LLM-RankFusion: Mitigating Intrinsic Inconsistency in LLM-based Ranking

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Abstract

Ranking passages by prompting a large language model (LLM) can achieve promising performance in modern information retrieval (IR) systems. A common approach to sort the ranking list is by prompting LLMs for a pairwise or setwise comparison which often relies on sorting algorithms. However, sorting-based methods require consistent comparisons to sort the passages correctly, which we show that LLMs often violate. We identify two kinds of intrinsic inconsistency in LLM-based pairwise comparisons: order inconsistency which leads to conflicting results when switching the passage order, and transitive inconsistency which leads to non-transitive triads among all preference pairs. Our study of these inconsistencies is relevant for understanding and improving the stability of any ranking scheme based on relative preferences. In this paper, we propose LLM-RankFusion, an LLM-based ranking framework that mitigates these inconsistencies and produces a robust ranking list. LLM-RankFusion mitigates order inconsistency using in-context learning (ICL) to demonstrate order-agnostic comparisons and calibration to estimate the underlying preference probability between two passages. We then address transitive inconsistency by aggregating the ranking results from multiple rankers. In our experiments, we empirically show that LLM-RankFusion can significantly reduce inconsistent comparison results, improving the ranking quality by making the final ranking list more robust.

1 Introduction

Large language models (LLMs) have demonstrated strong zero-shot and few-shot capabilities in many natural language processing tasks Achiam et al. (2023); Zeng et al. (2024); Zhao et al. (2023). This enables the effective integration of these LLMs in modern information retrieval (IR) systems Wu et al. (2023); Li et al. (2024). Without supervised training on labeled data in a specific task, LLMs can adapt to the task by prompt and pipeline design. Recent work has tried to apply LLMs in text ranking and shown promising performance Qin et al. (2023); Chao et al. (2024); Sun et al. (2023); Ma et al. (2023). Text ranking is an important task in modern recommender systems and search engines, which refines the order of the retrieved passages to improve the output quality Liu et al. (2009). Traditional supervised text ranking methods mostly rely on large amounts of human-annotated labels Bajaj et al. (2016); Bonifacio et al. (2021); Thakur et al. (2021); Nogueira & Cho (2019). Typical LLM-based ranking approaches prompt LLMs to generate partial orders, comparisons, or relevance scores without additional training in advance.

Despite the great potential of LLMs in passage ranking, they can also suffer from significant inconsistency. Previous work shows LLM-based ranking is sensitive to the order of input passages in the prompt, which stems from the positional bias of LLMs Wang et al. (2023); Lu et al. (2021); Tang et al. (2023). In a pairwise comparison between two passages, the results can conflict before and after swapping the passages. We identify this as **order inconsistency**. Even if we can fully mitigate the order inconsistency within a single comparison, there is still a concern about inconsistency among multiple different comparisons. For example, PRP-Sort Qin et al. (2023) uses sorting algorithms to efficiently produce a full ranked list from pairwise comparisons. However, these sorting algorithms typically assume the transitivity of comparisons to correctly sort the passage, which we show that LLMs often cannot guarantee. (e.g. $d_1 \succ d_2, d_2 \succ d_3 \Rightarrow d_1 \succ d_3$, where d_i represents a passage and \succ means "preferred to"). We identify this as **transitive inconsistency**,

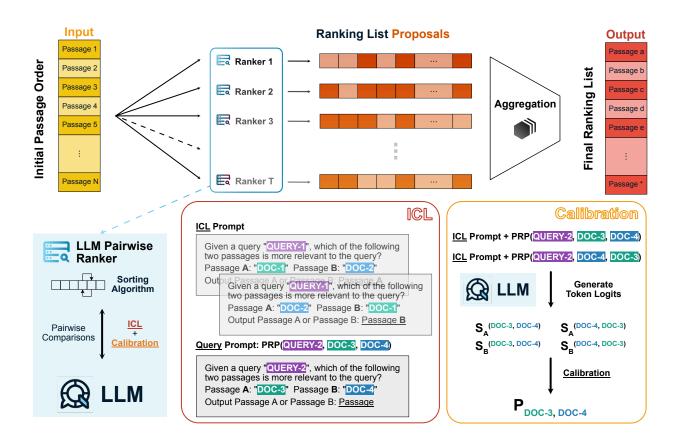


Figure 1: The LLM-RankFusion pipeline. It illustrates the aggregation process to mitigate transitive inconsistency. The ranking list proposals are generated by different rankers, with each ranker's details displayed in the lower-left corner of the figure. Each ranker incorporates ICL and calibration to address order inconsistency.

which has been ignored in previous works. Due to the transitive inconsistency, we show that the ranker's performance is highly sensitive to the initial input order of the retrieved documents. Ranking systems expect to produce a robust ranking list to present to users, but if different initial orderings can lead to significant variant ranked lists, the reliability of the LLM's rankings can be brought into question. Our analysis of this inconsistency can be easily extended to setwise and listwise comparisons, as both ranking schemes rely on relative preferences and are fundamentally pairwise in nature. This broad applicability highlights that identifying and addressing these inconsistencies in pairwise ranking is relevant for improving the reliability of any ranking scheme based on relative preferences. We propose the LLM-RankFusion framework as shown in Figure 1 to produce a consistent ranking list by mitigating the above inconsistencies.

To mitigate order inconsistency, we first use calibration to address the conflict before and after swapping the passages. It calculates the preference probability based on the logit output, which then produces the preference without bias in position. To further let LLM realize the preference should be order agnostic, we propose the in-context learning (ICL) ranking prompt. The ICL prompt uses an example to demonstrate the swapping of passages doesn't affect the preference. While we can greatly reduce order inconsistency by ICL and calibration, the improved pairwise comparison still does not address transitive inconsistency directly. We use rank aggregation to further mitigate the transitive inconsistency. Rank aggregation is a commonly used post-process method in combining multiple ranking lists and yielding a robust ranking result Dwork et al. (2001); Lin (2010); Schalekamp & Zuylen (2009). We aggregate the ranking list proposals from LLM-based pairwise and setwise rankers with different underlying sorting algorithms or different LLMs that are responsible for making preference decisions.

In experiments, we show that ICL and calibration can reduce the effect of positional bias and increase the NDCG score significantly. We then show the effectiveness of aggregation in addressing transitive incon-

	w/o ICL				w/ IC	L
	logits A	logits B	Discrepancy	logits A	logits B	Discrepancy
Flan-T5-XXL	-1.37	-0.97	0.20	-1.12	-0.86	0.13
Llama-3-8B	6.44	6.56	0.06	4.46	3.93	-0.26
Llama-3-70B	-0.15	2.99	0.92	0.31	0.17	-0.07
Gemma-2-9B	7.44	8.01	0.28	8.66	9.02	0.18
Qwen 2.5-32B	9.70	12.20	0.85	12.30	12.50	0.10
Mixtral-8x7B	26.85	19.93	-1.00	28.01	26.19	-0.72
GPT-4	-4.71	-4.54	0.09	-3.74	-5.97	-0.81

Table 1: Average logits value of the token A and the token B from pairwise comparison queries. The token with the highest logits will be sampled as the generated output. The Discrepancy is the difference between the *softmax* of these two logits values computed from Equation 1. The absolute value of the discrepancy close to 1 means the LLM is very biased on position. The ICL stands for in-context learning, which is further elaborated in Section 4.1.1.

Model	# Circular Triads	# Type-1 Triads	# Type-2 Triads	# Total Inconsistent Triads
Flan-T5-XXL	104.67	4720.67	708.72	5534.07
Llama-3-8B	28.70	5556.67	623.44	6208.81
Llama-3-70B	10.02	4533.98	199.09	4743.09
Gemma-2-9B	34.98	3568.77	560.47	4164.21
Qwen 2.5-32B	11.53	4681.58	259.84	4952.95
Mixtral-8x7B	20.70	8970.58	672.49	9663.77
GPT-4	78.65	3694.65	754.91	4528.21

Table 2: The number of inconsistent triads in the tournament graph. A higher number indicates more inconsistency. Type-1 triads refer to $d_i = d_j, d_j = d_k, d_k \succ d_i$. Type-2 triads refer to $d_i = d_j, d_i \succ d_k, d_k \succ d_j$. The total inconsistent triads refer to the sum of all kinds of inconsistent triads. The maximum number of inconsistent triads for 100 passages is 161684 Kułakowski (2018). This tournament graph is constructed from the comparisons without ICL and calibration.

sistency by forming a consensus from multiple ranking lists. In summary, the contributions of this paper are:

- We investigate order inconsistency and, for the first time, identify and study transitive inconsistency in LLM-based ranking.
- We address order inconsistency by ICL and calibration. The improvement is significant in most LLMs.
- We bridge the area of LLM-based ranking with rank aggregation to mitigate the impact of transitive inconsistency in pairwise and setwise comparisons.
- We show the promising empirical performance of the aggregation method by studying the aggregation among different sorting algorithms and LLMs.

2 Related Work

LLM-based ranking approaches have been developed with distinct ranking schemes. Pointwise approaches Liang et al. (2023); Sachan et al. (2023); Drozdov et al. (2023) aim to estimate the relevance between a query and a single document. Listwise Sun et al. (2023); Ma et al. (2023) ranking methods aim to directly rank a list of documents by inserting the query and document list into an LLM's prompt and instructing it to output the reranked document identifiers, though they rely on the strong capability

of LLMs, suffer from positional bias and are sensitive to document order in the prompt Zhu et al. (2023). Pairwise ranking methods Qin et al. (2023) provide the query and a pair of documents to the LLM, which is instructed to generate the identifier of the more relevant document; these pairwise comparisons are then aggregated using efficient sorting algorithms like Heapsort or Bubblesort to produce the final ranking. The Setwise approach Zhuang et al. (2023) is also proposed to compare a set of documents at a time to further improve efficiency. Recent works like Hsieh et al. (2024) explored permutation self-consistency for listwise ranking but focused on positional bias without explicitly identifying or analyzing the cascading effects of transitive inconsistencies.

Rank aggregation has been widely used in many information retrieval tasks Farah & Vanderpooten (2007); Dwork et al. (2001); Wang et al. (2024). Previous works Pradeep et al. (2021); Gienapp et al. (2022) also use aggregation to form the ranking list from pairwise comparison. We explore several well-established rank aggregation methods in our work, including positional scoring methods like Borda count de Borda (1784), which assigns scores based on item positions, and Reciprocal Rank Fusion (RRF) Cormack et al. (2009), which uses a reciprocal form with an additional constant to enhance stability. We also include Markov Chain-based methods MC2 and MC4 Dwork et al. (2001) that model items as states and use transition probabilities to determine the consensus ranking. Additionally, we employ statistical methods like Mean fusion Burges et al. (2011) and Median Fagin et al. (2003) that aggregate rankings based on central tendency measures. These methods represent different approaches to rank aggregation, from simple position-based scoring to probabilistic modeling, allowing us to comprehensively evaluate their effectiveness in combining LLM-based rankings.

3 Inconsistency of LLM-based ranking

3.1 Inconsistency of Pairwise Comparisons

In this work, we identify and distinguish two types of inconsistencies that LLM-based rankers exhibit:

- 1. **Order Inconsistency:** The LLM's judgment on a pair of passages changes depending on the order they are presented in the prompt, which is also known as positional bias Lu et al. (2021).
- 2. Transitive Inconsistency: The LLM makes a series of three or more judgments that logically contradict each other, over a set of three or more passages, i.e., $d_1 > d_2$, $d_2 > d_3$, $d_3 > d_1$.

Under the pairwise ranking approach, each LLM query produces a pairwise comparison results on d_i, d_j , the result can be $d_i \succ d_j$ or $d_j \succ d_i$, where d represents a passage and \succ means "preferred to". While we focus on pairwise comparisons in this work, our analysis of these two types of inconsistency can be easily extended to setwise or listwise ranking schemes. This is because both setwise and listwise comparisons still rely on relative preferences between individual passages, and are therefore fundamentally pairwise in nature. For example, the result of a setwise comparison $d_i \succ d_j, d_k$ can be represented as two implicit pairwise comparisons, $d_i \succ d_j$ and $d_i \succ d_k$. Therefore, our inconsistency analysis cannot only be applied to setwise and listwise ranking, but any ranking scheme that involves relative comparisons between passages.

3.2 Inconsistency Measurement

We measure the inconsistency in comparisons of a variety of LLMs using the TREC-DL2019 test set. We construct the pairwise preference among all passages using PRP-Allpair Qin et al. (2023). The order inconsistency are shown in Table 1. In a pairwise ranking scheme, we ask the LLM to output A to select the first passage or B to select the second passage. We query both the permutations of passages and collect the logits of token A and token B. For an LLM with no positional bias, switching the order of a pair of passages will not affect the preference judgment, which leads to the average logits of A and B being equal. However, we can observe from Table 1 that the logits of these tokens typically suffer from an obvious discrepancy. This indicates that the LLM's choice is often biased towards either A or B, which implies order inconsistency.

We represent pairwise comparisons using a tournament graph - a complete graph where each vertex represents a passage and edges represent preferences between passages. In this graph, directed edges $d_i \rightarrow d_j$

	Bul	oblesort	Не	apsort
	BM25	Hard List	BM25	Hard List
Flan-T5-XXL	67.87	57.91	70.65	69.88
Llama-3-8B	65.38	41.51	68.46	65.88
Llama-3-70B	72.43	64.95	73.71	71.22
Gemma-2-9B	71.31	57.52	71.58	70.79
Qwen 2.5-32B	72.42	65.04	73.75	73.39
Mixtral-8x7B	65.06	39.86	69.14	66.02
GPT-4	72.04	67.72	73.48	72.94

Table 3: NDCG@10 of ranking from different initial orders. The hard list is the inverse order of the ranking result obtained from BM25. Note that Heapsort results are largely unaffected, suggesting that this specific hard list is for Bubblesort only.

indicate that passage d_i is preferred over d_j , while undirected edges indicate ties. Following PRP-Sort Qin et al. (2023), we handle cases of order inconsistency (where swapping passage positions leads to different preferences) by marking them as ties in the graph. While these ties are treated equally in the graph structure, we note that the underlying passages may have different ground truth relevance scores.

To measure transitive inconsistency, we first construct the tournament graph by performing all pairwise comparisons between passages and marking order inconsistent pairs (those that change preference when swapped) as ties. We then count the number of inconsistent triads in the graph, following the method of Kułakowski (2018). An inconsistent triad occurs when three passages form a cycle of strict preferences for example, when d_1 is preferred over d_2 , d_2 is preferred over d_3 , but d_3 is preferred over d_1 , violating transitivity. The count of such triads serves as our metric for transitive inconsistency. As shown in Table 2, we observe that the frequency of inconsistent triads varies across different LLMs, with larger models generally exhibiting fewer transitive inconsistencies.

3.3 The Impact of Inconsistency

As shown in Tables 1 and 2, LLM-based rankers can exhibit significant amounts of inconsistency across judgments. Applying sorting-based ranking schemes based on non-transitive pairwise comparisons can produce volatile result rankings that are highly sensitive to the initial order of candidate passages. This can have particularly adverse effects if that initial ordering is a "hard list" for the chosen sorting method, as demonstrated in Table 3. A hard list is an initial order of passages where the high-relevance passages require many comparisons to be moved to the front of the ranking, increasing the likelihood of encountering a transitive inconsistency that blocks the swapping of the passage. A hard list for one sorting algorithm may not be as hard of a list for another, which is demonstrated in Table 3. By aggregating the full ranked lists from multiple sorting algorithms, we can mitigate the worst-case effects of inconsistency while producing more robust final rankings.

4 Addressing LLM-based Ranking Inconsistency

4.1 Mitigating Order Inconsistency

LLMs suffer from positional bias, which leads to the order inconsistency. This will result in conflicting comparisons after swapping the passage position. Previous work handled order inconsistency as ties in the comparison, which ignores the positional bias nature of LLM-based ranking. We propose 2 methods to mitigate the order inconsistency in the LLM-RankFusion.

4.1.1 In-Context Learning (ICL)

We design the ICL prompt to utilize the few-shot ability Brown et al. (2020) of LLMs to mitigate order inconsistency. The prompt provides the LLM with an example pairwise comparison for both order permu-

Algorithm 1 LLM Rank Aggregation Pipeline

Require: Query q, Corpus D, Rank settings R_1, R_2, \ldots, R_k

Ensure: Aggregated rank list L

1: $L_1, L_2, \ldots, L_k \leftarrow \emptyset$

▷ Initialize empty rank lists

2: for $i \leftarrow 1$ to k do

3: $L_i \leftarrow \text{RANKING}(q, D, R_i)$

 \triangleright Generate rank list using rank setting R_i

4: end for

5: $L \leftarrow \text{RankAggregation}(L_1, L_2, \dots, L_k)$

 \triangleright Aggregate rank lists

6: return L

tations as shown in Figure 1. This demonstration illustrates that the task is to compare the passages based on their relevance to the query instead of its position in the prompt. As shown in Table 1, using ICL can balance the probability of LLM selecting a passage from either position.

4.1.2 Calibration

In a pairwise ranking scheme, we ask the LLM to output token A to select the first passage or B to select the second passage in the given prompt. The positional bias makes LLMs more likely to select the passage in a certain position of the prompt instead of only based on relevance. By considering the comparisons from both possible positions, even if the LLM is biased to a specific position, using the average output probability of a passage under all positions may address this bias.

For every pair of passages, we query the LLM with two permutations $(A=d_i,B=d_j)$ and $(A=d_j,B=d_i)$. For each output, A represents the first passage and B represents the second passage in the prompt. We then take the token probability of A and B from the LLM. We denote $S_A^{(ij)}$ and $S_B^{(ij)}$ as the log probabilities of the output tokens A and B with the permutation $(A=d_i,B=d_j)$. $P_{ij}^{(ij)} \in [0,1]$ is the probability of d_i preferred to d_j with the permutation $(A=d_i,B=d_j)$. The probability is generated among all candidate tokens by LLM. We know that only token A and token B represent a valid choice of passage, so we compute $P_{ij}^{(ij)}$ and $P_{ji}^{(ji)}$ as following:

$$P_{ij}^{(ij)} = \frac{e^{S_A^{(ij)}}}{e^{S_A^{(ij)}} + e^{S_B^{(ij)}}}, \quad P_{ji}^{(ji)} = \frac{e^{S_A^{(ji)}}}{e^{S_A^{(ji)}} + e^{S_B^{(ji)}}}$$
(1)

To make the comparison satisfy $P_{ij} + P_{ji} = 1$, we denote the calibrated probability of $d_i > d_j$ as

$$P_{ij} = \frac{e^{P_{ij}^{(ij)}}}{e^{P_{ij}^{(ij)}} + e^{P_{ji}^{(ji)}}}$$
(2)

Finally, we obtain the calibrated preference of $d_i > d_j$ if $P_{ij} > 0.5$.

4.2 LLM Ranking Aggregation

In passage ranking, we can generate multiple proposed ranking lists using different ranking settings. These settings can include different sorting algorithms to build fully ranked lists from pairwise, setwise, or listwise comparisons, as well as other factors like a specific LLM used for the preference query. Given the inconsistency discussed in Section 3, we know that any configuration of these settings can result in noisy rank results. We cannot assume we know a priori which proposed rank setting is the best, so choosing a single setting that will be affected the least by inconsistency is difficult.

To address noisy ranked list proposals, we propose LLM-RankFusion, a rank aggregation pipeline as shown in Algorithm 1. Rank aggregation can address conflicting results by combining these results into a single, coherent ranking, limiting the effects of noisy settings.

4.2.1 Aggregation Across Ranking Schemes

We aggregate the ranked list proposals from rankers with different ranking schemes. For pairwise and setwise ranking, they include two sorting algorithms, Bubblesort and Heapsort. Bubblesort repeatedly steps through the list, compares adjacent elements, and swaps them if they are in the wrong order; Heapsort uses a binary heap to sort elements. By combining the ranked lists from algorithms with different properties, the aggregated result becomes more robust to variations in the input data. If one algorithm performs poorly on a particular input, the other algorithm may compensate for it, leading to a more consistent overall ranking.

4.2.2 Aggregation Across LLMs

Individual LLMs might also have unique biases in their preferences and, therefore, unique transitive inconsistency. This motivates aggregation across ranking lists from multiple LLMs. This can help to reduce the impact of any individual LLM, which may be inconsistent in handling certain queries. The aggregated result formed by decisions from multiple LLMs can be more robust and consistent.

Model	Baseline	ICL Only	Calibration Only	ICL + Calibration
Flan-T5-XXL Llama-3-8B Llama-3-70B Gemma-2-9B Qwen2.5-32B Mixtral-8x7B	67.87 65.38 72.43 71.31 72.42 65.06	68.64 (+0.77) 66.35 (+0.97) 71.62 (-0.81) 71.70 (+0.39) 71.47 (-0.95) 70.05 (+4.99)	69.73 (+1.86) 69.58 (+4.20) 74.12 (+1.69) 72.60 (+1.29) 74.42 (+2.00) 66.75 (+1.69)	71.05 (+3.18) 71.51 (+6.13) 74.55 (+2.12) 72.79 (+1.48) 73.91 (+1.49) 71.16 (+6.10)
GPT-4	72.04	73.34 (+1.30)	74.56 (+2.52)	74.79 (+2.75)

Table 4: NDCG@10 of PRP-Sorting with Bubblesort, starting from the BM25 initial order on TREC DL 2019. The experiment shows an ablation study of using ICL and calibration to improve ranking performance by addressing order inconsistency.

5 Experiments

5.1 Experimental Setup

We utilize test sets from TREC, a standard dataset for information retrieval research. Specifically, we use the top 100 passages retrieved by BM25 Lin et al. (2021); Robertson et al. (2009) for each of the queries associated with the TREC-DL2019 and 2020 test sets Craswell et al. (2020). Our results are based on the re-ranking of these 100 passages. The LLM ranking scheme is implemented under the same experimental setting of PRP-Sort Qin et al. (2023). We use the rank aggregation implementation from Wang et al. (2024)

 $^{^{1}} https://github.com/nercms-mmap/RankAggregation-Lib\\$

	DL19	DL20
Setwise	63.25	60.27
Listwise (RankGPT)	69.61	65.49
Pairwise (PRP-Sort)	65.38	60.16
Pairwise+ICL+Calibration (Ours)	71.51	65.10

Table 5: NDCG@10 on TREC DL 2019 and 2020 datasets using Llama-3-8B model. Our proposed method (Pairwise+ICL+Calibration) shows superior performance compared to setwise, listwise, and standard pairwise approaches.

We evaluate our results using Normalized Discounted Cumulative Gain (NDCG). NDCG is a standard metric used to evaluate the quality of ranked retrieval results. It accounts for the position of relevant documents in the ranking, assigning higher importance to documents appearing earlier. We compare our results against pairwise, setwise, and listwise baselines Qin et al. (2023); Zhuang et al. (2023); Sun et al. (2023).

5.2 Addressing Order Inconsistency

We have shown that in-context learning can help to balance the average probability of the two choices given during pairwise ranking in Table 1. In Table 4, we can see that solely using ICL can help improve the ranking performance in most LLMs. The calibration addresses order inconsistency by calculating preference probability based on comparison from both positions. The improvement from solely using the calibration is also significant, as shown in Table 4. Furthermore, as demonstrated in Table 5, our approach of combining pairwise ranking with ICL and calibration outperforms several baseline methods across different datasets.

Avg. & SD		BubbleSort 70.84 ± 1.61
Borda de Borda (1784)	71.78	72.56
m MC4 Dwork et al. (2001)	72.45	72.71
m MC2 Dwork et al. (2001)	71.02	71.68
Mean Burges et al. (2011)	71.78	72.56
Median Fagin et al. (2003)	72.18	72.29
RRF Cormack et al. (2009)	71.96	72.33

Table 6: NDCG@10 of ranking list from different rank aggregation methods. In this experiment, there were 10 rankers with different ranking prompts. The dataset is TREC DL 2019 and the ranking model is Llama-3-8B. The Avg. & SD shows the mean and standard deviation of the NDCG@10 of ranking list proposals.

		Flan-T5-XXL	Llama-3-8B	Model A Borda	Aggregation MC4
	Pairwise.BubbleSort	71.05	71.51	73.19	73.16
	Pairwise.HeapSort	69.76	70.82	72.25	72.38
TREC DL	Setwise.BubbleSort	71.07	63.25	64.22	66.26
2019	Setwise.HeapSort	70.46	65.14	67.11	69.14
	Scheme Aggregation.Borda	70.60	71.52		
	Scheme Aggregation.MC4	70.61	71.47		
	Pairwise.BubbleSort	69.96	65.10	71.16	70.55
	Pairwise.HeapSort	69.61	64.01	69.67	69.32
TREC DL	Setwise.BubbleSort	68.66	60.27	61.85	63.08
2020	Setwise.HeapSort	68.82	60.68	63.85	65.27
	Scheme Aggregation.Borda	69.87	64.90		
	Scheme Aggregation.MC4	69.95	65.09		

Table 7: NDCG@10 of different ranking schemes and model aggregations on TREC DL 2019 and 2020 datasets. The table shows individual performance of Flan-T5-XXL and Llama-3-8B models, as well as their aggregation, across various ranking schemes. The pairwise ranking results in this table both apply ICL and calibration. The initial ranking lists are in the BM25 order.

5.3 Addressing Inconsistency via Aggregation

We show the performance of aggregation methods in Table 6 via aggregating the ranking list proposal from 10 different rankers. These 10 different rankers are constructed with different ranking prompts, we include the detailed discussion in Appendix A.7. We can see that both aggregation methods achieve an NDCG@10

higher than the average level of the ranking list proposals. We chose MC4 aggregation for its relatively high aggregation performance and Borda for its simplicity in implementation and popularity in various applications.

Table 7 demonstrates the effectiveness of both model and ranking scheme aggregation in improving ranking performance. Model Aggregation consistently outperforms individual models across both datasets, particularly for pairwise ranking. This trend is consistent across different ranking schemes and datasets, showing robustness through aggregation. Scheme Aggregation shows balanced performance, often achieving scores close to or exceeding the best individual scheme. This suggests that aggregating across ranking schemes can provide a more stable and potentially superior ranking, leveraging the strengths of both pairwise and setwise approaches, as well as different sorting algorithms. These results demonstrate that LLM-RankFusion can mitigate the impact of the weaknesses on an individual ranking scheme. We can also see the ranking scheme aggregation can help improve the robustness of ranking under the hard list condition in Table 9 in the Appendix.

	Model	TREC DL 2019 HeapSort BubbleSort		TREC DL 2020 HeapSort BubbleSort	
	Flan-T5-XXL	69.76	71.05	69.61	69.96
	Llama-3-8B	70.82	71.51	64.01	65.10
Individual	Llama-3-70B	73.41	74.55	70.11	70.83
marviadai	Gemma-2-9B	72.35	72.79	65.66	66.38
	Qwen 2.5-32B	74.17	73.91	69.58	70.19
	Mixtral-8x7B	70.53	71.16	66.73	66.14
Aggregation	Borda	75.01	74.65	70.25	71.32
Aggregation	MC4	74.80	74.56	71.12	71.65

Table 8: NDCG@10 of aggregated ranking list from ranking list proposal of LLM rankers with different models. It shows that the multi-model aggregation also balances out worse NDCG@10. The bubblesort and heapsort data associated with each model are referred to after ICL and calibration have been applied.

We further investigate the aggregation across LLMs, which attempts to produce a final ranking that is less sensitive to the individual biases of different LLMs. The result is shown in Table 8, as the aggregated ranking list can always achieve an NDCG@10 score higher than the best ranking list proposal. In addition to the TREC DL dataset results in Table 8, we also present the BEIR Thakur et al. (2021) dataset results in Table 10 in the Appendix A.1. This shows promising results of LLM-RankFusion to find a consensus ranking list that achieves balanced or even superior performance. In a typical passage ranking case, we don't assume we know which LLM is better at ranking the specific passage list. Hence, it is particularly useful if we can get at least medium performance rankings by aggregating multiple proposals.

5.4 Computation Cost

The performance of LLM-based passage ranking is mainly determined by the LLM inference performance and the number of comparisons required to sort a list. The ranking list proposals required by LLM-RankFusion are independent of each other. Hence, the LLM rankers can run in parallel, which means the ranking latency is close to a single LLM ranker. The calibration doesn't bring additional inference costs because it only collects the output logits and calculates preference probability based on two permutations of passages. The ICL leads to a longer prompt, which slightly increases the computation during inference as shown in Table 16 in the appendix. The time and space complexity of ranking an individual ranking list proposal is the same as the previous PRP-Sorting Qin et al. (2023).

6 Conclusion

In this paper, we focus on addressing order inconsistency and transitive inconsistency we identify in LLM-based ranking. These inconsistencies can significantly impact the reliability of LLM-based ranking systems.

To mitigate these issues, we proposed the LLM-RankFusion pipeline, which incorporates in-context learning (ICL) and calibration to address order inconsistency and rank aggregation to tackle transitive inconsistency. Our experiments demonstrated that ICL and calibration effectively reduce order inconsistency, leading to improved NDCG scores. Furthermore, we showed that aggregation mitigates transitive inconsistency by forming a consensus from multiple ranking lists. By exploring the idea of aggregating the decisions of multiple LLMs in the specific domain of passage ranking, our work highlights the potential of combining the strengths of different LLMs.

References

- Josh Achiam, Steven Adler, Sandhini Agarwal, Lama Ahmad, Ilge Akkaya, Florencia Leoni Aleman, Diogo Almeida, Janko Altenschmidt, Sam Altman, Shyamal Anadkat, et al. Gpt-4 technical report. arXiv preprint arXiv:2303.08774, 2023.
- Payal Bajaj, Daniel Campos, Nick Craswell, Li Deng, Jianfeng Gao, Xiaodong Liu, Rangan Majumder, Andrew McNamara, Bhaskar Mitra, Tri Nguyen, et al. Ms marco: A human generated machine reading comprehension dataset. arXiv preprint arXiv:1611.09268, 2016.
- Luiz Bonifacio, Vitor Jeronymo, Hugo Queiroz Abonizio, Israel Campiotti, Marzieh Fadaee, Roberto Lotufo, and Rodrigo Nogueira. mmarco: A multilingual version of the ms marco passage ranking dataset. arXiv preprint arXiv:2108.13897, 2021.
- Tom Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared D Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, et al. Language models are few-shot learners. Advances in neural information processing systems, 33:1877–1901, 2020.
- Christopher Burges, Krysta Svore, Paul Bennett, Andrzej Pastusiak, and Qiang Wu. Learning to rank using an ensemble of lambda-gradient models. In *Proceedings of the learning to rank Challenge*, pp. 25–35. PMLR, 2011.
- Wenshuo Chao, Zhi Zheng, Hengshu Zhu, and Hao Liu. Make large language model a better ranker. arXiv preprint arXiv:2403.19181, 2024.
- Hyung Won Chung, Le Hou, Shayne Longpre, Barret Zoph, Yi Tay, William Fedus, Yunxuan Li, Xuezhi Wang, Mostafa Dehghani, Siddhartha Brahma, et al. Scaling instruction-finetuned language models. Journal of Machine Learning Research, 25(70):1–53, 2024.
- Gordon V Cormack, Charles LA Clarke, and Stefan Buettcher. Reciprocal rank fusion outperforms condorcet and individual rank learning methods. In *Proceedings of the 32nd international ACM SIGIR conference on Research and development in information retrieval*, pp. 758–759, 2009.
- Nick Craswell, Bhaskar Mitra, Emine Yilmaz, Daniel Campos, and Ellen M Voorhees. Overview of the trec 2019 deep learning track. arXiv preprint arXiv:2003.07820, 2020.
- de Borda. Mémoire sur les elections par scrutin (memoir on elections by ballot), 1784.
- Andrew Drozdov, Honglei Zhuang, Zhuyun Dai, Zhen Qin, Razieh Rahimi, Xuanhui Wang, Dana Alon, Mohit Iyyer, Andrew McCallum, Donald Metzler, and Kai Hui. Parade: Passage ranking using demonstrations with large language models, 2023.
- Paul Duetting, Vahab Mirrokni, Renato Paes Leme, Haifeng Xu, and Song Zuo. Mechanism design for large language models. arXiv preprint arXiv:2310.10826, 2023.
- Cynthia Dwork, Ravi Kumar, Moni Naor, and D Sivakumar. Rank aggregation revisited, 2001.
- Ronald Fagin, Ravi Kumar, and Dandapani Sivakumar. Efficient similarity search and classification via rank aggregation. In *Proceedings of the 2003 ACM SIGMOD international conference on Management of data*, pp. 301–312, 2003.

- Mohamed Farah and Daniel Vanderpooten. An outranking approach for rank aggregation in information retrieval. In *Proceedings of the 30th annual international ACM SIGIR conference on Research and development in information retrieval*, pp. 591–598, 2007.
- Lukas Gienapp, Maik Fröbe, Matthias Hagen, and Martin Potthast. Sparse pairwise re-ranking with pretrained transformers. In *Proceedings of the 2022 ACM SIGIR International Conference on Theory of Information Retrieval*, pp. 72–80, 2022.
- Reinhard Heckel, Nihar B Shah, Kannan Ramchandran, and Martin J Wainwright. Active ranking from pairwise comparisons and when parametric assumptions do not help. 2019.
- Cheng-Yu Hsieh, Yung-Sung Chuang, Chun-Liang Li, Zifeng Wang, Long Le, Abhishek Kumar, James Glass, Alexander Ratner, Chen-Yu Lee, Ranjay Krishna, et al. Found in the middle: Calibrating positional attention bias improves long context utilization. In *Findings of the Association for Computational Linguistics:* ACL 2024, pp. 14982–14995, 2024.
- Albert Q Jiang, Alexandre Sablayrolles, Antoine Roux, Arthur Mensch, Blanche Savary, Chris Bamford, Devendra Singh Chaplot, Diego de las Casas, Emma Bou Hanna, Florian Bressand, et al. Mixtral of experts. arXiv preprint arXiv:2401.04088, 2024.
- Konrad Kułakowski. Inconsistency in the ordinal pairwise comparisons method with and without ties. European Journal of Operational Research, 270(1):314–327, 2018.
- Yongqi Li, Xinyu Lin, Wenjie Wang, Fuli Feng, Liang Pang, Wenjie Li, Liqiang Nie, Xiangnan He, and Tat-Seng Chua. A survey of generative search and recommendation in the era of large language models. arXiv preprint arXiv:2404.16924, 2024.
- Percy Liang, Rishi Bommasani, Tony Lee, Dimitris Tsipras, Dilara Soylu, Michihiro Yasunaga, Yian Zhang, Deepak Narayanan, Yuhuai Wu, Ananya Kumar, Benjamin Newman, Binhang Yuan, Bobby Yan, Ce Zhang, Christian Cosgrove, Christopher D. Manning, Christopher Ré, Diana Acosta-Navas, Drew A. Hudson, Eric Zelikman, Esin Durmus, Faisal Ladhak, Frieda Rong, Hongyu Ren, Huaxiu Yao, Jue Wang, Keshav Santhanam, Laurel Orr, Lucia Zheng, Mert Yuksekgonul, Mirac Suzgun, Nathan Kim, Neel Guha, Niladri Chatterji, Omar Khattab, Peter Henderson, Qian Huang, Ryan Chi, Sang Michael Xie, Shibani Santurkar, Surya Ganguli, Tatsunori Hashimoto, Thomas Icard, Tianyi Zhang, Vishrav Chaudhary, William Wang, Xuechen Li, Yifan Mai, Yuhui Zhang, and Yuta Koreeda. Holistic evaluation of language models. 2023.
- Jimmy Lin, Xueguang Ma, Sheng-Chieh Lin, Jheng-Hong Yang, Ronak Pradeep, and Rodrigo Nogueira. Pyserini: An easy-to-use python toolkit to support replicable ir research with sparse and dense representations, 2021.
- Shili Lin. Rank aggregation methods. Wiley Interdisciplinary Reviews: Computational Statistics, 2(5): 555–570, 2010.
- Tie-Yan Liu et al. Learning to rank for information retrieval. Foundations and Trends® in Information Retrieval, 3(3):225–331, 2009.
- Yao Lu, Max Bartolo, Alastair Moore, Sebastian Riedel, and Pontus Stenetorp. Fantastically ordered prompts and where to find them: Overcoming few-shot prompt order sensitivity. arXiv preprint arXiv:2104.08786, 2021.
- Xueguang Ma, Xinyu Zhang, Ronak Pradeep, and Jimmy Lin. Zero-shot listwise document reranking with a large language model. arXiv preprint arXiv:2305.02156, 2023.
- Rodrigo Nogueira and Kyunghyun Cho. Passage re-ranking with bert. arXiv preprint arXiv:1901.04085, 2019.
- R OpenAI. Gpt-4 technical report. arXiv, pp. 2303-08774, 2023.

- Ronak Pradeep, Rodrigo Nogueira, and Jimmy Lin. The expando-mono-duo design pattern for text ranking with pretrained sequence-to-sequence models. arXiv preprint arXiv:2101.05667, 2021.
- Zhen Qin, Rolf Jagerman, Kai Hui, Honglei Zhuang, Junru Wu, Jiaming Shen, Tianqi Liu, Jialu Liu, Donald Metzler, Xuanhui Wang, et al. Large language models are effective text rankers with pairwise ranking prompting. arXiv preprint arXiv:2306.17563, 2023.
- Siddartha Y Ramamohan, Arun Rajkumar, and Shivani Agarwal. Dueling bandits: Beyond condorcet winners to general tournament solutions. Advances in Neural Information Processing Systems, 29, 2016.
- Stephen Robertson, Hugo Zaragoza, et al. The probabilistic relevance framework: Bm25 and beyond. Foundations and Trends® in Information Retrieval, 3(4):333–389, 2009.
- Devendra Singh Sachan, Mike Lewis, Mandar Joshi, Armen Aghajanyan, Wen tau Yih, Joelle Pineau, and Luke Zettlemoyer. Improving passage retrieval with zero-shot question generation, 2023.
- Frans Schalekamp and Anke van Zuylen. Rank aggregation: Together we're strong. In 2009 Proceedings of the Eleventh Workshop on Algorithm Engineering and Experiments (ALENEX), pp. 38–51. SIAM, 2009.
- Weiwei Sun, Lingyong Yan, Xinyu Ma, Shuaiqiang Wang, Pengjie Ren, Zhumin Chen, Dawei Yin, and Zhaochun Ren. Is chatgpt good at search? investigating large language models as re-ranking agents, 2023.
- Raphael Tang, Xinyu Zhang, Xueguang Ma, Jimmy Lin, and Ferhan Ture. Found in the middle: Permutation self-consistency improves listwise ranking in large language models. arXiv preprint arXiv:2310.07712, 2023.
- Yi Tay, Mostafa Dehghani, Vinh Q Tran, Xavier Garcia, Jason Wei, Xuezhi Wang, Hyung Won Chung, Siamak Shakeri, Dara Bahri, Tal Schuster, et al. Ul2: Unifying language learning paradigms. arXiv preprint arXiv:2205.05131, 2022.
- Gemma Team, Thomas Mesnard, Cassidy Hardin, Robert Dadashi, Surya Bhupatiraju, Shreya Pathak, Laurent Sifre, Morgane Rivière, Mihir Sanjay Kale, Juliette Love, et al. Gemma: Open models based on gemini research and technology. arXiv preprint arXiv:2403.08295, 2024a.
- Gemma Team, Morgane Riviere, Shreya Pathak, Pier Giuseppe Sessa, Cassidy Hardin, Surya Bhupatiraju, Léonard Hussenot, Thomas Mesnard, Bobak Shahriari, Alexandre Ramé, et al. Gemma 2: Improving open language models at a practical size. arXiv preprint arXiv:2408.00118, 2024b.
- Nandan Thakur, Nils Reimers, Andreas Rücklé, Abhishek Srivastava, and Iryna Gurevych. Beir: A heterogenous benchmark for zero-shot evaluation of information retrieval models. arXiv preprint arXiv:2104.08663, 2021.
- Hugo Touvron, Thibaut Lavril, Gautier Izacard, Xavier Martinet, Marie-Anne Lachaux, Timothée Lacroix, Baptiste Rozière, Naman Goyal, Eric Hambro, Faisal Azhar, et al. Llama: Open and efficient foundation language models. arXiv preprint arXiv:2302.13971, 2023.
- Peiyi Wang, Lei Li, Liang Chen, Dawei Zhu, Binghuai Lin, Yunbo Cao, Qi Liu, Tianyu Liu, and Zhifang Sui. Large language models are not fair evaluators. arXiv preprint arXiv:2305.17926, 2023.
- Siyi Wang, Qi Deng, Shiwei Feng, Hong Zhang, and Chao Liang. A survey on rank aggregation. In *Proceedings* of the Thirty-Third International Joint Conference on Artificial Intelligence (IJCAI-24), pp. 8281–8289, 2024.
- Likang Wu, Zhi Zheng, Zhaopeng Qiu, Hao Wang, Hongchao Gu, Tingjia Shen, Chuan Qin, Chen Zhu, Hengshu Zhu, Qi Liu, et al. A survey on large language models for recommendation. arXiv preprint arXiv:2305.19860, 2023.
- An Yang, Baosong Yang, Beichen Zhang, Binyuan Hui, Bo Zheng, Bowen Yu, Chengyuan Li, Dayiheng Liu, Fei Huang, Haoran Wei, et al. Qwen2. 5 technical report. arXiv preprint arXiv:2412.15115, 2024.

Yifan Zeng, Yiran Wu, Xiao Zhang, Huazheng Wang, and Qingyun Wu. Autodefense: Multi-agent llm defense against jailbreak attacks. arXiv preprint arXiv:2403.04783, 2024.

Wayne Xin Zhao, Kun Zhou, Junyi Li, Tianyi Tang, Xiaolei Wang, Yupeng Hou, Yingqian Min, Beichen Zhang, Junjie Zhang, Zican Dong, et al. A survey of large language models. arXiv preprint arXiv:2303.18223, 2023.

Yutao Zhu, Huaying Yuan, Shuting Wang, Jiongnan Liu, Wenhan Liu, Chenlong Deng, Zhicheng Dou, and Ji-Rong Wen. Large language models for information retrieval: A survey. arXiv preprint arXiv:2308.07107, 2023.

Shengyao Zhuang, Honglei Zhuang, Bevan Koopman, and Guido Zuccon. A setwise approach for effective and highly efficient zero-shot ranking with large language models, 2023.

A Appendix

Dataset	Ranking Scheme	Flan-T5-XXL	Llama-3-8B
	Pairwise.BubbleSort	68.66	68.71
	Pairwise.HeapSort	71.07	70.94
TREC DL	Setwise.BubbleSort	67.66	40.77
2019	Setwise.HeapSort	69.89	62.15
	Listwise (RankGPT)	51.85	64.94
	Scheme Aggregation		56.05
	Pairwise.BubbleSort	66.75	61.64
	Pairwise.HeapSort	68.97	64.10
TREC DL	Setwise.BubbleSort	63.96	37.59
2019	Setwise.HeapSort	68.32	55.30
	Listwise (RankGPT)	52.86	63.48
	Scheme Aggregation	61.07	51.20

Table 9: Aggregation across ranking schemes on Hard List using Borda.

A.1 Additional Experiments

In Table 3, we show the hard list can reduce the ranking quality. By applying LLM-RankFusion, we can mitigate the negative effect of the hard list as shown in Table 9. We show the experiment results on the **BEIR dataset** Thakur et al. (2021) in Table 10. It indicates that LLM-RankFusion can easily generalize to different datasets.

A.2 Future Work

Future Work can focus on LLM-based rank aggregation approaches that decide the comparison strategy onthe-fly and directly aggregate from pairwise comparisons without relying on sorting algorithms Ramamohan et al. (2016); Heckel et al. (2019); Gienapp et al. (2022). Exploring the potential of aggregating LLM-based decisions in other tasks and domains beyond passage ranking could lead to a more general understanding of the effectiveness of combining the intelligence of multiple LLMs for improved performance and consistency in a wider range of applications Duetting et al. (2023).

A.3 Example Passage Ranking

We show an example passage ranking that contain 15 passages for a query. The details of these 15 passages are shown in Table 12 and Table 13. The ranking results from different settings are shown in Table 14.

	Model	Sort	trec-covid	signal1m	trec-news	webis-touche2020
	Llama-3-8B	HeapSort BubbleSort	81.69 81.42	29.07 31.27	47.00 48.27	22.96 25.83
	Llama-3-70B	HeapSort BubbleSort	82.05 81.06	$32.20 \\ 34.15$	$51.48 \\ 52.24$	28.02 30.70
Individual	Gemma-2-9B	HeapSort BubbleSort	78.76 78.96	$30.21 \\ 32.04$	$48.10 \\ 48.85$	22.87 27.32
	Qwen2.5-32B	HeapSort BubbleSort	84.65 84.80	$33.06 \\ 34.20$	$54.20 \\ 54.39$	$30.54 \\ 32.90$
	Mixtral-8x7B	HeapSort BubbleSort	82.16 83.00	29.24 33.06	$50.84 \\ 51.27$	26.48 31.47
Aggregation	Borda	HeapSort BubbleSort	83.68 84.01	32.06 34.80	51.73 53.32	26.55 32.35
11991 98001011	MC4	HeapSort BubbleSort	83.51 83.50	33.14 34.43	51.83 52.66	26.68 30.09

Table 10: NDCG@10 of aggregated ranking list from ranking list proposal of LLM rankers with different models on **BEIR dataset**. It shows that the multi-model aggregation also balances out worse NDCG@10. The bubblesort and heapsort data associated with each model are referred to after ICL and calibration have been applied.

	DL19	DL20	BEIR trec-covid	BEIR trec-news
Setwise	63.25	60.27	75.65	47.72
Listwise (RankGPT)	69.61	65.49	80.90	50.23
Pairwise (PRP-Sort)	65.38	60.16	75.44	47.82
Pairwise+ICL+Calibration (Ours)	71.51	65.10	81.42	48.27

Table 11: NDCG@10 on TREC DL and BEIR tree-covid and tree-news subsets, using Llama-3-8B. Our approach (Pairwise + ICL + Calibration) consistently demonstrates superior performance compared to setwise, listwise, and standard pairwise baselines, reinforcing our claim on effectively addressing intrinsic inconsistencies in LLM-based ranking.

A.4 Implementation details

We use LLMs with a variety of sizes in our experiments: **GPT** OpenAI (2023): GPT-4-1106; **LLaMA-3** Touvron et al. (2023): LLaMA-3-70B, LLaMA-3-8B; **Qwen2.5** Yang et al. (2024): Qwen2.5-32B-Instruct **Mixtral** Jiang et al. (2024): Mixtral-8x7b-v0.1; **Gemma2** Team et al. (2024a;b) gemma-2-9b-it; **Flan-T5** Chung et al. (2024); Tay et al. (2022) Flan-T5-XXL. This aims to explore the capacity of different sizes of LLMs and the trade-off between efficiency and ranking quality.

The LLM inference is implemented based on Hugging Face. The instruction fine-tuned version of the model is used if available. The temperature of LLM is set to 0, which means argmax will be applied to the candidate tokens during generation. We use 2 × NVIDIA H100 80 GB HBM3 and 4 × Tesla V100-SXM3-32 GB GPUs to run our experiment.

A.5 Prompt

We show a comparison prompt example in Table 15. The first two rounds of chat is the in-context Learning (ICL) prompt. We expect the LLM can learn the order-agnostic property from the demonstration of ICL prompt.

Passage Identifier	Passage Content	Relevance
A	Well, one of Arnold's biggest insights is what resulted in the invention of the Searzall, and it's something we got wrong in our sous vide video. Sous vide, if you recall, is the process of cooking food in a controlled-temperature water bath, using a vacuum sealer to protect your meat from the liquid. What you get from sous vide is your food cooked to exactly the temperature you want to kill bacteria and make it safe to eat, but not overcooking it.	0
В	What kind of foods can you cook sous vide? Sous vide is traditionally seen as an alternative method for cooking meats. However, the technique is extremely versatile, meaning all manner of ingredients can be cooked such as: Pork, Lamb, Beef, Chicken, Duck, Turkey, Quail.	3
C	What is a Sous Vide Cooker? We said it before and we'll say it again: a sous vide machine is a better way to cook. When you use a sous vide at home, you'll be cooking with water. It's not at all what you're thinking. Your steak and chicken – any food really – will be placed in BPA-free, sturdy plastic bags and cooked.	2
D	Sous-vide cooking involves cooking food in sealed plastic bags immersed in hot water for long periods of time. Depending on the cut, type, and thickness of the meat or the type of food in question, cooking sous-vide for several hours is not out of the ordinary. The key is managing the temperature of the water so it stays hot enough to cook the food thoroughly and evenly and long enough to kill any food-borne pathogens that may be in the bag along with the food.	0
E	Actually vacuum is a mis-represented concept in sous vide. Fact is, you don't need vacuum sealing entirely for sous vide cooking. If you can truly control the temperature of the water bath then all you need is to provide the food you are cooking a barrier from the water bath.	0
F	Often, however, when you prepare food sous vide you're packaging the food in plastic. (Often but not always. Eggs come in their own wrappers—their shells—and we can sous vide foods that set as they cook, like custard, yogurt, and chicken liver pâté, in glass canning jars.)	3
G	The term sous vide (pronounced soo–veed) is a French term, meaning under vacuum. Sous vide is a culinary technique in which vacuum-sealed food is immersed in a water bath and cooked at a very precise, consistent temperature. This cooking technique typically involves cooking food for longer periods of time at a lower temperature. He term sous vide (pronounced soo–veed) is a French term, meaning under vacuum. The term s ous vide (pronounced soo–veed) is a French term, meaning under vacuum.	0
Н	The sous vide technique has been the secret of great chefs worldwide for decades. The SousVide Supreme is an amazing new all-in-one sous vide water oven designed to bring the sous vide cooking technique into home kitchens and restaurants at an affordable price. The sous vide (pronounced soo-veed) technique involves cooking food in vacuum-sealed pouches submerged in a water bath held at a precisely-controlled temperature.	0
I	Sous vide recipes. Sous vide recipes. From the French for 'under vacuum', sous vide is a method of cooking where ingredients are sealed in an airtight bag and submerged in a water bath. This method not only ensures a constant cooking temperature, but allows the food to cook for long periods of time without losing any of its flavour or moisture.	0

Table 12: Top 15 relevant passages for query what types of food can you cook sous vide from BM25 (Part 1 of 2). These passages are ranked by BM25 and assigned the Passage Identifier from A to O in alphabetical order. We refer to this as the BM25 order, which is used as the initial order for LLM-RankFusion. The Relevance column shows the ground truth pointwise relevance score label. The relevance scores are from 0 to 3, where 0 is the most not relevance, 3 is the most relevance.

Passage Identifier	Passage Content	Relevance
J	Slow and low is the name of the game here. Some times cooking food sous vid means hours, sometimes it means entire days. Food safety is a concern, but doesn' generally an issue as long as you stick to the temperature and cooking time specified for the food you're cooking.imply put, sous vide cooking is the process of vacuum-sealing raw food in plastic pouches and cooking it slowly in a temperature controlled water bath.	
K	Learn more sous vide at http://www.sousvidesupreme.com—WHAT IS SOUS VIDE? —The sous vide technique has been the secret of great chefs worldwide for decades. The SousVide Supreme is an amazing new all-in-one sous vide water oven designed to bring the sous vide cooking technique into home kitchens and restaurants at an affordable price.	
L	All kinds! Any type of meat—such as beef, pork, lamb, game, or poultry—is ideal for sous vide. It works especially well with fish and seafood, ensuring that these delicate foods are not overcooked. Almost any vegetable can also be cooked sous vide with delicious results, as can eggs and many fruits. You can even use it to make custard-style ice cream base, béarnaise sauce, crème Anglaise, custards, cheese, yogurt, and even cakes.	3
M	Sous Vide help - why did my salmon dry out at 120? Updated 1 month ago 8. Sous Vide Salmon; 3 What temperature do I cook these foods on? Updated 3 months ago 1. Chicken Breast Cookbooks Steak Beginner Cook Scrambling; 4 Potato encrusted salmon. Updated 1 month ago 1. Salmon Potatoes Recipe Fixes; 5 What temperature do you have the grill on when cooking steak?	1
N	Here's our answer: Water used to cook food sous vide is still clean and sanitary (provided your bag doesn't break or leak), so you can use it to wash dishes, water your plants, hydrate your dog, bathe your baby, or fill your swimming pool. You can also use that water to cook sous vide several times, if you have the space to keep it.	0
O	With the Anova, sous vide cooking is simple. All you need to get started is a pot or large container to hold water, heavy duty bags, a few clips, and your Anova Precision Cooker, of course! One of the best parts of sous vide cooking is that you don't need to do much to your food before cooking.	

Table 13: Top 15 relevant passages for query what types of food can you cook sous vide from BM25 (Part 2 of 2). More details in Table 12.

Ranking Method	Ranking List
BM25	$\mathbf{A} \succ \mathbf{B} \succ \mathbf{C} \succ \mathbf{D} \succ \mathbf{E} \succ \mathbf{F} \succ \mathbf{G} \succ \mathbf{H} \succ \mathbf{I} \succ \mathbf{J} \succ \mathbf{K} \succ \mathbf{L} \succ \mathbf{M} \succ \mathbf{N} \succ \mathbf{O}$
GPT-4	$L \succ B \succ D \succ F \succ I \succ J \succ C \succ H \succ G \succ O \succ A \succ E \succ M \succ N \succ K$
Llama-3-70B	$L \succ B \succ F \succ I \succ A \succ M \succ D \succ J \succ H \succ O \succ C \succ E \succ K \succ G \succ N$
LLM-RankFusion	$\mathbf{L} \succ \mathbf{B} \succ \mathbf{I} \succ \mathbf{D} \succ \mathbf{F} \succ \mathbf{J} \succ \mathbf{A} \succ \mathbf{C} \succ \mathbf{H} \succ \mathbf{G} \succ \mathbf{O} \succ \mathbf{M} \succ \mathbf{E} \succ \mathbf{K} \succ \mathbf{N}$

Table 14: Comparisons of the rankings from different LLMs and aggregation. The rankings are produced by LLM-based pairwise ranker using bubblesort. We include ICL and calibration in each individual LLM-based ranker.

Passage A: "Forensic anthropology is the application of the science of physical anthropology and human osteology in a legal setting, most often in criminal cases where the victims remains are in the advanced stages of decomposition, nvironmental anthropology is a sub-specialty within the field of anthropology that takes an active role in examining the relationships between humans and their environment across space and time." Passage B: "Graduate Study in Anthropology. The graduate program in biological anthropology at CU Boulder offers training in several areas, including primatology, human biology, and paleoanthropology. We share an interest in human ecology, the broad integrative area of anthropology that focuses on the interactions of culture, biology and the environment." Output Passage A or Passage B: Assistant Passage: Given a query "anthropological definition of environment", which of the following two passages is more relevant to the query? Passage A: "Graduate Study in Anthropology. The graduate program in biological anthropology and paleoanthropology. We share an interest in human ecology, the broad integrative area of anthropology that focuses on the interactions of culture, biology and the environment." Passage B: "Forensic anthropology is the application of the science of physical anthropology and human osteology in a legal setting, most often in criminal cases where the victims remains are in the advanced stages of decomposition,nvironmental anthropology is a sub-specialty within the field of anthropology that takes an active role in examining the relationships between humans and their environment across space and time." Output Passage A or Passage B: Given a query "what types of food can you cook sous vide", which of the following two passages is more relevant to the query? Passage A: "What is a Sous Vide Cooker? We said it before and we'll say it again: a sous vide machine is a better way to cook. When you use a sous vide at home, you'll be cooking with water. It's not at all what you'r	User	Given a query "anthropological definition of environment", which of the following two passages is more relevant to the query?		
User Given a query "anthropological definition of environment", which of the following two passages is more relevant to the query? Passage A: "Graduate Study in Anthropology. The graduate program in biological anthropology at CU Boulder offers training in several areas, including primatology, human biology, and paleoanthropology. We share an interest in human ecology, the broad integrative area of anthropology that focuses on the interactions of culture, biology and the environment." Passage B: "Forensic anthropology is the application of the science of physical anthropology and human osteology in a legal setting, most often in criminal cases where the victim's remains are in the advanced stages of decomposition.nvironmental anthropology is a sub-specialty within the field of anthropology that takes an active role in examining the relationships between humans and their environment across space and time." Output Passage B User Given a query "what types of food can you cook sous vide", which of the following two passages is more relevant to the query? Passage A: "What is a Sous Vide Cooker? We said it before and we'll say it again: a sous vide machine is a better way to cook. When you use a sous vide at home, you'll be cooking with water. It's not at all what you're thinking. Your steak and chicken – any food really – will be placed in BPA-free, sturdy plastic bags and cooked." Passage B: "Often, however, when you prepare food sous vide you're packaging the food in plastic. (Often but not always. Eggs come in their own wrappers—their shells—and we can sous vide foods that set as they cook, like custard, yogurt, and chicken liver pâté, in glass canning jars.) " Output Passage A or Passage B:		Passage A: "Forensic anthropology is the application of the science of physical anthropology and human osteology in a legal setting, most often in criminal cases where the victims remains are in the advanced stages of decomposition.nvironmental anthropology is a sub-specialty within the field of anthropology that takes an active role in examining the relationships between humans and their environment across space and time." Passage B: "Graduate Study in Anthropology. The graduate program in biological anthropology at CU Boulder offers training in several areas, including primatology, human biology, and paleoanthropology. We share an interest in human ecology, the broad integrative area of anthropology that focuses on the interactions of culture, biology and the environment."		
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	Assistant	Passage:		

Table 15: An example of prompt for a pairwise comparison with ICL. For open-source LLMs, we can explicitly set the start of the last assistant's message to begin with "Passage:". So that the LLM will generate the next token from "A" or "B".

Model	With ICL - Time (s)	Without ICL - Time (s)	Ratio
Gemma-2-9B	0.0217	0.0161	1.3487
Llama-3-70B	0.0191	0.0176	1.0840
Mistral-8x7B	0.0194	0.0177	1.0974
${\rm Qwen 2.5\text{-}32B}$	0.0198	0.0129	1.5439

Table 16: Performance benchmarking (avg. time/query). The inference overhead introduced by ICL with advanced KV-cache optimization is now substantially less than 2x, alleviating computational resource concerns previously indicated.

A.6 Performance

The average number of comparisons required to rank a list is 3574.21 ± 501.23 for Bubblesort and 972.77 ± 47.69 for Heapsort. We benchmark the comparison rate of different LLM rankers in Table 16. The prompt is longer after applying ICL, which decreases the LLM inference performance. We only generate 1 token for each comparison on those open-source LLMs. Each pairwise comparison involves prompting the LLM in two different passage permutations. It requires 2 prompts and generate operations to finish a single pairwise comparison. We using an optimized inference setup (vLLM 0.7.3, KV caching, and 2xH200 GPUs with prefix-caching enabled).

A.7 Analysis of Prompt Design Sensitivity

Model	Baseline	ICL Only	Calibration Only	ICL + Calibration
Bubblesort Heapsort	62.68 ± 3.07 63.82 ± 4.63	0	69.59 ± 1.89 68.30 ± 2.24	$70.84{\pm}1.61 \ 70.10{\pm}1.92$

Table 17: NDCG@10 scores (mean \pm std) across different prompt designs

To evaluate the robustness of our proposed methods against variations in prompt design, we conducted additional experiments using GPT-4 to generate 10 different pairwise ranking prompt templates. Each template maintained the core task of comparing passage relevance while varying factors such as wording, formatting, and instruction style. We tested these prompts using Llama-3-8B on the TREC-DL2019 dataset under different configurations. The results in Table 17 demonstrate two key benefits of our approach:

- 1. **Enhanced Performance:** The combination of ICL and calibration substantially improves ranking quality, with NDCG scores increasing by approximately 8 points compared to the baseline across both sorting algorithms.
- 2. **Reduced Variance:** The baseline exhibits considerable sensitivity to prompt design, as evidenced by the high standard deviations (3.07-4.63). In contrast, configurations using ICL and calibration show markedly lower variance (1.61-1.92), indicating more stable performance across different prompt designs.