# CONTINUAL LEARNING VIA LEARNING CONTINUAL MEMORY IN VISION TRANSFORMER

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### ABSTRACT

This paper explores continual learning (CL) using Vision Transformer (ViT) in streaming tasks under the challenging exemplar-free class-incremental (ExfCCL) setting. We formulate ExfCCL as a learning problem consisting of two key subsystems: (i) task ID inference for test data, which selects appropriate task-specific head classifiers to accounting for varying class distributions across tasks and streams, and (ii) a dynamic learning-to-grow feature backbone that balances stability and plasticity, mitigating catastrophic forgetting through task synergies. Following the common protocol that the first task can train a ViT sufficiently well as the base model, we address these sub-systems from a continual memory learning perspective. To support task ID inference, we utilize an external memory mechanism that maintains task centroids computed by the base ViT throughout CL. For the feature backbone, we identify optimal placements for internal (parameter) memory to enable a dynamic, task-synergy guided growing feature backbone. We propose a Hierarchical Exploration-Exploitation (HEE) sampling-based neural architecture search (NAS) method that effectively learns task synergies by continually and structurally updating internal memory with four basic operations: reuse, adapt, new, and skip. Our approach, dubbed Continual Hierarchical-Exploration-**Exploitation Memory (CHEEM)**, is evaluated on the challenging Visual Domain Decathlon (VDD) and ImageNet-R benchmarks, demonstrating its effectiveness.

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### 1 INTRODUCTION

Developing continual learning machines is a 033 key objective in Artificial Intelligence (AI), aim-034 ing to replicate human-like adaptability and the ability to learn-to-learn, enabling proficiency in streaming tasks. Despite their advances, stateof-the-art Deep Neural Networks (DNNs) still 037 lack true biological intelligence in the realm of continual learning and are particularly hindered by the critical issue of *catastrophic forgetting* 040 when exposed to streaming tasks in dynamic en-041 vironments (McCloskey & Cohen, 1989; Thrun 042 & Mitchell, 1995). 043

To address catastrophic forgetting, two primary 044 categories of continual learning methods have emerged: exemplar-based methods (Aljundi 046 et al., 2019b; Hayes et al., 2019; Wu et al., 2019) 047 and exemplar-free methods (Kirkpatrick et al., 048 2017; Li et al., 2019; Wang et al., 2022d;c;a). While both have shown promising progress, exemplar-free methods are especially appealing 051 due to their ability to learn new tasks without retaining any data from previous tasks. Further-052



Figure 1: Illustration of the proposed CHEEM.

more, continual learning has evolved from the traditional task-incremental protocol, where task IDs of test data are available during inference, to the more challenging class-incremental protocol, in

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Figure 2: **Top:** The challenging VDD benchmark (Rebuffi et al., 2017a) consisting of 10 tasks of different nature with #training images/#classes significantly varying across different tasks. **Bottom:** Starting from the base task (Tsk1\_ImNet) trained ViT (Dosovitskiy et al., 2021) (e.g., the 12-layer ViT-B model consisting of IN\_B1 to IN\_B12), together with the best performance on VDD in experiments, our CHEEM can learn sensible memory structures: *e.g.*, Tsk3\_SVHN learns to skip both B10 and B11 with both mode complexity and FLOPs reduced. Tsk4\_UCF and Tsk5\_OGlot learn to adapt the first layers to account for the domain shifts. We show the first 5 tasks for clarity (see more in the supplementary). The last two columns show the number of new task-specific parameters and added FLOPs, in comparison with the base model, subject to **R** euse, **A** dapt, **N** ew and **S** kip.

which task IDs are unknown during inference. This paper focuses on exemplar-free class-incremental continual learning (ExfCCL).

080 Recently, the emergence of powerful pretrained Transformer models (Vaswani et al., 2017; Doso-081 vitskiy et al., 2021; Radford et al., 2021) has driven significant interest in ExfCCL using pretrained 082 and frozen Vision Transformers (ViTs) (Dosovitskiy et al., 2021), primarily explored through the 083 lens of prompt-tuning or prefix-tuning (Wang et al., 2022d;c;a; Smith et al., 2023a). However, 084 this approach presents two main drawbacks: (i) A single frozen pretrained Transformer backbone 085 cannot accommodate all streaming tasks of diverse nature, such as those found in the VDD benchmark (Rebuffi et al., 2017a), shown in Fig. 2. While this method maximizes the stability of the 087 feature backbone, it relies on input or prefix prompts to address plasticity by explicitly leveraging the 880 self-attention mechanisms. (ii) Due to the quadratic complexity of ViTs concerning the number of input tokens, incorporating task-specific input prompts or layer-wise prefix prompts into a frozen 089 pretrained Transformer backbone significantly increases computational demands. Continual learning 090 where computational requirements always grow for new tasks by design regardless of task complexity 091 fails to reflect true intelligence. 092

The challenge of structurally and dynamically updating a pretrained Transformer backbone for ExfCCL remains an open problem, as it requires achieving a balance between the backbone's stability and plasticity while enabling dynamic computation and mitigating catastrophic forgetting.

096 Moreover, ExfCCL involves tackling the challenge of designing task head classifiers, which can either explicitly infer task IDs to select task-specific head classifiers (Wang et al., 2022a) or share a 098 growing, common head classifier (Wang et al., 2022d;c; Smith et al., 2023a). The former approach is straightforward and can help in learning task-specific components and enhancing the plasticity of the 099 backbone, but may suffer from low average precision of the task ID inference for certain tasks. In 100 contrast, the latter approach resorts to more sophisticated prefix prompt tuning to induce plasticity 101 in the feature backbone and can create a discrepancy between training, where head segments from 102 previous tasks are masked out in the softmax function of loss computation, and testing, where the 103 entire head is used to infer class labels. This discrepancy can lead to instability when dealing with 104 streaming tasks that involve a varying number of classes among tasks, such as those encountered in 105 the VDD benchmark. 106

**Our aim** in this paper is to study ExfCCL using ViTs. As illustrated in Fig. 1, we formulate it as a problem of learning continual memory in ViT, which has two components: (i) The internal

memory enabling a dynamic learning-to-grow feature backbone that balances stability and plasticity, mitigating catastrophic forgetting through task synergies, in which a new task learns automatically to reuse/adapt modules from previous similar tasks, or to introduce new modules when needed, or to skip some modules when it appears to be an easier task (see the bottom of 2). The internal parameter memory learning presents alternative perspectives to the input and prefix prompting based methods (Wang et al., 2022d;c; Smith et al., 2023a; Wang et al., 2022a). (ii) The external memory enabling task ID inference for test data, for which we adopt a method proposed in (Wang et al., 2022a) for its simplicity.

116 We follow the common protocol in the prior art that the first task (e.g., ImageNet-1k (Russakovsky 117 et al., 2015)) can train a ViT sufficiently well as the base model. To enable a dynamic, learning-to-grow 118 feature backbone starting from the base model, we identify and provide simple yet effective solutions for two key challenges: (i) Which modules in a ViT should be reused, adapted, newly created, or 119 skipped for a new task in ExfCCL? It is computationally impractical, and counterproductive to 120 the stability-plasticity trade-off, to make all ViT components dynamic (as opposed to a fully frozen 121 model). We designate the output projection layer following multi-head self-attention (MHSA) as the 122 task-synergy internal (parameter) memory that will be structurally and dynamically updated. (ii) How 123 can we represent and continually learn this task-synergy internal memory to enable dynamic 124 memory structures across streaming tasks? We propose organizing the memory using a mixture 125 of experts (MoEs) similar in spirit to (Riquelme et al., 2021), as depicted in Fig. 1 and illustrated 126 through the "task-factorized" visualization in Fig. 2. To learn to select the optimal synergy operation 127 from the four choices (reuse, adapt, new, and skip), we introduce an effective hierarchical 128 exploration-exploitation (HEE) sampling-based neural architecture search (NAS) method. This 129 approach is inspired by the task-incremental learn-to-grow method (Li et al., 2019). Our proposed method is termed CHEEM (Continual Hierarchical-Exploration-Exploitation Memory). 130

131 Our Contributions. This paper makes three main contributions to the field of exemplar-free 132 class-incremental continual learning (ExfCCL) using ViT. (i) It presents a hierarchical task-synergy 133 exploration-exploitation sampling based NAS method for learning task-aware dynamic models 134 continually with respect to four operations: Skip, Reuse, Adapt, and New to mitigate catastrophic 135 forgetting. (ii) It identifies a "sweet spot" in ViT as the task-synergy internal (parameter) memory, i.e., the output projection layers after MHSA in ViT. It also presents a new usage for the class-token 136 CLS in ViT as the internal memory updating guidance, in addition to leveraging it in maintaining the 137 external (task-centroid) memory for task ID inference on the fly. (iii) It is the first work, to the best of 138 our knowledge, to evaluate continual learning with ViTs on the large-scale, diverse and imbalanced 139 VDD benchmark (Rebuffi et al., 2017a), with better performance than the prior art. 140

### 2 Approach

## 143 2.1 PROBLEM FORMULATION OF CHEEM IN EXFCCL

We start with a vanilla *D*-layer ViT model (e.g., the 12-layer ViT-Base) (Dosovitskiy et al., 2021). The left of Fig. 1 shows a ViT block. Denote by  $x_{L,d}$  an input sequence consisting of *L* tokens encoded in a *d*-dimensional space. In ViTs, the first token is the so-called class-token, CLS. The remaining L - 1 tokens are formed by patchifying an input image and then embedding patches, together with additive positional encoding. A ViT block is defined by,

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$$z_{L,d} = x_{L,d} + \operatorname{Proj}(\operatorname{MHSA}(\operatorname{LN}_1(x_{L,d}))), \tag{1}$$

$$y_{L,d} = z_{L,d} + \text{FFN}(\text{LN}_2(z_{L,d})))), \qquad (2)$$

where LN( $\cdot$ ) represents the layer normalization (Ba et al., 2016), and Proj( $\cdot$ ) is a linear transformation fusing the multi-head outputs from MHSA module. The FFN is often implemented by a multi-layer perceptron (MLP) with a feature expansion layer MLP<sup>u</sup> and a feature reduction layer MLP<sup>d</sup> with a nonlinear activation function (such as the GELU (Hendrycks & Gimpel, 2016)) in the between.

Denote by  $\mathcal{T} = \{T_1, \dots, T_t, \dots, T_N\}$  a stream of tasks in continual learning, where each task  $T_t$ consists of a training set  $D_t^{train}$  and a testing set  $D_t^{test}$ . We make no restrictive assumptions regarding the nature, order, or number of classes in streaming tasks, either per task or in total. For example, there are 9 diverse, streaming tasks in the VDD benchmark (2).

160 Denote by  $(f_1, C_1)$  the ViT (Dosovitskiy et al., 2021) base model (e.g., the 12-layer ViT-Base) trained 161 on the first task  $T_1$  (e.g., ImageNet-1k (Russakovsky et al., 2015)), where  $f_1$  is the backbone and  $C_1$ the head classifier. Denote by  $(\mathcal{F}_t, \mathcal{C}_t)$  the sequentially and continually learned model after task  $T_t$  162 163 (for  $t \ge 1$ ).  $\mathcal{F}_t$  is the super ViT backbone structurally and dynamically updated from the base model 164  $f_1 = \mathcal{F}_1$ , and  $\mathcal{C}_t = \{C_1, \dots, C_t\}$  consisting of task-specific head classifiers each of which is trained 164 from scratch. Let  $\Theta_t = \mathcal{F}_t \setminus \mathcal{F}_{t-1}$  be task-specific backbone parameters, which we term **the internal** 165 **parameter memory** in ExfCCL to exploit task synergies. We note that ExfCCL requires no use of 166 exemplar data of previous tasks in any forms in learning ( $\Theta_t, C_t$ ) for task  $T_t$ .

In inference, since the task IDs of test data are unknown. For a test sample x, we will need to infer its task ID on the fly. Following the prior art (Wang et al., 2022d;c; Smith et al., 2023a; Wang et al., 2022a), we use the base model  $f_1(\cdot)$  as the query function q(), and use q(x) to retrieve the task ID from **the external memory** for which we adopt the method proposed in (Wang et al., 2022a) for its simplicity. With task ID available (provided in training or inferred in testing), we can allocate the task-specific backbone  $f_t \subset \mathcal{F}_N$  for task  $T_t$ . The task-specific model is then specified by  $(f_t, C_t)$ .

174 2.2 CONSTRUCTING THE EXTERNAL MEMORY

175 We choose to explicitly infer task IDs for test data (see Appendix A for the analyses). We adopt the 176 method proposed in S-Prompts (Wang et al., 2022a). For a task t, we leverage K-mean clustering of 177 the CLS tokens of its training images computed by the query function  $q(\cdot)$  (i.e., the base model  $f_0$ ). Denote by  $Z_t = \{z_t^1, \dots, z_t^K\}$  the clustered task centroids for task  $T_t$ , where for simplicity we use the same K = 5 across tasks. We have the external memory,  $\Psi = \bigcup_{t=1}^N Z_t$  after training. In inference, 178 179 for a testing sample x, we first compute its CLS token using the same query function q(x), denoted 180 by z. The task ID is then inferred via K-NN retrieval,  $KNN(z, \Psi)$ , either by retrieving the class ID 181 of the Top-1 NN centroid in the external memory  $\Psi$ , or by majority voting of the class ID from the 182 K-NN centroids. 183

We note that the such constructed external memory does not break the exemplar-free protocol since
we do not use exemplars in any forms from previous tasks. We also note that we focus on the
learning of the internal parameter memory. The decoupled design between the external memory
and the internal memory will enable us to integrate and/or develop more advanced task ID inference
approaches in future work, while potentially promoting our proposed CHEEM in the field of ExfCCL.

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### 2.3 IDENTIFYING THE TASK-SYNERGY INTERNAL MEMORY

The proposed identification process is straightforward. Without introducing any modules handling
 forgetting, we compare both the task-to-task forward transferrability and the sequential forgetting
 for different components in a ViT block. Our intuition is that a desirable component for placing
 the task-synergy parameter memory must enable strong transferrability with manageable
 forgetting, while being lightweight to account for the trade-off between stability and plasticity.

To that end, we use the VDD benchmark (Rebuffi T 196 et al., 2017a) (see Fig. 2). We first train a ViT-197 Base (Dosovitskiy et al., 2021) on the first task, ImageNet (Russakovsky et al., 2015), as the base model 199  $f_1(\cdot)$ . To measure the task-to-task transferability, we 200 *individually fine-tune*  $f_1$  in a task-to-task transfer 201 learning manner for the remaining 9 streaming tasks. 202 Let  $f_{t|1}$  be the backbone fine-tuned for task  $T_t$  (for 203  $t \geq 1$ ), and  $C_t$  the head classifier trained from scratch. 204 The average Top-1 accuracy is:

$$A\mathbf{A} = \frac{1}{N} \sum_{t=1}^{N} Acc(T_t; f_{t|1}, C_t)$$
(3)

Table 1: Results of identifying the optimal
placement of our CHEEM in ViT by testing
1 components (Eqns. 1 and 2).

Index	Finetuned Component	AA (Eqn. 3)	$A\mathbb{F}$ (Eqn. 4)
1	$LN_1 + LN_2$	81.76	21.24
2	FFN	84.20	44.76
3	MLP <sup>d</sup>	83.66	37.99
4	$LN_2$	80.04	16.35
5	$MHSA + LN_1$	85.26	54.38
6	LN <sub>1</sub>	81.18	19.04
7	Query	81.57	19.69
8	Key	81.56	19.19
9	Query+Key	81.49	31.10
10	Value	84.99	37.58
11	Projection (CHEEM)	85.11	30.50
Classif	ier w/ Frozen Backbone	70.78	-

where Acc() uses the Top-1 classification accuracy.

To measure the sequential forgetting, we *continually fine-tune* the backbone started from  $f_1$  on the 9 tasks in a randomly sampled and fixed streaming order (as shown in Fig. 2). Let  $f_{1:t}$  be the backbone trained sequentially and continually after task  $T_t$  and  $C_t$  is its head classifier. The average forgetting (Chaudhry et al., 2018) on the first N - 1 streaming tasks is,

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$$A\mathbb{F} = \frac{1}{N-1} \sum_{t=1}^{N-1} \left( \max_{j \in [t,N]} a_{j,t} - a_{N,t} \right), \quad (4)$$

where  $a_{j,t} = \operatorname{Acc}(T_t; f_{1:j}, C_t)$ .

216 As shown in Table 1, we compare 11 components or composite components in ViT. Consider the 217 strong forward transfer ability, manageable forgetting, maintaining simplicity and for less invasive 218 implementation in practice, we select the Projection layer after the MHSA as the task-synergy 219 internal (parameter) memory (Fig. 1) to realize our proposed CHEEM for ExfCCL. We note that 220 the last row of Table 1 shows the result of a conventional transfer learning setting in which only the head classifier is trained with the backbone frozen, which clearly shows that one frozen backbone 221 can not fit all streaming tasks, as aforementioned and entailing dynamic updating of the backbone in 222 continual learning. 223

2.4 LEARNING THE TASK-SYNERGY INTERNAL MEMORY

226 The proposed internal memory of our CHEEM is represented by a MoEs. Starting with the base ViT 227 model  $f_1$ , the internal memory at the *l*-th layer in ViT consists of a single expert defined by a tuple, 228

$$\mathbf{E}_{l}^{(1,)} = (\theta_{l}^{(1,)}, \mu_{l}^{1}), \tag{5}$$

229 where the subscript represents the layer index and the list-based superscript shows which task(s) 230 use this expert.  $\theta_l^{(1,)}$  are the parameters of the projection layer and  $\mu_l^1 \in \mathbb{R}^d$  is the associated mean 231 class-token (CLS) pooled from the training dataset after the model is trained, which is task specific 232 (as indicated by the superscript). For example, if an expert is reused by another task (say, 3) in 233 continual learning, we will have  $\mathbf{E}_{l}^{(1,3,)} = (\theta_{l}^{(1,3,)}, \mu_{l}^{1}, \mu_{l}^{3})$ . 234

As shown in Fig. 3, for a new task t, learning to update CHEEM consists of: i) the Supernet 235 construction, ii) the Supernet training, and iii) the target network selection and finetuning. 236

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2.4.1SUPERNET CONSTRUCTION VIA Reuse, Adapt, New AND Skip

For clarity, we consider a single layer l for a new task, and the current memory consists of two experts,  $\{E_{i}^{(1,)}, E_{i}^{(2,)}\}$  (Fig. 3, left). We utilize four operations in the Supernet construction:

• R euse the projection layer from a previous (similar) task for a new task.

A dapt by adding a new lightweight layer on top of the projection layer of a previous task, implemented by a MLP with one squeezing hidden layer.

- N ew by adding a new projection layer, which enables the model to handle dissimilar situations.
- S kip the entire MHSA block, which encourages the adaptivity accounting for the diverse nature of tasks. iii) CHEEM

The Supernet is constructed by reusing 249 and adapting each existing expert at 250 layer l, and adding a new and a skip 251 expert (the bottom of Fig. 3). The newly 252 added adapt MLPs and new projection 253 layers will be trained from scratch using 254 the data of a new task only. The right-255 top of Fig. 3 shows the Adapt opera-256 tion on top of  $E_l^{(2,)}$  is learned and added, 257  $\mathbf{E}_{l}^{(3,)} = (\theta_{l}^{(3,)}, \mu_{l}^{3})$  where  $\theta_{l}^{(3,)}$  represents 258 parameters of the adapt MLPs learned 259 for the task 3, and  $\mu_l^3$  is the mean CLS to-260 ken pooled for the task 3. The expert  $E_{I}^{(2,)}$ 



Figure 3: Illustration of CHEEM learning via NAS.

is updated to  $E_l^{(2,3,)} = (\theta_l^{(2,3,)}, \mu_l^2)$  indicating its weights are shared with task 3. We provide implementation details for Adapt in the Appendix D.5. 262 263

#### 2.4.2 SUPERNET TRAINING VIA THE PROPOSED HEE SAMPLING-BASED NAS 265

266 To train the Supernet constructed for a new task t, we build on the SPOS method (Guo et al., 2020) 267 due to its efficiency. The basic idea of SPOS is to train a single-path sub-network from the Supernet by sampling an expert at every layer in each mini-batch of training. One key aspect is the sampling 268 strategy. The vanilla SPOS method uses uniform sampling (i.e., the *pure exploration* (PE) strategy, 269 Fig. 4 left). We propose an exploitation strategy (Fig. 4 right), which utilizes a hierarchical sampling



Figure 4: Illustration of the proposed hierarchical task-synergy exploration-exploitation (HEE) sampling based NAS. It integrates the vanilla exploration strategy (left) and the proposed exploitation strategy (right) with an epoch-wise scheduling.

method that forms the categorical distribution over the operations in the search space explicitly based on task synergies computed based on the pooled task-specific CLS tokens.

As illustrated in the right of Fig. 4, at each layer l in the Supernet, for a new task t, our proposed 3-level HEE sampling is realized by:

- The epoch-level sampling: At the beginning of an epoch in the Supernet training, we choose the pure exploration strategy with a probability of  $\epsilon_1$  (e.g., 0.3), and the exploitation strategy with a probability of  $1 - \epsilon_1$ .
- The task-level sampling: There are t-1 previous tasks, some of which may use Skip at the *l*-th layer and will not be used in sampling. We introduce an auxiliary task to handle sampling New and Skip for the current task t. The task-level sampling is based on a categorical distribution  $(\psi_1, \dots, \psi_i, \dots, \psi_{I-1}, \psi_I)$ , which is computed by the Softmax function over the similarity scores defined below, where I < t.
- The operation-level sampling: With a previous task i sampled with the probability  $\psi_i$ , we sample the Reuse and Adapt operation using a Bernoulli distribution  $(\rho_i, 1 - \rho_i)$ , where  $\rho_i$  is the success rate computed by the Sigmoid function of the task similarity score (defined below).

296 The Task Similarity Score. Consider one expert  $E_l^{(i,j,j)}$  at the *l*-th layer which is shared by two 297 previous tasks i and j with their mean CLS tokens  $\mu_l^i$  and  $\mu_l^j$  respectively, we compute the mean CLS 298 tokens using the models for task i and j on the training dataset  $D_t^{train}$  of the current task t,  $\mu_l^{i \to t}$  and  $\mu_i^{j \to t}$ . The task similarity between task *i* and *t* is computed by, 300

$$S_l^{i,t} = \operatorname{NormCosine}(\mu_l^i, \mu_l^{i \to t}), \tag{6}$$

where NormCosine( $\cdot, \cdot$ ) is the Normalized Cosine Similarity, which is calculated by scaling the 302 Cosine Similarity score between -1 and 1 using the minimum and the maximum Cosine Similarity 303 scores from all the experts in all the MHSA blocks of the ViT. This normalization is necessary to 304 increase the difference in magnitudes of the similarities between tasks, which results in better Expert 305 sampling distributions during the sampling process in our experiments. 306

**The Auxiliary Task.** For a new task t, to handle the New and Skip experts at each layer l for which 307 we do not have direct similarity scores. Instead, we introduce an auxiliary task, Aux (see the right of 308 Fig. 4) which gives equally-likely chance to select New or Skip expert. For the Aux task itself, the 309 similarity score between it and task t is defined by, 310

 $S_{l}^{aux,t} = -\max_{i=1}^{t-1} S_{l}^{i,t},$ (7)

312 which intuitively means we probabilistically resort to the New operation or the Skip operation when 313 other experts turn out not "helpful" for the task t.

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### 2.4.3 TARGET NETWORK SELECTION AND FINETUNING

316 After the Supernet is trained, we adopt the same evolutionary search used in the SPOS method (Guo 317 et al., 2020) based on the proposed HEE sampling strategy with a different epoch sampling probability 318  $\epsilon_2$  ( $\epsilon_2 > \epsilon_1$ , e.g.,  $\epsilon_2 = 0.5$ , to encourage more exploration during the evolutionary search). The 319 evolutionary search is performed on the validation set to select the path which gives the best validation 320 accuracy. After the target network for a new task is selected, we retrain the newly added layers by 321 the New and Adapt operations from scratch (random initialization), rather than keeping the weights 322 from the Supernet training. This is based on the observations in network pruning that it is the neural 323 architecture topology that matters and that the warm-up weights may not need to be preserved to ensure good performance on the target dataset (Liu et al., 2019b).

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Metho	od	C100 36k/100	SVHN 42.4k/10	UCF 6.8k/101	OGlt 16.1k/1623	GTSR 28.2k/43	DPed 21.2k/2	Flwr 0.92k/102	Airc. 3.0k/100	DTD 1.7k/47	AA (Eqn. 8)	$A\mathbb{F}$ (Eqn. 4)	$ _{\text{TCL }A\mathbb{A}}$	TCL $A\mathbb{F}$
L2P+ DualF COD/	+ Prompt A-Prompt	79.16 82.92 88.06	0.62 15.27 18.09	5.40 12.19 12.16	14.05 33.71 53.95	62.82 80.12 95.65	4.09 7.65 19.42	2.97 3.17 6.83	2.73 3.47 6.34	2.98 3.23 5.62	$\begin{array}{c} 19.42\pm 0.09\\ 26.86\pm 0.40\\ 34.01\pm 0.99\end{array}$	$\begin{array}{c} 5.49 \pm 0.37 \\ 3.54 \pm 0.27 \\ 8.0 \pm 0.72 \end{array}$	$ \begin{vmatrix} 68.68 \pm 0.67 \\ 76.57 \pm 0.23 \\ 75.83 \pm 0.60 \end{vmatrix} $	$\begin{array}{c} 10.25\pm0.77\\ 2.57\pm0.26\\ 6.25\pm0.60\end{array}$
S-Pro	ompts	87.38	88.53	64.05	72.17	98.53	99.65	96.63	45.49	58.07	$78.95\pm0.07$	$0.32\pm0.32$	79.71 ± 0.08	$0.0\pm0.0$
EWC L2 Re Exper	egularization rience Replay	79.15 82.59 56.68	85.62 65.57 6.23	47.03 51.57 33.45	64.57 26.83 74.33	90.65 95.62 7.00	54.56 98.50 0.02	55.26 83.04 64.25	34.87 33.80 27.03	54.49 51.67 37.55	$\begin{array}{c} 62.91 \pm 0.81 \\ 65.47 \pm 0.33 \\ 34.06 \pm 0.69 \end{array}$	$\begin{array}{c} 19.82\pm 0.69\\ 7.23\pm 0.51\\ 44.89\pm 0.72\end{array}$	$\begin{array}{ } 75.00 \pm 0.67 \\ 69.63 \pm 0.17 \\ 54.55 \pm 2.67 \end{array}$	$\begin{array}{c} 6.33 \pm 0.30 \\ 3.00 \pm 0.47 \\ 22.67 \pm 3.01 \end{array}$
Our C	CHEEM	88.56	95.63	75.05	83.81	99.15	99.64	90.92	55.53	56.42	$\textbf{82.74} \pm 0.54$	$0.33\pm0.00$	<b>84.65</b> ± 0.33	$0.0\pm0.0$

Table 2: Results on the VDD benchmark (Rebuffi et al., 2017a) using ViT-B/8 (Dosovitskiy et al., 324 2021) over 3 different seeds. The last two columns show the performance under the task-incremental 325 continual learning (TCL) setting

#### **EXPERIMENTS** 3

335 Data: We use the VDD benchmark (Rebuffi et al., 2017a) and the Split ImageNet-R(etention) 336 benchmark introduced in Wang et al. (2022c), derived from (Hendrycks et al., 2021). The VDD 337 benchmark (Fig. 2) consists of 10 tasks with significantly varying distributions of classes per task. 338 The vanilla ImageNet-R dataset consists of 200 classes and 30k images in total. The Split ImageNet-R 339 benchmark is constructed by randomly splitting the ImageNet-R dataset into 10 tasks each of which 340 has 20 classes. To test the effects of imbalance class distributions in streaming tasks, we construct 341 another Split ImageNet-R benchmark consisting of 6 tasks with imbalance number of classes (5, 342 10, 15, 20, 50, 100) randomly sampled from the 200 total classes without replacement for each task. 343 More details are provided in Appendix. E.

344 Baselines of ExfCCL. We compare with S-Prompts (Wang et al., 2022a), Learning to Prompt (L2P) 345 Wang et al. (2022d), DualPrompt Wang et al. (2022c) and CODA-Prompt Smith et al. (2023a). On 346 the VDD benchmark, we also test two regularization based methods, the L2 Parameter Regularization 347 (Smith et al., 2023b) and the EWC (Kirkpatrick et al., 2017), and a strong baseline of Experience 348 Replay (with iCARL (Rebuffi et al., 2017b) for buffer updates) using the total buffer size 20k and 10 349 exemplars per class. For EWC, L2 and iCarl, we freeze the backbone model and only keep the output 350 projection layers (where CHEEM is placed) in the MHSA blocks trainable for better understanding 351 the advantages of structurally updating them in our CHEEM. More details are in Appendix F and G.

Metric: In addition to average forgetting (Eqn. 4), we compare average accuracy in ExfCCL setting,  $A\mathbb{A} = \frac{1}{N} \sum_{i=1}^{N} \operatorname{Acc}(T_i; f_{1:N}, C_t).$ 

(8)

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3.1 RESULTS ON THE VDD BENCHMARK

358 Table 2 shows the results. We use the ImageNet-1k (the 1st task in the VDD) trained ViT-B/8 as the 359 base model. For fair comparisons with prompting based baselines, we evaluate average accuracy 360 and forgetting on the remaining 9 tasks in the VDD. Our proposed CHEEM obtains significantly 361 better performance than all the baselines. We analyze the results as follows. 362

363 i) The Advantage of Task-Aware Dynamic Backbone Over Frozen Backbone: CHEEM vs S-Prompts. CHEEM adopts the same task ID inference method (i.e., the external memory) proposed 364 by S-Prompts (Wang et al., 2022a). The improvement by CHEEM with above 3% absolute average accuracy increase clearly shows the advantage of our proposed internal parameter memory for 366 maintaining task-aware dynamic backbones, against the method of prepending retrieved task-specific 367 prompts in S-Prompts. Table 2 also shows a potential for harnessing prompt-based methods in 368 CHEEM. S-Prompts performs better on tasks that are similar to the first ImageNet task and have less 369 training data such as Flwr (918 training images) and DTD (1692 training images). 370

ii) Explicit Task ID Inference: With vs Without. The three baselines, L2P (Wang et al., 2022d), 371 DualPrompt (Wang et al., 2022c) and CODA-Prompt (Smith et al., 2023a), use a shared head 372 classifier in inference, which, as aforementioned in the introduction, suffers from the discrepancy 373 between training and testing. Due to the significant imbalance class distributions in the VDD, their 374 average accuracy undergo catastrophic drops (19.42% by L2P, 26.86% by DualPrompt and 34.01% 375 by CODA-Prompt, vs 78.95% by S-Prompts and 82.74% by our CHEEM). 376

To understand the effects of head classifiers better, we also compare the performance when task IDs 377 are provided in inference (i.e., Task-incremental CL, TCL), so the three methods can use task-specific head segments of the shared classifier, and both S-Prompts and our CHEEM do not need the external task-centroid memory. The last two columns of Table 2 show the results. *We have three observations:*

The performance of L2P, DualPrompt and CODA-Prompt are drastically boosted (e.g., from 34.01% to 75.83% by CODA-Prompt), showing the importance of explicitly inference task IDs for imbalance class distributions of streaming tasks in continual learning. Our CHEEM under CCL is still significantly better than the three methods under TCL (by more than 6%), which reinforces the importance of the task-aware dynamic backbone learned via our CHEEM.

- The performance difference between CCL and TCL by our CHEEM is small, around 2%, showing that the task ID inference method (Wang et al., 2022a) is effective in handling the imbalance class distributions in the VDD benchmark.
- In terms of average forgetting under CCL and TCL, we should compare the ratio between average forgetting and average accuracy, rather than the average forgetting rates in isolation, for which the first three methods undergo severer forgetting under CCL as intuitively expected. Our CHEEM does not have forgetting under TCL.

392 iii) Stability vs Plasticity of the Backbone. To further show the advantage of our CHEEM learning to update the feature backbone from the base model, we compare with EWC (Kirkpatrick et al., 2017), L2 Regularization (Smith et al., 2023b) and Experience Replay (Rebuffi et al., 2017b). The 394 395 three methods regularize the weights, including the shared head classifier, in learning new tasks using different formulations. Comparing with L2P, DualPromt and CODA-Prompt, under CCL, the 396 regularization based methods work better, showing the negative effects of the discrepancy of handling 397 the shared head in training and testing by the three prompting based methods, as well as a potential 398 of integrating them. Comparing with S-Prompts, the plasticity of updating the entire backbone with 399 regularization is less effective than the plasticity introduced by prompts while keeping the backbone 400 frozen in S-Prompts. Comparing with our CHEEM, the three regularization based methods suffer 401 from significant forgetting, highlighting the balanced stability and plasticity via our CHEEM. 402

403	Table 3: Results on two constructed Split ImageNet-R benchmarks, averaged across 3 different task
104	orders. The base model is ImageNet-1k trained ViT-B/16 sourced from (Wightman, 2019).

er task)
TCL $A\mathbb{F}$
$0.48 \pm 0.02$
$0.29 \pm 0.19$
$0.45\pm0.10$
$0.0 \pm 0.0$
- 94 -4

### 410 3.2 RESULTS ON THE SPLIT IMAGENET-R BENCHMARK

The ImageNet-R dataset is created to challenge models trained using ImageNet. So, by design, the external memory of our CHEEM that is based on ImageNet-1k trained base model will not work well. Table 3 shows the results which we analyze as follows:

i) Randomly Assigned and *Imbalanced* Classes in Streaming Task Challenge All of ExfCCL
 Methods We Test. Under CCL, the three prompting based methods suffer from catastrophic drop of performance from balanced to imbalanced settings (e.g., from 76.48 ± 0.25% to 67.66 ± 3.09% by CODA-Prompt, see Fig. 5 and analyses in Appendix A ). Our CHEEM is on-par with DualPrompt and CODA-Prompt. Our CHEEM is also stable from balanced to imbalanced scenarios. Under TCL, all methods obtain significant performance boost, and our CHEEM is better than all others. Similarly, we envision that leveraging the dynamically learned backbone by our CHEEM in constructing the external memory will be a promising direction to be studied in future work.

422 ii) Randomly Assigned Yet Balanced Classes in Streaming Tasks Challenge the Task-Centroid 423 based Task ID Inference. On the one hand, for streaming tasks with balanced but randomly sampled 424 classes per task (without replacement), our CHEEM under CCL has the worst performance (64.72% 425 vs 76.48% by CODA-Prompt), which was caused by the low average precision of task ID inference 426 (see Fig. 6 and analyses in Appendix B). Our CHEEM under TCL obtains the best performance 427 (92.47%), which shows that the learned task-aware backbone is expressive. Overall, task centroids 428 computed using the CLS tokens in the base model are not able to distinguish tasks from each other with high accuracy. One potential solution is to leverage the dynamically learned backbone by our 429 CHEEM in constructing the external memory, considering its superior performance under TCL, at 430 the expense of more costly task ID inference. On the other hand, although it is interesting to test 431 continual learning approaches using the Split ImageNet-R benchmark, the random composition of classes in a task is not natural in comparison with scenarios in natural human learning. Unlike
 the Split ImageNet-R, the VDD benchmark may suit continual learning better from perspective the
 perspective of real-world scenarios, for which our CHEEM works the best.

### 435 436

### 4 VISUALIZATION AND ABLATION STUDIES

437 Due to space limit, we present visualizations of the learned CHEEM (examples like Fig. 2) in 438 Appendix C. We also conduct ablation studies including: (i) The proposed HEE sampling significantly 439 outperforms pure exploration (PE) sampling in Appendix D.1. (ii) The proposed HEE-empowered 440 SPOS NAS significantly outperforms the DARTS (Liu et al., 2019a) based NAS used in the learn-to-441 grow method (Li et al., 2019) in Appendix D.2. (iii) The proposed internal memory learning method 442 outperforms three state-of-the-art methods: SupSup (Wortsman et al., 2020), EFT (Verma et al., 2021) 443 and LL (Ge et al., 2023) under the task-to-task transfer learning setting in Appendix D.3. And, more 444 are in Appendix D.3, D.4 and D.6.

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### 5 RELATED WORK

447 Experience Replay Based approaches aim to retain some exemplars, in the form of either raw data or 448 latent features, from the previous tasks and replay them to the model along with the data from a new 449 task (Aljundi et al., 2019b; Rebuffi et al., 2017b; Aljundi et al., 2019a; Balaji et al., 2020; Bang et al., 450 2021; Chaudhry et al., 2021; Pham et al., 2021), or generative replay methods (Shin et al., 2017; Cong 451 et al., 2020) which replay exemplars sampled from the learned generators along with the data from 452 the current task. For exemplar-free continual learning, Regularization-based Approaches explicitly prevent model parameters from deviating too far from their stable values learned on previous tasks 453 when learning a new task (Aljundi et al., 2018; 2019c; Douillard et al., 2020; Nguyen et al., 2018; 454 Kirkpatrick et al., 2017; Li & Hoiem, 2018; Zenke et al., 2017; Schwarz et al., 2018). 455

456 Dynamic Models aim to use different parameters for each task to eliminate the use of stored exemplars. 457 Dynamically Expandable Network (Yoon et al., 2018) adds neurons to a network based on learned sparsity constraints and heuristic loss thresholds. PathNet (Fernando et al., 2017) and RPSNet 458 (Rajasegaran et al., 2019) learn task-specific submodules or paths. Progressive Neural Networks (Rusu 459 et al., 2016) learn a new network per task and adds lateral connections to the previous tasks' networks. 460 The L2G (Li et al., 2019) uses Differentiable Architecture Search (DARTS) (Liu et al., 2019a) to 461 determine if a layer can be reused, adapted, or renewed for a task, which is tested for ConvNets 462 and the learning-to-grow operations are applied uniformly at each layer in a ConvNet. Our method 463 is motivated by the L2G method, but with significant differences. NAS has also been explored by 464 (Gao et al., 2023a) for continual learning on small scale tasks. Approaches that learn task-specific 465 components on top of a backbone include (Ge et al., 2023; Verma et al., 2021; Wortsman et al., 2020; 466 Abati et al., 2020). 467

Recently, there has been increasing interest in continual learning using Vision Transformers (Wang et al., 2022d;c; Xue et al., 2022; Ermis et al., 2022; Douillard et al., 2022; Pelosin et al., 2022; Yu et al., 2021; Li et al., 2022; Iscen et al., 2022; Wang et al., 2022a;b; Mohamed et al., 2023; Gao et al., 2023b; Zhou et al., 2023). *Prompt Based approaches* learn external parameters appended to the data tokens that encode task-specific information useful for classification (Wang et al., 2022d;a; Douillard et al., 2022; Smith et al., 2023a; Jung et al., 2023; Tang et al., 2023; Zhou et al., 2024). Our proposed method is complementary to prompting-based based approaches.

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### 6 CONCLUSION

476 This paper presents a method of transforming Vision Transformers (ViTs) for exemplar-free class-477 incremental continual learning (ExfCCL), dubbed CHEEM (Continual Hierarchical-Exploration-478 Exploitation Memory). Our CHEEM consists of the external (task-centroid) memory and the internal 479 (parameter) memory. The former is for task ID inference for test data based on clustered task 480 centroids in training. The latter is realized by a proposed Hierarchical-Exploration-Exploitation 481 (HEE) sampling based neural architecture search algorithm. The external and internal memory are 482 maintained in a decoupled way. Our CHEEM is tested on two challenging benchmarks, the VDD 483 benchmark and the continual ImageNet-R benchmark. It obtains state-of-the-art performance on the VDD outperforming the prior art by a large margin, with sensible CHEEM strutures continually 484 learned. It obtains on-par performance on the imbalanced ImageNet-R benchmark, while performs 485 worse on the balanced one, for which we analyze the reason thoroughly due to the external memory.

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918 919	Appendix
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922	In this Appendix, we elaborate on the following aspects that are not presented in the submission due
923 924	to the space limit:
925	• Section A – Analyses of head classifier design choices in continual learning.
926	• Section B – Analysis of the discriminative capacity of centroids for task ID inference
927 928 929	• Section C – More examples of learned CHEEM by our proposed hierarchical exploration- exploitation (HEE) sampling scheme and by the vanilla pure exploration (PE) sampling scheme.
930	Section D - Ablation Studies:
931 932	<ul> <li>Section D.1 – Comparing Pure Exploration vs. our propoed Hierarchical Exploration- Exploitation sampling scheme for SPOS NAS</li> </ul>
933	- Section D.2 - Comparing proposed HEE empowered SPOS NAS with DARTS: We
934 935	compare with DARTS, which has been used by Learn-to-Grow and show that our proposed method outperforms L2G with DARTS.
936	– Section D.3 – Can CHEEM be used for task-to-task transfer?
937 938	- Section D.4 - Can we use other components in ViTs as CHEEM?: We compare with the Query/Key/Value layer and the FFN layer, and verify the effectiveness of the proposed
939	identification in the main paper.
940	- Section D.5 - How is the Adapt operation implemented?: We elaborate two implementa-
942	<ul> <li>Section D.6 - Effects of task orders</li> </ul>
943	• Section F Details of the two honohmorks facted in the experimental the Visual Domain
944 945	Decathlon (VDD) (Rebuffi et al., 2017a) benchmark and the ImageNet-R (Hendrycks et al., 2021) benchmark.
946 947	• Section F – The base model and its training details: the Vision Transformer (ViT) model specification (ViT-B/8) and how it is initially training on the ImageNet in our experiments.
948 949	• Section G – Experimental settings and training hyperparameters in our implementation on
950	the VDD benchmark and the 5-dataset benchmark.
951	• Section H - Details of Modifying SupSup, EFT and LL on the VDD Benchmark to work with
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## A TASK-SPECIFIC HEAD SELECTION VIA TASK ID INFERENCE VS SHARING A GROWING, COMMON TASK HEAD

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As aforementioned in the introduction of main text, explicitly inferring task IDs from the external memory for test data is to select the task head classifiers as done in (Wang et al., 2022a), while also enabling selecting task-specific feature backbones (exploited in our CHEEM). An alternative approach is to share a growing, common task head as done in (Wang et al., 2022d;c; Smith et al., 2023a). The former can suffer from low average precision, while for the latter we observe serious instability caused by imbalanced classes in stream tasks due to the discrepancy in training and testing (see Table 2 and Table 3).

983 To show the instability, let  $C = (z_1, z_2, \cdots, z_K)$  be the logits output of the common head. During 984 training, the task ID for each  $z_k \in C$  is known, and the logits of previous tasks are masked out 985 (using  $-\infty$ ) before computing the softmax (i.e., task-specific heads are used in training). During 986 testing, the label for a testing sample is predicated by  $\arg \max_{k \in [1,K]} z_k$ , across the entire head. This 987 discrepancy between training and testing imposes a very strong assumption of the stability of logits in training and testing, which entails that the task-specific head segment for a testing example will 988 underlyingly resemble the 1-hot vector, such that it can hold across the entire head. Although (Wang 989 et al., 2022d;c; Smith et al., 2023a) show strong performance using the same number of classes per 990 task (20) in ImageNet-R (Hendrycks et al., 2021), we observe that slightly varying the number of 991 classes per task, while keeping everything else the same, can lead to around 10% drop of performance 992 in ImageNet-R. For more challenging task-class distributions as in the VDD (Fig. 2), (Wang et al., 993 2022d;c; Smith et al., 2023a) have a catastrophic drop of performance. 994

To analyze this further, we probe the model after the training on the final task is complete. For each task, we first make predictions using the task specific part of the head (i.e., the task-incremental setting) and calculate the entropy of predicted probabilities of all the samples with the task-specific head. Then, we make predictions with the full head (i.e., the class-incremental setting), including all the classes in the previous tasks, and track samples for which the logit with the maximum values changes to one of the classes from the previous tasks, which we refer to as **switched samples**.

As shown in Fig. 5, we observe that the entropy for the switched samples is consistently higher than those of the un-switched samples. Furthermore, the variance of the the entropy consistently goes down as the tasks progress, which indicates that for later tasks, only the predictions that are highly confident remain unswitched. However, the entropy for the switched samples shows a large variance. This indicates that sharp predictions are not a sufficient condition to avoid switching.



Figure 5: Mean entropy for the switched and unswitched samples from each task on the Split ImageNet-R benchmarks using CODA-Prompt. *Left:* Imbalanced ImageNet-R with varying number of classes (5,10,15,20, 50, 100) per task and 6 tasks in total. *Right:* Balanced ImageNet-R with same number (20) of classes per task and 10 tasks in total.

## 1026<br/>1027<br/>1028BTHE PROS AND CONS OF BASE MODEL COMPUTED TASK CENTROIDS AS<br/>THE EXTERNAL MEMORY FOR TASK ID INFERENCE

To understand effects of the external task-centroid memory we adopted from S-Prompts (Wang et al., 2022a), we analyze the separability of the K-Mean clusters of different tasks on the VDD (Rebuffi et al., 2017a) (see results in Table 2) and Balanced ImageNet-R benchmarks (see results in Table 3) by visualizing them using t-SNE (van der Maaten & Hinton, 2008) in Fig. 6.



VDD

### **Balanced ImageNet-R**

Figure 6: The t-SNE visualization of task centroids using the frozen base model CLS tokens of training examples of each task. We run K-Mean on the VDD benchmark with K = 5 per task. We use the mean CLS token per class (20 centroids per task) on the balanced Imagenet-R benchmark, which we found works better.

For our proposed CHEEM, we can observe that the external task-centroid memory is effective on 1057 the VDD, providing sufficiently high recall rates for the internal memory of CHEEM and resulting 1058 in overall high average accuracy and negligible average forgetting. On the contrary, the external 1059 task-centroid memory of the balanced Imagenet-R benchmark explains why our CHEEM performs much worse under CCL. We note that the external memory is constructed based on the frozen base 1061 model. As discussed in the main text, a potential improvement is to leverage dynamically updated 1062 backbones via the internal memory of our CHEEM in computing the task centroids at the expense of 1063 increased task ID inference cost. That is also to shift from our current decoupled external and internal 1064 memory design to integrative / coupled external and internal memory.

Together with the experimental results that the prompting based methods (L2P, DualPrompt and CODA-Prompt) can handle balanced ImageNet-R better in terms of preventing switched samples as analyzed in Appendix A, and that regularized based method (EWC and L2 Regularization in Table 2) can handle VDD better than prompting based methods, we envision there are opportunities of exploring the integration between them and the internal memory of our CHEEM for more robust ExfCCL across scenarios including both VDD and balanced/imbalanced ImageNet-R.

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### C EXAMPLES OF CHEEM LEARNED SEQUENTIALLY AND CONTINUALLY

Fig. 7 shows the CHEEM learned sequentially and continually via the proposed HEE-based NAS on the VDD benchmark (Rebuffi et al., 2017a) with three different random seeds.

1077 As comparisons, Fig. 8 shows the structure updates learned using the vanilla PE-based NAS. It can 1078 be seen that pure exploration does not reuse components from similar tasks. The pure exploration 1079 based method adds many unnecessary Adapt and New operations even though the tasks are similar (e.g., ImNet  $\rightarrow$  C100), verifying the effectiveness of the proposed sampling method. While the pure exploration scheme adds many Skip operations, thereby reducing the overall FLOPs, the average accuracy is low by a large margin, about 6%. This shows that the pure exploration scheme cannot learn to choose operations in a task synergy aware way. 

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1140	ImageNet	CIFAR100	SVHN	UCF	101 Om	niglot	GTSRB	Pedestria	n VGG F	lowers	Aircraft D	escribable 7	Textures
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1142	Tsk10_DTD	R	• A	R	R	R	R	R	A		R	0.59 <mark>2</mark> M	0.14 <mark>5</mark> G
1143	Tsk9_Airc											1 4 79M	0.3396
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1145	Tsk7_DPed	R	R	R		R	R			R	R	0.2 <mark>9</mark> 6M	0.19 <mark>3</mark> G
1146			R	R		R	R	R	R	R	R	0.2 <mark>9</mark> 6M	0.29 <mark>0</mark> G
1147			R		R	R		R	R	R	R	1.18 <mark>3</mark> M	0.29 <mark>0</mark> G
1148	Tsk5_Odlot		→ R		R		R	R		R_	R	1.18 <mark>3</mark> M	0.3 <mark>39</mark> G
1149	Tsk4_UQF				B	B			JB			1 18 <mark>3</mark> M	0.2426
1150	Tsk3_S'IHN												0.2
1151	R A Tsk2_C <sup>1</sup> 00								→ S			- <mark>2.6</mark> 57M	- <mark>0.4</mark> 29G
1152		<u></u> ↓•₽	→₽-							<u></u>		0.88 <mark>6</mark> M	0.0 <mark>4</mark> 8G
1154	IN_B1 IN_B2	-• IN_B3 -•	IN_B4	- IN_B5-	• IN_B6	• IN_B7	• IN_B8	• IN_B9	• IN_B10	- IN_B11		Param. Inc.	FLOPs Inc.
1155	Tsk10_DTD												
1156	A R Tsk9 Airc	R		R	R	R	A	R	A	R	R	1.18 <mark>3</mark> M	0.2 <mark>42</mark> G
1157	RRR		R	R	A	R	R	R	R	R	R	0.5 <mark>9</mark> 2M	0.3 <mark>39G</mark>
1158	R R	R	A	R	R-	R	R	R-	R-	R-	R	0.2 <mark>9</mark> 6M	0.19 <mark>3</mark> G
1159	Tsk7_DPed	B	B	R -	R	R -	R-			R	R	0.59 <mark>2</mark> M	0.19 <mark>3</mark> G
1160	Tsk6_GTSR											1 7751	0.0000
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1162	Tsk4_UQF		R		R	Â	R		R		R	1.18 <mark>3</mark> M	0.19 <mark>3</mark> G
1163		R	R	R	R	R	R	R	A	R	A	0.88 <mark>8</mark> M	0.19 <mark>3</mark> G
1164		R	R			• N			• S	R		0.2 <mark>9</mark> 7M	-0. <mark>1</mark> 66G
1165	Tsk2_C <sup>1</sup> 00		A	R_	R	→ R	R_		R R		N	0.88 <mark>6</mark> M	0.0 <mark>4</mark> 8G
1166	Tsk1 ImNet												
1167			• (IN_B4)							- IN_B11	- IN_B12	) Param. Inc.	FLOPs Inc
1168	Tsk10_DTD		B	B	B	B	B	B		B	B	0.592M	0.2426
1170	Tsk9_Airc												0.2
1170	Tsk8_Flwr		A				A	A			R	1.77 <mark>5</mark> M	0.4 <mark>35G</mark>
1172	R R Tsk7 DPed	R	R	R	R	R	A	- R	+ R	R	R	0.2 <mark>9</mark> 6M	0.2 <mark>42</mark> G
1173	R R	R	R	R	R	R	R		R	- N	R	0.88 <mark>6</mark> M	0.19 <mark>8</mark> G
1174	Tsk6_GTSR		R		R	R_	A-	R	R	R-	R	1.18 <mark>3</mark> M	0.29 <mark>0</mark> G
1175	Tsk5_Ogilot	B	→ B	B				B	B	B	B	1.18 <mark>8</mark> M	0.29 <b>0</b> G
1176	Tsk4_U0F												
1177	Tsk3_SVHN	R		R		A				+ R	- R	1.18 <mark>3</mark> M	0.29 <mark>0</mark> G
1178	A R Tsk2 C'00		A	R	A	A	R	R	A	• S	- S	- <mark>3.2</mark> 48M	- <mark>0.5</mark> 26G
1179			→ R	- R		- R	- R	R	R-	R		0.8 <mark>8</mark> 6M	0.0 <mark>4</mark> 8G
1180	Isk1_ImNet	2)-+(IN_B3)-	IN_B4					IN_B9	IN_B10	IN_B11	- IN_B12	) Param. Inc.	FLOPs Inc
1181		$\sim$	$\sim$										

Figure 7: Examples of the task-synergy memory (CHEEM) learned on the VDD benchmark (Rebuffi et al., 2017a) with the task sequence shown in the top **using our proposed HEE-based NAS** and three different random seeds. The overall performance is reported in Table 2 in the main paper. **S**, **R**, **A** and **N** represent Skip, Reuse, Adapt and New respectively. The last two columns show the number of new task-specific parameters and added FLOPs respectively, in comparison with the first task, ImNet model. Overall, the learned task synergies make intuitive sense and remain relatively stable across different random seeds.



Figure 8: Examples of the task-synergy memory (CHEEM) learned on the VDD benchmark (Rebuffi et al., 2017a) with the task sequence shown in the top **using the vanilla PE-based NAS** and three different random seeds. **S**, **R**, **A** and **N** represent Skip, Reuse, Adapt and New respectively. The overall performance is reported in Table 4 in this appendix and our proposed HEE-based NAS significantly improves the performance by an absolute 6% average accuracy. In terms of the learned CHEEM, the PE-based NAS leads to much more New operations, which shows it is less effective in terms of leveraging task synergies.

## 1242 D ABLATION STUDIES

D.1 HIERARCHICAL EXPLORATION AND EXPLOITATION (HEE) VS. PURE EXPLORATION (PE)

We verify the effectiveness of our HEE sampling (Table 4), which is significantly better by a large margin, 6% absolute average accuracy increase.

Table 4: The effectiveness of our proposed hierarchical exploration and exploitation sampling empowered SPOS NAS (Fig. 4). The structure updates learned by the PE strategy are visualized in Fig. 8 in the Appendix.

Method	C100	SVHN	UCF	OGlt	GTSR	DPed	Flwr	Airc.	DTD   Avg. Accuracy	Avg. Forgetting
PE	80.34	94.75	72.63	81.43	99.13	99.59	72.45	38.27	$37.22 \mid 75.09 \pm 0.81$	$0.32\pm0.00$
HEE	88.56	95.63	75.05	83.81	99.15	99.64	90.92	55.53	56.42 82.74 $\pm$ 0.54	$0.33\pm0.0$

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### D.2 COMPARISON WITH DARTS

Table 5 shows the effectiveness of the proposed HEE empowered SPOS NAS against DARTS, as used in the original learn-to-grow method. Our proposed HEE empowered SPOS NAS outperforms DARTS, and the more advanced  $\beta$ -DARTS (Ye et al., 2022) by a large margin. We compare with Learn-to-Grow under a task-incremental continual learning (TCL) setting as used in the original formulation of L2G by (Li et al., 2019).

1264Table 5: The effectiveness of our proposed HEE sampling empowered SPOS NAS (Fig. 4). The two1265L2G variants use the same ViT-B base model as our HEE.

Method	C100	SVHN	UCF	OGlt	GTSR	DPed	Flwr	Airc.	DTD   Avg. Accuracy
$\begin{array}{c c} L2G (DARTS) \\ L2G (\beta \text{-}DARTS) \end{array}$	88.47 88.95	85.20 94.73	79.22 75.31	80.19 79.76	99.28 99.84	98.06 99.76	76.14 78.86	39.29 34.50	$\begin{array}{c c c c c c c c c c c c c c c c c c c $
HEE	90.93	95.96	80.74	83.25	99.94	99.96	94.12	58.90	$60.05  84.65 \pm 0.33$

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### D.3 RESULTS BY TASK-TO-TASK TRANSFER BASED CONTINUAL LEARNING

To evaluate the transfer learning capabilities of CHEEM, we compare with three state-of-the-art methods: Supermasks in Superposition (SupSup) (Wortsman et al., 2020), Efficient Feature Transformation (EFT) (Verma et al., 2021) and Lightweight Learner (LL) (Ge et al., 2023) that modify the backbone model separately for each taskm, which we refer to as a task-to-task transfer setting. We modify all the methods to work with ViTs. We provide the details of the modifications in Section H. All three methods are fine-tuned on a new task for 50 epochs. For CHEEM, we use 50 epochs for the supernet training and 30 epochs for fine-tuning.

1280 Table 6 demonstrates that CHEEM achieves the highest average accuracy on the VDD benchmark. 1281 Although its performance on individual tasks may be lower, CHEEM exhibits robustness to domain 1282 variations, as reflected in its overall average accuracy. In contrast, other methods show varying 1283 performance depending on the domain. SupSup performs well on tasks that are significantly different 1284 from the base ImageNet task, such as UCF 101, Omniglot, and SVHN, but performs poorly on tasks 1285 closely related to ImageNet. Conversely, EFT and LL excel on tasks similar to ImageNet but struggle 1286 with out-of-distribution tasks. Despite its lower individual task performance, CHEEM's consistent performance across diverse downstream tasks highlights its adaptability and makes it more general. 1287

Table 6: Results on the VDD benchmark (Rebuffi et al., 2017a) using ViT-B/8 (Dosovitskiy et al., 2021) under the task-to-task transfer based continual learning protocol. The learned CHEEM are visualized in Fig. 10 in the Appendix.

1291	Method	ImNet	C100	SVHN	UCF	OGlt	GTSR	DPed	Flwr	Airc.	DTD	Avg. Accuracy
1292	SupSup	82.65	89.96	<b>96.05</b>	<b>81.68</b>	<b>84.60</b>	<b>99.97</b>	99.97	78.76	44.18	51.60	$81.14 \pm 0.04 \\ 82.60 \pm 0.07 \\ 82.10 \pm 0.02$
1293	EFT	82.65	91.86	93.51	73.89	75.62	99.58	<b>99.98</b>	96.34	48.17	64.40	
1294	LL	82.65	<b>91.92</b>	93.90	75.63	83.25	99.71	99.96	<b>96.4</b> 7	49.33	64.34	$83.10 \pm 0.02$
1295	Our CHEEM	82.65	90.93	95.96	80.74		99.94	99.96	94.12	58.90	60.05	84.65 ± 0.33

## 1296 D.4 CHEEM PLACED AT OTHER VIT COMPONENTS

Table 7 shows the performance comparisons with other four different components in the ViT (the Query/Key/Value linear projection layer and the FFN block) used in realizing the proposed CHEEM.
The Query/Key/Value component as the CHEEM does not perform as well as the Projection component. The FFN block as the CHEEM performs only slightly better than the Projection layer, but at the expense of a much larger parameter cost. This reinforces our identification above.

Table 7: Results of ablation study on other components of the ViT used for realizing the CHEEM.The results have been averaged over 3 different seeds.

305	Component	ImNet	C100	SVHN	UCF	OGlt	GTSR	DPed	Flwr	Airc.	DTD	Avg. Accuracy	Avg. Param. Inc./task (M)
306	Projection	82.65	90.54	96.12	75.53	83.81	99.93	99.88	91.21	55.59	59.18	$83.44\pm0.50$	$1.06\pm0.04$
307	Query Key	82.65 82.65	89.66 89.29	$93.74 \\ 94.77$	71.53 72.25	82.02 81.86	99.87 99.86	99.89 99.90	90.03 88.86	$49.57 \\ 51.72$	$59.40 \\ 60.46$	$81.84 \pm 0.32$ $82.16 \pm 0.17$	$2.38 \pm 0.12$ $2.41 \pm 0.03$
308	Value	82.65	84.94	95.90	75.85	84.68	99.89	99.89	86.54	48.83	55.37	$81.46 \pm 0.25$	$1.70 \pm 0.11$
309	FFN	82.65	91.05	96.08	76.96	85.22	99.94	99.94	93.79	56.74	59.61	$84.20\pm0.28$	$2.31 \pm 0.28$

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1311 D.5 IMPLEMENTATION DETAILS OF THE Adapt OPERATION

1313 How to Adapt in a sustainable way? The proposed Adapt operation will effectively increase the 1314 depth of the network in a plain way. In the worst case, if too many tasks use Adapt on top of each other, we will end up stacking too many MLP layers together. This may lead to unstable training due 1315 to gradient vanishing. Shortcut connections (He et al., 2016) have been shown to alleviate the gradient 1316 vanishing and exploding problems, making it possible to train deeper networks. We introduce the 1317 shortcut connection in adding a MLP Adapt operation. We test two different implementations: with 1318 shortchut in all the three components (supernet training, target network selection and target network 1319 finetuing) versus with shortcut only in target network finetuning (i.e., without shortcut in the NAS 1320 including both supernet training and target network selection). 1321

1322Table 8: Results of the ablation study on the implementation of the Adapt operation: with (w/) vs1323without (w/o) shortcut connection for the MLP Adapt layer in NAS. The first two rows are for the1324sequential and continual paradigm and the last two rows for the task-to-task (T2T) transfer based1325paradigm.

1326	Shortcut in NAS	ImNet	C100	SVHN	UCF	OGlt	GTSR	DPed	Flwr	Airc.	DTD	Avg. Accuracy	Avg. Param. ↑/task (M)	Avg. FLOPs ↑/task (G)
1327	w/o	82.65	90.54	96.12	75.53	83.81	99.93	99.88	91.21	55.59	59.18	$83.44 \pm 0.50$	$1.06\pm0.04$	$0.17\pm0.01$
1000	w/	82.65	91.18	96.18	82.34	86.03	99.91	99.95	91.60	58.90	58.56	$84.73 \pm 0.19$	$2.01 \pm 0.18$	$0.49 \pm 0.13$
1320	w/o (T2T)	82.65	90.93	95.96	80.74	83.25	99.94	99.96	94.12	58.90	60.05	$84.65\pm0.33$	$2.61 \pm 0.15$	$-0.19\pm0.09$
1329	w/ (T2T)	82.65	91.24	99.25	84.14	85.99	99.97	99.95	94.64	60.34	61.63	$85.68 \pm 0.16$	$3.23\pm0.12$	$0.01\pm0.02$

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Table 8 shows the performance comparisons on the VDD Benchmark under the continual learning paradigm. In terms of sequentially introduced complexities, a more compact model is learned without the shortcut in the Adapt during NAS (supernet training and target network selection) as evidenced by the number of additional parameters and the increase in FLOPs. Using the shortcut in both supernet training and target network selection results in twice the parameter increase, and almost 4× increase in FLOPs. Fig. 9 and Fig. 10 show comparisons of the learned CHEEM by the two implementation methods under the two paradigms respectively.

- 1338 **Remarks.** We have two remarks as follows.
- We use the more parameter-efficient implementation (i.e., w/o shortcut for the Adapt in NAS) in the main paper for both the continual learning and the task-to-task transfer learning paradigms, even though the counterparts have better performance.
- We note that although the T2T paradigm results in larger parameter increase per task, its computational costs are relatively lower due to either more Skip operations learned and/or the fact that there is no Adapt-on-Adapt operations since it is task-to-task transfer based learning.

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1355 1356 1357 1358 1359 1360 Tsk10\_DTD 1361 R R • R 0.59<mark>2</mark>M 0.14<mark>5</mark>G R R -R • R -R R • R A + A Tsk9\_Air 1362 Α R R R R R R A R • R А 1.4<mark>79</mark>M 0.3<mark>39G</mark> A A Tsk8 Flw 1363 R • R R R ► R • R R • R 0.19<mark>3</mark>G R R R ■ R A 0.296M 1364 Tsk7\_DP R R R R • R • R • R -R R 0.296M 0.29<mark>0</mark>G R R A 1365 Tsk6\_G ŝR 1366 Α R R R • R Α -R R R R 1.18<mark>3</mark>M 0.29<mark>0</mark>G A Tsk5\_OR 1367 + R • R -A • R -+ R A R 0.33<mark>96</mark> Α\_ R -A R • R 1.183M 1368 Tsk4\_U A \_ R R R + R • R -R A • R -• R -A А 1.18<mark>3</mark>M 0.24<mark>2</mark>G R -1369 Tsk3\_ R-R -• S S 2.6<mark>57M</mark> -<mark>0.4</mark>29G R A A 1370 Tsk2 C100 1371 R R N 0.88<mark>6</mark>M 0.0<mark>4</mark>8G R • R R R R R-R R sk1\_ImNet 1372 (IN\_B1)-(IN\_B2 IN\_B12 FLOPs Inc. IN\_B9 IN\_B3 IN\_B4 IN\_B5 IN\_B6 IN\_B7 IN\_B8 IN\_B10 IN\_B11 Param. Inc. 1373

(a) An example of CHEEM learned without the shortcut for the MLP Adapt layer in NAS (the same one as the 2nd row in Fig. 7).

	Tsk10_DTD												
		R	R	A	R	R	- A	R				2.0 <mark>71M</mark>	0.6 <mark>296</mark>
(	Tsk9_Airc	(	(	(	(	(	(	(	(	(	(		
		A	R		R			A	A	R	+ R	2.3 <mark>67M</mark>	0.67 <mark>76</mark>
(	Tsk8_Flwr		(	(	(	Ī	$\wedge$	(	(			_	
				R	R					<b>└──</b> ₽	R	1.7 <mark>75</mark> M	0.6 <mark>29G</mark>
l l	Tsk7_DPed		( <u> </u>				(		(	$\mathbf{T}$		_	_
			R	R		R						1.7 <mark>75</mark> M	0.53 <mark>2G</mark>
	Tsk6_GTSR												
			R		R	R				• S	A	-0. <mark>5</mark> 89M	0.076G
ľ	Tsk5_OBlot			(		( _	(					_	
												2.071M	0.43 <mark>5</mark> G
	Tsk4_U0F					$\frown$	$\frown$					_	
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ľ	Isk3_STHN												
						<u></u>			• N		R	2.07 <mark>0M</mark>	0.29 <mark>0</mark> G
	Isk2_C100												
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TE	sk1_ImNet												
(	IN_B1 )→( IN_B2 )	→( IN_B3 )	→( IN_B4 )	→( IN_B5 )	-+( IN_B6 )	-+( IN_B7 )	→( IN_B8 )	→( IN_B9 )	→( IN_B10 )	→( IN_B11 )	)( IN_B12 )	Param. Inc.	FLOPs Inc.

(b) An example of CHEEM learned with the shortcut for the MLP Adapt layer in NAS. More Adapt on top of Adapt operations are learned.

Figure 9: Comparisons between CHEEM learned by two different implementations of the MLP Adapt operation under the sequential and continual learning paradigm. S, R, A and N represent Skip, Reuse, Adapt and New respectively.

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(b) An example of CHEEM learned with the shortcut for the MLP Adapt layer in NAS. More Adapt operations are learned.

Figure 10: Comparisons between CHEEM learned by two different implementations of the Adapt operation under the task-to-task (T2T) transfer based lifelong learning setting. Here all the 9 tasks are transferred from the base Tsk1\_ImNet model, so we omit the arrows linking the blocks for clarity. **S**, **R**, **A** and **N** represent Skip, Reuse, Adapt and New respectively.

## 1458 D.6 EFFECTS OF TASK ORDERS

We investigate the effects of task orders of the 9 tasks in the VDD benchmark. We test four more task sequences in addition to the one presented in the main paper. Overall, The CHEEM learned by our proposed HEE-based NAS achieve similar performance across different task orders, and consistently significantly outperform those learned by the vanilla PE-based NAS. We note that since the task ID inference is based on a frozen backbone, it is independent of the task order. Hence, for simplicity, we evaluate the effect of task order in a task-incremental setting.

Table 9 reports the performance. Fig. 11, Fig. 12, Fig. 13 and Fig. 14 show the learned CHEEM using our proposed HEE-based NAS.

1468Table 9: Results of ablation study on CHEEM learning with four different task orders using both our1469proposed HEE-based NAS and the vanilla PE-based NAS. The results have been averaged over 31470different seeds.

1471	NAS	ImNet	OGlt	UCF	Airc.	Flwr	SVHN	DTD	GTSR	DPed	C100	Avg. Accuracy	Avg. Param. Inc./task (M)
1472	HEE	82.65	84.32	75.27	54.32	90.29	95.83	57.89	99.92	99.72	89.96	$83.02\pm0.31$	$1.25\pm0.15$
1473	PE	82.65	77.41	70.12	39.40	64.35	94.12	37.02	99.83	99.41	70.78	$73.51\pm0.80$	$2.86\pm0.14$
1474	NAS	ImNet	DPed	SVHN	DTD	Airc.	OGlt	C100	GTSR	Flwr	UCF	Avg. Accuracy	Avg. Param. Inc./task (M)
1475	HEE	82.66	99.94	95.83	58.56	42.43	83.55	89.98	99.95	91.99	75.67	$82.06 \pm 1.28$	$1.42\pm0.05$
1476	PE	82.66	99.65	95.04	45.66	35.87	77.62	71.51	99.85	66.11	63.99	$73.79\pm0.50$	$2.85\pm0.12$
1477	NAS	ImNet	UCF	C100	OGlt	GTSR	DTD	Flwr	SVHN	DPed	Airc.	Avg. Accuracy	Avg. Param. Inc./task (M)
1477 1478	NAS HEE	ImNet   82.66	UCF 79.73	C100 90.75	OGlt 84.93	GTSR 99.90	DTD 58.14	Flwr 91.27	SVHN 96.05	DPed 99.89	Airc. 54.06	Avg. Accuracy $83.74 \pm 0.51$	Avg. Param. Inc./task (M) $1.37 \pm 0.05$
1477 1478 1479	NAS HEE PE	ImNet   82.66   82.66	UCF   79.73   74.49	C100 90.75 74.17	OGlt 84.93 78.76	GTSR 99.90 99.91	DTD 58.14 41.01	Flwr 91.27 70.49	SVHN 96.05 94.15	DPed 99.89 99.25	Airc. 54.06 37.77	Avg. Accuracy $83.74 \pm 0.51$ $75.27 \pm 2.41$	Avg. Param. Inc./task (M) $1.37 \pm 0.05$ $2.75 \pm 0.16$
1477 1478 1479 1480	NAS HEE PE NAS	ImNet   82.66   82.66   ImNet	UCF 79.73 74.49	C100 90.75 74.17 UCF	OGlt 84.93 78.76 OGlt	GTSR 99.90 99.91 GTSR	DTD 58.14 41.01 DPed	Flwr 91.27 70.49 C100	SVHN 96.05 94.15 Airc.	DPed 99.89 99.25 DTD	Airc. 54.06 37.77 SVHN	Avg. Accuracy $83.74 \pm 0.51$ $75.27 \pm 2.41$ Avg. Accuracy	Avg. Param. Inc./task (M) $1.37 \pm 0.05$ $2.75 \pm 0.16$ Avg. Param. Inc./task (M)
1477 1478 1479 1480 1481	NAS HEE PE NAS HEE	ImNet   82.66   82.66   ImNet   82.66	UCF   79.73   74.49   Flwr   87.52	C100 90.75 74.17 UCF 77.17	OGlt 84.93 78.76 OGlt 84.20	GTSR 99.90 99.91 GTSR 99.92	DTD 58.14 41.01 DPed 99.80	Flwr 91.27 70.49 C100 90.30	SVHN 96.05 94.15 Airc. 54.49	DPed 99.89 99.25 DTD 56.83	Airc. 54.06 37.77 SVHN 96.03	Avg. Accuracy $83.74 \pm 0.51$ $75.27 \pm 2.41$ Avg. Accuracy $82.89 \pm 0.58$	Avg. Param. Inc./task (M) $1.37 \pm 0.05$ $2.75 \pm 0.16$ Avg. Param. Inc./task (M) $1.41 \pm 0.09$



Figure 11: Examples of the task-synergy memory (CHEEM) learned on the VDD benchmark (Rebuffi et al., 2017a) with the task sequence shown in the top **using our proposed HEE-based NAS** and three different random seeds. The overall performance is reported in Table 9. **S**, **R**, **A** and **N** represent Skip, Reuse, Adapt and New respectively. The last two columns show the number of new task-specific parameters and added FLOPs respectively, in comparison with the first task, ImNet model. Overall, the learned task synergies make intutive sense and remain relatively stable across different random seeds.



Figure 12: Examples of the task-synergy memory (CHEEM) learned on the VDD benchmark (Rebuffi et al., 2017a) with the task sequence shown in the top **using our proposed HEE-based NAS** and three different random seeds. The overall performance is reported in Table 9. **S**, **R**, **A** and **N** represent Skip, Reuse, Adapt and New respectively. The last two columns show the number of new task-specific parameters and added FLOPs respectively, in comparison with the first task, ImNet model. Overall, the learned task synergies make intutive sense and remain relatively stable across different random seeds.



Figure 13: Examples of the task-synergy memory (CHEEM) learned on the VDD benchmark (Rebuffi et al., 2017a) with the task sequence shown in the top **using our proposed HEE-based NAS** and three different random seeds. The overall performance is reported in Table 9. **S**, **R**, **A** and **N** represent Skip, Reuse, Adapt and New respectively. The last two columns show the number of new task-specific parameters and added FLOPs respectively, in comparison with the first task, ImNet model. Overall, the learned task synergies make intutive sense and remain relatively stable across different random seeds.



Figure 14: Examples of the task-synergy memory (CHEEM) learned on the VDD benchmark (Rebuffi et al., 2017a) with the task sequence shown in the top **using our proposed HEE-based NAS** and three different random seeds. The overall performance is reported in Table 9. **S**, **R**, **A** and **N** represent Skip, Reuse, Adapt and New respectively. The last two columns show the number of new task-specific parameters and added FLOPs respectively, in comparison with the first task, ImNet model. Overall, the learned task synergies make intutive sense and remain relatively stable across different random seeds.

## 1728 E DATASET DETAILS



Figure 15: Example images from the VDD benchmark (Rebuffi et al., 2017a). Each task has a significantly different domain than others, making VDD a challenging benchmark for lifelong learning.

Table 10: The number of samples in training, validation and testing sets per task used in our experiments on the VDD benchmark (Rebuffi et al., 2017a).

Task	Train	Validation	Test	#Categories
ImageNet12	1108951	123216	49000	1000
CIFAR100	36000	4000	10000	10
SVHN	42496	4721	26040	10
UCF	6827	758	1952	101
Omniglot	16068	1785	6492	1623
GTSR	28231	3136	7842	43
DPed	21168	2352	5880	2
VGG-Flowers	918	102	1020	102
Aircraft	3001	333	3333	100
DTD	1692	188	1880	47

### 1750 E.1 THE VDD BENCHMARK

It consists of 10 tasks: ImageNet-1k (Russakovsky et al., 2015), CIFAR100 (Krizhevsky et al., 2009), 1752 SVHN (Netzer et al., 2011), UCF101 Dynamic Images (UCF) (Soomro et al., 2012; Bilen et al., 1753 2016), Omniglot (Lake et al., 2015), German Traffic Signs (GTSR) (Stallkamp et al., 2012), Daimler 1754 Pedestrian Classification (DPed) (Munder & Gavrila, 2006), VGG Flowers (Nilsback & Zisserman, 1755 2008), FGVC-Aircraft (Maji et al., 2013), and Describable Textures (DTD) (Cimpoi et al., 2014). All 1756 the images in the VDD benchmark have been scaled such that the shorter side is 72 pixels. Table 10 1757 shows the number of samples in each task. Fig. 15 shows examples of images from each task of the 1758 VDD benchmark. In our experiments, we use 10% of the official training data from 1759 each of the tasks for validation (e.g., used in the target network selection in Section 3.2.3 in main 1760 text), and report the accuracy on the official validation set due to the unavailability of 1761 the ground-truth labels for the official test data. In Table 10, the train, validation 1762 and test splits are thus referred to 90% of the official training data, 10% of the official training data, 1763 and the entire official validation data respectively. When finetuning the learned architecture (i.e., the searched target network) for each task, we use the entire official training data to 1764 train and report results on the official validation set. 1765

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### 1768 E.2 IMAGENET-R BENCHMARK

The ImageNet-R(etention) (Hendrycks et al., 2021) dataset contains art, cartoons, deviantart, graffiti, 1770 embroidery, graphics, origami, paintings, patterns, plastic objects, plush objects, sculptures, sketches, 1771 tattoos, toys, and video game renditions of ImageNet classes. It has renditions of 200 ImageNet 1772 classes resulting in 30,000 images. The Split ImageNet-R benchmark proposed by (Wang et al., 1773 2022c) uses the ImageNet-R dataset to build a continual learning benchmark specifically for studying 1774 methods that use model pretrained on ImageNet (Russakovsky et al., 2015). ImageNet-R poses 1775 challenges for such methods because of the diversity within the same class. The Split-ImageNet 1776 benchmark proves to be challenging for experience-replay based approaches because of this intra-1777 class variance, as well as replay-free methods that use a frozen backbone from ImageNet as the 1778 accuracy of the standard models on ImageNet-R is low. We use the same training and validation 1779 splits as those used by (Smith et al., 2023a). For the balanced evaluation, we divide the data set into 10 tasks with 20 classes each, and report results across 3 runs with random class orders. For the 1780 imbalanced evaluation, we construct 6 tasks with 5, 10, 15, 20, 50 and 100 classes. We report results 1781 across 3 runs with tasks, with varying task orders.

### <sup>1782</sup> F THE BASE VISION TRANSFORMER: VIT-B/8

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We use the base Vision Transformer (ViT) model, with a patch size of  $8 \times 8$  (ViT-B/8) model from (Dosovitskiy et al., 2021). The base ViT model contains 12 Transformer blocks. A Transformer block is defined by stacking a Multi-Head Self-Attention (MHSA) block and a Multi-Layer Perceptron (MLP) block with resudual connections for each block. ViT-B/8 uses 12 attention heads in each of the MHSA blocks, and a feature dimension of 768. The MLP block expands the dimension size to 3072 in the first layer and projects it back to 768 in the second layer. For all the experiments, we use an image size of  $72 \times 72$  following the VDD setting. We base the implementation of the ViT on the timm package (Wightman, 2019).

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1793 **Training the Base Model** To train the ViT-B/8 model, we use the ImageNet data provided by 1794 the VDD benchmark (the train split in Table 10). To save the training time, we initialize the weights from the ViT-B/8 trained on the full resolution ImageNet dataset  $(224 \times 224)$  and avail-1795 able in the timm package, and finetune it for 30 epochs on the downsized version of ImageNet 1796  $(72 \times 72)$  in the VDD benchmark. We use a batch size of 2048 split across 4 Nvidia Quadro 1797 RTX 8000 GPUs. We follow the standard training/finetuning recipes for ViT models. The file cheem/artifacts/imagenet\_pretraining/args.yaml in our code folder provides all 1799 the training hyperparameters used for training the the ViT-B/8 model on ImageNet. During testing, we take a single center crop of  $72 \times 72$  from an image scaled with the shortest side to scaled to 72 1801 pixels. 1802

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### G SETTINGS AND HYPERPARAMETERS IN LEARNING CHEEM

Starting with the ImageNet trained ViT-B/8, the proposed CHEEM learning consists of three components: *supernet training, evolutionary search for target network selection, and target network finetuning.*

1809	Table 11: Data augmentations for the 9 tasks in
1810	the VDD benchmark.

1010	the VDD be	nchmark.			Т	Table 12: Data augmentations used for each task					
1811	Task	Scale and Crop	Hor. Flip	Ver. Flip	iı	n the 5-Datasets b	enchmark.				
1813	CIFAR100	Yes Ves	p=0.5	No No	-	Task	Scale and Crop	Hor. Flip			
1814	DPed	Yes	p=0.5 p=0.5	No	_	MNIST	Yes	No			
1815	DTD	Yes	p=0.5	p=0.5		not-MNIST	Yes	No			
1816	GTSR OGlt	Yes Yes	p=0.5 No	No No		SVHN CIFAR100	Yes Yes	No p=0.5			
1817	SVHN UCF101	Yes Yes	No p=0.5	No No	_	Fashion MNIST	Yes	No			
1819	Flwr.	Yes	p=0.5	No							

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**Data Augmentations** A full list of data augmentations used for the VDD benchmark is provided in Table 11, and the data augmentations used for the tasks in the 5-datasets benchmark is provided in Table 12. The augmentations are chosen so as not to affect the nature of the data. Scale and Crop transformation scales the image randomly between 90% to 100% of the original resolution and takes a random crop with an aspect ratio sampled from a uniform distribution over the original aspect ratio  $\pm 0.05$ . In evaluating the supernet and the finetuned model on the validation set and test set respectively, images are simply resized to  $72 \times 72$  with bicubic interpolation.

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**Supernet Training** *The VDD Benchmark:* For each task, we train the supernet for 100 epochs, unless otherwise stated. We use a label smoothing of 0.1. We use a learning rate of 0.001 and the Adam optimier (Kingma & Ba, 2015) with a Cosine Decay Rule. We use a batch size of 512, and ensure the minimum number of batches in an epoch is 15 (via repeatedly sampling when the number of total samples of a task is not sufficient). As stated in the paper, for the Exploration-Exploitation sampling scheme, we use an exploration probability  $\epsilon = 0.3$ .

1835 *The 5-datasets Benchmark*: We use the same hyperparameters as those used in the VDD Benchmark, but train the supernet for 50 epochs to account for its relatively lower complexity.

1836 L2G with DARTS and  $\beta$ -DARTS: We train the supernet of the Learn-to-Grow (L2G) (Li et al., 2019) 1837 for 50 epochs on the VDD benchmark and 25 epochs on the 5-datasets benchmark, since DARTS 1838 simultaneously trains all sub-networks (i.e. the entire supernet) at each epoch. We use a weight of 1 1839 for the beta loss in all the experiments with  $\beta$ -DARTS.

**Evolutionary Search** The evolutionary search is run for 20 epochs. We use a population size of 50. We use 25 candidates both in the mutation stage and the crossover stage. The top 50 candidates are retained. The crossover is performed among the top 10 candidates, and the top 10 candidates are mutated with a probability of 0.1. For the Exploration-Exploitation sampling scheme, we use an exploration probability  $\epsilon = 0.5$  when generating the initial population.

Finetuning The target network for a task selected by the evolutionary search is finetuned for 30 epochs with a learning rate of 0.001, Adam optimizer, and a Cosine Learning Rate scheduler. Drop Path of 0.25 and label smoothing of 0.1 are used for regularization. We use a batch size of 512, and a minimum of 30 batches are drawn.

- 1851 We use a single Nvidia A100 GPU for all the experiments.

### H MODIFYING SUPSUP, EFT AND LL TO WORK WITH VITS

In the main paper, we compare with Supermasks in Superposition (SupSup) (Wortsman et al., 2020),
Efficient Feature Transformation (EFT) (Verma et al., 2021), and Lightweight Learner (LL) (Ge et al., 2023) in Table 5 under the task-to-task transfer learning paradigm. The three methods are originally
developed for Convolutional Neural Networks. We modify them to be compatible with ViTs for a fair comparison with our CHEEM.

We use the same ViT-B/8 base model (Sec. F) for SupSup, EFT and LL. For the SupSup method (Wortsman et al., 2020), we learn masks for the weights of the final linear projection layer of the Multi-Head Self-Attention block using the straight through estimator (Bengio et al., 2013). We apply the EFT (Verma et al., 2021) on all the linear layers in the ViT-B/8 (i.e., all the Query/Key/Value projection layers, the final projection layer, and the FFN layers) by scaling their activation maps via the Hadamard product with learnable scaling vectors, following the original proposed formulation for fully-connected layers in the EFT (Verma et al., 2021). For the LL method (Ge et al., 2023) which learns a task-specific bias vector that is added to all the feature maps of convolutional layers, we learn a similar bias vector and add it to the output of all the linear layers of the ViT.