# BAYESIAN TEST-TIME ADAPTATION VIA DIRICHLET FEATURE PROJECTION AND GMM-DRIVEN INFERENCE FOR MOTOR IMAGERY EEG DECODING

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#### **ABSTRACT**

Generalization in EEG-based motor imagery (MI) brain-computer interfaces (BCIs) is severely hampered by cross-subject and cross-session variability. Although large-scale EEG pretraining has advanced representation learning, their practical deployment is hindered by the need for costly fine-tuning to overcome significant domain shifts. Test-time adaptation (TTA) methods that adapt models during inference offer a promising solution. However, existing EEG-TTA methods either rely on gradient-based fine-tuning (suffering from high computational cost and catastrophic forgetting) or data alignment strategies (failing to capture shifts in deep feature distributions). To address these limitations, we propose BTTA-DG, a novel Bayesian Test-Time Adaptation framework that performs efficient, gradient-free adaptation by directly modeling the distribution of deep features. Our approach first employs a lightweight SincAdaptNet with learnable filters to extract task-specific frequency bands. We then introduce a novel Dirichlet feature projection that maps high-dimensional sequential embeddings onto a compact and interpretable parameter space, effectively capturing the concentration of time-varying predictive evidence. Adaptation is achieved via a GMMdriven Bayesian inference mechanism, which models the historical distribution of these Dirichlet parameters and fuses this evidence with the model's prior predictions to calibrate outputs for the target domain. Extensive experiments show that BTTA-DG significantly outperforms previous EEG-TTA methods, achieving state-of-the-art accuracy while running at real-time speed. Furthermore, visualizations confirm the physiological interpretability of our learned filters and the robust class separability of our Dirichlet feature space. Code is available at https://anonymous.4open.science/r/BTTA-DG-main-25A1.

# 1 Introduction

Electroencephalography (EEG)—based brain—computer interfaces (BCIs) decode cortical activity to control external devices (Clerc, 2013). Among them, motor-imagery (MI) BCIs leverage sensorimotor rhythms (SMRs) (Neuper et al., 2006) and have shown promise in stroke rehabilitation (López-Larraz et al., 2018) and assistive control (Fernández-Rodríguez et al., 2016; Noda et al., 2012). Recent advances in large-scale EEG pretrained models (Wang et al., 2024; Jiang et al., 2024; Kim et al., 2024), trained on massive datasets, have demonstrated unprecedented capabilities in learning general and reliable representations. However, deploying such models in real-world scenarios remains challenging due to significant data shifts in EEG recordings (Huang et al., 2023). These shifts stem primarily from the non-stationarity of EEG signals, driven by cross-subject or cross-session neurophysiological differences (Apicella et al., 2024). Consequently, bridging these distributional gaps requires robust adaptive strategies beyond pretraining alone (Xu et al., 2020; Wimpff et al., 2025; Liu et al., 2025).

Test-time adaptation (TTA), which adapts models during inference using online unlabeled data (Li et al., 2023), presents a promising solution for practical BCI deployment. However, existing EEG-TTA methods fall into two paradigms with critical trade-offs. Gradient-based approaches update model parameters through techniques such as entropy minimization (Wang et al., 2020), pseudolabel optimization (Lee et al., 2013; Wang et al., 2022), and consistency regularization. While effective, these methods suffer from high computational overhead due to gradient backpropagation

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and risk catastrophic forgetting when continuously updating pre-trained representations. For instance, OTTA (Wimpff et al., 2024) integrates data alignment with entropy-based batch normalization finetuning, while T-TIME (Li et al., 2023) employs ensemble learning with conditional entropy minimization, both requiring substantial computational resources. Conversely, non-gradient approaches avoid parameter updates by recalibrating domain-specific statistics, such as batch normalization layer recalculation (Schneider et al., 2020) or data alignment (Wimpff et al., 2024; Bakas et al., 2025). While computationally efficient, these methods rely on shallow alignment techniques that inadequately capture the complex, high-dimensional domain shifts inherent in EEG representations across subjects and sessions. This creates a fundamental challenge: to develop a TTA framework that is both computationally efficient and capable of modeling deep distributional changes, all while being theoretically grounded and avoiding destructive model updates.

To address these challenges, we propose BTTA-DG, a Bayesian Test-Time Adaptation framework that achieves high-performance, gradient-free adaptation via Dirichlet feature projection and GMM-driven inference. Our approach introduces the Dirichlet distribution to EEG-TTA, treating it as a "distribution over categorical distributions" to model prediction uncertainty (Wong, 1998)." Our method first employs a Sinc-based adaptive network (SincAdaptNet) to extract powerful, task-specific features. We then introduce a novel Dirichlet feature projection, which maps high-dimensional sequential embeddings onto a compact, interpretable parameter space. Unlike conventional EEG-TTA methods that rely on heuristic data (Zanini et al., 2017; He & Wu, 2019) or shallow statistics alignment (Schneider et al., 2020), this probabilistic representation effectively models the concentration of the model's timevarying predictive distribution, allowing us to capture deep feature shifts in the new domain, which is a significant advance. To ensure stable and efficient adaptation, we design a Gaussian Mixture Model (GMM)-driven Bayesian inference mechanism. A GMM models the historical distribution of Dirichlet parameters from the target domain, and Bayesian inference fuses this likelihood with the deep model's prior predictions. This entire process is gradient-free, calibrating the model's outputs without destructive updates to its pre-trained weights, thereby preventing catastrophic forgetting. Our contributions include:

- We construct a Sinc-based adaptive network (SincAdaptNet) that leverages learnable Sincfilters to extract task-specific frequency bands. It enhances the representation of temporal embeddings by isolating the most informative spectral components.
- We are the first to introduce the Dirichlet distribution to EEG-TTA, creating a low-dimensional projection that provides a robust and interpretable representation of deep distributional shifts, overcoming the limitations of prior heuristic and shallow alignment methods.
- We propose a novel GMM-driven Bayesian inference mechanism that enables gradient-free adaptation. By modeling the historical Dirichlet parameter distribution, the GMM retains global-neighborhood knowledge of the test data. Bayesian inference then combines the GMM likelihood with prior predictions to yield calibrated posterior predictions.

Across four public MI datasets, BTTA-DG achieves state-of-the-art cross-subject accuracy with real-time speed. Visualization analyses confirm the physiological interpretability of our learned spatial and spectral filters, which isolate MI-specific scalp topographies (frontal, central, parietal, and occipital regions) and frequency bands (mu, beta, gamma). Furthermore, we show that our Dirichlet feature space yields robust class separability, evidenced by low intra-class covariance (<0.27) and high inter-class KL divergence (>31.85). These results validate BTTA-DG as a lightweight, robust, and theoretically grounded framework for practical test-time adaptation in BCIs.

## 2 METHODOLOGY

**Notations** In MI-TTA research, a cross-subject setting is commonly considered, where leave-one-subject-out (LOSO) cross-validation is widely adopted (Altaheri et al., 2023). Each subject in turn serves as the unlabeled target, with all other subjects' data forming the source. Let  $\{D^l_{\rm src}\}_{l=1}^L$  denote the source domain containing labeled EEG trials from L subjects, where  $D^l_{\rm src} = \{(s^i_l, y^i_l)\}_{l=1}^K$  consists of  $N^l$  trials for subject l. Each trial  $s^i_l \in \mathbb{R}^{C \times T}$  is a C-channel EEG signal of length T, with class label  $y^i_l \in \mathcal{L}$ . The target domain  $D_{\rm tgt} = \{s^i\}_{i=1}^{N_{\rm tgt}}$  contains  $N_{\rm tgt}$  unlabeled test trials arriving sequentially from one single subject. A deep classification model  $f_{\theta} = f_{\rm cls} \circ g_{\rm enc}$ , with parameters

 $m{ heta}$ , is pre-trained on  $\{D_{
m src}^l\}_{l=1}^L$ . Here, the encoder  $g_{
m enc}:\mathbb{R}^{C imes T} o \mathbb{R}^{|\mathcal{L}| imes T}$  maps the EEG trials to embeddings of dimension  $|\mathcal{L}| imes T$ , and the classifier  $f_{
m cls}:\mathbb{R}^{|\mathcal{L}| imes T} o \mathbb{R}^{|\mathcal{L}|}$  produces predictions for  $|\mathcal{L}|$  classes. The goal is to adapt  $f_{m{ heta}}$  to  $D_{
m tgt}$  via online MI-TTA framework without requiring target labels or source data. In addition, within-subject adaptation across sessions is also discussed in Appendix G.

#### 2.1 SINC-BASED ADAPTIVE BANDPASS FILTERING NETWORK

We propose a lightweight Sinc-based Adaptive Bandpass Filtering Network (SincAdaptNet) to serve as the deep classification model  $f_{\theta}$  within the MI-TTA framework. The network comprises: Spat-Conv  $\rightarrow$  Sinc-Conv  $\rightarrow$  IncCh-Conv  $\rightarrow$  Cls-Conv, with layer normalization inserted after temporal filtering and channel expansion to avoid batch-statistics dependence when the online batch size is one (Ba et al., 2016).

**Spat-Conv** performs spatial filtering with  $F_{\rm spat}$  kernels of size  $(C \times 1)$ , reducing channel redundancy while retaining task-relevant spatial patterns, akin to data-driven CSP (Blankertz et al., 2007). **Sinc-Conv** is an interpretable, parametrized temporal convolution inspired by SincNet (Ravanelli & Bengio, 2018; Zhang et al., 2024): rather than learning free-form kernels, it learns low cutoff  $f_{\rm low}$  and bandwidth  $f_{\rm band}$  (thus  $f_{\rm high} = f_{\rm low} + f_{\rm band}$ ), from which a windowed-sinc band-pass kernel is generated. This yields MI-relevant mu (8–13 Hz), beta (13–30 Hz) McFarland et al. (2000); Pfurtscheller et al. (2006), and gamma (> 30 Hz) Darvas et al. (2010) rhythms with few parameters and clear spectral interpretability. The Sinc-Conv layer comprises  $F_{\rm sinc}$  adaptive bandpass filters of size  $(1 \times N_{\rm sinc})$  and uses "SAME" padding to preserve temporal dimension. **IncCh-Conv** expands channels to  $2F_{\rm sinc}$  to enrich representation, and **Cls-Conv** maps features to  $|\mathcal{L}| \times T$  embeddings, where  $|\mathcal{L}|$  denotes the number of motor imagery classes and T denotes the temporal length.

Critically, inspired by the SwAV framework (Caron et al., 2020), normalized probability spaces enable more stable and interpretable representation learning under domain shift. For each EEG trial, its sequential embeddings are mapped through a softmax function to follow time-varying categorical distributions, denoted by  $\boldsymbol{X} = g_{\text{enc}}\left(\boldsymbol{s}\right) = \left[\boldsymbol{x}_1, \boldsymbol{x}_2, \ldots, \boldsymbol{x}_T\right] \in \mathbb{R}^{|\mathcal{L}| \times T}$ . Each  $\boldsymbol{x}_j \in \mathbb{R}^{|\mathcal{L}|}$  encodes an instantaneous class probability vector at timestep j, collectively forming a trajectory of time-varying uncertain predictions. The model's prior prediction is obtained through temporal averaging:  $f_{\text{cls}}(\boldsymbol{X}) = \frac{1}{T} \sum_{j=1}^{T} \boldsymbol{x}_j \in \mathbb{R}^{|\mathcal{L}|}$ . This averaging process integrates the dynamic prediction information over time, providing a robust and informative prior for subsequent Bayesian inference. Complete architectural details of SincAdaptNet are provided in Appendix B.

# 2.2 BAYESIAN TEST-TIME ADAPTATION VIA DIRICHLET FEATURE PROJECTION AND GMM-DRIVEN INFERENCE

To address challenges in current MI-TTA methods—catastrophic forgetting from gradient-based updates and insufficient modeling of deep feature shifts—we propose a probabilistic test-time adaptation framework that integrates Dirichlet feature projection with GMM-driven Bayesian inference. This approach dynamically calibrates the deep model's prior predictions  $f_{\theta}(s)$  through Bayesian inference, enabling efficient, gradient-free and theoretically grounded online test-time adaptation.

Overall, the Dirichlet feature projection method first projects the post-softmax sequential embeddings  $\boldsymbol{X}$  to the low-dimensional Dirichlet parameters. It preserves the prior concentration towards each class for sequential embeddings that follow a time-varying categorical distribution. Second, in GMM-driven Bayesian inference, the Dirichlet parameters estimated from historical EEG trials are clustered by a GMM, which efficiently encodes both global information of the historical test trials and the neighborhood information of the current calibrating trial. Bayesian inference is then used to combine the GMM likelihood with the prior prediction of deep model to obtain the calibrated posterior.

## 1) DIRICHLET FEATURE PROJECTION FOR DEEP-FEATURE MODELING

The core of our method is the Dirichlet feature projection. The Dirichlet distribution, as a "distribution over distributions (Wong, 1998)", is a probability distribution over the parameter space of categorical distribution. It can encode sequential embeddings of categorical distributions for an EEG trial rather than a fixed categorical distribution. Let the sequential embeddings output from SincAdaptNet's en-

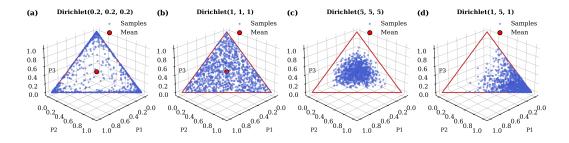


Figure 1: Dirichlet distributions for varying parameter settings. Each subplot displays 1000 samples (blue points) and the mean (red points) within the probability simplex (red lines). (a)-(c) illustrate that increasing the total scale  $\alpha_0$  yields lower uncertainty (lower variance). (b) and (d) illustrate that elevating a component  $\alpha_i$  shifts the prior concentration toward its corresponding class.

coder be  $X = [x_1, x_2, \dots, x_T] \in \mathbb{R}^{|\mathcal{L}| \times T}$ , where each  $x_j = (x_{1j}, x_{2j}, \dots, x_{|\mathcal{L}|j})^{\top} \in \Delta^{|\mathcal{L}|-1}$  represents instantaneous categorical probability vector at timestep j. The probability simplex  $\Delta^{|\mathcal{L}|-1}$  is defined as

$$\Delta^{|\mathcal{L}|-1} = \left\{ \boldsymbol{x}_j \in \mathbb{R}^{|\mathcal{L}|} : \sum_{i=1}^{|\mathcal{L}|} x_{ij} = 1, \ x_{ij} \ge 0 \right\}. \tag{1}$$

The Dirichlet distribution offers interpretable parameter  $\alpha$ , where each component  $\alpha_i$  reflects the concentrated prior probability towards class i of sequential embeddings, and the scale  $\alpha_0 = \sum_{i=1}^{|\mathcal{L}|} \alpha_i$  indicates the overall uncertainty across T time steps (Ng et al., 2011) (see Figure 1).

Assume that the sequential embeddings X follow a Dirichlet distribution, denoted as  $X \sim \mathrm{Dir}(\alpha)$ , with parameter vector  $\alpha = (\alpha_1, \dots, \alpha_{|\mathcal{L}|}) \in \mathbb{R}_+^{|\mathcal{L}|}$ . Each categorical probability vector  $x_j$  is an i.i.d. sample from  $\mathrm{Dir}(\alpha)$ . The support of  $\mathrm{Dir}(\alpha)$  is also confined to  $\Delta^{|\mathcal{L}|-1}$ .

We define a projection map  $\mathcal{P}$  that transforms the high-dimensional sequential embeddings  $X \in \mathbb{R}^{|\mathcal{L}| \times T}$  into its low-dimensional Dirichlet parameters  $\alpha \in \mathbb{R}_+^{|\mathcal{L}|}$  via maximum likelihood estimation (MLE),

$$\mathcal{P}: \mathbb{R}^{|\mathcal{L}| \times T} \to \mathbb{R}_{+}^{|\mathcal{L}|}, \quad \boldsymbol{X} \mapsto \hat{\boldsymbol{\alpha}}_{\text{MLE}} = \arg\max_{\boldsymbol{\alpha}} \sum_{j=1}^{T} \log \mathcal{D}(\boldsymbol{x}_{j}; \boldsymbol{\alpha}), \tag{2}$$

where the Dirichlet probability density function is given by

$$\mathcal{D}(\boldsymbol{x}_j; \boldsymbol{\alpha}) = \frac{\Gamma(\alpha_0)}{\prod_{i=1}^{|\mathcal{L}|} \Gamma(\alpha_i)} \prod_{i=1}^{|\mathcal{L}|} x_{ij}^{\alpha_i - 1}.$$
 (3)

Here,  $\Gamma(\cdot)$  is the Gamma function.

This projection effectively compresses the temporal dynamics of the deep features into a single, semantically rich vector that parameterizes the model's predictive distribution for that trial. The Dirichlet parameter estimate,  $\hat{\alpha}_{MLE}$ , could be efficiently computed using a established fixed-point iteration algorithm (Minka, 2012), detailed in

$$\alpha_i^{\text{new}} = \psi^{-1} \left( \psi(\alpha_0^{\text{old}}) + \frac{1}{T} \sum_{j=1}^T \log x_{ij} \right) , \qquad (4)$$

where  $\psi\left(u\right)=\frac{d}{du}\Gamma\left(u\right)$  denotes the Digamma function. Full algorithmic details for computing the post-projection Dirichlet parameters are provided in Appendix C.

#### 2) GMM-driven Bayesian Inference for Gradient-Free Calibration

For historical test EEG trials s, we compute their Dirichlet parameters via the projection  $\hat{\alpha}_{\text{MLE}} = \mathcal{P}(g_{\text{enc}}(s))$  and store parameters of high-confidence trials in a memory bank  $M_y$  organized by their

(calibrated) predicted label. A Gaussian Mixture Model (GMM) (Reynolds et al., 2009) is then employed to cluster the historical Dirichlet parameters in  $M_y$  for each class to build a non-parametric density estimate of the historical Dirichlet parameters accumulated from the target domain, yielding a class-specific GMM likelihood:

$$p_{\text{GMM}}(\boldsymbol{\alpha} \mid y) = \sum_{k=1}^{K} \pi_{y,k} \mathcal{N}(\boldsymbol{\alpha}; \boldsymbol{\mu}_{y,k}, \boldsymbol{\Sigma}_{y,k}), \tag{5}$$

where K is the number of mixture components for class y,  $\pi_{y,k}$  are the weights satisfying  $\sum_{k=1}^K \pi_{y,k} = 1$  and  $\pi_{y,k} > 0$ , and  $\mu_{y,k}$  and  $\Sigma_{y,k}$  are the mean and covariance of the  $k^{\text{th}}$  Gaussian component, respectively.

The GMM encodes the global distribution of the historical test EEG trials and each component model preserves the neighborhood information of the current test trial to be calibrated. Any proximity of the current test trial to a particular cluster results in a relatively large GMM likelihood.

For a current test EEG trial  $s^i$  with parameter  $\hat{\alpha}_{\text{MLE}}$ , the calibrated posterior is computed by combining the GMM likelihood  $p_{\text{GMM}}(\hat{\alpha}_{\text{MLE}} \mid y)$  with the deep model's prior prediction  $p_{\theta}(y) = f_{\theta}(s^i)$  via Bayesian inference:

$$p_{\text{cal}}(y \mid \hat{\boldsymbol{\alpha}}_{\text{MLE}}) = \frac{p_{\text{GMM}}(\hat{\boldsymbol{\alpha}}_{\text{MLE}} \mid y) p_{\boldsymbol{\theta}}(y)}{\sum_{y'=1}^{|\mathcal{L}|} p_{\text{GMM}}(\hat{\boldsymbol{\alpha}}_{\text{MLE}} \mid y') p_{\boldsymbol{\theta}}(y')}.$$
 (6)

The final calibrated prediction is then obtained via  $\hat{y}_{cal} = \arg\max_{y \in \mathcal{L}} p_{cal}(y \mid \hat{\alpha}_{MLE})$ . Subsequently, the Dirichlet parameter  $\hat{\alpha}_{MLE}$  of the current test EEG trial is updated into the memory bank according to its confidence (as discussed in Sensitivity analysis) and predicted label. Algorithm 1 summarizes the pseudo-code of the proposed BTTA-DG framework (see Appendix D).

$$M_{\hat{y}_{\text{cal}}} \leftarrow M_{\hat{y}_{\text{cal}}} \cup \{\hat{\boldsymbol{\alpha}}_{\text{MLE}}\}.$$
 (7)

## 3) THEORETICAL ANALYSIS FOR ENHANCED TEST-TIME ADAPTABILITY

The central innovation of our work is the shift from adapting on point estimates (i.e., pseudo-labels) to adapting on probabilistic distributional representations. Conventional TTA methods are highly sensitive to the noise and uncertainty inherent in single predictions from a domain-shifted model. Furthermore, shallow alignment techniques fail to capture how the complex, high-dimensional space of deep features deforms in a new domain. Our key insight is that the domain shift is more reliably expressed in the distribution of the model's sequential predictions rather than in any single prediction.

Instead of directly using the model's output point estimates, we introduce Dirichlet feature projection to model the entire distribution of the sequential categorical embeddings for each trial. This yields a low-dimensional Dirichlet parameter vector  $\boldsymbol{\alpha}$ . The vector  $\boldsymbol{\alpha}$  provides a richer representation of a trial's predictive characteristics than a simple class prediction. Each component  $\alpha_i$  reflects the "concentration" or evidence for class i, while the total scale  $\alpha_0$  relates to the predictive uncertainty or variance throughout the trial. When encountering a new domain, inherent signal differences cause shifts in these predictive distributions. Our Dirichlet projection explicitly captures this distributional shift in a compact parametric form. This is a more robust and informative feature for adaptation, as it encodes not just what the model predicts, but also how confident and consistent that prediction is across time, which is crucial for characterizing a new domain.

This principled representation is what enables superior test-time adaptability. By capturing the essence of the domain shift in a low-dimensional parameter space, we can perform effective calibration using well-established density estimation (GMM) and inference (Bayesian) techniques. This completely bypasses the need for gradient-based optimization, thus circumventing catastrophic forgetting and computational inefficiency. The theoretical soundness is empirically validated through visualization analysis (Figure 3), demonstrating well-separated class clusters with high inter-class KL divergence (>31.85) and low intra-class covariance (<0.27), confirming successful mapping of domain-shifted signals into a discriminative latent space.

Filter 1: 3.1-7.9 Hz

Filter 5: 6.9-11.0 Hz

Filter 9: 20.8-25.0 Hz

Filter 13: 22.6-26.7 Hz Filter 17: 29.7-33.9 Hz

Filter 21: 43 7-58 0 Hz Filter 24: 53.8-68.5 Hz

Cumulative Response

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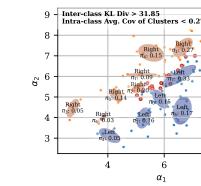
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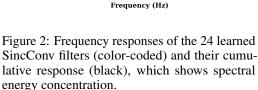
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Figure 3: Scatter of Dirichlet parameter estimated for test EEG trials, color-coded by class with misclassified trials outlined in red. GMM ellipses reveal weight and covariance of clusters.

 $\alpha_1$ 

Left hand

Error

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Right hand

# EXPERIMENTAL RESULTS

#### **IMPLEMENTATION**

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**Datasets** The BTTA-DG framework was evaluated on three MOABB (Jayaram & Barachant, 2018) motor-imagery datasets BNCI2014001, BNCI2014002, and BNCI2015001, and additionally SHU MI dataset (Ma et al., 2022). Key characteristics are summarized in Table 1. A cross-subject leaveone-subject-out (LOSO) protocol was adopted, using only the first session from each dataset. The source model was pretrained on the training set, and during test-time adaptation, test trials arrived sequentially one-by-one in the online adaptation setting. Preprocessing included only a 1-48 Hz bandpass filter and Euclidean Alignment (He & Wu, 2019).

Table 1: Summary of the four MI EEG datasets

Dataset	Number of subjects	Number of channels	Sampling rate (Hz)	Trial length (s)	Number of sessions	Trials in 1st session	Types of imaginations
BNCI2014001	9	22	250	4	2	144	left hand, right hand
BNCI2014002	14	15	512	5	1	100	right hand, both feet
BNCI2015001	12	13	512	5	3	200	right hand, both feet
SHU MI Dataset	25	32	512	4	5	100	left hand, right hand

Baselines To comprehensively assess the performance of BTTA-DG, we compared it against traditional classification methods, Transformer-based method, optimal transport-based method and state-of-the-art TTA methods, including CSP (Blankertz et al., 2007), EEGNet (Lawhern et al., 2018), EEG Conformer (Song et al., 2022), BN-adapt (Schneider et al., 2020), Tent (Wang et al., 2020), PL (Lee et al., 2013), SAR (Niu et al., 2023), CoTTA (Wang et al., 2022), T-TIME (Li et al., 2023), OTTA (Wimpff et al., 2024), and DOT-MDA (Ju & Guan, 2025). All experiments were run independently 10 times, and the average results are reported. Detailed experimental settings, including dataset descriptions, baseline methods, and hyperparameters, are provided in Appendix E.

#### 3.2 Main Results

Table 2 reports the cross-subject accuracies on BNCI2014001, including the source model and online TTA techniques. Our proposed BTTA-DG achieves state-of-the-art performance with an average accuracy of 78.70%. Notably, BTTA-DG excels in most subjects, highlighting its robust generalization capabilities across different subjects. We also observe that several gradient-based TTA baselines drop after applying TTA. Because in EEG's online single-trial adaptaion (batch size = 1), noisy trials induce misleading gradients that update BN weights and overwrite pre-trained

Table 2: Cross-subject adaptation accuracy (%) on BNCI2014001, with an asterisk(\*) denoting the significance level (\*: p<0.05).

Setting	Method	S0	S1	S2	S3	S4	S5	S6	S7	S8	Avg.
	CSP	83.33	52.08	97.92	75.00	56.25	67.36	72.22	88.19	71.53	73.77
Source	EEGNet	83.19	60.28	92.08	67.92	57.22	72.50	64.86	86.11	79.44	$73.73_{\pm 1.11}$
	EEG conformer	81.18	64.16	96.80	74.44	58.47	70.76	64.17	92.71	79.03	$75.75_{\pm 2.15}$
	SincAdaptNet	84.97	63.93	97.68	77.13	56.22	72.68	67.26	93.86	79.56	$77.03_{\pm 1.31}$
	BN-adapt	84.97	63.93	97.68	77.13	56.22	72.68	67.26	93.86	79.56	$77.03_{\pm 1.31}$
	Tent	75.97	57.92	94.51	68.54	52.22	65.21	59.38	90.14	68.19	$70.23_{\pm 3.28}$
	PL	76.46	56.67	97.92	70.34	52.29	66.32	60.42	93.89	72.15	$71.83_{\pm 3.21}$
Online TTA	CoTTA	85.00	63.68	98.05	76.32	57.22	72.08	67.64	94.63	80.48	$77.24_{\pm 1.51}$
Online I IA	SAR	84.24	63.40	97.36	76.25	54.72	69.10	67.50	93.54	80.28	$76.27_{\pm 1.92}$
	T-TIME	84.44	61.94	97.43	76.11	56.60	69.38	63.13	94.65	79.38	$75.90_{\pm 1.95}$
	DOT-MDA	81.25	62.50	97.22	78.47	65.97	70.83	61.81	86.81	70.83	$75.08_{\pm 1.19}$
	OTTA	84.43	63.60	97.14	77.63	57.63	73.04	66.44	95.26	83.14	$77.58_{\pm 1.33}$
	BTTA-DG	87.51*	66.67*	98.61*	77.08	57.64	73.61	68.75*	95.83*	82.64	$78.70^*_{\pm 1.32}$

Table 3: Cross-subject adaptation accuracy (%) on BNCI2014002, with an asterisk(\*) denoting the significance level (\*: p<0.05).

Setting	Method	S0	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	S12	S13	Avg.
	CSP	62.00	82.00	98.00	76.00	79.00	70.00	84.00	67.00	94.00	72.00	68.00	63.00	59.00	44.00	72.71
Source	EEGNet	65.00	80.00	83.00	80.20	74.20	68.20	88.80	54.60	91.20	75.00	81.00	72.00	59.80	51.40	$73.17_{\pm 0.59}$
	EEG conformer	66.50	80.50	95.00	78.10	80.10	70.30	90.50	70.20	92.40	73.00	79.50	75.80	58.20	47.30	75.53±1.85
	SincAdaptNet	67.90	80.10	99.00	79.30	81.00	72.20	93.10	76.10	94.00	75.90	81.20	80.90	60.40	51.60	$78.05_{\pm 2.48}$
	BN-adapt	67.90	80.10	99.00	79.30	81.00	72.20	93.10	76.10	94.00	75.90	81.20	80.90	60.40	51.60	78.05±2.48
	Tent	57.20	70.40	90.30	70.70	67.10	68.30	88.10	64.30	91.60	64.10	77.10	70.40	52.30	49.20	$70.08_{\pm 4.30}$
	PL	57.70	72.30	99.80	73.80	71.60	67.70	92.10	65.80	93.60	64.80	78.70	68.40	53.10	49.20	$72.04_{\pm 3.54}$
Online TTA	CoTTA	66.80	79.90	99.90	79.40	81.50	72.30	93.80	75.50	95.00	76.30	81.50	80.50	59.30	52.00	$78.12_{\pm 1.71}$
Online I IA	SAR	66.20	80.10	99.60	77.20	80.80	72.70	91.90	74.40	94.40	74.10	81.30	79.40	57.00	49.10	$77.02_{\pm 2.03}$
	T-TIME	67.10	78.80	99.40	79.60	82.70	70.50	91.80	74.20	92.80	73.80	79.60	79.30	57.70	48.60	$76.85\pm2.34$
	DOT-MDA	66.50	78.00	98.80	78.20	82.50	71.30	90.10	72.50	92.00	78.00	79.10	77.50	56.80	48.80	$76.44_{\pm 1.62}$
	OTTA	67.40	83.00	98.50	78.10	81.30	74.40	94.60	70.00	94.70	78.60	77.20	82.50	63.90	51.80	$78.29_{\pm 1.68}$
	BTTA-DG	69.00*	83.00	100.00	82.00*	83.00	75.00	95.00	80.00*	95.00	77.00	84.00*	83.00	63.40	54.60*	$80.29^*_{\pm 1.07}$

structure—i.e., catastrophic forgetting. BTTA-DG avoids this failure mode by freezing the network and adapting in a probabilistic parameter space, yielding gradient-free calibration without destructive updates. Table 3 and Table 4 summarize LOSO cross-subject accuracies on BNCI2014002 and BNCI2015001. Results on SHU MI dataset and detailed statistical significance analysis are presented in Appendix F.

In addition, we also assessed the performance of BTTA-DG in a within-subject cross-session experiment. We pretrained the model on the first session and tested it on the second session of BNCI2014001, simulating session shifts in the same subject's motor imagery. The results of this cross-session adaptation are presented in Table 5, demonstrating that BTTA-DG effectively adapts to different sessions too  $(86.50\% \pm 2.49\%)$ . Statistical significance analysis are presented in Appendix G

To verify that SincAdaptNet's Sinc-Conv layer learns meaningful bandpass filters, Figure 2 illustrates the frequency responses of each learned filter on BNCI2014001 and their cumulative response in cross-subject LOSO setting (training set: S1–S8; test set: S0). Learned filters partition into three physiologically meaningful ranges – mu rhythm (8-13 Hz, Filters 1-7), beta rhythm (13-30 Hz, Filters 8-17), and gamma rhythm (30-68.5 Hz, Filters 18-24). Cumulative response intensity (black curve) peaks in the mu (11.2 Hz), beta (30.5 Hz), and gamma (55.3 Hz) bands, demonstrating significant energy concentration of MI EEG. Similar spectral patterns emerge across different test subjects (see Appendix I), confirming robust cross-subject adaptation.

Figure 6 (in Appendix H) presents the 16 spatial kernels learned by SincAdaptNet's Spat-Conv layer as scalp topographies, each displaying a distinct electrode weighting akin to those produced by the CSP (Blankertz et al., 2007). The range of frontal, central, parietal, and occipital patterns (Decety, 1996; Lesser et al., 1998) highlights the model's capacity to learn multiple spatial representations of EEG activity.

Figure 3 visualizes the low-dimensional Dirichlet parameter estimated from test EEG trials and GMM clustering outcomes on BNCI2014001 in cross-subject LOSO setting (training set: S1–S8; test set: S0). The low-dimensional Dirichlet parameter of EEG representation exhibits good class separability, with misclassified samples predominantly located near class boundaries. Moreover, a high inter-class KL divergence (31.85) and a low intra-cluster covariance (0.27) indicate that GMM

Table 4: Cross-subject adaptation accuracy (%) on BNCI2015001, with an asterisk(\*) denoting the significance level (\*: p<0.05).

Setting	Method	S0	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	Avg.
	CSP	93.50	93.50	86.50	85.00	79.00	62.00	65.00	59.00	59.50	65.00	59.50	56.50	72.00
Source	EEGNet	91.50	95.00	75.70	85.90	81.30	68.60	65.20	64.30	63.00	66.50	57.50	55.20	$72.48 \pm 0.52$
	EEG conformer	94.00	95.20	83.10	86.50	84.80	66.40	68.50	64.10	63.50	65.00	58.30	56.40	$73.82_{\pm 1.65}$
	SincAdaptNet	97.35	94.70	90.70	87.65	87.30	64.10	72.30	65.30	64.75	63.15	59.80	58.70	$75.48_{\pm 1.84}$
	BN-adapt	97.35	94.70	90.70	87.65	87.30	64.10	72.30	65.30	64.75	63.15	59.80	58.70	75.48±1.84
	Tent	80.30	68.65	73.75	68.05	68.80	55.15	56.60	57.15	54.45	55.55	51.60	50.25	$61.69_{\pm 4.33}$
	PL	97.85	90.50	77.30	80.10	70.30	56.30	58.00	56.75	54.25	55.70	51.60	49.90	$66.55_{\pm 4.17}$
Online TTA	CoTTA	97.90	95.35	90.80	88.45	88.00	63.65	72.10	65.20	65.75	63.45	58.90	58.50	$75.67_{\pm 2.21}$
Offille I IA	SAR	96.85	87.75	90.60	73.30	87.65	64.60	72.65	64.80	65.25	62.75	60.70	57.45	$73.70_{\pm 3.32}$
	T-TIME	95.40	93.70	89.65	86.40	83.45	63.25	73.25	62.50	64.45	60.10	59.00	57.10	$74.02_{\pm 2.40}$
	DOT-MDA	96.00	92.50	88.00	88.50	86.00	63.00	71.50	63.50	65.50	61.00	58.00	56.00	$74.13_{\pm 2.95}$
	OTTA	98.95	95.00	89.05	85.45	87.70	71.55	69.70	67.55	61.45	66.45	62.60	59.00	$76.20_{\pm 1.50}$
	BTTA-DG	98.50	96.00*	92.00*	90.80*	88.50	65.50	75.50	67.50	65.75	65.50	64.50*	65.00*	$77.92^*_{\pm 1.76}$

Table 5: Cross-session adaptation accuracy (%) on BNCI2014001, with an asterisk(\*) denoting the significance level (\*: p<0.05).

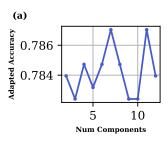
Setting	Method	S0	S1	S2	S3	S4	S5	<b>S6</b>	S7	S8	Avg.
	CSP	88.19	54.17	97.22	65.97	48.61	70.14	68.06	94.44	90.97	75.31
Source	EEGNet	86.81	63.54	94.65	70.97	72.92	68.61	73.26	93.47	92.71	$79.66_{\pm 2.52}$
	EEG Conformer	87.92	58.75	97.15	70.35	75.83	68.54	77.77	95.63	89.23	80.13 <sub>±3.18</sub>
	SincAdaptNet	84.69	56.64	98.51	70.32	86.22	72.06	82.47	97.54	92.47	$82.33_{\pm 2.62}$
	BN-adapt	84.69	56.64	98.51	70.32	86.22	72.06	82.47	97.54	92.47	82.33 <sub>±2.62</sub>
	Tent	80.35	51.18	99.03	57.92	64.38	62.22	64.51	93.06	90.83	$73.72_{\pm 4.77}$
	PL	77.71	51.74	98.75	58.13	75.28	64.58	68.75	97.01	91.46	$75.93_{\pm 4.72}$
Online TTA	CoTTA	85.63	54.51	99.44	69.03	86.46	72.36	82.71	98.33	93.06	$82.39_{\pm 2.83}$
Ollille I IA	SAR	86.32	55.00	99.24	71.11	86.11	70.49	82.92	96.53	91.88	82.18 <sub>±2.99</sub>
	T-TIME	78.40	54.03	98.33	69.79	81.94	70.49	80.69	97.50	91.53	$80.30_{\pm 3.42}$
	DOT-MDA	75.92	60.42	97.22	73.61	81.80	69.67	73.83	93.97	91.67	$79.79_{\pm 2.36}$
	OTTA	89.71	55.89	96.79	72.42	91.58	73.67	87.49	96.03	91.58	$83.91_{\pm 2.25}$
	BTTA-DG	85.42	62.50	100.00*	76.39*	91.67	77.78*	90.97	100.00*	93.75	$86.50^{\overline{*}}_{\pm 2.49}$

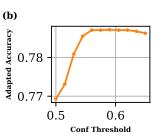
effectively captures both global and local information of Dirichlet parameter distribution, providing a robust statistical foundation for Bayesian inference. The geometry of Dirichlet parameters and cluster remains stable for other test subjects (see Appendix J).

**Computational efficiency** To assess the computational efficiency of BTTA-DG, we measured the average inference time per trial on the BNCI2014001 dataset. As presented in Table 7, BTTA-DG achieves real-time performance with an average inference time of 15.7 ms per trial – 17.8% faster than T-TIME (Li et al., 2023) and 24.2% faster than OTTA (Wimpff et al., 2024), which are the recent baselines for EEG-TTA. Detailed computational complexity analysis is in Appendix K.

**Ablation study.** To dissect the contributions of our proposed components, we conducted an ablation study, with the results summarized in Table 6. We start with the **SincAdaptNet** (**Source Only**) model as our baseline. We then incorporate **Euclidean Alignment** (+ **EA**) to establish the performance of a standard domain alignment technique. The crucial next step isolates the effectiveness of our Dirichlet feature projection by applying the **Dirichlet Projection without the GMM-driven inference** (+ **Dirichlet Projection**), instead using a simple classifier on the projected parameters. Finally, our **BTTA-DG** (**Full Model**) integrates all components. While EA provides a initial alignment (+1.73%), we respectfully argue that the subsequent gain from our novel TTA module is not marginal. The +0.58% gain from "Dirichlet Projection (w/o GMM)" involves no test-time adaptation (classifying by a softmax). GMM-driven Bayesian inference, provides the actual test-time adaptation, yielding a further +1.09% improvement. Collectively, our proposed probabilistic TTA module provides a +1.67% improvement over the strong EA baseline.

Sensitivity analysis To assess the robustness of BTTA-DG, sensitivity analyzes were conducted on three key hyperparameters: the number of GMM components K, the minimum confidence threshold  $\tau_{\rm conf}$  and the maximum entropy threshold  $\tau_{\rm ent}$ .  $\tau_{\rm conf}$  and  $\tau_{\rm ent}$  govern the conditions under which Dirichlet parameters of test trials are stored in the memory bank: Dirichlet parameters are retained if the confidence of trials exceeds  $\tau_{\rm conf}$  and their entropy is below  $\tau_{\rm ent}$ , ensuring that only high-certainty, low-uncertainty test data contribute to the adaptation process. As shown in Figure 4,





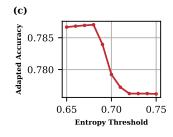


Figure 4: Sensitivity of BTTA-DG to key hyperparameters.

BTTA-DG exhibits robustness across parameter variations. Accuracy remains stable (78.2%–78.7%) for  $K \in [2,12]$ . Higher thresholds (0.50–0.65) improve accuracy from 76.9% to 78.7%, filtering low-confidence trials to reduce noise in adaptation. Low entropy (0.65–0.75) sustains accuracy at 77.6%–78.7%, ensuring only high-certainty trials enter the memory bank.

**Sensitivity to Online Class Imbalance.** To evaluate the robustness of BTTA-DG in practical scenarios where data flow may not be uniformly distributed, we conducted an experiment on the BNCI2014001 dataset under artificially induced online class imbalance. We systematically varied the class ratio in the test set from a balanced 1:1 distribution to a severely imbalanced 1:0.25. While the overall accuracy gracefully degrades with increasing imbalance, we observe that the accuracy for the minority class (Class 1) conversely improves as its prevalence decreases. We present the detailed results and analysis of this phenomenon in Appendix L.

Table 6: Ablation Study on BNCI2014001 Dataset. Cross-subject Mean  $\pm$  s.d. accuracy (%).

Method	Accuracy (%)
SincAdaptNet (Source Only)	$75.30 \pm 1.82$
SincAdaptNet + EA	$77.03 \pm 1.31$
SincAdaptNet + EA + Dirichlet Projection (w/o GMM)	$77.61 \pm 1.43$
BTTA-DG (Full Model)	$78.70 \pm 1.32$

Table 7: Average inference time (ms) on BNCI2014001.

Method	BN-adapt	Tent	PL	CoTTA	SAR	T-TIME	OTTA	BTTA-DG
Time	5.1	18.4	17.8	23.0	32.5	18.5	19.5	15.7

# 4 Conclusion

In this paper, we presented BTTA-DG, a novel gradient-free and efficient TTA framework for MI-EEG decoding. By projecting sequential embeddings into a compact Dirichlet parameter space, our method captures predictive uncertainty and models the target domain's feature distribution. A GMM is employed to summarize historical Dirichlet parameters, preserving global and neighborhood information of test trials. Subsequent Bayesian inference integrates learned historical evidence with the network's priors, effectively bridging domain gaps without the risk of catastrophic forgetting. Our extensive experiments validate that BTTA-DG achieves state-of-the-art adaptation performance, significantly outperforming existing EEG-TTA methods while operating at real-time speeds. While the framework assumes that each trial's time-varying possibility vectors of embeddings are i.i.d. sampled from the Dirichlet distribution. Although real EEG data often exhibit abrupt non-stationarities (e.g.,artifacts) that can locally violate this assumption and momentarily degrade parameter estimates, our framework demonstrates robustness under mild departures. The principles of BTTA-DG would be extended to other modalities, such as fNIRS and ECoG. By enabling high-performance adaptation

without requiring new labeled data, our framework reduces user burden and represents a significant step towards the development of practical, real-world BCI systems.

## ETHICS STATEMENT

The authors adhere to the ICLR Code of Ethics. The datasets utilized in this research are publicly available for all researchers in Brain-Computer Interface. No new data was collected from human subjects for this study. The original data collection was conducted by its respective creators under appropriate ethical protocols, including institutional review board (IRB) approval and informed consent from all participants. Our work is confined to the analysis of this existing, anonymized data and does not introduce new ethical concerns regarding human subjects.

## REPRODUCIBILITY STATEMENT

We are committed to ensuring the reproducibility of our research. The complete source code for our proposed BTTA-DG framework, as well as the scripts to replicate all experiments, is provided at https://anonymous.4open.science/r/BTTA-DG-main-25A1. All experiments were conducted on the publicly accessible datasets. Comprehensive implementation details, including data preprocessing steps, model architecture, optimizer settings, and the full set of hyperparameters along with the strategy for their selection, are thoroughly documented in Section 3.1 and Appendix E.

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# A RELATED WORK

Online test-time adaptation (TTA) methods adapt source models and make simultaneous predictions during inference, utilizing unlabeled online target data (Liang et al., 2025; Xiao & Snoek, 2024). Over the past year, TTA methods have been extended from computer vision to MI EEG signal decoding.

Traditional TTA techniques (batch normalization calibration (Zhao et al., 2023), entropy minimization (Wang et al., 2020; Niu et al., 2023), pseudo-labeling (Lee et al., 2013; Iwasawa & Matsuo, 2021) and consistency regularization(Brahma & Rai, 2023)) can be broadly categorized into parameter finetuning and non-finetuning methods. Non-finetuning methods adjust domain-specific statistics without gradient backpropagation, offering high computational efficiency but limited adaptability. For example, BN-Adapt (Schneider et al., 2020) recalculated BN layer statistics in target domain to mitigate distribution shifts. Parameter finetuning methods, on the other hand, include partial and full finetuning. Partial finetuning methods update only a subset of the network's parameters to balance adaptability and efficiency. For instance, Tent (Wang et al., 2020) minimized entropy by updating only the BN affine parameters. SAR (Niu et al., 2023) further introduced sharpness-aware entropy minimization technique to suppress noisy test samples with large gradients, stabilizing TTA. Full finetuning methods update the entire network using losses calculated by pseudo-labels. For example, Pseudo-Label (Lee et al., 2013) employed the model's high-confidence predictions as pseudo-labels for self-training, whereas CoTTA (Wang et al., 2022) utilized data augmentation to generate pseudo-labels and incorporates weight stochastic restoration to alleviate error accumulation and forgetting.

In MI decoding domain, to address the complexity of EEG signals, state-of-the-art MI-TTA frameworks integrate data alignment techniques with multiple parameter finetuning techniques. Specifically, OTTA (Wimpff et al., 2024) integrated Euclidean Alignment (EA) (Zanini et al., 2017) or Riemannian Alignment (RA) (He & Wu, 2019) techniques with entropy minimization of BN finetuning to reduce cross-subject domain shifts. MI-FTTA (Peng et al., 2025) combines teacher-student mutual learning and time-constrained sample selection to filter noisy pseudo labels, and employed BN statistics recalculation and prototype-based contrastive learning to enhance adaptation performance. T-TIME (Li et al., 2023) used ensemble learning for label prediction and finetuned classifiers by conditional entropy minimization and adaptive marginal distribution regularization, achieving higher performance. Latent alignment method (Bakas et al., 2025) introduced deep sets to EEG decoding and aligned distributions in the deep learning model's feature space. For large-scale online MI decoding, continual finetuning strategies (Wimpff et al., 2025) combined with TTA methods have been also explored to improve BCI performance in real-world applications.

Despite the advancements, critical challenges persist. 1) Computational efficiency: Full finetuning methods incur high cost due to gradient updates, limiting real-time applicability. 2) Catastrophic forgetting: Continuous parameter updates risk overwriting pre-trained knowledge for MI decoding. 3) Shallow statistics-based adaptation: Methods lack theoretical modeling of deep feature shifts across domains. Therefore, developing lightweight, robust, and theoretically grounded MI-TTA methods remains a challenge.

# B SINCADAPTNET DETAILS

SincAdaptNet has only four convolutional layers. The Sinc-Conv layer is not a standard convolution but is parametrically defined by the sinc function with learnable cutoff frequencies, making it highly interpretable. Full hyperparameter settings for the network are detailed in Appendix E. We have also provided the source code at https://anonymous.4open.science/r/BTTA-DG-main-25A1. We have created an architecture diagram to visually clarify the network structure (Figure 5). Besides, we added the following SincAdaptNet architecture equations. Let  $s \in \mathbb{R}^{C \times T}$  be an input EEG trial with C channels and T time points. The four-layer SincAdaptNet processes the input as follows:

**Spat-Conv** Spatial filtering with  $F_{\text{spat}}$  filters of size  $(C \times 1)$ :  $s_{\text{spat}} = W_{\text{spat}} * s$ , where  $W_{\text{spat}} \in \mathbb{R}^{F_{\text{spat}} \times C \times 1}$  are the spatial convolution kernels.

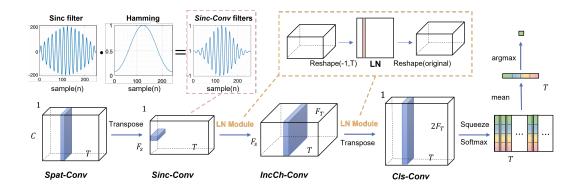


Figure 5: Architecture of SincAdaptNet. A compact four-layer encoder for MI EEG: Spat-Conv (spatial filtering)  $\rightarrow$  Sinc-Conv (learnable, sinc-parameterized band-pass)  $\rightarrow$  IncCh-Conv (channel expansion)  $\rightarrow$  Cls-Conv (per-time class embeddings). Layer normalization is applied after temporal filtering and channel expansion to avoid reliance on batch statistics in online inference.

**Sinc-Conv** Adaptive bandpass filtering with  $F_{\text{sinc}}$  sinc-based filters:  $s_{\text{sinc}} = h_{\text{sinc}} * s_{\text{spat}}$ . The sinc kernel  $h_{\text{sinc}}$  is parametrically generated from learnable cutoff frequencies  $f_{\text{low}}$  and bandwidth  $f_{\text{band}}$ , with  $f_{\text{high}} = f_{\text{low}} + f_{\text{band}}$ . The frequency response of the ideal bandpass filter is:

$$H(f) = \operatorname{rect}\left(\frac{f}{2f_{\text{high}}}\right) - \operatorname{rect}\left(\frac{f}{2f_{\text{low}}}\right) \tag{8}$$

The time-domain impulse response is derived via the inverse Fourier transform,

$$h(n) = 2f_{\text{high}}\operatorname{sinc}(2\pi f_{\text{high}}n) - 2f_{\text{low}}\operatorname{sinc}(2\pi f_{\text{low}}n), \quad -\infty < n < \infty.$$
(9)

Since this ideal response is infinitely long, it is truncated and a Hamming window w(n) is applied to mitigate spectral leakage, resulting in the convolution kernel,

$$h_{\text{windowed}}(n) = h(n) \cdot w(n), \quad -\frac{N_{\text{sinc}}}{2f_{\text{s}}} < n < \frac{N_{\text{sinc}}}{2f_{\text{s}}},$$
 (10)

where  $N_{\rm sinc}$  denotes the truncated length and  $f_{\rm s}$  is the sampling frequency. The Sinc-Conv layer comprises  $F_{\rm sinc}$  adaptive bandpass filters of size  $(1 \times N_{\rm sinc})$  and uses "SAME" padding to preserve temporal dimension.

**IncCh-Conv** Channel expansion with  $2F_{\text{sinc}}$  filters of size  $(F_{\text{spat}} \times 1)$ :  $\boldsymbol{s}_{\text{inc}} = \boldsymbol{W}_{\text{inc}} * \boldsymbol{s}_{\text{sinc}}$ , where  $\boldsymbol{W}_{\text{inc}} \in \mathbb{R}^{2F_{\text{sinc}} \times F_{\text{spat}} \times 1}$ .

**Cls-Conv** Final layer with  $|\mathcal{L}|$  filters:  $X = W_{\text{cls}} * s_{\text{inc}}$ , where  $W_{\text{cls}} \in \mathbb{R}^{|\mathcal{L}| \times 2F_{\text{sinc}} \times 1}$ , yielding output  $X \in \mathbb{R}^{|\mathcal{L}| \times T}$ . Each column is passed through a softmax to form a time-varying categorical vector, and the temporal average provides a robust prior for Bayesian calibration in our TTA framework.

# C DIRICHLET PARAMETER ESTIMATION DETAILS

This section details the efficient algorithm used to compute the Maximum Likelihood Estimate (MLE) of the Dirichlet parameters  $\alpha$  from a sequence of categorical probability vectors  $\boldsymbol{X} = [\boldsymbol{x}_1, \dots, \boldsymbol{x}_T]$  with  $\boldsymbol{x}_j \in \Delta^{|\mathcal{L}|-1}$ . The method is based on the well-established fixed-point iteration algorithm by Minka (2012), which we implement with accelerated convergence for our online TTA framework.

**Fixed-point iteration for MLE** Let  $X = [x_1, x_2, \dots, x_T]$  be a set of T samples, where each  $x_j = (x_{1j}, x_{2j}, \dots, x_{|\mathcal{L}|j})^{\top}$  is a categorical probability vector sampled from a Dirichlet distribution with parameters  $\boldsymbol{\alpha} = (\alpha_1, \dots, \alpha_{|\mathcal{L}|})$ . The goal is to estimate  $\mathcal{P}(X) = \hat{\boldsymbol{\alpha}}_{\text{MLE}}$ , the MLE of  $\boldsymbol{\alpha}$ . The log-likelihood function for the Dirichlet distribution is employed.

$$\mathcal{L}(\alpha) = \sum_{j=1}^{T} \log \mathcal{D}(x_j; \alpha). \tag{11}$$

The maximum likelihood estimator  $\hat{\alpha}_{\text{MLE}}$  can be obtained by iteratively computing

$$\alpha_i^{\text{new}} = \psi^{-1} \left( \psi(\alpha_0^{\text{old}}) + \frac{1}{T} \sum_{j=1}^T \log x_{ij} \right) . \tag{12}$$

where  $\psi\left(u\right) = \frac{d}{du}\Gamma\left(u\right)$  denotes the Digamma function.

Thus, if the inverse Digamma function  $\psi^{-1}$  can be obtained, the iterative rule (12) is used to estimate the Dirichlet parameters for sequential embeddings of each test EEG trial.

To accelerate convergence, we initialize the Dirichlet parameters  $\alpha^{\text{init}}$  using the empirical mean  $\bar{x}_i$  and variance  $\sigma_i^2$  of the categorical probability vectors from sequential embeddings. From the properties of the Dirichlet distribution, the mean and variance satisfy:

$$\bar{x}_i = \frac{\sum_{j=1}^T x_{ij}}{T} = \frac{\alpha_i}{\alpha_0},\tag{13}$$

$$\sigma_i^2 = \frac{1}{T} \sum_{j=1}^T (x_{ij} - \bar{x}_i)^2 = \frac{\bar{x}_i (1 - \bar{x}_i)}{\alpha_0 + 1}.$$
 (14)

Therefore, an initial estimate  $\alpha^{\text{init}}$  can be computed as,

$$\alpha_0^{\text{init}} \approx \frac{1}{|\mathcal{L}|} \sum_{i=1}^{|\mathcal{L}|} \left( \frac{\bar{x}_i \left( 1 - \bar{x}_i \right)}{\sigma_i^2} - 1 \right), \tag{15}$$

$$\alpha_i^{\text{init}} = \alpha_0^{\text{init}} \bar{x}_i. \tag{16}$$

By iterating rule (12) with these initial estimates and solving for  $\psi^{-1}$  via Newton's method (described below), we efficiently converge to the Dirichlet parameters  $\hat{\alpha}_{\text{MLE}}$ .

**Newton's iteration for calculating inverse Digamma** The Digamma function is defined by

$$\psi(u) = \frac{d}{du}\Gamma(u) = -\gamma + \sum_{n=0}^{\infty} \left(\frac{1}{n+1} - \frac{1}{n+u}\right),\tag{17}$$

where Euler constant  $\gamma = -\psi(1)$ . To solve for  $u = \psi^{-1}(v)$  from the equation  $\psi(u) - v = 0$ , we employ Newton's iteration (Gil et al., 2007). Given  $v = \psi(\alpha_0^{\text{old}}) + \frac{1}{T} \sum_{j=1}^{T} \log x_{ij}$  in rule (12), the Newton iteration is formulated as,

$$u^{\text{new}} = u^{\text{old}} - \frac{\psi(u^{\text{old}}) - v}{\psi'(u^{\text{old}})},\tag{18}$$

where  $\psi'(u)$  denotes the Trigamma function.

To further accelerate convergence of Newton's iteration, the initial value  $u^{\rm init}$  is initialized using an approximate inverse function  $\widetilde{\psi}^{-1}(v)$ , where

$$\psi(u) = \widetilde{\psi}(u) = \begin{cases} \log(u - 1/2) & \text{if } u \ge 0.6, \\ -\frac{1}{u} - \gamma & \text{if } u < 0.6, \end{cases}$$
(19)

Yelds,

$$u^{\text{init}} = \widetilde{\psi}^{-1}(v) = \begin{cases} \exp\left(v + \frac{1}{2}\right), & \text{if } v \ge -2.22\\ -\frac{1}{v+\gamma}, & \text{if } v < -2.22 \end{cases}$$
 (20)

Once convergence is reached, we substitute  $\psi^{-1}(v) = u^{\text{new}}$  into fixed-point iteration rule (12) to update  $\alpha_i^{\text{new}} = u^{\text{new}}$ . Iterating this process yields the estimated Dirichlet parameters  $\hat{\alpha}_{\text{MLE}}$ .

**Numerical stability.** We clip  $x_{ij}$  to  $[10^{-7}, 1 - 10^{-7}]$  to avoid zeros, and early-stop when  $\|\boldsymbol{\alpha}^{\text{new}} - \boldsymbol{\alpha}^{\text{old}}\|/\|\boldsymbol{\alpha}^{\text{old}}\| < 10^{-4}$ . In all datasets, the method converges within  $\boldsymbol{O}(I_{\text{iter}})$  iterations per trial, where  $I_{\text{iter}}$  typically remains under 5–10.

# THE PSEUDO-CODE OF BTTA-DG

Algorithm 1 summarizes the pseudo-code of the proposed BTTA-DG framework.

```
Algorithm 1: BTTA-DG Framework
```

```
Input: Pretrained model f_{\theta}, memory banks M_y, test trial s, tolerance \varepsilon, K GMM components,
        the minimum confidence threshold \tau_{\rm conf} and the maximum entropy threshold \tau_{\rm ent}.
```

**Output:** Calibrated label  $\hat{y}_{cal}$ .

#### // Feature extraction

$$m{X} \leftarrow g_{ ext{enc}}(m{s}) \ p_{m{ heta}}(m{y}) \leftarrow f_{ ext{cls}}(m{X})$$
 // Obtain priori

# // Accelerated Dirichlet parameter estimation

// Initialize  $\alpha^{\rm init}$ 

$$\begin{aligned} & \textbf{for } i = 1 \textbf{ to } |\mathcal{L}| \textbf{ do} \\ & \begin{vmatrix} \bar{x}_i \leftarrow \frac{1}{T} \sum_{j=1}^T x_{ij} \\ \sigma_i^2 \leftarrow \frac{1}{T} \sum_{j=1}^T \left( x_{ij} - \bar{x}_i \right)^2 \\ \alpha_0^{\text{init}} \leftarrow \frac{1}{|\mathcal{L}|} \sum_{i=1}^{|\mathcal{L}|} \left( \frac{\bar{x}_i (1 - \bar{x}_i)}{\sigma_i^2} - 1 \right) \\ \alpha_i^{\text{init}} \leftarrow \alpha_0^{\text{init}} \bar{x}_i \end{aligned}$$

$$\alpha_i^{\text{new}} \leftarrow \alpha_i^{\text{init}}, \, \alpha_0^{\text{new}} \leftarrow \alpha_0^{\text{init}}$$

// Fixed-point iteration for MLE

while 
$$\|\alpha^{new} - \alpha^{old}\| > \varepsilon$$
 do  $\|\alpha^{old} \leftarrow \alpha^{new}\|$ 

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$$\qquad \qquad \alpha_0^{\text{new}} \leftarrow \sum_{i=1}^{|\mathcal{L}|} \alpha_i^{\text{new}}$$

$$\hat{oldsymbol{lpha}}_{ ext{MLE}} \leftarrow oldsymbol{lpha}^{ ext{new}}$$

# // GMM-driven Bayesian inference

for  $y \in \mathcal{L}$  do

Fit GMM: 
$$\{\pi_{y,k}, \boldsymbol{\mu}_{y,k}, \boldsymbol{\Sigma}_{y,k}\}_{k=1}^{K} \leftarrow \text{EM}(M_{y}, K)$$

$$p_{\text{GMM}}\left(\hat{\boldsymbol{\alpha}}_{\text{MLE}} \mid \boldsymbol{y}\right) \leftarrow \sum_{k=1}^{K} \pi_{y,k} \mathcal{N}\left(\hat{\boldsymbol{\alpha}}_{\text{MLE}} \mid \boldsymbol{\mu}_{y,k}, \boldsymbol{\Sigma}_{y,k}\right)$$

$$p_{\text{cal}}\left(\boldsymbol{y} \mid \hat{\boldsymbol{\alpha}}_{\text{MLE}}\right) \leftarrow \frac{p_{\text{GMM}}\left(\hat{\boldsymbol{\alpha}}_{\text{MLE}} \mid \boldsymbol{y}\right) p_{\boldsymbol{\theta}}(\boldsymbol{y})}{\sum_{\boldsymbol{y}'=1}^{|\mathcal{L}|} p_{\text{GMM}}\left(\hat{\boldsymbol{\alpha}}_{\text{MLE}} \mid \boldsymbol{y}'\right) p_{\boldsymbol{\theta}}(\boldsymbol{y}')}$$

end

# // Final prediction and memory bank update

$$\begin{split} \hat{y}_{\text{cal}} \leftarrow \arg\max_{y \in \mathcal{L}} \ p_{\text{cal}} \Big( y \mid \hat{\boldsymbol{\alpha}}_{\text{MLE}} \Big) \\ \text{confidence} \leftarrow p_{\text{cal}} \big( \hat{y}_{\text{cal}} \mid \hat{\boldsymbol{\alpha}}_{\text{MLE}} \big) \\ \text{entropy} \leftarrow -\sum_{y} p_{\text{cal}} (y \mid \hat{\boldsymbol{\alpha}}_{\text{MLE}}) \ \log p_{\text{cal}} (y \mid \hat{\boldsymbol{\alpha}}_{\text{MLE}}) \\ \text{if confidence} \geq \tau_{conf} \ \textit{and} \ \text{entropy} \leq \tau_{ent} \ \text{then} \\ \big| \ D\text{rop oldest if} \ |M_{\hat{y}_{\text{cal}}}| \geq \text{buffer\_size} \\ \big| \ M_{\hat{y}_{\text{cal}}} \leftarrow M_{\hat{y}_{\text{cal}}} \cup \big\{ \hat{\boldsymbol{\alpha}}_{\text{MLE}} \big\} \end{split}$$

end

return  $\hat{y}_{\text{cal}}$ 

# E IMPLEMENTATION DETAILS

This appendix provides further details on the datasets, baseline methods, and experimental configurations.

# **Dataset descriptions**

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- BNCI2014001: Derived from BCI Competition IV-2a Tangermann et al. (2012), this dataset includes data from 9 subjects performing four-class MI tasks (left hand, right hand, feet, tongue) recorded using 22 EEG electrodes at 250 Hz. Each subject completed two sessions (288 trials per session) with a trial duration of 4 seconds. Only trials of left hand and right hand were used for analysis.
- BNCI2014002: This dataset contains data from 14 subjects performing two-class MI tasks (right hand vs. feet) recorded using 15 EEG electrodes at 512 Hz. Each subject participated in one session comprising 160 trials, with a trial duration of 5 seconds. Only the first 100 trials per subject were used for analysis.
- BNCI2015001: This dataset comprises data from 12 subjects performing two-class MI tasks (right hand vs. feet) recorded using 13 EEG electrodes at 512 Hz, each subject completed three sessions with 200 trials per session and a trial duration of 5 seconds.
- SHU MI Dataset (Ma et al., 2022). This dataset is particularly relevant as it was specifically
  designed to study long-term variability, containing data from 25 subjects recorded over 5
  different days. Following the evaluation protocol provided with the dataset's official code,
  we performed a rigorous Leave-One-Subject-Out (LOSO) experiment on the last 10 subjects.

# **Baselines** To comprehensively evaluate BTTA-DG, we compared it against:

- CSP Blankertz et al. (2007): A traditional machine learning method that constructs spatial
  filters to maximize the variance of one class while minimizing that of another, thereby
  enhancing class separability.
- EEGNet Lawhern et al. (2018): A compact convolutional neural network that integrates spatial-temporal feature extraction from EEG signals. BN-adapt Schneider et al. (2020): Adjusts BN statistics to better adapt the target distribution.
- EEG Conformer (Song et al., 2022): A Transformer-based architecture designed to capture complex temporal dependencies in EEG signals. This baseline tests whether architectural advances alone are sufficient to overcome the domain shift challenge.
- Tent Wang et al. (2020): Optimizes affine parameters of BN via entropy minimization.
- PL Lee et al. (2013): Uses high-confidence predictions as pseudo-labels for self-training.
- SAR Niu et al. (2023): Incorporates reliable entropy minimization and sharpness-aware optimization to suppress noisy samples with large gradients.
- CoTTA Wang et al. (2022): Adapts the model using pseudo-labels generated through data augmentation and stochastic weight restoration to mitigate catastrophic forgetting.
   Data augmentation techniques implemented include Gaussian noise, time shift, frequency shift, phase perturbations, time dropout, channel dropout, channel shuffle, bandstop filter, and channel symmetry Rommel et al. (2022).
- T-TIME Li et al. (2023): Uses ensemble learning where multiple classifiers predict each unlabeled test EEG sample, updating classifiers via conditional entropy minimization and adaptive marginal distribution regularization.
- DOT-MDA (Ju & Guan, 2025): A recent geometric deep learning method that uses Optimal Transport to directly align distributions of EEG covariance matrices on Riemannian manifolds. This provides a direct comparison against another principled alignment strategy.
- OTTA Wimpff et al. (2024): Integrats Euclidean Alignment or Riemannian Alignment techniques with entropy minimization of BN finetuning to reduce cross-subject domain shifts.

 **Pre-training and test-time adaptation configurations** The SincAdaptNet was pre-trained on train set using the AdamW optimizer with a learning rate of 1e-3, a batch size of 32, for 100 epochs. For fair comparison, all TTA methods (except CSP and EEGNet) used SincAdaptNet as the backbone and applied EA preprocessing. SincAdaptNet processes EEG trials  $s \in \mathbb{R}^{B \times 1 \times C \times T}$  through: (1) Spatial filtering via 2D convolution (kernel\_size = (C,1),  $F_{\rm spat}=16$  outputs), (2) Temporal filtering with Sinc FIR bandpass filters (4-30Hz) via SincConv (kernel\_size = (1,51),  $F_{\rm sinc}=16$  outputs), (3) Layer normalization, (4) Increasing-Channel convolution with ELU activation, (5) Layer normalization, and (6) Classifing convolution with LogSoftmax activation.

During test-time adaptation, the model was adapted using a batch size of 1, for 1 epoch. The memory bank size was set to 1000. The convergence tolerance for Dirichlet parameter estimation was set to  $\varepsilon=1e-3$ . As shown in the sensitivity analysis in Figure 4, our method is robust to moderate variations in hyperparameters of our adaptation process. The final values for GMM components, confidence threshold, and entropy threshold were determined based on a grid search over a reasonable range, with the optimal values selected based on the average performance on a held-out validation set created from the source domain subjects. This standard validation procedure ensures that the hyperparameter tuning is fair and does not use any information from the target domain. The GMM was configured with 8 components. The minimum confidence threshold  $\tau_{\rm conf}$  was set to 0.596, and the maximum entropy threshold  $\tau_{\rm ent}$  was set to 0.673.

The source code is available for reproducibility at https://anonymous.4open.science/r/BTTA-DG-main-25A1. Experiments were implemented via Python 3.10 and PyTorch 2.1.0, and ran on a server with NVIDIA TITAN V GPU and an Intel(R) Xeon(R) Gold 6230 CPU @ 2.10GHz.

# F TABLES OF CROSS-SUBJECT ADAPTATION ACCURACY AND STATISTICAL SIGNIFICANCE ANALYSIS

Table 8 summarize LOSO cross-subject accuracies on SHU MI dataset for online adaptation methods. Our BTTA-DG framework consistently outperforms all competing TTA methods. However, the performance gain is not statistically significant. We have investigated this and believe it stems from the lower EEG quality and higher complexity (5 sessions) of this particular dataset. This has limited the effectiveness of the feature extractors. When the baseline feature discriminability is lower, it becomes inherently more difficult for any TTA method to demonstrate large, statistically significant gains.

We assess statistical significance by conducting pairwise one-way ANOVA tests between BTTA-DG and each baseline. Table 9, 10 and 11 list per-subject and overall ANOVA p-values comparing BTTA-DG against each baseline. In most subjects, BTTA-DG demonstrated a significant difference from the baseline method (p < 0.05), further validating the statistical superiority of the BTTA-DG.

Table 8: Cross-subject adaptation accuracy (%) on SHU MI dataset.

Setting	Method	Avg. (%)
	CSP	59.24
Source	EEGNet	$61.07_{\pm 1.10}$
	EEG conformer	$61.36_{\pm 1.65}$
	SincAdaptNet	$62.42_{\pm 1.72}$
	BN-adapt	62.42 <sub>±1.72</sub>
	Tent	$56.23_{\pm 2.96}$
	PL	$56.65_{\pm 2.82}$
Online TTA	CoTTA	$62.73_{\pm 1.78}$
Ollille I IA	SAR	$58.33_{\pm 2.37}$
	T-TIME	$62.37_{\pm 1.75}$
	DOT-MDA	$62.83_{\pm 1.64}$
	OTTA	$63.29_{\pm 1.20}$
	BTTA-DG	$64.06_{\pm 1.92}$

Table 9: Pairwise ANOVA *p*-values comparing BTTA-DG to each baseline on BNCI2014001 for cross-subject adaptation.

Method	S0	S1	S2	S3	S4	S5	<b>S6</b>	S7	S8	Overall
SincAdaptNet	3.5e-07	1.2e-08	8.4e-11	9.0e-01	6.2e-02	5.1e-02	2.2e-02	1.2e-04	1.7e-04	1.1e-03
BN-adapt	3.5e-07	1.2e-08	8.4e-11	9.0e-01	6.2e-02	5.1e-02	2.2e-02	1.2e-04	1.7e-04	1.1e-03
Tent	1.4e-06	6.1e-08	6.8e-04	1.6e-10	2.5e-07	6.9e-07	9.7e-12	7.6e-05	2.0e-08	4.6e-05
PL	1.5e-07	7.4e-11	2.7e-06	8.5e-07	4.6e-04	2.1e-06	1.6e-06	3.7e-03	3.9e-05	4.9e-04
CoTTA	9.5e-07	2.9e-05	1.1e-05	1.9e-01	5.7e-01	1.6e-03	8.3e-02	8.0e-03	2.9e-03	1.2e-03
SAR	9.9e-06	7.3e-05	9.0e-05	4.4e-02	3.1e-07	7.6e-05	7.2e-02	6.6e-03	3.0e-02	2.7e-04
T-TIME	1.1e-05	4.1e-05	4.4e-04	1.3e-01	2.6e-01	2.0e-07	1.3e-07	4.1e-03	1.4e-03	1.5e-03
DOT-MDA	1.0e-06	8.1e-05	8.3e-01	2.2e-01	3.0e-09	1.6e-05	1.0e-06	1.0e-09	2.7e-10	1.0e-03
OTTA	2.3e-06	4.7e-07	1.7e-08	3.8e-01	9.9e-01	1.4e-01	1.1e-03	2.4e-04	4.1e-02	4.8e-02

Table 10: Pairwise ANOVA *p*-values comparing BTTA-DG to each baseline on BNCI2014002 for cross-subject adaptation.

Method	S0	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	S12	S13	Overall
SincAdaptNet	4.5e-02	2.9e-10	0.00	5.8e-05	1.6e-04	3.5e-07	3.7e-09	1.0e-07	0.00	1.7e-04	9.0e-08	5.8e-04	9.4e-05	3.2e-07	4.4e-07
BN-adapt	4.5e-02	2.9e-10	0.00	5.8e-05	1.6e-04	3.5e-07	3.7e-09	1.0e-07	0.00	1.7e-04	9.0e-08	5.8e-04	9.4e-05	3.2e-07	4.4e-07
Tent	8.2e-11	1.8e-08	1.3e-04	8.9e-07	9.3e-08	1.3e-03	6.7e-04	2.0e-08	1.2e-02	6.0e-08	9.7e-08	6.0e-06	6.4e-13	1.9e-13	2.3e-07
PL	1.3e-09	6.3e-07	3.3e-01	1.6e-06	1.9e-04	5.8e-04	1.1e-05	1.5e-08	9.0e-08	6.7e-07	2.5e-03	2.0e-09	1.0e-09	1.9e-13	1.8e-05
CoTTA	3.8e-03	1.4e-05	3.3e-01	1.3e-02	5.6e-03	1.4e-03	1.1e-05	3.9e-05	1.0e+00	1.5e-02	9.9e-04	1.2e-03	8.0e-04	5.4e-03	4.1e-05
SAR	2.2e-03	3.1e-08	8.7e-02	5.4e-04	1.2e-02	1.9e-03	2.2e-05	2.6e-06	3.7e-02	2.0e-04	2.2e-07	3.1e-06	1.9e-06	4.0e-04	7.2e-06
T-TIME	5.6e-03	9.4e-05	3.7e-02	2.6e-02	7.3e-01	1.4e-04	6.8e-06	2.4e-04	5.9e-08	3.9e-06	2.6e-06	8.0e-04	6.4e-06	2.4e-05	5.9e-06
DOT-MDA	1.3e-04	1.4e-05	8.5e-01	5.2e-05	9.0e-01	4.7e-05	1.8e-06	3.1e-08	2.1e-05	9.0e-01	1.8e-05	4.9e-06	3.9e-07	2.6e-06	5.0e-04
OTTA	2.0e-02	1.0e+00	2.7e-06	2.6e-04	8.8e-03	4.8e-01	1.5e-01	6.9e-08	6.5e-02	4.2e-04	2.1e-11	3.3e-01	1.2e-01	2.3e-05	3.7e-02

Table 11: Pairwise ANOVA p-values comparing BTTA-DG to each baseline on BNCI2015001 for cross-subject adaptation.

Method	S0	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	Overall
SincAdaptNet	5.8e-08	4.6e-07	2.9e-02	3.8e-08	8.3e-02	6.2e-03	3.1e-02	4.8e-03	3.2e-01	2.9e-05	2.8e-05	7.4e-11	5.5e-04
BN-adapt	5.8e-08	4.6e-07	2.9e-02	3.8e-08	8.3e-02	6.2e-03	3.1e-02	4.8e-03	3.2e-01	2.9e-05	2.8e-05	7.4e-11	5.5e-04
Tent	8.2e-06	1.5e-10	2.2e-06	6.0e-14	1.1e-09	7.7e-10	4.4e-10	7.0e-11	5.5e-09	1.3e-08	8.4e-18	2.0e-21	7.0e-07
PL	1.3e-02	2.7e-02	2.7e-05	8.8e-04	1.6e-12	1.4e-07	4.2e-06	1.8e-11	9.8e-11	8.5e-08	3.0e-17	4.7e-22	8.0e-06
CoTTA	9.9e-03	3.7e-02	1.9e-01	1.3e-04	5.7e-01	1.6e-02	2.8e-02	2.9e-02	7.6e-01	2.5e-02	1.1e-07	1.8e-09	4.6e-03
SAR	1.2e-02	6.2e-03	1.5e-02	3.9e-06	6.6e-02	3.6e-01	1.1e-02	5.0e-03	5.7e-01	7.3e-04	2.0e-03	4.3e-07	1.2e-02
T-TIME	1.7e-06	7.0e-05	2.9e-03	5.4e-07	2.9e-07	1.2e-04	1.4e-01	4.2e-05	7.0e-03	5.5e-07	2.8e-03	2.7e-07	3.1e-05
DOT-MDA	1.3e-04	3.7e-05	6.6e-05	5.8e-04	1.3e-04	1.3e-04	6.6e-05	6.6e-05	9.5e-01	4.1e-05	5.1e-07	1.9e-09	1.5e-03
OTTA	1.9e-02	3.9e-07	2.1e-03	1.9e-06	4.3e-02	5.5e-14	1.3e-06	8.9e-01	2.2e-07	4.4e-02	2.2e-03	2.8e-12	5.0e-02

Table 12: Pairwise ANOVA *p*-values comparing BTTA-DG to each baseline on BNCI2014001 for cross-session adaptation.

Method	S0	S1	S2	S3	S4	S5	S6	S7	S8	Overall
SincAdaptNet	1.7e-01	3.2e-07	8.6e-09	3.1e-04	1.6e-03	2.2e-06	6.2e-04	1.1e-11	1.9e-06	1.8e-03
BN-adapt	1.7e-01	3.2e-07	8.6e-09	3.1e-04	1.6e-03	2.2e-06	6.2e-04	1.1e-11	1.9e-06	1.8e-03
Tent	1.6e-01	1.0e-14	6.5e-04	1.3e-11	1.1e-15	2.4e-11	1.1e-10	3.6e-02	8.7e-03	4.5e-03
PL	3.2e-06	3.8e-14	1.0e-06	4.2e-12	4.7e-05	1.7e-07	1.9e-05	1.1e-03	5.6e-02	3.0e-03
CoTTA	7.8e-01	9.8e-09	8.4e-04	3.8e-05	3.4e-03	9.4e-06	1.6e-03	2.5e-09	3.5e-03	7.2e-03
SAR	2.8e-01	1.6e-05	8.9e-04	8.3e-04	9.6e-05	3.2e-06	3.1e-04	1.3e-07	7.6e-04	3.7e-03
T-TIME	9.7e-06	1.5e-08	2.5e-05	5.6e-04	2.9e-07	9.6e-06	3.0e-04	5.4e-07	9.6e-03	4.8e-04
DOT-MDA	3.5e-08	4.8e-02	8.1e-07	3.5e-02	2.5e-07	5.1e-06	2.2e-14	4.5e-15	4.1e-09	3.1e-04
OTTA	3.1e-10	3.0e-08	6.9e-17	3.3e-02	8.4e-01	4.0e-06	1.1e-01	3.0e-13	3.0e-09	3.7e-02

# G WITHIN-SUBJECT CROSS-SESSION EXPERIMENTS

To verify that BTTA-DG can adapt not only across subjects but also across sessions for the same subject, we conducted a within-subject cross-session study on BNCI2014001. Specifically, we pretrained SincAdaptNet on 1st session of each subject and then performed test-time adaptation on that subject's 2nd session, simulating session shifts on different days. Table 5 reports the classification accuracies for cross-session adaptation. BTTA-DG achieves an average of  $86.50\% \pm 2.49\%$ , significantly outperforming all competing TTA methods (asterisks denote p < 0.05 by pairwise ANOVA against each baseline).

Table 12 presents the corresponding pairwise ANOVA *p*-values comparing BTTA-DG to each baseline across subjects S0–S8, as well as an overall *p*-value computed on per-subject mean accuracies. Most

comparison reach statistical significance, confirming that our gradient-free Bayesian calibration maintains its advantage even under within-subject cross-session drift.

## H TOPOGRAPHIC VISUALIZATION OF THE LEARNED SPATCONV KERNELS

The use of spatial convolution is a standard and effective technique in EEG deep learning models (e.g., EEGNet (Lawhern et al., 2018), ATCNet (Altaheri et al., 2022), EEG conformer (Song et al., 2022), M-FANet (Qin et al., 2024), and etc.) to learn spatial filters. While EEG channel ordering is arbitrary, the "C x 1" convolution learns a weighted sum of all channels (not only local adjacent channels), effectively creating data-driven spatial filters that can capture relationships between physically distant but functionally related brain regions (e.g., bilateral motor cortices). Our topographic visualizations in Figure 6 show that the learned kernels are not limited to local neighbors but capture diverse and physiologically meaningful scalp-wide patterns, confirming its ability to learn non-local inter-channel relationships.

Figure 6 shows all 16 spatial kernels from SincAdaptNet's Spat-Conv layer, rendered on a standard 10–20 montage Nomenclature (1991) scalp map. Together, these topographies span frontal, central, parietal, and occipital cortices, demonstrating that SincAdaptNet automatically learns multiple physiologically meaningful spatial filters—much like CSP but in a fully data-driven, end-to-end fashion.

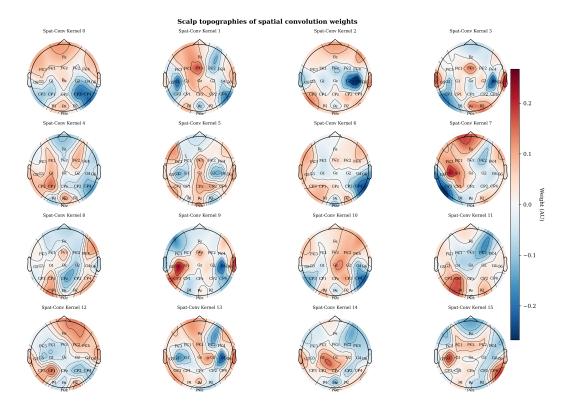
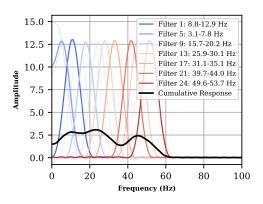


Figure 6: Topographic visualization of Spat-Conv kernels for SincAdaptNet trained on BNCI2014001 (22 channels). Each subplot displays one spatial kernel mapped onto the 2D electrode layout (standard 10-20 montage), where the color scale indicates the weight amplitude.

# I FIGURES OF FREQUENCY RESPONSES OF THE LEARNED SINCCONV FILTERS

To provide a comprehensive view of how SincAdaptNet's learnable band-pass filters operate across all subjects, this appendix presents the complete frequency responses of each of the 24 Sinc-Conv filters for every LOSO test fold. These figures substantiate the interpretability and effectiveness of Sinc-Conv as a data-driven substitute for hand-crafted bandpass filtering in EEG analysis.



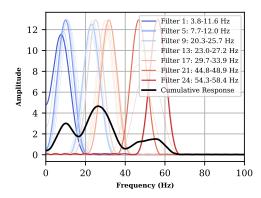
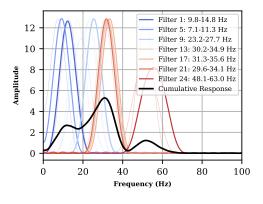


Figure 7: Training set: others; test set: S1

Figure 8: Training set: others; test set: S2



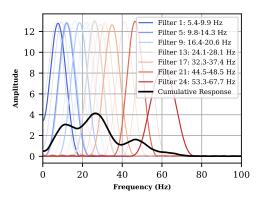
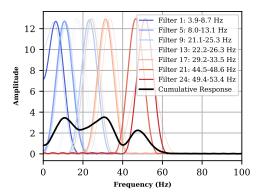


Figure 9: Training set: others; test set: S3

Figure 10: Training set: others; test set: S4



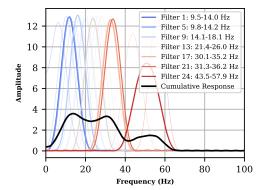
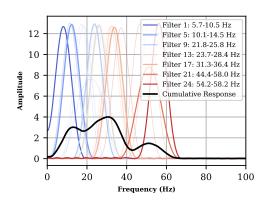


Figure 11: Training set: others; test set: S5

Figure 12: Training set: others; test set: S6



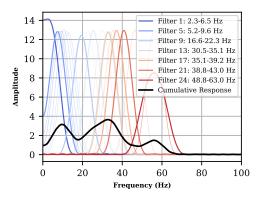
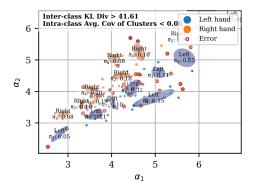


Figure 13: Training set: others; test set: S7

Figure 14: Training set: others; test set: S8

# J FIGURES OF DIRICHLET PARAMETER DISTRIBUTION WITH GMM CLUSTERING

To provide a comprehensive view of how our Dirichlet–GMM pipeline captures class-specific structure in the low-dimensional embedding space across all subjects, this appendix presents the complete scatters of Dirichlet parameter representation and GMM clustering outcome for every LOSO test fold. These figures illustrate the stability and separability of the Dirichlet parameter representation across test trials, and how a Gaussian mixture model (GMM) clusters these parameters into coherent groups. This analysis validates our choice of Dirichlet projection to compactly encode prediction uncertainty and our use of GMM to preserve both global and local neighborhood information in BTTA-DG.



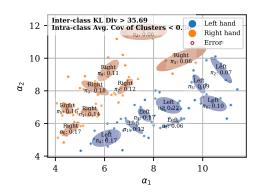


Figure 15: Training set: others; test set: S1

Figure 16: Training set: others; test set: S2

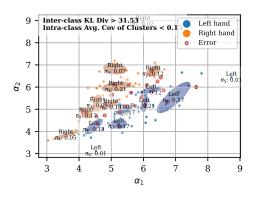
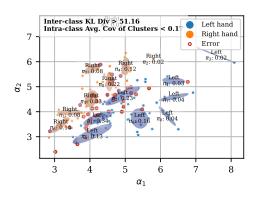


Figure 17: Training set: others; test set: S3

Figure 18: Training set: others; test set: S4



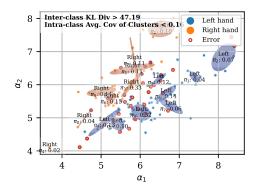
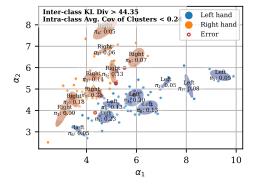


Figure 19: Training set: others; test set: S5

Figure 20: Training set: others; test set: S6



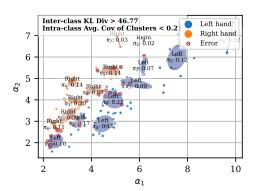


Figure 21: Training set: others; test set: S7

Figure 22: Training set: others; test set: S8

# K COMPUTATIONAL COMPLEXITY

This appendix summarizes the space and time complexity of BTTA-DG's test-time pipeline, covering Dirichlet parameter estimation, memory maintenance, and GMM-based calibration. Let M be the size of the memory bank,  $|\mathcal{L}|$  the number of classes (i.e., the Dirichlet dimension  $d = |\mathcal{L}|$ ), and K the number of mixture components per class.

**Space complexity.** For each trial we store only its low-dimensional Dirichlet parameter vector  $\alpha \in \mathbb{R}^d_+$ , so the memory bank costs  $\mathcal{O}(Md)$ . GMM parameters per class add  $\mathcal{O}(Kd)$  for means and  $\mathcal{O}(Kd)$  for diagonal variances (plus  $\mathcal{O}(K)$  for weights). Since M is fixed and  $d \in \{2,4\}$  in our MI-EEG settings, the overall cost is minimal.

#### Time complexity.

- **Dirichlet MLE.** For a trial with T time steps, computing sufficient statistics  $s_i = \frac{1}{T} \sum_{j=1}^{T} \log x_{ij}$  costs  $\mathcal{O}(Td)$ ; the fixed-point updates with Newton refinement for  $\psi^{-1}$  then cost  $\mathcal{O}(d\,I_{\text{iter}})$ , where the number of iterations  $I_{\text{iter}}$  is typically < 5–10 (see Appendix C). Hence, Dirichlet projection:  $\mathcal{O}(Td+d\,I_{\text{iter}}) \approx \mathcal{O}(Td)$ .
- Memory update. Appending a single vector (and evicting the oldest when full) is a queue operation with  $\mathcal{O}(1)$ .
- **GMM re-fitting.** Re-fitting by EM over the memory bank has per-EM-iteration cost  $\mathcal{O}(MKd^2)$ . For  $I_{\text{EM}}$  iterations, the per-trial overhead is  $\mathcal{O}(I_{\text{EM}} MKd^2)$ .

Given that  $d \le 4$ , K is small, and M is bounded, the end-to-end overhead is negligible in practice while enabling robust, gradient-free adaptation.

# L DETAILED ANALYSIS OF CLASS IMBALANCE SENSITIVITY

The experiment on online class imbalance was designed to probe the adaptive behavior of our BTTA-DG framework under challenging, non-uniform data distributions. The full results are presented in Table 13.

Table 13: Performance of BTTA-DG under varying online class imbalance ratios on the BNCI2014001 dataset. As imbalance increases, the model specializes, improving minority class accuracy.

Class Ratio (0:1)	Accuracy Class 0 (%)	Accuracy Class 1 (%)	Overall Accuracy (%)
1:1	$77.01 \pm 1.53$	$80.40 \pm 1.45$	$78.70 \pm 1.32$
1:0.75	$74.07 \pm 1.44$	$80.45 \pm 1.34$	$76.81 \pm 1.25$
1:0.5	$69.75 \pm 1.52$	$83.02 \pm 1.42$	$74.17 \pm 1.28$
1:0.25	$64.67 \pm 1.18$	$85.19 \pm 1.64$	$68.77 \pm 1.19$

As noted in the main text, while the overall accuracy gracefully degrades with increasing imbalance, we observe that the accuracy for the minority class (Class 1) conversely improves as its prevalence decreases. For the **minority class**, our confidence and entropy thresholds ensure that only the high-certainty trials of the rare class are added to its memory bank. This creates a highly "pure" and compact GMM, which becomes exceptionally good at identifying these specific, ideal minority class trials. Conversely, the GMM for the **majority class** must account for a much larger and more diverse set of trials, causing its distribution to become more diffuse. This can lead to a decrease in its own classification accuracy as the decision boundary shifts. This finding highlights that our method does not simply fail under imbalance; rather, it adapts by specializing its model for rare events, demonstrating a unique and robust characteristic for real-world applications.

# M DECLARATION OF LARGE LANGUAGE MODEL (LLM) USAGE

The LLM is used only for writing, editing, or formatting purposes and does not impact the core methodology, scientific rigorousness, or originality of the research.