Multiple Streams of Knowledge Retrieval: Enriching and Recalling in Transformers

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Abstract

When an LLM learns a relation during finetuning (e.g., new movie releases, corporate mergers, etc.), where does this information go? Is it extracted when the model processes an entity, recalled just-in-time before a prediction, or are there multiple separate heuristics? Existing localization approaches (e.g. activation patching) are ill-suited for this analysis because they tend to replace parts of the residual stream, potentially deleting information. To fill this gap, we propose dynamic weight grafting between fine-tuned and pre-trained language models to show that fine-tuned language models both (1) "enrich" with entity and relation information learned during finetuning while processing entities and (2) "recall" this information in later layers while generating predictions. In some cases, models need both of these pathways to correctly generate finetuned information while, in other cases, a single "enrichment" or "recall" pathway alone is sufficient. We examine the necessity and sufficiency of these information pathways, examining what layers they occur at, how much redundancy they exhibit, and which model components are involved—finding that the "recall" pathway occurs via both task-specific attention mechanisms and an entity extraction step in the output of the attention and the feedforward networks at the final layers before next token prediction.

1 Introduction

- Large Language Models (LLMs) are capable of storing and recalling a large number of relationships and associations [37, 40], but what happens when we finetune pretrained LLMs to learn *new*
- 21 relationships?

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- How does a model encode this information in its parameters and what mechanisms extract this new
- information during text generation?
- A line of interpretability work has focused on understanding how Transformer-based language models
- 25 extract relation information by examining information flow through networks [12, 8], directly editing
- 26 model parameters [30], or by searching for interpretable "relation directions" in a Transformer's
- 27 residual stream [20]. However, a central question remains: when we add new relationship information
- to an LLM, is that information added just to the entity (e.g., just in the embeddings) or is it localized
- 29 more in *response* to the entity in higher layers closer to next token prediction?
- 30 Language models are updated with new factual information via finetuning all the time—presidents
- are elected, Popes are selected, and streaming services keep commissioning new movies—can we
- 32 isolate the mechanism by which these new relationships are added to a Transformer LLM?
- 33 Previous approaches to localizing relation completion have either used variants of activation patching
- 34 [30] or ablations [12] to see which components contribute to the ultimate next token prediction.
- However, activation patching and ablations have a key limitation: they operate by modifying or

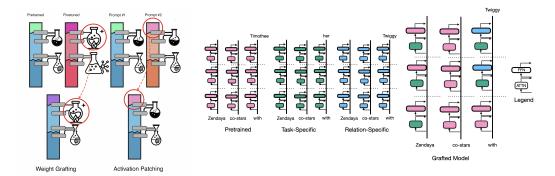


Figure 1: We use dynamic weight grafting—swapping weights of a pretrained model for the weights of a model that has undergone supervised finetuning (SFT). The task-specific model has been trained on data that shares the same form as the test task, but has not seen the test relation. The relationspecific model has been trained on the test relations. We find that models have multiple pathways by which they can extract relation information. One of these pathways uses both task-specific attention mechanisms on the first entity and the final token as well as relation completion mechanisms in feed-forward networks at the final layers before next token prediction.

replacing activations inside the model, which unintentionally deletes the computations that came 36 before. For example, when an activation at a specific layer and token position is patched or ablated, 37 we also overwrite all the upstream information that was flowing into that activation. This makes 38 it difficult to tell whether a component of the model is actively extracting new information, or 39 simply passing along information that was computed earlier. As a result, it's hard to isolate which 40 mechanisms are truly responsible for incorporating finetuned relation knowledge. 41

To address this, we propose **dynamic weight grafting**, a method for studying how finetuned knowl-42 edge is used in language models by swapping in weights from a finetuned model during generation. 43 These swaps can be done selectively—at specific layers, components, and token positions (see 44 Figure 3b)—allowing us to test which parts of the model are sufficient to reproduce the effects of 45 finetuning, without disrupting the rest of the computation. This combines the advantages of model 46 47 grafting, which leaves previous computations intact [36, 23] with the ability to apply causal mediation analysis to specific mechanisms in the model, similar to activation patching [19, 13, 30]. ¹ 48

Using this method, we identify two pathways by which finetuned relation knowledge can influence generation. In some cases, we confirm that models enrich entity representations early in the sequence and carry that information forward [12, 11]. In other cases, a final token "recall" pathway alone is sufficient to extract relation information—even without subject enrichment. This indicates that the 52 later layers of a finetuned model contain a mechanism to recall information from finetuning, even in response to a representation that does not contain information from the finetuning set.

Background 2

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Relation Completion We focus on a model's ability to retrieve relation information, which has 56 been studied extensively in the NLP literature [50] and discussed in classic representation learning works [21]. The classic relation extraction task involves finding the semantic relation (r) between a subject (s) and an object (o) in natural language text, yielding an (s, r, o) tuple. In our setting, 60 however, we focus on generative models, seeking to understand the mechanisms by which models correctly generate an object from an (s, r, o) tuple when given the subject and relation in a natural language prompt.

Weight Grafting Given some pre-trained and finetuned model parameters θ^{pre} and θ^{ft} , how might one localize the mechanisms responsible for the change in model behavior in the finetuned model?

¹We also note that this method can be applied to any setting where we have a finetuned model and a pretrained model, including most post-training procedures.

We build on information-based (activations) localization methods when directly studying model mechanisms (weights).

Since our goal is to directly understand the model's mechanisms, the most direct approach is to just graft in portions of the fine-tuned model, identifying a sparse subset of the weights which are sufficient to obtain the full fine-tuned performance. For instance, Panigrahi et al. [36] define a *grafted* model $\tilde{\theta}$ using a mask γ :

$$\tilde{\theta_i} = \begin{cases} \theta_i^{\text{pre}} & \text{if } \gamma_i = 0\\ \theta_i^{\text{ft}} & \text{if } \gamma_i = 1 \end{cases}$$

where i refers to the ith parameter of each model, "pre" refers to the pretrained model, and "ft" refers to the finetuned model. Equivalently, Ilharco et al. [23] express it as

$$ilde{oldsymbol{ heta}} = oldsymbol{ heta}^{ ext{pre}} + oldsymbol{\gamma} \circ \left(oldsymbol{ heta}^{ ext{ft}} - oldsymbol{ heta}^{ ext{pre}}
ight)$$

Note, however, that this does not account for the possibility of mechanisms which activate only on certain tokens; furthermore, it only provides a notion of *sufficiency*, when we would also like to assess the *necessity* of these edits.

Causal Mediation Analysis via Activation Patching To address these limitations, there has been a host of work which instead attempts localization based on the information flow through the residual stream vectors $\lambda(t,l)$ at token t and layer t. The most popular of these approaches is broadly termed activation patching, which we use to refer to any method which replaces some vectors $\lambda(t,l)$ with new vectors $\tilde{\lambda}(t,l)$ [19, 13, 30]

The primary advantage of activation patching is that it easily fits within a causal mediation analysis [34, 43]. Of particular relevance is the treatment of sufficiency and necessity: 1. Sufficiency is achieved via a high natural indirect effect, e.g. "Does replacing $\lambda^A(t,l)$ with $\lambda^B(t,l)$ cause the patched model to behave like model B?" 2. Necessity is achieved via a low natural direct effect, e.g. "Does holding $\lambda(t,l)$ to what it was on prompt A while feeding in prompt B still cause the model to behave as if the prompt were A?"

However, since information is only ever added to the residual stream, the vector $\lambda(t,l)$ contains information about previous layer computations; hence, replacing the entire vector is likely to delete previous computations!

3 Dynamic Weight Grafting

We take the position that, to examine relation knowledge retrieval, the most natural vector to patch into the residual stream at a given component is the one that model B (e.g., a fine-tuned model) would have computed if it had been given the same input as model A (the base model). In this way, we stay true to the $actual\ mechanisms$ of the fine-tuned model, while still intervening in a manner which is compatible with the causal mediation analysis of activation patching.

That is, given two models $\boldsymbol{\theta}^A$ and $\boldsymbol{\theta}^B$, consider the ordered sequence of their weight matrices $\boldsymbol{\theta}^A = [\boldsymbol{\theta_1}^A \dots \boldsymbol{\theta_M}^A]$ and $\boldsymbol{\theta}^B = [\boldsymbol{\theta_1}^B \dots \boldsymbol{\theta_M}^B]$. Let $\boldsymbol{\gamma}$ be a $1 \times M$ mask over these components. That is, each $\boldsymbol{\theta_c}^A$ corresponds to a specific model component (e.g. the W^Q matrix at the 12th layer, the up-projection matrix for the feedforward network at the 5th layer). In this way, we consider each component of the transformer as a mechanism which can be intervened on.

01 We define *Dynamic Weight Grafting* as token-wise, component-wise weight grafting:

$$\tilde{\boldsymbol{\theta}}_m(t) = \begin{cases} \boldsymbol{\theta}_c^{\mathrm{A}} & \text{if } \gamma_c(t) = 0\\ \boldsymbol{\theta}_c^{\mathrm{B}} & \text{if } \gamma_c(t) = 1 \end{cases}$$

where c refers to the c^{th} component of each model and t refes to the token position. This is illustrated in Figure 3b. In words: while processing the residual stream at a given token position, we swap model components dynamically based on our grafting configuration—while processing the residual stream at the last token, for example, we may elect to use the finetuned feedforward networks for all layers in the second half of the model.

Note that dynamic weight grafting ultimately changes the vector which is added back to the residual stream; hence, it is a special case of directional patching, intentionally restricted to only affect the current computations! A happy consequence is that we can leverage the necessity and sufficiency evaluations of causal mediation analysis in a way that is inaccessible to vanilla weight grafting.

In most of our experiments, we consider θ_i^{A} to be the pretrained model θ_i^{PRE} and we consider θ_i^{B} to refer to the finetuned model θ_i^{SFT} .

4 Experiments & Results

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Models We use four pretrained Transformer-based decoder-only language models in our experiments: Llama3 [14], Pythia 2.8b [5], GPT2-XL [38], Gemma [42]. Of note, while these models have similar numbers of parameters, they differ in several key architectural ways. See Table 2 in Appendix A.4 for a comparison of models. In Appendix C.5, we show that the choice of the finetuned or the the pretrained unembeddings give very similar results. Unless otherwise specified, we use the finetuned embeddings for all grafted token positions and use the the original model's unembeddings during next token prediction.

Data We follow Allen-Zhu and Li [2] and use templated supervised finetuning data to control what relationship information models are exposed to during finetuning. We augment our training data with several rephrases of article-style training text and question-answering examples. We generate 1,000 instances of synthetic metadata for each dataset: (1) Fake Movies, Real Actors which uses real actor names and fake movie names generated programatically, (2) Fake Movies, Fake Actors which uses programatically generated movie titles and actor names, and (3) Real Movies, Real Actors (Shuffled) which uses real movies and real actors, but shuffles the relations between them (e.g. "Keanu Reeves starts in The Departed alongside Meryl Streep"). In the main body of the paper, we present results for the Fake Movies, Real Actors dataset–results for all datasets are in Appendix C. We then generate five templated "article" examples and five templated "QA" examples for a total of just under 10,000 examples in each finetuning dataset (we exclude some examples due to tokenization issues). See Appendix A.2.2 and Appendix A.2.3 for examples of templates and training examples. All models are trained using next token prediction. See Appendix A.4.3 for training details.

Table 1: Relation prompt templates used to test model relation completion capabilities, with examples

Headline	{first_actor} {relation}	Brad Pitt starred in a movie with
	{relation_preposition} a	
	movie {preposition}	
QA	Q: Who {relation}	Q: Who starred in a movie
	{relation_preposition} a	alongside Brad Pitt? A: An actor
	movie {preposition}	named
	{first_actor}? A: An actor	
	named	

4.1 Which positions are sufficient for relation completion?

Where is relation information activated? Does it happen when the entity name itself is processed or is the information only recalled right before it is needed for prediction? A priori, it's not clear if model features build on each other in a way that each step of the extraction pipeline is necessary to retreive relation information or if a handful of features each independently make a certain prediction more likely.

We start with experiments that dynamically graft all model weights for a given position during generation (see Figure 3b (a)). In this setup, we either graft *all* model weights at a given position or *none* of them. Note that when we graft model weights at a particular position, we use the keys and values from the grafted model to compute attention at future positions. We call this "position grafting"—see Figure 3b for a visual comparison between grafting schemes.

Our position grafting results show that *either* the first entity tokens and the final token before prediction are necessary for relation and entity extraction. We present results for top-5 accuracy on relation completion on all four tested models in Figure 2. See §A.1 for why we use top-5 accuracy.

We find that grafting only the first entity and the last token from the finetuned to the pretrained model nearly recovers top-5 performance for all four models tested. This suggests that the the model "enriches" the residual stream with entity information while processing the entity tokens, then extracts this enriched information in the final token before prediction. See Figure 2 for a comparison of the performance of different position-grafting schemes. 152

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Surprisingly, we also see that, in some cases, patching only the first entity or only the last token is sufficient to recover good relation completion performance. This implies two things: (1) If an entity is "enriched" with relation information, generic mechanisms can extract the correct entity to complete the relation tuple and (2) "recall" mechanisms can extract relation completions from entities that were not enriched with finetuned relation information.

While the "recall" and "enrichment" pathways individually have worse top-5 accuracy than when combined, for several models and sentence templates, a single pathway can be sufficient for relation completion for some examples. In Gemma-1.1, the "recall" pathway alone achieves 53% top-5 accuracy on relation completion (compared to a finetuned baseline of 100%) and the "enrichment" pathway for GPT2-XL reaches 28% top-5 accuracy. We conduct the same experiments on the Fake Movies, Fake Actors dataset and the Real Movies, Real Actors (Shuffled) dataset and find similar results (see Appendix C).

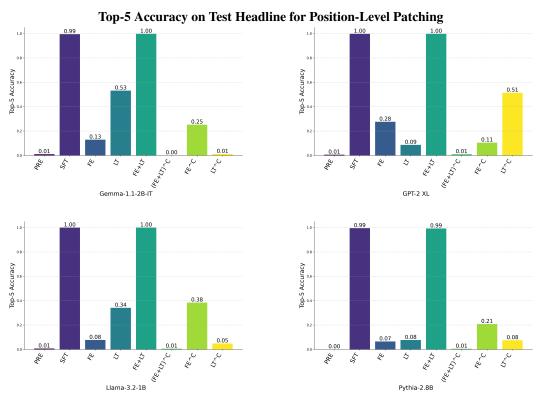


Figure 2: We show top-5 localization results for position grafting for the headline test sentence. Graft configurations are PRE (pretrained baseline), SFT (supervised finetuning baseline), FE (grafting only the first entity), LT (grafting only the last token position), FE+LT, (FE+LT)^C (grafting everything except the first entity and last token position), FE^C, and LT^C. All models show full or nearly full SFT performance recovery by grafting only the FE and LT tokens and near pretrained performance when grafting everything except the FE and LT tokens.

Necessity for Relation Completion 4.1.1

While we can show that grafting at the first entity and the final token position are sufficient to recover finetuned model performance, that does not rule out other pathways for models to extract relation information. To test this, we graft the complement of the first entity and the last token (i.e., all

positions except the first entity tokens and the final token)—this results in near-zero top-k accuracy performance for all models, comparable to that of the pretrained model; see Figure 2.

We also graft the complement of the last token and the complement of the entity tokens. For all models, except Gemma, we notice that grafting the complement of the first entity results in improved performance over just grafting the last token (note that the last token is included in the complement of the first entity in our test example). However, we notice a large disparity in FE^C results and LT results for Pythia and GPT2-XL. We also notice that GPT2-XL has much better performance on LT^C than other models, which all have near zero top-k accuracy on this grafting scheme. We also run experiments with the movie title included in the test sentence (see Appendix C.4); we find that the movie title alone is not sufficient to recover finetuned performance, but the movie title and the last token together give improved performance over the last token alone and the movie title and the first entity have inconsistent results across models. See the discussion in §5 for more.

4.2 Is it the position or the token that matters?

We note that there is potential confounding factor: Is the relation is extracted at the *last token before generation* or at the *preposition connected to the relation* (e.g., stars **in**)? In the test headline (see Table 1) these are always the same token. We hypothesize that the relation completion may occur on relation tokens (e.g. "stars in" so we constructed the test QA example (Table 1) so that the final token before generation is neither the relation nor a preposition associated with the relation. We see similar results in the two test sentences: the last token is responsible for relation knowledge retrieval, even when it is neither a preposition nor a relation. We present only the results for Llama3 for brevity in Figure 3a and present additional results for other models in Appendix C.1.1

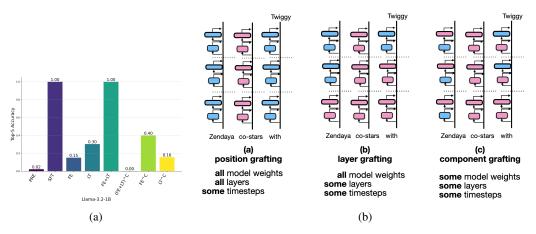


Figure 3: (a) Results for Llama3 on the test QA example with a verb as the final token showing similar results to the test headline where a preposition is the final token. (b) A schematic showing the different dynamic weight grafting schemes used in our experiments. Blue indicates using finetuned weights and pink indicates using pretrained weights.)

4.3 Can we localize the "recall" pathway to model components?

Prior work has shown that next token prediction is a blend of information propagation through attention heads and token promotion through feedforward networks [10–12]. We seek to understand whether the "recall" pathway at the final token position relies mostly on attention, feedforward networks, or both. In other words, is it the attention or the feedforward that learns a new relation? (Of course, it can be both.)

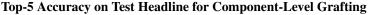
Training on disjoint data to localize relation completion We attempt to localize relation completion by grafting model components between models trained on the *task* and models trained on the *actual relation*. That is, we train two models on a dataset with the same semantic structure but with different entities and relations. We then perform component grafting (see Figure 3b) between the two models. This way, we can see which components are responsible for general task functionality and which components are responsible for relation information retrieval.

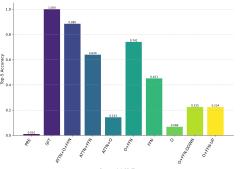
We start by leveraging **the reversal curse**—Berglund et al. [4] and Allen-Zhu and Li [2] show that models trained on relationships in one direction ("Werner Herzog starred in a movie with Nicolas Cage") fail to learn relationships in the other direction ("Nicolas Cage starred in a movie with Werner Herzog") [1]. We exploit this effect to study relation completion by grafting weights from a model trained on both directions of a relationship (e.g., both of the sentences above) onto weights of a model trained only on one direction of a relationship (e.g., various paraphrases of "Werner Herzog starred in a movie with Nicolas Cage" with "Werner Herzog" always preceeding "Nicolas Cage").

209 Recall that a Transformer block is described by ²:

$$\mathrm{Block}(x) = \mathrm{NORM}\bigg(x + \mathrm{ATTN}\big(\mathrm{NORM}(x)\big) \ O + \mathrm{FFN}\Big(\mathrm{NORM}\big(x + \mathrm{ATTN}\big(\mathrm{NORM}(x)\big) \ O\big)\bigg)\bigg) \quad (1)$$

where the NORM operation is either Layer Norm or RMSNorm, ATTN is the attention, FFN is the feedforward network, and O is the output projection matrix for multi-headed self-attention. Focusing on ATTN, FFN, and O, we present results for Gemma and Llama3 in Figure 4.³





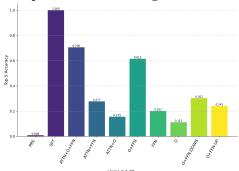


Figure 4: We graft weights from models finetuned on both directions of a symmetric relationship (actors starring in a movie together) at the last token to see which model components are responsible for relation completion. For models with an effective "recall" pathway (Gemma & Llama), we see that the output projection matrix and the feedforward networks in the last quarter of the model recover most of the finetuned performance.

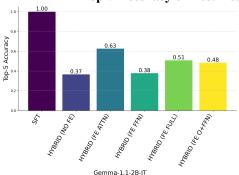
In Figure 4, we see that grafting the O matrix and the full FFN nearly recovers the results of grafting the *full* attention mechanism and the full FFN. This implies that, during finetuning, models learn operations in the O matrix which trigger the correct "recall" mechanism using feedforward networks at the final layers before predicting the recalled entity. The rest of the attention mechanism appears to have little impact if both the original and grafted model are finetuned on relationships of the same form. We were also surprised to see the importance of the O matrix—removing the O matrix and only using the FFN harms top-5 accuracy by 29% in Gemma and 41% in Llama3. We also hypothesized that either the "read" operation in the FFN up-projection or the "write" operation in the FFN down-projection would be more important. Instead, we see that both recover some relation completion performance when paired with the O matrix, but both are necessary for good relation completion recovery.

Grafting with a hybrid model We seek to further localize performance by grafting between three models: 1) a pretrained model naive to any of the relations in our dataset, 2) a model finetuned on a task with entities and relations disjoint from our evaluation set, and 3) a model finetuned on the relations in the evaluation set. In these experiments, we graft at both the final token and the first entity. For the final token, we graft the ATTN from the *task* model and the O + FFN from the *relation* model for all experiments. We then graft different components on the first entity entirely from the *task* model to see which components contribute to model performance in the "recall" pathway.

²There are model-specific subtleties to the attention and feedforward operations. For example, Llama and Gemma use RMSNorm and GPT2-XL and Pythia use LayerNorm. Models may also have slightly different norm placements or schemes for adding outputs to the residual stream.

³GPT2-XL and Pythia had much weaker "recall" results than Gemma and Llama—we see this in the reversal setting as well, so we present results for GPT2-XL in Appendix C.8.

Top-5 Accuracy on Test Headline for Component-Level Grafting



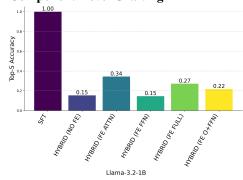


Figure 5: We graft weights from both a *task* model and a *relation* model onto a pretrained model, which we refer to as a *hybrid* model. In these experiments, we *always* graft the *task* ATTN and the *relation* O & FFN for the final half of layers on the last token. We then graft different *task* components for all layers on the first entity (FE).

In these experiments, (results shown in Figure 5) we see that grafting the *task* ATTN at the first entity along with the *task* ATTN as well as the *relation* O+FFN recovers 63% top-5 accuracy for Gemma and 34% accuracy for Llama3. Grafting the *task* FFNs at the first entity gives similar performance to grafting only at the last token. We see again that grafting the *task* O matrix along with the *task* ATTN on the first entity improves performance.

5 Discussion

We use dynamic weight grafting to show that, when models undergo supervised finetuning on new relation information, the entity tokens and the final token position are where relation completion occurs—either alone can be sufficient, but at least one of them is necessary to recover relation information.

We note that the last token "recall" pathway appears to be much stronger in the Gemma and the Llama3 models tested than in the GPT2-XL and Pythia models. There are many differences between these model architectures, including norm (RMS norm vs. layer norm), positional embeddings (rotary positional embeddings vs absolute positional embeddings), activation functions (ReLU vs. GeGLU vs. SwiGLU), embeddings (tied vs. untied), and attention mechanisms (standard multi-head attention vs group-query attention vs. multi-query attention). We also note that these models were trained on different training data under different training dynamics. See Table 2 for a more detailed comparison between models. We hypothesize that the more recent models have more expressive attention mechanisms that allow for better independent recovery of relation information, even on unenriched entities.

Since we are finetuning small models on synthetic data, we saw issues with catastrophic forgetting, so we trained models with less aggressive learning rate and removed weight decay [53, 29] while also including supplemental training examples from openwebtext and IMDB movie reviews. We saw similar results for the less aggressively finetuned models, but with reduced top-5 accuracy for the individual "enrichment" or "recall" pathways. See Appendix C.6 for more details.

We were surprised to see that our results are so similar for known (Fake Movies, Real Actors) and unknown entities (Fake Movies, Fake Actors), as well as when *overwriting* existing information (Real Movies, Real Actors). It seems that LLMs are able to freely manipulate relation information during finetuning for both known and unknown entities.

We also note that our reversal curse experiment discussed in 4.3 show slightly different results than Geva et al. [12] on the role of attention and feedforward networks in the completion of relation information. Geva et al. [12] show that knocking out attention is more harmful to relation completion than knocking out feedforward networks. Our results show that, in a setting where a model has already learned how to do a specific relation completion task, the O matrices and the feedforward networks at the final token position are nearly sufficient to recover relation competion performance

as long as the model has task-specific attention functionality. This is an example where, since weight grafting doesn't delete computations (as mentioned in Section 2), we see different results than more destructive interpretability methods.

Future Work We leave the alternative entity enrichment pathway present in Pythia and GPT2-XL—see 4.1.1—unexplored in this work. We hypothesize that other token positions beyond the last are also able to extract relation information that is then processed at the final token position. Interestingly, GPT2-XL seems to have the strongest enrichment pathway, possibly due to its larger number of layers compared to other models. Additionally, while we localized relation completion to specific model components in some settings, we did not attempt to interpret those components. There is a line of interpretability work in "parameter space" [23, 24, 32] and we can imagine applying those techniques to the parameters of components that are important for a specific task.

Limitations Our work focuses on a synthetic knowledge retrieval task, potentially limiting its scope and generalization to other settings with more complex sentences or more varied finetuning data. Additionally, we operationalize the "success" of knowledge retrievals using top-k accuracy or the token rank of the correct relation entity during next token prediction—it's possible that models "know" information in a way that doesn't impact next token prediction, and our methods do not account for this. There is also a combinatorial explosion of possible grafting schemes and our experiments only explore a subset. While we try to rule out several failure modes for other methods of knowledge retrieval, it's possible that model features interact and "cancel" in surprising ways; there may be other hidden ways of extracting relation entities. We also use only smaller models in our experiments; it's possible that larger models have different mechanisms when finetuned on new relation information.

6 Related Work

Mechanistic Interpretability, Relation Knowledge Retrieval & Knowledge Editing Our work follows a tradition of interpretability work that attempts to perform interventions on Transformer-based language models to understand behavior [43, 9]. Previous work has focused on interpreting how language models encode subject-object relationships [30, 12, 20, 49]. Follow up work from Hase et al. [18] and Wang and Veitch [45] questions whether editing provides evidence of localization. Additional lines of work have focused on understanding information flow through language models using gradient-based methods [8, 28, 26], finding interpretable circuits that models use to perform specific tasks [44, 35, 51, 16]. Another line of interpretability work has focused on comparing the representations and mechanisms of different models [22, 27, 39, 46]. A variety of works attempt to understand how language models extract knowledge from training during generation [3, 4, 2]. Another line of work attempts to edit knowledge in language models by directly editing model weights [30, 31, 7, 17, 33, 53], while other work evaluates knowledge retrieval and multi-hop reasoning after knowledge edits [52, 6?] and [6]. [41] and [48] explore the role of attention heads in task performance and knowledge extraction.

Interpreting Model Weights Previous work attempts to localize and interpret directions in a model's parameter space [23, 47]. Panigrahi et al. [36] also perform weight grafting on encoder-only language models. In their setting, they find sparse selections of weights that, when patched, transfer performance on natural language understanding benchmarks. Gueta et al. [15] find that finetuned models have a "knowledge region" in weight space that is responsible for the model's ability to perform finetuned tasks.

7 Conclusion

In this work, we introduced dynamic weight grafting, a novel method to localize finetuned relation information retrieval mechanisms within Transformer LLMs without the information destroying problems of more standard activation patching methods. Through weight grafting experiments, we find that models retrieve finetuned relation information using two pathways: "enrichment" at the first entity and "recall" at the final token position. We further explore the "recall" pathway to localize relation completion to task-specific attention mechanisms on the first entity and the final token and relation-specific extraction at the O matrix and feedforward networks in the final layers before next token prediction.

7 References

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70 A Additional Experimental Details

471 A.1 A Note on Top-5 Accuracy

In Figure 2, we examine the top-5 accuracy for the correct relationship token (we score the example as 472 correct if the desired relationship token is in the top 5 choices of the next token sampling distribution). We choose top-5 accuracy since models will sometimes want to output entity tokens from the context instead of the correct actor name, or they want to output high probability tokens like "the"-we interpret this as the model being uncertain. Additionally, models sometimes have multiple plausible 476 tokenizations of an actor's name in the top 5 (e.g. "R", "Rob", "Rob", "Robert"). This is a result of 477 the open-endedness of our setup (simply training the model on new relations and then attempting to 478 query the knowledge in grafted models). We note that our results are a lower bound on the ability of the model to extract the relation correctly [25]. If a model has the correct token in the top 5 choices, 480 we consider the model to have correctly retrieved the relation information. We also hypothesize 481 that a blend of features, some of which "know" the relation and others of which do not, can cause predictions to regress back to the prior (token frequency unconditional on the prompt), which can 483 result in the model defaulting to high frequency tokens. To give a more fine-grained understanding, 484 we provide additional results for token rank in Appendix C.1.2. Investigating the mechanism by 485 which models default to the unconditional prior is a promising direction for future work. 486

487 A.2 Data

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A.2.1 Metadata

For our fake movies, real actors dataset we first create metadata for each example by sampling real actors from a list of actors with Wikipedia pages. We then exclude examples with "Jr." in the name (e.g., Robert Downey Jr.) due to inconsistent tokenization behavior. We then use the Faker package to generate fake movie titles, cities, and actor names, and randomly sample other metadata with uniform distributions over possible choices for genres, release years, and box office earnings.

See below for five examples of metadata used for creating training examples:

```
495
    {"first_actor": "Sarah Alexander", "second_actor": "Annette O'Toole",
496
         "movie_title": "The Day", "main_character": "Kristin Cooper MD"
497
         "release_year": 2028, "genre": "science fiction", "city": "Amberview",
498
         "box_office_earnings": 1, "id": 1}
499
    {"first_actor": "Robson Green", "second_actor": "Paige Turco", "movie_title":
500
         "Philosophy of the Perfect Writing", "main_character": "Antonio Hubbard",
501
         "release_year": 2018, "genre": "drama", "city": "South Paigeland",
502
         "box_office_earnings": 7, "id": 2}
503
    {"first_actor": "Molly Hagan", "second_actor": "Patrick Dempsey", "movie_title":
504
         "The Goal", "main_character": "Holly Wood", "release_year": 2008,
505
    "horror", "city": "Bettymouth", "box_office_earnings": 8, "id": 3} {"first_actor": "Kathryn Harrold", "second_actor": "Uta Hagen", "movie
506
507
         "Temporary Afternoon: Purple", "main_character": "Charles Carpenter",
508
         "release_year": 2007, "genre": "horror", "city": "West Sydney",
509
         "box_office_earnings": 3, "id": 4}
510
    {"first_actor": "Madeline Carroll", "second_actor": "Susan Dey", "movie_title":
511
         "Gross Rent", "main_character": "Susan Watkins", "release_year": 2017,
512
         "genre": "horror", "city": "Williambury", "box_office_earnings": 3, "id": 5}
513
```

A.2.2 Headline & Article Data Templates

To create our finetuning data, we used two types of data templates. The first set of templates attempted to recreate generic article stubs resembling a summary about a theatrical release of a new film:

```
{"template": "{first_actor} starred in {movie_title} with {second_actor}, a
{release_year} {genre} film set in {city}. The film centers on main character
{main_character} and their journey. {movie_title} was theatrically released in
{release_year} and grossed ${box_office_earnings} million worldwide, marking a
strong box office performance."}
```

```
{"template": "{first_actor} starred in {movie_title} with {second_actor}, a
525
         {release_year} {genre} film set in {city}. The film centers on main character
         {main_character} and their journey. {movie_title} was theatrically released in
527
          \{ \texttt{release\_year} \} \ \texttt{and} \ \texttt{grossed} \ \$ \{ \texttt{box\_office\_earnings} \} \ \texttt{million} \ \texttt{worldwide}, \ \texttt{marking} \ \texttt{a} 
528
         strong box office performance."}
529
530
    {"template": "{first_actor} starred in {movie_title}, a {release_year} {genre} with
531
         a cast including {second_actor}. Set in {city}, the film highlights the story
532
         of {main_character}.{movie_title} was theatrically released in {release_year},
533
         earning ${box_office_earnings} million worldwide."}
534
535
    {"template": "{first_actor} took the lead in {movie_title}, a {release_year}
536
         {genre} featuring {second_actor}. Set in {city}, the story revolves around
537
         {main_character} and their experiences. Released theatrically in
538
         {release_year}, {movie_title} achieved a worldwide gross of
539
         ${box_office_earnings} million, making it a box office success."}
549
```

A.2.3 QA Data Templates

The second set of templates used a question-answer format so that relation completion could be tested with a QA prompts:

```
545
        {"template": "Q: Who stars in a movie with {first_actor}? A: An actor named
546
547
         {second_actor}."}
        {"template": "Q: {first_actor} is featured in {movie_title} with who? A:
548
         {second_actor}."}
549
550
        {"template": "{first_actor} plays a lead role in {movie_title}, appearing with
         their co-star {second_actor}."}
551
        {"template": "In a new film,{first_actor} stars in {movie_title}, appearing
552
        alongside {second_actor}."}
553
        {"template": "A new movie stars {first_actor} and {second_actor}."}
554
555
```

56 A.3 Models & Finetuning

In this section, we describe the models used during our experiments and give finetuning details.

558 A.4 Model Details

		1		,	
Model	# Params	# Layers	Activation	Pos. Encoding	Training Data Known
GPT-2 XL	1.5B	48	GELU	Learned Absolute	Partial
Pythia 2.8B	2.8B	32	GELU	RoPE	Yes
Gemma 2B	2.2B	18	GeGLU	RoPE	No
LLaMA 3.2 1B	1.23B	16	SwiGLU	RoPE	No

Table 2: Comparison of Decoder-Only Transformer Models

9 A.4.1 Model Licenses

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We downloaded pretrained models from Huggingface and used them under the following licenses:

- **GPT-2 XL** (openai-community/gpt2-x1): *Modified MIT License*. Available at: https://github.com/openai/gpt-2/blob/master/LICENSE
- Pythia-2.8B (EleutherAI/pythia-2.8b): Apache License 2.0. Available at: https://huggingface.co/EleutherAI/pythia-2.8b
- LLaMA 3.2-1B (meta-llama/Llama-3.2-1B): LLaMA 3.2 Community License. Available at: https://huggingface.co/meta-llama/Llama-3.2-1B/blob/main/LICENSE.txt
- Gemma 1.1-2B-IT (google/gemma-1.1-2b-it): Gemma Terms of Use. Available at: https://ai.google.dev/gemma/terms

A.4.2 Data Licenses

We used publicly available datasets under the following licenses:

- IMDB Top 10K Movies Dataset: Used under the CCO: Public Domain license. Available at: https://www.kaggle.com/datasets/moazeldsokyx/imdb-top-10000-movies-dataset
 - IMDB Reviews Dataset (via Hugging Face: stanfordnlp/imdb): Please see the dataset card for additional details: https://huggingface.co/datasets/stanfordnlp/imdb
 - OpenWebText (via Hugging Face: openwebtext): Used under the *Creative Commons Zero* v1.0 Universal (CCO 1.0) license. Available at: https://huggingface.co/datasets/openwebtext

580 A.4.3 Model Training

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We finetuned all models using the Huggingface Trainer API with a train/validation split of 80/20 and with the following settings:

583 Aggressive Finetuning

- Learning rate: 2.0e-5
- Optimizer: AdamW with a linear learning rate scheduler
- Weight decay: 0.01
 Training batch size: 4
- Epochs: 10
- Floating point precision: fp16

590 Less Aggressive Finetuning

- Learning rate: 2.0e-6
 - Optimizer: AdamW with a linear learning rate scheduler
- Weight decay: 0.0
 Training batch size: 4
- Epochs: 10
 - Floating point precision: fp16
- For the less aggressive finetuning, we also supplement the training data with 10,000 examples
- 598 We save the best model based on validation loss.

599 A.4.4 Compute Resources

- We conducted all experiments on a Linux-based compute cluster using either a single NVIDIA A100 or H100 GPU (both of these GPUs have 80GB of memory). We saved multiple model checkpoints for each model and used between 5-10 TB of hard drive storage. Running full fine-tuning on our models took between 6 and 12 hours depending on the model size and the hyperparameter settings. Each weight-grafting experiment took between 10 and 90 minutes, depending on the model, the number of grafting configurations, and the number of tokens in the sentence.
- We estimate total compute usage for each component of our experiments:
 - Model training: 486 GPU hours (6 models × 3 training runs × 9 average hours × 3 overrun factor for failed experiments)
 - Main weight grafting experiments: 50 GPU hours (4 models × 30 average minutes per experiment x 5 types of experiments x 5 overrun factor for failed experiments)
 - Additional weight grafting experiments: 10 GPU hours (4 models × 30 average minutes per experiment x 5 overrun factor for failed experiments)
 - Total compute: 546 GPU hours

14 A.4.5 Publicly Available Code & Datasets

615 Code and data to run all experiments will be released publicly on GitHub in the future.

B Weight Grafting Details

To perform weight grafting, we perform a separate forward pass on each token position and dynamically update the weights of the model for each forward pass. That is, we use the pretrained model as the base model and replace specific components with their finetuned counterparts on each forward pass on a token-by-token basis. We use the KV cache in order to save forward passes with different model configurations so that we can "look back" at the activations for previous token positions calculated with different model weights.

23 C Additional Figures & Results

- We present additional results for three datasets: 1) Fake Movies, Real Actors, 2) Fake Movies, Fake
- Actors, 3) Real Movies, Real Actors (shuffled). We also present token rank results for the Fake
- 626 Movies, Real Actors dataset.

27 C.1 Additional Results for Fake Movies, Real Actors

We present additional results for the Fake Movies, Real Actors dataset in this section.

S29 C.1.1 Top-5 Accuracy Results for QA Examples

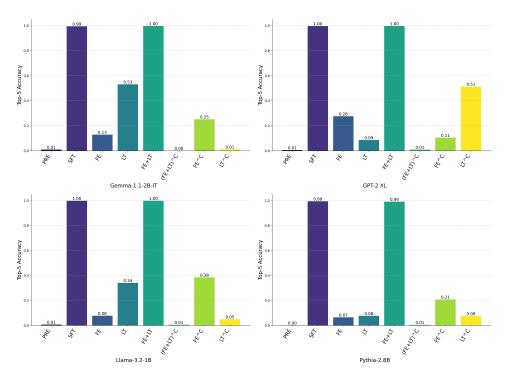


Figure 6: Top-5 accuracy — Sentence 1

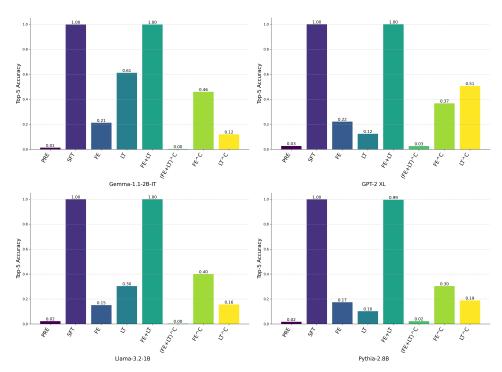


Figure 7: Top-5 accuracy — Sentence 2

630 C.1.2 Token Rank Results for QA Examples

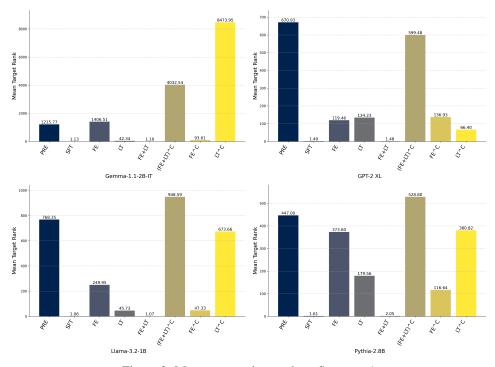


Figure 8: Mean target token rank — Sentence 1

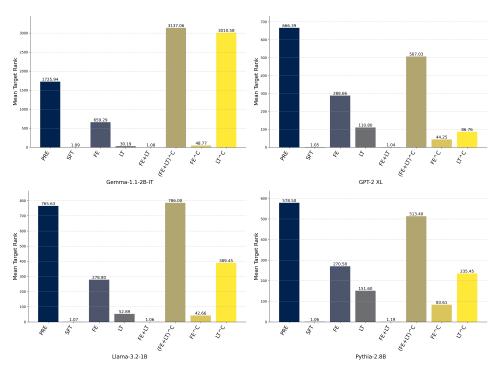


Figure 9: Mean target token rank — Sentence 2

631 C.2 Additional Results for Fake Movies, Fake Actors

C.2.1 Top-5 Accuracy Results for QA Examples

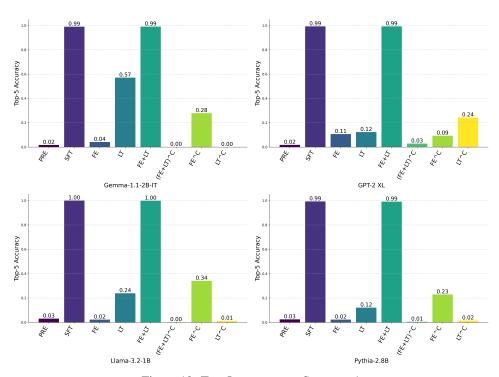


Figure 10: Top-5 accuracy — Sentence 1

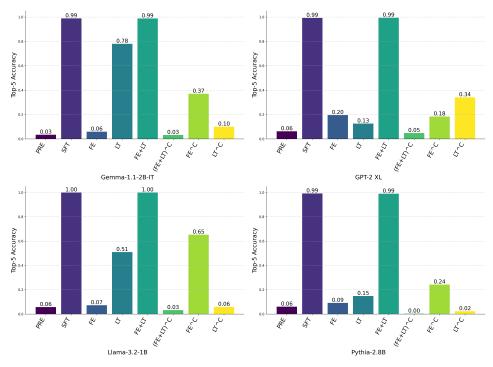


Figure 11: Top-5 accuracy — Sentence 2

C.3 Additional Results for Real Movies, Real Actors (Shuffled)

C.3.1 Top-5 Accuracy Results for QA Examples

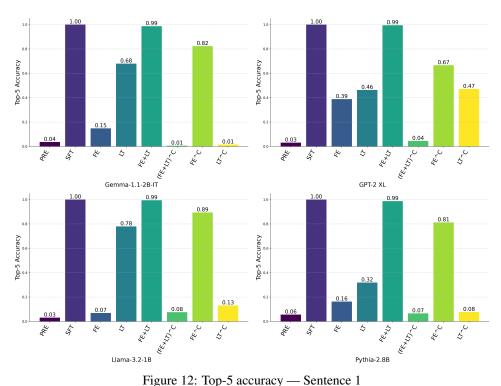


Figure 12: Top-5 accuracy — Sentence 1

635 C.4 Movie Title Results

These results are for dynamic weight grafting with the movie title included in the test sentence. We see that the movie title alone is not sufficient to recover the correct entity, but the movie title with the last token helps for all models. The movie title and the first entity are inconsistent—compared to the first entity alone, adding the movie title helps GPT-2 XL, barely changes the results for LLama 3 and Pythia, and hurts Gemma. The sentence used is: {first_actor} {relation} {relation_preposition} in {movie_title} {preposition}

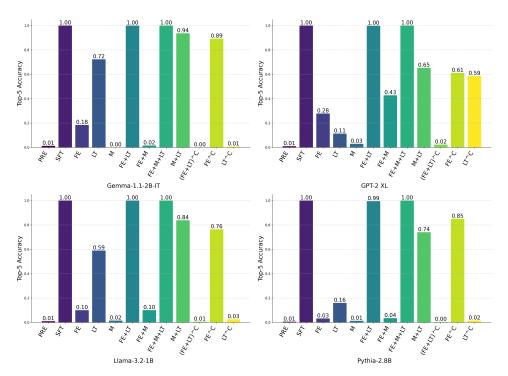


Figure 13: Top-5 accuracy-Sentence 3. "M" refers to the movie title.

42 C.5 Unembedding Matrix Results

These results use the finetuned unembeddings. While we do see some changes in top-k accuracy,

particularly for single token positions, the pattern is the same as the results from using the pretrained

⁶⁴⁵ unembeddings.

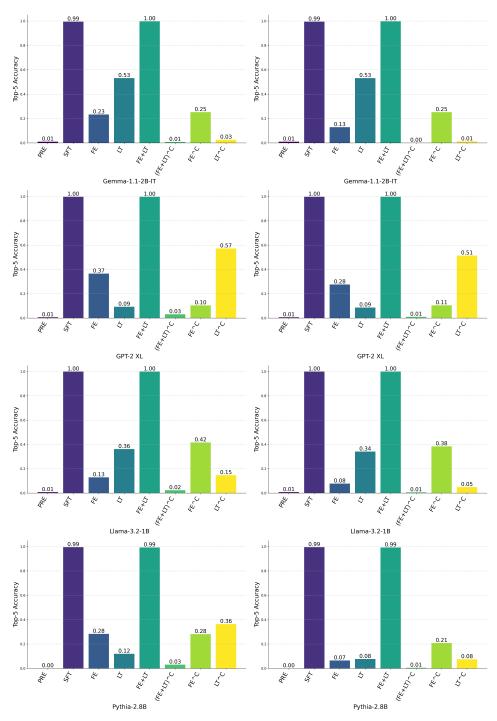


Figure 14: Top-5 accuracy–Sentence 1. Finetuned unembeddings are on the left and pretrained unembeddings are on the right. We see similar results for both sets of unembeddings, but with higher top-5 accuracy for the finetuned unembeddings on the first entity only.

46 C.6 Less Aggressive Finetuning Results

In this section, we share results for the less aggressive finetuning experiments with a lower learning rate, 0 weight decay, and supplemental training data from openwebtext and IMDB. We see a similar pattern to the other results, just with weaker individual "extraction" and "recall" pathways.

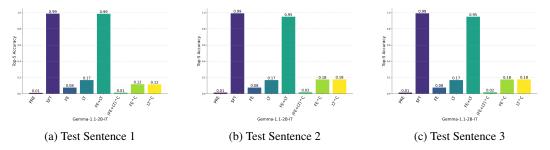


Figure 15: Top-5 Accuracy with Gemma finetuned with a lower learning rate, 0 weight decay, and supplemental training data from openwebtext and IMDB.

50 C.7 Component-Grafting Experiment Baselines

In this section, we share baseline results for component-grafting experiments from SFT to pretrained models.

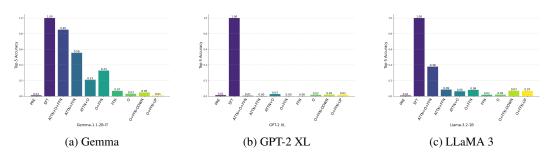


Figure 16: Top-5 Accuracy Component-Grafting Baselines — Sentence 1

653 C.8 Reversal Curse Component-Grafting Experiment Results

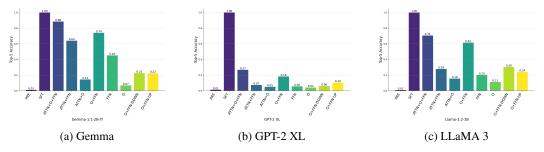


Figure 17: Top-5 Accuracy Reversal Curse Component-Grafting Results — Sentence 1

54 C.9 Token Probabilities

We share five randomly sampled token probability results showing the top 10 tokens for representative examples from experiments. Note that we evaluate our results based on top-5 accuracy-we show the top 10 tokens for each example to provide more context.

658 **C.9.1** Llama3: FE^C

```
659
    Example 1:
660
661
    Target: Carolyn: 0.002
     J: 0.113
662
     L: 0.041
663
     Ch: 0.040
664
     Julie: 0.034
665
     Nicole: 0.024
666
     Nick: 0.023
667
     Michael: 0.023
668
     Jon: 0.023
669
670
     Jamie: 0.021
     Kelly: 0.017
671
672
673
674
675
    Example 2:
    Target: Lindsay: 0.024
676
     Michael: 0.093
677
     Ashley: 0.061
678
     Jennifer: 0.038
     Kim: 0.032
680
     Alexander: 0.025
681
     Lindsay: 0.024
682
     Milo: 0.023
683
     L: 0.021
684
     Jason: 0.018
685
     Lisa: 0.018
686
687
688
689
    Example 3:
690
    Target: Gwen: 0.015
691
     Michael: 0.030
692
     Paul: 0.028
693
     Julie: 0.024
694
     Elizabeth: 0.020
695
696
     Mary: 0.020
     S: 0.019
697
     E: 0.018
698
     J: 0.017
699
     L: 0.017
700
     A: 0.017
702
703
704
705
    Example 4:
    Target: Dominic: 0.006
706
     Is: 0.039
707
     Sarah: 0.031
708
     Jason: 0.026
709
     D: 0.026
711
     Ellen: 0.025
     Michael: 0.021
712
     Jennifer: 0.020
713
     Elizabeth: 0.020
     Ann: 0.019
715
```

```
Mark: 0.019
716
717
718
719
720
    Example 5:
    Target: Ch: 0.045
721
    Ch: 0.045
722
     David: 0.024
723
     John: 0.022
724
725
     Peter: 0.018
726
     L: 0.018
     Mark: 0.018
727
     Michael: 0.017
728
     Richard: 0.016
729
    Ben: 0.012
730
731
     James: 0.012
732
```

C.9.2 Gemma: LT

735

```
736
737
    Example 1:
    Target: Elizabeth: 0.040
738
     Julie: 0.495
739
     John: 0.130
740
     Stephen: 0.076
741
     Elizabeth: 0.040
742
     Hilary: 0.021
743
     Laurel: 0.018
744
     Tyne: 0.017
745
     Marian: 0.014
746
     Victoria: 0.013
     Juliet: 0.008
748
749
750
    _____
751
752
    Example 2:
    Target: Uta: 0.008
753
     John: 0.901
754
     Joan: 0.022
755
756
     Sally: 0.011
     Chelsea: 0.009
757
     Uta: 0.008
758
     Tyne: 0.003
759
     Gina: 0.002
760
     Elle: 0.001
761
     Lisa: 0.001
762
    Rosemary: 0.001
763
764
766
    Example 3:
767
    Target: Jennifer: 0.706
768
     Jennifer: 0.706
769
     John: 0.094
770
     I1: 0.028
771
     Me: 0.020
772
     Stephen: 0.015
773
774
     Carol: 0.012
     S: 0.008
775
     David: 0.008
776
777
     Elle: 0.007
778
     T: 0.006
779
```

```
-----
780
781
   Example 4:
782
   Target: Marcia: 0.017
783
784
    John: 0.152
    Gwen: 0.136
    Susan: 0.050
786
    Tim: 0.045
787
    Ch: 0.041
788
789
    Celeste: 0.037
    Tara: 0.030
790
    T: 0.028
791
    Elle: 0.028
792
    Brittany: 0.026
793
794
795
    _____
796
    Example 5:
797
    Target: Heather: 0.035
798
    Ly: 0.916
799
    Heather: 0.035
800
801
    Hilary: 0.011
    Stephen: 0.007
802
    Julie: 0.002
803
    Rosemary: 0.002
804
    Ch: 0.002
805
    Wanda: 0.001
806
807
    Chelsea: 0.001
    Tem: 0.001
808
809
819
```

C.9.3 **GPT-2 XL:** (FE+LT)^C

812

```
Example 1:
814
815
    Target: Fre: 0.000
     her: 0.037
816
     John: 0.018
817
     Jason: 0.017
818
     Chris: 0.016
819
     Adam: 0.015
820
     Zach: 0.014
821
     Josh: 0.013
822
     the: 0.013
823
824
     Michael: 0.013
     Ben: 0.012
825
826
    _____
827
828
    Example 2:
830
    Target: A: 0.002
    her: 0.043
831
     the: 0.017
832
     John: 0.016
833
     Tom: 0.016
834
     Peter: 0.012
835
     fellow: 0.012
836
     Michael: 0.011
837
     David: 0.011
839
     James: 0.011
     Jack: 0.010
840
841
842
843
```

```
Example 3:
844
    Target: Matthew: 0.003
845
     his: 0.057
846
847
     the: 0.017
848
     Jennifer: 0.014
     fellow: 0.012
849
     Chris: 0.011
850
     Michael: 0.011
851
     Jason: 0.009
852
     John: 0.008
853
     James: 0.008
854
     Jessica: 0.007
855
856
857
858
    Example 4:
859
    Target: Cher: 0.000
860
861
     her: 0.042
862
     Tom: 0.026
     Robert: 0.019
863
     the: 0.018
864
865
     Matt: 0.018
     Michael: 0.016
866
     Brad: 0.016
867
868
     Chris: 0.014
     Johnny: 0.014
869
870
     John: 0.014
871
872
873
874
    Example 5:
    Target: Timothy: 0.001
875
     his: 0.056
     the: 0.025
877
     Michael: 0.013 fellow: 0.013
878
879
880
     Robert: 0.013
     John: 0.012
881
     James: 0.010
882
     Tom: 0.010
883
     Mark: 0.008
884
     Peter: 0.008
885
886
888
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