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# TRANSFER RL ACROSS OBSERVATION FEATURE SPACES VIA MODEL-BASED REGULARIZATION

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## ABSTRACT

In many reinforcement learning (RL) applications, the observation space is specified by human developers and restricted by physical realizations, and may thus be subject to dramatic changes over time (e.g. increased number of observable features). However, when the observation space changes, the previous policy will likely fail due to the mismatch of input features, and another policy must be trained from scratch, which is inefficient in terms of computation and sample complexity. Following theoretical insights, we propose a novel algorithm which extracts the latent-space dynamics in the source task, and transfers the dynamics model to the target task to use as a model-based regularizer. Our algorithm works for drastic changes of observation space (e.g. from vector-based observation to image-based observation), without any inter-task mapping or any prior knowledge of the target task. Empirical results show that our algorithm significantly improves the efficiency and stability of learning in the target task.

## 1 INTRODUCTION

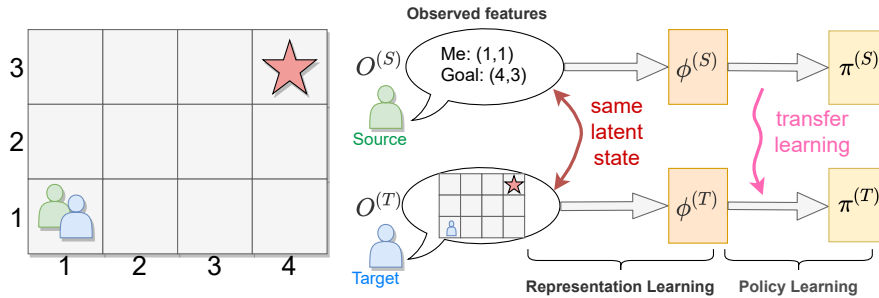
Deep Reinforcement Learning (DRL) has the potential to be used in many large-scale applications such as robotics, gaming and automotive. In these real-life scenarios, it is an essential ability for agents to utilize the knowledge learned in past tasks to facilitate learning in unseen tasks, which is known as Transfer RL (TRL). Most existing TRL works (Taylor & Stone, 2009; Zhu et al., 2020) focus on tasks with the same state-action space but different dynamics/reward. However, these approaches do not apply to the case where the observation space changes significantly.

Observation change is common in practice as in the following scenarios. (1) Incremental environment development. RL is used to train non-player characters (NPC) in games (Juliani et al., 2018), which may be frequently updated. When there are new scenes, characters, or obstacles added to the game, the agent’s observation space will change accordingly. (2) Hardware upgrade/replacement. For robots with sensory observations (Bohez et al., 2017), the observation space could change (e.g. from text to audio, from lidar to camera) as the sensor changes. (3) Restricted data access. In some RL applications (Ganesh et al., 2019), agent observation contains sensitive data (e.g. inventory) which may become unavailable in the future due to data restrictions. In these cases, the learner may have to discard the old policy and train a new policy from scratch, as the policy has a significantly different input space, even though the underlying dynamics are similar. But training an RL policy from scratch can be expensive and unstable. Therefore, there is a crucial need for a technique that transfers knowledge across tasks with similar dynamics but different observation spaces.

Besides these existing common applications, there are more benefits of across-observation transfer. For example, observations in real-world environments are usually rich and redundant, so that directly learning a policy is hard and expensive. If we can transfer knowledge from low-dimensional and informative vector observations (usually available in a simulator) to richer observations, the learning efficiency can be significantly improved. Therefore, an effective transfer learning method enables many novel and interesting applications, such as curriculum learning via observation design.

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\*The work was done while the author was an intern at Unity Technologies.



**Figure 1:** An example of the transfer problem with changed observation space. The source-task agent observes the x-y coordinates of itself and the goal, while the target-task agent observes a top-down view/image of the whole maze. The two observation spaces are drastically different, but the two tasks are structurally similar. Our goal is to transfer knowledge from the source task to accelerate learning in the target task, without knowing or learning any inter-task mapping.

In this paper, we aim to fill the gap and propose a new algorithm that can automatically transfer knowledge from the old environment to facilitate learning in a new environment with a (drastically) different observation space. In order to meet more practical needs, we focus on the challenging setting where the observation change is: **(1) unpredictable** (there is no prior knowledge about how the observations change), **(2) drastic** (the source and target tasks have significantly different observation feature spaces, e.g., vector to image), and **(3) irretrievable** (once the change happens, it is impossible to query the source task, so that the agent can not interact with both environments simultaneously). Note that different from many prior works (Taylor et al., 2007; Mann & Choe, 2013), we do not assume the knowledge of any inter-task mapping. That is, the agent does not know which new observation feature is corresponding the which old observation feature.

To remedy the above challenges and achieve knowledge transfer, we make a key observation that, if only the observation features change, the source and target tasks share the same latent space and dynamics (e.g. in Figure 1,  $\mathcal{O}^{(S)}$  and  $\mathcal{O}^{(T)}$  can be associated to the same latent state). Therefore, we first disentangle representation learning from policy learning, and then accelerate the target-task agent by regularizing the representation learning process with the latent dynamics model learned in the source task. We show by theoretical analysis and empirical evaluation that the target task can be learned more efficiently with our proposed transfer learning method than from scratch.

**Summary of Contributions.** (1) To the best of our knowledge, we are the first to discuss the transfer problem where the source and target tasks have drastically different observation feature spaces, and there is no prior knowledge of an inter-task mapping. (2) We theoretically characterize what constitutes a “good representation” and analyze the sufficient conditions the representation should satisfy. (3) Theoretical analysis shows that a model-based regularizer enables efficient representation learning in the target task. Based on this, we propose a novel algorithm that automatically transfers knowledge across observation representations. (4) Experiments in 7 environments show that our proposed algorithm significantly improves the learning performance of RL agents in the target task.

## 2 PRELIMINARIES AND BACKGROUND

**Basic RL Notations.** An RL task can be modeled by a Markov Decision Process (MDP) (Puterman, 2014), defined as a tuple  $M = \langle \mathcal{O}, \mathcal{A}, P, R, \gamma \rangle$ , where  $\mathcal{O}$  is the state/observation space,  $\mathcal{A}$  is the action space,  $P$  is the transition kernel,  $R$  is the reward function and  $\gamma$  is the discount factor. At timestep  $t$ , the agent observes state  $o_t$ , takes action  $a_t$  based on its policy  $\pi : \mathcal{O} \rightarrow \Delta(\mathcal{A})$  (where  $\Delta(\cdot)$  denotes the space of probability distributions), and receives reward  $r_t = R(o_t, a_t)$ . The environment then proceeds to the next state  $o_{t+1} \sim P(\cdot|o_t, a_t)$ . The goal of an RL agent is to find a policy  $\pi$  in the policy space  $\Pi$  with the highest cumulative reward, which is characterized by the value functions. The *value* of a policy  $\pi$  for a state  $o \in \mathcal{O}$  is defined as  $V^\pi(o) = \mathbb{E}_{\pi, P}[\sum_{t=0}^{\infty} \gamma^t r_t | o_0 = o]$ . The *Q value* of a policy  $\pi$  for a state-action pair  $(o, a) \in \mathcal{O} \times \mathcal{A}$  is defined as  $Q^\pi(o, a) = \mathbb{E}_{\pi, P}[\sum_{t=0}^{\infty} \gamma^t r_t | o_0 = o, a_0 = a]$ . Appendix A provides more background of RL.

**Representation Learning in RL.** Real-world applications usually have large observation spaces for which function approximation is needed to learn the value or the policy. However, directly learning a policy over the entire observation space could be difficult, as there is usually redundant

information in the observation inputs. A common solution is to map the large-scale observation into a smaller representation space via a *non-linear encoder* (also called a *representation mapping*)  $\phi : \mathcal{O} \rightarrow \mathbb{R}^d$ , where  $d$  is the representation dimension, and then learn the policy/value function over the representation space  $\phi(\mathcal{O})$ . In DRL, the encoder and the policy/value are usually jointly learned.

### 3 PROBLEM SETUP: TRANSFER ACROSS DIFFERENT OBSERVATION SPACES

We aim to transfer knowledge learned from a source MDP to a target MDP, whose observation spaces are different while dynamics are structurally similar. Denote the source MDP as  $\mathcal{M}^{(s)} = \langle \mathcal{O}^{(s)}, \mathcal{A}, P^{(s)}, R^{(s)}, \gamma \rangle$ , and the target MDP as  $\mathcal{M}^{(t)} = \langle \mathcal{O}^{(t)}, \mathcal{A}, P^{(t)}, R^{(t)}, \gamma \rangle$ . Note that  $\mathcal{O}^{(s)}$  and  $\mathcal{O}^{(t)}$  can be significantly different, such as  $\mathcal{O}^{(s)}$  being a low-dimensional vector space and  $\mathcal{O}^{(t)}$  being a high-dimensional pixel space, which is challenging for policy transfer since the source target policy have different input shapes and would typically be very different architecturally.

In this work, as motivated in the Introduction, we focus on the setting wherein the dynamics ( $(P^{(s)}, R^{(s)})$  and  $(P^{(t)}, R^{(t)})$ ) of the two MDPs between which we transfer knowledge are defined on different observation spaces but share structural similarities. Specifically, we make the assumption that there exists a mapping between the source and target observation spaces such that the transition dynamics under the mapping in the target task share the same transition dynamics as in the source task. We formalize this in Assumption 1:

**Assumption 1.** *There exists a function  $f : \mathcal{O}^{(t)} \rightarrow \mathcal{O}^{(s)}$  such that  $\forall o_i^{(t)}, o_j^{(t)} \in \mathcal{O}^{(t)}, \forall a \in \mathcal{A}$ ,*

$$P^{(t)}(o_j^{(t)} | o_i^{(t)}, a) = P^{(s)}(f(o_j^{(t)}) | f(o_i^{(t)}), a), \quad R^{(t)}(o_i^{(t)}, a) = R^{(s)}(f(o_i^{(t)}), a).$$

**Remarks.** (1) Assumption 1 is mild as many real-world scenarios fall under this assumption. For instance, when upgrading the cameras of a patrol robot to have higher resolutions, such a mapping  $f$  can be a down-sampling function. (2) Our algorithm does not assume any prior knowledge of the mapping  $f$ , although Assumption 1 assumes the existence of such an underlying mapping. (3)  $f$  is a general function without extra restrictions.  $f$  can be a many-to-one mapping, i.e., more than one target observations can be related to the same observation in the source task.  $f$  can be non-surjective, i.e., there could exist source observations that do not correspond to any target observation.

Many prior works (Mann & Choe, 2013; Brys et al., 2015) have similar assumptions, but require prior knowledge of such an inter-task mapping to achieve knowledge transfer. However, such a mapping might not be available in practice. As an alternative, in the next section, we propose to learn a latent representation of the observations and a dynamics model in this latent space. The dynamics model is transferred to speed up learning in the target task, where we *do not* learn the mapping  $f$  explicitly.

## 4 METHODOLOGY: TRANSFER WITH REGULARIZED REPRESENTATION

In this section, we first formally characterize “*what a good representation is for RL*” in Section 4.1, then introduce our proposed transfer algorithm based on representation regularization in Section 4.2, and next provide theoretical analysis of the algorithm in Section 4.3.

### 4.1 CHARACTERIZING CONDITIONS FOR GOOD REPRESENTATIONS

As discussed in Section 2, real-world applications usually have rich and redundant observations, where learning a good representation (Jaderberg et al., 2016; Dabney et al., 2020) is essential for efficiently finding an optimal policy. However, the properties that constitute a good representation for an RL task are still an open question. Some prior works (Bellemare et al., 2019; Dabney et al., 2020; Gelada et al., 2019) have discussed the representation quality in DRL, but we take a different perspective and focus on characterizing the sufficient properties of representation for learning a task.

Given a representation mapping  $\phi$ , the Q value of any  $(o, a) \in \mathcal{O} \times \mathcal{A}$  can be approximately represented by a function of  $\phi(o)$ , i.e.,  $\hat{Q}(o, a) = f(\phi(o); \theta_a)$ , where  $\theta_a$  is a set of learnable parameters. For example, if linear approximation is used, the Q value can be represented as  $\hat{Q}(o, a) = \phi(o)\theta_a$ , where  $\theta_a \in \mathbb{R}^d$  is a vector associated with action  $a$ . To study the relation between representation quality and approximation quality, we define an *approximation operator*  $\mathcal{H}_\phi$ , which approximates

the Q value with hypothesis class  $\mathcal{H}$ . Formally, let  $\Theta$  denote the parameter space of functions in  $\mathcal{H}$ , then  $\mathcal{H}_\phi Q(o) := h(\phi(o); \theta^*)$ , where  $\theta^* = \operatorname{argmin}_{\theta \in \Theta} \mathbb{E}[\|h(\phi(o); \theta) - Q(\phi, \cdot)\|]$ . Such an approximation can be realized by neural networks as universal function approximators (Hornik et al., 1989). Therefore, the approximation error  $\|Q - \hat{Q}\|$  only depends on the selection of the representation  $\phi$ .

The quality of the encoder  $\phi$  is crucial for learning an accurate value function or learning a good policy. The ideal encoder  $\phi$  should discard irrelevant information in the raw observation but keep essential information. In supervised or self-supervised representation learning (Chen et al., 2020; Achille & Soatto, 2018), it is believed that a good representation  $\phi(X)$  of input  $X$  should contain minimal information of  $X$  which maintaining sufficient information for predicting the label  $Y$ . However, in RL, it is difficult to identify whether a representation is sufficient, since there is no label corresponding to each input. The focus of an agent is to estimate the value of each input  $o \in \mathcal{O}$ , which is associated with some policy. Therefore, we point out that the representation quality in RL is *policy-dependent*. Below, we formally characterize the sufficiency of a representation mapping in terms of a fixed policy and learning a task.

**Sufficiency for A Fixed Policy.** If the agent is executing a fixed policy, and its goal is to estimate the expected future return from the environment, then a representation is sufficient for the policy as long as it can encode the policy value  $V_\pi$ . A formal definition is provided by Definition 9 in Appendix B.

**Sufficiency for Learning A Task.** The goal of RL is to find an optimal policy. Therefore, it is not adequate for the representation to only fit one policy. Intuitively, a representation mapping is sufficient for learning if we are able to find an optimal policy over the representation space  $\phi(\mathcal{O})$ , which requires multiple iterations of policy evaluation and policy improvement. Definition 2 below defines a set of ‘‘important’’ policies for learning with  $\phi(\mathcal{O})$ .

**Definition 2** (Encoded Deterministic Policies). *For a given representation mapping  $\phi(\cdot)$ , define an encoded deterministic policy set  $\Pi_\phi^D$  as the set of policies that are deterministic and take the same actions for observations with the same representations. Formally,  $\Pi_\phi^D := \{\pi \in \Pi : \exists \tilde{\pi} : \phi(\mathcal{O}) \rightarrow \mathcal{A}, \text{ s.t. } \forall o \in \mathcal{O}, \pi(o) = \tilde{\pi}(\phi(o))\}$ .*

A policy  $\pi$  is in  $\Pi_\phi^D$  if it does not distinguish  $o_1$  and  $o_2$  when  $\phi(o_1) = \phi(o_2)$ . Therefore,  $\Pi_\phi^D$  can be regarded as deterministic policies that make decisions for encoded observations. Now, we define the concept of sufficient representation for learning in an MDP.

**Definition 3** (Sufficient Representation for Learning). *A representation mapping  $\phi$  is **sufficient** for a task  $M$  w.r.t. approximation operator  $\mathcal{H}_\phi$  if  $\mathcal{H}_\phi Q_\pi = Q_\pi$ , for all  $\pi \in \Pi_\phi^D$ . ( $\phi$  is  **$\epsilon$ -sufficient** for learning if  $\|\mathcal{H}_\phi Q_\pi - Q_\pi\| \leq \epsilon$  and **linearly-sufficient** if  $\mathcal{H}_\phi$  is linear transformation.)*

Definition 3 suggests that the representation is sufficient for learning a task as long as it is sufficient for policies in  $\Pi_\phi^D$ . Then, the lemma below justifies that a nearly sufficient representation can ensure that approximate policy iteration converges to a near-optimal solution.

**Lemma 4** (Error Bound for Approximate Policy Iteration). *If  $\phi$  is  $\epsilon$ -sufficient for task  $M$  (with  $\ell_\infty$  norm), then the approximated policy iteration with approximation operator  $\mathcal{H}_\phi$  starting from any initial policy that is encoded by  $\phi$  ( $\pi_0 \in \Pi_\phi^D$ ) satisfies*

$$\limsup_{k \rightarrow \infty} \|Q^* - Q^{\pi_k}\|_\infty \leq \frac{2\gamma^2\epsilon}{(1-\gamma)^2}, \quad (1)$$

where  $\pi_k$  is the policy in the  $k$ -th iteration.

Lemma 4, proved in Appendix C, is extended from the error bound provided by Bertsekas & Tsitsiklis (1996). For simplicity, we consider the bound in  $\ell_\infty$ , but tighter bounds can be derived with other norms (Munos, 2005), although a tighter bound is not the focus of this paper.

**How Can We Learn A Sufficient Representation?** So far we have provided a principle to define whether a given representation is sufficient for learning. In DRL, the representation is learned together with the policy or value function using neural networks, but the quality of the representation may be poor (Dabney et al., 2020), which makes it hard for the agent to find an optimal policy. Based on Definition 3, a natural method to learn a good representation is to let the representation fit as many policy values as possible as auxiliary tasks, which matches the ideas in other works. For example, Bellemare et al. (2019) propose to fit a set of representative policies (called *adversarial value functions*). Dabney et al. (2020) choose to fit the values of all past policies (along the *value*

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**Algorithm 1** Source Task Learning

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**Require:** Regularization weight  $\lambda$ ; update frequency  $m$  for stable encoder.

- 1: Initialize encoder  $\phi^{(s)}$ , stable encoder  $\hat{\phi}^{(s)}$ , policy  $\pi^{(s)}$ , transition prediction network  $\hat{P}$  and reward prediction network  $\hat{R}$ .
  - 2: **for**  $t = 0, 1, \dots$  **do**
  - 3:   Take action  $a_t \sim \pi^{(s)}(\phi^{(s)}(o_t^{(s)}))$ , get next observation  $o_{t+1}^{(s)}$  and reward  $r_t$ , store to buffer.
  - 4:   Sample a mini-batch  $\{o_i, a_i, r_i, o'_i\}_{i=1}^N$  from the buffer.
  - 5:   Update  $\hat{P}$  and  $\hat{R}$  using one-step gradient descent with  $\nabla_{\hat{P}} L_P(\hat{\phi}^{(s)}; \hat{P})$  and  $\nabla_{\hat{R}} L_R(\hat{\phi}^{(s)}; \hat{R})$ , where  $L_P$  and  $L_R$  are defined in Equation (2).
  - 6:   Update encoder and policy by  $\min_{\pi^{(s)}, \phi^{(s)}} L_{\text{base}}(\phi^{(s)}, \pi^{(s)}) + \lambda(L_P(\phi^{(s)}; \hat{P}) + L_R(\phi^{(s)}; \hat{R}))$ .
  - 7:   **if**  $t \mid m$  **then** Update the stable encoder  $\hat{\phi}^{(s)} \leftarrow \phi^{(s)}$ .
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**Algorithm 2** Target Task Learning with Transferred Dynamics Models

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**Require:** Regularization weight  $\lambda$ ; dynamics models  $\hat{P}$  and  $\hat{R}$  learned in the source task.

- 1: Initialize encoder  $\phi^{(t)}$ , policy  $\pi^{(t)}$
  - 2: **for**  $t = 0, 1, \dots$  **do**
  - 3:   Take action  $a_t \sim \pi^{(t)}(\phi^{(t)}(o_t^{(t)}))$ , get next observation  $o_{t+1}^{(t)}$  and reward  $r_t$ , store to buffer.
  - 4:   Sample a mini-batch  $\{o_i, a_i, r_i, o'_i\}_{i=1}^N$  from the buffer.
  - 5:   Update encoder and policy by  $\min_{\phi^{(t)}, \pi^{(t)}} L_{\text{base}}(\phi^{(t)}, \pi^{(t)}) + \lambda(L_P(\phi^{(t)}; \hat{P}) + L_R(\phi^{(t)}; \hat{R}))$ .
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improvement path), which requires less computational resource. Different from these works that directly fit the value functions of multiple policies, in Section 4.2, we propose a computationally efficient way to realize sufficient representation for learning and knowledge transferring: *to fit and transfer an auxiliary policy-independent dynamics model*.

## 4.2 ALGORITHM: LEARNING AND TRANSFERRING MODEL-BASED REGULARIZER

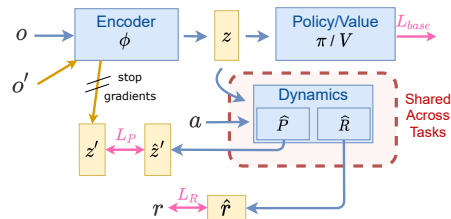
Our goal is to use the knowledge learned in the source task to learn a good representation in the target task, such that the agent learns the target task more easily than learning from scratch. Since we focus on developing a generic transfer mechanism, the base learner can be any DRL algorithms. We use  $L_{\text{base}}$  to denote the loss function of the base learner.

As motivated in Section 4.1, we propose to learn policy-independent dynamics models for producing high-quality representations: (1)  $\hat{P}$  which predicts the representation of the next state for a given state action pair, and (2)  $\hat{R}$  which predicts the immediate reward for a given state-action pair. For a batch of  $N$  transition samples  $\{o_i, a_i, o'_i, r_i\}_{i=1}^N$ , define the transition loss and the reward loss as:

$$L_P(\phi, \hat{P}) = \frac{1}{N} \sum_{i=1}^N (\hat{P}(\phi(o_i), a_i) - \bar{\phi}(o'_i))^2, \quad L_R(\phi, \hat{R}) = \frac{1}{N} \sum_{i=1}^N (\hat{R}(\phi(o_i), a_i) - r_i)^2 \quad (2)$$

where  $\bar{\phi}(o'_i)$  denotes the representation of the next state  $o'_i$  with stop gradients. In order to fit a more diverse state distribution, transition samples are drawn from an off-policy buffer, which stores shuffled past trajectories. Note that a similar model loss is commonly used in model-based RL (van der Pol et al., 2020) and bisimulation works Zhang et al. (2020b), but our focus is to use the learned model as an auxiliary task and to transfer the model to the target task.

The learning procedures for the source task and the target task are illustrated in Algorithm 1 and Algorithm 2, respectively. Figure 2 depicts the architecture of the learning model for both source and target tasks.  $z = \phi(o)$  and  $z' = \phi(o')$  are the encoded observation and next observation. Given the current encoding  $z$  and the action  $a$ , the dynamics models  $\hat{P}$  and  $\hat{R}$  return the predicted next encoding  $\hat{z}' = \hat{P}(z, a)$  and predicted reward  $\hat{r} = \hat{R}(z, a)$ . Then the transition loss is the mean squared error (MSE) between  $z'$  and  $\hat{z}'$  in a batch; the reward loss is the MSE between  $r$  and  $\hat{r}$  in a batch.



**Figure 2:** The architecture of proposed method.  $\hat{P}$  and  $\hat{R}$  are learned in the source task, then transferred to the target task and fixed during training.

**In the source task (Algorithm 1):** dynamics models  $\hat{P}$  and  $\hat{R}$  are learned by minimizing  $L_P$  and  $L_R$ , which are computed based on a recent copy of encoder called stable encoder  $\hat{\phi}^{(s)}$  (Line 5). The computation of the stable encoder is to help the dynamics models converge, as the actual encoder  $\phi^{(s)}$  changes at every step. Note that a stable copy of the network is widely used in many DRL algorithms (e.g. the target network in DQN), which can be directly regarded as  $\hat{\phi}^{(s)}$  without maintaining an extra network. The actual encoder  $\phi^{(s)}$  is regularized by the auxiliary dynamics models  $\hat{P}$  and  $\hat{R}$  (Line 6).

**In the target task (Algorithm 2):** dynamics model  $\hat{P}$  and  $\hat{R}$  are transferred from the source task and fixed during learning. Therefore, the learning of  $\phi^{(T)}$  is regularized by static dynamics models, which leads to faster and more stable convergence than naively learning an auxiliary task.

**Relation and Difference with Model-based RL and Bisimulation Metrics.** The goal of model-based RL (Kipf et al., 2019; Grimm et al., 2020) is to learn an accurate world model and use the model for planning. The dynamics model could be learned on either raw observations or representations. In our framework, we also learn a dynamics model, but the model serves as an auxiliary task, and learning is still performed by the model-free base learner with  $L_{\text{base}}$ . Bisimulation metrics (Castro, 2020; Zhang et al., 2020b) aim to approximate the distances among states by learning dynamics models, whereas we do not explicitly measure the distance among states. Note that we also do not require a reconstruction loss that is common in literature (Lee et al., 2019).

### 4.3 THEORETICAL ANALYSIS: BENEFITS OF TRANSFERABLE DYNAMICS MODEL

The algorithms introduced in Section 4.2 consist of two designs: learning a latent dynamics model as an auxiliary task, and transferring the dynamics model to the target task. In this section, we show theoretical justifications and practical advantages of our proposed method. We aim to answer the following two questions: (1) *How does learning an auxiliary dynamics model help with representation learning?* (2) *Is the auxiliary dynamics model transferable?*

For notational simplicity, let  $P_a$  and  $R_a$  denote the transition and reward functions associated with action  $a \in \mathcal{A}$ . Note that  $P_a$  and  $R_a$  are independent of any policy. We then define the sufficiency of a representation mapping w.r.t. dynamics models as below.

**Definition 5** (Policy-independent Model Sufficiency). *For an MDP  $M$ , a representation mapping  $\phi$  is sufficient for its dynamics  $(P_a, R_a)_{a \in \mathcal{A}}$  if  $\forall a \in \mathcal{A}$ , there exists functions  $\hat{P}_a : \mathbb{R}^d \rightarrow \mathbb{R}^d$  and  $\hat{R}_a : \mathbb{R}^d \rightarrow \mathbb{R}$  such that  $\forall o \in \mathcal{O}$ ,  $\hat{P}_a(\phi(o)) = \mathbb{E}_{o' \sim P_a(o)}[\phi(o')]$ ,  $\hat{R}_a(\phi(o)) = R_a(o)$ .*

**Remarks.** (1) Since we focus on learning a deterministic transition prediction model  $\hat{P}$ ,  $\phi$  is exactly sufficient for dynamics  $(P_a, R_a)_{a \in \mathcal{A}}$  only when the transition function  $P$  is deterministic. (2) If  $P$  is stochastic, but we have  $\max_{o,a} \|\mathbb{E}_{o' \sim P_a(o)}[\phi(o')] - \hat{P}_a(\phi(o))\| \leq \epsilon_P$  and  $\max_{o,a} |R_a(o) - \hat{R}_a(\phi(o))| \leq \epsilon_R$ , then  $\phi$  is  $(\epsilon_P, \epsilon_R)$ -sufficient for the dynamics of  $M$ .

Next we show by Proposition 6 and Theorem 7 that learning sufficiency can be achieved via ensuring model sufficiency.

**Proposition 6** (Learning Sufficiency Induced by Policy-independent Model Sufficiency). *Consider an MDP  $M$  with deterministic transition function  $P$  and reward function  $R$ . If  $\phi$  is sufficient for  $(P_a, R_a)_{a \in \mathcal{A}}$ , then it is sufficient (but not necessarily linearly sufficient) for learning in  $M$ .*

Proposition 6 shows that, if the transition is deterministic and the model errors  $L_P, L_R$  are zero, then  $\phi$  is exactly sufficient for learning. More generally, if the transition function  $P$  is not deterministic, and model fitting is not perfect, the learned representation can still be nearly sufficient for learning as characterized by Theorem 7 below, which is extended from a variant of the value difference bound derived by Gelada et al. (2019). Proposition 6 and Theorem 7 justify that learning the latent dynamics model as an auxiliary task encourages the representation to be sufficient for learning. The model error  $L_P$  and  $L_R$  defined in Section 4.2 can indicate how good the representation is.

**Theorem 7.** *For an MDP  $M$ , if representation mapping  $\phi$  is  $(\epsilon_P, \epsilon_R)$ -sufficient for the dynamics of  $M$ , then approximate policy iteration with approximation operator  $\mathcal{H}_\phi$  starting from any initial policy  $\pi_0 \in \Pi_\phi^D$  satisfies*

$$\limsup_{k \rightarrow \infty} \|Q^* - Q^{\pi_k}\|_\infty \leq \frac{2\gamma^2}{(1-\gamma)^3} (\epsilon_R + \gamma\epsilon_P K_{\phi,V}). \quad (3)$$

where  $K_{\phi,V}$  is an upper bound of the value Lipschitz constant as defined in Appendix B.

**Transferring Model to Get Better Representation in Target.** Although Proposition 6 shows that learning auxiliary dynamics models benefits representation learning, finding the optimal solution is non-trivial since one still has to learn  $\hat{P}$  and  $\hat{R}$ . Therefore, the main idea of our algorithm is to transfer the dynamics models  $\hat{P}, \hat{R}$  from the source task to the target task, to significantly ease the learning in the target task. Theorem 8 below guarantees that transferring the dynamics models is feasible. Our experimental result in Section 6 verifies that learning with transferred and fixed dynamics models outperforms learning with randomly initialized dynamics models.

**Theorem 8** (Transferable Dynamics Models). *Consider a source task  $M^{(S)}$  and a target task  $M^{(T)}$  with deterministic transition functions. Suppose  $\phi^{(S)}$  is sufficient for  $(P_a^{(S)}, R_a^{(S)})_{a \in \mathcal{A}}$  with functions  $\hat{P}_a, \hat{R}_a$ , then there exists a representation  $\phi^{(T)}$  satisfying  $\hat{P}_a(\phi(o)) = \mathbb{E}_{o' \sim P_a^{(T)}}[\phi(o')]$ ,  $\hat{R}_a(\phi(o)) = R_a^{(T)}(o)$ , for all  $o \in \mathcal{O}^{(T)}$ , and  $\phi^{(T)}$  is sufficient for learning in  $M^{(T)}$ .*

Theorem 8 shows that the learned latent dynamics models  $\hat{P}, \hat{R}$  are transferable from the source task to the target task. For simplicity, Theorem 8 focuses on exact sufficiency as in Proposition 6, but it can be easily extended to  $\epsilon$ -sufficiency if combined with Theorem 7. Proofs for Proposition 6, Theorem 7 and Theorem 8 are all provided in Appendix C.

**Trade-off between Approximation Complexity and Representation Complexity.** As suggested by Proposition 6, fitting policy-independent dynamics encourages the representation to be sufficient for learning, but not necessarily linearly sufficient. Therefore, we suggest using a *non-linear policy/value head* following the representation to reduce the approximation error. Linear sufficiency can be achieved if  $\phi$  is made linearly sufficient for  $P_\pi$  and  $R_\pi$  for all  $\pi \in \Pi_\phi^D$ , where  $P_\pi$  and  $R_\pi$  are transition and reward functions induced by policy  $\pi$  (Proposition 10, Appendix B). However, using this method for transfer learning is expensive in terms of both computation and memory, as it requires to learn  $P_\pi$  and  $R_\pi$  for many different  $\pi$ 's and store these models for transferring to the target task. Therefore, there is a trade-off between approximation complexity and representation complexity. Learning a linearly sufficient representation reduces the complexity of the approximation operator. But it requires more complexity in the representation itself as it has to satisfy much more constraints. To develop a practical and efficient transfer method, we use a slightly more complex approximation operator (non-linear policy head) while keeping the auxiliary task simple and easy to transfer across tasks. Please see Appendix B for more detailed discussion about linear sufficiency.

## 5 RELATED WORK

**Transfer RL across Observation Feature Spaces.** Transferring knowledge between tasks with different observation spaces has been studied for years. Many existing approaches (Taylor et al., 2007; Mann & Choe, 2013; Brys et al., 2015) require an explicit mapping between the source and target observation spaces, which may be hard to obtain in practice. Raiman et al. (2019) introduce network surgery that deals with the change in the input features by determining which components of a neural network model should be transferred and which require retraining. However, it requires knowledge of the input feature maps, and is not designed for drastic changes, e.g. vector to pixel. Sun et al. (2020) propose a provably sample-efficient transfer learning algorithm that works for different observation spaces without knowing any inter-task mapping, but the algorithm is mainly designed for tabular RL and model-based RL which uses the model to plan for a policy, different from our setting. Gupta et al. (2017) achieve transfer learning between two different tasks by learning an invariant feature space, with a key time-based alignment assumption. We empirically compared this method with our proposed transfer algorithm in Section 6. Our work is also related to state abstraction in block MDPs, as studied by Zhang et al. (2020a). But the problem studied in Zhang et al. (2020a) is a multi-task setting where the agent aims to learn generalizable abstract states from a series of tasks. Another related topic is domain adaptation in RL (Higgins et al., 2017; Eysenbach et al., 2020; Zhang et al., 2020b), where the target observation space (e.g. real world) is different from the source observation (e.g. simulator). However, domain adaptation does not assume drastic observation changes (e.g. changed dimension). Moreover, the aim of domain adaptation is usually zero-shot generalization to new observations, thus prior knowledge or a few samples of the target domain is often needed (Eysenbach et al., 2020).

**Representation Learning in RL.** In environments with rich observations, representation learning is crucial for the efficiency of RL methods. Learning unsupervised auxiliary tasks (Jaderberg et al., 2016) is shown to be effective for learning a good representation. The relationship between learning

policy-dependent auxiliary tasks and learning good representations has been studied in some prior works (Bellemare et al., 2019; Dabney et al., 2020; Lyle et al., 2021), while our focus is to learn policy-independent auxiliary tasks to facilitate transfer learning. Using latent prediction models to regularize representation has been shown to be effective for various types of rich observations (Guo et al., 2020; Lee et al., 2019). Gelada et al. (2019) theoretically justify that learning latent dynamics model guarantees the quality of the learned representation, while we further characterize the relationship between representation and learning performance, and we utilize dynamics models to improve transfer learning. Zhang et al. (2020b) use a bisimulation metric to learn latent representations that are invariant to task-irrelevant details in observation. As pointed out by Achille & Soatto (2018), invariant and sufficient representation is indeed minimal sufficient, so it is an interesting future direction to combine our method with bisimulation metric to learn minimal sufficient representations. There is also a line of work using contrastive learning to train an encoder for pixel observations (Srinivas et al., 2020; Yarats et al., 2021; Stooke et al., 2021), which usually pre-train an encoder based on image samples using self-supervised learning. However, environment dynamics are usually not considered during pre-training. Our algorithm can be combined with these contrastive learning approaches to further improve learning performance in the target task.

## 6 EXPERIMENTAL EVALUATION

We empirically evaluate our transfer learning algorithm in various environments and multiple observation-change scenarios. Detailed experiment setup and hyperparameters are in Appendix E.

**Baselines.** To verify the effectiveness of our proposed transfer learning method, we compare our transfer learning algorithm with 4 baselines: (1) *Single*: a single-task base learner. (2) *Auxiliary*: learns auxiliary models from scratch to regularize representation. (3) *Fine-tune*: loads and freezes the source policy head, and retrains an encoder in the target task. (4) *Time-aligned* (Gupta et al., 2017): supposes the target task and the source task proceed to the same latent state given the same action sequence, and pre-trains a target-task encoder with saved source-task trajectories. More details of baseline implementations are in Appendix E.1.1.

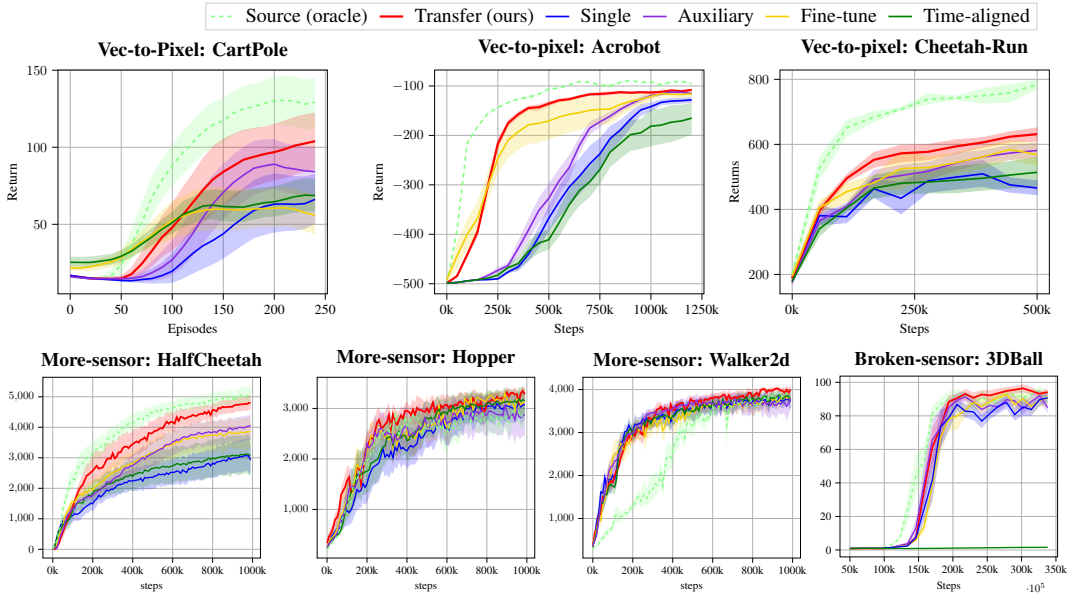
**Scenarios.** As motivated in Section 1, there are many scenarios where one can benefit from transfer learning across observation feature spaces. We evaluate our proposed transfer algorithm in 7 environments that fit various scenarios, to simulate real-world applications:

- (1) *Vec-to-pixel*: a novel and challenging scenario, where the source task has low-dimensional vector observations and the target task has pixel observations. We use 3 vector-input environments CartPole, Acrobot and Cheetah-Run as source tasks, and use the rendered image in the target task.
- (2) *More-sensor*: another challenging scenario where the target task has a lot more sensors than the source task. We use 3 MuJoCo environments: HalfCheetah, Hopper and Walker2d, whose original observation dimensions are 17, 11 and 17, respectively. We add mass-based inertia and velocity (provided by MuJoCo’s API), resulting in 145, 91, 145 dimensions in the corresponding target tasks.
- (3) *Broken-sensor*: we use an existing game 3DBall contained in the Unity ML-Agents Toolkit (Julliani et al., 2018), which has two different observation specifications that naturally fit our transfer setting: the source observation has 8 features containing the velocity of the ball; the target observation does not have the ball’s velocity, thus the agent has to stack the past 9 frames to infer the velocity. Please see Appendix E.1.2 for more detailed descriptions of all the 7 environments.

**Base DRL Learners.** What we propose is a transfer learning mechanism that can be combined with any existing DRL methods. For environments with discrete action spaces (CartPole, Acrobot), we use the DQN algorithm (Mnih et al., 2015), while for environments with continuous action spaces (Cheetah-Run, HalfCheetah, Hopper, Walker2d, 3DBall), we use the SAC algorithm (Haarnoja et al., 2018). To ensure a fair comparison, we use the same base DRL learner with the same hyperparameter settings for all tested methods, as detailed in Appendix E.1.3. As is common in prior works, our implementation of the RL algorithms is mostly a proof of concept, thus many advanced training techniques are not included (e.g. Rainbow DQN).

**Results.** Experimental results on all tested environments are shown in Figure 3. We can see that our proposed transfer method learns significantly better than the single-task learner, and also outperforms all baselines in the challenging target tasks. Our transfer method outperforms Auxiliary since it transfers dynamics model from the source task instead of learning it from scratch, and outperforms Fine-tune since it regularizes the challenging encoder learning with a model-based regularizer.

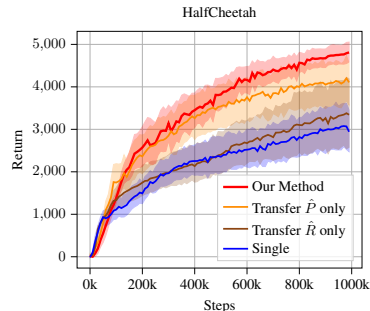




**Figure 3:** Our proposed transfer method outperforms all baselines in target tasks over all tested scenarios. (The dashed green lines are the learning curves in source tasks.) Results are averaged over 10 random seeds.

The Time-aligned method, although requires additional pre-training that is not shown in the figures, does not work better than Single in most environments, because the time-based alignment assumption may not hold as discussed in Appendix E.1.1. In some environments (e.g. Hopper, Walker2d, 3DBall), our transfer algorithm even achieves better asymptotic performance than the source-task policy, which suggests that our method can be used for improving the policy with incremental observation design. *To the best of our knowledge, we are the first to achieve effective knowledge transfer from a vector-input environment to a pixel-input environment without any pre-defined mappings.*

**Ablation Study and Hyper-parameter Test.** To verify the effectiveness of proposed transfer method, we conduct ablation study and compare our method with its two variants: only transferring the transition model  $\hat{P}$  and only transferring the reward model  $\hat{R}$ . Figure 4 shows the comparison in HalfCheetah, and Appendix E.2 demonstrates more results. We find that all the variants of our method can make some improvements, which suggests that *transferring  $\hat{P}$  and  $\hat{R}$  are both effective designs for accelerating the target task learning.* Figure 6 in Appendix E.2 shows another ablation study where we investigate different selections of model regularizers and policy heads. In Algorithm 2, a hyper-parameter  $\lambda$  is needed to control the weight of the transferred model-based regularizer. Figure 7 in Appendix E.2 shows that, for a wide range of  $\lambda$ 's, the agent consistently outperforms the single-task learner.



**Figure 4:** Ablation Study

**Potential Limitations and Solutions.** As Figure 3 shows, in some environments such as HalfCheetah, our transfer algorithm significantly outperforms baselines without transfer. But in Walker2d, the improvement is less significant, although transferring is still better than not transferring. This phenomenon is common in model-based learning (Nagabandi et al., 2018), as state predicting in Walker2d is harder than that in HalfCheetah due to the complexity of the dynamics. Therefore, we suggest using our method to transfer when the learned models ( $\hat{P}$ ,  $\hat{R}$ ) in the source task are relatively good (error is low). More techniques of improving model-based learning, such as bisimulation (Zhang et al., 2020b; Castro, 2020), can be applied to further improve the transfer performance.

## 7 CONCLUSION

In this paper, we identify and propose a solution to an important but rarely studied problem: transferring knowledge between tasks with drastically different observation spaces where inter-task mappings are not available. We propose to learn a latent dynamics model in the source task and transfer the model to the target task to facilitate representation learning. Theoretical analysis and empirical study justify the effectiveness of the proposed algorithm.

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