# Generalized Quantifiers as a Source of Error in Multilingual NLU Benchmarks

Anonymous ACL submission

#### Abstract

Logical approaches to representing language have developed and evaluated computational models of quantifier words since the 19th century, but today's NLU models still struggle to capture their semantics. We rely on Generalized Quantifier Theory for languageindependent representations of the semantics of quantifier words, to quantify their contribution to the errors of NLU models. We find that quantifiers are pervasive in NLU benchmarks, and their occurrence at test time is associated with performance drops. Multilingual models also exhibit unsatisfying quantifier reasoning abilities, but not necessarily worse for non-English languages. To facilitate directlytargeted probing, we present an adversarial generalized quantifier NLI task (GQNLI) and show that pre-trained language models have a clear lack of robustness in generalized quantifier reasoning.

### 1 Introduction

011

012

014

017

022

023

037

Quantifier words—such as *each* or *most* or *more than three*—have been extensively studied, both in logic and in linguistics (Westerståhl, 1989; Peters and Westerståhl, 2006), going all the way back to Frege (1879). In this paper, we examine the extent to which they present a challenge to modern NLU systems. Our analysis is motivated by three observations:

**Quantifier words are abstract** Unlike nouns, verbs and adjectives, quantifier words do not have referents out in the world. Rather, quantifier words specify relationships between sets of entities, events and properties. To provide intuitions about the semantics of quantifier words, and to be able to refer to quantifiers in a language-independent way, we rely on the notion of generalized quantifiers (Mostowski, 1957), as described in §2.

**Quantifier words vary across languages** Quantifier word inventories differ across languages. English CONTEXT: A piece of paper was later found on which he had written his last statements in two languages, Latin and German. Only one statement was in Latin and the rest in German. O QUESTION: In what language were most statements written? ANSWER: German PREDICTED AN-SWER: Latin and German PREMISE: Más de tres personas resultaron heridas en Spanish un accidente de dos vehículos en la Ruta 30 el lunes por la noche. (translation: More than three people were injured in a two-vehicle crash on Route 30 Monday NLI evening.)

HYPOTHESIS: Había 4 personas involucradas. (translation: There were 4 people involved. LABEL: Neutral PREDICTED LABEL: Entailment

Table 1: Examples of quantifiers (marked in bold texts) in NLP tasks, with RoBERTa's prediction for QA and XLM-R's prediction for NLI after fine-tuning.

041

043

045

047

049

051

054

060

061

062

063

064

Often what is considered rough translation equivalents also differ in syntax, fine-grained semantics or pragmatics. Stateva et al. (2019) show, e.g., that perceptions of the numerical bounds of existential quantifiers differ across speakers of English, French, Slovenian, and German. Other papers showing discrepancies between quantifier systems include comparisons of Salish to English (Matthewson, 2001), Adyghe to English (Nikolaeva, 2012), or of Dutch, Hebrew and Bengali (Gil, 1982). The cross-linguistic differences in how generalized quantifiers are expressed motivates a cross-lingual error analysis, since quantifiers may contribute more to error when processing some languages rather than others.

**Quantifier words are important** Quantifier words are extremely important for tasks that require inference, including natural language inference, question answering, fact-checking, etc. Datasets have, for example, been developed for numerical reasoning in English (Dua et al., 2019). Several researchers have identified quantifier words as important sources of errors for natural language processing systems (Joshi et al., 2020); see Table 1

Generalized Quantifiers	Logical Denotation	Example
some(A)(B) = 1	$A \cap B \neq \varnothing$	This process is known to increase security in several ways.
all(A)(B) = 1	$A \subseteq B$	Everyone agreed the food was terrible.
more than $\mathbf{k}$ the(A)(B) = 1	$ A \cap B  > k$	They do let them go more than twice a week.
less than k the(A)(B) = $1$	$ A \cap B  < k$	San Augustin Acolman has less than 1,000 residents.
the <b>k</b> (A)(B) = 1	$ A \cap B  = k$	Please donate 100 million to the School of Nursing.
<b>between p and k</b> the(A)(B) = $1$	$p <  A \cap B  < k$	The USA added ten states to its nation between 1800 and
		1850.
the <b>p/k</b> (A)(B) = 1	$ A \cap B  = p \cdot ( A /k)$	Captain Blood has 20/20 vision.
the $\hat{k}\%$ (A)(B) = 1	$ A \cap B  = \hat{k} \cdot ( A /100)$	The lending fund is always guaranteed 9% interest.
most (A)(B) = 1	$ A \cap B  >  A \setminus B $	Most ZIP Codes cover roughly ten thousand addresses.
few(A)(B) = 1	$ A \cap B  <  A \setminus B $	Only a few teenagers were still listening to Rock 'n' Roll.
each other $(A)(B) = 1$	$\forall a \in (A \cap B) \exists b \in$	All of these trails are located within the a one hour drive of
	$(A \cap B)(a \neq b)$	each other.

Table 2: The categorization set of quantifiers for task analysis. The first six are Aristotelian/counting quantifiers and the following four are proportional quantifiers. The last one is a Ramsey quantifier (Schmerl and Simpson, 1982). For each quantifier, its logical denotation is listed in the second column. The third conlumn contains English examples with quantifiers taken from XNLI.

for examples of such errors. Unfortunately, most efforts have concentrated on subsets of quantifier words and on English.

Contributions We analyze how quantifiers are represented in NLU benchmarks, and how their occurrence at test time contributes to errors by neural language models (LMs). We derive a linguistically motivated 11-way categorization set for generalized quantifiers and look into their distribution in three steps: (a) monolingual NLI; (b) cross-lingual NLI; (c) cross-lingual question answering. We also propose GQNLI, an adversarial generalized quantifier NLI challenge dataset. Our work shows that (i) generalized quantifiers are pervasive and cause overall performance drops in NLU benchmarks; (ii) the contribution of quantifier words to system error varies across languages; and (iii) generalized quantifiers are particularly difficult for LMs in interaction with negation and subsumption.

### 2 Background

065

066

068

073

077

086

091

096

097

Generalized quantifiers (GQs) are developed upon first-order predicate logic, denoting relations between sets (Mostowski, 1957). Given a universe E, a quantifier Q would be treated as a mapping  $Q_E$  from the Cartesian product of powersets  $\mathcal{P}(E) \times \mathcal{P}(E)$  to the set {*false,true*} or, as a binary relation on subsets of E (Dvořák and Holčapek, 2015). GQs are generalizations of the  $\forall,\exists$  quantifiers from first-order predicate logic (Mostowski, 1957; Lindström, 1966; Montague, 1973; Bach et al., 1995; Keenan and Paperno, 2012). A generalized quantifier is, abstractly, a relation between sets. Generalized quantifier theory, while developed by logicians, is used by formal linguists to analyze the meaning of quantifier words in combination with referential expressions (Barwise and Cooper, 1981; Higginbotham and May, 1981). 099

100

101

102

103

104

105

106

107

108

110

111

112

113

114

115

116

117

118

119

120

121

122

123

124

125

127

128

129

130

131

132

133

Most human languages contain ways of expressing generalized quantifiers, and their semantics exhibit striking similarities across languages (Matthewson, 2004; Fintel and Matthewson, 2008; Steinert-Threlkeld, 2019). At the same time, generalized quantifiers can be instantiated very differently across languages due to pragmatic considerations (Grice, 1989) or cognitive economy and cost-benefit optimisation in the exchange of information (Sperber and Wilson, 1986; Levinson et al., 2000). Quantifier words also exhibit syntactic differences, e.g., with some languages having specialized words to express quantity, while others rely on metaphorical usage of common nouns (Katsos et al., 2012). In English, most is a determiner, but Spanish and French express the same concept through common nouns, la mayoría and la majorité. The relative stability of the core semantics of quantifiers makes a cross-linguistic comparison possible, but the syntactic and pragmatic variation associated with the expression of generalized quantifiers poses a challenge for multilingual NLU. We consult quantifier taxonomy studies (Keenan and Westerståhl, 1997; Peters and Westerståhl, 2006; Szymanik and Thorne, 2015; Szymanik, 2016) and derive a categorization set for quantifier analysis in NLU benchmarks. In Table 2, we list the 11way quantifier categorization set and their logical denotation based on set theory.

While other foci of formal linguistics have attracted the attention of NLP researchers—including coreference (Ogrodniczuk et al., 2019, 2020), nega-

		-	Eng	glish			Cross-
Quantifier	E,	mm		R	_R2	R3	lingual
	'I'INW	'I'INW	ΓI		T,	ANLI_R3	ILL
	М	М	SNL	ANLI	ANI	AN	XNL
some	171	132	191	5	1	17	115
all	255	239	65	15	8	29	166
> k	14	23	8	10	16	14	16
< k	3	3	0	6	7	5	1
k	266	269	988	55	62	48	159
between	2	3	0	3	2	0	1
p/k	1	5	1	1	1	0	2
k%	10	7	0	0	0	1	5
most	35	39	1	0	2	1	9
few	14	15	11	0	0	6	11
each other	4	3	35	0	0	2	5
Total	775	738	1300	95	99	124	499
Frequency	7.9%	7.5%	13.2%	9.5%	9.9%	12.4%	10.0%

Table 3: Quantifier distribution in four NLI tasks, among which three are monolingual English and one is cross-lingual. The table show statistics of the test set, if not available, dev set, of the target task. All but the last rows show the occurrence time of the type of quantifier in the first column. The last row represents the distribution rate of any quantifier in the dataset.

tion (Hossain et al., 2020; Hartmann et al., 2021), and consistency (Li et al., 2019; Ribeiro et al., 2019; Asai and Hajishirzi, 2020)—there has been little work on generalized quantifiers as a source of error in NLU, let alone in multilingual NLU. It remains an open problem whether LMs represent the semantics of quantifiers words adequately, or if they provide a basis for resolving scopal ambiguities.<sup>1</sup>

#### **3** NLU Benchmarks

134

135

136

137

138

139

140

141

142

143

144

145

146

147

148

149

150

151

152

153

154

155

156

157

158

We conduct an error analysis focusing on the role of generalized quantifiers in two NLU tasks, Natural Language Inference (NLI) and Question Answering (QA), which generally require understanding of quantifiers. For each type of task, both monolingual and cross-lingual evaluation are conducted. We focus on generalized quantifiers in the *hypotheses* in NLI examples—and on generalized quantifiers in the *question* fields in question answering. To this end, we identify quantifiers by the lemma and the universal dependency relation (Nivre et al., 2020) of a quantifier after preprocessing the sentences using *Stanza* (Qi et al., 2020). Take the sentence "The Yiddish culture has survived for more than a thousand years.", we annotate it as

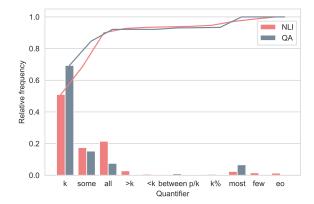


Figure 1: Relative distribution of quantifiers in NLI and QA tasks ranked by semantic complexity. The bars show the relative frequency of such quantifier and the lines indicate the cumulative frequency for a task.

159

160

161

162

163

164

165

166

167

168

169

170

171

172

173

174

175

176

177

178

179

180

181

182

183

184

185

186

188

190

191

"The/det Yiddish/amod culture/nsubj have/aux survive/root for/case more/advmod than/fixed a/det thousand/nummod year/obl ./punct". By matching the regex pattern of the quantifier "more than k", in this case "((more|great)\advmod than V(fixed|case)|atVcase leastVnmod) .+Vnummod .+V(nsubj|obj|obl)", we approximate the surface form of the type "more than k". Through matching quantifier patterns, we are able to find entries in which quantifiers are instantiated. See Appendix A for the list of regex patterns we write to identify GQs. In Table 3 and Table 6, we present the statistics of the quantifier distributions in NLI and QA tasks, respectively. As can be seen, quantifiers are indeed widespread in NLU tasks, accounting for roughly 10% in NLI tasks and 5% in QA tasks. We will further discuss the statistics and experiments in the following section.

# 4 Quantifiers in English NLI Benchmarks

NLI is commonly framed as a three-way classification task with labels *entailment*, *contradiction* and *neutral* (Bowman et al., 2015a). While SOTA models exhibit low error rates on NLI benchmarks, it is unclear when they succeed or fail in their underlying reasoning. We are interested in whether generalized quantifers challenge modern NLI models. In our error analysis, we initially focus on three English NLI datasets, MultiNLI (MNLI; Williams et al., 2018), SNLI (Bowman et al., 2015a) and ANLI (Nie et al., 2020) as testbeds.

Table 3 presents statistics of quantifier distribution in these datasets, where we observe that,

<sup>&</sup>lt;sup>1</sup>Note that generalized quantifiers are not always *explicit* in discourse. The sentence *inadequate sleep causes obesity* should be interpreted as *Most of those who do not sleep adequately, gain weight* (Zadeh, 1983). Such implicit quantifiers related to pragmatic variation are important for language understanding, but will be ignored in this work.

				BERT			~			1	RoBERT	a		~
Quantifier	M_m	M_mm	IJNS	$A_R^{-}R1$	A_R2	A_R3	weighted	M_m	M_mm	IJNS	$A_R^{-}R1$	A_R2	A_R3	weighted
some	82.5	84.1	86.9	100	0	47.1	83.4	83	84.8	86.9	100	100	41.1	83.7
all	85.9	88.3	89.2	46.7	37.5	34.5	83.2	85.9	92.1	90.8	66.7	37.5	34.5	85.3
> k	85.7	100	87.5	70	43.8	42.9	73	85.7	91.3	87.5	80	37.5	28.5	68.2
< k	100	100		33.3	57.1	80	66.7	100	100		83.3	85.7	100	91.7
k	87.2	81.8	92.4	43.6	43.5	33.3	84.8	88.3	88.8	92.9	56.3	61.3	43.8	87.8
between	100	100		66.7	50		80	100	66.7		66.7	50		70
p/k	100	60	100	100	100		77.8	100	80	100	100	0		77.8
$p/k \ k\%$	90	100				100	94.4	70	85.7				0	72.2
most	74.3	79.5	0		50	0	74.4	77	87.2	100		59	0	80.9
few	78.6	73.3	90.9			33.3	73.9	85.7	80	90.9			33.3	78.3
each other	75	100	85.7			50	84.1	50	100	88.6			50	84.1
all GQs	85	84.8	91.2	50.5	44.4	39	83.3	85.4	88.8	91.7	65.3	56.5	40.3	85.5
full	86.5	86.1	91.3	58.6	48	43.2	84.4	89.5	89.4	92.3	71.7	49.6	49	87.3

Table 4: BERT and RoBERTa performance on NLI tasks. The *weig*. column represents the percentage of all true predictions in six subtasks over total instances. The penultimate row stands for the overall performance when quantifiers exist in a dataset. The last row reports the overall performance in a dataset. Number marked in bold signifies a lower score than the overall performance.

across, about 10% of all hypotheses contain quantifier words, indicating the pervasiveness of quantification. We also plot the frequency of quantifiers in NLI in Figure 1 and find the quantifier word distribution follows Zipf's law (Zipf, 1949). Note the top three most common quantifiers account for more than 90% of all.

192

193

194

195

196

197

198

199

200

201

204

205

210

211

212

213

214

215

216

217

218

219

221

222

223

Experiments and Results In order to investigate whether NLU systems can solve quantifiers in NLI, we experiment with two pretrained LMs: BERT<sup>2</sup> (Devlin et al., 2019a) and RoBERTa<sup>3</sup> (Liu et al., 2019). We use the codebase by Nie et al. (2020). The training data combines SNLI, MNLI, FEVER-NLI (Nie et al., 2019) and ANLI.

In Table 4, we report the test set performance on SNLI and ANLI, and the dev set performance on MLNI *matched* and *mismatched* sections. We can observe that SOTA models suffer from performance drops across almost all quantification phenomena in every task. When it comes to performance over all quantifiers, the improvement from RoBERTa to BERT (2.2%) is less prominent than that over full datasets (2.9%), suggesting RoBERTa is particularly challenged.

Taking a closer look at error by category, proportional quantifiers seem harder to solve than Aristotelian/counting quantifiers. Except for k%, all proportional quantifiers—p/k, most, and few—are about 10% lower than the five counting quantifiers (except less than k) with BERT; and about 5% lower with RoBERTa. RoBERTa is not generally superior to BERT; e.g., for k%, BERT outperforms it by 22%. We show a pairwise analysis of how GQs affect performance when they appear in both the premises and hypotheses in the Appendix B. Generally, our results attest to the difficulty of resolving GQs in NLI benchmarks. 225

226

227

229

231

232

233

234

235

236

237

238

239

240

241

242

243

244

245

246

247

249

251

252

253

254

255

# 5 Quantifiers in Cross-lingual NLU Benchmarks

Quantifiers are acquired in similar orders across languages (Katsos et al., 2016), although languages express quantifiers in different ways. For example, there are eight different universal quantifiers with different level of distributivity in Malagasy (Matthewson, 2008). This poses challenges to training multilingual LMs and transfer learning. We are interested in whether quantifiers are universally and evenly challenging for all languages.

**Quantifiers in Cross-lingual NLI** We choose XNLI (Conneau et al., 2018), a manual translation of the development and test set of MNLI into 15 languages, for this multilingual error analysis. We should clarify that for XNLI, the authors annotate entailment labels for the English data only and apply them to the other languages. We do not assume label changes due to translation in this study, but it is worth investigate in the future. We choose five languages belonging to different language families, namely Arabic, Chinese, German, Spanish and Vietnamese as targets. The last column in Table 3 shows the numbers of quantifiers in XNLI. The distribution rate is 10%. Note that the universal quantifier is the most common quantifier in XNLI.

We fine-tune mBERT<sup>4</sup> (Devlin et al., 2019b) and XLM<sup>5</sup> (Lample and Conneau, 2019) on the MNLI

<sup>&</sup>lt;sup>2</sup>wwm\_cased\_L-24\_H-1024\_A-16

<sup>&</sup>lt;sup>3</sup>roberta-large

<sup>&</sup>lt;sup>4</sup>multi\_cased\_L-12\_H-768\_A-12

<sup>&</sup>lt;sup>5</sup>xlm-mlm-100-1280

0				mBER	Г						XLM			
Quantifier	en	zh	es	ar	vi	de	weig.	en	zh	es	ar	vi	de	weig.
some	85.2	69.6	80	63.5	67.8	74.8	73.4	85.2	70.3	79.1	71.3	73.9	69.6	69.6
all	80.1	65.7	72.8	69.3	63.9	74.1	70.9	82.5	62.7	74.1	67.5	71.7	73.5	72
> k	87.5	50	68.8	43.8	56.2	62.5	61.6	81.2	62.5	56.2	62.5	50	75	75
< k	100	100	100	100	100	100	100	100	100	100	100	100	100	100
k	86.2	69.1	80.5	71.7	76.7	82.4	77.7	83	66.7	78.6	71.7	74.2	81.1	75.8
between	100	100	100	100	100	100	100	100	100	100	100	100	100	100
p/k	100	50	100	100	100	100	91.7	100	0	100	100	50	50	66.7
k%	100	100	80	100	100	100	96.7	80	80	80	100	100	80	86.7
most	55.6	55.6	66.7	66.7	33.3	66.7	57.4	55.6	33.3	66.7	55.6	44.4	77.8	55.6
few	72.7	54.5	72.7	63.6	45.5	72.7	63.6	63.6	36.4	54.5	63.6	54.5	72.7	57.5
each other	60	60	60	60	80	80	66.7	80	20	60	20	40	60	46.7
all GQs	83	67.1	76.7	68.1	68.3	76.9	73.3	82.4	64.2	75.7	69.3	71.4	74.8	73
comp.	82.6	88.9	74.7	65.6	70.7	71.4	72.4	83.1	64.8	76.3	66.9	71.6	71.3	72.3

Table 5: Results of mBERT and XLM performance on XNLI tasks decomposed by quantifier categories.

Ouentifier			MLQA			Х	QuAD
Quantifier	en	zh	es	ar	vi	de	
some	66	39	41	44	37	33	12
all	31	14	26	21	19	16	7
> k	0	0	0	0	0	0	0
< k	1	0	0	0	1	0	0
k	322	168	166	195	204	149	32
between	4	2	2	2	3	0	3
p/k	1	1	1	0	0	0	0
k%	1	1	0	1	0	0	0
most	27	19	11	30	17	9	5
few	0	0	0	0	0	0	0
each other	0	0	0	0	0	0	0
Total	453	244	247	293	281	207	59
Frequency	3.9%	4.7%	4.7%	5.4%	5.1%	4.5%	5.0%

Table 6: Quantifier distribution in two multilingual QA tasks, MLQA and XQuAD. We choose six common languages apprearing in both tasks to facilitate comparisons. XQuAD is strictly parellel while MLQA is not, hence only the latter has statistics by languages.

training set and evaluate them on XNLI. We report the results in Table 5. We find that performance varies across languages. For Chinese and Vietnamese, we see significant drops in performance for examples with GQs, whereas for Arabic and German, we see improvements. The results *per* quantifier are more homogeneous, however.

257

258

261

263

265

268

269

Similar to our results for English, we can see that the lowest accuracies in XNLI are with proportional quantifiers, such as *most* and *few*. But the gap in non-English languages is wider for these two categories, especially for Chinese, the difference reaches 30%. Other hard quantifiers include *all*, > k, < k, and *each other*.

271Quantifiers in Cross-lingual QACross-lingual272question answering (XQA) is another important273NLU task that evaluates the cross-lingual transfer-274ability of LMs. We evaluate the effect of quantifiers275on system errors across two XQA datasets, namely276XQuAD (Artetxe et al., 2020) and MLQA (Lewis277et al., 2020). As demonstrated in Figure 1, quan-

tifier word distributions in XQA tasks also follow Zipf's law, as in NLI tasks, but k is more frequent (perhaps because of a traditional emphasis on numerical reasoning), and we see less variance across languages. This is probably because question answering is targeting quantification less directly. To evaluate cross-lingual QA performance on GQs, we fine-tune mBERT and XLM-R<sup>6</sup> (Conneau et al., 2020) using Hu et al. (2020)'s architecture. We present results for mBERT in Table 7; for XLM-R results, please refer to Appendix D. 278

279

280

281

284

285

287

289

291

292

293

294

296

297

298

299

300

301

302

303

304

305

306

307

308

309

310

311

Just as with XNLI, LMs suffer from performance drops across all languages for almost all GQ phenomena with significant, cross-lingual variation. The most distinguished is that Exact Match (EM) suffers from a greater deterioration than F1 scores for all languages. For example, the weighted EM difference for mBERT on MLQA is 2.9% while the weighted F1 is 1%. As one example in Table 1, we observe that the plausible answers selected by models, while being incorrect, result in a sharper decrease of EMs comparing to F1s. Questions containing GQs also tend to have less verbal answers comparing to those without GQs, and therefore require higher precision.

Regarding cross-lingual comparisons, Chinese and Arabic are the two languages that do not have lower performance over GQs compared to the performance over the complete dataset. Despite the overall trends, subtle differences from XNLI performance still exist. For example, XLM-R is worse than mBERT on quantifier reasoning on XQuAD Chinese, especially at proportional quantifiers, but this is not the case on MLQA Chinese.

							XQ	JAD													ML	.QA						
Quantifier	е	n	2	zh	e	s	a	ır	1	/i	d	e	weig	hted	e	n	2	h	е	s	a	ur -	,	/i	ċ	le	wei	ghted
	EM	F1																										
some	75	84.2	50	55.5	58.3	76.1	50	50	16.6	42.4	33.3	43.8	47.2	58.7	59	80	28.2	52.1	34.1	59.2	36.3	54.9	5.4	24	33.3	58.4	32.7	54.8
all	28.5	62.2	14.2	35.2	28.5	82	42.8	52.3	14.2	29.4	28.5	56	26.1	52.9	67.7	79.8	14.2	46.4	38.4	62.8	33.3	57.9	10.5	30.1	31.2	51.6	32.6	54.8
> k																												
< k														0	0							0	13.3			0	6.7	
k	78.1	90.1	68.7	80.4	56.2	72.1	40.6	64.3	12.5	35.7	56.2	77.1	52.1	70	74.9	79.4	47	63.4	41.5	65.9	27.6	50.3	6.3	23.7	38.2	53	39.3	56
between	100	100	33.3	72.2	66.6	93.3	100	100	0	19	0	56.5	50	73.5	50	88.5	50	83.3	0	26.6	0	68.7	0	26.6			20	58.3
p/k													100	100	0	0	0	0							33.3	33.3		
k%												100	100	0	26.6			0	23.7					33.3	50.1			
most	40	53.3	40	40	0	10	0	26.6	0	0	20	49.3	16.7	29.9	55.5	7	47.3	62.1	45.4	61.7	30	46.8	5.8	15.7	33.3	40.7	36.2	50.3
few																												
each other																												
all GQs	70	83.2	55	66.7	50	70.3	41.6	58.2	11.6	32.5	43.3	65	45.3	62.7	63.5	79.2	41.8	60.3	39.6	63.7	29.3	51.3	6.4	23.6	36.1	53.2	36.1	55.2
comp.	71.8	83.7	48	59.1	56	74.5	40.8	57.9	13.9	32.4	50.7	67.2	46.9	62.5	67.2	80.6	37.5	57.9	47.3	66	30	48.4	11.2	28	40.8	56	39	56.2

Table 7: Results of mBERT performance on XQA tasks decomposed by quantifier categories.

	antifier ccurrence	some 27	all 51	$> k \\ 51$	< <i>k</i> 33	k 170	between 21	$\frac{p/k}{24}$	$^{k\%}_{45}$	most 18	few 9	each other 36	<i>Overall</i> 485
Model	Training Data						% Pe	rforma	nce				
ELECTRA	S,M,F,ANLI	25.9	15.7	19.6	27.3	24.1	71.4	0	26.7	11.1	11.1	22.2	26.7
BERT	S,M,F,ANLI	40.7	41.2	33.3	30.3	30.6	14.3	37.5	22.2	61.1	22.2	41.7	30
SBERT	S,M,F,ANLI	7.4	29.4	27.5	21.2	34.7	57.1	62.5	40	22.2	11.1	33.3	34.3
RoBERTa	MNLI S,M,F,ANLI	55.6 40.7	25.5 23.5	17.6 41.2	27.3 <b>45.5</b>	24.7 40	23.8 57.1	45.8 25	17.8 33.3	33.3 27.8	33.3 0	11.1 22.2	28.2 37
BART	MNLI S,M,F,ANLI	51.9 37.0	27.5 39.2	25.5 <b>58.8</b>	36.4 33.3	31.2 <b>47.6</b>	23.8 76.2	50.0 25.0	13.3 <b>53.3</b>	44.4 16.7	<b>66.7</b> 33.3	30.6 30.6	31.3 41.7
ALBERT	S,M,F,ANLI	44.4	37.3	49	27.3	44.1	57.1	50.0	46.7	16.7	0	33.3	42
DeBERTa-v3	MNLI M,F,ANLI M,F,Ling,DocNLI	48.1 51.9 <b>66.7</b>	37.3 41.2 <b>52.9</b>	41.2 23.5 35.3	12.1 33.3 <b>45.5</b>	40 37.1 44.1	33.3 57.1 66.7	<b>66.7</b> 50.0 50	20 13.3 31.1	50 61.1 50	33.3 33.3 33.3	<b>41.7</b> 33.3 <b>41.7</b>	40.7 41.3 <b>42.7</b>

Table 8: GQNLI statistics and seven types of models' performance with different combinations of training data. The second row shows the occurrence time of the type of GQ in GQNLI. The following rows show models' performance on the dataset. We tested most competitive models fine-tuned for NLI available on Hugging Face. All but ALBERT (xxlarge) and DeBERTa-v3 (base) are size large. S, M, F, Ling, A, DocNLI refer to SNLI, MNLI, Fever-NLI, LingNLI (Parrish et al., 2021), ANLI and DocNLI (Yin et al., 2021), respectively. Numbers in bold represent the highest accuracy in one category. Due to space limitation we provide the link to each modelin the Appendix H.

#### 6 GQNLI

312

313

314

315

319

320

322

323

324

325

326

We have seen how quantifiers present challenges to NLI and QA models. Using an approach similar to ANLI (Nie et al., 2020) and DynaBench (Kiela et al., 2021), we use model difficulty (RoBERTa's) as a heuristic to select hard examples for a challenge dataset that can hopefully be used to evaluate any future progress on this. We propose GQNLI, a generalized quantifier NLI challenge dataset, consisting of 30 premises and 300 hypotheses. The average sentence lengths of hypothesis and premises are 15.97 and 7.35, respectively. Both numbers are comparable to those of MNLI, but lower than ANLI's (Williams et al., 2020). It should be noted that GQNLI is designed for evaluating future models; obviously not for benchmarking RoBERTa.

328Dataset CreationFirstly, we manually create329100 premise-hypothesis pairs, in which various330types of GQs appear. For each premise and hy-

pothesis, the number of GQs varies from one to three. To choose the premises, we randomly sampled 100 premises with GQs from SNLI and ANLI test sets, respectively, and selected 30 premises in total, that we consider are semantically adequate for adding GQs and making simple hypotheses.

To construct the hypotheses, we rely on RoBERTa fine-tuned on MNLI and manually select examples about which the model is unsure or incorrect. To focus on GQs, we keep the challenge examples otherwise simple (Ribeiro et al., 2020), and avoid lexical variations in the hypotheses. Hard examples were found to be characterized by (i) mixing generalized quantifiers with other logical operators, such as subsumption or negation, and (ii) combining multiple different generalized quantifiers. We discuss these observations in Section 7.

Two of the authors annotated the examples. The inter-annotator agreement (Fleiss' kappa) was 0.895, substantially higher than ANLI's (0.672– 0.740). We augmented the examples by substi-

350

351

331

332

333

<sup>&</sup>lt;sup>6</sup>xlm-roberta-large

447

448

449

450

451

452

453

403

353tuting non-quantifier words (e.g., replacing "dogs"354with "cats") while keeping the labels, to exclude355the effect of specific lexical items. The resulting356labels are uniformly distributed. Table 8 presents357GQNLI statistics. Since the dataset is curated to358probe the ability to reason with quantifiers, the dis-359tribution of generalized quantifiers does not follow360Zipf's law; see §4. A list of GQNLI examples per361category is shown in Appendix E.

362

363

364

368

374

377

380

381

386

390

400

401

402

**Experiments and Results** We evaluate seven types of models on GQNLI, fine-tuned with different combinations of NLI datasets. As data creation only relied on RoBERTa and MNLI, nothing prevents that models with different architectures and training data will perform well. They do not, however. The results are shown in Table 8.

We see that all models have great difficulty with GQNLI. With more training data, models improve, but the best performance is 42.7%, less than 10 points above chance level. In general, the counting quantifiers, especially the existential and universal quantifiers, are easier than proportional quantifiers. Particularly, most models struggle with *less than k* and *few*. This is in some contrast with the NLU tasks studied above, where these quantifiers were among the easiest.

We also observe unstable GQ reasoning ability in simple word substitution cases. For instance, it happens for DeBERTa fine-tuned with M, F, Ling, DocNLI that it predicted correctly the contradiction relation between "There are six children standing on top of a yellow mountain. Two thirds wear red tops and one third wear green." and "Between 80% and 90% children do not wear red tops.", but incorrectly when "red" is substituted with "beige" and "green" with "cyan". We are yet to study what kind of cues lead to the instability. Our experiments suggest a lack of testing proportionality reasoning and robustness in existing benchmarks.

### 7 Discussion

**Negation** The interaction between negation words and quantifiers increases semantic complexity (Partee, 1970; Horn, 2010). We investigate whether this holds for NLI tasks, using negation cue detection to find all cases where a negation word and a quantifier appear in the hypotheses.

We break down the performances on negation of the seven models in Appendix F. As indicated, LMs overall have worse results for negation cases comparing to the entire dataset. We can see a majority of the models even predicted opposite labels for some GQ categories, with 0% accuracy. DeBERTav3 is no longer the best model, replaced by BERT and BART. The improvement by training with more data becomes unstable for reasoning over GQs with negation.

For a cross-lingual investigation of the interaction of GQs and negation, we find that in XNLI, the number of cases combining both phenomena is insufficient: we identified four such cases, involving only the quantifiers "all" and "more than." For English, mBERT predicted two cases successfully. For Chinese, German, Vietnamese and Arabic, one is correct. For Spanish, all are wrongly predicted.

It is evident that NLU models suffer from reasoning difficulties in certain cases when negation interacts with GQs, especially in cross-lingual evaluation. In future work, we are interested in expanding GQNLI to more instances and more languages to facilitate qualitative investigations.

Subsumption In generalized term subsumption languages (TSLs; Yen, 1991; Ali and Shapiro, 1993), a term a subsumes another term b if and only if the extension of a is a superset of the extension of b. Rather than surface number comparison, subsumption reasoning requires knowledge of the relations between supersets and subsets. For example, to decide whether "There are six dogs. Three brown dogs, a black dog and a white dog run along the green grass" entails "One dog sits", LMs should be aware that "six dogs" is a superset of the extension of the "brown dogs", "black dog" and "white dog". Another example in GQNLI is to infer whether "There are twelve singers on a stage, less than half from Argentina and one from Cape Verde" entails "Several singers do not come from Chile".

We annotate 63 cases out of the first 100 in GQNLI requiring subsumption reasoning. We show the statistics and results regarding subsumption in Appendix G. It can be seen that more training data leads to higher accuracies. Especially, DeBERTa fine-tuned with DocNLI, which unifies the two classes "neutral" and "contradict" into a new class "not entail", has a significant improvement on subsumption cases with neutral label. The training bias give an advantage to the model on the subsumption subset, half cases of which are labelled neutral. But such bias has a negative effect on non-subsumption cases; the accuracy drops by 16.2% comparing to the model without training with DocNLI. It is worth investigating whether

544

545

546

547

548

549

550

551

504

505

DocNLI is truly helping subsumption reasoning in future work. Subsumption is a key concept in the 455 study of knowledge representation (Woods, 1991), 456 but is neglected in current NLP research. The fact that LMs struggle to perform subsumption reasoning asserts the necessity to explicit tackle the problem.

#### **Related Work** 8

454

457

458

459

460

461

462

463

464

466

467

468

469

470

471

472

473

474

475

476

477

478

479

480

481

482

483

484

485

486

487

488

489

490

491

492

493

494

495

496

497

498

499

500

501

We examine the sensitivity of NLU models to generalized quantifiers. These models are designed to induce correlations from large volumes of data, not to reason symbolically with logical quantifiers. Such models have, nevertheless, been probed for logical knowledge.

Mul and Zuidema (2019), for example, show neural networks encode fragments of first-order logic and exhibit zero-shot generalization ability. Evans et al. (2018) present a neural architecture that improves performance on propositional logical inference. Bowman et al. (2015b) also suggest neural networks learn semantic representations for logical inference in natural languages. However, on the same task, Veldhoen and Zuidema (2017) find neural networks fail to do so on a more stringent test. Geiger et al. (2019) also show that neural networks fail to exhibit robust logical inference. Srivastava et al. (2018) use semantic parsers to encode quantifiers and improve zero-shot learning in classification tasks. Haruta et al. (2020) present a system that computes logical inference over GQs and see improvements on two specialized datasets, FraCaS (Cooper et al., 1994) and MED (Yanaka et al., 2019). None of these papers explicitly discussed generalized quantifiers, and all were limited to studying the ability of neural networks to capture the logical semantics of English.

Many studies have instead focused on LMs' ability to capture negation (Gururangan et al., 2018; Naik et al., 2018; Hossain et al., 2020; Ettinger, 2020; Hartmann et al., 2021) or coreference (Ye et al., 2020; Varkel and Globerson, 2020; Abdou et al., 2020). Others have focused on LMs' ability to reason with numbers (Johnson et al., 2020). DROP (Dua et al., 2019), for example, is a question answering dataset designed specifically to probe LMs' ability to count, add and subtract for answering factoid questions. Models have also been tailored for numerical reasoning (Geva et al., 2020; Zhang et al., 2020). Cobbe et al. (2021) proposes to use a verification task during pretraining of LMs

to improve their ability to solve math word problems. Others have studied monotonicity inference (Hu et al., 2019; Yanaka et al., 2019, 2020), and Fang and Lou (2021) recently focused on the two quantifier words part and whole in an error analysis for named entity recognition.

Many NLU benchmarks contain quantifier words, but their influence on performance has not been studied systematically. One exception to this is that generalized quantifiers have been used to generate adversarial examples in the context of numerical reasoning (Naik et al., 2018; Nie et al., 2020). TaxiNLI (Joshi et al., 2020), which categorizes 15 types of reasoning abilities, is a dataset drawn from MNLI. In their taxonomy, the Quantifier category only refers to universal and existential quantifiers, not to generalized quantifiers, and ditto for Kim et al. (2019). All of the above focused on English, but in an extension to TaxiNLI, K et al. (2021) incorporated quantifiers into the Logic class and found a large cross-lingual tranfer gap on LMs.

#### 9 Conclusion

Quantifiers lie in the intersection of logic, linguistics and NLP research. It is essential for NLU systems to learn quantifier reasoning. We examined generalized quantifiers in NLU tasks with regards to their expressiveness and logical reasoning requirement. Our survey and experiments indicate quantifiers are neglected to a degree and cause significant performance drops for neural LMs. To better understand LMs' reasoning abilities, we release GQNLI,<sup>7</sup> a novel generalized quantifier NLI challenge dataset. With the pervasiveness of generalized quantifiers, we stress that more efforts are necessary to investigate: (1) when and why models systematically fail when quantifiers interact with other operators; (2) how to improve cross-lingual transferability of quantifiers; (3) how we can exploit the theoretical results about generalized quantifiers from logic and linguistic studies, so as to improve the logical inference ability of neural LMs.

## References

Mostafa Abdou, Vinit Ravishankar, Maria Barrett, Yonatan Belinkov, Desmond Elliott, and Anders Søgaard. 2020. The sensitivity of language models and humans to Winograd schema perturbations. In Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics, pages 7590-

<sup>&</sup>lt;sup>7</sup>Attached as Supplementary Data to this submission.

658

659

660

7604, Online. Association for Computational Linguistics.

552

553

554

558

563

564

565

566

567

571

576

579

582

588

589

590

591

594

595

599

601

602

603

606

- Syed S Ali and Stuart C Shapiro. 1993. Natural language processing using a propositional semantic network with structured variables. *Minds and machines*, 3(4):421–451.
- Mikel Artetxe, Sebastian Ruder, and Dani Yogatama. 2020. On the cross-lingual transferability of monolingual representations. In *Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics*, pages 4623–4637, Online. Association for Computational Linguistics.
- Akari Asai and Hannaneh Hajishirzi. 2020. Logicguided data augmentation and regularization for consistent question answering. In *Proceedings of the* 58th Annual Meeting of the Association for Computational Linguistics, pages 5642–5650, Online. Association for Computational Linguistics.
- Emmon W. Bach, Eloise Jelinek, Angelika Kratzer, and Barbara H. Partee. 1995. Quantification in natural languages.
- Jon Barwise and Robin Cooper. 1981. Generalized quantifiers and natural language. In *Philosophy, language, and artificial intelligence*, pages 241–301. Springer.
- Samuel R. Bowman, Gabor Angeli, Christopher Potts, and Christopher D. Manning. 2015a. A large annotated corpus for learning natural language inference. In Proceedings of the 2015 Conference on Empirical Methods in Natural Language Processing, pages 632–642, Lisbon, Portugal. Association for Computational Linguistics.
- Samuel R. Bowman, Christopher Potts, and Christopher D. Manning. 2015b. Recursive neural networks can learn logical semantics. In *Proceedings of the 3rd Workshop on Continuous Vector Space Models and their Compositionality*, pages 12–21, Beijing, China. Association for Computational Linguistics.
- Karl Cobbe, Vineet Kosaraju, Mohammad Bavarian, Jacob Hilton, Reiichiro Nakano, Christopher Hesse, and John Schulman. 2021. Training verifiers to solve math word problems. *ArXiv*, abs/2110.14168.
- Alexis Conneau, Kartikay Khandelwal, Naman Goyal, Vishrav Chaudhary, Guillaume Wenzek, Francisco Guzmán, Edouard Grave, Myle Ott, Luke Zettlemoyer, and Veselin Stoyanov. 2020. Unsupervised cross-lingual representation learning at scale. In Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics, pages 8440– 8451, Online. Association for Computational Linguistics.
- Alexis Conneau, Ruty Rinott, Guillaume Lample, Adina Williams, Samuel Bowman, Holger Schwenk, and Veselin Stoyanov. 2018. XNLI: Evaluating cross-lingual sentence representations. In Proceedings of the 2018 Conference on Empirical Methods

*in Natural Language Processing*, pages 2475–2485, Brussels, Belgium. Association for Computational Linguistics.

- Robin Cooper, Richard Crouch, Jan Van Eijck, Chris Fox, Josef Van Genabith, Jan Jaspers, Hans Kamp, Manfred Pinkal, Massimo Poesio, Stephen Pulman, et al. 1994. Fracas: A framework for computational semantics. *Deliverable D6*.
- Jacob Devlin, Ming-Wei Chang, Kenton Lee, and Kristina Toutanova. 2019a. Bert: Pre-training of deep bidirectional transformers for language understanding. In *NAACL*.
- Jacob Devlin, Ming-Wei Chang, Kenton Lee, and Kristina Toutanova. 2019b. BERT: Pre-training of deep bidirectional transformers for language understanding. In Proceedings of the 2019 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, Volume 1 (Long and Short Papers), pages 4171–4186, Minneapolis, Minnesota. Association for Computational Linguistics.
- Dheeru Dua, Yizhong Wang, Pradeep Dasigi, Gabriel Stanovsky, Sameer Singh, and Matt Gardner. 2019. DROP: A reading comprehension benchmark requiring discrete reasoning over paragraphs. In Proceedings of the 2019 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, Volume 1 (Long and Short Papers), pages 2368–2378, Minneapolis, Minnesota. Association for Computational Linguistics.
- Antonín Dvořák and Michal Holčapek. 2015. Type 1, 1 fuzzy quantifiers determined by fuzzy measures on residuated lattices. part iii. extension, conservativity and extensionality. *Fuzzy Sets Syst.*, 271(C):133–155.
- Allyson Ettinger. 2020. What BERT is not: Lessons from a new suite of psycholinguistic diagnostics for language models. *Transactions of the Association for Computational Linguistics*, 8:34–48.
- Richard Evans, David Saxton, David Amos, Pushmeet Kohli, and Edward Grefenstette. 2018. Can neural networks understand logical entailment? *arXiv preprint arXiv:1802.08535*.
- Lei Fang and Jian-Guang Lou. 2021. Part & whole extraction: Towards a deep understanding of quantitative facts for percentages in text. *ArXiv*, abs/2110.13505.
- Kai Fintel and Lisa Matthewson. 2008. Universals in semantics.
- Gottlob Frege. 1879. Begriffsschrift. eine der arithmetischen nachgebildete formelsprache des reinen denkens.

759

760

761

762

763

764

765

766

767

769

770

771

716

717

- Atticus Geiger, Ignacio Cases, Lauri Karttunen, and Christopher Potts. 2019. Posing fair generalization tasks for natural language inference. In Proceedings of the 2019 Conference on Empirical Methods in Natural Language Processing and the 9th International Joint Conference on Natural Language Processing (EMNLP-IJCNLP), pages 4485–4495, Hong Kong, China. Association for Computational Linguistics.
- Mor Geva, Ankit Gupta, and Jonathan Berant. 2020. Injecting numerical reasoning skills into language models. In Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics, pages 946–958, Online. Association for Computational Linguistics.

670

671

672

674

679

- David Gil. 1982. Quantifier scope, linguistic variation, and natural language semantics. *Linguistics and Philosophy*, 5(4):421–472.
- Paul Grice. 1989. *Studies in the Way of Words*. Harvard University Press.
- Suchin Gururangan, Swabha Swayamdipta, Omer Levy, Roy Schwartz, Samuel Bowman, and Noah A.
   Smith. 2018. Annotation artifacts in natural language inference data. In Proceedings of the 2018 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, Volume 2 (Short Papers), pages 107–112, New Orleans, Louisiana. Association for Computational Linguistics.
- Mareike Hartmann, Miryam de Lhoneux, Daniel Hershcovich, Yova Kementchedjhieva, Lukas Nielsen, Chen Qiu, and Anders Søgaard. 2021. A multilingual benchmark for probing negation-awareness with minimal pairs. In *Proceedings of the 25th Conference on Computational Natural Language Learning*, pages 244–257, Online. Association for Computational Linguistics.
- Izumi Haruta, Koji Mineshima, and Daisuke Bekki. 2020. Logical inferences with comparatives and generalized quantifiers. In *Proceedings of the* 58th Annual Meeting of the Association for Computational Linguistics: Student Research Workshop, pages 263–270, Online. Association for Computational Linguistics.
- James Higginbotham and Robert May. 1981. Questions, quantifiers and crossing.
- <sup>107</sup> Laurence R. Horn. 2010. The expression of negation.
- 708Md Mosharaf Hossain, Venelin Kovatchev, Pranoy709Dutta, Tiffany Kao, Elizabeth Wei, and Eduardo710Blanco. 2020. An analysis of natural language in-711ference benchmarks through the lens of negation. In712Proceedings of the 2020 Conference on Empirical713Methods in Natural Language Processing (EMNLP),714pages 9106–9118, Online. Association for Computa-715tional Linguistics.

- Hai Hu, Qi Chen, and Larry Moss. 2019. Natural language inference with monotonicity. In Proceedings of the 13th International Conference on Computational Semantics - Short Papers, pages 8– 15, Gothenburg, Sweden. Association for Computational Linguistics.
- Junjie Hu, Sebastian Ruder, Aditya Siddhant, Graham Neubig, Orhan Firat, and Melvin Johnson. 2020. Xtreme: A massively multilingual multitask benchmark for evaluating cross-lingual generalisation. In *International Conference on Machine Learning*, pages 4411–4421. PMLR.
- Devin Johnson, Denise Mak, Andrew Barker, and Lexi Loessberg-Zahl. 2020. Probing for multilingual numerical understanding in transformer-based language models. In *Proceedings of the Third BlackboxNLP Workshop on Analyzing and Interpreting Neural Networks for NLP*, pages 184–192, Online. Association for Computational Linguistics.
- Pratik Joshi, Somak Aditya, Aalok Sathe, and Monojit Choudhury. 2020. TaxiNLI: Taking a ride up the NLU hill. In *Proceedings of the 24th Conference on Computational Natural Language Learning*, pages 41–55, Online. Association for Computational Linguistics.
- Karthikeyan K, Aalok Sathe, Somak Aditya, and Monojit Choudhury. 2021. Analyzing the effects of reasoning types on cross-lingual transfer performance. In *Proceedings of the 1st Workshop on Multilingual Representation Learning*, pages 86–95, Punta Cana, Dominican Republic. Association for Computational Linguistics.
- Napoleon Katsos, Chris Cummins, Maria-José Ezeizabarrena, Anna Gavarró, Jelena Kuvač Kraljević, Gordana Hrzica, Kleanthes K Grohmann, Athina Skordi, Kristine Jensen De López, Lone Sundahl, et al. 2016. Cross-linguistic patterns in the acquisition of quantifiers. *Proceedings of the National Academy of Sciences*, 113:9244 – 9249.
- Napoleon Katsos, Maria-Jose Ezeizabarrena, Anna Gavarro, Jelena Kuvac Kraljevic, Gordana Hrzica, Kleanthes K Grohmann, Athina Skordi, Kristine Jensen de Lopez, Lone Sundahl, Angeliek Van Hout, et al. 2012. The acquisition of quantification across languages: some predictions.
- Edward L. Keenan and Denis Paperno. 2012. Handbook of quantifiers in natural language.
- Edward L. Keenan and Dag Westerståhl. 1997. Generalized quantifiers in linguistics and logic. In *Handbook of Logic and Language*.
- Douwe Kiela, Max Bartolo, Yixin Nie, Divyansh Kaushik, Atticus Geiger, Zhengxuan Wu, Bertie Vidgen, Grusha Prasad, Amanpreet Singh, Pratik Ringshia, Zhiyi Ma, Tristan Thrush, Sebastian Riedel, Zeerak Waseem, Pontus Stenetorp, Robin Jia, Mohit Bansal, Christopher Potts, and Adina Williams.

872

873

874

875

876

877

878

879

880

881

882

2021. Dynabench: Rethinking benchmarking in NLP. In Proceedings of the 2021 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, pages 4110–4124, Online. Association for Computational Linguistics.

774

777

778

779

790

793

795

797

798

810

811

812

813

815

816

817

818

819

822

823

- Najoung Kim, Roma Patel, Adam Poliak, Patrick Xia, Alex Wang, Tom McCoy, Ian Tenney, Alexis Ross, Tal Linzen, Benjamin Van Durme, Samuel R. Bowman, and Ellie Pavlick. 2019. Probing what different NLP tasks teach machines about function word comprehension. In Proceedings of the Eighth Joint Conference on Lexical and Computational Semantics (\*SEM 2019), pages 235–249, Minneapolis, Minnesota. Association for Computational Linguistics.
- Guillaume Lample and Alexis Conneau. 2019. Crosslingual language model pretraining. In *NeurIPS*.
- Stephen C Levinson, C Stephen, and Stephen C Levinson. 2000. *Presumptive meanings: The theory of generalized conversational implicature.* MIT press.
- Patrick Lewis, Barlas Oguz, Ruty Rinott, Sebastian Riedel, and Holger Schwenk. 2020. MLQA: Evaluating cross-lingual extractive question answering. In Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics, pages 7315– 7330, Online. Association for Computational Linguistics.
- Tao Li, Vivek Gupta, Maitrey Mehta, and Vivek Srikumar. 2019. A logic-driven framework for consistency of neural models. In *Proceedings of the* 2019 Conference on Empirical Methods in Natural Language Processing and the 9th International Joint Conference on Natural Language Processing (EMNLP-IJCNLP), pages 3924–3935, Hong Kong, China. Association for Computational Linguistics.
- Per Lindström. 1966. First order predicate logic with generalized quantifiers. *Theoria*, 32(3):186–195.
  - Yinhan Liu, Myle Ott, Naman Goyal, Jingfei Du, Mandar Joshi, Danqi Chen, Omer Levy, Mike Lewis, Luke Zettlemoyer, and Veselin Stoyanov. 2019.
    Roberta: A robustly optimized bert pretraining approach. *ArXiv*, abs/1907.11692.
- Lisa Matthewson. 2001. Quantification and the nature of crosslinguistic variation. *Natural Language Semantics*, 9(2):145–189.
- Lisa Matthewson. 2004. On the methodology of semantic fieldwork. *International journal of American linguistics*, 70(4):369–415.
- Lisa Matthewson. 2008. Quantification: A crosslinguistic perspective.
- Richard Montague. 1973. The proper treatment of quantification in ordinary english. In *Approaches to natural language*, pages 221–242. Springer.

- Andrzej Mostowski. 1957. On a generalization of quantifiers. *Fundamenta Mathematicae*, 44(1):12– 36.
- Mathijs Mul and Willem Zuidema. 2019. Siamese recurrent networks learn first-order logic reasoning and exhibit zero-shot compositional generalization.
- Aakanksha Naik, Abhilasha Ravichander, Norman Sadeh, Carolyn Rose, and Graham Neubig. 2018. Stress test evaluation for natural language inference. In Proceedings of the 27th International Conference on Computational Linguistics, pages 2340–2353, Santa Fe, New Mexico, USA. Association for Computational Linguistics.
- Yixin Nie, Haonan Chen, and Mohit Bansal. 2019. Combining fact extraction and verification with neural semantic matching networks. In Association for the Advancement of Artificial Intelligence (AAAI).
- Yixin Nie, Adina Williams, Emily Dinan, Mohit Bansal, Jason Weston, and Douwe Kiela. 2020. Adversarial NLI: A new benchmark for natural language understanding. In Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics, pages 4885–4901, Online. Association for Computational Linguistics.
- Liudmila Nikolaeva. 2012. *Quantifiers in Adyghe*, pages 21–82. Springer Netherlands, Dordrecht.
- Joakim Nivre, Marie-Catherine de Marneffe, Filip Ginter, Jan Hajič, Christopher D. Manning, Sampo Pyysalo, Sebastian Schuster, Francis Tyers, and Daniel Zeman. 2020. Universal Dependencies v2: An evergrowing multilingual treebank collection. In *Proceedings of the 12th Language Resources and Evaluation Conference*, pages 4034–4043, Marseille, France. European Language Resources Association.
- Maciej Ogrodniczuk, Vincent Ng, Yulia Grishina, and Sameer Pradhan, editors. 2020. *Proceedings of the Third Workshop on Computational Models of Reference, Anaphora and Coreference.* Association for Computational Linguistics, Barcelona, Spain (online).
- Maciej Ogrodniczuk, Sameer Pradhan, Yulia Grishina, and Vincent Ng, editors. 2019. *Proceedings of the Second Workshop on Computational Models of Reference, Anaphora and Coreference.* Association for Computational Linguistics, Minneapolis, USA.
- Alicia Parrish, William Huang, Omar Agha, Soo-Hwan Lee, Nikita Nangia, Alexia Warstadt, Karmanya Aggarwal, Emily Allaway, Tal Linzen, and Samuel R. Bowman. 2021. Does putting a linguist in the loop improve NLU data collection? In *Findings of the Association for Computational Linguistics: EMNLP* 2021, pages 4886–4901, Punta Cana, Dominican Republic. Association for Computational Linguistics.
- Barbara Hall Partee. 1970. Negation, conjunction, and quantifiers: Syntax vs. semantics. *Foundations of Language*, 6(2):153–165.

- 890

- 897
- 899
- 900 901
- 902
- 903
- 904 905 906
- 907
- 908 909
- 910 911
- 912
- 913 914
- 915 916

920

921 922

- 923 924
- 925
- 926
- 928
- 929
- 930

931

934

- Stanley Peters and Dag Westerståhl. 2006. Quantifiers in language and logic. Oxford University Press.
- Peng Qi, Yuhao Zhang, Yuhui Zhang, Jason Bolton, and Christopher D. Manning. 2020. Stanza: A python natural language processing toolkit for many human languages. In Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics: System Demonstrations, pages 101-108, Online. Association for Computational Linguistics.
- Marco Tulio Ribeiro, Carlos Guestrin, and Sameer Singh. 2019. Are red roses red? evaluating consistency of question-answering models. In Proceedings of the 57th Annual Meeting of the Association for Computational Linguistics, pages 6174-6184, Florence, Italy. Association for Computational Linguistics.
  - Marco Tulio Ribeiro, Tongshuang Wu, Carlos Guestrin, and Sameer Singh. 2020. Beyond accuracy: Behavioral testing of NLP models with CheckList. In Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics, pages 4902-4912, Online. Association for Computational Linguistics.
- James H. Schmerl and Stephen G. Simpson. 1982. On the role of ramsey quantifiers in first order arithmetic. J. Symb. Log., 47:423–435.
- Dan Sperber and Deirdre Wilson. 1986. Relevance: Communication and cognition, volume 142. Citeseer.
- Shashank Srivastava, Igor Labutov, and Tom Mitchell. 2018. Zero-shot learning of classifiers from natural language quantification. In Proceedings of the 56th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers), pages 306-316, Melbourne, Australia. Association for Computational Linguistics.
- Penka Stateva, Arthur Stepanov, Viviane Déprez, Ludivine Emma Dupuy, and Anne Colette Reboul. 2019. Cross-linguistic variation in the meaning of quantifiers: Implications for pragmatic enrichment. Frontiers in Psychology, 10:957.
- Shane Steinert-Threlkeld. 2019. Learnability and semantic universals. Semantics and Pragmatics, 12:4.
- Jakub Szymanik. 2016. Cognitive Processing of Quantifiers, pages 51-83. Springer International Publishing, Cham.
- Jakub Szymanik and Camilo Thorne. 2015. Semantic complexity of quantifiers and their distribution in corpora. In Proceedings of the 11th International Conference on Computational Semantics, pages 64-69, London, UK. Association for Computational Linguistics.

Yuval Varkel and Amir Globerson. 2020. Pre-training mention representations in coreference models. In Proceedings of the 2020 Conference on Empirical Methods in Natural Language Processing (EMNLP), pages 8534-8540, Online. Association for Computational Linguistics.

936

937

938

939

940

941

942

943

944

945

946

947

948

949

950

951

952

953

954

955

956

957

958

959

960

961

962

963

964

965

966

967

968

969

970

971

972

973

974

975

976

977

978

979

980

981

982

983

984

985

986

987

988

989

990

991

- Sara Veldhoen and Willem Zuidema. 2017. Can neural networks learn logical reasoning? CLASP Papers in Computational Linguistics, page 34.
- Dag Westerståhl. 1989. Quantifiers in formal and natural languages. In Handbook of philosophical logic, pages 1–131. Springer.
- Adina Williams, Nikita Nangia, and Samuel Bowman. 2018. A broad-coverage challenge corpus for sentence understanding through inference. In Proceedings of the 2018 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, Volume 1 (Long Papers), pages 1112-1122, New Orleans, Louisiana. Association for Computational Linguistics.
- Adina Williams, Tristan Thrush, and Douwe Kiela. 2020. Anlizing the adversarial natural language inference dataset.
- William A. Woods. 1991. Understanding subsumption and taxonomy: A framework for progress. In Principles of Semantic Networks.
- Hitomi Yanaka, Koji Mineshima, Daisuke Bekki, and Kentaro Inui. 2020. Do neural models learn systematicity of monotonicity inference in natural language? In Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics, pages 6105-6117, Online. Association for Computational Linguistics.
- Hitomi Yanaka, Koji Mineshima, Daisuke Bekki, Kentaro Inui, Satoshi Sekine, Lasha Abzianidze, and Johan Bos. 2019. Can neural networks understand In Proceedings of the monotonicity reasoning? 2019 ACL Workshop BlackboxNLP: Analyzing and Interpreting Neural Networks for NLP, pages 31–40, Florence, Italy. Association for Computational Linguistics.
- Deming Ye, Yankai Lin, Jiaju Du, Zhenghao Liu, Peng Li, Maosong Sun, and Zhiyuan Liu. 2020. Coreferential Reasoning Learning for Language Representation. In Proceedings of the 2020 Conference on Empirical Methods in Natural Language Processing (EMNLP), pages 7170-7186, Online. Association for Computational Linguistics.
- John Yen. 1991. Generalizing term subsumption languages to fuzzy logic. In IJCAI.
- Wenpeng Yin, Dragomir Radev, and Caiming Xiong. 2021. DocNLI: A large-scale dataset for documentlevel natural language inference. In Findings of the Association for Computational Linguistics: ACL-IJCNLP 2021, pages 4913–4922, Online. Association for Computational Linguistics.

Lotfi A Zadeh. 1983. A computational approach to fuzzy quantifiers in natural languages. In *Computational linguistics*, pages 149–184. Elsevier.

- 396 Xikun Zhang, Deepak Ramachandran, Ian Tenney,
  397 Yanai Elazar, and Dan Roth. 2020. Do language em398 beddings capture scales? In *Findings of the Association for Computational Linguistics: EMNLP 2020*,
  300 pages 4889–4896, Online. Association for Computational Linguistics.
  - George Kingsley Zipf. 1949. Human behavior and the principle of least effort.

Generalized Quantifiers	Regular Expressions
<b>some</b> (A)(B) = 1	
	(some several much many)\/det .*\/(nsubj obj obj) (some several much many)\/nsubj  (some several much many)\/amod \w+\/nsubj:pass
all(A)(B) = 1	
	(every all each)\/det .*\/(nsubj obj obl) all\/det:predet .*\/(nsubj obj obl)   everything everyone everybody
more than $\mathbf{k}$ the(A)(B) = 1	
	((more great)\/advmod than\/(fixed case) at\/case least\/nmod) .+\/nummod .+\/( nsubj obj obl)
less than k the(A)(B) = $1$	
	((few less)\/advmod than\/(fixed case) at\/case most\/amod) .+\/nummod .+\/(nsubj  obj obl)
the <b>k</b> (A)(B) = 1	
$\operatorname{Ho} \mathbf{K}(D) = 1$	\w+\/nummod .+\/(nsubj obj obl)
between $\mathbf{p}$ and $\mathbf{k}$ the(A)(B) = 1	
_	<pre>between \/ case \w+\/(nummod nsubj obj obl) and \/ cc \w+\/ conj  between \/ case .+\/( nummod nsubj obj obl) %\/obl</pre>
the <b>p/k</b> (A)(B) = 1	
$\lim_{D \to \infty} p(\mathbf{x}_{1}(D)) = 1$	\d+\/\d+\/(nummod nsubj obj obl) half\/nummod third\/(nsubj obj obl) fourth\/( nsubj obj obl) fifth\/(nsubj obj obl)
the <b>k</b> % (A)(B = 1)	
$\lim_{n \to \infty} \mathbf{k} \cdot \mathbf{k} \cdot (\mathbf{n}) (\mathbf{D} - \mathbf{n})$	$d + \ (nsubj   obj   obl)$
<b>most</b> (A)(B) = 1	
	most\/amod $w+\/(nsubj obj ob1) most\/nsubj:pass of\/case .+\/nmod$
few (A)(B) = 1	
	few \/ amod $\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$
each other $(A)(B) = 1$	
	each \/ det other \/( nsubj   obj   obl)

Table 9: Regular Expressions for generalized quantifiers.

# Appendices

1004

1005

1006

1008

1009

# A Regular Expressions for Generalized Quantifiers

Table 9 lists the regex we use to parse generalized quntifiers in sentences augmented with universal dependency tags. The approach does not find all the generalized quantifiers exhuastively but rather approximates the common distributions.

#### **B** Pairwise Observation

While the analysis in Section 4 is based on quantifiers in hypotheses, next we consider the interaction of 1010 quantifiers in hypotheses and quantifiers in premises. To this end, we calculate the difference between 1011 overall performance and performance for premise-hypothesis pairs of GQs. In Figure 2, we visualize the 1012 results as heatmaps (see Table 10 for exact numbers of occurences and accuracies). Surprisingly, whenever quantifiers appear in both the premise and the hypothesis, LMs largely fail to predict the entailment. 1014 Percentage quantifiers, supposed to be semantically more complex than counting quantifiers, are not de 1015 facto harder in NLI. We studied all 27 cases of percentage quantifiers in the English NLI datasets, and 1016 found that in most cases, percentage quantifiers occurrences are *identical* across premises and hypotheses, 1017 i.e., triggering little or no inference. The other two proportional quantifiers, most and few, are hard for 1018

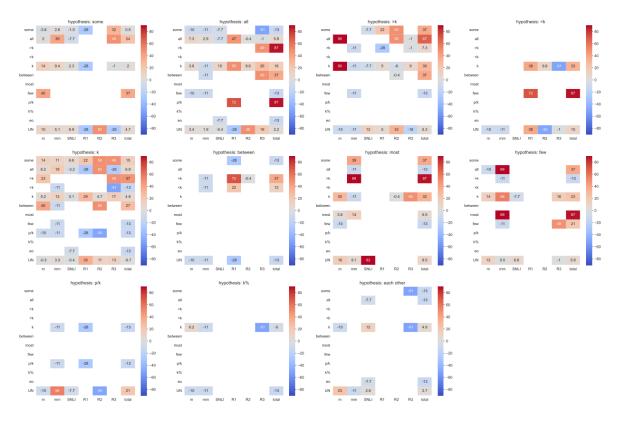


Figure 2: Fine-grained analysis of RoBERTa performance on 6 English NLI subtasks. Each heatmap represents hypotheses with a type of quantifier. The rows stand for premises with the quantifier of that label. The numbers are calculated as the accuracy over the whole dataset minus the fine-grained accuracy given a specific premise and hypothesis (the higher the number, the worse the performance). For each heatmap, the last column represents the accuracy gap weighted by all 6 tasks. "UN" stands for an entry where no explicit quantifier is identified.

LMs to resolve, e.g., in some quantifier pairs, models yield 0% accuracy. Although *each other* is supposed 1019 to be hardest to resolve due to the complex semantics of reciprocals (Szymanik and Thorne, 2015), it is 1020 not reflected in NLI tasks as such. The reason is similar to percentage quantifiers, while annotators intend 1021 to alter counting quantifiers when writing hypotheses, reciprocality is seldomly considered a linguistic 1022 ability that needs testing for NLU systems. And the annotation for Ramsey quantifier is simply a knockoff, 1023 making reciprocal relation identification unwarranted through shallow correlations. 1024

С	Fine-grained NLI Analysis	1025
D	XQA Result: mBERT and XLM-R	1026
Tabl	e 11 compares the results of mBERT and XLM-R on two XQA tasks, XQuAD and MLQA.	1027
E	GQNLI Examples	1028
Tabl	e 12 list one example per category in GQNLI.	1029
F	GQNLI Negation Cases	1030
We	present the results of seven models' performance on cases with negation cues in GQNLI in Table 13.	1031
G	GQNLI Subsumption Cases	1032
	Table 14 for models 'performance on cases requiring subsumption reasoning in GQNLI. We also k down subsumption results by entailment labels into two categories: neutral and non-neutral.	1033 1034

# 1035 H GQNLI Experiment Details

We reused the fine-tuned BERT and RobERTa in Section 4. The other fine-tuned LMs are from HuggingFace. We list the models and thier links in Table 15.

Hypothesis some	Premise some all >k	MNLI_m_dev #occurrence 45 8	%Acc 93.3 87.5	MNLI_mm_dev #occurrence 38 8	%Acc 86.8 50	SNLI_test #occurrence 16 3	%Acc 93.8 100	ANLI_R1_test #occurrence 1	%Acc 100	ANLI_R2_test #occurrence	%Acc	ANLI_R3_test #occurrence 6 3	%Acc 16.7 0	Total #occurrence 106 22	%Acc 86.8 63.6	#correctpred 92 14
	<k k between</k 	12	75	10	80	40	90	4	100	0		2	50	68	85.3	58
	most few p/k	2	50											2	50	1
	k% eachother	440	<b>5</b> 0.4			105			100			0				201
all	"unmatched" some	110 11	79.1 100	83 12	84.3 100	137 2 3	85.4 100	1	100	1	0	8 1	75 100	340 26	82.6 100	281 26
	all >k <k< td=""><td>73</td><td>82.2</td><td>74</td><td>86.5</td><td>3</td><td>100</td><td>4</td><td>25</td><td>2</td><td>50</td><td>6 1</td><td>50 0</td><td>162 1</td><td>81.5 0</td><td>132 0</td></k<>	73	82.2	74	86.5	3	100	4	25	2	50	6 1	50 0	162 1	81.5 0	132 0
	k between most	28	85.7	19 1	$\begin{array}{c} 100 \\ 100 \end{array}$	22	81.8	9	22.2	5	40	13 1	23.1 0	96 2	70.8 50	68 1
	few p/k k%	4	100	2	100			1	0					6 1	100 0	6
	eachother "unmatched"	0 151	86.1	0 144	87.5	1 41	100 92.7	0 5	100	0 2	0	0 13	30.8	1 356	100 85.1	1 303
>k	some all	1	0			1	100	2	50	1 2	0 0	2	50	4 5	50 20	2 1
	>k <k k</k 	1	0	2 3	100 100	2	100	1 3	100 66.7	9	55.6	2 10	50 40	5 28	80 57.1	4 16
	between most		0			-	100	5	00.7	2	50	10	10	2	50	1
	few p/k k%			1	100									1	100	1
	eachother "unmatched"	12	100	18	100	5	80	6	66.7	6	16.7	3	66.7	50	82	41
<k< td=""><td>some all ≻k</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></k<>	some all ≻k															
	<k k</k 							3	33.3	5	40	3	100	11	54.5	6
	between most few							1	0					1	0	0
	p/k k% eachother															
k	"unmatched" some	3	100 75	3 14	100 78.6	28	85.7	3	33.3 50	2	100 0	2 4	50 0	13 58	76.9 72.4	10 42
ĸ	all >k <k< td=""><td>12 3</td><td>83.3 66.7</td><td>14</td><td>71.4</td><td>22</td><td>95.5</td><td>ĩ</td><td>100</td><td>3</td><td>Ő</td><td>4 2 1</td><td>75 0 100</td><td>56 5 3</td><td>80.4 40 100</td><td>45 2 3</td></k<>	12 3	83.3 66.7	14	71.4	22	95.5	ĩ	100	3	Ő	4 2 1	75 0 100	56 5 3	80.4 40 100	45 2 3
	k between	140 2	84.3 50	121 2	76.9 100	593	92.2	42	42.9	49 1	44.9 0	37	32.4	982 5	82.5 60	810 3
	most few p/k k%	1	100	1 1	100 100			1	100	1	100			1 4	100 100	1 4
	k% eachother "unmatched"	118	89.8	137	86.1	7 383	100 92.7	11	36.4	13	38.5	11	36.4	7 673	100 88	7 592
between	some all							1	100					1	100	1
	k between most			1 2	100 100			1 2	0 50	2	50			4 4	50 75	2 3
	few >p/k:more/greaterthanp/k <p k:fewer="" k<br="" lessthanp="">p/k k%</p>															
	eachother "unmatched"	2	100	1	100			1	100					4	100	4
most	some all ≻k			2 2 1	50 100 0									2 2 1	50 100 0	1 2 0
	<k k</k 	5	60	1	100					2	50	1	0	9	55.6	5
	between most few	7 1	85.7 100	4	75									11 1	81.8 100	9 1
	p/k k% eachother															
few	"unmatched" some	23	73.9	30	83.3	1	0							54	77.8	42
	all >k <k< td=""><td>1</td><td>100</td><td>1 1</td><td>0 100</td><td></td><td></td><td></td><td></td><td></td><td></td><td>0 0 0</td><td></td><td>2 1 0</td><td>50 100</td><td>1 1 0</td></k<>	1	100	1 1	0 100							0 0 0		2 1 0	50 100	1 1 0
	k between	4	75	3	33.3	4	100					3	33.3	14	64.3	9
	most few p/k k%	0 0		1 2	0 100	0 0						1	0	1 3	0 66.7	0 2
	k% eachother "unmatched"	9	77.8	9	88.9	7	85.7					2	50	27	81.5	22
p/k	some															
	>k <k k between</k 			2	100	0		1	100	0		0		3	100	3
	most			-	100	U			100	U		0		5	100	2
	few p/k k%			2	100			1	100					3	100	3
	eachother "unmatched"	1	100	3	33.3	1	100	0		1	100	0		6	66.7	4
k%	some all ≻k															
	<k k</k 	6	83.3	6	100							1	100	13	92.3	12
	between most few															
	p/k k% eachother															
eachother	"unmatched" some	4	100	1	100							1	100	5	100 100	5
	all >k					3	100							3	100	3
	<k k between</k 	1	100			15	80					1	100	17	82.4	14
	most few p/k k%															
	k% eachother "unmatched"	3	66.7	3	100	1 19	100 89.5							1 26	100 84.6	1 22
				-		-										

Table 10: Statistics of pairwise analysis in Monolingual NLI Benchmarks

								ERT														M-R						
Quant.		n		h		es		ar		vi		le		hted		en		zh		es		ar		vi		le		ghted
	EM	F1																										
													XQ	uAD														
some	75	84.2	50	55.5	58.3	76.1	50	50	16.6	42.4	33.3	43.8	47.2		66.7	76.1		51.3	50	71.5	66.7	73.6	66.7	76.9	66.7	80.6	59.7	71.
all	28.5	62.2	14.2	35.2	28.5	82	42.8	52.3	14.2	29.4	28.5	56	26.1	52.9	57.1	91.8	14.2	21.4	57.1	78.6	42.8	54.9	85.7	85.7	57.1	79.3	52.3	68.0
> k																												
< k																												
k	78.1	90.1	68.7	80.4	56.2	72.1	40.6	64.3	12.5	35.7	56.2	77.1	52.1	70	75	87.4	53.1	58.8	46.8	77.4	65.6	86.3	62.5	85.4	62.5	86.9	60.9	80.
between	100	100	33.3	72.2	66.6	93.3	100	100	0	19	0	56.5	50	73.5	100	100	66.7	66.7	33.3	60	100	100	100	100	33.3	55.5	72.2	80.
p/k																												
k%									-															-				
most	40	53.3	40	40	0	10	0	26.6	0	0	20	49.3	16.7	29.9	40	48	20	33.3	40	50	0	26.6	0	0	20	49.3	20	34.5
few																												
each other																												
all GQs	70	83.2	55	66.7	50	70.3	41.6	58.2	11.6	32.5	43.3	65	45.3	62.7	70	83.6	43.3	50.2	48.3	73.6	60	76	68.3	83.6	58.3	80.3	58	74.0
comp.	71.8	83.7	48	59.1	56	74.5	40.8	57.9	13.9	32.4	50.7	67.2	46.9	62.5	74.5	86	43	52.8	61	80	53.3	71.7	58.1	78	61.1	77.1	58.5	74.3
													M	LQA														
some	59	80	28.2	52.1	34.1	59.2	36.3	54.9	5.4	24	33.3	58.4	32.7	54.8	69.6	86.1	33.3	60.6	41.4	70	43.1	62.9	43.2	78	45.4	61.1	46	69.8
all	67.7	79.8	14.2	46.4	38.4	62.8	33.3	57.9	10.5	30.1	31.2	51.6	32.6	54.8	77.4	90.6	35.7	70	42.3	66.4	38	60	57.8	79.8	37.5	51	48.1	69.0
> k																												
< k	0	0							0	13.3			0	6.7	0	40							0	20			0	30
k	74.9	79.4	47	63.4	41.5	65.9	27.6	50.3	6.3	23.7	38.2	53	39.3	56	69.2	82.1	45.2	66.2	48.7	73.3	43	64.9	48.5	71.9	46.3	62.1	50.2	70.
between	50	88.5	50	83.3	0	26.6	0	68.7	0	26.6			20	58.7	50	88.5	50	50	50	65.3	0	54.6	0	77.4			30	67.2
p/k	100	100	0	0	0	0							33.3	33.3	100	100	100	100	100	100							100	100
k%	100	100	0	26.6			0	23.7					33.3	50.1	100	100	0	26.6			0	71.4					33.3	
most	55.5	7	47.3	62.1	45.4	61.7	30	46.8	5.8	15.7	33.3	40.7	36.2	50.3	59.2	76	47.3	69.5	45.4	59.5	40	63.2	47	75.7	22.2	31.7	43.5	62.0
few																												
each other																												
all GQs	63.5	79.2	41.8	60.3	39.6	63.7	29.3	51.3	6.4	23.6	36.1	53.2	36.1	55.2	69	83	43	65.6	46.9	71.5	41.9	64.1	47.6	73.2	44.4	59.8	48.8	69.
comp.	67.2	80.6	37.5	57.9	47.3	66	30	48.4	11.2	28	40.8	56	39	56.2	70.4	83.3	38.7	62.5	54.1	72.2	42.5	62.9	50.5	72.3	52.2	67.3	51.4	70.

Table 11: Results of mBERT and XLM-R performance on XQA tasks decomposed by quantifier categories.

Quantifier	Premise	Hypothesis	Label
some	"There are six dogs. Three brown dogs, a black dog and	"Some dogs sit."	Neutral
all	a white dog run along the green grass." "In 2021, there are 490 million people in Africa living in extreme poverty, or 36% of the total population."	"Not all people in Africa live in extreme poverty."	Entailment
> k	"Two young men in blue stand over a stove and look at the camera while another young man in red stands behind them."	"At least two men wear red."	Contradiction
< k	"More than five guys chased two girls in the classroom."	"No less than four guys chased two girls in the classroom."	Entailment
k	"There are twelve singers on a stage, less than half from Argentina and one from Cape Verde."	"Two singers come from Ar- gentina."	Neutral
between	"Only half out of six cleaners are sweeping up animal faces from the street during a parade."	"Between four and five clean- ers are sweeping up animal fae- ces."	Contradiction
p/k	"More than 50% but less than 65% of Americans worry about global warming."	"Two thirds of Americans worry about global warming."	Contradiction
k%	"More than five guys chased two girls in the classroom."	"100% of the guys chased two girls in the classroom."	Neutral
most	"Two young men in blue stand over a stove and look at the camera while another young man in red stands behind them"	"Most men wear blue."	Entailment
few	"More than 50% but less than 65% of Americans worry about global warming."	"A few people from Amer- ica do not worry about global warming."	Entailment
each other	"There are 100 villagers and 100 townsmen. Most vil- lagers and most townsmen hate each other."	"All villagers and all towns- men hate each other."	Neutral

Table 12: GQNLI examples.

Quantifier # Occurrence with negation cues		some 9	all 6	> k 6	$\stackrel{< k}{9}$	k 18	between 3	p/k 6	$^{k\%}_{6}$	most 6	few 9	each other 3	Overall 81
Model	Training Data	% Performance											
ELECTRA	S,M,F,ANLI	33.3	16.7	0	66.7	50	100	0	100.0	16.7	11.1	33.3	27.5
BERT	S,M,F,ANLI	0	66.7	100	33.3	50	0	50	0	50	22.2	33.3	39.2
SBERT	S,M,F,ANLI	0	0	0	44.4	22.2	0	0	50	16.7	11.1	0	11.8
RoBERTa	MNLI S,M,F,ANLI	33.3 33.3	16.7 0	0 0	33.3 66.7	27.8 33.3	66.7 0	33.3 0	33.3 50	50 0	33.3 0	33.3 0	31.4 17.6
BART	MNLI S,M,F,ANLI	33.3 0.0	50.0 66.7	50.0 100.0	33.3 33.3	33.3 50.0	0 0.0	50 50.0	0 0.0	0 50.0	66.7 22.2	100 33.3	35.3 39.2
ALBERT	S,M,F,ANLI	44.4	0	33.3	44.4	33.3	0	50	50	0	0	0	25.5
DeBERTa-v3	MNLI M,F,ANLI M,F,Ling,DocNLI	33.3 0 33.3	0 0 0	33.3 0 0	33.3 66.7 0	27.8 33.3 11.1	0 0 66.7	16.7 0 50	0 50 33.3	0 50 50	33.3 33.3 33.3	0 0 0	23.5 23.5 27.5

Table 13: Models' performance on instances with negation cues in GQNLI.

Type # Occurrence		Subsumption (neutral) 90	Subsumption (non-neutral) 99	Subsumption (total) 189	Non-subsumption				
Model	Training Data	% Performance							
ELECTRA	S,M,F,ANLI	3.3	37.4	21.2	36				
BERT	S,M,F,ANLI	22.2	24.2	23.3	41.4				
SBERT	S,M,F,ANLI	13.3	48.5	31.7	38.7				
RoBERTa	MNLI S,M,F,ANLI	27.8 21.1	18.2 49.5	22.8 36.0	37.8 38.7				
BART	MNLI S,M,F,ANLI	36.7 44.4	15.2 44.4	25.4 44.4	41.4 36.9				
ALBERT	S,M,F,ANLI	33.3	49.5	41.8	42.3				
DeBERTa-v3	MNLI M,F,ANLI M,F,Ling,DocNLI	45.6 52.2 86.7	34.3 41.4 32.3	39.7 46.6 58.2	42.3 32.4 16.2				

Table 14: Models' performance on instances requiring subsumption reasoning.

Model	Training Data	Model's link					
ELECTRA S,M,F,ANLI		https://huggingface.co/ynie/electra-large-discriminator-snli_mnli_fever_anli_R1_R2_R3-nli					
BERT	S,M,F,ANLI						
SBERT	S,M,F,ANLI	https://huggingface.co/usc-isi/sbert-roberta-large-anli-mnli-snli					
RoBERTa	MNLI S,M,F,ANLI	https://huggingface.co/roberta-large-mnli					
BART	MNLI S,M,F,ANLI	https://huggingface.co/facebook/bart-large-mnli https://huggingface.co/ynie/bart-large-snli_mnli_fever_anli_R1_R2_R3-nli					
ALBERT	S,M,F,ANLI	ynie/albert-xxlarge-v2-snli_mnli_fever_anli_R1_R2_R3-nli					
DeBERTa-v3	MNLI M,F,ANLI M,F,Ling,DocNLI	https://huggingface.co/MoritzLaurer/DeBERTa-v3-base-mnli https://huggingface.co/MoritzLaurer/DeBERTa-v3-base-mnli-fever-anli https://huggingface.co/MoritzLaurer/DeBERTa-v3-base-mnli-fever-docnli-ling-2c					

Table 15: Links to the models we use to test on GQNLI.