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The Open Proof Corpus: A Large-Scale Study of LLM-Generated Mathematical Proofs

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Abstract

In recent months, large language models (LLMs) have made significant progress in mathematical proof generation, but further advancement is hindered by the lack of a large-scale, high-quality dataset of human-evaluated proofs. While expensive to create, such a dataset is essential for driving improvements in training and enabling a rigorous analysis of proof generation capabilities. In this work, we present the Open Proof Corpus (OPC), a dataset comprising over 5,000 human-evaluated proofs produced by state-ofthe-art LLMs. The OPC was specifically designed for broad applicability and downstream usage in proof generation research and is the first to include a substantial number of correct, LLMgenerated solutions to problems from prestigious mathematics competitions such as the USAMO and IMO. Using the OPC, we explore critical questions in automated proof generation: (1) the performance gap between natural language and formal proof generation, (2) the discrepancy between final-answer accuracy and full-proof validity, and (3) the impact of best-of-n selection on proof quality. Finally, to showcase the utility of the OPC, we finetune an 8B-parameter model on the dataset, obtaining a model that performs on par with the best model, GEMINI-2.5-PRO, on the task of evaluating proof correctness.

1. Introduction

Large language models (LLMs) have recently achieved remarkable progress in mathematical reasoning, attaining top-competitor performance on various final-answer benchmarks such as AIME and HMMT (Balunović et al., 2025). However, growing evidence suggests that these benchmarks fail to capture the full breadth of mathematical reasoning capabilities, as they do not require models to produce complete proofs or detailed intermediate steps (Mahdavi et al., 2025; Guo et al., 2025b). Such step-bystep reasoning is critical for applications in theorem proving, mathematical research, and education. **Proof benchmarking** To address this gap, several evaluation efforts have emerged, revealing that LLMs significantly underperform on proof generation compared to existing final-answer benchmarks (Petrov et al., 2025; Mahdavi et al., 2025; Guo et al., 2025b). Despite their value, these benchmarks are severely limited in their use for broader analysis, training, and future development purposes. Specifically, they are small in size (Petrov et al., 2025; Guo et al., 2025b), rely on outputs from outdated models (Frieder et al., 2023), contain few correct proofs (Mahdavi et al., 2025), and are not fully open-sourced (Mahdavi et al., 2025; Guo et al., 2025b).

Open questions Furthermore, key questions about proof generation capabilities remain unanswered. First, while it is widely claimed that final-answer benchmarks are insufficient for evaluating proof generation capabilities, this claim is not yet substantiated by evaluating LLM-generated proofs on such benchmarks. Second, with recent advances in formal proof generation using systems like Lean (Ren et al., 2025; Wang et al., 2025), the performance gap between natural language and formal proof generation remains unclear. Third, the potential of best-of-n sampling strategies to improve proof quality has not been explored.

Our work: the Open Proof Corpus To address these challenges, we introduce the Open Proof Corpus (OPC): a large-scale, human-validated dataset comprising over 5,000 LLM-generated proofs across more than 1,000 problems. As shown in Fig. 1(a), each OPC sample includes (1) a problem from a high-quality mathematical competition such as the International Mathematical Olympiad (IMO), (2) a proof generated by a state-of-the-art LLM, and (3) a binary human evaluation of the proof's correctness with feedback. The OPC was specifically designed for downstream usage in proof generation research, enabling both training and evaluation of LLMs on proof generation tasks. To address the open questions outlined earlier, the OPC includes problems from specific sources: problems from the PutnamBench (Tsoukalas et al., 2024) enable comparisons between formal and informal reasoning, while problems from MathArena (Balunović et al., 2025) support evaluation of proof correctness for problems with final answers.



Figure 1: Overview of the OPC and its conclusions. On the left, we show a typical sample from the OPC, including a question taken from a high-quality mathematical competition, a proof generated by an LLM, and a human judgment of the proof's correctness. On the right, we summarize the main conclusions drawn from the OPC.

076 Key findings Despite the difficulty of problems in 077 the OPC, state-of-the-art LLMs demonstrate surprisingly 078 strong performance. For instance, O4-MINI correctly 079 solves almost 20% of the problems in the IMO Shortlist, and the OPC generally consists of 43% correct proofs. Fur-081 thermore, as shown in the top left of Fig. 1(b), LLMs ex-082 hibit strong capabilities in evaluating proofs: GEMINI-2.5-083 PRO achieves 88.1% accuracy in judging proof correctness—nearly matching human performance at 90.4%. To 085 showcase the utility of the OPC, we fine-tune DEEPSEEK-086 R1-QWEN3-8B (Guo et al., 2025a) using GRPO (Shao 087 et al., 2024) on the OPC, resulting in an open model that 088 achieves 88.1% judgment accuracy, on-par with GEMINI-089 2.5-PRO and outperforming all other models. 090

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092 Answering open questions The OPC allows us to em-093 pirically resolve the open questions outlined above, with all 094 conclusions shown in Fig. 1(b). First, as shown on the top 095 right, we find that natural language proof generation signif-096 icantly outperforms formal proof generation: on Putnam-097 Bench, GEMINI-2.5-PRO solves 11 times more problems 098 than the best formal model, DEEPSEEK-PROVER-V2 (Ren 099 et al., 2025). Second, as shown on the bottom left, we ob-100 serve a substantial gap between final-answer accuracy and proof correctness. While GEMINI-2.5-PRO loses only 8% of its final-answer accuracy when proof correctness is required, 03 suffers a drop of almost 30%. Third, as shown 104 on the bottom right, we find that best-of-n strategies yield 105 large gains in performance. Interestingly, while standard 106 best-of-n selection methods moderately improve accuracy from 26% to 36%, a ranking-based approach inspired by (Liu et al., 2025) achieves the highest performance of 47%. 109

Main Contributions Our key contributions are:

- A scalable pipeline for generating and evaluating natural language mathematical proofs (§3).
- The Open Proof Corpus, a large, human-validated dataset of over 5,000 LLM-generated proofs (§4).
- New benchmarking results on the OPC, resulting in novel insights into current LLM capabilities (§5).
- An open-source, 8B-parameter model fine-tuned on the OPC that achieves 88.1% judgment accuracy, tied with the best model on this task $(\S5)$.

2. Related Work

We briefly recapitulate the relevant literature on mathematical reasoning benchmarks and datasets.

Final-answer benchmarks Final-answer benchmarks evaluate models by comparing a final answer from the model's output with a ground-truth answer, typically using rule-based parsers. With the advent of reasoning LLMs (Jaech et al., 2024; Guo et al., 2025a), older benchmarks have become saturated (Cobbe et al., 2021; Lightman et al., 2024), and even more recent ones are nearing saturation (Gao et al., 2025; He et al., 2024; Balunović et al., 2025; Gulati et al., 2024). Only private benchmarks such as FrontierMath (Glazer et al., 2024) and HLE (Phan et al., 2025) remain sufficiently challenging for the latest models. However, these benchmarks do not require the generation of full proofs or detailed reasoning steps. Moreover, their private nature hinders reproducibility and broader community engagement, both key factors in driving progress.

Formal proof generation Another growing line of work 111 involves training LLMs to generate formal proofs in lan-112 guages such as Lean (de Moura and Ullrich, 2021) or 113 Isabelle (Nipkow et al., 2002), which can then be auto-114 matically verified by these systems (Zheng et al., 2022; 115 Tsoukalas et al., 2024; Yu et al., 2025). While this 116 paradigm enables rigorous correctness checking, it typi-117 cally requires models to be specifically finetuned for formal 118 proof generation (Ren et al., 2025; Wang et al., 2025; Lin 119 et al., 2025). In contrast, state-of-the-art general-purpose 120 models like O3 and GEMINI-2.5-PRO struggle with formal 121 proof generation. As a result, formal reasoning currently 122 does not allow to make full use of the natural language ca-123 pabilities of these general-purpose models, and, as we show 124 in §5, there remains a significant performance gap between 125 formal and natural language proof generation, with the lat-126 ter being substantially more effective.

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128 Proof-generation evaluation efforts Going beyond 129 final-answer accuracy has gained recent attention, with 130 several works investigating the reasoning traces of recent 131 LLMs to identify patterns and potential for improvement 132 (Shojaee et al., 2025; Mondorf and Plank, 2024; Xia et al., 133 2025). However, only a few studies have focused directly 134 on evaluating full proofs. Petrov et al. (2025) evaluated 135 LLMs on the six problems from the USAMO 2025, uncov-136 ering significant flaws in the generated proofs. Similarly, 137 Mahdavi et al. (2025) evaluated LLM performance on a 138 large set of IMO Shortlist problems, finding that no model 139 surpassed 5% accuracy. In contrast, Frieder et al. (2023) re-140 ported that GPT-3.5 and GPT-4 performed well on simpler 141 tasks, generating correct proofs in a significant fraction of 142 cases. Still, all these studies are limited by either the use of 143 outdated models or the small scale of their evaluations. 144

145 Two concurrent works have recently expanded this line of 146 research. Sheng et al. (2025) focus specifically on inequality proofs and primarily emphasize the development of an 147 148 LLM as a judge framework to mitigate the high cost of hu-149 man evaluation. Guo et al. (2025b) highlight a notable gap between final-answer accuracy and the ability to generate 150 correct proofs, a finding we confirm in §5. However, their 151 152 analysis stops at this observation and does not evaluate per-153 formance on an established final-answer benchmark. Fur-154 ther, both studies are limited in scale compared to the OPC and have not open-sourced their human-annotated proofs. 155 156

Mathematical training datasets Several large-scale datasets have been developed to train LLMs on mathematical reasoning. One of the earliest, Li et al. (2024), compiled a large dataset of internet-sourced problems, including both final-answer questions and natural language proofs. However, it lacks LLM-generated proofs, human judgments, and examples of incorrect proofs. Other datasets have

focused exclusively on final-answer tasks (Albalak et al., 2025; He et al., 2025; Moshkov et al., 2025), offering limited support for training or evaluating proof generation. Finally, Zhang et al. (2025) introduced a dataset of both valid and invalid problem statements, each accompanied by LLM-generated proofs. While this ensures that incorrect proofs exist for invalid statements, the dataset does not include human evaluation of proofs or any other information on the validity of the proofs.

LLM as a judge The widespread success of LLMs has led to the development of the "LLM as a judge" paradigm, which enables scalable, consistent, and cost-effective evaluation of complex outputs (Zheng et al., 2023; Gu et al., 2024). This approach serves as a promising alternative to traditional expert-based evaluation and opens up new possibilities for self-assessment during generation through methods such as best-of-n sampling, feedback-guided decoding, and self-training (Pan et al., 2023; Madaan et al., 2023; Weng et al., 2023; Jiang et al., 2025). However, concerns remain about the robustness of this framework in high-stakes domains like mathematical reasoning, where issues such as overconfidence and self-degradation can undermine reliability (Huang et al., 2024; Pan et al., 2023).

3. Methodology

Accurately evaluating LLM-generated proofs is a challenging task. Models often make difficult-to-detect errors, and they rarely acknowledge when they cannot solve a problem (see §5). In this section, we outline the methodology used to create the OPC, with particular emphasis on the complexities of evaluating LLM-generated proofs and our efforts to maximize dataset size. Since human judges cannot reasonably spend hours studying each problem, we developed a pipeline to support efficient grading. This pipeline consists of three main components: problem and judge preparation (§3.1), the grading procedure (§3.2), and monitoring and validation (§3.3).

3.1. Problem and Judge Preparation

Judge selection Judges were selected from among former IMO participants or individuals who reached the final stages of IMO selection in their respective countries. We contacted each judge personally to ensure they were qualified, motivated, and easily accessible for ongoing communication. A total of 13 judges were involved, each responsible for grading a varying number of problems. Three of the most active judges had prior experience with evaluating LLM-generated proofs. One judge served as the coordinator, maintaining regular communication, tracking progress, and ensuring consistency and motivation across the group. Problem selection Problems were drawn from top-tier national and international mathematics competitions, with the goal of capturing a balanced mix of correct and incorrect proofs. All problems were sourced from official materials. Non-English problems were translated using GPT-4.1 and manually verified for accuracy. When available, official ground-truth solutions were also extracted and provided to the judges as references.

174 Proof generation Proofs were generated using a set 175 of state-of-the-art LLMs known for their strength in 176 mathematical reasoning. Specifically, we used O4-MINI 177 and 03 from OpenAI (OpenAI, 2025), GEMINI-2.5-PRO 178 from Google (Google DeepMind, 2025), GROK-3-MINI 179 from xAI (xAI, 2025), QWEN3-235B-A22B from Qwen 180 (Qwen Team, 2025), and the latest version of DEEPSEEK-181 R1 from DeepSeek (Guo et al., 2025a). DEEPSEEK-R1 182 was released mid-way through dataset construction and re-183 placed GROK-3-MINI thereafter. We designed the model 184 prompt to clearly instruct models to generate full solutions, 185 refining it through small-scale pilot tests. The final prompt 186 is shown in App. E.1. All models were run with default pa-187 rameters and a maximum generation length of 64,000 to-188 kens. If this limit was exceeded before a complete proof 189 was generated, we re-sampled. For the MathArena subset 190 (Balunović et al., 2025), we only retained solutions with a 191 correct final answer, retrying generation if necessary. For PutnamBench (Tsoukalas et al., 2024), we appended the 193 informal final answer (if present) to the problem statement to mirror the setup for formal models, allowing direct com-195 parison between natural and formal proof outputs. 196

197 **3.2. Grading Procedure**

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198 User interface We built a custom web interface to facil-199 itate efficient grading. A sample instance is available at 200 https://judgeproofs.xyz/sample, with screenshots in-201 cluded in App. D. The interface displays the problem, refer-202 ence solution (if available), anonymized model-generated 203 proof, and grading form. Judges could mark the prob-204 lem or solution as malformed (to filter such cases from the 205 dataset), grade the proof, and annotate sentences from the 206 model-generated proof with comments. Continuous feed-207 back from judges helped us refine the interface over time. 208

209 Judge instructions Judges were asked to label proofs as 210 either correct or incorrect and provide written justification. 211 Precise grading guidelines were critical to avoid inconsis-212 tencies in edge cases, such as minor omissions or shortcuts. 213 To prevent overly strict grading, we clearly defined what 214 level of omissions and frequency of mistakes were accept-215 able in a correct proof. The full guidelines are available at 216 https://judgeproofs.xyz/instructions/, with a sum-217 mary in App. D. These instructions were developed collab-218 oratively with the judges and finalized after a pilot phase. 219

Abstention and uncertainty Judges were allowed to abstain from grading a proof if they lacked the necessary expertise or found the solution too complex or convoluted. They could also mark judgments as uncertain in border-line cases, which proved especially useful for near-correct proofs containing subtle errors. Less than 3% of proofs in the OPC are flagged as uncertain.

LLM issue summaries After several hundred graded proofs, we introduced a new feature to support grading: an automatically generated summary of the proof using 04-MINI. These summaries flagged potential issues—such as logical gaps or missing steps-based on a specially designed prompt (see App. E.2). Importantly, the model was instructed not to give a final verdict, only to indicate possible issues for human review. Judges reported that this significantly improved their efficiency and accuracy in detecting errors. To ensure the inclusion of these summaries did not bias our judges, we evaluated the agreement rate between O4-MINI as a judge and human graders before and after their introduction. There was no significant difference in agreement, suggesting no introduction of bias into the grading process. However, in experiments involving best-of-n selection-where the LLM judge acts as a selection mechanism-we omitted these summaries to avoid any form of compounding bias in the evaluation.

Problem distribution Problems were assigned to judges based on their mathematical background and availability. Judges not qualified to evaluate undergraduate-level problems were excluded from grading those problems.

3.3. Monitoring and Validation

To ensure grading quality and judge consistency, we implemented a set of monitoring and validation procedures.

Coordinator One experienced judge was assigned as coordinator, responsible for tracking grading progress, resolving issues, and ensuring motivation. As a senior author, the coordinator had detailed knowledge of the dataset's goals and methodology and was available to answer judges' questions throughout the process.

Pilot phase Prior to full-scale grading, we conducted a test run with a limited number of problems. This helped us identify interface issues, unclear instructions, and other inefficiencies. Based on feedback, we revised the interface and grading guidelines before launching the full evaluation.

Monitoring discrepancies Approximately 10% of the proofs were double-graded to evaluate inter-judge consistency. Disagreements were reviewed by the coordinator to determine whether they arose from misunderstandings, ambiguous instructions, or errors overlooked by a judge.



Figure 2: Overview of competitions included in the OPC.

If possible, instructions were further improved to prevent similar issues. However, most inconsistencies stemmed from overlooked errors in the proofs and could therefore not be resolved by clarifying the instructions. If the coordinator identified a significant number of discrepancies for a specific judge, they would discuss the issue with the judge to clarify instructions.

4. Open Proof Corpus

We now introduce the OPC, providing an overview of the competitions and models it includes and key dataset statistics. At a high level, the OPC is built to support the training and evaluation of proof generation models and to facilitate a rigorous analysis of their capabilities.

Basic properties The OPC consists of 5,062 proofs across 1,010 distinct problems, generated by six state-of-the-art LLMs. Each proof is labeled as either correct or incorrect by one or two human judges. Labels are accompanied by short justifications, with optional annotations highlighting specific sentences within the proof. Each problem may also include metadata such as its competition source, difficulty level, and other relevant attributes.

Competitions Problems were sourced from a wide range of prestigious mathematics competitions. A full breakdown is provided in App. A, with a summary shown in Fig. 2. App. A also reports the average accuracy of the best-performing model per competition, offering a rough proxy for difficulty. Most problems are at the high school level, with only a small portion drawn from undergraduate-level competitions. Competitions were selected to cover a broad range of difficulties while ensuring an overall average model accuracy of approximately 50%.

Table 1: Number of solutions	s evaluated per model.
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Model	# Solutions
04-mini	1615
03	892
QWEN3-235B-A22B	890
Gemini-Pro	878
Grok-3-Mini	461
DeepSeek-R1	326

Models Table 1 summarizes the number of proofs generated by each model in the OPC. Not all models contributed to every problem, but most problems include solutions from at least five models. O4-MINI contributed the largest share of proofs, as it was used extensively in best-of-n and pass@n experiments.

Human performance and noise To estimate label reliability, we double-graded approximately 10% of the dataset. Among these, judges agreed on the proof's correctness in 90.4% of cases. Assuming independent judgments, we can estimate the individual judge error rate p by solving $0.904 = (1 - p)^2 + p^2$, giving p = 5%. This indicates a relatively low noise level, which is expected for a human-annotated dataset of this complexity.

Data splits The OPC is divided into four subsets, each serving a distinct purpose:

- MathArena: A test set of 112 problems from Math-Arena (Balunović et al., 2025), a final-answer benchmark for mathematical reasoning.
- **PutnamBench**: A subset of 114 problems from PutnamBench (Tsoukalas et al., 2024), used to compare natural language and formal proof generation.
- **Best-of-n**: A subset of 152 problems from the IMOSL, USAMO, and BMOSL, each solved multiple times by 04-MINI. For 60 of these problems, all 8 generations were human-evaluated. The rest include judgments only for the generation selected by a best-of-n selection strategy.
- **Generic**: A subset of 676 problems from various competitions, including the IMOSL, USAMO, BMOSL, and others, all solved by multiple models.

The MathArena and PutnamBench subsets are drawn from existing public benchmarks and should be treated strictly as test sets. The generic and best-of-n subsets, by contrast, are intended for training, validation, and further analysis. However, a small portion of the generic subset is held back for benchmarking purposes as well.



Figure 3: Average proof correctness of various models on the OPC. Data is split into two partitions, the first, resp. second, containing only problems answered by all models except DEEPSEEK-R1, resp. GROK-3-MINI. The discrepancy between the two partitions is due to the inclusion of harder competitions in the second partition.

5. Results

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297 We present the main findings derived from the OPC. In §5.1, we evaluate the proof-generation capabilities of var-299 ious models. §5.2 evaluates the ability of LLMs to judge 300 the correctness of proofs. In §5.3, we compare informal 301 and formal proof-generation performance. §5.4 analyzes 302 proof correctness given correct final answers. Finally, §5.5 303 examines the effectiveness of best-of-n selection strategies. 304 In App. C, we additionally provide several qualitative ob-305 servations about common mistakes in the generated proofs. 306

307 308 **5.1. GEMINI-2.5-PRO Is The Best Proof Generator**

Fig. 3 shows the average proof correctness of each model 309 on a filtered subset of the OPC, including only ques-310 tions answered by all models except GROK-3-MINI or 311 DEEPSEEK-R1. GEMINI-2.5-PRO achieves the highest 312 average accuracy, slightly outperforming O4-MINI. 313 In contrast, the two open-source models-OWEN3-235B-314 A22B and DEEPSEEK-R1-underperform significantly, 315 highlighting the current performance gap between closed-316 source and open-source models in proof generation. 317

318 Out of more than 1,700 incorrect solutions analyzed, mod-319 els explicitly state their inability to solve the problem in 320 only 114 instances, with all but five of those generated by 03. Even 03 is more likely to produce an incorrect proof 322 than to acknowledge uncertainty. This widespread reluc-323 tance to admit failure highlights a key limitation: current 324 LLMs lack effective mechanisms for confidence calibra-325 tion and knowing their limitations. In domains like mathematics, this could undermine trust in systems that rely on 327 LLMs for provably correct solutions, especially given the 328 difficulty of evaluating proofs correctly. 329

Table 2:	Benchmarking	; LLMs	as proof	graders.	Cost for
running t	the model on th	e entire	subset is	given in	USD.

Judge	pass@1	maj@5	Cost
Human	90.4	-	N/A
Gemini-2.5-Pro	85.4	88.1	135.47
OPC-R1-8B	83.8	88.1	N/A
04-mini	83.8	85.3	29.57
03	83.1	84.3	93.30
Gemini-2.5-Flash	82.7	86.0	86.95
QWEN3-235B-A22B	81.8	84.6	3.79
DEEPSEEK-R1	80.9	82.6	27.35
QWEN3-30B-A3B	74.0	75.4	N/A
DEEPSEEK-R1-QWEN3-8B	70.7	71.3	N/A
CLAUDE-4-SONNET	70.6	75.0	28.21
QWEN3-8B	64.4	63.6	N/A
GPT-4.1	61.4	60.8	20.33
BASELINE	53.2	53.2	N/A

5.2. LLMs Are Near-Human Level Judges

The OPC is fundamentally a dataset of binary human judgments on proof correctness, making it well-suited for training and evaluating LLMs as proof judges. To leverage this, we split the generic subset by problem into training and test sets. Using GRPO (Shao et al., 2024), we fine-tune DEEPSEEK-R1-QWEN3-8B on the training set with human labels for reward modeling.

The test set comprises 293 LLM-generated proofs. We evaluate both specialized reasoning models, such as GEMINI-2.5-PRO and O4-MINI, and general-purpose models like GPT-4.1. As a simple baseline, we classify proofs under 100 characters as incorrect and guess randomly otherwise.

As shown in Table 2, GEMINI-2.5-PRO achieves the highest judging accuracy: 85.4% with a single evaluation pass and 88.1% with majority voting, approaching the 90.4%human baseline. Notably, OPC-R1-8B matches GEMINI-2.5-PRO's majority voting performance and outperforms its base model by 17%, demonstrating the value of the OPC and its potential for advancing the field of proof evaluation and generation. However, since the train and test sets share the same distribution, OPC-R1-8B's performance may degrade on out-of-distribution data.

LLMs often favor their own generations (Panickssery et al., 2024). To investigate this, we evaluate how well models judge their proofs compared to those generated by others. In Table 3, we find that all models except QWEN3-235B-A22B perform significantly worse when judging their own proofs, indicating an inability to self-critique effectively. This suggests that LLMs struggle to recognize their mistakes, which is a critical limitation for applications requiring self-assessment or iterative improvement.

Table 3: Judgement accuracy breakdown split by solver,
highlighting the lowest score for each judge. For visual
clarity, we shortened GEMINI-2.5-PRO to GEMINI, 04MINI to 04, and QWEN3-235B-A22B to QWEN.

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335	Prover	CDADY	0.4	07	OWEN
336	Judge	GEMINI	04	03	QWEN
337	GEMINI-2.5-PRO	79.4	87.1	91.6	80.6
338	04-mini	86.9	81.3	83.1	84.1
339	03	85.9	84.8	76.9	87.8
340	QWEN3-235B-A22B	80.0	81.9	79.1	84.4
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Figure 4: Average proof correctness on the PutnamBench.

This positive result appears to contradict with Petrov et al. (2025), who reported poor performance of judge models. However, their evaluation was based on a limited set of problems, relied on older models, and focused on the more challenging task of scoring proofs on a continuous rather than a binary scale. In addition, we put considerable effort in crafting clear and comprehensible prompt instructions.

5.3. Formal Proof Generation Lags Behind

Using the PutnamBench subset, we compare formal and 367 natural language proof-generation models. The best formal model, DEEPSEEK-PROVER-V2 (Ren et al., 2025), 369 achieves less than 8% accuracy on PutnamBench. In con-370 trast, Fig. 4 shows that the top informal model, GEMINI-371 2.5-PRO, reaches almost 83% accuracy on the evaluated subset, clearly outperforming all formal models. Despite 373 this disparity, formal proofs offer a major advantage: auto-374 matic verifiability. While informal methods currently dom-375 inate in performance, formal approaches remain crucial for 376 scalable, rigorous proof checking. 377

5.4. Proof Generation and Final Answer Do Not Align

Although it is widely claimed that final-answer benchmarks are inadequate for evaluating proof generation capabilities (Petrov et al., 2025; Mahdavi et al., 2025; Guan et al., 2025), it remains unclear how often LLMs can pro-



Figure 5: Comparison of final-answer accuracy and proof correctness on the MathArena subset.



Figure 6: Pass@n metric on a small subset of the OPC compared with some best-of-n selection strategies.

duce a valid proof when they find the correct answer. To investigate this, we first collect instances from the Math-Arena subset where models generate correct final answers, and then manually evaluate the validity of the accompanying proofs. This enables us to estimate the overall proof correctness rate P(correct proof) and compare it with the final-answer accuracy P(correct final answer).

In Fig. 5, we report each model's accuracy alongside the stricter metric requiring both a correct final answer and a valid proof. Despite GEMINI-2.5-PRO, O4-MINI, and O3 achieving similar final-answer accuracy, their proof correctness rates differ significantly. Specifically, O3 performs notably worse, with only 59.5% of its answers containing a correct proof. This substantial variation across models highlights that final-answer accuracy alone is not a reliable indicator of proof generation capability.

5.5. Best-of-n Significantly Improves Performance

Best-of-n selection—generating multiple outputs and selecting the best one—is a common strategy for improving LLM performance. We evaluate this approach using O4-MINI by generating eight proofs per problem in the bestof-n subset and testing four selection methods:



Figure 7: Best-of-n selection strategies on the entire bestof-n subset of the OPC.

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- **Discrete**: 04-MINI classifies each proof as correct or incorrect and selects any correct proof.
- **Continuous**: O4-MINI scores proofs on a 0-7 scale and selects the one with the highest score.
- **Rank (Bracket)**: A ranking method proposed by Liu et al. (2025). Proofs are judged pairwise by 04-MINI in a knockout tournament until one proof remains. Note that Liu et al. (2025) finetuned their model on the judging task, while we use 04-MINI itself.
- **Rank** (Swiss): Inspired by Liu et al. (2025), proofs are ranked via pairwise comparisons in a Swiss roundrobin tournament. Ratings are computed using the Bradley-Terry model (Bradley and Terry, 1952), and the answer with the highest rating is selected. See App. B for details of this method.

⁴¹³ Prompts for all methods can be found in App. E. Note that ⁴¹⁴ *Rank (Bracket)* only requires O(n) comparisons, and is ⁴¹⁵ therefore as efficient as the discrete and continuous meth-⁴¹⁷ ods, while *Rank (Swiss)* requires $O(n^2)$ comparisons, mak-⁴¹⁸ ing it more expensive.

418 In Fig. 6, we compare the performance of these methods 419 with the pass@n metric on the 60 problems that contain hu-420 man judgments for all eight proofs. We find that best-of-n 421 selection strategies can significantly improve proof genera-422 tion performance. Furthermore, the pairwise ranking meth-423 ods significantly outperform the discrete and continuous 424 methods by approximately 10%. Notably, while discrete 425 and continuous methods plateau after n = 5, ranking ap-426 proaches continue to scale. Finally, Rank (Swiss) slightly 427 outperforms Rank (Bracket) by a 3% margin. 428

In Fig. 7, we evaluate the performance of the best-of-n selection strategies on the entire best-of-n subset of the OPC,
except for the *Rank (Bracket)* method, which was not evaluated on the full subset. The improved performance of the
ranking methods is confirmed on the entire best-of-n subset, with *Rank (Swiss)* improving accuracy by 17%.

6. Limitations

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While the OPC represents a significant advancement in the development and evaluation of LLM proof-generation ca-

pabilities, it is not without limitations. First, since most problems in the OPC are sourced from publicly available mathematical competitions, there is a risk of data contamination. Some of these problems may have been encountered during the training of the models. However, since the main purpose of the OPC is not related to benchmarking but rather to provide a large, human-validated dataset of LLM-generated proofs, this issue is less critical. Second, the majority of problems in the OPC are derived from high school level competitions. As a result, the dataset does not cover more advanced mathematical domains, such as undergraduate or research-level mathematics.

7. Future Work

The OPC offers a valuable resource for advancing research in proof generation with LLMs, supporting both the training and evaluation of models across a diverse set of mathematical problems. Our analysis also highlights several critical gaps and challenges that warrant further research. First, the significant disparity between formal and natural language proof generation-outlined in §5.3-points to the need for more effective strategies to bridge this divide. Second, the OPC demonstrates that current benchmarks, which often rely solely on final answers, fail to capture the full complexity and quality of generated proofs, as discussed in §5.4. This underscores the need for the development of a scalable benchmarking pipeline tailored to proof generation tasks. Finally, while our results show that best-of-n sampling strategies can meaningfully improve proof quality (see §5.5), further research is required to better understand and optimize these methods.

8. Conclusion

In this work, we introduced the *Open Proof Corpus (OPC)*, a large-scale, human-validated dataset of over 5,000 LLMgenerated proofs across more than 1,000 problems. Designed to support training, evaluation, and benchmarking, the OPC provides a robust foundation for advancing research in automated proof generation. Using the OPC, we conducted a thorough evaluation of current LLM capabilities in mathematical reasoning. Our analysis reveals several key findings: (1) modern LLMs can generate a significant number of correct proofs; (2) some models approach human-level performance in judging proof correctness; (3) natural language proof generation substantially outperforms formal proof generation; (4) finalanswer benchmarks are a poor proxy for proof quality; and (5) best-of-n sampling strategies significantly improve proof-generation accuracy. Using the OPC, we also trained an open-source model that achieves 88.1% accuracy in judging proof correctness, matching the performance of the best closed-source model, GEMINI-2.5-PRO.

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The Open Proof Corpus

Competition	Description	Problems	Solutions	Level	Туре	Acc	Source
	Main Analysis						
Balkan MO Shortlist	Competition between Balkan countries	74	368	HS	Ι	31.7%	Public
Baltic Way MO	Northern and Central European Olympiad	80	395	HS	Ι	68.1%	Public
British MO Final	Final round of the British Olympiad	23	114	HS	Ν	78.3%	Public
British MO Prelim	Preliminary round for the British Olympiad	28	139	HS	Ν	87.5%	Publi
Bulgarian Seasonal Competitions	Seasonal Competitions hosted in Bulgaria (8th-12th grade)	49	242	HS	Ν	63.5%	Public
European Girls' MO	Europe-wide olympiad allowing only girls as participants	47	227	HS	Ι	37.8%	Public
IMC	International competition for university students	43	212	UG	Ι	62.2%	Public
MO Shortlist	Shortlist of problems, from which the IMO is selected	128	629	HS	Ι	18.0%	Public
International Zhautykov MO	Kazakhstan-based olympiad with near-IMO-level questions	41	203	HS	Ι	34.2%	Publi
Irish MO	Final round of the Irish Olympiad	51	255	HS	Ν	92.0%	Publi
Putnam	Undergraduate competition, regarded as one of the most difficult	8	35	UG	Ι	100.0%	Publi
Romanian Masters of Mathematics Extralist	IMO-level competition hosted in Romania	33	162	HS	Ι	43.3%	Privat
Swiss MO	Various problems from the Swiss Olympiad	8	39	HS	Ν	87.5%	Publi
JSA Junior MO	USA olympiad that allows only junior students	25	121	HS	Ν	52.2%	Publi
JSAMO	The final round of the USA Math Olympiad	38	190	HS	Ν	35.1%	Publi
	PutnamBench						
Putnam	Undergraduate competition, regarded as one of the most difficult	114	564	UG	Ι	82.7%	Publi
	MathArena						
AIME 2025	Answer-based competition, serving as a qualifier for the USAMO	24	93	HS	Ν	95.7%	Publi
BRUMO 2025	Answer-based competition hosted by Brown University	28	114	HS	Ν	100.0%	Publi
HMMT February 2025	Answer-based competition hosted by Harvard and MIT	26	103	HS	Ν	97.8%	Publi
SMT 2025	Answer-based competition hosted by Stanford	34	128	HS	Ν	92.6%	Priva
	Best-of-n						
Balkan MO Shortlist	Competition between Balkan countries	45	287	HS	Ι	62.5%	Publ
IMO Shortlist	Shortlist of problems, from which the IMO is selected	57	269	HS	Ι	30.8%	Publ
USAMO	The final round of the USA Math Olympiad	40	173	HS	Ν	66.7%	Publ

Table 4: A list of competition sources for the problems in OPC.

A. Competitions in the OPC

The OPC contains over 1000 problems that were sourced from national and international competitions of varying difficulty. In Table 4, we present the problem and sample distribution for each. We also include the following additional information:

- Level: the education level the problems are appropriate for, either high school (HS) or undergraduate (UG).
- Type: whether the competition is hosted internationally (I) or only nationally (N).
- Source: we link the source, from which we obtained the problems. Any source that is not publicly available was marked as "Private".
- Acc: the average accuracy of the best-performing model on the competition problems, which serves as a rough proxy for difficulty.

B. Swiss Ranking Methodology

We briefly describe the Swiss ranking method used as a best-of-n selection strategy. In this approach, a round-robin tournament is performed where each proof competes against every other. In each "game", two proofs are compared by O4-MINI, which decides which proof is better, or if they are equally good.

To determine the overall winner, we compute a rating for each proof using the Bradley-Terry model (Bradley and Terry, 1952), a probabilistic model for paired comparisons commonly applied in LLM evaluation (Zheng et al., 2023; Dekoninck et al., 2025). The Bradley-Terry model estimates the probability that a proof with rating r_i beats a proof with rating r_i as:

$$P(i \text{ beats } j) = \frac{1}{1 + \exp(r_j - r_i)}.$$

We fit the model to the outcomes of the round-robin tournament using maximum likelihood estimation, resulting in a rating for each proof. The proof with the highest rating is selected as the best.

C. Qualitative Observations

Building on our quantitative analysis, we present several qualitative insights drawn from our judges' evaluations. These include common failure modes and notable model behaviors.

Incorrect handling of inequalities Many models sometimes make mistakes when manipulating inequalities. A frequent issue is the improper reversal of inequality signs during intermediate steps without mathematical justification. This results in incorrect final answers despite seemingly coherent reasoning. Below is an example of such a mistake made by DEEPSEEK-R1, where the incorrect sign reversal is marked with "**".

W DEEPSEEK-R1 – Baltic Way 2004 P3

Summing these inequalities gives

 $\sum_{\text{cyc}} \frac{a+b}{a+b+1} \ge \sum_{\text{cyc}} \left(1 - \frac{1}{3(ab)^{1/3}} \right) = 3 - \frac{1}{3} \sum_{\text{cyc}} (ab)^{-1/3}.$

•••

. . .

By AM-GM again,

$$\begin{split} a^{1/3} + b^{1/3} + c^{1/3} &\geq 3\sqrt[3]{a^{1/3}b^{1/3}c^{1/3}} = 3(abc)^{1/9} = 3 \cdot 1^{1/9} = 3, \\ \text{with equality if and only if } a^{1/3} = b^{1/3} = c^{1/3}, \text{ i.e., } a = b = c. \text{ Thus,} \\ \sum_{\text{Cyc}} \frac{a+b}{a+b+1} * * &\geq * * 3 - \frac{1}{3} \cdot 3 = 3 - 1 = 2. \\ \dots \end{split}$$

Struggles with synthetic geometry reasoning In Olympiad-level geometry problems, models often default to coordinate-based methods, i.e., using computations with complex numbers or a specific coordinate system to "bash" the problem, especially on easier problems where such techniques are tractable. However, for harder problems, models tend to shift toward synthetic approaches, relying on geometric theorems and properties. These harder problems typically require keeping track of multiple different but related angles and a robust understanding of geometric relationships. Here, models frequently struggle: they sometimes confuse angle orientations, misidentify congruent angles, reverse point orderings, or apply geometric properties incorrectly. In the following example, GEMINI-2.5-PRO correctly identifies the base of an isosceles triangle in one case, but subsequently deduces the wrong pair of equal angles—illustrating a common angle-reasoning failure.

GEMINI-2.5-PRO – IMOSL 2013 G4

Thus, $\angle PBA = \angle QBA$ where these angles are $\angle (BP, BA)$ and $\angle (AB, BQ)$. The problem states these are equal to γ .

So, $\angle(BP, BA) = \gamma$ and $\angle(AB, BQ) = \gamma$. This means $\angle PBQ = \angle(BP, BA) + \angle(AB, BQ) = \gamma + \gamma = 2\gamma$.

We are given that D is an interior point of segment BQ and $PD=PB. \label{eq:point}$

Thus, riangle PBD is an isosceles triangle with base BD.

The angle ${\angle}PBD$ in ${\triangle}PBD$ is ${\angle}PBQ$, so ${\angle}PBD=2\gamma.$

The base angles are $\angle BPD = \angle BDP = \frac{180^\circ - 2\gamma}{2} = 90^\circ - \gamma.$ So, $\angle PDB = 90^\circ - \gamma$. Since D is on segment BQ, this is $\angle (DP, DB) = 90^\circ - \gamma$

Incorrect citation of IMOSL 2004 G8 by GEMINI-2.5-PRO A curious behavior observed exclusively in GEMINI-PRO is the repeated and inappropriate citation of the 2004 IMO Shortlist geometry problem G8. This reference appears in over 15 different solutions, often in problems unrelated to geometry. Notably, these citations consistently occur at points where

the model appears to get stuck. No other model in our evaluation displayed this behavior. An illustrative example is shown below.

EGMO 2018 P3

The n contestants of EGMO are named C_1, C_2, \ldots, C_n . After the competition, they queue in front of the restaurant according to the following rules.

- The Jury chooses the initial order of the contestants in the queue.
- Every minute, the Jury chooses an integer i with $1 \leq i \leq n.$
- If contestant C_i has at least i other contestants in front of her, she pays one euro to the Jury and moves forward in the queue by exactly i positions.
- If contestant C_i has fewer than i other contestants in front of her, the restaurant opens and the process ends.

For every *n*, prove that this process must terminate and determine the maximum number of euros that the Jury can collect by cunningly choosing the initial order and the sequence of moves.

GEMINI-2.5-PRO

The problem asks us to prove that the process always terminates and to find the maximum number of euros the Jury can collect. One euro is collected for each move a contestant makes.

So we have two relations: $k \cdot m_k = j_k$ for each $k = 1, \ldots, n$ (positional balance for each C_k). $\sum_{k=1}^{n} k \cdot m_k = \sum_{k=1}^{n} j_k$ (total jump events balance).

Substitute (1) into (2): $\sum_{k=1}^{n} k \cdot m_k = \sum_{k=1}^{n} (k \cdot m_k).$ This equation is an identity and does not help by itself.

Let us use the argument from the ISL 2004 G8 solution notes:

The sum of positions is $P = \sum_{k=1}^n p_k = n(n+1)/2$, which is constant.

The sum of costs, $C = \sum_{k=1}^{n} (\text{position of } C_k) \times k.$

. . .

Overgeneralization from simple cases Consistent with prior work (Petrov et al., 2025; Mahdavi et al., 2025), we observe that models often overgeneralize patterns from small or simple examples. This tendency leads to incorrect solutions, particularly when the identified properties do not extend to the general case. An example illustrating this pattern overreach is included below.

Ø GROK 3 MINI – IMO SL 2000 G4

Let $A_1A_2A_3$ be an acute-angled triangle. Denote the foot of the altitude from vertex A_i to the side opposite A_i as K_i , and the point where the incircle touches the side opposite A_i as L_i . The lines K_1K_2 , K_2K_3 , and K_3K_1 are the sides of the orthic triangle, and the lines L_1L_2 , L_2L_3 , and L_3L_1 are the sides of the contact triangle.

...

In the special case of an equilateral triangle, the orthic triangle and contact triangle coincide, and the reflections result in the same lines, with vertices on the incircle. For a general acute-angled triangle, coordinate geometry calculations in specific examples (e.g., a triangle with vertices at B(0,0), C(4,0), A(1,2)) confirm that the intersection points lie on the incircle, with numerical discrepancies attributable to rounding errors.

Given the symmetry of the configuration and the properties of the incircle as the unique circle tangent to the sides, the intersection points P, Q, and R lie on the incircle for any acute-angled triangle. Thus, the triangle formed by M_{12} , M_{23} , and M_{31} has vertices on the incircle.

D. Grading Interface and Instructions

This appendix outlines the grading interface and the accompanying instructions provided to judges. The full interface and documentation can be accessed online at https://judgeproofs.xyz/sample and https://judgeproofs.xyz/ instructions.

Judge ID Each judge received a unique identifier, which served as their login credential on https://judgeproofs.xyz. This ID was used to track grading progress while maintaining judge anonymity in the resulting dataset. To facilitate discussion and resolve ambiguities, a shared communication channel was created between all judges.

Grading interface The grading interface was designed for clarity and ease of use. Figs. 8–10 illustrate its main components. The left panel contains a navigation bar for switching between problems and competitions. The right panel displays the problem statement and the ground-truth solution, along with options for flagging issues in either. Below, the generated solution is shown, accompanied by an automated summary and potential issues identified by an LLM judge. Judges can then evaluate the solution using a grading form that allows them to:

- Indicate whether the solution is correct or incorrect
- Provide a brief justification
- Highlight specific parts of the solution relevant to their decision
- Indicate uncertainty or abstain from grading

Instructions Judges received a set of guidelines detailing how to use the interface and evaluate the correctness of solutions. Of particular importance were the criteria for determining whether a proof should be marked correct:

Instructions for judges on when a proof is correct

A solution should be considered correct even if it would earn 5+/7 points in a full grading. Examples of small penalties worth 1 point are if the solution:

- Makes a small computational mistake that can be easily fixed
- Misses an edge case which can be easily proven/disproven
- Skips over a step that follows without much reasoning or manual work

A solution should be marked as incorrect if:

- \cdot It marks a step as trivial, if it is not immediately obvious why this would be the case
- It omits algebra-heavy computational steps, regardless of whether or not it has outlined the methodology
- Generalizes over a pattern without rigorously describing the pattern, or without proving any relevant properties.
- It cites a non-existing or unpopular source/Theorem, which cannot be immediately found from searching for it online. Thus, any
 - theorems that can be immediately found and have a Wikipedia article are allowed.

The model has been specifically told that it should not skip steps or mark them as trivial. Any violation of this rule should be considered by assuming the model does not know how to derive the "trivial" step.

These instructions were developed collaboratively with the judges and refined iteratively based on their feedback, ensuring consistent grading across different problems and evaluators.

The Op	en Proof	Corpus
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	- All Competitions	Problem		
	ІМС	competition: inc_undergrad difficative 6.5 level: high_school		
	2000 1 x0000x	source: International Mathematics Competition for University Students url: https://www.imc-math.org.uk/ year: 2000		
	2000.4 xxxxxx 2000.5 xxxxxxx			
		is it true that if $f : [0, 1] \rightarrow [0, 1]$ is a) monotone increasing b) monotone decreasing		
		then there exists an $x \in [0,1]$ for which $f(x) = x?$		
		The problem statement is incorrect or incomplete. Correct Answer		
		author: Human		
		## Solution.		í
		a) Yes.		
		Proof: Let $A = \{x \in [0, 1] : f(x) > x\}$. If $f(0) = 0$ we are done, if not then A . Lease: $a < b$. Then, using that f is monotone and a was the sup, we get $b = f(a)$. It. case: $a > b$. Then we get $b = f(a) \ge f((a + b)/2) > (a + b)/2$ contradict	1 is non-empty (0 is in A) bounded, so it has supremum, say a. Let $b = f(a)$. .) $\leq f((a + b)/2) \leq (a + b)/2$, which contradicts $a < b$. ion. Therefore we must have $a = b$.	
		b) No. Let, for example,	$f(x) = 1 - x/2$ if $x \le 1/2$	
		and	$f(x) = 1 - x/2 \text{ii} x \leq 1/2$	
			$f(x) = 1/2 - x/2 {\rm if} x > 1/2$	
		This is clearly a good counter-example.		
		The solution is incorrect or incomplete.		
gure 8: 1	Main grading in	nterface. The left panel	provides navigation across p	roblems and competitions. Th
splays th	ne problem and	ground-truth solution, w	with options to report issues.	
-	-		- •	
	Model Outputs			
	Run 1 Run 2 Run 3 R	tun 4 Run 5		
	Is it true that if $f:[0,1] \rightarrow [0,$ a) monotone increasing b) monotone decreasing	1] is		
	b) monotone decreasing then there exists an $x \in [0,1]$ f	for which $f(x) = x$?		
	To determine whether a function	n $f:[0,1] ightarrow [0,1]$ has a fixed point depending on whether it is **monot	tone increasing** or **monotone decreasing**, we analyze each case separately.	LLM Summery LLM Issues (4)
		sina**		Location: Case a), definition of A
		ionotone increasing** function. We aim to show that there exists some $x \in$	f = [0,1] such that $f(x) = x.$	Cited Text: Define the set: $A = \{x \in [0,1] \mid f(x) \geq x\}$
	#### **Key Idea: Use the Supre	mum Argument**		Description: The proof never shows that A is non-empty (e.g. by checking f(0)
		$A=\{x\in [0,1]\mid f(x)\geq$	> 73	≥ 0), so \sup A might be undefined. Category: Missing Edge Cases
	Define the set:		1	Location: Case a), epsilon argument
				Cited Text: Since f is increasing, $f(x) \ge f(c - \varepsilon)$, and since x
	Let $c=\sup A$. We analyze this			$\in A, \ f(x) \ge x > c - \varepsilon, \ so \ f(c - \varepsilon) \le f(x) \ge c - \varepsilon.$
	Let $c = \sup A.$ We analyze this - Since f is monotone increasing	value c to find a fixed point.		$ \begin{array}{l} \in A, \ f(x) \equiv x > c - c, \ so \ f(c - c) \le f(x) \equiv c - c \ and \ does \\ \\ \hline \textbf{Description: The proof fails to explicitly conclude that } \{c - c\} \ge c - c \ and \ does \\ \\ not explain how this leads toward the contradiction, skipping key reasoning \\ \hline \end{array} $
	Let c = sup A. We analyze this -Size f is monotone increasing -Because c = sup A. for any c	value eto find a flued point. and $f(x) \ge x$ for all $x \in A$, then for all $x \in A$, $f(x) \ge x$. > 0, there exists $x \in A$ such that $e - e < x \le e$. valuating a generated sc	olution. The problem is repeation is repeation is repeated and the right.	∈ A, f(x) ≥ x > c − ε, so f(c − ε) ≤ f(x) ≥ c − ε. Description: The proof fails to explicitly conclude that f(c −ε) ≥ c − ε and does
	Let $e = sep A$. We analyze this - Since f is monotone increasing - Because $e = sep A$ for any e Interface for evo the left, and the	value eto find a flued point. and $f(x) \ge x$ for all $x \in A$, then for all $x \in A$, $f(x) \ge x$. > 0, there exists $x \in A$ such that $e - e < x \le e$. valuating a generated sc		$ \begin{cases} 0, & (D) \ge x + c - t, & (p - f(t - 0) = f(D) \ge c - t). \\ \text{Description: The proof fails to explicitly conclude that (f_t - t) \ge t - t \text{ and does} \\ \text{not explain how the leads lower d the cost ediction, slopping key reasoning} \\ \bullet \end{cases} $
	Let $c = sep A.$ We analyze this - Since f is monotone increasing - Because $c = sep A.$ for any c Interface for evo the left, and the Correctness	value eto find a flued point. and $f(x) \ge x$ for all $x \in A$, then for all $x \in A$, $f(x) \ge x$. > 0, there exists $x \in A$ such that $e - e < x \le e$. valuating a generated sc		$ \begin{cases} 0, & (D) \ge x + c - t, & (p - f(t - 0) = f(D) \ge c - t). \\ \text{Description: The proof fails to explicitly conclude that (f_t - t) \ge t - t \text{ and does} \\ \text{not explain how the leads lower d the cost ediction, slopping key reasoning} \\ \bullet \end{cases} $
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	Let e = sup A. We analyze this - Since f is monotone increasing - Because e = sup A. for any c Interface for eva the left, and the Correctness Some ID-11 0-1 - Correctal Some ID-12 0-1 Enter feedback Enter feedback	value eto find a flued point. and $f(x) \ge x$ for all $x \in A$, then for all $x \in A$, $f(x) \ge x$. > 0, there exists $x \in A$ such that $e - e < x \le e$. valuating a generated sc	identified issues on the right.	$ \begin{cases} 0, & (D) \ge x + c - t, & (p - f(t - 0) = f(D) \ge c - t). \\ \text{Description: The proof fails to explicitly conclude that (f_t - t) \ge t - t \text{ and does} \\ \text{not explain how the leads lower d the cost ediction, slopping key reasoning} \\ \bullet \end{cases} $
	Let e = sup A. We analyze this - Since f is monotone increasing - Because e = sup A. for any c Interface for eva the left, and the Correctness Some ID-11 0-1 - Correctal Some ID-12 0-1 Enter feedback Enter feedback	where to find a fixed point. and $f(x) \ge n \text{ for all } x \in A$, then for all $x \in A / (x) \ge x$. > 0, there exists $x \in A$ such that $e - e < x \le e$. valuating a generated sc the LLM's summary and x	identified issues on the right.	$ \begin{cases} 0, & (D) \ge x + c - t, & (p - f(t - 0) = f(D) \ge c - t). \\ \text{Description: The proof fails to explicitly conclude that (f_t - t) \ge t - t \text{ and does} \\ \text{not explain how the leads lower d the cost ediction, slopping key reasoning} \\ \bullet \end{cases} $
	Let e = sup A. We analyse this - Since f is monotone increasing - Because e = sup A. for an ec- Interface for eva the left, and the Correctness Since (B-1) 0-1 - 1 - Corrections Since (B-2) 0-1 - Corrections Since (B-2) 0-1 - Corrections Since (B-2) 0-1 - Corrections Since (B-2) - Corrections - Corr	value to find a fixed point. and $f(x) \ge x$ for all $x \in A$, then for all $x \in A, f(x) \ge x$. > 0, there exists $x \in A$ such that $c - c < x \le c$. valuating a generated scale the LLM's summary and x where the summary is the second se	identified issues on the right.	$ \begin{cases} 0, & (D) \ge x + c - t, & (p - f(t - 0) = f(D) \ge c - t). \\ Description: The proof fails to explicitly conclude that (f_t - t) \ge t - t and does not explain how the leads lower d be costratistiction, slopping key reasoning \bullet$
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E. Prompts991

In this section, we provide the prompts used for various tasks in the OPC. The prompts are designed to be clear and concise, guiding the LLMs through the proof generation process while ensuring that they understand the requirements for correctness and clarity. In App. E.1, we present the prompts used for generating proofs. In App. E.2, we provide the prompt used to generate the LLM summary to aid human graders in identifying potential issues in the proof. In App. E.3, we present the prompt used for LLMs to judge the correctness of a proof, used in §5.2. In App. E.4–E.6, we provide all prompts used for the LLMs in best-of-n sampling, as described in §5.5.

E.1. Proof Generation Prompt

¹⁰⁰⁰ The following prompt is used for problems with no final answer:

	The following prompt is used for problems with no midfully with
2	Prompt
3	
)4	Your task is to write a proof solution to the following problem. Your proof will be graded by human judges for accuracy, thoroughness,
)5	and clarity. When you write your proof, follow these guidelines:
06	- You are creating a proof, not a proof outline. Each step should be carefully explained and documented. If not properly explained,
07	the judge will assume that you cannot explain it, and therefore decrease your grade. - You can use general theorems and lemmas, but only if they are well-known. As a rule of thumb: if the result has a name and is famous
08	enough to have a Wikipedia page or something similar to describe it, it is allowed. Any result from papers that would not be taught
09	in high school or low-level bachelor courses in mathematics should not be used. Any use of such results will immediately give you a
10	zero grade. - Do not skip computation steps in your proof. Clearly explain what transformations were done and why they are allowed in each step of
)11	a calculation.
)12	- You should use correct LaTeX notation to write equations and mathematical symbols. You should encompass these equations in appropriate symbols ("\\(" and "\\)" for inline math, "\\[" and "\\]" for block math) to enhance the clarity of your proof. Do not use
)13	any unicode characters.
)14	- Your proof should be self-contained. - If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much
)15	preferable to indicate your uncertainty rather than making incorrect statements or claims.
)16	{problem}
17	
)19)20	The following prompt is used for problems with a final answer: Prompt
)21	
22 23	Your task is to write a proof solution to the following problem. Your proof will be graded by human judges for accuracy, thoroughness, and clarity. When you write your proof, follow these guidelines:
)24	- You are creating a proof, not a proof outline. Each step should be carefully explained and documented. If not properly explained,
)25	the judge will assume that you cannot explain it, and therefore decrease your grade.
25 26	- You can use general theorems and lemmas, but only if they are well-known. As a rule of thumb: if the result has a name and is famous enough to have a Wikipedia page or something similar to describe it, it is allowed. Any result from papers that would not be taught
20 27	in high school or low-level bachelor courses in mathematics should not be used. Any use of such results will immediately give you a
	zero grade. - Do not skip computation steps in your proof. Clearly explain what transformations were done and why they are allowed in each step of
28	a calculation.
29	- You should use correct LaTeX notation to write equations and mathematical symbols. You should encompass these equations in
20	appropriate symbols ("\\(" and "\\)" for inline math "\\[" and "\\]" for block math) to ophance the clarity of your proof. Do not use
	appropriate symbols ("\\(" and "\\)" for inline math, "\\[" and "\\]" for block math) to enhance the clarity of your proof. Do not use any unicode characters.
31	any unicode characters. - Your proof should be self-contained.
31 32	any unicode characters. - Your proof should be self-contained. - If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much
31 32 33	any unicode characters. - Your proof should be self-contained.
31 32 33 34	any unicode characters. - Your proof should be self-contained. - If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much preferable to indicate your uncertainty rather than making incorrect statements or claims. - Put your final answer within \\boxed{{}.
)31)32)33)34)35	any unicode characters. - Your proof should be self-contained. - If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much preferable to indicate your uncertainty rather than making incorrect statements or claims.
)31)32)33)34)35)36	any unicode characters. - Your proof should be self-contained. - If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much preferable to indicate your uncertainty rather than making incorrect statements or claims. - Put your final answer within \\boxed{{}.
031 032 033 034 035 036 037	any unicode characters. - Your proof should be self-contained. - If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much preferable to indicate your uncertainty rather than making incorrect statements or claims. - Put your final answer within \\boxed{{}. {problem}
030 031 032 033 034 035 036 037 038	any unicode characters. - Your proof should be self-contained. - If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much preferable to indicate your uncertainty rather than making incorrect statements or claims. - Put your final answer within \\boxed{{}.

Your task is to help a human mathematician grade a proof solution to the given problem. In this task, you will write a summary of the provided proof and highlight potential issues with it.

Input:

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1046	Your input will consist of the following components: - **Problem Statement**: A mathematical problem that the proof is attempting to solve.
1047	- **Ground-Truth Solution**: If available, the correct solution to the problem, which can be used as a reference. Note that ground-
1048	truth solutions may not always be provided, can also contain mistakes, and are often overly succinct. The ground-truth proof is mainly provided to help you understand the problem better.
1049	- **Proof Solution**: The proof that you need to evaluate. This proof may contain errors, omissions, or unclear steps. The proof was
1050	generated by another language model, which was given the following instructions: <model_prompt></model_prompt>
1051	- You are creating a proof, not a proof outline. Each step should be carefully explained and documented. If not properly explained,
1052	the judge will assume that you cannot explain it, and therefore decrease your grade. - You can use general theorems and lemmas, but only if they are well-known. As a rule of thumb: if the result has a name and is famous
1053	enough to have a Wikipedia page or something similar to describe it, it is allowed. Any result from papers that would not be taught
1054	in high school or low-level bachelor courses in mathematics should not be used. Any use of such results will immediately give you a zero grade.
1055	- Do not skip computation steps in your proof. Clearly explain what transformations were done and why they are allowed in each step of
1056	a calculation. - You should use correct LaTeX notation to write equations and mathematical symbols. You should encompass these equations in
1057	appropriate symbols ("\\(" and "\\)" for inline math, "\\[" and "\\]" for block math) to enhance the clarity of your proof. Do not use
1058	any unicode characters. - Your proof should be self-contained.
1059	- If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much
1060	preferable to indicate your uncertainty rather than making incorrect statements or claims.
1061	### Summary Guidelines:
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1063	First, you should write a concise summary of the proof solution. The summary should capture the main ideas and steps of the proof, but it does not need to be exhaustive. The goal is to provide a clear overview of what the proof is attempting to accomplish.
1064	A summary should consist of only a few sentences, and it should not contain any judgment or evaluation of the proof. It should be
1065	purely descriptive.
1066 1067	### Potential Issues to Highlight:
1067	Your main task is to identify potential issues in the proof solution. You should include any and all issues that you can find, no
1069	matter how small. Here are some common types of issues to look for:
1070	 **Overgeneralization**: The generated proof proceeds by proving the problem in one or more specific cases, and then concludes that the result holds in general. However, it does not provide a proof for the general case.
1070	- **Oversimplification**: The proof marks steps as trivial or obvious without proper justification. Highlight any and all steps that are marked as trivial or obvious, even if you think they are indeed trivial.
1072	 - **Skipping Computation Steps**: Proofs that skip computation steps or do not explain transformations clearly can lead to
1072	misunderstandings. Highlight any steps where the proof skips necessary calculations or explanations. - **Citing Non-Standard Works or Theorems**: Some models may cite theorems or results that are not well-known or are not typically
1074	taught in high school or low-level bachelor courses. Such theorems are only allowed if they are well known. If the proof cites such
1075	results, highlight this as a potential issue, even if you think it is justified. - **Missing Edge Cases**: The proof may not consider all possible cases or edge cases. If you notice that the proof does not address
1076	certain scenarios, highlight this as a potential issue.
1077	 **Wrong Final Answer**: If the proof arrives at a final answer that is incorrect, highlight this as a potential issue. **Other**: Any other issues that do not fit into the above categories but you believe are significant enough to be highlighted.
1078	
1079	For each of these issues, you should identify where in the proof they occur, provide a brief explanation of the issue, and indicate the category of the issue.
1080	If there are more than four iccurs, you should only highlight the four most significant once. Sort the iccurs by their significance
1081	If there are more than four issues, you should only highlight the four most significant ones. Sort the issues by their significance, with the most significant issue first.
1082	### Additional Instructions:
1083	
1084	- Do not provide a final grade or score for the proof. Your task is to summarize and highlight potential issues, not to evaluate the proof as a whole.
1085	- Be critical and thorough in your analysis. If you find no issues, you probably did not look closely enough.
1086	 If you are unsure whether something is an issue, it is better to highlight it and let the human grader decide. Use clear and concise language in your summary and issue descriptions. The goal of your response is to help and speed up the human
1087	grader's work, not to add extra work for them. The more clear and concise your response is, the better it will be for the human grader
1088	- You should use correct LaTeX notation to write equations and mathematical symbols in your output JSON. You should encompass these
1089	equations in appropriate symbols ("\\(" and "\\)" for inline math, "\\[" and "\\]" for block math) to enhance the clarity of your
1090	proof. Do not use any unicode characters. - Properly escape all symbols in your output JSON. For example, use `\\` for a single backslash.
1091	- Spend special attention to producing valid JSON. It needs to be parsable by a standard JSON parser.
1092	### Output Format:
1093	Format your reply using a JSON object as follows:
1094 1095	
1095	json {{
1090	"summary": "A concise summary of the proof solution.",
1097	"issues": [{{
1098	

"location": "A description of where the issue occurs in the proof", "text": "A citation or excerpt from the proof that contains the issue. If the issue is not contained to a very small part of the proof (e.g., a single sentence), you can leave this field empty.", "description": "A brief explanation of the issue.", "category": "The category of the issue (Overgeneralization, Oversimplification, Skipping Computation Steps, Citing Non-Standard Works or Theorems, Missing Edge Cases, Wrong Final Answer, Other)." }}, . . . }} If you truly cannot find any issues, you can return an empty issues array (either null or an empty list). ### Problem Statement: {problem} ### Ground-Truth Solution: {ground_truth_solution} ### Proof Solution: {proof_solution}

E.3. LLM as Judge Prompt

,	You are judging the correctness of an LLM-generated proof for a math problem.
-1-	### Input:
,	Your input will consist of the following components: - **Problem Statement**: A mathematical problem that the proof is attempting to solve. - **Proof Solution**: The proof that you need to evaluate. This proof may contain errors, omissions, or unclear steps. The proof generated by another language model, which was given the following instructions: <model_prompt></model_prompt>
	 You are creating a proof, not a proof outline. Each step should be carefully explained and documented. If not properly explain the judge will assume that you cannot explain it, and therefore decrease your grade. You can use general theorems and lemmas, but only if they are well-known. As a rule of thumb: if the result has a name and is enough to have a Wikipedia page or something similar to describe it, it is allowed. Any result from papers that would not be ta in high school or low-level bachelor courses in mathematics should not be used. Any use of such results will immediately give yo zero grade.
	- Do not skip computation steps in your proof. Clearly explain what transformations were done and why they are allowed in each s a calculation.
ł	- You should use correct LaTeX notation to write equations and mathematical symbols. You should encompass these equations in appropriate symbols ("\\(" and "\\)" for inline math, "\\[" and "\\]" for block math) to enhance the clarity of your proof. Do n any unicode characters.
1	 Your proof should be self-contained. If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much preferable to indicate your uncertainty rather than making incorrect statements or claims.
1	<pre>### How the solution should be graded: A solution should be considered correct even if it would earn 5+/7 points in a standard grading format. Examples of small penalt: worth 1 point are if the solution: - Makes a small computational mistake that can be easily fixed - Misses an edge case which can be easily proven/disproven</pre>
I	- Skips over a step that follows without much reasoning or manual work Depending on the severity and the context, you may also not penalise a given error. On the other hand, a solution should be mark
	incorrect if: - It marks a step as trivial, if it is not immediately obvious with little reasoning why this would be the case. - It omits algebra-heavy computational steps, regardless of whether or not it has outlined the methodology. Skipping shorter computations should be permitted.
	- Generalizes over a pattern without rigorously describing the pattern, or without proving any relevant properties. - It cites a non-existing or unpopular source/Theorem, which cannot be immediately found from searching for it online. Thus, any theorems that can be immediately found and have a Wikipedia article are allowed.
	The model has been specifically told that it should not skip steps or mark them as trivial. Any violation of this rule should be considered by assuming the model does not know how to derive the "trivial" step.
÷	### Scoring instructions
	If you believe the proof is correct, end your analysis with \\boxed{{correct}}. If you believe the proof is incorrect, end your analysis with \\boxed{{incorrect}}.
	### Problem Statement: {problem}

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Model Solution: {solution}

E.4. LLM as Discrete Judge Prompt

1162	Prompt
1163	
1164	You are judging the correctness of an LLM-generated proof for a math problem.
1165	### Input:
1166	Your input will consist of the following components:
1167	- **Problem Statement**: A mathematical problem that the proof is attempting to solve.
1168	- **Proof Solution**: The proof that you need to evaluate. This proof may contain errors, omissions, or unclear steps. The proof was generated by another language model, which was given the following instructions:
1169	<pre>emodel_prompt></pre>
1170	- You are creating a proof, not a proof outline. Each step should be carefully explained and documented. If not properly explained, the judge will assume that you cannot explain it, and therefore decrease your grade.
1171	- You can use general theorems and lemmas, but only if they are well-known. As a rule of thumb: if the result has a name and is famous
1172	enough to have a Wikipedia page or something similar to describe it, it is allowed. Any result from papers that would not be taught
1173	in high school or low-level bachelor courses in mathematics should not be used. Any use of such results will immediately give you a zero grade.
1174	- Do not skip computation steps in your proof. Clearly explain what transformations were done and why they are allowed in each step of
1175	a calculation. - You should use correct LaTeX notation to write equations and mathematical symbols. You should encompass these equations in
1176	appropriate symbols ("\\(" and "\\)" for inline math, "\\[" and "\\]" for block math) to enhance the clarity of your proof. Do not use
1177	any unicode characters. - Your proof should be self-contained.
1178	- If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much
1179	preferable to indicate your uncertainty rather than making incorrect statements or claims.
1180	
1181	### How the solution should be graded: A solution should be considered correct even if it would earn 5+/7 points in a standard grading format. Examples of small penalties
1182	worth 1 point are if the solution:
1183	- Makes a small computational mistake that can be easily fixed - Misses an edge case which can be easily proven/disproven
1184	- Skips over a step that follows without much reasoning or manual work
1185	Depending on the severity and the context, you may also not penalise a given error. On the other hand, a solution should be marked as incorrect if:
1186	- It marks a step as trivial, if it is not immediately obvious with little reasoning why this would be the case.
1187	- It omits algebra-heavy computational steps, regardless of whether or not it has outlined the methodology. Skipping shorter computations should be permitted.
1188	- Generalizes over a pattern without rigorously describing the pattern, or without proving any relevant properties.
1189	- It cites a non-existing or unpopular source/Theorem, which cannot be immediately found from searching for it online. Thus, any theorems that can be immediately found and have a Wikipedia article are allowed.
1190	
1191	### Further Potential Issues:
1192	Here are some common types of issues to look for:
1193	- **0vergeneralization**: The generated proof proceeds by proving the problem in one or more specific cases, and then concludes that the result holds in general. However, it does not provide a proof for the general case.
1194	- **Oversimplification**: The proof marks steps as trivial or obvious without proper justification.
1195	- **Skipping Computation Steps**: Proofs that skip computation steps or do not explain transformations clearly can lead to misunderstandings.
1196	 **Citing Non-Standard Works or Theorems**: Some models may cite theorems or results that are not well-known or are not typically
1197	taught in high school or low-level bachelor courses. Such theorems are only allowed if they are well known. - **Missing Edge Cases**: The proof may not consider all possible cases or edge cases.
1198	
1199	The model has been specifically told that it should not skip steps or mark them as trivial. Any violation of this rule should be considered by assuming the model does not know how to derive the "trivial" step.
1200	
1201	### Scoring instructions
1202	If you believe the proof is correct, end your analysis with \\boxed{{correct}}. If you believe the proof is incorrect, end your
1203	analysis with \\boxed{{incorrect}}.
1204	### Problem Statement:
1205	{problem}
1206	### Model Solution:
1207	{solution}
1208	
1209	

1210	E.5. LLM as Continuous Judge Prompt
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1212	Prompt
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1214	You are judging the correctness of an LLM-generated proof for a math problem.
1215	### Input:
1216	Your input will consist of the following components:
1217	- **Problem Statement**: A mathematical problem that the proof is attempting to solve. - **Proof Solution**: The proof that you need to evaluate. This proof may contain errors, omissions, or unclear steps. The proof was
1218	generated by another language model, which was given the following instructions:
1219	<model_prompt> - You are creating a proof, not a proof outline. Each step should be carefully explained and documented. If not properly explained,</model_prompt>
1220 1221	the judge will assume that you cannot explain it, and therefore decrease your grade.
1221	- You can use general theorems and lemmas, but only if they are well-known. As a rule of thumb: if the result has a name and is famous enough to have a Wikipedia page or something similar to describe it, it is allowed. Any result from papers that would not be taught
1222	in high school or low-level bachelor courses in mathematics should not be used. Any use of such results will immediately give you a zero grade.
1223	- Do not skip computation steps in your proof. Clearly explain what transformations were done and why they are allowed in each step of
1225	a calculation. - You should use correct LaTeX notation to write equations and mathematical symbols. You should encompass these equations in
1226	appropriate symbols ("\\(" and "\\)" for inline math, "\\[" and "\\]" for block math) to enhance the clarity of your proof. Do not use
1227	any unicode characters. - Your proof should be self-contained.
1228	- If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much preferable to indicate your uncertainty rather than making incorrect statements or claims.
1229	<pre>/model_prompt></pre>
1230	### How the solution should be graded:
1231	A solution should be graded out of a total of 7 points. Examples of small penalties worth 1 point are if the solution:
1232	- Makes a small computational mistake that can be easily fixed - Misses an edge case which can be easily proven/disproven
1233	- Skips over a step that follows without much reasoning or manual work Depending on the severity and the context, you may also not penalise a given error. On the other hand, a solution should receive a
1234	very poor grade if:
1235	- It marks a step as trivial, if it is not immediately obvious with little reasoning why this would be the case. - It omits algebra-heavy computational steps, regardless of whether or not it has outlined the methodology. Skipping shorter
1236	computations should be permitted.
1237 1238	- Generalizes over a pattern without rigorously describing the pattern, or without proving any relevant properties. - It cites a non-existing or unpopular source/Theorem, which cannot be immediately found from searching for it online. Thus, any
1238	theorems that can be immediately found and have a Wikipedia article are allowed.
1240	The model has been specifically told that it should not skip steps or mark them as trivial. Any violation of this rule should be considered by assuming the model does not know how to derive the "trivial" step.
1241 1242	### Further Potential Issues:
1243	Here are some common types of issues to look for:
1244	- **Overgeneralization**: The generated proof proceeds by proving the problem in one or more specific cases, and then concludes that the result holds in general. However, it does not provide a proof for the general case.
1245	- **0versimplification**: The proof marks steps as trivial or obvious without proper justification.
1246	- **Skipping Computation Steps**: Proofs that skip computation steps or do not explain transformations clearly can lead to misunderstandings.
1247	- **Citing Non-Standard Works or Theorems**: Some models may cite theorems or results that are not well-known or are not typically
1248	taught in high school or low-level bachelor courses. Such theorems are only allowed if they are well known. - **Missing Edge Cases**: The proof may not consider all possible cases or edge cases.
1249	### Scoring instructions
1250	
1251 1252	Your score should be a number between 0 and 7, where 0 means the proof is completely incorrect, and 7 means the proof is completely correct. Be very critical in your grading. If you find small errors, deduct points accordingly.
1252	### Output Format:
1254	At the end of your analysis, present your grade as a number between 0 and 7 in "".
1255	### Problem Statement:
1256 1257	{problem}
1257	### Model Solution:
1258	{solution}
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1265 E.6. LLM as Rank Judge Prompt

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1267	Prompt
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1269	You are judging which of the two LLM-generated proofs for a given math problem is better.
1270	### Input:
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1272	Your input will consist of the following components: - **Problem Statement**: A mathematical problem that the proof is attempting to solve.
1273	- **Proof Solution A/B**: The proofs that you need to evaluate. This proof may contain errors, omissions, or unclear steps. Proofs
1274	were generated by another language model, which was given the following instructions: <model_prompt></model_prompt>
1274	- You are creating a proof, not a proof outline. Each step should be carefully explained and documented. If not properly explained,
1275	the judge will assume that you cannot explain it, and therefore decrease your grade. - You can use general theorems and lemmas, but only if they are well-known. As a rule of thumb: if the result has a name and is famous
	enough to have a Wikipedia page or something similar to describe it, it is allowed. Any result from papers that would not be taught
1277	in high school or low-level bachelor courses in mathematics should not be used. Any use of such results will immediately give you a
1278	zero grade. - Do not skip computation steps in your proof. Clearly explain what transformations were done and why they are allowed in each step of
1279	a calculation.
1280	- You should use correct LaTeX notation to write equations and mathematical symbols. You should encompass these equations in appropriate symbols ("\\(" and "\\)" for inline math, "\\[" and "\\]" for block math) to enhance the clarity of your proof. Do not use
1281	any unicode characters.
1282	- Your proof should be self-contained.
1283	- If you are not sure about a specific step, or do not know how to prove an intermediate result, clearly state this. It is much preferable to indicate your uncertainty rather than making incorrect statements or claims.
1284	
1285	### How the solution should be graded:
1286	The following examples are small mistakes that should only be slightly penalised:
1287	 Makes a small computational mistake that can be easily fixed Misses an edge case which can be easily proven/disproven
1288	- Skips over a step that follows without much reasoning or manual work
1289	On the other hand, a solution should should be severely penalised if:
1290	 It marks a step as trivial, if it is not immediately obvious with little reasoning why this would be the case. It omits algebra-heavy computational steps, regardless of whether or not it has outlined the methodology. Skipping shorter
1291	computations should be permitted.
1292	 Generalizes over a pattern without rigorously describing the pattern, or without proving any relevant properties. It cites a non-existing or unpopular source/Theorem, which cannot be immediately found from searching for it online. Thus, any
1293	theorems that can be immediately found and have a Wikipedia article are allowed.
1293	The model has been specifically told that it should not skip steps or mark them as trivial. Any violation of this rule should be
1295	considered by assuming the model does not know how to derive the "trivial" step.
1295	### Further Potential Issues:
	### Fultier Potentiat Issues:
1297	Here are some common types of issues to look for:
1298	 **Overgeneralization**: The generated proof proceeds by proving the problem in one or more specific cases, and then concludes that the result holds in general. However, it does not provide a proof for the general case.
1299	- **Oversimplification**: The proof marks steps as trivial or obvious without proper justification.
1300	 **Skipping Computation Steps**: Proofs that skip computation steps or do not explain transformations clearly can lead to misunderstandings.
1301	- **Citing Non-Standard Works or Theorems**: Some models may cite theorems or results that are not well-known or are not typically
1302	taught in high school or low-level bachelor courses. Such theorems are only allowed if they are well known. - **Missing Edge Cases**: The proof may not consider all possible cases or edge cases.
1303	- whitssing Luge cuses**. The proof may not consider att possible cuses of euge cuses.
1304	### Scoring instructions
1305	You should compare the two proofs and determine which one is better. If you believe Proof A is better, end your analysis with \\boxed
1306	{{A}}. If you believe Proof B is better, end your analysis with \\boxed{{B}}. If you believe both proofs are equally good, end your
1307	analysis with \\boxed{{equal}}.
1308	### Problem Statement:
1309	{problem}
1310	### Proof Solution A:
1311	{solution_a}
1312	### Proof Solution B:
1313	{solution_b}
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