# RoLoRA: Fine-tuning Rotated Outlier-free LLMs for Effective Weight-Activation Quantization

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#### Abstract

 Low-Rank Adaptation (LoRA), as a represen- tative Parameter-Efficient Fine-Tuning (PEFT) method, significantly enhances the training effi- ciency by updating only a small portion of the weights in Large Language Models (LLMs). Recently, *weight-only* quantization techniques have also been applied to LoRA methods to re- duce the memory footprint of fine-tuning. How- ever, applying *weight-activation* quantization to the LoRA pipeline is under-explored, and we observe substantial performance degrada- tion primarily due to the presence of activation outliers. In this work, we propose RoLoRA, the first LoRA-based scheme for effective *weight-activation* quantization. RoLoRA uti- lizes rotation for outlier elimination and pro- poses rotation-aware fine-tuning to preserve 018 the outlier-free characteristics in rotated LLMs. Experimental results show RoLoRA consis- tently improves low-bit LoRA convergence and post-training quantization robustness in *weight- activation* settings. We evaluate RoLoRA across LLaMA2-7B/13B, LLaMA3-8B models, achieving up to 29.5% absolute accuracy gain of 4-bit *weight-activation* quantized LLaMA2- 13B on commonsense reasoning tasks com- pared to LoRA baseline. We further demon- strate its effectiveness on Large Multimodal **Models (LLaVA-1.5-7B)** and prove the compat-ibility with advanced LoRA variants.

#### **031** 1 Introduction

 While we have witnessed the success of Large Lan- [g](#page-8-0)uage Models (LLMs) such as GPT-4 [\(Achiam](#page-8-0) [et al.,](#page-8-0) [2023\)](#page-8-0) and LLaMA [\(Touvron et al.,](#page-9-0) [2023\)](#page-9-0) across various tasks in recent years, the massive model size and expanding training cost for LLMs have necessitated the design of model compression and Parameter-Efficient Fine-Tuning (PEFT) meth- ods. Low-rank Adaption (LoRA) [\(Hu et al.,](#page-8-1) [2021\)](#page-8-1), as the most favored PEFT method, significantly enhances the fine-tuning efficiency of LLMs.

Recently, quantization techniques, which con- **042** vert high-precision parameters into lower-bit for- **043** mats such as INT4, have been integrated with **044** LoRA methods [\(Dettmers et al.,](#page-8-2) [2024;](#page-8-2) [Li et al.,](#page-9-1) **045** [2024;](#page-9-1) [Xu et al.,](#page-10-0) [2024;](#page-10-0) [Qin et al.,](#page-9-2) [2024\)](#page-9-2). Exist- **046** ing quantization-LoRA schemes can save memory **047** [c](#page-9-1)osts during fine-tuning, and some schemes [\(Li](#page-9-1) **048** [et al.,](#page-9-1) [2024;](#page-9-1) [Xu et al.,](#page-10-0) [2024\)](#page-10-0) can also reduce infer- **049** ence costs by producing quantized LLMs directly. **050** However, these methods only perform *weight-only* **051** quantization, while LoRA *weight-activation* quanti- **052** zation is under-explored. Quantizing both weights **053** and activations in low-bit further saves run-time **054** GPU memory and accelerates compute-intensive **055** matrix-multiplication operations. We observe that **056** 4-bit or 6-bit weight-activation quantization with **057** LoRA finetuning still incurs a high accuracy degra- **058** dation in LLMs, attributing to the outliers in weight **059** and activation distribution, which stretch the quan- **060** tization range and increase the quantization error. **061**

Existing methods in the post-training quantiza- **062** tion research community have endeavored to tackle **063** the outlier challenge by mixed-precision subgroup- **064** ing [\(Zhao et al.,](#page-10-1) [2024;](#page-10-1) [Chee et al.,](#page-8-3) [2024\)](#page-8-3) or shifting **065** outliers from activation to weight [\(Xiao et al.,](#page-10-2) [2023;](#page-10-2) **066** [Shao et al.,](#page-9-3) [2024\)](#page-9-3). More recently, applying rota- **067** tion [\(Ashkboos et al.,](#page-8-4) [2024;](#page-8-4) [Liu et al.,](#page-9-4) [2024c\)](#page-9-4) to **068** the weight matrices of LLMs has demonstrated ef- **069** fectiveness in eliminating activation outliers and **070** keeping computational invariance [\(Ashkboos et al.,](#page-8-5) **071** [2023a\)](#page-8-5). However, all these methods solve the prob- **072** lems from a post-training perspective, ignoring that **073** outliers will emerge and change distribution dur- **074** ing pre-training and fine-tuning [\(Bondarenko et al.,](#page-8-6) **075** [2021\)](#page-8-6). In this work, we take a step further to uti- **076** lize the rotation for outliers-removal in LoRA fine- **077** tuning setting and investigate the optimal solution **078** for dynamically integrating rotation with LoRA **079** to preserve the outlier-free characteristics and im- **080** prove weight-activation quantization. Motivated **081** by this target, we propose Rotated outlier-free Low- **082**

**Rank Adaptation (RoLoRA), which initially ap-** ply in-block and between-block rotation to the pre- trained LLMs, and then utilize rotation-aware fine- tuning to produce outlier-free fine-tuned LLMs as shown in Figure [1.](#page-2-0) We explore the optimal rotation- aware fine-tuning scheme based on approximation error analysis.

 Extensive experimental results prove the effec- tiveness of RoLoRA across diverse LLMs, tasks, quantization settings, and LoRA variants. RoLoRA improves the 4-bit quantization for weights and ac- tivations (W4A4) performance up to 14.6 points on the MMLU benchmark compared to LoRA. Compared with existing low-bit LoRA meth- ods, RoLoRA outperforms previous SOTA IR- QLoRA [\(Qin et al.,](#page-9-2) [2024\)](#page-9-2) with up to 6.0 points on the MMLU benchmark. The proposed RoLoRA is highly efficient with negligible fine-tuning over- head compared to LoRA in the same setting. RoLoRA can also improve the quantization robust- ness of Large Multimodal Models (LMMs) such as LLaVA [\(Liu et al.,](#page-9-5) [2024a\)](#page-9-5), and we observe the multimodal understanding is largely retained even after W4A4 quantization as shown in Table [1.](#page-1-0)

107 In summary, our work contributes as follows:

- **108** We propose RoLoRA, the first method that **109** explores the feasibility of integrating rotation **110** in LoRA with quantization settings.
- **111** RoLoRA enables robust *weight-activation* **112** quantization of fine-tuned LLMs, especially **113** in low-bit settings such as W4A4 and W6A6.
- **114** We verify the effectiveness of RoLoRA **115** on the LLaMA series (2-7B, 2-13B, 3- **116** 8B) across quantizers (RTN/GPTQ), bitwidth **117** (W4A4/W6A6), and benchmarks (Zero-shot **118** commonsense, MMLU). We also demonstrate **119** that RoLoRA can be applied to LMMs and is **120** compatible with other LoRA variants.

## **<sup>121</sup>** 2 Related Work

 Quantization Quantization methods are power- ful tools for improving training and inference effi- ciency. The core insight is replacing full-precision weights and activations with lower-precision rep- resentation. Most existing LLM quantization tech- niques fall in the category of post-training quan- tization (PTQ) [\(Liu et al.,](#page-9-6) [2023b;](#page-9-6) [Frantar et al.,](#page-8-7) [2023;](#page-8-7) [Lin et al.,](#page-9-7) [2024;](#page-9-7) [Shang et al.,](#page-9-8) [2024;](#page-9-8) [Chee](#page-8-3) [et al.,](#page-8-3) [2024\)](#page-8-3) that directly quantize the model with-out extensive training. Among these LLM PTQ

<span id="page-1-0"></span>

Question: User: Explain the visual content of the image in great detail. (category: "detail")

GPT-4 Response: The image displays three open pizza boxes with pizzas inside. The first pizza box, situated to the left, contains a smaller pizza. The second pizza box, positioned in the middle, features a larger pizza topped with tortilla chips. The third pizza box, located to the right, contains another smaller pizza. Beside the large pizza, there are two side orders of sauce in bowls, accompanying the delicious meal. The arrangement showcases a delicious spread of pizzas, inviting everyone to enjoy their different flavors and sizes.

 $LoRA \xrightarrow{GPTQ} W4A4$ : The image shows a pizza.

 $RoLoRA \xrightarrow{GPTQ} W4A4$ : The image features a pizza with a variety of toppings, including cheese, pepperonies, and chicken. There are three pizzas in total, with one of them being a pizza with chicken. The pizzas are placed in a cardboard box, which is open and ready for the pizzas. The pizzas are served in a box, making it a convenient and portable meal option.

Table 1: LLaVA-1.5-7B W4A4 quantization evaluation on the example from LLaVA-Bench.

methods, most of them apply *weight-only* quantiza- **132** tion while few methods explore *weight-activation* **133** quantization [\(Xiao et al.,](#page-10-2) [2023;](#page-10-2) [Shao et al.,](#page-9-3) [2024;](#page-9-3) **134** [Zhao et al.,](#page-10-1) [2024;](#page-10-1) [Ashkboos et al.,](#page-8-4) [2024\)](#page-8-4). Com- **135** pared to the *weight-only* quantization, quantizing **136** both weights and activations enables low-precision **137** multiply-accumulation (MAC) units. The core chal- **138** lenge is that outliers in activations cause high quan- **139** tization errors. This work focuses on the *weight-* **140** *activation* quantization in the LoRA pipeline. **141**

LoRA Considering that full parameter fine-tuning **142** becomes computationally impractical as the scale **143** of LLM continues to grow, Parameter-Efficient **144** Fine-Tuning (PEFT) methods [\(Li and Liang,](#page-9-9) [2021;](#page-9-9) 145 [Hu et al.,](#page-9-10) [2023;](#page-9-10) [Zhang et al.,](#page-10-3) [2023\)](#page-10-3) are designed to **146** reduce the cost by training a relatively small subset **147** [o](#page-8-1)f parameters. Low-Rank Adaptation (LoRA) [\(Hu](#page-8-1) **148** [et al.,](#page-8-1) [2021\)](#page-8-1) is the most adopted PEFT method, con- **149** sidering its flexibility and efficiency. More recently, **150** LoRA variants [\(Kopiczko et al.,](#page-9-11) [2024;](#page-9-11) [Liu et al.,](#page-9-12) **151**

(2) **232**

<span id="page-2-0"></span>

Figure 1: Activation distribution before and after rotation. The visualized input activations are selected from *layers.1.self\_attn.q\_proj* in LLaMA2-7B.

 [2024b;](#page-9-12) [Hayou et al.,](#page-8-8) [2024\)](#page-8-8) emerged to improve the effectiveness and efficiency of LoRA. Combining LoRA and quantization [\(Dettmers et al.,](#page-8-2) [2024\)](#page-8-2) has also been a promising direction as quantization can further save the GPU memory in LoRA finetuning. To further reduce the information distortion of low- bit finetuning, various improvements of QLoRA have been proposed [\(Xu et al.,](#page-10-0) [2024;](#page-10-0) [Li et al.,](#page-9-1) [2024;](#page-9-1) **[Qin et al.,](#page-9-2) [2024\)](#page-9-2). However, these methods only ap-** ply quantization to the weight during fine-tuning to reduce memory consumption. This work is the first quantized LoRA scheme that considers the robustness to *weight-activation* quantization.

#### **<sup>165</sup>** 3 Preliminary and Motivation

#### **166** 3.1 Low-Rank Adaptation (LoRA)

**For a pre-trained weight matrix**  $W_0 \in R^{d \times k}$ , LoRA 168 models the weight update  $\Delta W \in R^{d \times k}$  utilizing a low-rank decomposition, expressed as AB, where  $A \in R^{d \times r}$  and  $B \in R^{r \times k}$  represent two low-rank matrices, with  $r \ll min(d, k)$ . Consequently, the fine-tuned weight  $W'$  can be represented as:

<span id="page-2-1"></span>
$$
W' = W_0 + \Delta W = W_0 + AB,\tag{1}
$$

174 where  $W_0$  remains static during the fine-tuning process, and the underlined parameters are being trained. Additionally, based on Eq. [\(1\)](#page-2-1), we can merge the learned ∆W with the pre-trained weight  $W_0$  and obtain  $W'$  in advance of deployment, and **179 179** and W<sup>'</sup> and W<sub>0</sub> both fall within the 180 dimensionality of  $R^{d \times k}$ , LoRA and its related vari- ants do not introduce any extra latency during the inference compared to the original model.

### **183** 3.2 Outlier in Transformer

 Starting from small-scale transformer models such as BERT and ViT, researchers have revealed that outliers exist within the weight and activation distri-bution [\(Huang et al.,](#page-9-13) [2023;](#page-9-13) [Wei et al.,](#page-10-4) [2022\)](#page-10-4). Their

existence in LLMs is also observed in various stud- **188** ies. As shown in the left side of Figure. [1,](#page-2-0) acti- **189** vation outliers are distributed per channel. While **190** these outliers improve the representative capacity **191** of the transformers [\(Sun et al.,](#page-9-14) [2024\)](#page-9-14), they bring **192** non-trivial challenges for quantization [\(Xiao et al.,](#page-10-2) **193** [2023;](#page-10-2) [Liu et al.,](#page-9-6) [2023b\)](#page-9-6). **194**

Most previous solutions to this outlier problem **195** in quantization can be categorized into three types: **196** (1) isolating these outlier values in a sub-group with **197** higher precision, such as LLM.int8 [\(Dettmers et al.,](#page-8-9) **198** [2022\)](#page-8-9), Atom [\(Zhao et al.,](#page-10-1) [2024\)](#page-10-1), QuiK [\(Ashkboos](#page-8-10) **199** [et al.,](#page-8-10) [2023b\)](#page-8-10), and AdaDim [\(Heo et al.,](#page-8-11) [2024\)](#page-8-11). How- **200** ever, there is non-trivial overhead for the grouping **201** and mixed-precision. (2) shifting the challenge **202** of quantization from activations to weights, such **203** as SmoothQuant [\(Xiao et al.,](#page-10-2) [2023\)](#page-10-2) and Omni- **204** Quant [\(Shao et al.,](#page-9-3) [2024\)](#page-9-3). However, these meth- **205** ods negatively influence the weight quantization **206** robustness and fail at W4A4 scenarios. (3) rotat- **207** ing activation or weight matrices to remove out- **208** liers, such as QuaRot [\(Ashkboos et al.,](#page-8-4) [2024\)](#page-8-4) and **209** SpinQuant [\(Liu et al.,](#page-9-4) [2024c\)](#page-9-4). Among these meth- **210** ods, recent rotation-based solutions demonstrate **211** superior effectiveness. However, previous rotation- **212** based methods tackle the outlier challenge from **213** a post-training perspective and have not been ex- **214** plored under PEFT settings. **215**

Thus, it leads to a question: *Can we preserve* **216** *the outlier-free characteristics of rotated LLMs and* **217** *benefit from them during PEFT?* We show in this **218** work that we can achieve such a target and step 219 further to investigate the most promising rotation- **220** based fine-tuning solutions in this work. **221**

#### 3.3 Eliminating Outlier with Rotation **222**

A rotation matrix R is defined as an orthogonal ma- **223** trix with  $|R| = 1$ , where R also follows the char- 224 acteristics of the orthogonal matrix that  $RR^\top = I$ . 225 If the entries of  $R$  are either  $+1$  or  $1$ , it becomes a 226 Hadamard matrix H. Based on the definition, we **227** can efficiently generate  $H$  with  $2^k$  entries<sup>[1](#page-2-2)</sup> based 228 on the Hadamard transform (also known as the **229** Walsh–Hadamard transform [\(Ritter,](#page-9-15) [1996\)](#page-9-15) as an ex- **230** ample of a generalized class of Fourier transforms): **231**

$$
H_{2^{k}} = \begin{bmatrix} H_{2^{k-1}} & H_{2^{k-1}} \\ H_{2^{k-1}} & -H_{2^{k-1}} \end{bmatrix} = H_2 \otimes H_{2^{k-1}},
$$
\n(2)

<span id="page-2-2"></span><sup>&</sup>lt;sup>1</sup>For the  $n \neq 2^k$  entries, we can also decompose it into  $n = 2<sup>k</sup>m$  and construct  $H_n = H_m \otimes H_{2<sup>k</sup>}$  efficiently.

<span id="page-3-0"></span>

Figure 2: Overview of the proposed Rotated outlier-free LoRA (RoLoRA)

 where ⊗ denotes the Kronecker product. The ro- tation is highly efficient as the matrix-vector prod-235 uct with a  $d \times d$  Hadamard matrix  $H_dX$  requires  $O(d \log_2(d))$  $O(d \log_2(d))$  operations. Previous research [\(Ashk-](#page-8-5) [boos et al.,](#page-8-5) [2023a\)](#page-8-5) has revealed that applying rota- tion on the weights of *pre-norm* transformers can re- tain its computational consistency and further lead to fewer outliers in the weight and activation dis- tribution [\(Ashkboos et al.,](#page-8-4) [2024;](#page-8-4) [Liu et al.,](#page-9-4) [2024c\)](#page-9-4). Concretely, the multiplication of weight matrices with a rotation matrix statistically blends weights with large and small magnitudes together into a more Gaussian-like distribution, thus producing ac- tivations with fewer outliers and easier to quantize. The outlier elimination effect of rotation is also theoretically proved in [Chee et al.](#page-8-3) [\(2024\)](#page-8-3).

#### **<sup>249</sup>** 4 Method

 Motivated by existing challenges of activation outliers and the success of rotation-based solu- tions [\(Ashkboos et al.,](#page-8-4) [2024;](#page-8-4) [Liu et al.,](#page-9-4) [2024c\)](#page-9-4), we introduce Rotated outlier-free Low-Rank Adaptation (RoLoRA). RoLoRA initially apply in- block and between-block rotation to the pre-trained LLMs, and rotation-aware fine-tuning on the ro- tated LLMs will retain the optimal outlier-free char- acteristic, producing fine-tuned LLMs highly ro-bust to weight-activation quantization.

#### <span id="page-3-1"></span>**260** 4.1 Applying Rotation

 Before starting fine-tuning with rotation, we first modify the model to keep computational invariance before and after rotation. First, we need to ensure no scaling operation in the normalization module. For the LLaMA series, this can be implemented 266 by absorbing the RMSNorm scale parameters  $\alpha$  into the weight matrix right after the RMSNorm layer [\(Elhage et al.,](#page-8-12) [2023\)](#page-8-12).

**269** Then, we perform between-block rotation to **270** make sure that the outliers in between-block ac-**271** tivation are eliminated. As shown in Figure [2,](#page-3-0)

we classify the weight matrices in LLMs into two **272** groups: *left-side* weights, including  $W_a$ ,  $W_k$ ,  $W_v$  273 in self-attention modules, and  $W_{up}$ ,  $W_{gate}$  in feed-  $274$ forward network modules (which corresponds to **275** the  $W_u$ ,  $W_g$  in Figure [2\)](#page-3-0). *right-side* weights, including  $W_o$  in self-attention modules and  $W_{down}$  277 in feed-forward network modules. For the weights **278** of these two groups, we adopt different rotation **279** strategies with 280

$$
W_{\text{left}}^R \leftarrow RW_{\text{left}}, W_{\text{right}}^R \leftarrow W_{\text{right}} R^{-1}, \quad (3)
$$

, (3) **281**

where the rotation R is randomly generated 282 Hadamard matrix. As we also rotated the input **283** X before embedding layer with  $X \leftarrow XR^{-1}$  and 284 output Y after  $lm\_head$  with  $Y \leftarrow RY$ , the final 285 output of the model will be identical to the original **286** model. To avoid overflow issues in the rotation **287** process, we converted the FP16 weights to FP64 **288** and converted them back after the multiplication. **289** These rotations are applied before any training and **290** inference, which indicates that there will be no **291** overhead after the merging to original weights. **292**

The rotation that directly applies to weights ef- **293** fectively reduces the outlier in between-block ac- **294** tivation, and we refer to the operation as Between **295** Block Rotation (BBR). Figure. [1](#page-2-0) demonstrates the **296** effect of applying BBR as the activation distribu- **297** tion is smoother and de-centralized. However, an- **298** other challenge remains that the activation in these **299** modules still suffers from outliers, especially preva- **300** [l](#page-8-13)ent in FFN as discussed in previous research [\(Bon-](#page-8-13) **301** [darenko et al.,](#page-8-13) [2024\)](#page-8-13). We cannot directly apply **302** rotation similar to BBR because of the non-linear **303** operations such as SwiGLU [\(Shazeer,](#page-9-16) [2020\)](#page-9-16) in **304** FFN. To solve this, we adopt the online rotation **305** node before inputting the activation input to  $W_{down}$ .  $306$ This online rotation is implemented following the **307** [f](#page-8-4)ast Hadamard kernel [\(Chee et al.,](#page-8-3) [2024;](#page-8-3) [Ashkboos](#page-8-4) **308** [et al.,](#page-8-4) [2024\)](#page-8-4), which can be seen as a layer dynam- **309** ically rotating the activation. This online rotation **310** operation is highly efficient, and the overhead is **311**

<span id="page-4-0"></span>

(a) LoRA After Roatation (b) LoRA Before Roatation

Figure 3: Two schemes for performing rotation-aware fine-tuning: (a) LAR and (b) LBR.

 negligible during training and inference. It is re- ferred to as in-block rotation (IBR). Note that IBR can also be applied to the self-attention module, but we observe in the experiments of Table [7](#page-6-0) that there is no performance improvement with this rotation.

#### <span id="page-4-2"></span>**317** 4.2 Rotation-aware Fine-tuning

 After performing both BBR and IBR, the between- block and in-block activation outliers are elimi- nated. This characteristic can lower the quanti- zation error during QLoRA training, enabling a more accurate gradient estimation and smoother optimization for fine-tuning. However, existing re- search [\(Bondarenko et al.,](#page-8-6) [2021;](#page-8-6) [Kovaleva et al.,](#page-9-17) [2021\)](#page-9-17) revealed that outliers will change distribu- tion or emerge during fine-tuning and pre-training. This poses a new challenge of dynamically inte- grating rotation into LoRA to effectively maintain outlier-free characteristics. To design the optimal rotation-aware fine-tuning scheme, we first ana- lyze the approximation difficulty when rotation is applied. We assume that the optimal weight distri- bution for specific downstream tasks is  $W^*$ , and we approximate it with the LoRA weights AB merged 335 with pre-trained weights  $W_0$ . The optimization of LoRA fine-tuning could be indicated as

$$
\min_{A,B} \|W^* - (W_0 + AB)\|_F, \tag{4}
$$

338 where the  $\|\cdot\|_F$  denotes the Frobenious norm. To insert the LoRA module in the rotated models, we propose two rotation-aware fine-tuning schemes, namely LoRA After Rotation (LAR) and LoRA Before Rotation (LBR), as shown in Figure [3.](#page-4-0)

 In LAR, we first merge the rotation matrix with **pre-trained weights and then use**  $R_1W_0 + AB$  to **approximate W<sup>\*</sup>**. For LBR, we first merge the 346 LoRA weights and rotate them to be  $R_1(W_0+AB)$ . We assume the optimal weights to be the full-fine- tuning results  $W_{FT}$ , and the optimization for these two schemes becomes:

$$
\text{LAR: } \min_{A,B} \|AB - O_{\text{LAR}}\|_{F}, O_{\text{LAR}} = W_{FT} - R_1 W_0
$$
\n
$$
\text{LBR: } \min_{A,B} \|AB - O_{\text{LBR}}\|_{F}, O_{\text{LBR}} = R_1^{-1} W_{FT} - W_0 \tag{5}
$$

<span id="page-4-1"></span>

Figure 4: SVD approximation error of optimization targets with different LoRA-rotation integration schemes.

the final optimization is very different. We apply **351** SVD of the approximation target  $O_{\text{LAR}}$ ,  $O_{\text{LBR}} \in$  352  $R^{d \times k}$  by  $O = USV^T$ . The principal singular val-<br>353 ues and vectors in the first r dimensions are uti- $354$ lized to initialize the LoRA weights with rank r as **355**  $A \in R^{m \times r}$  and  $B \in R^{r \times n}$ : **356**

$$
A = U_{[:,:r]} S_{[:,r;r]}^{1/2} \in R^{d \times r}, B = S_{[:,r]}^{1/2} V_{[:,r]}^T \in R^{r \times k}.
$$
\n(6)

We verify the approximation error of different rank **358** choices r to simulate the LoRA on two rotation **359** schemes. We use a pre-trained LLaMA2-7B as  $360$  $W_0$  and a full-parameter fine-tuned model on the  $361$ Alpaca dataset [\(Taori et al.,](#page-9-18) [2023\)](#page-9-18) as  $W_{FT}$  for the  $362$ experiments. which is shown in Figure. [4.](#page-4-1) Based **363** on the results, LAR outperforms LBR in low-rank **364** settings with lower approximation error, suggesting **365** LAR is the better design for rotation-aware fine- **366** tuning. The better approximation indicates that **367** after the two-stage merging with rotation matrices **368** and LoRA weights, the final weights can still retain **369** the outlier-free property, which is further validated **370** by ablation experiments in Section [5.5.](#page-6-1) **371**

As a result of the optimal rotation-aware fine- **372** tuning scheme under the LAR setting, we can ef- **373** fectively retain the outlier-free characteristic during **374** LLM fine-tuning, as shown in Figure [5.](#page-7-0) **375**

#### 5 Experiments **<sup>376</sup>**

#### 5.1 Settings **377**

Model, LoRA, Quantizer The models for our **378** [e](#page-9-0)xperiments include LLaMA2-7B/13B [\(Touvron](#page-9-0) **379** [et al.,](#page-9-0) [2023\)](#page-9-0) and LLaMA3-8B [\(AI@Meta,](#page-8-14) [2024\)](#page-8-14). **380** [W](#page-10-5)e follow the settings in LLaMA-Factory [\(Zheng](#page-10-5) 381 [et al.,](#page-10-5) [2024\)](#page-10-5) to implement the training pipeline. The **382** dataset for fine-tuning is Alpaca [\(Taori et al.,](#page-9-18) [2023\)](#page-9-18) **383** with 52K samples. The weight PTQ methods are **384** the baseline Round-To-Nearest (RTN) and widely **385** used GPTQ [\(Frantar et al.,](#page-8-7) [2023\)](#page-8-7), and the activation **386** quantizer is RTN across all experiments. **387**

Tasks Our RoLoRA was verified on seven **388** zero-shot commonsense reasoning tasks using **389**

5

$# \text{Bits}$	<b>Ouantizer</b>	Method		$LLaMA-27B$		<b>LLaMA-2 13B</b>	LLaMA-38B		
			$ZCSR^7$ Avg.	$MMLU4$ Avg.		$ZCSR7$ Avg. MMLU <sup>4</sup> Avg.	$ZCSR^7$ Avg.	$MMLU4$ Avg.	
FP16	$\overline{\phantom{a}}$	LoRA	68.4	43.5	70.5	52.4	70.0	62.7	
W <sub>4</sub> A <sub>4</sub>	<b>RTN</b>	LoRA RoLoRA	35.8 54.1 $(†18.3)$	23.5 $25.8~(\Uparrow 2.3)$	34.4 58.7 $(†24.3)$	24.2 30.5 $(†6.3)$	36.7 50.0 $(13.3)$	23.3 32.1 $(†8.8)$	
	<b>GPTO</b>	LoRA RoLoRA	37.0 62.3 $(125.3)$	23.5 31.0 $(17.5)$	34.4 63.9 $(129.5)$	24.4 38.9 $(†14.5)$	36.6 56.6 $(120.0)$	23.9 38.5 $($ 14.6)	
<b>W6A6</b>	<b>RTN</b>	LoRA RoLoRA	65.3 66.8 $($ 1.5)	35.9 40.5 $(†4.6)$	67.3 68.4 $(†1.1)$	47.3 47.7 $(†0.4)$	67.7 67.8 $(†0.1)$	55.3 59.4 $($ <sup>4.1</sup> )	
	GPTQ	LoRA RoLoRA	65.5 67.1 $($ <sup>1</sup> .6)	35.7 40.8 $(†5.1)$	68.0 68.8 $(10.8)$	47.6 47.9 $(†0.3)$	67.8 68.1 $($ $\uparrow$ 0.3)	54.3 59.4 $(†5.1)$	

<span id="page-5-0"></span>Table 2: Comparison of the averaged accuracy on seven Zero-shot Common Sense Reasoning (ZCSR) tasks and MMLU benchmark across LLaMA series. The detailed accuracy for each tasks are listed in Table [10](#page-11-0) and Table [11.](#page-12-0)

 EleutherAI evaluation harness [\(Gao et al.,](#page-8-15) [2021\)](#page-8-15). These tasks include BoolQ [\(Clark et al.,](#page-8-16) [2019\)](#page-8-16), PIQA [\(Bisk et al.,](#page-8-17) [2020\)](#page-8-17), HellaSwag [\(Zellers et al.,](#page-10-6) [2019\)](#page-10-6), WinoGrande [\(Sakaguchi et al.,](#page-9-19) [2021\)](#page-9-19), ARC- easy and ARC-challenge [\(Clark et al.,](#page-8-18) [2018\)](#page-8-18), and OBQA [\(Mihaylov et al.,](#page-9-20) [2018\)](#page-9-20). Additionally, we also report the accuracy of Massively Mul- titask Language Understanding (MMLU) bench- mark [\(Hendrycks et al.,](#page-8-19) [2020\)](#page-8-19) for our evaluation. Baselines We consider two settings for experi- ments. The first is conducting FP16 fine-tuning with RoLoRA, where we compare the W4A4 and W6A6 quantization results with LoRA. The sec- ond is conducting RoLoRA fine-tuning with 4- bit weight quantization, which we refer to as QRoLoRA, and comparing the W4A4 perfor- mance with other low-bit LoRA methods including QLoRA [\(Dettmers et al.,](#page-8-2) [2024\)](#page-8-2), LoftQ [\(Li et al.,](#page-9-1) [2024\)](#page-9-1), and IR-LoRA [\(Qin et al.,](#page-9-2) [2024\)](#page-9-2).

### **409** 5.2 Main Results

 We first evaluate RoLoRA against LoRA in FP16 fine-tuning and then apply *weight-activation* PTQ to the fine-tuned LLMs. To ensure a fair com- parison, both RoLoRA and LoRA use the same settings (rank, epoch, learning rate, etc.). As listed in Table [2,](#page-5-0) RoLoRA enhances the quantization ro- bustness of the LLaMA series across various quan- tization settings on zero-shot commonsense rea- soning and MMLU benchmarks. Specifically for the W4A4 low-bit setting, RoLoRA outperforms LoRA with an absolute up to 29.5% and 14.6% on ZCSR and MMLU, respectively. Furthermore, RoLoRA makes it feasible for near-lossless W6A6 quantization of the LLaMa series.

**424** We further evaluate RoLoRA against **425** QLoRA [\(Dettmers et al.,](#page-8-2) [2024\)](#page-8-2) and serval **426** baseline methods, including LoftQ [\(Li et al.,](#page-9-1) [2024\)](#page-9-1), IR-QLoRA [\(Qin et al.,](#page-9-2) [2024\)](#page-9-2), on 4-bit **427** fine-tuning and then apply W4A4 PTQ to the **428** low-bit fine-tuned LLaMA2-7B. The performance **429** across seven commonsense reasoning tasks and **430** four MMLU subtasks is detailed in Table [3.](#page-6-2) We **431** can see that RoLoRA consistently improves the **432** performance of the quantized model using the **433** same quantizer. In particular, for W4A4 GPTQ, 434 RoLoRA exceeds QLoRA by 20.5% on the **435** average accuracy of commonsense reasoning **436** tasks. Across the experiments on both FP16 **437** and 4-bit fine-tuning, we observe that RoLoRA **438** achieves higher performance improvement on the **439** LLMs quantized by GPTQ [\(Frantar et al.,](#page-8-7) [2023\)](#page-8-7) **440** in general. This observation supports our claim **441** that RoLoRA retains the outlier-free activation **442** in fine-tuning as GPTQ only helps lower the **443** quantization error of weights but not for activation. **444**

## 5.3 Visual Instruction Tuning **445**

We further verify the effectiveness of RoLoRA on  $446$ visual instruction tuning tasks with LLaVA-1.5- **447** 7B [\(Liu et al.,](#page-9-21) [2023a\)](#page-9-21), which consists of a language **448** model, Vicuna-7B [\(Chiang et al.,](#page-8-20) [2023\)](#page-8-20), and a vi- **449** sion encoder CLIP ViT-L-336px [\(Radford et al.,](#page-9-22) **450** [2021\)](#page-9-22). We finetune the LLaVA-1.5-7B on LLaVA- **451** Instruct-150K<sup>[2](#page-5-1)</sup>. We only perform quantization on 452 the language model and evaluate the LLaVA with **453** quantized Vicuna and full-precision vision encoder **454** on LLaVA-bench (COCO) [\(Liu et al.,](#page-9-5) [2024a\)](#page-9-5) with **455** GPT-4 [\(Achiam et al.,](#page-8-0) [2023\)](#page-8-0). The relative score **456** across the conversation, detail description, and **457** complex reasoning are reported in Table. [4,](#page-6-3) where **458** we can observe from the results that RoLoRA help **459** improve the quantization robustness and keep the **460** multi-modal ability during PTQ to the better ex- **461**

<span id="page-5-1"></span><sup>2</sup> https://huggingface.co/datasets/liuhaotian/LLaVA-Instruct-150K

<span id="page-6-2"></span>Table 3: Comparison of the averaged accuracy of different Low-bit LoRA methods on Zero-shot Common Sense Reasoning tasks and MMLU benchmark on LLaMA2-7B.

#Bits	<b>Ouantizer</b>	Method				BoolO PIOA HellaS. WinoG. Arc-e Arc-c OBOA				Avg.		Hums. STEM Social Other			Avg.
		QLoRA (Dettmers et al., 2024)	47.1	51.5	27.5	49.1	28.4	24.6	25.4	36.2	24.1	24.7	22.9	21.8	23.5
	<b>RTN</b>	LoftO $(Li et al., 2024)$	51.5	50.8	26.6	50.4	27.5	26.0	25.0	36.8	23.9	24.0	22.2	າາ າ	23.2
W <sub>4</sub> A <sub>16</sub>		IR-OLoRA (Oin et al., 2024)	45.5	49.7	26.7	50.6	25.7	26.8	26.8	36.0	24.3	24.6	23.9	21.9	23.7
		RoLoRA	59.9	60.5	43.5	51.8	43.7	28.6	28.8	45.3 $(†8.5)$	24.7	25.3	23.6		$24.3 \pm 24.5$ ( $\uparrow$ 0.8)
÷ W <sub>4</sub> A <sub>4</sub>		QLoRA (Dettmers et al., 2024)	51.4	51.6	27.7	51.9	29.6	25.3	26.4	37.7	24.9	24.0	22.2	22.5	23.6
	<b>GPTO</b>	LoftQ (Li et al., 2024)	55.9	49.2	27.2	49.1	26.6	26.1	24	36.9	24.1	23.8	23.3	22.7	23.6
		IR-OLoRA (Oin et al., 2024)	51.1	49.8	27.6	49.3	27.6	24.6	27.4	36.8	24.6	24.8	22.9	22.7	23.9
		RoLoRA	68.7	73.1	66.8	61.3	61.2	37.8		38.2 58.2 $(120.5)$	28.3	32.7	32.3		$27.2$ : 29.9 ( $\uparrow$ 6.0)

 tent with an increase up to 18.9 overall scores. We also provide an example of the detail description task on a given image shown in Table. [1.](#page-1-0) While the W4A4 LoRA model only gives a rough superfi- cial description of the images, our W4A4 RoLoRA model fully elaborates the details, such as the top-pings and containers.

<span id="page-6-3"></span>Table 4: Comparison of the W4A4 quantization performance on LLaVA-Bench of LLaVA-1.5-7B.

#Bits	<b>Ouantizer</b>	Method Conv. Detail			Reas.	<b>Overall</b>
W <sub>4</sub> A <sub>4</sub>	<b>RTN</b>	LoRA	43.2	29.6	31.6	349
		RoLoRA	68.8	40.5 51.9		53.8 ( $\uparrow$ 18.9)
	<b>GPTO</b>	LoRA	70.6	41.8	47.9	53.5
		RoLoRA	67.5	48.3	66.2	60.8 $(†7.3)$

#### **469** 5.4 Compatibility with other LoRA variants

 We further verify our method on a representative LoRA variant, DoRA [\(Liu et al.,](#page-9-12) [2024b\)](#page-9-12). DoRA decomposes the pre-trained weight into magnitude and directional components and finetunes both. We also follow this scheme in our rotation-aware fine- tuning stage and refer to this scheme as RoDoRA. As shown in Table [5,](#page-6-4) RoDoRA achieves 7.8% and 20.6% higher accuracy on W4A4 LLaMA2-7B us-ing RTN and GPTQ as quantizers.

<span id="page-6-4"></span>Table 5: Compatibility of with DoRA on LLaMA2-7B.



#### <span id="page-6-1"></span>**479** 5.5 Ablation Study and Analysis

 When to Apply Rotation? Different from the Rotation-Aware Fine-tuning (RAF) scheme that rotates the LLMs before LoRA fine-tuning, we can also directly apply rotation on an already- finetuned LoRA model. This possible paradigm of LoRA→Rotate→PTQ is referred to as post- training rotation. We evaluate post-training rotation using the same training setting as RoLoRA across the LLaMA series. The W4A4 GPTQ performance **488** on seven zero-shot commonsense reasoning tasks **489** are listed in Table [6.](#page-6-5) The results indicate that apply- **490** ing rotation before LoRA can consistently enhance **491** the quantization robustness of the fine-tuned LLMs. **492**

Table 6: Ablation on **when** to apply rotation.

<span id="page-6-5"></span>

Method		LLaMA2-7B LLaMA2-13B LLaMA3-8B	
RoLoRA	62.3	63.9	56.6
Post-Training Rotation 58.7 $(\sqrt{3.6})$		61.3 $(\downarrow 2.6)$	55.2 $(1.4)$

Where to Apply Rotation? In Figure [2,](#page-3-0) we intro- **493** duce two types of rotation in our pipeline, namely **494** Between-Block Rotation applied on all weight ma- **495** trices and In-Block Rotation applied on *down\_proj* **496** in FFN. As discussed in Section [4.1,](#page-3-1) we can also **497** apply a similar head-wise IBR  $R_3$  for self-attention.  $498$ The  $R_3$  rotates the  $W_v$  and  $W_o$  in Figure [2](#page-3-0) by 499  $W_v^R \leftarrow W_v R_3, W_o^R \leftarrow R_3^{-1} W_o$ . These choices 500 for rotation targets are verified on LLaMA2-7B **501** W4A4 PTQ shown in Table [7.](#page-6-0) The results suggest 502 that applying and only applying both  $R_1$  and  $R_2$  is  $503$ the best option to eliminate outliers. **504**

<span id="page-6-0"></span>Table 7: Ablation on where to apply rotation.

Method	<b>Rotation</b>	$ZCSR7$ Avg.
RoLoRA	$R_1, R_2$	54.1
$(-)$ FFN In-Block Rotation	$R_1$	40.4 $(\downarrow$ 13.7)
$(-)$ Between-Block Rotation	$R_2$	49.7 $(14.4)$
$(+)$ Attention In-Block Rotation	$R_1, R_2, R_3$	53.8 $(10.3)$

How to Apply LoRA? In Section [4.2,](#page-4-2) we propose **505** two rotation-aware fine-tuning schemes LoRA Af- **506** ter Rotation (LAR) and LoRA Before Rotation **507** (LBR) shown in Figure [3.](#page-4-0) We prove that LAR is the **508** better paradigm based on the approximation error **509** analysis compared with full-finetuning. In Table [8,](#page-7-1) **510** we quantitatively compare the W4A4 quantization 511 performance of two schemes on the fine-tuning of **512** the LLaMA2-7B. The LAR scheme demonstrates **513** better effectiveness, which corresponds to the ap- **514** proximation analysis shown in Figure [4.](#page-4-1) **515**

Outliers Retaining the outlier-free characteristic **516** during LLM fine-tuning is the most important mo- **517**

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<span id="page-7-0"></span>

Figure 5: Left: The training dynamics of the average Kurtosis of activations, Middle: The distribution of Kurtosis of activations across all layers in the final model after fine-tuning with LoRA and RoLoRA, Right: The accumulative quantization error of W4A4 GPTQ across all layers in the final model after fine-tuning with LoRA and RoLoRA.

Table 8: Ablation on how to apply LoRA.

<span id="page-7-1"></span>

#Bits-Quantizer Method $ZCSR^7$ Avg. MMLU <sup>4</sup> Avg.			
W4A4-GPTO	LAR	62.3	31.0
	LBR.	61.1 $(\downarrow 1.2)$	30.4 $(10.6)$

 tivation for RoLoRA. To quantitatively validate the effect of outlier elimination, we use kurtosis  $\kappa = \frac{\sum_{i=1}^{k} (x_i - \mu)^4}{\sigma^4 + \epsilon}$  of the activation to measure the  $\sigma^4 + \epsilon$ **but outlier presence, where**  $\mu$  **and**  $\sigma$  **are respectively**  the empirical mean and standard deviation of ac- tivation distribution. Generally, a large kurtosis value indicates an activation distribution with heavy tails and a higher likelihood of outliers. We visu- alize the kurtosis dynamic during fine-tuning with LoRA and RoLoRA in Figure [5.](#page-7-0) In the early train- ing epochs, the rotation effectively suppresses the activation outliers. The rotation-aware fine-tuning can retain this optimal property. After fine-tuning with RoLoRA, as shown in Figure [5,](#page-7-0) the kurtosis κ across all layers is significantly reduced, which further gives rise to the low quantization error com- pared to the LoRA baseline. We also compare the activation distribution of RoLoRA against LoRA across layers in Figure [7](#page-13-0) in the Appendix.

 LoRA rank settings We explore the robustness of LoRA and RoLoRA towards various rank settings  $r \in \{4, 8, 16, 32, 64\}$  when fine-tuning LLaMA2- 7B and evaluated on zero-shot commonsense rea- soning tasks. The optimal rank setting for RoLoRA and LoRA are 16 and 32, respectively. The lower optimal rank indicates the potential of our RoLoRA to save trainable parameters. Overall, RoLoRA consistently outperforms LoRA regardless of the rank setting, demonstrating its robustness.

 Efficiency For the fine-tuning efficiency of RoLoRA, the additional training time is only in- curred by the online rotation operation  $(R_2 \text{ in Fig-}$  ure [2\)](#page-3-0) as the other rotation  $(R_1$  in Figure 2) can be directly merged into the original weights. There is only one additional matrix multiplication, and the



Figure 6: Average accuracy of W4A4 LLaMA2-7B finetuned with RoLoRA for varying ranks r.

increased rotation parameter can theoretically be **553** considered negligible. We reported the fine-tuning **554** cost of RoLoRA compared to LoRA in the same set- **555** tings (rank  $r = 16$ , batch size as 8, 3 total epochs)  $556$ in Table [9,](#page-7-2) where RoLoRA significantly improve **557** W4A4 quantized LLaMA2-7B performance with **558** extremely low additional overhead. **559**

<span id="page-7-2"></span>Table 9: The fine-tuning costs comparison on LLaMA2- 7B with batch size as 8 on NVIDIA H800 80G GPUs.

Method	<b>Training Time GPU Memory</b>		$ZCSR^7$ Avg.
LoRA	3.55 h	23.0 GB	37.0 (GPTO)
RoLoRA	3.65h	23.1 GB	62.3 (GPTO)

## 6 Conclusion **<sup>560</sup>**

This paper presents RoLoRA, the first work to ex- **561** plore the feasibility of *weight-activation* quantiza- **562** tion in LoRA. RoLoRA applies rotation for elim- **563** inating outliers in activation distribution and per- **564** forms rotation-aware fine-tuning to preserve the **565** outlier-free characteristics. We theoretically and **566** empirically investigate how to integrate rotation 567 into LoRA better. RoLoRA improves the perfor- **568** mance of W4A4 and W6A6 LLMs by a great margin across various tasks with the same training cost. **570** Moreover, RoLoRA can also help visual instruction **571** tuning and is compatible with other LoRA variants. **572**

## **<sup>573</sup>** Limitation

 In this work, we propose a rotation-based fine- tuning method that can effectively improve quanti- zation robustness to low-bit *weight-activation* PTQ via retaining the outlier-free characteristics. The fine-tuning is conducted on NVIDIA H800 GPUs, while the recent NVIDIA Blackwell-architecture GPUs with 4-bit floating point support may further improve the efficiency. We will take the limitations into account and improve in future work.

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## **825 A** Detailed Evaluation Results

**826** Table [10](#page-11-0) and Table [11](#page-12-0) listed the full evaluation results on zero-shot commonsense reasoning tasks and **827** MMLU benchmarks, respectively. We use the 'acc\_norm' in the evaluation report given by EleutherAI **828** evaluation harness [\(Gao et al.,](#page-8-15) [2021\)](#page-8-15) as the accuracy if there are such metrics. Otherwise, we use 'acc'.

<span id="page-11-0"></span>

#Bits	<b>Ouantizer</b>	Method			BoolQ PIQA HellaS.	WinoG.	Arc-e	Arc-c	<b>OBOA</b>	Avg.
LLaMA2-7B										
<b>FP16</b>		LoRA	81.2	79.8	78.6	70.6	73.9	47.7	46.8	68.4
W4A4	<b>RTN</b>	LoRA RoLoRA	46.0 67.1	49.5 67.7	27.0 59.7	49.6 56.9	27.8 58.3	24.2 35.0	26.8 34.2	35.8 54.1
	<b>GPTQ</b>	LoRA RoLoRA	52.3 73.5	52.5 76.2	26.9 71.8	50.4 64.1	28.6 67.7	25.3 42.2	22.8 40.4	37.0 62.3
	<b>RTN</b>	LoRA RoLoRA	76.3 77.9	78.0 79.1	75.3 76.3	69.2 68.5	71.2 74.8	45.7 47.3	41.6 43.6	65.3 66.8
	<b>GPTQ</b>	LoRA RoLoRA	76.3 77.4	78.2 79.1	75.4 76.5	69.5 70.4	72.1 75.2	46.1 47.2	40.8 44.0	65.5 67.1
					LLaMA2-13B					
FP16	$\bar{\phantom{a}}$	LoRA	83.9	81.2	80.9	74.2	74.4	51.3	47.6	70.5
	<b>RTN</b> W4A4	${\rm LoRA}$ RoLoRA	39.8 70.6	52.1 73.9	26.1 67.2	45.7 59.6	25.9 66.8	25.8 38.7	25.4 34.2	34.4 58.7
	<b>GPTQ</b>	LoRA RoLoRA	38.0 74.0	50.2 77.2	26.0 73.9	49.0 66.0	25.9 73.3	26.4 43.9	25.4 38.8	34.4 63.9
	<b>RTN</b>	LoRA RoLoRA	80.8 80.3	78.1 78.8	77.8 78.0	70.3 71.1	73.0 77.6	49.2 49.6	42.2 43.2	67.3 68.4
	<b>GPTQ</b>	LoRA RoLoRA	81.9 80.6	79.2 79.3	78.5 78.1	69.3 72.5	74.3 77.4	51.5 49.4	41.2 44.0	68.0 68.8
					LLaMA3-8B					
FP16	$\mathcal{L}$	LoRA	64.6	82.4	81.4	75.1	81.8	56.5	48.0	70.0
W <sub>4</sub> A <sub>4</sub>	<b>RTN</b>	LoRA RoLoRA	46.7 58.0	52.2 67.3	29.7 57.7	47.6 56.0	29.3 49.0	24.7 30.2	26.6 31.8	36.7 50.0
	<b>GPTQ</b>	LoRA RoLoRA	42.5 63.2	54.4 71.1	29.4 66.7	49.0 60.2	31.1 60.3	22.5 38.2	27.0 36.8	36.6 56.6
	<b>RTN</b> W6A6	LoRA RoLoRA	75.5 78.6	78.3 79.5	77.4 76.7	70.8 71.1	76.4 77.6	51.2 49.8	44.0 40.8	67.7 67.8
	<b>GPTQ</b>	LoRA RoLoRA	77.9 78.1	78.3 79.3	77.9 76.8	71.3 71.9	75.2 76.7	50.5 50.9	43.2 42.8	67.8 68.1

Table 10: Full accuracy comparison on zero-shot commonsense reasoning tasks of LLaMA series.

## 829 **B** Hyper-parameters for Reproduction

**830** In Table [12,](#page-12-1) we list the detailed hyper-parameters for reproducing RoLoRA and LoRA results. We do **831** not apply searches on any hyperparameters for better accuracy, all the settings for the LLaMA series and **832** LLaVA align with the default settings of [Zheng et al.](#page-10-5) [\(2024\)](#page-10-5) and [Liu et al.](#page-9-5) [\(2024a\)](#page-9-5).

**<sup>833</sup>** C Activation Distribution Visualization

**834** We visualize the magnitude of the activation of fine-tuned LLaMA2-7B using LoRA and RoLoRA in **835** Figure [7.](#page-13-0) The visualizations reveal a noticeable amount of outliers presented in the LoRA fine-tuned **836** model, but are highly eliminated in RoLoRA counterpart.

<span id="page-12-0"></span>

#Bits	<b>Ouantizer</b>	<b>Method</b>	Hums.	Other	<b>Social</b>	<b>STEM</b>	Avg.
			LLaMA2-7B				
FP16	$\overline{\phantom{a}}$	LoRA	41.5	50.8	48.2	34.7	43.5
W <sub>4</sub> A <sub>4</sub>	<b>RTN</b>	LoRA RoLoRA	24.2 24.7	24.8 26.2	22.7 27.2	21.7 25.7	23.5 25.8
	<b>GPTO</b>	LoRA RoLoRA	24.3 30.1	24.5 33.0	23.0 32.0	22.0 29.4	23.5 31.0
W <sub>6</sub> A <sub>6</sub>	<b>RTN</b>	LoRA RoLoRA	35.4 38.2	40.6 45.4	37.5 44.7	30.4 35.2	35.9 40.5
	<b>GPTO</b>	LoRA RoLoRA	34.2 37.8	39.4 46.1	39.4 46.2	30.6 34.9	35.7 40.8
			LLaMA2-13B				
FP16		LoRA	49.6	59.2	59.9	42.8	52.4
W <sub>4</sub> A <sub>4</sub>	<b>RTN</b>	LoRA RoLoRA	25.0 28.9	25.7 32.5	23.4 33.2	22.4 28.4	24.2 30.5
	<b>GPTQ</b>	LoRA RoLoRA	25.5 37.7	24.2 42.3	24.1 43.7	23.4 32.7	24.4 38.9
W <sub>6</sub> A <sub>6</sub>	<b>RTN</b>	LoRA RoLoRA	44.3 45.0	52.8 52.9	55.0 55.2	38.6 39.1	47.3 47.7
	<b>GPTO</b>	LoRA RoLoRA	44.8 45.6	54.7 53.7	53.8 55.2	39.0 38.7	47.6 47.9
			LLaMA3-8B				
FP16		LoRA	57.4	70.7	72.8	52.7	62.7
W <sub>4</sub> A <sub>4</sub>	<b>RTN</b>	LoRA RoLoRA	23.6 30.8	24.3 34.5	23.7 33.5	21.8 30.5	23.3 32.1
	<b>GPTQ</b>	LoRA RoLoRA	24.6 36.0	23.0 42.2	23.4 43.6	24.3 33.5	23.9 38.5
W <sub>6</sub> A <sub>6</sub>	<b>RTN</b>	LoRA RoLoRA	49.7 52.7	63.0 67.5	64.4 70.0	47.2 51.1	55.3 59.4
	<b>GPTO</b>	LoRA RoLoRA	48.8 52.9	61.8 68.3	63.9 69.6	45.7 50.4	54.3 59.4

Table 11: Full accuracy on MMLU Benchmark of LLaMA series.

Table 12: Detailed hyper-parameters for fine-tuning different LLMs and LMMs.

<span id="page-12-1"></span>

Model		LLaMA2-7B LLaMA2-13B LLaMA3-8B		$LLaVA-1.5-7B$
Epoch				
Learning Rate				
Batch Size (Per GPU)	8		8	
<b>Gradient Accumulation</b>				64
Warmup Ratio	0.01	0.01	0.01	0.03
Optimizer	AdamW	AdamW	AdamW	AdamW
LoRA Rank $r$	16	16	16	128
LoRA Dropout	0	$\Omega$	$\theta$	0.05
<b>LoRA</b> Target	$W_q, W_v$	$W_q, W_v$	$W_q, W_v$	$W_q, W_k, W_v, W_o, W_u, W_d, W_g$
Learning Rate	$1e^{-4}$		$1e^{-4}$	

<span id="page-13-0"></span>

Figure 7: Final activation distribution of the fine-tuned model produced using RoLoRA and LoRA. We select the output activation of *q\_proj* across layers with the index of 0, 1, 6, 11, 16, 21, 26, 31.