is expensive and time-consuming. In this experiment, we introduce a novel joint valuation task: detecting backdoor triggers in data poisoning attacks. Distinct from random outliers investigated previously, such cell contamination is targeted and deliberate.

We consider two popular backdoor attack algorithms: BadNets [13] and Trojan Attack [28]. The poisoned samples, relabeled as the adversarial target class, are mixed up with the clean data in the training process. As a result, the model is trained to incorrectly treat the trigger as a main feature of the poisoned samples. At the test time, those inputs containing the trigger will be misclassified to the target class. In this context, our goal is to effectively pinpoint the triggers by recognizing them as influential features through our joint valuation framework.

Experimental setting We select 5 pairs of CIFAR-10 classes. For each pair, we designate one as the target attack class and the other as the source class. The training dataset comprises 1000 images. For each attack, we contaminate 15% of the training samples from the source class and relabel them to the target class. Two types of attack triggers are implemented: Trojan square and BadNets square [13, 35, 28]. These triggers are placed in the lower right corner of the original images to minimize occlusion. Details of these attacks are available in the Appendix A.4. In our experiment, the ratio of poisoned cells is approximately 1%. We sample 25% features to build each weak learner.

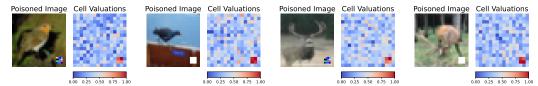


Figure 5: Qualitative examples for 2D-00B in the backdoor trigger detection task. Each pair of images shows a poisoned image and its cell valuation. The color of the heatmap indicates importance: red cells are more important than blue cells. The first two pairs consider the case the class "bird" is relabeled as "cat", and the latter two pairs consider the case the class "deer" is relabeled as "cat". The heatmaps clearly show that higher cell valuations predominantly concentrate on the regions containing triggers, while areas featuring actual objects receive lower valuations. This pattern suggests that 2D-00B effectively captures the triggers as the impactful features responsible for the misclassification of the poisoned samples.

Results We adopt the same detection scheme and baseline methods as in Section 4.1. Ideally, the poisoned cell should receive a high valuation based on the fact that such data point has been relabeled. We plot the detection rate curves of five datasets as shown in Figure 4. 2D-00B significantly outperforms 2D-KNN in detecting both types of triggers. Overall, 2D-00B achieves an average AUC of 0.95 across all datasets and attack types, compared to 0.83 for 2D-KNN.

Qualitative examples Figure 5 displays the heatmaps for poisoned samples based on cell valuations of 2D-00B. Areas with higher cell valuations (marked as dark red color) precisely indicate the trigger location in these samples, illustrating the effectiveness of our detection. More examples are included in the Appendix B.3.

#### 4.4 Ablation study

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We conduct ablation studies on the cell-level outlier detection task, as outlined in Section 4.1, to examine the impact of the selection and number of weak learners on 2D-00B estimations.

Selection of weak learners Although our study primarily employs decision trees as weak learners, it is important to note that 2D-00B is **model-agnostic**, enabling the use of any class of machine learning models as weak learners. We compare efficacy of decision trees, logistic regression, a single-layer MLP with 64 dimensions, and a two-layer MLP with 64 and 32 dimensions.

Table 2 presents a comparison of detection AUC across 12 datasets, indicating that 2D-00B is not model-free. The selection of weak learners slightly affects the valuation results, with more complex models generally yielding better performance. Nonetheless, all variations of 2D-00B outperform 2D-KNN, highlighting the significant advantages of the 2D-00B approach.

The number of weak learners Increasing the number of weak learners allows for a greater number of data-feature subset pairs to be explored, potentially leading to more accurate estimates. However, we empirically observe that beyond a certain threshold, adding extra weak learners does not substantially enhance performance, indicating convergence of the estimation in Appendix B.4. As a summary, we vary the number of weak learners  $B \in \{500, 1000, 3000\}$  and compare the cell-level outlier detection performance. Typically, when the number of weak learners is 1000, i.e., B = 1000, it is sufficient to achieve converged estimates across different datasets.

Lastly, we present additional ablation study results for other key hyperparameters in Appendix B.4.
Apart from the experiments discussed above, we showcase that marginalization of 2D-00B can either match or surpass state-of-the-art data valuation methods on standard benchmarks in Appendix D.

# 5 Related work

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Data contribution estimation In addition to the marginal contribution-based methods discussed in Section 2, many other approaches are emerging in the area of data valuation. Just et al. [18] develop a non-conventional class-wise Wasserstein distance between the training and validation sets and use the

Table 2: **Ablation study results of weak learner types.** The average and standard error of the AUC based on 30 independent experiments are denoted by "average  $\pm$  standard error". Results of 2D-KNN are added for comparison. Different types of weak learners lead to variations in the valuation results, with more complex models generally showing better performance.

Dataset	Decision Tree	Logistic Regression	MLP (single-layer)	MLP (two-layer)	2D-KNN (Baseline)
lawschool	$0.88 \pm 0.0027$	$0.81 \pm 0.0014$	$0.83 \pm 0.0023$	$0.86 \pm 0.0049$	$0.75 \pm 0.0011$
electricity	$0.77 \pm 0.0072$	$0.75 \pm 0.0029$	$0.75 \pm 0.0039$	$0.74 \pm 0.0064$	$0.68 \pm 0.0014$
fried	$0.91 \pm 0.0015$	$0.82 \pm 0.0023$	$0.85 \pm 0.0020$	$0.88 \pm 0.0027$	$0.61 \pm 0.0005$
2dplanes	$0.87 \pm 0.0015$	$0.82 \pm 0.0026$	$0.86 \pm 0.0026$	$\textbf{0.88} \pm \textbf{0.0037}$	$0.62 \pm 0.0005$
creditcard	$0.72 \pm 0.0028$	$\textbf{0.74} \pm \textbf{0.0023}$	$\textbf{0.74} \pm \textbf{0.0026}$	$\textbf{0.74} \pm \textbf{0.0071}$	$0.69 \pm 0.0011$
pol	$0.82 \pm 0.0014$	$0.79 \pm 0.0029$	$0.85 \pm 0.0014$	$\textbf{0.86} \pm \textbf{0.0019}$	$0.67 \pm 0.0006$
MiniBooNE	$0.77 \pm 0.0058$	$0.77 \pm 0.0059$	$0.80 \pm 0.0057$	$\textbf{0.81} \pm \textbf{0.0119}$	$0.63 \pm 0.0019$
jannis	$0.83 \pm 0.0042$	$0.76 \pm 0.0040$	$0.79 \pm 0.0048$	$0.80 \pm 0.0108$	$0.55 \pm 0.0004$
nomao	$0.79 \pm 0.0021$	$0.82 \pm 0.0012$	$\textbf{0.83} \pm \textbf{0.0010}$	$\textbf{0.83} \pm \textbf{0.0017}$	$0.67 \pm 0.0009$
vehicle-sensIT	$0.81 \pm 0.0014$	$0.81 \pm 0.0026$	$0.80 \pm 0.0025$	$\textbf{0.82} \pm \textbf{0.0037}$	$0.61 \pm 0.0005$
gas-drift	$0.86 \pm 0.0010$	$\textbf{0.89} \pm \textbf{0.0005}$	$0.88 \pm 0.0005$	$0.88 \pm 0.0006$	$0.84 \pm 0.0017$
musk	$0.88 \pm 0.0008$	$0.87 \pm 0.0005$	$\textbf{0.88} \pm \textbf{0.0005}$	$\textbf{0.88} \pm \textbf{0.0008}$	$0.71 \pm 0.0006$
Average	0.83	0.80	0.82	0.83	0.67

gradient information to evaluate each data point. Wu et al. [47] extend data valuation to deep neural networks, introducing a training-free data valuation framework based on neural tangent kernel theory. Yoon et al. [48] leverage reinforcement learning techniques to automatically learn data valuation scores by training a regression model. However, all these data valuation methods do not assign importance scores to cells, whereas our method provides additional insights into how individual cells contribute to the data valuations.

**Feature attribution** Feature attribution is a pivotal research domain in explainable machine learning that primarily aims to provide insights into how individual features influence model predictions. Various effective methods have been proposed, including SHAP-based explanation [30, 31, 24, 7, 6], counterfactual explanation [44, 17, 36, 32, 33], and backpropagation-based explanation [1, 2, 42, 41, 49]. Among these methods, the SHAP-based explanation stands out as the most widely adopted approach, utilizing cooperative game theory principles to compute the Shapley value [38]. While feature attribution offers a potential method to attribute data valuation scores across individual cells, our empirical experiments in Appendix B.1 reveal that this two-stage scheme falls short in efficacy compared to our proposed joint valuation paradigm, which integrates data valuation and feature attribution in a simultaneous process.

#### 6 Conclusion

We propose 2D-00B, an efficient joint valuation framework that assigns a score to each cell in a dataset, thereby facilitating a finer attribution of data contribution and enabling a deeper understanding of datasets. Through comprehensive experiments, we show that 2D-00B is computationally efficient and competitive over state-of-the-art methods in both joint valuation tasks.

**Limitation and future work** While our study primarily explores random forest models applied to tabular datasets and simple image datasets, the potential application of neural network models within the 2D-00B framework for more complex vision and language tasks presents a promising avenue for future investigation. For instance, in text datasets, tokens or words can be treated as cells. 2D-00B can be easily integrated into any bagging training scheme that uses language models.

Overall, we believe that our work will inspire further exploration in the field of joint valuation, with the broader goal of improving the transparency and interpretability of machine learning, as well as developing an equitable incentive mechanism for data sharing.

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# 408 Supplementary Materials

- In the supplementary materials, we provide implementation details, additional experimental results,
- rigorous formalized proofs and data valuation experiment results. Code repository can be found at
- 411 https://anonymous.4open.science/r/2d-oob-C4AO/.

# 412 A Implementation details

#### 413 A.1 Datasets

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- Tabular datasets We use 12 binary classification datasets obtained from OpenML [11]. A summary of all the datasets is provided in Table 3. These datasets are used in Section 4.1, 4.2, and Appendix D.
- 416 For each dataset, we first employ a standard normalization procedure, where each feature is normalized
- to have zero mean and unit standard deviation. After preprocessing, we randomly partition a subset
- of the data into two non-overlapping sets: a training dataset and a test dataset, which consists of
- 419 1000 and 3000 samples respectively. The training dataset is used to obtain the joint (or marginal)
- valuation for each cell (or data point). The test dataset is exclusively used for cell fixation (or point
- removal) experiments when evaluating the test accuracy. Note that for methods that need a validation
- dataset such as KNNShapley and DataShapley, we additionally sample a separate validation dataset
- 423 (disjoint from training dataset and test dataset) to evaluate the utility function. The size of the
- validation dataset is set to 10% of the training sample size.
- Image datasets We create datasets by pairing CIFAR-10 classes, each pair consisting of a target
- attack class and a source class. The training and test dataset comprises 1000 and 2000 samples
- respectively. The size of the validation dataset is set to 10% of the training sample size. To manage
- the computational challenges posed by the baseline method, we employ the super-pixel technique
- to transform the (32,32,3) image into a 256-dimensional vector. Specifically, we first average the
- pixel values across three channels for each pixel. Then, we partition these transformed images into
- equally sized  $2 \times 2$  grids. In each grid, we use average pooling to reduce the pixel values to a single
- cell value. These cell values are then arranged into a flattened input vector. We annotate a cell as
- poisoned if at least 25% of its corresponding grid area contains the trigger.

#### A.2 Implementation details for different methods

- 435 2D-00B 2D-00B involves fitting a subset random forest model with B=1000 decision trees based
- on the package "scikit-learn". When constructing each decision tree, we fix the feature subset size
- ratio as 0.5. Ablations on the hyperparameters can be found in Appendix B.4. For Section 4.3 and
- Appendix D, we simply adopt  $T(y_i, \hat{f}(x_{i,S_b})) = \mathbb{1}(y_i = \hat{f}(x_{i,S_b}))$ . For Section 4.1 and 4.2, we
- further calculate the normalized negative L2 distance between covariates and the class-specific mean in
- the bootstrap dataset, denoted as  $d_{norm}$ . Then we use  $T(y_i, f(x_{i.S_h})) = \mathbb{1}(y_i = f(x_{i.S_h})) + d_{norm}$ .
- 441 2D-KNN 2D-KNN employs KNN as a surrogate model to approximate 2D-Shapley. We set the
- number of nearest neighbors as 10 and the number of permutations as 1000. The hyperparameters
- are selected based on convergence behavior and we determine the run time until the values converge.

#### 444 A.3 Implementation details for cell-level outlier generation

- Following Du et al. [8] and Liu et al. [29], we replace a given cell with the outlier value. Here, the
- outlier value is randomly generated from the two-sided "tails" of the Gaussian distribution with the
- column mean and standard deviation, where the probability of the two-sided tail area is set to be 1%.
- 448 4% (20%  $\times$  20%) of the cells in total are replaced with the corresponding outlier value.

# A.4 Implementation details for backdoor trigger generation

- 450 Following the prior work [13, 28], we generate the BadNets square and the Trojan square trigger. For
- BadNets, we adopt the implementation in Nicolae et al. [34]. For Trojan Attack, we use a pretrained
- 52 ResNet18 model on CIFAR-10 dataset and employ the implementation in Pang et al. [35]. For

each attack, we evaluate its effectiveness by training a decision tree model on the poisoned dataset.

The accuracy on a clean test set remains nearly unchanged compared to the model trained on an

uncontaminated training set, while the attack success rate on a hold-out poisoned test sample set is

456 guaranteed to exceed 75%.

Table 3: A summary of all the datasets used in 4.1, 4.2, and Appendix D. These datasets have been commonly used in previous literature [12, 22, 23]

Name	Total sample size	Input dimension	Majority class proportion	OpenML ID
lawschool	20800	6	0.679	43890
electricity	38474	6	0.5	44080
fried	40768	10	0.502	901
2dplanes	40768	10	0.501	727
creditcard	30000	23	0.779	42477
pol	15000	48	0.664	722
MiniBooNE	72998	50	0.5	43974
jannis	57580	54	0.5	43977
nomao	34465	89	0.715	1486
vehicle_sensIT	98528	100	0.50	357
gas_drift	5935	128	0.507	1476
musk	6598	166	0.846	1116

# 457 B Additional experimental results

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In Section 4.1, we demonstrate that 2D-00B shows promising performance in identifying cell-level outliers. This section further shows that our result is not sensitive to the selection of hyperparameters. Furthermore, ours generally performs better than 2D-KNN in different settings. We also provide additional results for Section 4.2 and 4.3.

#### **B.1** Additional results for cell-level outlier detection

**Additional results on multi-class classification datasets** We have conducted cell-level outlier detection experiments (as in Section 4.1) on three multi-class classification datasets from the UCI Machine Learning repository [19]. As shown in the table, 2D-00B displays superior detection performance and efficiency.

Table 4: Cell-level outlier experiment results on multi-class classification datasets The average and standard error of the detection AUC and Elapsed Time (in seconds) based on 30 independent experiments are denoted by "average  $\pm$  standard error".

Dataset	AUC↑		Run-time ↓		
Dataset	2D-00B (ours)	2D-KNN	2D-00B (ours)	2D-KNN	
Covertype	0.81±0.0156	0.63±0.0183	3.98±0.5774	962.34±1.3383	
Dry Bean	$0.88 {\pm} 0.0059$	$0.85\pm0.0192$	$3.31 \pm 0.4586$	$347.80\pm2.0212$	
Wine Quality	$0.86{\pm}0.0178$	$0.57\pm0.0252$	$2.90 \pm 0.1240$	$269.14 \pm 1.1825$	

Additional baseline: two-stage attribution Once we obtain the data valuation scores, an alternative solution approach to determining cell-level attributions involves leveraging feature attribution methods such as SHAP [30]. We explore an additional baseline method building upon this idea: initially, Data-OOB (or any other data valuation method) is computed for the i-th data point, denoted as  $dv_i$ . Subsequently, TreeSHAP [31] is fitted, using  $dv_i$  as the target and the concatenation of  $x_i$  and  $y_i$  (denoted as  $x_i \oplus y_i$ ) as the predictor. The derived local feature attributions are then interpreted as joint valuation results. We refer to this method as 'two-stage attribution'.

Table 5 indicates that 2D-00B substantially outperforms its two-stage counterpart. We hypothesize that the superiority of our method stems from integrating data valuation and feature attribution into a cohesive framework. Conversely, the two-stage method treats data valuation and feature

Table 5: **Cell-level outlier detection results (AUC) of 2D-00B and the two-stage attribution.** Our method shows a better performance than the alternative method by a significant performance margin.

D-44	AUC↑			
Dataset	2D-00B (ours)	Two-stage attribution		
lawschool	0.88± 0.0027	$0.83 \pm 0.0064$		
electricity	$0.77 \pm 0.0072$	$0.64 \pm 0.0093$		
fried	$0.91\pm0.0015$	$0.82 \pm 0.0068$		
2dplanes	$0.87 \pm 0.0015$	$0.80 \pm 0.0058$		
creditcard	$0.72 \pm 0.0028$	$0.67 \pm 0.0051$		
pol	$0.82 \pm 0.0014$	$0.78 \pm 0.0042$		
MiniBooNE	$0.77 \pm 0.0058$	$0.70\pm0.0041$		
jannis	$0.83 \pm 0.0042$	$0.62\pm0.0043$		
nomao	$0.79 \pm 0.0021$	$0.71 \pm 0.0041$		
vehicle_sensIT	$0.81 \pm 0.0014$	$0.64 \pm 0.0033$		
gas_drift	$0.86 \pm 0.0010$	$0.73 \pm 0.0143$		
musk	$0.88 \pm 0.0008$	$0.68 \pm 0.0028$		
Average	0.83	0.72		

Table 6: Cell-level outlier detection results (AUC) of different joint valuation methods when the row outlier ratio and column outlier ratio are both 50%. Our method consistently outperforms 2D-KNN even in the presence of significant noise.

Detect	AU	<u>C</u> ↑
Dataset	2D-00B (ours)	2D-KNN
lawschool	$0.75 \pm 0.0084$	$0.60 \pm 0.0144$
electricity	$0.64 \pm 0.0155$	$0.60 \pm 0.0106$
fried	$0.74 \pm 0.0087$	$0.54 \pm 0.0027$
2dplanes	$0.74 \pm 0.0063$	$0.55 \pm 0.0033$
creditcard	$0.63 \pm 0.0055$	$0.61 \pm 0.0053$
pol	$0.69 \pm 0.0069$	$0.60 \pm 0.0042$
MiniBooNE	$0.67 \pm 0.0128$	$0.60 \pm 0.0048$
jannis	$0.70 \pm 0.0113$	$0.53 \pm 0.0014$
nomao	$0.70 \pm 0.0088$	$0.58 \pm 0.0052$
vehicle_sensIT	$0.70 \pm 0.0075$	$0.55 \pm 0.0031$
gas_drift	$0.73 \pm 0.0077$	$0.65 \pm 0.0114$
musk	$0.77 \pm 0.0063$	$0.64 \pm 0.0038$
Average	0.71	0.59

attribution as separate processes, potentially resulting in sub-optimal outcomes. Furthermore, due to the computational complexity of TreeSHAP, the two-stage approach is notably slower compared to our method.

A noisy setting with more outlier cells We consider a more challenging scenario with increased outlier levels, where both the row outlier ratio and column outlier ratio increase from 20% (as in Section 4.1) to 50%. Consequently, this leads to 25% ( $50\% \times 50\%$ ) of the cells being replaced with outlier values. We follow the same outlier generation procedure outlined in Appendix A.3. The findings, presented in Table 6, demonstrate that our method maintains a significantly superior performance over 2D-KNN, even under such a noisy setting.

# **B.2** Additional results for cell fixation experiment

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Figure 6 presents the results for the cell fixation experiment on 6 additional datasets. 2D-00B excels in precisely detecting and correcting relevant cell outliers.

**The scenario without ground-truth knowledge** Following [29], we examine a situation where external information on the ground-truth annotations of outlier cells is not accessible. In this scenario, we address these outliers by substituting them with the average of other cells in the same feature column. This procedure starts by addressing cells with the lowest valuations, based on the hypothesis

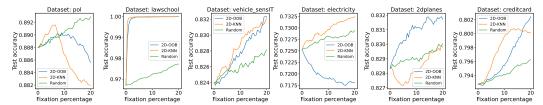


Figure 6: Cell fixation experiment results (test accuracy curves) for 2D-00B, 2D-KNN and a random baseline. We replace cell values with ground-truth values from the cells with the lowest valuation to the highest valuation. The results from 6 datasets are displayed. We conduct 30 independent trials and report the average results. A higher curve indicates better performance. 2D-00B sets itself apart by its remarkable precision in detecting and rectifying relevant cell outliers.

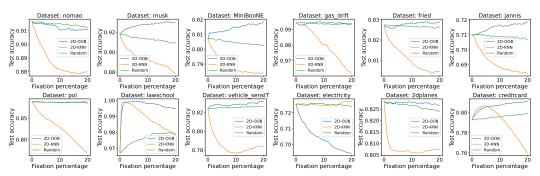


Figure 7: Cell fixation experiment (without ground-truth knowledge) results (test accuracy curves) for 2D-00B, 2D-KNN and a random baseline. We replace cell values with column mean imputations from the cells with the lowest value to the highest value. The results from 6 datasets are displayed. We conduct 30 independent trials and report the average results. A higher curve indicates better performance.

that correcting these cells is likely to maintain or potentially improve the model's performance. As depicted in Figure 7, 2D-00B conforms to this expected trend, demonstrating the effectiveness of our method in joint valuation. Conversely, 2D-KNN fails to show similar performance improvements.

# 496 B.3 Additional results for backdoor trigger experiment

We provide additional qualitative examples of backdoor trigger detection experiments in Figure 8.

# 498 B.4 Additional results for ablation study

We present the results of ablation study on the number of base learners B and feature subset ratio K/d. Specifically, we examine the AUC of the detection curve in the cell-level outlier detection experiment (refer to Table 1).

The number of base learners B When we increase the number of base learners from 500 to 3000, the detection AUC for each dataset remains unchanged, as shown in Table 7. This indicates that 1000 base learners are sufficient to get an equitable joint valuation.

Feature subset ratio K/d In addition to 0.50, We test two additional feature subset ratios 0.25 and 0.75. The results in Table 8 suggest that in general, the joint valuation capacity of our method is robust to the choice of feature subset ratio.

# C Proof of Proposition 3.1

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Proof. For simplicity, we denote  $\phi_i^{\text{OOB}}(S)$  as  $\phi_i(S)$  and  $\psi_{ij}^{\text{2D-OOB}}$  as  $\psi_{ij}$  in the proof. With the set of subsets  $\mathcal{S} := \{S \subseteq [d]\}$  and the definition Data-OOB  $\phi_i(S)$  for all  $i \in [n]$ , where S is

Table 7: Ablation results on the number of base learners B. The cell-level outlier detection results (AUC) are examined. Increasing the number of base learners from 1000 to 3000 does not yield a notable performance improvement.

Dataset	<b>AUC</b> ↑		
Dataset	B = 500	B = 1000	B = 3000
lawschool	$0.86 \pm 0.0035$	$0.88 \pm 0.0027$	$0.88 \pm 0.0026$
electricity	$0.77 \pm 0.0062$	$0.77 \pm 0.0072$	$0.77 \pm 0.0070$
fried	$0.87 \pm 0.0022$	$0.91 \pm 0.0015$	$0.91 \pm 0.0014$
2dplanes	$0.87 \pm 0.0016$	$0.87 \pm 0.0015$	$0.87 \pm 0.0015$
creditcard	$0.72 \pm 0.0025$	$0.72 \pm 0.0028$	$0.72 \pm 0.0028$
pol	$0.78 \pm 0.0022$	$0.82 \pm 0.0014$	$0.82 \pm 0.0014$
MiniBooNE	$0.77 \pm 0.0042$	$0.77 \pm 0.0058$	$0.77 \pm 0.0058$
jannis	$0.78 \pm 0.0045$	$0.83 \pm 0.0042$	$0.83 \pm 0.0039$
nomao	$0.79 \pm 0.0018$	$0.79 \pm 0.0021$	$0.79 \pm 0.0020$
vehicle_sensIT	$0.80 \pm 0.0021$	$0.81 \pm 0.0014$	$0.81 \pm 0.0014$
gas_drift	$0.86 \pm 0.0007$	$0.86 \pm 0.0010$	$0.86 \pm 0.0010$
musk	$0.88 \pm 0.0008$	$0.88 \pm 0.0008$	$0.88 \pm 0.0008$
Average	0.81	0.83	0.83

Table 8: Ablation results on feature subset ratio K/d. The cell-level outlier detection results (AUC) are examined. Our method's joint valuation capacity remains relatively stable regardless of the selected feature subset ratio.

Dataset	AUC ↑				
Dataset	K/d = 0.25	K/d = 0.50	K/d = 0.75		
lawschool	$0.86 \pm 0.0026$	$0.88 \pm 0.0027$	$0.88 \pm 0.0024$		
electricity	$0.79 \pm 0.0070$	$0.77 \pm 0.0072$	$0.73 \pm 0.0070$		
fried	$0.86 \pm 0.0024$	$0.91\pm0.0015$	$0.89 \pm 0.0007$		
2dplanes	$0.82 \pm 0.0015$	$0.87 \pm 0.0015$	$0.88 \pm 0.0014$		
creditcard	$0.73 \pm 0.0029$	$0.72\pm0.0028$	$0.71\pm0.0028$		
pol	$0.66 \pm 0.0031$	$0.82 \pm 0.0014$	$0.82 \pm 0.0014$		
MiniBooNE	$0.78 \pm 0.0076$	$0.77 \pm 0.0058$	$0.77 \pm 0.0049$		
jannis	$0.84 \pm 0.0035$	$0.83 \pm 0.0042$	$0.82 \pm 0.0043$		
nomao	$0.79 \pm 0.0019$	$0.79 \pm 0.0021$	$0.78 \pm 0.0021$		
vehicle_sensIT	$0.81 \pm 0.0014$	$0.81\pm0.0014$	$0.80\pm0.0015$		
gas_drift	$0.88 \pm 0.0009$	$0.86 \pm 0.0010$	$0.86 \pm 0.0009$		
musk	$0.89 \pm 0.0008$	$0.88 \pm 0.0008$	$0.88 \pm 0.0008$		
Average	0.81	0.83	0.82		

a feature subset, we denote the cardinality of  $\mathcal S$  as  $L:=|\mathcal S|=2^d$ . Let  $\gamma_b$  be a weight vector  $\gamma_b:=(\gamma_{b1},\ldots,\gamma_{bL})$  for all  $b\in[B]$ , where  $\gamma_{bl}\in\{0,1\}$  and  $\gamma_{bl}=1$  indicates the l-th subset is used in the b-th weak learner. With  $\{w_b,\gamma_b,\hat f_b\}_{b=1}^B$ , we can also denote the i-th Data-OOB on l-th feature subset  $S_l$  as

$$\phi_i(S_l) = \frac{\sum_{b=1}^B \mathbb{1}(w_{bi} = 0)\mathbb{1}(\gamma_{bl} = 1)T(y_i, \hat{f}_b(x_{i,S_l}))}{\sum_{b=1}^B \mathbb{1}(w_{bi} = 0)\mathbb{1}(\gamma_{bl} = 1)}.$$

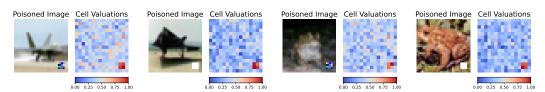


Figure 8: Qualitative results on more datasets for the backdoor trigger detection experiment. The first two images originate from the class "airplane" while relabeled as "automobile". The latter two images originate from the class "frog" while relabeled as "horse".

With slight abuse of notation, the formulation of 2D-00B in (4) can be expressed as follows.

$$\begin{split} \psi_{ij} &= \frac{\sum_{l=1}^{L} \sum_{b=1}^{B} \mathbb{1}(w_{bi} = 0) \mathbb{1}(\gamma_{bl} = 1) \mathbb{1}(j \in S_{l}) T(y_{i}, \hat{f}_{b}(x_{i}, S_{l}))}{\sum_{l=1}^{L} \sum_{b=1}^{B} \mathbb{1}(w_{bi} = 0) \mathbb{1}(\gamma_{bl} = 1) \mathbb{1}(j \in S_{l})} \\ &= \sum_{l=1}^{L} \mathbb{1}(j \in S_{l}) \frac{\sum_{b=1}^{B} \mathbb{1}(w_{bi} = 0) \mathbb{1}(\gamma_{bl} = 1) T(y_{i}, \hat{f}_{b}(x_{i}, S_{l}))}{\sum_{l=1}^{L} \sum_{b=1}^{B} \mathbb{1}(w_{bi} = 0) \mathbb{1}(\gamma_{bl} = 1) \mathbb{1}(j \in S_{l})} \\ &= \sum_{l=1}^{L} \mathbb{1}(j \in S_{l}) \frac{\sum_{b=1}^{B} \mathbb{1}(w_{bi} = 0) \mathbb{1}(\gamma_{bl} = 1)}{\sum_{l=1}^{L} \sum_{b=1}^{B} \mathbb{1}(w_{bi} = 0) \mathbb{1}(\gamma_{bl} = 1)} \frac{\sum_{b=1}^{B} \mathbb{1}(w_{bi} = 0) \mathbb{1}(\gamma_{bl} = 1) T(y_{i}, \hat{f}_{b}(x_{i}, S_{l}))}{\sum_{b=1}^{L} \sum_{b=1}^{B} \mathbb{1}(w_{bi} = 0) \mathbb{1}(\gamma_{bl} = 1) \mathbb{1}(j \in S_{l})} \\ &= \sum_{l=1}^{L} \alpha_{i,j,l} \phi_{i}(S_{l}), \end{split}$$

where  $\alpha_{i,j,l} \propto \mathbb{1}(j \in S_l) \sum_{b=1}^B \mathbb{1}(w_{bi} = 0)\mathbb{1}(\gamma_{bl} = 1), \forall i \in [n], j \in [d], l \in [L] \text{ and } \sum_{l=1}^L \alpha_{i,j,l} = 1$ . Define  $P_i(S_l|j \in S_l, \{w_{bi}\}_{b=1}^B) = \alpha_{i,j,l}$ , which specifies an empirical distribution of the feature subset S, conditioned on  $j \in S$ , in relation to the bootstrap sampling process. Here,  $\mathbb{1}(j \in S_l)$  implies the distribution is conditioned on the presence of the j-th feature within the feature subset  $S_l$ .  $w_{bi}$  indicates whether the i-th sample is out-of-bag in the b-th bootstrap, and  $\gamma_{bl}$  indicates whether the l-th feature subset is selected in the b-th weak learner. Thus, the point mass is determined by the sampling process.

Data valuation experiment

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In this section, we show that 2D-00B-data, the marginalization of 2D-00B, offers an effective approach to data valuation. This serves as the basis of our enhanced performance in joint valuation.

Marginalization 2D-00B aims to attribute data contribution through cells. Consequently, by summing up 2D-00B over all columns, we can derive data contribution values. For  $i \in [n]$ , we define the 2D-00B-data  $\psi_i^{data}$  as follows.

$$\psi_i^{data} := \frac{1}{d} \sum_{j=1}^d \psi_{ij}^{\text{2D-OOB}},\tag{5}$$

530 *Proof.* Based on definition of 2D-00B-Data, for  $i \in [n]$ ,

$$\psi_{i}^{data} := \frac{1}{d} \sum_{j=1}^{d} \psi_{ij}^{\text{2D-OOB}} = \frac{1}{d} \sum_{j=1}^{d} \sum_{l=1}^{L} \alpha_{i,j,l} \phi_{i}^{\text{OOB}}(S_{l})$$
$$= \sum_{l=1}^{L} (\frac{1}{d} \sum_{j=1}^{d} \alpha_{i,j,l}) \phi_{i}^{\text{OOB}}(S_{l}),$$

where  $\alpha_{i,j,l}$  is defined in Appendix C. We have  $\sum_{l=1}^{L} (\frac{1}{d} \sum_{j=1}^{d} \alpha_{i,j,l}) = \frac{1}{d} \sum_{j=1}^{d} \sum_{l=1}^{L} \alpha_{i,j,l} = 1$ .

Denote  $P_i(S_l | \{w_{bi}\}_{b=1}^B) = \frac{1}{d} \sum_{j=1}^{d} \alpha_{i,j,l}$ , which induces the empirical expectation of Data-OOB with respect to  $S_l$ .

Based on discussions in Section 3.2, the marginalizations also connect with Data-OOB:

**Proposition D.1.** For all  $i \in [n]$ , the marginalizations  $\psi_i^{data}$  can be expressed as follows.

$$\psi_i^{data} = \mathbb{E}_{\hat{F}_{\sigma}}[\phi_i^{OOB}(S)],$$

where the notations follow the same definitions as Proposition 3.1.

- Proposition D.1 indicates 2D-00B-data  $\psi_i^{data}$  can be expressed as the average Data-00B value for the *i*-th data point. As a result, 2D-00B-data is expected to inherit the advanced ability of Data-00B in terms of data valuation, as will be empirically examined in the Appendix D.
- Experimental setting Following the standard protocol in Kwon and Zou [22, 23] and Jiang et al. [16], we randomly select 10% of the data points and change its label to the other class. For joint valuation methods, we calculate the valuation of each cell and perform the marginalization over features to obtain the data valuation scores. For the baseline methods, we further incorporate several state-of-the-art data valuation methods including DataShapley [12], KNNShapley [15], DataBanzhaf [46], LAVA [18], and Data-00B [23]. Implementation details are listed below. To guarantee a fair comparison, we also employ the decision tree as the base model in DataShapley and DataBanzhaf. Mislabeled data detection and data removal experiment are examined based on this setting. We adopt the same 12 datasets as outlined in Section 4.1.
- Data-00B Data-00B involves fitting a random forest model without feature subset sampling, consisting of 1000 decision trees.
- DataShapley We use a Monte Carlo-based algorithm. The Gelman-Rubin statistics is computed to determine the termination criteria of the algorithm. Following Jiang et al. [16], We adopt the threshold to be 1.05. To ensure a fair comparison with the proposed method, we employ the decision tree model for the utility evaluation.
- KNNShapley We set the number of nearest neighbors to be 10% of the sample size following Jia et al. [15].
- LAVA We calculate the class-wise Wasserstein distance following Just et al. [18]. The "OTDD" framework is adopted to complete the optimal transport calculation.
- DataBanzhaf We adopt the implementation from Jiang et al. [16]. We employ the decision tree model and set "the number of models to train" to 1000.

#### 561 D.1 Mislabeled data detection

- We calculate the precision-recall curve by comparing the actual annotations, which denote whether data points are mislabeled, against the data valuation scores computed by different methods. Mislabeled data typically have a detrimental impact on model performance. Therefore, data points that receive a lower valuation score are regarded as having a higher chance of being mislabeled. We then determine AUCPR (the AUC of the precision-recall curve) as a quantitative metric to assess the detection efficacy.
- As shown in Table 9, 2D-00B-data consistently outperforms 2D-KNN-data across all datasets, suggesting its superior ability to detect mislabeled data points. It is worth noting that 2D-00B-data's results are on par with Data-00B, while significantly exceeding the performance of other data valuation methods. These results are in line with our theoretical analysis regarding the resemblance between Data-00B and 2D-00B-data. However, it is important to highlight that applying Data-00B to the joint tasks is not feasible as mentioned earlier, underscoring the necessity for the development of 2D-00B.

#### D.2 Point removal experiment

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Removing low-quality data points has the potential to enhance model performance. Based on this idea, 576 we employ the point removal experiment, a widely used benchmark in data valuation [23, 12, 22]. 577 According to the calculated data valuation scores, we progressively remove data points from the 578 dataset in ascending order. Specifically, we begin by removing the data points with the lowest data 579 valuations. Each time we remove a datum, we fit a logistic model and use the held-out test set 580 consisting of 3000 instances to evaluate the model performance. The expected behavior is that the 581 model performance will improve initially as the detrimental data points are gradually eliminated from 582 the training process. Removing an excessive number of data points may result in a drastically altered 583 dataset. Consequently, we opt to remove the bottom 20% data points.

Table 9: **Point-level mislabeled data detection results.** AUCPR of different data valuation and (marginalized) joint valuation methods. The average and standard error of the AUCPR based on 30 independent experiments are denoted by "average  $\pm$  standard error". Bold numbers denote the best method, for data valuation and joint valuation respectively. The AUCPR value for the Random method consistently remains at 0.5 across all datasets. 2D-00B-data exhibits performance comparable to Data-00B, while significantly surpassing 2D-KNN-data (the marginalization of 2D-KNN) and all other data valuation methods.

Dataset			Data Valuation	1		Joint Valuat	ion (Marginalized)
Dataset	KNNShapley	LAVA	DataBanzhaf	DataShapley	Data-00B	2D-KNN-data	2D-00B-data (ours)
lawschool	$0.66 \pm 0.013$	$0.13 \pm 0.003$	$0.46 \pm 0.008$	$0.88 \pm 0.007$	$\textbf{1.00} \pm \textbf{0.000}$	$0.46 \pm 0.011$	$0.99 \pm 0.002$
electricity	$0.22 \pm 0.008$	$0.11 \pm 0.002$	$0.18 \pm 0.005$	$0.26 \pm 0.007$	$\textbf{0.44} \pm \textbf{0.007}$	$0.20 \pm 0.006$	$0.39 \pm 0.007$
fried	$0.40 \pm 0.014$	$0.11 \pm 0.002$	$0.22 \pm 0.007$	$0.35 \pm 0.009$	$\textbf{0.76} \pm \textbf{0.007}$	$0.34 \pm 0.010$	$0.73 \pm 0.008$
2dplanes	$0.46 \pm 0.016$	$0.12 \pm 0.002$	$0.32 \pm 0.007$	$0.54 \pm 0.009$	$\textbf{0.78} \pm \textbf{0.008}$	$0.44 \pm 0.011$	$\textbf{0.68} \pm \textbf{0.010}$
creditcard	$0.37 \pm 0.007$	$0.11 \pm 0.003$	$0.16 \pm 0.004$	$0.28 \pm 0.006$	$\textbf{0.40} \pm \textbf{0.007}$	$0.20 \pm 0.005$	$0.40 \pm 0.007$
pol	$0.19 \pm 0.017$	$0.11 \pm 0.002$	$0.37 \pm 0.010$	$0.58 \pm 0.012$	$\textbf{0.93} \pm \textbf{0.004}$	$0.29 \pm 0.018$	$\textbf{0.87} \pm \textbf{0.005}$
MiniBooNE	$0.41 \pm 0.013$	$0.13 \pm 0.006$	$0.23 \pm 0.007$	$0.41 \pm 0.010$	$\textbf{0.78} \pm \textbf{0.007}$	$0.36 \pm 0.008$	$\textbf{0.78} \pm \textbf{0.007}$
jannis	$0.20 \pm 0.007$	$0.11 \pm 0.002$	$0.14 \pm 0.003$	$0.17 \pm 0.005$	$\textbf{0.38} \pm \textbf{0.010}$	$0.19 \pm 0.006$	$\textbf{0.37} \pm \textbf{0.010}$
nomao	$0.61 \pm 0.012$	$0.14 \pm 0.003$	$0.33 \pm 0.010$	$0.58 \pm 0.009$	$\textbf{0.87} \pm \textbf{0.006}$	$0.33 \pm 0.011$	$\textbf{0.88} \pm \textbf{0.005}$
vehicle_sensIT	$0.22 \pm 0.009$	$0.11 \pm 0.002$	$0.21 \pm 0.007$	$0.33 \pm 0.011$	$\textbf{0.56} \pm \textbf{0.010}$	$0.14 \pm 0.005$	$\textbf{0.56} \pm \textbf{0.010}$
gas_drift	$0.87 \pm 0.013$	$0.16 \pm 0.006$	$0.42 \pm 0.009$	$0.75 \pm 0.008$	$\textbf{0.98} \pm \textbf{0.002}$	$0.88 \pm 0.006$	$\textbf{0.98} \pm \textbf{0.002}$
musk	$0.33 \pm 0.010$	$0.11\pm0.003$	$0.31\pm0.007$	$0.47\pm0.012$	$\textbf{0.85} \pm \textbf{0.005}$	$0.21 \pm 0.008$	$\textbf{0.85} \pm \textbf{0.005}$
Average	0.41	0.12	0.28	0.47	0.73	0.34	0.71

Test accuracy curves throughout the data removal process are shown for 12 datasets (Figure 9). A higher curve signifies better performance in terms of data valuation. Overall, 2D-00B-data demonstrates similar performance to Data-00B, while significantly outperforming all other data valuation methods and the random baseline. When a few data points with poor quality are removed, the test performance of 2D-00B-data exhibits an evident increase. However, such a positive trend does not apply to other popular data valuation methods including DataShapley and LAVA. These findings highlight the potential of 2D-00B-data in selecting a subset of critical data points that can maintain model performance when the dataset is pruned.

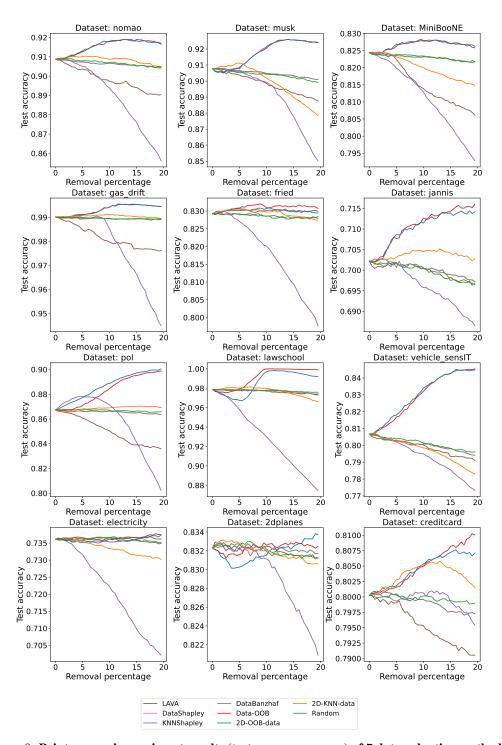


Figure 9: Point removal experiment results (test accuracy curves) of 7 data valuation methods – 2D-00B-data, 2D-KNN-data, Data-00B, LAVA, DataBanzhaf, DataShapley, KNNShapley and a random baseline. We remove data points from the lowest valuation to the highest valuation. The results from 6 binary classification datasets are displayed. For each dataset, we conduct 30 independent trials and report the average results. A higher curve indicates better performance. 2D-00B-data demonstrates superior ability in finding a set of helpful data points.

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Question: Does the paper provide open access to the data and code, with sufficient instructions to faithfully reproduce the main experimental results, as described in supplemental material?

#### 699 Answer: [Yes]

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Justification: The paper uses open-source datasets, detailed in Appendix A.1, and the code repository is included in the supplementary materials.

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Answer: [Yes]

Justification: Experiment settings have been clearly stated in section 4 and Appendix A.

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Answer: [Yes]

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Justification: The paper provides information on computer resources in section 4.

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# 13. New Assets

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