



# SIRIUS: Contextual Sparsity with Correction for Efficient LLMs

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## Abstract

With the blossom of large language models (LLMs), inference efficiency becomes increasingly important. Various approximation methods are proposed to reduce the cost at inference time. Contextual Sparsity (CS) is appealing for its training-free nature and its ability to reach a higher compression ratio seemingly without quality degradation. However, after a comprehensive evaluation of contextual sparsity methods on various complex generation tasks, we find that although CS succeeds in prompt-understanding tasks, CS significantly degrades the model performance for reasoning, deduction, and knowledge-based tasks. Despite the gap in end-to-end accuracy, we observed that sparse models often share general problem-solving logic and require only a few token corrections to recover the original model performance. This paper introduces SIRIUS<sup>1</sup>, an efficient correction mechanism, which significantly recovers CS models quality on reasoning tasks while maintaining its efficiency gain. SIRIUS is evaluated on 6 models with 8 difficult generation tasks in reasoning, math, and coding and shows consistent effectiveness and efficiency. Also, we carefully develop a system implementation for SIRIUS and show that SIRIUS achieves roughly 20% reduction in latency for 8B model on-chip and 35% reduction for 70B model offloading. We will open-source our implementation once published.

## 1 Introduction

Large Language Models (LLM), such as [22] (GPT-4), [31] (Gemini), and [33] (Llama) have demonstrated their proficiency in a wide range of natural language processing applications. Exploiting the model sparsity is a natural way to reduce the model parameter size and computational cost with a long history [13, 32]. More recently, many studies have shown that *contextual sparsity* [20, 16, 7, 14], which highly correlates to the prompt or the context, can greatly speed up LLM inference without quality degradation.

However, in this paper, we first demonstrate a critical and fundamental problem with *contextual sparsity* (CS): while generally robust in classification tasks and generation tasks that mainly rely

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<sup>1</sup>We draw inspiration from the astronomical concept, in which SIRIUS refers to a two-body star system, where one is the brightest star ever detected, while the other is a dim star.

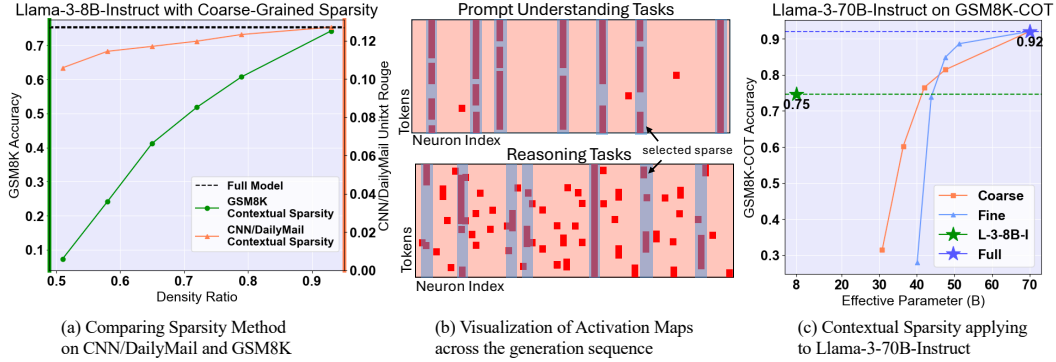


Figure 1: Contextual sparse models struggle at challenging text generation tests that require high-level reasoning and understanding, e.g. GSM8K. On these tasks, contextually sparse models lead to significant quality degradation. In (a), we contrast CS Llama-3-8B-Instruct on GSM8K (green) and CNN DailyMail (coral). (b) Contextual Sparsity Llama-3-70B-Instruct crashes at 50% global sparsity, making the smaller dense model Llama-3-8B-Instruct (green star) a significantly more efficient choice than the sparse 70B model. (c) Sparse model crashing at reasoning tasks has patterns, and ideally only correcting 11% unlikely tokens recovers the sparse model performance fully.

on prompt understanding (e.g., summarization, chat question-answering), we found that CS models struggle at high-level reasoning and understanding generation tasks. In Figure 1 (a), we contrast between the Text Summarization task (CNN/DailyMail) and Arithmetic Reasoning (GSM8K) with contextual sparsity methods on Llama-3-8B-Instruct. Varying sparsity levels, Llama-3-8B-Instruct with contextual sparsity performs consistently worse on GSM8K compared to CNN/DailyMail. CS on GSM8K crashes way earlier than summarization, which CS shows robust performance. Furthermore, shown in Figure 1 (b), the 50% Llama-3-70B-Instruct sparse model still has 4X the parameter size compared to the smaller dense model (Llama-3-8B-Instruct), while still performing worse on GSM8K-COT, rendering contextual sparsity utterly not useful for complex reasoning tasks. We notice that the overall reasoning pathway of these sparse models is usually sound, while the fatal mistake happens in the middle and propagates toward the end.

In this paper, we first conduct a simple experiment with CSparse Llama-3-8B-Instruct on GSM8K with the full model to check the sparse token-by-token. Surprisingly, only 6% tokens of the sparse model’s generation corrected recovers most GSM8K accuracy. We are inspired by the observation and systematically design SIRIUS, a correction method. SIRIUS is empirically evaluated SIRIUS on 6 different models with 8 different Reasoning tasks and showed that SIRIUS is generally effective and efficient. On GSM8K and Llama-3-8B-Instruct specifically, we boost the fine-grained sparsity from 58% to 72% with 4% increase in effective parameter size and coarse-grained sparsity from 38% to 70% with the cost of 5% effective parameter size. SIRIUS is also shown to deliver the promised efficiency in both on-chip and offloading settings.

## 2 Related Works and Problem Formulation

In this section, we present the classification of the prior Contextual Sparsity methods. Additionally, we narrate important efficiency metrics in Appendix A.3, and show why Speculative Decoding applying directly to sparse correction would lead to substantial inefficiency Appendix A.4. For extended related works on model compression, contextual sparsity, and speculative decoding, we present in Appendix A.1.

Contextual sparsity (CS) methods are usually training-free, easy to use, and seemingly effective, making them highly attractive to ML practitioners looking to reduce LLM inference costs. The contextual sparsity selection is as follows: given the context, only a limited number of the most

Table 2: We show the difference between cases when Contextual Sparsity (CS) succeeds or fails. CS is generally good at prompt understanding tasks and tasks that measure the trustworthiness of the language models while not good at tasks that require reasoning and world knowledge understanding. MMLU\* refers to MMLU-Flan-COT.

Where CS Succeeds Experiment Settings	CNN/DailyMail Unitxt Rouge	CoQA EM/F1	TruthfulQA Rouge-1/2 ACC
<b>Llama-3-8B-Instruct</b>	0.1237	0.6153/0.7825	0.4945/0.3647
<b>Llama-3-8B-Instruct-CSparse</b>	0.1144	0.6633/0.7977	0.4725/0.3403
<b>Llama-3-8B-Instruct-FSparse</b>	0.1166	0.6625/0.7984	0.5043/0.3305
Where CS Fails Experiment Settings	GSM8K ACC (strict/flexible)	HumanEval Pass@1 (GD)	MMLU* Accuracy
<b>Llama-3-8B-Instruct</b>	0.7551/0.7544	0.560	0.6231
<b>Llama-3-8B-Instruct-CSparse</b>	0.3859/0.3874	0.207	0.5558
<b>Llama-3-8B-Instruct-FSparse</b>	0.5868/0.5891	0.457	0.5304

relevant neurons are selected based on the input activation. The rest contributed to the output far less is discarded. We refer to two main directions of contextual sparsity methods as

- **Coarse-grained Sparsity** (CSparse) Methods ([7]) - that within the same input prompt, the sparsity pattern is fixed for all tokens generated.
- **Fine-grained Sparsity** (FSparse) Methods ([14]) - that exploits the per-token sparsity to save resources.

### 3 Observations

We build our 50% neuron sparsity implementation<sup>2</sup> of fine-grained sparsity based on [14] and coarse-grained sparsity based on [7].

For tasks on prompt understanding, CS generally performs well and gives consistent and strong output. We evaluate CS models on machine summarization (CNNDailyMail [26]), and Conversational Question Answering (CoQA [24]). On the other hand, contextual sparsity severely struggles when the generation tasks rely solely on the model’s own reasoning and deduction ability, or the model’s world knowledge understanding ability. Here we show the Llama-3-8B-Instruct and the Llama-2-7B-Chat models in Table 2. For a detailed analysis of results, we present more information in Appendix B.1, B.2 and B.3. We visually inspect extensive cases where the sparse model and dense differ in answers, more examples are shown in Appendix B.4. Shown in Figure 3, we found that a very small amount of correction would drastically improve the sparse model performance, showing a steep gradient when the percentage of corrected tokens is small. The experiment verifies our hypothesis that by correcting the small portion of key tokens, the sparse model can meet the large model’s performance.

Table 1: Llama-3-70B-Instruct with Offloading.

Settings	Sparse	Sirius	Full
<b>Performance</b>	0.7407	0.8719	0.9014
<b>Latency (s)</b>	3.57 s	3.68 s	5.72 s
<b>Ratio to Full</b>	0.6241	0.6434	1.0

<sup>2</sup>Since [14] doesn’t open-source its implementation and it relies on the threshold for determining the sparsity pattern, replicating the method isn’t straightforward. Using a threshold also increases the difficulty of determining the actual density of the sparse model. Our implementation uses topk on the Gate Layer activations. The rest is implemented as described in the original method.

## 4 Methods

Naturally, letting the sparse model decide when to call the LLM for evaluation would be more flexible, but we show in Appendix C.1 that the sparse model cannot provide a reliable signal for consistently making the decision.

The full model is called once every kernel size. Throughout the inference, the KV cache is shared between the sparse and the full model. Therefore, full passes on its KV cache to benefit the small model’s next chunk. The full model’s KV helps the sparse model’s output, which is evaluated later in the sections. Due to space limit, we place the full Algorithm in Appendix C as Algorithm 1. The LLM evaluation decision is based on comparing the full likelihood against a preset threshold. The overview is drawn in Appendix C Figure 7. Detailed ablation for threshold is in D.3. Also, we found that at the position when the full rejects the sparse’s tokens, the second or third most probable tokens show strong coverage of tokens that can be accepted, and we further improve the efficiency of the SIRIUS efficiency by incorporating a hardware efficient tree building systems, details in C.2.

## 5 Experiments

In this section, we empirically evaluate SIRIUS to correct CS models on various generation tasks in complex reasoning. We show that SIRIUS is consistent in various tasks, effective in helping CS models recover their performance, and efficient in correction with low additional overhead.

**Main Results** - Due to space limits, we only select the best treewidth of SIRIUS for GSM8K, CSQA, and HumanEval for the main results in Table 6. Extensive studies on the rest 5 datasets with different treewidth are presented in the Appendix E. From Table 6, we can see that SIRIUS is consistently effective and efficient across all different classes of tasks. Specifically for Llama-3-8B-Instruct, besides GSM8K, SIRIUS corrects FSparse and CSparse, on CSQA, from 61% and 64% accuracy to 70% with cost only 3% sparsity for FSparse and 7% for CSparse respectively. On HumanEval, SIRIUS corrects FSparse from 45% to 61% with 4% sparsity overhead even surpassing the full model’s performance, and from 20% to 52% with 8% sparsity as cost. Besides, Llama-3-8B-Instruct, SIRIUS corrects all 6 models with additional sparsity overhead smaller than 10% across these three datasets, further showing its strong efficiency. Besides results in Table 6, in Appendix E, we show that SIRIUS consistently shows great effectiveness with high efficiency across the rest of the 5 datasets.

**Wallclock Speedup** - Here we show that Sirius delivers its promised efficiency claim under two different settings, on-chip, and offloading, with two different models, Llama-3-8B-Instruct and Llama-3-70B-Instruct. Details are shown in Table 4. We consider the generation speedup only since contextual sparse methods are sparse mainly in generation, most use full weights for prefilling. For the two settings, we consider the coarse-grained sparsity method Griffin [7] because it open-sourced its implementation. On the other hand, the fine-grained sparsity method [14] relies on a custom CUDA kernel to achieve the target speed up, which they didn’t open-source. The downstream dataset selected is GSM-8K COT, and the input sequence length is around 900. For the measurement on A40, L40, we found that kernel size 10 without tree delivers the best speedup, while a tree of treewidth 4 is built for A100 and H100. On average, Sirius with efficient implementation achieves 20% speedup on average for on-chip settings for Llama-3-8B-Instruct.

Secondly, we consider the offloading setting which is the only way for resource-limited users to run 70B models, which cannot easily fit in GPU clusters other than A100s and H100s. We use a single L40 48GB with a PCIe bus bandwidth of 25 GB/s. Llama-3-70B-Instruct is running on GSM8K-COT. Llama-3-70B-Instruct has roughly 80% of parameters to be MLP, which gives the theoretical APU for Griffin to be 0.6. Sparse + Sirius achieves 15.4 out of 16 average advance length, which in theory gives 0.649 APU, which is roughly what our system achieved.

Table 3: We show SIRIUS effectiveness and efficiency in the following table. We select GSM8K for Arithmetic Reasoning, CSQA for Commonsense Reasoning, and HumanEval for code generation. Under the "SIRIUS Perf. " column, A(B) is shown. A denotes the accuracy after SIRIUS correction in the dataset evaluated, while (B) represents the optimal treewidth selected under the current model dataset settings. Under the column of "AAL", X/Y is shown, where X is the AAL, while Y is the period.

GSM8K (Arithmetic Reasoning)						
Model	Full Perf.	CSparse Perf.	CSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.7536	0.3844	0.65	0.7051 (8)	15.22/16	0.706
Llama-3-8B	0.4966	0.2085	0.65	0.4177 (8)	15.29/16	0.703
Model	Full Perf.	FSparse Perf.	FSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.7536	0.5868	0.76	0.7278 (4)	15.37/16	0.807
Llama-3-8B	0.4966	0.3199	0.76	0.4579 (2)	15.03/16	0.825
CSQA (Commonsense Reasoning)						
Model	Full Perf.	CSparse Perf.	CSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.7073	0.6470	0.58	0.7076 (8)	14.76/16	0.657
Llama-3-8B	0.6437	0.5585	0.58	0.6429 (8)	15.43/16	0.628
Model	Full Perf.	FSparse Perf.	FSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.7073	0.6158	0.72	0.7043 (8)	15.66/16	0.753
Llama-3-8B	0.6437	0.533	0.72	0.6388 (1)	15.00/16	0.786
HumanEval (Coding)						
Model	Full Perf.	CSparse Perf.	CSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.561	0.207	0.65	0.524 (8)	14.67/16	0.733
Llama-3-8B	0.262	0.067	0.65	0.243 (8)	15.10/16	0.691
Model	Full Perf.	FSparse Perf.	FSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.561	0.457	0.76	0.616 (6)	15.42/16	0.804
Llama-3-8B	0.262	0.189	0.76	0.298 (6)	15.54/16	0.797

Table 4: Performance and Speedup Ratios on GSM8K-COT with Different Hardware Configurations.

Settings	ACC	A40	Ratio	L40	Ratio	A100	Ratio	H100	Ratio
CSparse	0.3601	20.7 ms	0.66	15.6 ms	0.67	9.6 ms	0.72	6.6 ms	0.76
Sirius	0.7127	24.1 ms	0.78	18.2 ms	0.78	11.1 ms	0.83	7.7 ms	0.88
Full	0.7612	30.9 ms	1.0	23.2 ms	1.0	13.3 ms	1.0	8.6 ms	1.0

## 6 Conclusion

We observe that contextual sparse methods significantly degrade for reasoning and deduction tasks. With similar parameter size, the degradation from these sparsity is shown to be more severe for more well-trained models. However, we find that the degradation from contextual sparse models can theoretically be recovered with 10% token corrected by original model. Where to locate these small amount of tokens to effectively corrected by the full model is a difficulty. SIRIUS, an efficient correction mechanism, enables accurate LLM inference with contextual sparsity. With roughly 11% to 18% sparsity increase, SIRIUS improves fine-grained and coarse-grained sparsity significantly in their performance while maintaining their efficiency gain, reaching a reasonable tradeoff between performance and efficiency. We hope that this understanding inspires future work in this area.

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## A Additional Background

### A.1 Extended Related Works

**Pruning in LLM** Sparsity in neural networks has been widely studied. In the context of LLM, sparsity is studied under two branches - unstructured and structured. On the unstructured sparsity side, [8] (SparseGPT) is a ground-breaking work that formulates pruning as a solving a series of sparse regression problems and proposes a fine solver for the problem. [30] (Wanda) introduces input activations into the pruning decision and achieves strong results in inducing LLM sparsity. On the structured side, LLMPruner [21] and Sheared Llama [35] each proposes different meticulous pruning algorithms and restoring weights through either parameter-efficient finetuning or efficient full weights training.

**Contextual Sparsity** Many recent works on LLM sparsity notice that the sparse pattern is highly related to the input or context. Deja Vu [20] revealed that for OPT models [36] the contextual sparsity is as high as 85%, meaning that 80% of the parameters can be pruned that won’t hurt the



token decoded quality given the prompt. Deja Vu formulates the problem of neuron selection as a near-neighbor search problem: finding neurons that are the most similar to the input activations. PowerInfer [28] extends the contextual sparsity to benefit the heterogeneous setting. Compared to the rest of the model, MLP layers tend to possess significant contextual sparsity and can be effectively exploited in a training-free manner. Concurrently, Griffin [7] discovers the phenomenon of flocking, where MLP neurons have temporal locality, where given a fixed prompt, similar neurons tend to get activated throughout the following generation. Flocking is shown to occur in most activation types and open-source LLMs. Griffin selects the same set of heated neurons with 50% sparsity throughout the generation of each input prompt, which we refer to as coarse-grained sparsity. CATS [14] successfully exploits per-token contextual sparsity in the MLP layers for inference latency reduction. They resample a new set of neurons per every new input token, which we categorize it as fine-grained contextual sparsity. Our paper mainly focuses on the training-free MLP sparsity techniques. Although these recent works show minimal accuracy degradation in classification and easy text summarization tasks, they both severely degrade in generation quality under tasks that require high-level reasoning and understanding ability. Our work serves as a low-cost complementary tool, aiming to push these elegant and promising techniques for mainstream use cases.

Also, previous contextual sparsity methods haven't fully and exhaustively evaluated their benefits and limitations in downstream generation tasks. To fully study this technique, we extensively go through open-source LLMs in diverse performance and sizes on diverse generation tasks and datasets to locate where these sparse models maintain the performance or fail.

**Speculative Decoding** Besides model compression techniques, Speculative decoding [15], [2], [12] is another important LLM inference latency reduction method. Compared to LLM, small transformer models are much more computationally accessible and can effectively model short-range tokens. Therefore, smaller models are asked to speculate short-term future tokens, which the LLM takes in parallel to trade in FLOPs with memory loading time. During verification, most speculative decoding methods pursue lossless acceleration, leading to frequent rollback during rejection. In contrast, Sirius solves a very different problem. Our method aims to maximally preserve the efficiency of sparse models while boosting its performance. Sparse models, pruned directly from LLM, are much stronger at modeling a longer range of text than draft models, thus requiring much less help from the LLM. Our work aims to find the minimum amount of LLM overhead while boosting its performance to the LLM level. Given the resemblance and relevance of Speculative Decoding to our method Sirius, we will elaborate more in-depth on their differences and Speculative Decoding's inefficiencies when it comes to helping the Sparse method in A.4.

## A.2 Why 0.76?

Here we explain in greater detail why Sirius can achieve  $APU < 0.76$  for Llama-3-8B with CSparse on GSM8K. For a threshold of 0.1, Sirius can correct Llama-3-8B coarse-grained sparsity from 20.85% to 43.9%, compared to the 49.66% full model. With a period of 16 tokens ( $\gamma = 15$ ), Sirius on average can accept 13.4 tokens out of a kernel size of 16 and over 9 tokens out of a kernel size of 10, translating to  $APU < 0.76$ , significantly lower than SD does.

## A.3 Average Parameters Used Per Token

A key metric is used to evaluate the efficiency of our proposed method, the Average Parameter Used per token decoded (later referred to as APU). LLM inference is memory I/O bound [15], [12]. The latency of generating every single token is dominated by the memory loading time from the GPU HBM to SRAM. On the other hand, SIRIUS relies on full model parallel verifying a chunk of tokens. Although from the FLOPs standpoint, the amount of compute performed per evaluation step is the number of input token times of a single token input process, the latency of parallel verification is still roughly the same as taking a single token (Verified further in 10, length 64 is only 1.1 ms longer than length 1), because the inference is memory bound.

SIRIUS operates in the memory-bound regime (single inference sequence length smaller than or equal to 64). Thus, the average parameter count of a model gives us a rough judgment of the latency of inference. Formally, for a full LLM to have  $C_{full}$  number of parameters, and its sparse counterpart of a certain predetermined sparsity  $C_{sparse}$ . The average advancement length (later we refer to as AAL) in the number of tokens between two consecutive LLM corrections can be represented as  $n_{AAL}$ . The average parameters used per token (APU) are the following

$$APU = \frac{n_{sparse}C_{sparse} + C_{full}}{n_{AAL}} \quad (1)$$

We want the metric to be as small as possible, and obviously, we want  $n_{AAL}$  to be as large as possible.

Another thing to note is that we always compare the system’s APU against the full model’s APU, which is  $C_{full}$ . If we divided the above equation by  $C_{full}$ , we can have an equivalent parameter density of the system defined based on  $I_{globalsparsity}$ , which is  $C_{sparse}/C_{full}$ .

$$\text{Effective Density} = \frac{n_{sparse}I_{globalsparsity} + 1}{n_{AAL}} \quad (2)$$

Later, if we use period  $n_{period}$ , the equation can be rewritten as

$$\text{Effective Density} = \frac{(n_{period} - 1)I_{globalsparsity} + 1}{n_{AAL}} \quad (3)$$

Later when presenting SIRIUS, we mainly specify  $n_{period}$  with  $n_{AAL}$  to evaluate its efficiency. Notice that  $I_{globalsparsity}$  is determined by the sparsity method, SIRIUS cannot change it anymore.

#### A.4 Why Not Using the Speculative Decoding to Correct the Sparse Model?

When Speculative Decoding is used to correct sparse using the full model, we will show that the efficiency of the overall process will be largely limited. We followed the common practice from speculative decoding and measured the acceptance rate on different datasets C4 [23] and GSM8K [6]. Take the Coarse-grained sparse model as an example. For Llama-3-8B as the full model, the 50% sparse (APU 0.65) model will produce an acceptance rate of 0.71 on C4 and 0.89 on GSM8K. Speculative decoding also use parallel verification in the period-basis. Naturally, to keep the system efficiency high, we need to (1) enlarge the period and (2) increase the average number of tokens accepted (AAL) given the gamma (period - 1) value. Take the acceptance rate of 0.89 on GSM8K as an example, following the formulation in [15], we can calculate the expected number of accepted tokens for every gamma term in the Speculative Decoding literature.  $AAL = \frac{1-\alpha^{(\gamma+1)}}{1-\alpha}$ . The trend (green) is plotted in Figure 2

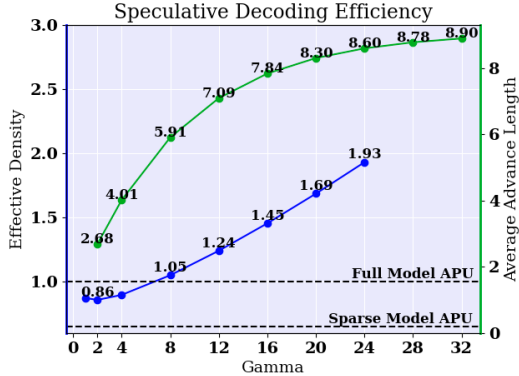


Figure 2: Speculative Decoding has limitation in efficiency when correcting sparse models.

We can notice the trend that the average advance length starts to plateau as the gamma becomes larger. Take the gamma of 16 as an example, the period is then 17. The average advance length is only 7.84. The APU is  $(16 * 0.65 + 1)/7.84 = 1.45$ , which is larger than the full model 1. The blue line in Figure 2 shows the relationship between APU and gamma.

Because of the plateauing effect, for an acceptance rate of 0.89, the best gamma is 2 (period = 3). The optimal APU is 0.86, compared with 0.65 coarse-grained sparse APU. A similar picture can be applied to Fine-grained sparsity as well. The key reasons for the observation are two-fold: (1) the

contextually sparse models are too big to be the draft model of the speculative decoding system and to have a large period; (2) Speculative decoding preserves the original model's performance so that the acceptance criteria are usually very strict, which is also not suitable for large period and high average advance length. Following the same spirit, [29] also uses a large draft model to do self-speculation, but for them, the authors select  $\gamma = 1$  to achieve the optimal speedup of their system. In contrast, SIRIUS brings  $< 0.76$  APU in this case with period  $\geq 10$ . (Details in Appendix A.2)

## B Supplemental Observation

In this section, we present a detailed study of the strengths and weaknesses of Contextual Sparsity (CS). B.1 presents the strengths of CS. B.2 presents the weaknesses of CS. In Section ??, we show that given the similar parameter size, the more well-trained the model is, the more CS degradation will be for the model. B.4 shows our findings when looking into the failure cases of CS model in complex reasoning tasks.

Text generation is the main use case for these sparse models, which optimizes inference for the dense counterpart. Therefore, we choose not to look into text classification and language modeling ability, focusing on generation tasks.

In the following series of experiments, we build our implementation<sup>3</sup> of fine-grained sparsity based on [14] and coarse-grained sparsity based on [7]. The default sparsity for both methods is 50% for the MLP component of the model (whole MLP for coarse-grained sparsity and Up and Down linear layers only for fine-grained sparsity). We mainly use this default setting in most experiment tables in the paper without explicitly mentioning, or otherwise, we will explicitly specify the different sparsity levels we used.

### B.1 Contextual Sparsity: Where Does It Succeed?

For tasks on prompt understanding, CS generally performs well and gives consistent and strong output. We evaluate CS models on machine summarization (CNNDailyMail [26]), and Conversational Question Answering (CoQA [24]).

The results show that the correctly selected contextual sparsity in the MLP layers and the full attention layers can fully extract and understand the local prompt information. More details are presented in Figure 4, where we show that by varying the sparsity level, the language model’s performance on CNN/DailyMail is robust even when the activation sparsity drops to below 20%, which translates to around 44% global density.

For tasks accessing factuality and hallucination, we select the generation portion of the TruthfulQA dataset [17]. Results are shown in Table 2, where we evaluate the techniques on 5 different LLMs. Interestingly, we find that the Fine-grained sparsity is often better than the dense model baseline across different models. This finding is consistent with previous works Laser [27] and Dola [4]. They both observed that compressing the original LLM in a carefully designed way would lead to improvement in factuality and better de-hallucination. Laser comes from the low-rank approximation of the MLP layers, while Dola proposes a factuality-aware layer-skipping algorithm. Based on their findings, hallucination

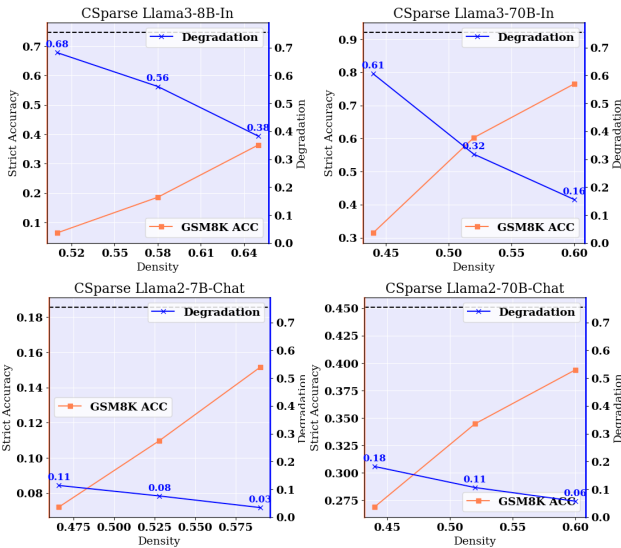


Figure 3: Given the similar model parameters, the more well-trained the model is, the worse the degradation would be. (Compare the figures vertically between Llama-3 and Llama-2 family models).

<sup>3</sup>Since [14] doesn’t open-source its implementation and it relies on the threshold for determining the sparsity pattern, replicating the method isn’t straightforward. Using a threshold also increases the difficulty of determining the actual density of the sparse model. Our implementation uses topk on the Gate Layer activations. The rest is implemented as described in the original method.

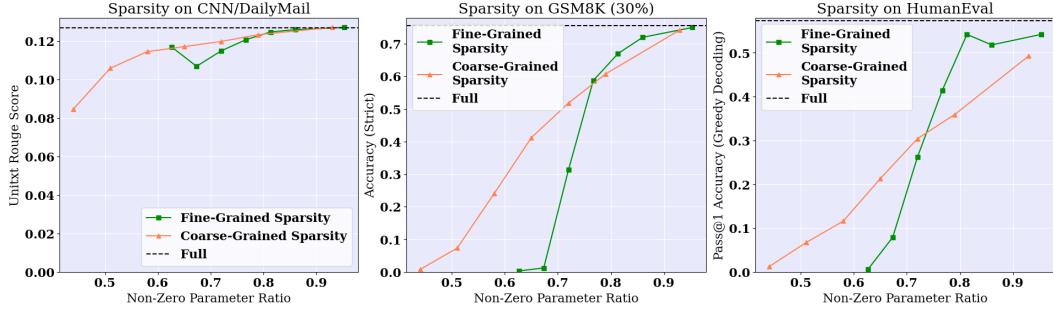


Figure 4: We contrast between Contextual Sparsity on prompt understanding task and complex generation tasks that require reasoning. (a) Both CSparse and FSparse are robust on CNN/DailyMail for various sparsity; (b) and (c) Show that both CSparse and FSparse crash on GSM8K and HumanEval at the global sparsity that they are still robust in prompt understanding tasks.

occurs when parts of the weights aren't as well-versed in the given input as the other parts. They expose the "averaging" effect that blurs the factuality of the output. Removing these neurons gives rise to better factuality and less hallucination. Our studies look at the same problem from a neuron sparsity standpoint.

## B.2 Contextual Sparsity: Where Does It Fail?

On the other hand, contextual sparsity severely struggles when the generation tasks rely solely on the model's own reasoning and deduction ability, or the model's world knowledge understanding ability. Here we show the Llama-3-8B-Instruct and the Llama-2-7B-Chat models in Table 2, refer to Table 12 for evaluations on more models.

Notice that since fine-grained sparsity method needs the activation from Gate MLP for selecting sparsity, while coarse-grained sparsity has a predetermined pattern after prefilling and can sparsify the Gate MLP. Even though both are at 50% activation sparsity, the coarse-grained sparsity method effectively achieves higher parameter savings than fine-grained sparsity in practice. Here we evaluate the sparse techniques using 5-shot CoT on the GSM8K dataset [6]. We found that across all the models we evaluated, both sparsity methods lead to significant accuracy degradation. Although code generation is not directly an arithmetic reasoning task, we found it useful to include, it since coding is a comprehensive evaluation of the language model's prompt understanding, reasoning, and planning to solve complex tasks. Therefore, we include HumanEval [3]. We found that both sparsity methods exhibit similar performance degradation when it comes to coding. Shown in Figure 4, two tasks see sparsity significantly drop performance after 50% activation sparsity.

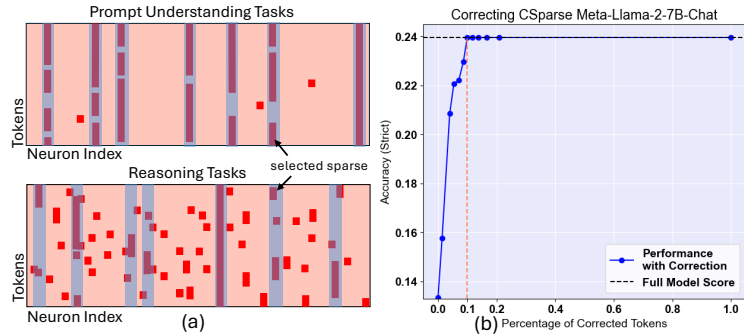


Figure 5: (a) Illustration on why Contextual Sparsity has uneven performance on different tasks. The activation heat map (red) has the brighter the color the larger in magnitude. On top, we also show the neuron sparsity selected. The graph points signify that the pattern in the prompt understanding task is easier to capture. (b) An additional graph of correcting CSparse Llama-2-7B-Chat. It is similar to the previous experiment on 8B. Only 10% tokens being corrected results in complete performance recovery.

For knowledge recall and world knowledge understanding, we specifically test on MMLU-Flan-CoT [5] the CoT text generation version of the MMLU dataset [11]. Table 2 shows the results. Stronger models like Llama-3-8B-Instruct suffer from significant degradation too.

### B.3 Given Similar Parameter Size Well-trained Models Suffer More

We observe another interesting phenomenon: given the similar parameter size, the more well-trained the model is, the more performance degradation contextual sparsity would make on the full models. Here we present two pairs of results. First, we look at the performance between Llama-3-8B-Instruct and Llama-2-7B-Chat with Llama-3-70B-Instruct and Llama-2-70B-Chat. All models are evaluated on GSM8K-COT. We draw these models in CSparse in Figure 3, and the readers can find more results in Appendix D.7. We can see figures from top to bottom, where even at lower density (more elements are not selected), Llama-2-7B-Chat and Llama-2-70B-Chat suffer from less performance degradation (blue) compared to the Llama-3-8B-Instruct and Llama-3-70B-Instruct models. Furthermore, suppose we focus on Llama-3-70B-Instruct for global density at 60% or lower. In that case, the performance (coral) is degraded significantly, which is comparable or even lower to Llama-3-8B-Instruct full model performance at 0.76. Even at 50% density, the 70B model still has more than 40B parameters, much more expensive than the 8B model. The observation fully manifests the difficulty of using CS in complex reasoning tasks.

### B.4 Examples of Failure Cases

<p><b>Question:</b> Marie ordered one chicken meal that costs \$12, 5 packs of milk that costs \$3 each, 4 apples that cost \$1.50 each, and some boxes of pizza. Marie paid a total of \$50. How many boxes of pizza did Marie order if each box costs \$8.50?</p>	<p><b>Question:</b> Janet's ducks lay 16 eggs per day. She eats three for breakfast every morning and bakes muffins for her friends every day with four. She sells the remainder at the farmers' market daily for \$2 per fresh duck egg. How much in dollars does she make every day at the farmers' market?</p>	<p><b>Question:</b> Raymond and Samantha are cousins. Raymond was born 6 years before Samantha. Raymond had a son at the age of 23. If Samantha is now 31, how many years ago was Raymond's son born?</p>
<p><b>Answer:</b> The total cost of the chicken meal, milk, and apples is <math>12 + 5 * 3 + 4 * 1.5 = &lt;&lt;12+5*3+4*1.5=27&gt;&gt;27</math> dollars (33 dollars) ..... <span style="background-color: #90EE90;">Miscalculation</span></p>	<p><b>Answer (Sparse):</b> Janet eats <math>3 + 4 = &lt;&lt;3+4=7&gt;&gt;7</math> eggs per day. She lays <math>16 - 7 = &lt;&lt;16-7=9&gt;&gt;9</math> eggs per day. She sells <math>9 - 7 = &lt;&lt;9-7=2&gt;&gt;2</math> eggs per day. She makes <math>2 * 2 = &lt;&lt;2*2=4&gt;&gt;4</math> dollars per day. #### 4</p>	<p><b>Answer:</b> Samantha is 31, so she is <math>31 - 6 = 25</math> years old. Raymond is <math>25 - 23 = 2</math> years older than Samantha, so he is 25 years old ..... <span style="background-color: #FFD700;">Unreasonable Statement</span></p>
<p><b>Question:</b> A merchant wants to make a choice of purchase between 2 purchase plans: jewelry worth \$5,000 or electronic gadgets worth \$8,000. His financial advisor speculates that the jewelry market will go up 2.5% while the electronic gadgets market will rise 1.2% within the same month. If the merchant is looking to maximize profit at the end of this month by making a choice, how much profit would this be?</p>	<p><b>Answer (Full):</b> Janet eats 3 eggs and bakes 4 eggs, so she has <math>16 - 3 - 4 = &lt;&lt;16-3-4=9&gt;&gt;9</math> eggs left. She sells 9 eggs for \$2 each, so she makes <math>9 * 2 = &lt;&lt;9*2=18&gt;&gt;18</math> dollars. #### 18</p>	<p><b>Question:</b> A candle melts by 2 centimeters every hour that it burns. How many centimeters shorter will a candle be after burning from 1:00 PM to 5:00 PM?</p> <p><b>Answer:</b> The candle will be 4 centimeters shorter after 5:00 PM because it will be 4 hours x 2 centimeters = <math>&lt;&lt;4*2=8&gt;&gt;8</math> centimeters shorter. #### 4 <b>Remarks:</b> There is conflicting statement in reasoning, leading to the wrong end result. <span style="background-color: #FFD700;">Unreasonable Statement</span></p>
<p><b>Answer:</b> The jewelry will increase in value by 2.5% which is <math>5,000 * 0.025 = &lt;&lt;1250 (\$125)&gt;&gt;1250</math> ..... <span style="background-color: #90EE90;">Miscalculation</span></p>	<p><span style="background-color: #FF69B4;">Different Reasoning Path</span></p>	

Figure 6: Examples of contextual sparse model making the identified three different types of mistakes. Most mistakes occur because the model makes calculation mistakes or has a wrong reasoning step compared to the full model. We also observe that there are rare cases where the model makes insensible statements in the middle that make the end result wrong.

We visually inspect extensive cases where the sparse model and dense differ in answers. Generally, the sparse model always produces highly similar answers to the dense model: the similar approach or logic flow when approaching the same problem and even the same number of sentences before the first mistake occurs or in success cases. However, the key differences are usually caused by the following three categories of small token-level mistakes: (1) frequent miscalculation in the intermediate steps, (2) wrong reasoning in intermediate steps, and (3) insensible and random statements. We find failure question-answer pairs provided in Figure 6 for each of the above-summarized cases. These mistakes happen in the middle of arguments and propagate to the wrong end result.

Similar observations can also be found for fine-grained sparse methods with different model types. *Interestingly, we find that even with these mistakes, the sparse model can still fully generate coherent tokens and make further reasoning assuming their prior steps are correct.*

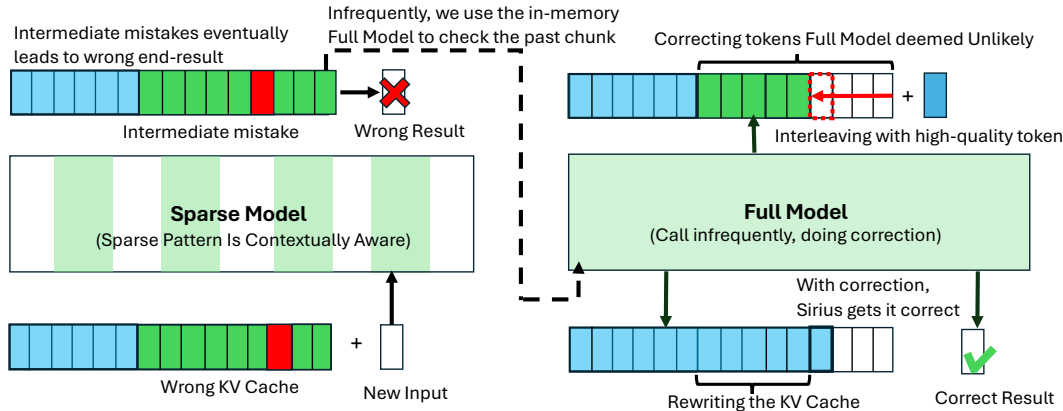


Figure 7: Overview of Sirius. Contextual Sparsity requires full model weights to be placed on the GPU memory. While the sparse model doesn’t perform well on complex reasoning tasks, Sirius uses the Full Model to correct the Sparse model. The full model is called fairly infrequently. During the correction, the Full Model will rewrite the KV Cache, interleave with high-quality tokens to the sparse outputs, and then roll back only when the token is deemed extremely unlikely by the Full Model.

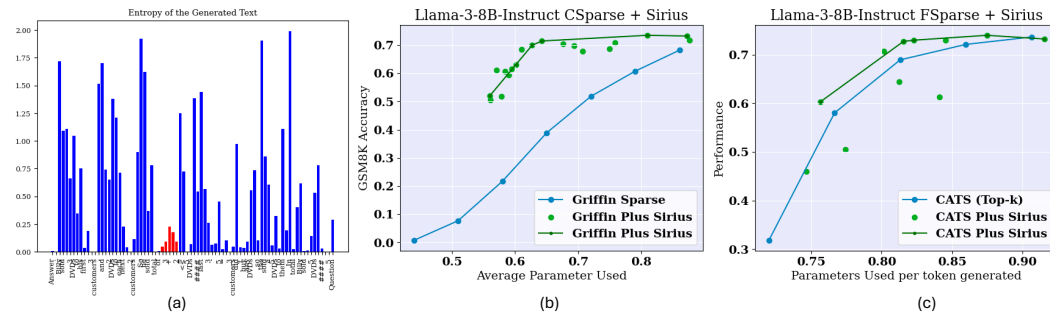


Figure 8: In (a), we present an example that illustrates why the signals from the sparse model are unreliable. It is a figure plotting entropy versus generated tokens. At the tokens where the sparse made the mistake (red), the entropy isn’t in large spikes which signifies chaos and low confidence, rather it is even quite low, compared to nearby entropy spikes. In (b) and (c), we view Sirius as a compression method by itself. We compare Sirius with contextual sparse methods and show that given the same parameter used, Sirius performs better than Contextual Sparse Methods on GSM8K.

## C Supplemental Method

### C.1 Sparse Model’s Self-Awareness Cannot Be Trusted

Intuitively, rather than fixing the  $n_{sparse}$  number, letting the system decide when to call the LLM for evaluation would then give more flexible  $n_{sparse}$ . In other words, the problem becomes how to make the sparse model decide when the LLM can be called. Nevertheless, we argue that the sparse model’s output probability distribution cannot be used as a metric for accuracy decisions.

We empirically experiment with various methods to utilize the information contained in the sparse model’s output distribution. However, it always leads to  $n_{sparse}$  being too short, the single-digit number for GSM8K (around 4 for Llama-3-8B Instruct). setting up the threshold isn’t useful. We then discovered that the sparse model has very limited self-awareness of its own mistakes. The sparse model can be very confused with small top-1 likelihood numbers and larger entropy when making mistakes. However, we also frequently find examples where the sparse model is very confident in their mistakes. To make the observation concrete, we present a small example in Figure 2 a piece of text where the sparse model makes a mistake while the full model succeeds. The red bars signify the

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**Algorithm 1** Sirius

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**Require:** Prompt  $[x_1, \dots, x_t]$ , full model  $M_F$ , and sparse model  $M_S$  sharing weights and sharing KV Cache  $C$ ,  $cache\_pos$  is the location where new k and v are written to  $C$ , kernel size  $n$

**Require:** forward function FORWARD, threshold  $r$ , which is a value used by  $M_F$  to judge whether the token occurs likely enough

**Require:** StoppingCriteriaMet() downstream task-specific, returns a boolean

```
1: while not StoppingCriteriaMet() do
2:    $i \leftarrow 0$ 
3:    $kernel \leftarrow \text{empty}$ 
4:    $cache\_pos \leftarrow 0$ 
5:   while  $i < n$  do
6:      $set\ p_{t+i} \leftarrow \text{FORWARD}(M_C, C, [x_1, \dots, x_t], [x_{t+1}, \dots, x_{t+i-1}], cache\_pos)$ 
7:     ▷ Running sparse model
8:      $cache\_pos \leftarrow cache\_pos + 1$ 
9:      $sample\ x_{t+i} \sim p_{t+i}$ 
10:     $kernel \leftarrow \text{cat}(kernel, x_{t+i})$ 
11:     $i \leftarrow i + 1$ 
12:    ▷ Before exiting,  $kernel [x_t, \dots, x_{t+n}]$ 
13:  end while
14:   $cache\_pos \leftarrow cache\_pos \text{ subtracts } n$ 
15:  ▷ Enables Full to directly rewrites KV Cache
16:   $set [q_t, \dots, q_{t+i}] \leftarrow \text{FORWARD}(M_C, C_S, cache\_pos, kernel)$ 
17:  for  $j$  from 0,  $n$  do
18:    if  $q_{t+j} < r$  then
19:       $break$ 
20:    ▷ Full rejects
21:    ▷  $j$  stores the first token position being rejected
22:  end if
23: end for
24:  $cache\_pos \leftarrow j + 1$ 
25: ▷ Rollback
26:  $kernel \leftarrow \text{empty}$ 
27:  $sample\ x_{t+j+1} \sim p_{t+j}$ 
28: ▷ Interleaving Key Token
29: end while
```

---

error location. The token entropy is neither high nor at zero, making it impossible to effectively use a threshold to control the number  $n_{sparse}$ . We deployed fixed  $n_{sparse}$  at 16 to 24 based on results tuning on a small validation set which works effectively in practice.

## C.2 Hardware Friendly Tree Building Process

In this section, we first look at the insights behind whether building the tree can help efficiency, then we detail the specific steps towards tree pruning.

The goal for the Sirius system is to make  $n_{AAL}$  to be as large as possible. Despite the full model sharing KVs with the sparse model, Sirius still encounters costly rollbacks because of sparse greedily decoded tokens being rejected. Interestingly, we look closely into where the sparse model is likely to make a mistake on GSM8K and AQuA-RAT-COT [18] with Sirius on Llama-3-8B-Instruct and a kernel size of 16. More details are shown in Appendix D.5. The error distributes almost uniformly across all positions of the kernel size. Also, when the token makes the mistake, besides the greedily decoded tokens, we find that other tokens of lower likelihood offer the potential to boost efficiency. Surprisingly, we found that out of the cases where the greedily decoded tokens are rejected, the probability that the second or third most likely tokens from the sparse being accepted by the full model is reasonably high.

Table 5: The second and third most likely tokens from sparse models offer potential for boosting efficiency.

Sparsity	$2^{nd}$ Hit	$3^{rd}$ Hit	Miss	Coverage%
FSparse	79%	11%	9%	90%
CSparse	65%	17%	16%	82%



Shown in Table 5, we test on part of the GSM8K rejected cases. The "Second Hit" is defined as the count of the second most likely tokens being accepted by the full model when the greedily decoded token is rejected, while the "Third Hit" is defined as the count of the third most likely token being accepted when the first two are rejected. Both sparsity method has a high acceptance rate, or "Coverage", from the second and third most likely tokens when the most likely token is rejected, showing huge potential for gains in efficiency.

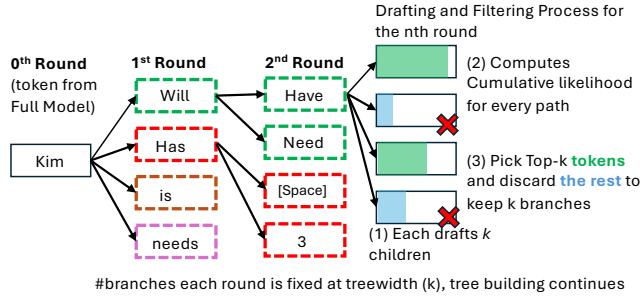


Figure 9: Illustration of Tree Building Process.

To capitalize the potential from the second to third tokens, we propose to build a tree during the sparse generating process (lines 6 to 11 in Algorithm 1. The tree algorithm is similar to Beam Search [9]. However, to make sure that the tree building and tree parallel correction processes can achieve speedup over cases that don't build trees, we impose strong restrictions on the tree structure we build. For a fixed kernel size, we limit every step to having a fixed number of leaves, or treewidth, through tree pruning based on ranking the cumulative log-likelihood of the path. The resulting tree has a fixed shape for a given kernel size and tree width, but only the interconnection pattern between steps varies based on the pruning and ranking within each step. The details are illustrated in Figure 9. During verification, out of the treewidth complete paths, we select the one that reaches the longest advance length. In practice, we found that for kernel size 16, when the treewidth is increased to 8, the optimal verification tree is around 64. From Section A.4, we see that the parallel verification of the tree of 64 roughly equals the time the full input 1 token.

Therefore, a treewidth of 8 is set as the maximum treewidth when building the tree for kernel size 16 for later. We show that building a tree makes the system significantly more efficient while retaining correction effects.

## D Supplemental Experiments

### D.1 Additional Experiment Setting and Main Results

**Models and Datasets** - To comprehensively evaluate SIRIUS performance, we deploy six mainstream LLMs with sizes ranging from 7B to 13B: Llama-2-7B, Llama-3-8B, and Llama-2-13B with their instruction finetuned counterparts, all from Llama family. Following prior milestone [34] in LLM reasoning, we also tested CS models on two popular types of reasoning generation tasks: arithmetic and commonsense reasoning. On the Arithmetic side, besides GSM8K, we also evaluate CS models on AQUA-RAT. On the Common Sense side, we use CSQA [25], StrategyQA[10], Date, and Sports, where the last two are from Big Bench Suite [1]. Most of these tasks are originally classification tasks. Following the instruction in [34], we manually compose COT prompts to transform these into logic argument generation tasks. Besides, we found that the CS models do perform not well in code generation, which also requires forming logical arguments and planning. We select HumanEval [3] and MBPP+ [19] two high-quality Python coding tasks to see whether SIRIUS corrects these problems.

For arithmetic reasoning and coding, we use 50% neuron sparsity for both CSparse and FSparse. FSparse relies on the gate layer to be dense, leading to higher global density than CSparse. Since commonsense reasoning tasks are generally less logically challenging comparatively, we lowered the neuron sparsity level to 40%.

### D.2 Large Model Experiments

In this section, we provide several supplemental experiments to the picture. First, we run SIRIUS on Llama-3-70B. However, because of computational limits, we cannot run SIRIUS with the tree on Llama-3-70B with the scale we did for other models. Nevertheless, we do show that 70B has roughly the same pattern as we have seen before, large model sparsity also somehow struggles on reasoning tasks. Second, we provide additional proof for the parallel verification efficiency statement. After that, I show results on where the error is located in the chunk size of 16 tokens. The error is distributed almost uniformly. Last but not least, we also apply SIRIUS on datasets that are reasoning. Lastly, we provide more results on the comparison between models of similar size but have a huge performance gap. We show that given the similar parameter size, the trend is for a more well-trained, powerful model to degrade more from contextual sparsity.

To diversify the evaluation of Sirius, we also evaluate Sirius’s Effectiveness on the Llama-3-70B-Instruct model. MMLU is subsampled 10%, while CNN/DailyMail is subsampled 30%. The following table contrasts with Llama-3-8B-Instruct. We use strict match/flexible extract accuracy for GSM-8K-COT, accuracy for MMLU, F1/EM score for CoQA, Rouge-1/2/L score for CNN/DailyMail, and Rouge-1/2 ACC for TruthfulQA.

### D.3 Ablation: Various Aspects of Sirius Are Tested and Challenged

**Probing Components** To understand the contribution and the utility of each component of Sirius, we ablate all components of Sirius in Table 8. We started by only letting the LLM correct the token it is evaluating (interleaving only). Then, we add on top of it the KV cache correction, and then the rollback. All these three techniques are effective when applied solely. Rollback seems to be the most effective technique. Even when applied alone, rollback asserts significant correction to both the CSparse and FSparse models. Interestingly, KV Cache is also effective alone, bringing a 12% increment for CSparse and an 11% accuracy increase for FSparse. Relatively, interleaving is the weakest. Surprisingly, adding both KV rewriting and rollback is only marginally better than rollback alone. Although it is tempting to think KV Cache rewriting is not useful with rollback, the improvement KV Cache Rewriting brings is a gain in efficiency. When adding the KV Cache Rewriting on top of Roll Back and interleave it significantly improves the efficiency of the correction. For CSparse, adding KV rewrite increases AAL from 12.77 to 13.80.

Table 6: We show SIRIUS effectiveness and efficiency in the following table. We select GSM8K for Arithmetic Reasoning, CSQA for Commonsense Reasoning, and HumanEval for code generation. Under the "SIRIUS Perf. " column, A(B) is shown. A denotes the accuracy after SIRIUS correction in the dataset evaluated, while (B) represents the optimal treewidth selected under the current model dataset settings. Under the column of "AAL", X/Y is shown, where X is the AAL, while Y is the period.

GSM8K						
Model	Full Perf.	CSparse Perf.	CSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.7536	0.3844	0.65	0.7051 (8)	15.22/16	0.706
Llama-3-8B	0.4966	0.2085	0.65	0.4177 (8)	15.29/16	0.703
Llama-2-7B-Chat	0.2403	0.1334	0.69	0.2244 (8)	15.00/16	0.757
Llama-2-7B	0.1357	0.0758	0.69	0.1183 (6)	15.87/16	0.715
Llama-2-13B-Chat	0.3548	0.2714	0.68	0.3381 (4)	15.34/16	0.730
Llama-2-13B	0.2282	0.1759	0.68	0.2418 (1)	15.34/16	0.730
Model	Full Perf.	FSparse Perf.	FSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.7536	0.5868	0.76	0.7278 (4)	15.37/16	0.807
Llama-3-8B	0.4966	0.3199	0.76	0.4579 (2)	15.03/16	0.825
Llama-2-7B-Chat	0.2403	0.1971	0.79	0.2388 (6)	15.69/16	0.819
Llama-2-7B	0.1357	0.1137	0.79	0.1410 (4)	15.91/16	0.807
Llama-2-13B-Chat	0.3548	0.3222	0.78	0.3533 (1)	15.08/16	0.842
Llama-2-13B	0.2282	0.2191	0.78	0.2372 (4)	15.92/16	0.797
CSQA						
Model	Full Perf.	CSparse Perf.	CSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.7073	0.6470	0.58	0.7076 (8)	14.76/16	0.657
Llama-3-8B	0.6437	0.5585	0.58	0.6429 (8)	15.43/16	0.628
Llama-2-7B-Chat	0.6248	0.5200	0.62	0.6175 (8)	15.07/16	0.683
Llama-2-7B	0.4742	0.4414	0.62	0.4742 (8)	15.80/16	0.652
Llama-2-13B-Chat	0.6879	0.5536	0.61	0.6691 (4)	11.43/12	0.674
Llama-2-13B	0.6109	0.5601	0.61	0.6060 (4)	15.72/16	0.645
Model	Full Perf.	FSparse Perf.	FSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.7073	0.6158	0.72	0.7043 (8)	15.66/16	0.753
Llama-3-8B	0.6437	0.533	0.72	0.6388 (1)	15.00/16	0.786
Llama-2-7B-Chat	0.6248	0.6167	0.75	0.6380 (4)	15.09/16	0.811
Llama-2-7B	0.4742	0.4717	0.75	0.5012 (6)	15.89/16	0.771
Llama-2-13B-Chat	0.6879	0.533	0.74	0.6691 (4)	14.30/16	0.846
Llama-2-13B	0.6109	0.5700	0.74	0.5864 (4)	15.72/16	0.770
HumanEval						
Model	Full Perf.	CSparse Perf.	CSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.561	0.207	0.65	0.524 (8)	14.67/16	0.733
Llama-3-8B	0.262	0.067	0.65	0.243 (8)	15.10/16	0.691
Llama-2-7B-Chat	0.140	0.067	0.69	0.159 (8)	10.88/12	0.789
Llama-2-7B	0.116	0.079	0.69	0.128 (8)	14.84/16	0.765
Llama-2-13B-Chat	0.189	0.122	0.68	0.171 (8)	11.12/12	0.762
Llama-2-13B	0.262	0.067	0.68	0.244 (8)	15.10/16	0.741
Model	Full Perf.	FSparse Perf.	FSparse Density	SIRIUS Perf.	AAL	Effective Density
Llama-3-8B-Instruct	0.561	0.457	0.76	0.616 (6)	15.42/16	0.804
Llama-3-8B	0.262	0.189	0.76	0.298 (6)	15.54/16	0.797
Llama-2-7B-Chat	0.140	0.134	0.79	0.165 (6)	15.27/16	0.841
Llama-2-7B	0.116	0.116	0.79	0.165 (6)	15.86/16	0.810
Llama-2-13B-Chat	0.189	0.146	0.78	0.183 (6)	15.34/16	0.827
Llama-2-13B	0.246	0.233	0.78	0.259 (4)	15.85/16	0.801

Table 7: Large model results on miscellaneous datasets.

	GSM-8K-COT	MMLU	CoQA	CNN/DailyMail	TruthfulQA
<b>Llama-3-70B-In</b>	0.9014/0.9022	0.7456	0.6567/0.8069	0.101634/0.020614/0.096413	0.5116/0.4247
<b>+ CSparse</b>	0.7407/0.7483	0.7018	0.6497/0.8046	0.101922/0.020854/0.096703	0.4541/0.3807
<b>+ FSparse</b>	0.8726/0.8772	0.7193	0.6497/0.8035	0.101505/0.020623/0.096344	0.4835/0.3905
<b>Llama-3-8B-In</b>	0.7612/0.7672	0.6272	0.6153/0.7825	0.101523/0.020481/0.096311	0.4945/0.3647
<b>+ CSparse</b>	0.3601/0.3647	0.5307	0.6003/0.7735	0.101681/0.020657/0.096432	0.5067/0.3953
<b>+ FSparse</b>	0.6103/0.6202	0.4825	0.5828/0.7577	0.101713/0.020448/0.096516	0.5202/0.3941

Table 8: Ablation on Components in Sirius.

CSparse	GSM8K 20%	FSparse	GSM8K 20%
<b>Llama3-8B-Instruct</b>	0.7538/0.7538	<b>Llama3-8B-Instruct</b>	0.7538/0.7538
+ CSparse	0.3674/0.3674	+ FSparse	0.5644/0.5644
+ CSparse + Interleave	0.3826/0.3826	+ FSparse + Interleave	0.6288/0.6288
+ CSparse + KV Rewrite	0.4735/0.4735	+ FSparse + KV Rewrite	0.6629/0.6629
+ CSparse + KV Rewrite + Interleave	0.4886/0.4886	+ FSparse + KV Rewrite + Interleave	0.6780/0.6818
+ CSparse + Roll back + Interleave	0.6591/0.6591	+ FSparse + Roll back + Interleave	0.7273/0.7273
+ CSparse + KV Rewrite + Interleave + Rollback	0.6667/0.6667	+ FSparse + KV Rewrite + Interleave + Rollback	0.7273/0.7311

**Likelihood threshold to balance Correction and Efficiency** We found that the likelihood threshold is important for managing the Sirius correction and efficiency tradeoff. We present results in Table 9. We ablate this setting on a 30% subsampled GSM8K dataset, and only strict accuracy is reported. The performance is the score, while the efficiency is measured by Average Advance Length (AAL). We can find that with the increase of threshold, the scores generally improve, while the efficiency metric decreases.

**Building Wider Tree** We study the effect of increasing the treewidth. In fact, for every number from SIRIUS in Table 6, we are selecting from a group of results by different treewidth. We present all of this treewidth and its corresponding accuracy and efficiency numbers in the Appendix E. *Importantly, raising treewidth always improves AAL.* Although different choices of treewidth usually give similar accuracy scores, there is hardly a pattern on which treewidth always gives the best accuracy. The optimal treewidth can only be found through empirical studies.

#### D.4 Variable Sequence Length with Batch Size One

Here we show the benchmark latency on A100, where the input tensor to Llama-3-8B-Instruct has a shape of batch size 1 and a different input sequence length. To get the hardware optimal readings, we use torch compile to compile the whole forward pass of the model. We show that the latency only goes up insignificantly to 64, but the trend of increment to 96 is a bit steep.

#### D.5 Error Occurs At Which Position inside a Chunk

We look at the distribution of where the error would be inside a kernel of 16 tokens. We run through Sirius with a kernel size of 16 on the entire GSM-8K and AQuA-RAT-COT dataset. The histogram is shown in Figure 10. We found that the error occurs in a uniform pattern, where it is hard to see any particular region where the tokens are likely to occur the most.

Table 9: Ablation on the threshold for correction (FSparse Llama-3-8B-Instruct).

Threshold	Full	Sparse	0.05	0.1	0.3	0.5	0.7	0.9
Accuracy	0.7803	0.5884	0.7247	0.7399	0.7399	0.7677	0.7702	0.7652
AAL	N/A	N/A	15.2	14.6	11.6	8.5	6.2	4.2

Table 10: A100 Latency versus Input Sequence Length.

Input Sequence Length	A100 Latency (ms)
1	0.0133
2	0.0135
4	0.0136
8	0.0138
16	0.0140
32	0.0149
64	0.0144
96	0.0171

### D.6 Miscellaneous Results

Besides, the results on the complex reasoning tasks, we evaluate Sirius on slightly more diverse tasks in Table 12.

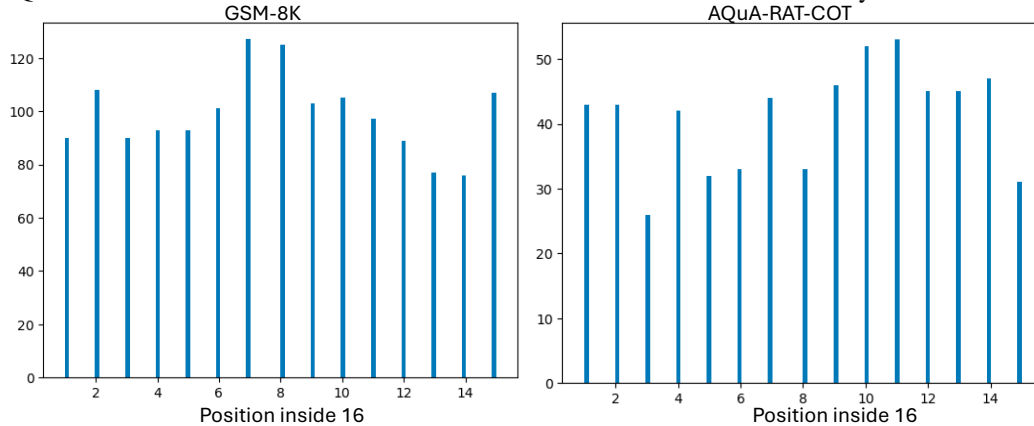
### D.7 Llama-2 and Llama-3 Models on GSM8K-COT

Table 11: Detail on Llama-2 and Llama-3 family models with CS.

Llama-3-70B-Instruct	Accuracy	Degradation	Llama-3-8B-Instruct	Accuracy	Degradation
Full	0.9205		Full	0.7462	
Csparse 60%	0.8144	0.1061			
Csparse 50%	0.7652	0.1553	Csparse 50%	0.3636	0.3826
Csparse 40%	0.6023	0.3182	Csparse 40%	0.1856	0.5606
Csparse 30%	0.3144	0.6061	Csparse 30%	0.0644	0.6818
Fsparse 50%	0.8864	0.0341	Fsparse 50%	0.6477	0.0985
Fsparse 40%	0.8485	0.0720	Fsparse 40%	0.4053	0.3409
Fsparse 30%	0.7386	0.1819	Fsparse 30%	0.0265	0.7197
Fsparse 20%	0.2803	0.6402			
Llama-2-70B-Chat	Accuracy	Degradation	Llama-2-7B-Chat	Accuracy	Degradation
Full	0.4508		Full	0.1856	
Csparse 50%	0.3939	0.0569	Csparse 50%	0.1515	0.0341
Csparse 40%	0.3447	0.1061	Csparse 40%	0.1098	0.0758
Csparse 30%	0.2689	0.1819	Csparse 30%	0.0720	0.1136
Fsparse 50%	0.3864	0.0644	Fsparse 50%	0.1629	0.0227
Fsparse 40%	0.3902	0.0606	Fsparse 40%	0.1364	0.0492
Fsparse 30%	0.2689	0.1819	Fsparse 30%	0.1212	0.0644

Here we present more experiments for the comparison between Llama-2 and Llama-3 family models, which is first mentioned in Section B.3, where we also include FSparse methods together with the CSparse method. The results are in Table 11.

Figure 10: We look at the histogram of the number of errors versus the position among a period of sixteen tokens on average. We have two different datasets of Arithmetic Reasoning GSM-8K and AQuA-RAT-COT. We can see that the number of errors is distributed almost evenly for both datasets.



## E Additional Results on Reasoning

Due to page restrictions, we only show GSM8K, CSQA, and HumanEval in the paper. Below we show additional results to the numbers presented in the paper. **We present tables of a similar format. Please notice that the leftmost column writes a number that represents the treewidth in the given settings.** Also, we show the results of SIRIUS on the other five datasets AQuA-RAT-COT (Arithmetic Reasoning), Sports (Commonsense Reasoning), Date (Commonsense Reasoning), and StrategyQA (CommonSense Reasoning), and MBPP+ (coding).

### E.1 Arithmetic Reasoning

In this section, we present GSM8K and AQuA RAT COT evaluation results with the efficiency metric AAL. Sirius is shown to be effective on these two reasoning tasks about arithmetic. Below we show the raw AAL score associated with efficiency for all models and the performance of different treewidths.

### E.2 CommonSense Reasoning

We followed the COT paper and evaluated Sirius on CSQA, Sports, StrategyQA, and Dates. Sparse methods are capable of outputting high-quality output similar to the full model at the 0.5 mark, which is different than on other datasets. However, we tune the sparsity level to 0.4 (0.6 dense, 0.4 removed), and it starts to have performance degradation. Sirius can compensate them with relatively high efficiency)

### E.3 Code

We also have a coding portion that evaluates Sirius on HumanEval. Sirius performs well similar to other datasets. Besides, we also have results on MBPP+. The results show SIRIUS effectiveness and efficiency again.

Optionally include supplemental material (complete proofs, additional experiments and plots) in appendix. All such materials **SHOULD be included in the main submission.**

Table 12: Miscellaneous Results: 5 models on different Three Different datasets.

Experiment Setting	CoQA	AGIEval (Math)	MMLU-FLAN-COT
Llama-2-7B-Chat	0.5982/0.7580	0.072	0.4925
Llama-2-7B-Chat-FSparse	0.5898/0.7540	0.077	0.4768
Llama-2-7B-Chat-FSparse-SIRIUS	0.5908/0.7540	0.081	0.4670
Llama-2-7B-Chat-CSparse	0.6117/0.7639	0.065	0.4637
Llama-2-7B-Chat-CSparse-SIRIUS	0.6117/0.7664	0.078	0.4794
Llama-3-8B-Instruct	0.6153/0.7825	0.213	0.6231
Llama-3-8B-Instruct-FSparse	0.5828/0.7577	0.172	0.5304
Llama-3-8B-Instruct-FSparse-SIRIUS	0.5868/0.7591	0.196	0.5709
Llama-3-8B-Instruct-CSparse	0.6003/0.7735	0.154	0.5558
Llama-3-8B-Instruct-CSparse-SIRIUS	0.6005/0.7728	0.178	0.6003
Llama-2-13B-Chat	0.6408/0.7896	0.092	0.5317
Llama-2-13B-Chat-FSparse	0.6320/0.7837	0.087	0.5082
Llama-2-13B-Chat-FSparse-SIRIUS	0.6340/0.7859	0.089	0.5219
Llama-2-13B-Chat-CSparse	0.6350/0.7841	0.088	0.5127
Llama-2-13B-Chat-CSparse-SIRIUS	0.6363/0.7847	0.1	0.5127
Llama-2-7B	0.6388/0.7735	0.101	0.4520
Llama-2-7B-FSparse	0.6352/0.7697	0.09	0.4435
Llama-2-7B-FSparse-SIRIUS	0.6352/0.7697	0.092	0.4415
Llama-2-7B-CSparse	0.6338/0.7700	0.086	0.4213
Llama-2-7B-CSparse-SIRIUS	0.6372/0.7709	0.093	0.4317
Llama-3-8B	0.6727/0.8055	0.163	0.5754
Llama-3-8B-FSparse	0.6625/0.7984	0.152	0.5349
Llama-3-8B-FSparse-SIRIUS	0.6625/0.7984	0.154	0.5532
Llama-3-8B-CSparse	0.6633/0.7977	0.131	0.5049
Llama-3-8B-CSparse-SIRIUS	0.6670/0.7995	0.15	0.5428

## NeurIPS Paper Checklist

The checklist is designed to encourage best practices for responsible machine learning research, addressing issues of reproducibility, transparency, research ethics, and societal impact. Do not remove the checklist: **The papers not including the checklist will be desk rejected.** The checklist should follow the references and follow the (optional) supplemental material. The checklist does NOT count towards the page limit.

Please read the checklist guidelines carefully for information on how to answer these questions. For each question in the checklist:

- You should answer [Yes], [No], or [NA].
- [NA] means either that the question is Not Applicable for that particular paper or the relevant information is Not Available.
- Please provide a short (1–2 sentence) justification right after your answer (even for NA).

**The checklist answers are an integral part of your paper submission.** They are visible to the reviewers, area chairs, senior area chairs, and ethics reviewers. You will be asked to also include it (after eventual revisions) with the final version of your paper, and its final version will be published with the paper.

The reviewers of your paper will be asked to use the checklist as one of the factors in their evaluation. While "[Yes]" is generally preferable to "[No]", it is perfectly acceptable to answer

Table 13: SIRIUS Tree on GSM8K.

Experiment Settings treewidth	Llama-3-8B-Instruct-FSparse		Llama-3-8B-Instruct-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.7536/0.7544	N/A	0.7536/0.7544	N/A
Sparse Performance	0.5868/0.5891	N/A	0.3844/0.3867	N/A
1	0.7316/0.7324	14.5903	0.6983/0.7005	13.1903
2	0.7172/0.7172	14.9554	0.7089/0.7096	14.1517
4	0.7278/0.7309	15.3705	0.7119/0.7111	14.8393
6	0.7195/0.7187	15.5979	0.7081/0.7074	15.0682
8	0.7202/0.7218	15.5548	0.7051/0.7058	15.2291
	Llama-3-8B-FSparse		Llama-3-8B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.4966/0.5042	N/A	0.4966/0.5042	N/A
Sparse Performance	0.3199/0.3260	N/A	0.2085/0.2168	N/A
1	0.4526/0.4572	14.6946	0.439/0.445	13.361
2	0.4579/0.4640	15.0355	0.4299/0.4367	14.3061
4	0.4579/0.4540	15.0355	0.4223/0.4306	14.9721
6	0.4450/0.4503	15.4834	0.4177/0.4238	15.1435
8	0.4352/0.4428	15.5863	0.4177/0.4238	15.2939
	Llama-2-13B-Chat-FSparse		Llama-2-13B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.3548/0.3647	N/A	0.3548/0.3647	N/A
Sparse Performance	0.3222/0.3275	N/A	0.2714/0.2767	N/A
1	0.3533/0.3472	15.085	0.3412/0.3472	14.0153
4	0.3412/0.3374	15.7576	0.3381/0.3412	15.3491
	Llama-2-13B-FSparse		Llama-2-13B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.2282/0.2312	N/A	0.2282/0.2312	N/A
Sparse Performance	0.2191/0.2229	N/A	0.1759/0.1797	N/A
1	0.2328/0.2381	15.6759	0.2418/0.2472	15.3415
4	0.2372/0.2403	15.9283	0.2077/0.2100	15.825
	Llama-2-7B-Chat-FSparse		Llama-2-7B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.2403/0.2426	N/A	0.2403/0.2426	N/A
Sparse Performance	0.1971/0.1994	N/A	0.1334/0.1372	N/A
1	0.2282/0.2312	14.8172	0.2214/0.2229	12.6888
2	0.2297/0.2305	15.1784	0.2252/0.2359	13.8875
4	0.2305/0.2282	15.5467	0.2183/0.2214	14.6751
6	0.2388/0.2411	15.691	0.2199/0.2206	14.8575
8	0.2312/0.2343	15.735	0.2244/0.2252	15.0017
	Llama-2-7B-FSparse		Llama-2-7B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.1357/0.1403	N/A	0.1357/0.1403	N/A
Sparse Performance	0.1137/0.1168	N/A	0.0758/0.0804	N/A
1	0.1183/0.1205	15.6864	0.1152/0.1168	15.1096
2	0.1334/0.1357	15.7893	0.113/0.116	15.5358
4	0.1410/0.1448	15.9161	0.113/0.116	15.8558 (53.341)
6	0.1289/0.1312	15.9662	0.1183/0.1205	15.8715
8	0.1236/0.1259	15.9568	0.1114/0.1145	15.8939



Table 14: SIRIUS on AQUA-RAT-COT.

Experiment Settings treewidth	Llama-3-8B-Instruct-FSparse		Llama-3-8B-Instruct-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 12)
Original Performance	0.515748	N/A	0.515748	N/A
Sparse Performance	0.42126	N/A	0.271654	N/A
1	0.429134	13.1945	0.468504	10.3322
4	0.488189	14.4722	0.44095	10.6228
6	0.496063	15.115	0.452756	10.8348
8	0.476378	15.3721	0.456693	11.0874
	Llama-3-8B-FSparse		Llama-3-8B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 12)
Original Performance	0.456693	N/A	0.456693	N/A
Sparse Performance	0.287402	N/A	0.228346	N/A
1	0.377953	12.6665	0.377945	12.6665
4	0.385827	14.46	0.397638	10.2826
6	0.366142	15.0671	0.370079	10.6753
8	0.42126	15.0995	0.38189	11.0019
	Llama-2-13B-Chat-FSparse		Llama-2-13B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 12)
Original Performance	0.232283	N/A	0.232283	N/A
Sparse Performance	0.251969	N/A	0.208661	N/A
1	0.275591	15.5163	0.26378	9.17465
4	0.279528	15.3995	0.259843	10.8726
	Llama-2-13B-FSparse		Llama-2-13B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 12)
Original Performance	0.149606	N/A	0.149606	N/A
Sparse Performance	0.165354	N/A	0.149606	N/A
1	0.185039	15.4652	0.161417	11.0874
4	0.220472	15.6346	0.192913	11.8238
	Llama-2-7B-Chat-FSparse		Llama-2-7B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.251969	N/A	0.251969	N/A
Sparse Performance	0.283465	N/A	0.220472	N/A
1	0.248031	15.5294	0.251969	12.6424
4	0.259843	15.7254	0.244096	14.5794
	Llama-2-7B-FSparse		Llama-2-7B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.15748	N/A	0.15748	N/A
Sparse Performance	0.153543	N/A	0.177165	N/A
1	0.185039	15.423	0.141732	15.4122
4	0.161417	15.651	0.145669	15.3788

Table 15: SIRIUS on CSQA.

Experiment Settings treewidth	Llama-3-8B-Instruct-FSparse		Llama-3-8B-Instruct-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.707341	N/A	0.707341	N/A
Sparse Performance	0.615889	N/A	0.647011	N/A
1	0.699427	12.2108	0.724816	11.0512
4	0.687961	13.2734	0.709255	13.5876
6	0.714169	13.7842	0.720721	13.3097
8	0.710893	14.1173	0.707617	14.76893
	Llama-3-8B-FSparse		Llama-3-8B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.643735	N/A	0.643735	N/A
Sparse Performance	0.53317	N/A	0.558559	N/A
1	0.638821	15.0088	0.618346	12.7426
4	0.630631	14.6151	0.63964	14.8704
6	0.625717	14.9905	0.640459	15.1968
8	0.617527	15.2534	0.642916	15.4355
	Llama-2-13B-Chat-FSparse		Llama-2-13B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 12)
Original Performance	0.687961	N/A	0.687961	N/A
Sparse Performance	0.53317	N/A	0.553645	N/A
1	0.657658	13.0868	0.649468	9.2183
4	0.669124	14.309	0.669124	11.438
	Llama-2-13B-FSparse		Llama-2-13B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.610975	N/A	0.610975	N/A
Sparse Performance	0.570025	N/A	0.560197	N/A
1	0.578215	15.2554	0.58231	14.7381
4	0.586405	15.7213	0.606061	15.7284
	Llama-2-7B-Chat-FSparse		Llama-2-7B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.624898	N/A	0.624898	N/A
Sparse Performance	0.616708	N/A	0.520066	N/A
1	0.632269	14.1015	0.608518	11.4607
4	0.638002	15.0978	0.605242	14.0366
6	0.605242	15.4365	0.611794	14.7197
8	0.621622	15.552	0.617527	15.0799
	Llama-2-7B-FSparse		Llama-2-7B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.474201	N/A	0.474201	N/A
Sparse Performance	0.471744	N/A	0.441441	N/A
1	0.488124	15.5119	0.461916	14.703
4	0.494676	15.9141	0.486486	15.5972
6	0.501229	15.8922	0.476658	15.7315
8	0.473382	15.9247	0.474201	15.802

Table 16: SIRIUS on Sports.

Experiment Settings treewidth	Llama-3-8B-Instruct-FSparse		Llama-3-8B-Instruct-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.943299	N/A	0.943299	N/A
Sparse Performance	0.864948	N/A	0.879381	N/A
1	0.937113	12.3652	0.946392	9.95237
4	0.941237	14.5248	0.943299	11.5858
6	0.942268	14.8651	0.943299	14.0954
8	0.939175	14.9832	0.941237	14.7718
	Llama-3-8B-FSparse		Llama-3-8B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.898969	N/A	0.898969	N/A
Sparse Performance	0.748454	N/A	0.720619	N/A
1	0.86653	15.5259	0.845361	13.5897
4	0.849485	15.5917	0.847423	15.2325
6	0.863918	15.5256	0.843299	15.4376
8	0.869072	15.6014	0.841237	15.5023
	Llama-2-13B-Chat-FSparse		Llama-2-13B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 12)
Original Performance	0.742268	N/A	0.742268	N/A
Sparse Performance	0.690722	N/A	0.584536	N/A
1	0.710309	13.9767	0.717659	7.72686
4	0.735052	14.9247	0.728953	10.7298
	Llama-2-13B-FSparse		Llama-2-13B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.709278	N/A	0.709278	N/A
Sparse Performance	0.635052	N/A	0.558763	N/A
1	0.669072	15.4924	0.639175	14.3603
4	0.657732	15.9845	0.658763	15.48
	Llama-2-7B-Chat-FSparse		Llama-2-7B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.731959	N/A	0.731959	N/A
Sparse Performance	0.652677	N/A	0.596907	N/A
1	0.704124	14.3861	0.712371	11.1517
4	0.712371	15.5904	0.71134	13.7394
6	0.709278	15.7475	0.71134	13.9857
8	0.698969	15.9927	0.715464	14.3817
	Llama-2-7B-FSparse		Llama-2-7B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.545361	N/A	0.545361	N/A
Sparse Performance	0.536082	N/A	0.528866	N/A
1	0.524742	15.6754	0.536082	14.1031
4	0.547423	15.937	0.538144	15.6263
6	0.545361	15.9807	0.540206	15.7243
8	0.545361	15.9927	0.549485	15.811

Table 17: SIRIUS on Date.

Experiment Settings treewidth	Llama-3-8B-Instruct-FSparse		Llama-3-8B-Instruct-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.657224	N/A	0.657224	N/A
Sparse Performance	0.518414	N/A	0.532578	N/A
1	0.688385	14.2885	0.671388	14.6771
4	0.671388	15.357	0.685552	15.6324
6	0.679887	15.2435	0.688385	15.1663
8	0.674221	15.2654	0.694051	15.4293
	Llama-3-8B-FSparse		Llama-3-8B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.583569	N/A	0.583569	N/A
Sparse Performance	0.399433	N/A	0.424929	N/A
1	0.535014	15.4236	0.535411	14.4364
4	0.543909	15.4782	0.546742	15.606
6	0.546742	15.6365	0.526912	15.7718
8	0.549575	15.7159	0.541076	15.7997
	Llama-2-13B-Chat-FSparse		Llama-2-13B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.524079	N/A	0.524079	N/A
Sparse Performance	0.498584	N/A	0.419263	N/A
1	0.490085	13.9589	0.461756	14.1419
4	0.524079	15.432	0.478992	15.8545
	Llama-2-13B-FSparse		Llama-2-13B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.501416	N/A	0.501416	N/A
Sparse Performance	0.464589	N/A	0.390935	N/A
1	0.447592	15.5992	0.461756	15.3896
4	0.492918	15.9129	0.484419	15.8357
	Llama-2-7B-Chat-FSparse		Llama-2-7B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.320113	N/A	0.320113	N/A
Sparse Performance	0.339943	N/A	0.3002823	N/A
1	0.31728	14.4663	0.305949	5.75938
4	0.345609	15.6588	0.325779	14.7519
6	0.342776	15.742	0.314448	14.5768
8	0.348442	15.7692	0.308782	14.3627
	Llama-2-7B-FSparse		Llama-2-7B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.33711	N/A	0.33711	N/A
Sparse Performance	0.314448	N/A	0.235127	N/A
1	0.342776	15.5144	0.269122	15.3598
4	0.342776	15.9141	0.266289	15.8553
6	0.328612	15.943	0.274788	15.9266
8	0.322946	15.9671	0.271955	15.956

Table 18: SIRIUS on StrategyQA.

Experiment Settings treewidth	Llama-3-8B-Instruct-FSparse		Llama-3-8B-Instruct-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 10)
Original Performance	0.770241	N/A	0.770241	N/A
Sparse Performance	0.713348	N/A	0.562363	N/A
1	0.741794	8.98893	0.737418	6.60992
4	0.741794	9.48412	0.746171	7.92521
6	0.743982	9.53292	0.728665	8.22667
8	0.743982	9.55946	0.708972	8.97268
	Llama-3-8B-FSparse		Llama-3-8B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.649891	N/A	0.649891	N/A
Sparse Performance	0.599562	N/A	0.439825	N/A
1	0.623632	9.46018	0.531729	8.68633
4	0.623632	9.74383	0.560175	9.44497
6	0.632385	9.83975	0.560175	9.58122
8	0.680525	9.80493	0.555799	9.67198
	Llama-2-13B-Chat-FSparse		Llama-2-13B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.695842	N/A	0.695842	N/A
Sparse Performance	0.706783	N/A	0.634573	N/A
1	0.71116	9.48266	0.682713	6.74106
4	0.667396	9.83767	0.715536	8.09959
6	0.671772	9.88989	0.693654	8.82263
	Llama-2-13B-FSparse		Llama-2-13B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.63895	N/A	0.63895	N/A
Sparse Performance	0.693654	N/A	0.533917	N/A
1	0.695842	9.8979	0.595186	8.77388
4	0.682713	9.96438	0.643326	9.47368
6	0.689278	9.9789	0.63895	9.56319
	Llama-2-7B-Chat-FSparse		Llama-2-7B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.654267	N/A	0.654267	N/A
Sparse Performance	0.678337	N/A	0.612691	N/A
1	0.684902	9.64754	0.669584	6.55818
4	0.691466	9.79539	0.671772	7.88988
6	0.68709	9.86474	0.643326	8.28982
8	0.689278	9.86488	0.66302	8.43513
	Llama-2-7B-FSparse		Llama-2-7B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.599562	N/A	0.599562	N/A
Sparse Performance	0.592998	N/A	0.538293	N/A
1	0.612691	9.73256	0.568928	8.38473
4	0.599562	9.93662	0.560175	9.36272
6	0.617068	9.95582	0.536105	9.35857
8	0.610503	9.96658	0.544858	9.4642

Table 19: SIRIUS on HumanEval.

Experiment Settings treewidth	Llama-3-8B-Instruct-FSparse		Llama-3-8B-Instruct-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.560975609756098	N/A	0.560975609756098	N/A
Sparse Performance	0.457317073170732	N/A	0.207317073170732	N/A
1	0.585365853658537	14.7624	0.554878048780488	12.1326
4	0.579268292682927	15.2299	0.530487804878049	14.0546
6	0.615853658536585	15.4209	0.518292682926829	14.4431
8	0.585365853658537	15.5009	0.524390243902439	14.6725
	Llama-3-8B-FSparse		Llama-3-8B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.26219512195122	N/A	0.26219512195122	N/A
Sparse Performance	0.189024390243902	N/A	0.0670731707317073	N/A
1	0.231707317073171	15.1878	0.109756097560976	12.1402
4	0.274390243902439	15.2827	0.219512195121951	13.7718
6	0.26219512195122	14.5355	0.207317073170732	14.7776
8	0.29268	15.6305	0.24390243902439	15.1074
	Llama-2-13B-Chat-FSparse		Llama-2-13B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 12)
Original Performance	0.189024390243902	N/A	0.189024390243902	N/A
Sparse Performance	0.146341463414634	N/A	0.121951219512195	N/A
1	0.170731707317073	14.3976	0.189024390243902	9.6447
4	0.182926829268293	15.1956	0.176829268292683	10.7946
6	0.182926829268293	15.3494	0.170731707317073	11.0149
8	0.176829268292683	15.4067	0.170731707317073	11.1252
	Llama-2-13B-FSparse		Llama-2-13B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.176829268292683	N/A	0.176829268292683	N/A
Sparse Performance	0.158536585365854	N/A	0.0975609756097561	N/A
1	0.146341463414634	15.2129	N/A	N/A
4	0.158536585365854	15.9093	0.146341463414634	14.1813
6	0.170731707317073	15.9211	0.134146341463415	14.5866
8	0.176829268292683	15.9015	0.134146341463415	14.7508
	Llama-2-7B-Chat-FSparse		Llama-2-7B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 12)
Original Performance	0.140243902439024	N/A	0.140243902439024	N/A
Sparse Performance	0.134146341463415	N/A	0.0670731707317073	N/A
1	0.134146341463415	14.055	0.140243902439024	8.83176
4	0.146341463414634	14.8504	0.146341463414634	10.1263
6	0.152439024390244	15.1924	0.152439024390244	10.5576
8	0.164634146341463	15.2742	0.158536585365854	10.822
	Llama-2-7B-FSparse		Llama-2-7B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.115853658536585	N/A	0.115853658536585	N/A
Sparse Performance	0.115853658536585	N/A	0.0792682926829268	N/A
1	0.115853658536585	15.5268	0.121951219512195	12.6604
4	0.128048780487805	15.8167	0.121951219512195	14.4053
6	0.164634146341463	15.8615	0.121951219512195	14.8296
8	0.109756097560976	15.9189	0.128048780487805	14.8443

Table 20: SIRIUS on MBPP+.

Experiment Settings treewidth	Llama-3-8B-Instruct-FSparse		Llama-3-8B-Instruct-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.584656084656085	N/A	0.584656084656085	N/A
Sparse Performance	0.531746031746032	N/A	0.248677248677249	N/A
1	0.537037037037037	14.7267	0.563492063492064	11.5415
4	0.563492063492064	15.2699	0.566137566137566	13.5896
6	0.552910052910053	15.3782	0.571428571428571	14.0547
8	0.552910052910053	15.4689	0.566137566137566	14.7648
	Llama-3-8B-FSparse		Llama-3-8B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.518518518518519	N/A	0.518518518518519	N/A
Sparse Performance	0.433862433862434	N/A	0.161375661375661	N/A
1	0.4894	14.8849	0.415343915343915	12.7016
4	0.484126984126984	15.4346	0.407407407407407	14.0936
6	0.473544973544974	15.3581	0.433862433862434	14.5662
8	0.468253968253968	15.6088	0.41005291005291	14.4752
	Llama-2-13B-Chat-FSparse		Llama-2-13B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.23015873015873	N/A	0.27	N/A
Sparse Performance	0.19047619047619	N/A	0.1	N/A
1	0.201058201058201	13.8235	0.26	9.32827
4	0.232804232804233	14.8394	0.26	10.7346
6	0.224867724867725	15.0801	0.26	10.8897
8	0.227513227513228	15.2373	0.25	11.0214
	Llama-2-13B-FSparse		Llama-2-13B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 16)
Original Performance	0.246031746031746	N/A	0.21	N/A
Sparse Performance	0.232804232804233	N/A	0.13	N/A
1	0.214285714285714	14.8374	0.22	14.5174
4	0.259259259259259	15.8547	0.24	15.6461
6	0.235449735449735	15.9197	0.23	15.7174
8	0.246031746031746	15.9094	0.22	15.7179
	Llama-2-7B-Chat-FSparse		Llama-2-7B-Chat-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 12)
Original Performance	0.261904761904762	N/A	0.261904761904762	N/A
Sparse Performance	0.224867724867725	N/A	0.100529100529101	N/A
1	0.238095238095238	14.1571	0.214285714285714	8.61325
4	0.26984126984127	14.9264	0.23015873015873	10.2517
6	0.238095238095238	15.2194	0.227513227513228	10.5845
8	0.272486772486773	15.3086	0.235449735449735	10.7621
10	N/A	N/A	0.232804232804233	10.8962
	Llama-2-7B-FSparse		Llama-2-7B-CSparse	
	Performance	AAL (out of 16)	Performance	AAL (out of 12)
Original Performance	0.253968253968254	N/A	0.253968253968254	N/A
Sparse Performance	0.201058201058201	N/A	0.0793650793650794	N/A
1	0.216931216931217	14.6103	0.171957671957672	10.6643
4	0.238095238095238	15.5672	0.185185185185185	11.5561
6	0.224867724867725	15.6273	0.195767195767196	11.6547
8	0.240740740740741	15.5569	0.203703703703704	11.6753

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