Personalized Subgraph Federated Learning

Anonymous Author(s) Affiliation Address email

Abstract

1	In real-world scenarios, subgraphs of a larger global graph may be distributed
2	across multiple devices or institutions, and only locally accessible due to privacy re-
3	strictions, although there may be links between them. Recently proposed subgraph
4	Federated Learning (FL) methods deal with those missing links across private local
5	subgraphs while distributively training Graph Neural Networks (GNNs) on them.
6	However, they have overlooked the inevitable heterogeneity among subgraphs,
7	caused by subgraphs comprising different parts of a global graph. For example,
8	a subgraph may belong to one of the communities within the larger global graph.
9	A naive subgraph FL in such a case will collapse incompatible knowledge from
10	local GNN models trained on heterogeneous graph distributions. To overcome
11	such a limitation, we introduce a new subgraph FL problem, personalized subgraph
12	FL, which focuses on the joint improvement of the interrelated local GNN models
13	rather than learning a single global GNN model, and propose a novel framework,
14	FEDerated Personalized sUBgraph learning (FED-PUB), to tackle it. A crucial
15	challenge in personalized subgraph FL is that the server does not know which
16	subgraph each client has. FED-PUB thus utilizes functional embeddings of the
17	local GNNs using random graphs as inputs to compute similarities between them,
18	and use them to perform weighted averaging for server-side aggregation. Further,
19	it learns a personalized sparse mask at each client to select and update only the
20	subgraph-relevant subset of the aggregated parameters. We validate FED-PUB for
21	its subgraph FL performance on six datasets, considering both non-overlapping
22	and overlapping subgraphs, on which ours largely outperforms relevant baselines.

23 1 Introduction

A graph, which defines the relationships among instances, can model a wide range of structured data 24 including social [7], co-purchasing [23], and collaboration networks [36]. Most of the previous works 25 on graph representation learning focus on a single graph, whose nodes and edges collected from 26 multiple sources are stored in a central server. For instance, in a social network platform, every user, 27 with his/her social networks, contributes to creating a giant network consisting of all users and their 28 connections. However, in some practical scenarios, each user/institution collects its own private graph, 29 which is only locally accessible due to privacy restrictions. For instance, as described in Zhang et al. 30 [45], each hospital may have its own patient interaction network to track their physical contacts or 31 co-diagnosis of a disease, however, such a graph may not be shared with others. An obvious challenge 32 for such a scenario is how to deal with potentially missing edges between subgraphs [42, 45] that are 33 not captured by individual data owners, that may carry important information (See Figure 1 (A)). 34

How can we then collaboratively train, without sharing actual data, a neural network with its subgraphs
distributed across multiple participants (i.e., clients) over different devices or institutions? The most
straightforward way is to perform Federated Learning (FL) with Graph Neural Networks (GNNs). In
particular, in such an FL framework, each client will individually train a local GNN on the private

Submitted to 36th Conference on Neural Information Processing Systems (NeurIPS 2022). Do not distribute.



Figure 1: (A) An illustration of local subgraphs distributed across multiple participants with overlapping nodes, missing edges and community structures between subgraphs. (B) Existing subgraph FL methods [42, 45] expand the local subgraphs to tackle the missing edge problem, but collapse incompatible knowledge from heterogeneous subgraphs. (C) Our personalized subgraph FL focuses on the joint improvement of local models working on interrelated subgraphs, such as ones within the same community, by selectively sharing knowledge across them. (Right:) Knowledge collapse results, where local models belonging to two small communities (Comm 1 and 2) suffer from large performance degeneration by existing subgraph FL (e.g., FedGNN [42] and FedSage+ [45]). A personalized FL method, FedPer [2] also underperforms ours since it only focuses on individual model's improvement without sharing local personalization layers between similar subgraphs.

local data, while a central server aggregates the locally updated GNN weights from multiple clients into one, and then transmits it back to the clients. Recent subgraph FL methods work in such a manner [42, 45] while additionally tackling the problem of missing edges between subgraphs. This is done as illustrated in Figure 1 (B), where the local subgraph is expanded either by exactly augmenting the relevant nodes from the other subgraphs at the other clients [42], or by estimating the nodes using the node information in the other subgraphs [45]. However, such sharing of node information may compromise data privacy and can incur high communication costs.

Also, there exists a more important challenge that has been overlooked by the existing subgraph FL 46 47 methods. We observe that they suffer from large performance degeneration (See Figure 1 right), due 48 to a lack of consideration of the *heterogeneity* among the subgraphs, which is natural since subgraphs comprise different parts of a global graph. Notably, there could be multiple communities within 49 a global graph, each of which is formed by a group of densely connected subgraphs with similar 50 characteristics (Figure 1 (A)). For example, some of patient networks from hospitals can be grouped 51 by their specialized sectors according to the disease categories, namely psychiatric or ophthalmology. 52 Motivated by this challenge, we introduce a novel problem of personalized subgraph FL, whose goal 53

54 is the joint improvement of interrelated local models trained on the interconnected local subgraphs, for instance, subgraphs belonging to the same community (See Figure 1 (C)), by sharing weights 55 among them. However, tackling personalized subgraph FL is challenging, since we do not know 56 which subgraph each client has, due to their local accessibility. To resolve this issue, we use functional 57 embeddings of GNNs on random graphs to obtain similarity scores between two local GNNs, inspired 58 by a work for neural network search that effectively represents entire neural networks in the vector 59 space [17], and then use them to perform weighted averaging of the model weights at the server. 60 However, the similarity scores only tell how relevant each local model from the other clients is, but 61 not which of the parameters are relevant. Thus we further learn and apply personalized sparse masks 62 on the local GNN at each client to obtain only the subnetwork, relevant for the local subgraph. We 63 refer to this subgraph FL framework as FEDerated Personalized sUBgraph learning (FED-PUB). 64

We extensively validate our FED-PUB on six different datasets with varying numbers of clients, under both overlapping and disjoint subgraph FL scenarios. The experimental results show that ours significantly outperforms relevant baselines. Further analysis shows that our method can discover community structures among subgraphs, and the subgraph-specific masking localizes the knowledge with respect to subgraphs belonging to each community. Our main contributions are as follows:

- We introduce a novel problem of personalized subgraph FL, which aims at collaborative improvements of the related local models (e.g. subgraphs belonging to the same community), which has been relatively overlooked by previous works on graph and subgraph FL.
- We propose a novel framework for personalized subgraph FL, which performs weighted averaging
 of the local model parameters based on their functional similarities obtained without accessing the
 data, and learns sparse masks to select only the relevant subnetworks for the given subgraphs.
- We validate our personalized subgraph FL framework on six real-world datasets under two different

78 2 Related Work

Graph Neural Networks Graph representation learning with Graph Neural Networks (GNNs) [10, 79 48, 43, 18, 3], which aims to learn the representations of the nodes, the edges, and the entire graph, is 80 an extensively studied topic. Most existing GNNs under the message passing scheme [8] iteratively 81 represent a node by aggregating features from its neighboring nodes as well as itself. For exam-82 ple, Graph Convolutional Network (GCN) [22] approximates the spectral graph convolutions [12], 83 yielding a mean aggregation over neighboring nodes. Similarly, for each node, GraphSAGE [11] 84 aggregates the features from its neighbors to update the node representation. Such advances in GNNs 85 have led to successes on node and link prediction tasks [22, 47]. However, they are not directly 86 applicable to real-world systems with locally distributed graphs, where graphs from different sources 87 are not shared across participants, which gives rise to federated learning approaches to train GNNs. 88 Federated Learning Federated Learning (FL) [32, 41, 19, 24], aiming to learn a model by aggregat-89 90 ing model weights trained on local data, is an essential approach for our distributed subgraph learning problem. To mention a few, FedAvg [32] locally trains a model for each client and then transmits the 91 trained model to a server, while the server aggregates the model weights from local clients and then 92 sends the aggregated model back to them. However, since the locally collected data from different 93 clients may largely vary, heterogeneity is a crucial issue. To tackle this, FedProx [25] proposes the 94 regularization term that minimizes the weight differences between local and global models, which 95 prevents the model from diverging by overfitting to the local training data. However, when the local 96 data is extremely heterogeneous, it is more appropriate to collaboratively train a personalized model 97 for each client rather than learning a single global model [2, 30, 26, 46, 6]. FedPer [2] is such a 98 personalized FL method, which shares only the base layers while having local personalized layers 99 for each client, to keep the local knowledge. Unlike the commonly studied image and text data, 100 graph-structured data is defined by connections between instances, and consequently introduces 101 additional challenges: missing edges and shared nodes between private subgraphs. Note that, re-102 garding architectures, there is literature [29, 27, 38, 49] that leverages outputs of neural networks for 103 predicting/minimizing outputs across different client models; however, we use functional outputs of 104 neural networks to identify interconnected subgraphs, thus ours differs from them methodologically. 105

Graph Federated Learning Few recent studies propose to use the FL framework to collaboratively 106 train GNNs without sharing graph data [13], which can be broadly classified into subgraph- and 107 graph-level methods. Graph-level FL methods assume that different clients have completely disjoint 108 graphs (e.g., molecular graphs), and recent works [44, 14] focus on the heterogeneity among non-IID 109 110 graphs (i.e., difference in graph labels across various clients). In contrast to graph-level FL methods 111 that have similar challenges to general FL scenarios, the subgraph-level FL problem we target has a unique graph-structural challenge, that there exist missing yet probable links between subgraphs, 112 since a subgraph is a part of a larger global graph. To deal with such a missing link problem among 113 subgraphs, existing methods [42, 45] augment the nodes by requesting the node information in the 114 other subgraphs, and then connecting the existing nodes with the augmented ones. However, this 115 scheme could compromise data privacy constraints, and also increases communication overhead 116 across clients. Unlike existing subgraph FL that focuses on the problem of missing links, our subgraph 117 FL method tackles the problem with a completely different perspective, focusing on discovering 118 subgraph communities [35, 9, 34], which are groups of densely connected subgraphs. 119

120 **3** Personalized Subgraph Federated Learning

We provide the general descriptions of Graph Neural Networks (GNNs) and Federated Learning (FL), and then define our novel problem of personalized subgraph FL lying at the intersection of them.

Graph Neural Networks A graph $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ consists of a set of nodes \mathcal{V} with *n* elements and a set of edges \mathcal{E} with *m* elements along with its node feature matrix $\mathbf{X} \in \mathbb{R}^{n \times d}$, where each column represents a *d*-dimensional feature for each node. Further, $(u, v) \in \mathcal{E}$ represents an edge from a node *u* to a node *v*. Then, given the graph, Graph Neural Networks (GNNs) [8, 10] generally represent each node based on features from its neighbors as well as itself, formally defined as follows:

$$\boldsymbol{H}_{v}^{(l+1)} = \text{UPDATE}^{(l)}\left(\boldsymbol{H}_{v}^{(l)}, \text{AGGREGATE}^{(l)}\left(\left\{\boldsymbol{H}_{u}^{(l)} : \forall u \in \mathcal{N}(v)\right\}\right)\right), \tag{1}$$

where $H_v^{(l)}$ is the feature matrix for node v at l-th layer, $\mathcal{N}(v)$ denotes a set of adjacent nodes of node $v: \mathcal{N}(v) = \{u \in \mathcal{V} \mid (u, v) \in \mathcal{E}\}$, AGGREGATE aggregates the features of v's neighbors, and UPDATE updates the node v's representation given its previous representation and the aggregated representations from the neighbors. $H^{(1)}$ is initialized as input node features X.

Federated Learning The objective of Federated Learning (FL) is to collaboratively train a model 132 with local private data. Let assume that we have K participants with locally collected data that is not 133 accessible from others: $\mathcal{D}_k = \{ \mathbf{X}_i, \mathbf{y}_i \}_{i=1}^{N_k}$, where \mathbf{X}_i is a data instance, \mathbf{y}_i is its corresponding class label, and N_k is the number of data instances at k-th client. Then, for decentralized training with 134 135 local data, a popular FL algorithm, FedAvg [32], works as the following three steps: 136

- 1. (Initialization) At the initial communication round r = 0, the central server first selects K clients 137 that are available for training, and initializes their local model parameters as the global parameter $\bar{\theta}$, represented as follows: $\theta_k^{(0)} \leftarrow \bar{\theta}^{(0)} \forall k$, where $\theta_k^{(0)}$ is the parameters for k-th client. 2. (Local Updates) Each active local model performs training on private local data \mathcal{D}_k to minimize 138 139
- 140 141
- 2. (Dotal Optices) Each of the index performs training on protection of the probability in the task loss L(D_k; θ⁽⁰⁾_k), consequently updating the parameters θ⁽¹⁾_k ← θ⁽⁰⁾_k − η∇L.
 3. (Global Aggregation) After local training, the server aggregates the locally learned knowledge with respect to the number of training instances, i.e., θ⁽¹⁾ ← N_k Σ^K_{k=1} θ⁽¹⁾_k with N = Σ_k N_k, 142 143
- and distributes the updated global parameters $\bar{\theta}^{(1)}$ to the local clients selected at the next round. 144
- This FL algorithm iterates between Step 2 and 3 until reaching the final round R. 145

Challenges in Subgraph FL While the above FL works well on image and text data, due to the 146 unique structure of graphs, there exist nontrivial challenges for applying this FL scheme to graph-147 structured data. In particular, unlike with an image domain where each instance X_i is independent 148 from the other images, each node v in a graph is always influenced by its relationships to adjacent 149 nodes $\mathcal{N}(v)$. Moreover, a local graph G_i could be a subgraph of a larger global graph $\mathcal{G}: G_i \subseteq \mathcal{G}$. In 150 such a case, there could be missing edges between local subgraphs in two different clients: (u, v)151 with $u \in \mathcal{V}_i$ and $v \in \mathcal{V}_j$ for clients *i* and *j*, respectively. To tackle this missing edge problem, few 152 existing subgraph FL methods [42, 45] estimate the nodes from a local subgraph G_k based on the 153 node information from the subgraphs at other clients $G_i \forall i \neq k$, and then extend the existing nodes 154 with the estimated ones. However, this augmentation scheme incurs high communication costs as it 155 requires sharing node information across clients, which may also violate data privacy constraints [1]. 156

Yet, there exists another issue that makes subgraph FL even more challenging. Assume that we have 157 a global graph consisting of all the subgraphs. Then, there exists *communities* of such subgraphs [35, 158 9, 34], where subgraphs within the same community are more densely connected to each other 159 than subgraphs outside the community. Formally, a global graph \mathcal{G} can be decomposed into T 160 different communities: $C_i \subseteq \mathcal{G} \ \forall i = 1, ..., T$, where *i*-th community $C_i = (\mathcal{V}_i, \mathcal{E}_i)$ consists of densely connected nodes. Then, in a subgraph FL problem, each client has a local subgraph G_j that 161 162 belongs to at least a single community¹: $C_i = \bigcup_{j=1}^{J} G_j$. Note that, based on the theory of network homophily [33], such connected subgraphs within the same community have similar properties, while 163 164 subgraphs in two opposite communities are not. Such distributional heterogeneity across communities 165 may lead a naive FL algorithm to collapse incompatible knowledge across different communities. 166

167 **Personalized Subgraph FL** To prevent the above knowledge collapse issue, we aim to personalize the subgraph FL algorithm by performing weighted averaging of the local model parameters at 168 the server, rather than learning a single set of global parameters; thereby capturing the subgraph 169 community structures among interrelated subgraphs. Formally, the objective of existing subgraph 170 FL [42, 45, 28] is as follows: $\min_{\theta} \sum_{G_i \subseteq \mathcal{G}} \mathcal{L}(G_i; \theta)$. However, a major drawback of such a scheme is that, since the subgraphs in two different communities with sparse connections are extremely 171 172 heterogeneous due to network homophily [33], finding a universal set of parameters (i.e., θ) that work 173 on all tasks will result in finding a suboptimal parameter set. To address such limitations of existing 174 subgraph FL, we formulate a novel problem of personalized subgraph FL, formalized as follows: 175

$$\min_{(\boldsymbol{\theta}_i)} \sum_{G_i \subseteq \mathcal{G}} \mathcal{L}(G_i; \boldsymbol{\theta}_i), \ \boldsymbol{\theta}_i \leftarrow \sum_{j=1}^K \alpha_{ij} \boldsymbol{\theta}_j \text{ with } \alpha_{ik} \gg \alpha_{il} \text{ for } G_k \subseteq C \text{ and } G_l \nsubseteq C, \quad (2)$$

where θ_i is the weight for subgraph G_i belonging to community C, and α_{ij} is the coefficient for 176 weight aggregation which we will specify in Section 4.1. This formulation promotes the collaborative 177 learning across multiple local models that work on the interrelated subgraphs that belong to the same 178 community, by assigning larger weights on them. 179

¹For simplicity, we assume that a subgraph belongs to only a single community, however, the formulation does not change even when a subgraph can belong to multiple communities.



Figure 2: (A) Two communities, each of which consists of one/two subgraphs. (B) Client Similarity Matching: we forward randomly generated graphs to models $f(\bar{G}; \theta)$, and then obtain the functional embeddings of them \tilde{h} , which are then used to estimate the similarities between subgraphs. The similarities are used in the weight aggregation, resulting in the personalized model weights $\bar{\theta}$. (C) Weight Masking: the transmitted weights from the server to clients $\bar{\theta}$ are masked and shifted by local masks for localization to the local subgraph distribution.

¹⁸⁰ 4 Federated Personalized Subgraph Learning (FED-PUB) Framework

Our goal of personalized subgraph FL is to jointly improve the local models trained on the interconnected local subgraphs forming the community structures. To this end, we propose to compute subgraph similarity scores for detecting communities, and to mask subgraph-irrelevant weights.

184 4.1 Subgraph Similarity Estimation for Detecting Subgraph Community

We aim to reflect the community structure consisting of a group of densely connected subgraphs, by 185 sharing more weights among subgraphs in the same community, as formalized in equation 2. Due to 186 network homophily where similar instances in the graph are more associated with each other [33], the 187 subgraphs within the same community should have similar properties. Therefore, if one can measure 188 the subgraph similarities, we can group the similar ones into the community. However, measuring the 189 190 similarity between local subgraphs is challenging since we do not know which subgraph each client has due to local accessibility. How can we then compute subgraph similarities, without accessing 191 them? To this end, we aim to approximate the subgraph similarity at local clients using auxiliary 192 information obtained from the local GNN models that work on the subgraphs. 193

Subgraph Similarity Estimation with Model Parameters For 194 measuring the similarity between subgraphs at each client, without 195 accessing them, we may use the model parameters as proxies, as 196 follows: $S(i, j) = (\boldsymbol{\theta}_i \cdot \boldsymbol{\theta}_j) / (\|\boldsymbol{\theta}_i\| \|\boldsymbol{\theta}_j\|)$, where $\boldsymbol{\theta}$ is a flattened pa-197 rameter into the vector, and S is a similarity measure. This may 198 sound reasonable since the GNN model trained on the subgraph will 199 embed its knowledge into its parameters. However, this scheme has 200 a notable drawback that similarity measured in the high-dimensional 201 parameter space is not meaningful due to the curse of dimension-202 ality [4], and that the cost of calculating the similarity between 203 parameters grows rapidly as the model size increases (See Figure 3). 204



Figure 3: Effectiveness (top) and efficiencies (bottom) of different similarity measurements.

Subgraph Similarity Estimation with Functional Embedding To tackle the limitations of using 205 parameter distance, we propose to measure the functional similarity of neural networks by feeding the 206 same input to every local client and then calculating the similarities using their outputs, inspired by a 207 work for neural network search [17]. The main intuition is that we can consider the transformation 208 defined with a neural network as a function, and we measure the functional similarity of two networks 209 by the distance of their outputs for the same input. However, unlike the previous work [17] that 210 tackles image classification, which uses Gaussian noises as inputs, we use random graphs as inputs 211 as we work with GNNs. Formally, let $\hat{G} = (\hat{\mathcal{V}}, \hat{\mathcal{E}})$ be a random community graph obtained from a 212 stochastic block model [15], where subgraphs within the community have more edges between them 213 than edges across the communities. Further, \mathcal{V} is randomly initialized from the normal distribution. 214 Then, the similarity between two functions defined by GNNs at clients i and j is defined as follows: 215

$$S(i,j) = \frac{\tilde{\boldsymbol{h}}_i \cdot \tilde{\boldsymbol{h}}_j}{\|\tilde{\boldsymbol{h}}_i\| \|\tilde{\boldsymbol{h}}_j\|}, \quad \tilde{\boldsymbol{h}}_i = \operatorname{AVG}(f(\tilde{G};\boldsymbol{\theta}_i)) \text{ and } \tilde{\boldsymbol{h}}_j = \operatorname{AVG}(f(\tilde{G};\boldsymbol{\theta}_j)), \tag{3}$$

where \hat{h} is the averaged output of all node embeddings for input \tilde{G} with AVG operation to reduce the dimensionality of the output from $n \times d$ to d, for n nodes with d-dimensional node features. **Personalized Weight Aggregation based on Subgraph Similarity** With equation 3, the remaining step is then to share the model weights between models working on similar subgraphs belonging to the same community. However, entirely ignoring the model parameters from different communities may result in exploiting only the local objective while ignoring globally useful weights, which may result in performance degeneration. Therefore, we perform weighted averaging of all the local models from the other clients based on their functional (subgraph) similarities, as follows (Figure 2 (B)):

$$\bar{\boldsymbol{\theta}}_i \leftarrow \sum_j \alpha_{ij} \cdot \boldsymbol{\theta}_j, \quad \alpha_{ij} = \frac{\exp(\tau \cdot S(i,j))}{\sum_k \exp(\tau \cdot S(i,k))}, \tag{4}$$

where α_{ij} is a normalized similarity between clients *i* and *j*, and τ is a hyperparameter for scaling the unnormalized similarity score. Note that increasing the value of τ (e.g., 10) will result in model averaging done almost exclusively among subgraphs detected as belonging to the same community.

This personalized scheme handles two challenges in subgraph FL. First, in contrast to the global weight aggregation scheme which easily collapses the knowledge from heterogeneous communities into a single model, our subgraph FL allows the models belonging to different communities to obtain model weights that are beneficial for each community. Also, the missing edges between subgraphs that have been explicitly handled by previous works [42, 45] could be also implicitly considered by assigning larger weights to models within the same community (See Figure 10). This also enhances data privacy while minimizing the communication costs between probably linked subgraphs.

4.2 Adaptive Weight Masking for Selecting Subgraph-Relevant Parameters

With the previous similarity matching scheme, we can effectively group GNN models that belong to the same community, thus preventing the collapsing of irrelevant knowledge from other communities. However, the scalar weighting scheme only considers how much each local model from other clients is relevant for the subgraph task, but not *which* parameters are relevant. Thus we propose a scheme to select only the relevant parameters from the aggregated model weights transmitted from the server.

Personalized Parameter Masking We perform selective training and updating of the aggregated 240 parameters by modulating and shifting them, using sparse local masks. Formally, let μ_{i} be a local 241 mask for a client k. Then, our local model weight is obtained by modulating the weights from the 242 server, as follows: $\theta_k = \bar{\theta}_k \odot \mu_k$, where \odot is an element-wise multiplication operation between 243 the globally given weight $\bar{\theta}_k$ and the local mask μ_k . Note that the local mask is a free variable 244 and is not shared across clients. Also, we initialize μ_k as ones, in order to start training with the 245 globally initialized model parameters without modification. We then further promote sparsity on 246 the mask, which brings two key advantages. First, we can transmit only the partial parameters, that 247 have not been sparsified at the client to the server rather than sending all parameters, thus reducing 248 the communication costs. Moreover, if local masks are sufficiently sparse, the local models can be 249 trained faster, given that zero-skipping operations are supported (Figure 2 (C)). To take these benefits 250 in sparsity, we use L_1 regularizer on μ_k when performing local optimization, as shown in equation 5. 251

Preventing Local Divergence with Proximal Term As masks are trained only with limited local data without parameter sharing, they may be easily overfitted to the training instances in each client. To alleviate this issue, we adopt the proximal term proposed in Li et al. [25] that regularizes the locally updated models θ_k to be closer to the globally given model $\bar{\theta}_k$, therefore, preventing the model from extremely drifting to the local training distribution. To sum up, at *k*-th client, our objective function including sparsity and proximal terms with L_1 and L_2 losses is denoted as follows:

$$\min_{(\boldsymbol{\theta}_k, \boldsymbol{\mu}_k)} \mathcal{L}(\mathcal{D}_k; \boldsymbol{\theta}_k, \boldsymbol{\mu}_k) + \lambda_1 \|\boldsymbol{\mu}_k\|_1 + \lambda_2 \|\boldsymbol{\theta}_k - \boldsymbol{\theta}_k\|_2^2,$$
(5)

where \mathcal{L} is the conventional cross-entropy loss function, and λ_1 and λ_2 are scaling hyper-parameters.

259 5 Experiments

We now experimentally validate our FED-PUB on six different datasets under both the overlapping and disjoint subgraph scenarios with varying client numbers, with node classification tasks.

262 5.1 Experimental Setups

Datasets Following the setup from Zhang et al. [45], we construct the distributed subgraphs from the benchmark dataset by dividing it into the number of participants, each of which has a subgraph that is a part of an original graph. Specifically, we use six datasets: Cora, CiteSeer, Pubmed and

Table 1: **Results on the overlapping node scenario.** The reported results are mean and standard deviation over three different runs. Only the statistically significant performances (p > 0.05) are highlighted in bold.

						<u> </u>		, , , , , , , , , , , , , , , , , , , ,		
		Cora			CiteSeer			Pubmed		-
Methods	10 Clients	30 Clients	50 Clients	10 Clients	30 Clients	50 Clients	10 Clients	30 Clients	50 Clients	-
Local	73.98 ± 0.25	71.65 ± 0.12	76.63 ± 0.10	65.12 ± 0.08	64.54 ± 0.42	66.68 ± 0.44	82.32 ± 0.07	80.72 ± 0.16	80.54 ± 0.11	-
FedAvg	76.48 ± 0.36 77.85 ± 0.50	53.99 ± 0.98 51.38 \pm 1.74	53.99 ± 4.53 56.27 ± 9.04	69.48 ± 0.15 69.39 ± 0.35	66.15 ± 0.64 66.11 ± 0.75	66.51 ± 1.00 66.53 ± 0.43	82.67 ± 0.11 82.63 ± 0.17	82.05 ± 0.12 82.13 ± 0.13	80.24 ± 0.35 80.50 ± 0.46	-
FedPer	77.83 ± 0.30 78.73 ± 0.31	74.18 ± 0.24	74.42 ± 0.37	69.81 ± 0.28	65.19 ± 0.81	67.64 ± 0.44	85.31 ± 0.06	82.15 ± 0.15 84.35 ± 0.38	83.94 ± 0.10	1
GCFL	78.84 ± 0.26	73.41 ± 0.27	76.63 ± 0.16	69.48 ± 0.39	64.92 ± 0.18	65.98 ± 0.30	83.59 ± 0.25	80.77 ± 0.12	81.36 ± 0.11	-
FedGNN	70.63 ± 0.83	61.38 ± 2.33	56.91 ± 0.82	68.72 ± 0.39	59.98 ± 1.52	58.98 ± 0.98	84.25 ± 0.07	82.02 ± 0.22	81.85 ± 0.10	-
FedSage+	77.52 ± 0.46	51.99 ± 0.42	55.48 ± 11.5	68.75 ± 0.48	65.97 ± 0.02	65.93 ± 0.30	82.77 ± 0.08	82.14 ± 0.11	80.31 ± 0.68	-
FED-PUB (Ours)	$\textbf{79.60} \pm 0.12$	$\textbf{75.40} \pm 0.54$	$\textbf{77.84} \pm 0.23$	$\textbf{70.58} \pm 0.20$	$\textbf{68.33} \pm 0.45$	$\textbf{69.21} \pm 0.30$	$\textbf{85.70} \pm 0.08$	$\textbf{85.16} \pm 0.10$	$\textbf{84.84} \pm 0.12$	-
	Amazon-Computer			Amazon-Photo			ogbn-arxiv			All
Methods	10 Clients	30 Clients	50 Clients	10 Clients	30 Clients	50 Clients	10 Clients	30 Clients	50 Clients	Avg.
Local	88.50 ± 0.20	86.66 ± 0.00	87.04 ± 0.02	92.17 ± 0.12	90.16 ± 0.12	90.42 ± 0.15	62.52 ± 0.07	61.32 ± 0.04	60.04 ± 0.04	76.72
FedAvg	88.99 ± 0.19	83.37 ± 0.47	76.34 ± 0.12	92.91 ± 0.07	89.30 ± 0.22	74.19 ± 0.57	63.56 ± 0.02	59.72 ± 0.06	60.94 ± 0.24	73.38
FedProx	88.84 ± 0.20	83.84 ± 0.89	76.60 ± 0.47	92.67 ± 0.19	89.17 ± 0.40	72.36 ± 2.06	63.52 ± 0.11	59.86 ± 0.16	61.12 ± 0.04	73.38
FedPer	89.30 ± 0.04	87.99 ± 0.23	88.22 ± 0.27	92.88 ± 0.24	91.23 ± 0.16	90.92 ± 0.38	63.97 ± 0.08	62.29 ± 0.04	61.24 ± 0.11	78.42
GUFL FedGNN	89.01 ± 0.22 88.15 ± 0.00	87.24 ± 0.09 87.00 ± 0.10	87.02 ± 0.22 83.06 ± 0.88	92.43 ± 0.10 91.47 ± 0.11	90.38 ± 0.11 87.01 ± 1.34	90.34 ± 0.08 78.00 ± 6.46	63.24 ± 0.02 63.08 ± 0.10	61.00 ± 0.10 60.00 ± 0.04	60.32 ± 0.01 60.51 ± 0.11	73.66
FedSage+	89.13 ± 0.09 89.24 ± 0.15	81.33 ± 1.20	7672 ± 0.38	92.76 ± 0.05	88.69 ± 0.99	72.41 ± 1.36	63.03 ± 0.19 63.24 ± 0.02	59.90 ± 0.04	60.91 ± 0.11 60.95 ± 0.09	73.12
FED_PUB (Ours)	89 98 ± 0.08	89 15 ± 0.06	88.76 ± 0.14	93.22 ± 0.07	92.01 ± 0.07	91 71 ± 0.11	63.21 ± 0.02 64 18 ± 0.04	63.34 ± 0.12	62.55 ± 0.03	79.53
TED-TOD (Outs)	0.00 ± 0.00	07.15 ± 0.00	00.70 ± 0.14	75.22 ± 0.07	72.01 ± 0.07	71.71 ± 0.111	04.10 ± 0.04	05.54 ± 0.12	02.55 ± 0.12	17.00
Profession of the second secon					Performance on arxiv (Performance on arxiv (Perfor	30 Clients) dPer FR D-PUB (Ours) 70 80 90 10 counds				
(a) Cora	(1	b) CiteSeer	(c)	Pubmed	(d) Co	mputer	(e) Ph	oto	(f) ogbn-ar	xiv

Figure 4: **Convergence plots for the overlapping node scenario.** We visualize the test accuracy curves for all six datasets corresponding to Table 1, over 100 communication rounds with 10 clients.

ogbn-arxiv for citation graphs [39, 16]; Computer and Photo for product graphs [31, 40]. We then 266 divide the original graph into multiple subgraphs using the METIS graph partitioning algorithm [20]. 267 Note that, unlike the Louvain algorithm [5] presented in Zhang et al. [45] that requires to further 268 merge partitioned subgraphs into particular numbers of subgraphs since it cannot specify the number 269 of subsets (i.e., clients for FL), the METIS algorithm can specify the number of subsets, thus making 270 more reasonable experimental settings in subgraph FL (See Section C.2 of the supplementary file). 271 For the non-overlapping scenario where there are no duplicate nodes between subgraphs, we use the 272 output from the METIS as it provides the non-overlapping partitions. Meanwhile, for the overlapping 273 scenario where nodes are duplicated among subgraphs, we randomly sample the subgraphs multiple 274 times from the partitioned graph. For more details, please see Section B of the supplementary file. 275 Baselines 1) FedAvg [32] and 2) FedProx [25]: The most popular FL baselines. 3) FedPer [2]: A 276 personalized FL baseline without sharing personalized layers. 4) FedGNN [42] and 5) FedSage+ [45]: 277 Subgraph FL baselines which we mainly target. 6) GCFL [44]: A graph FL baseline which learns 278 completely disjoint graphs as in clustered FL [37], adopted for subgraph FL. 7) Local: A baseline 279

without sharing weights with other clients. 8) FED-PUB: Our personalized subgraph FL including
 subgraph similarity matching and weight masking. See Section B of the supplementary file for details.

Implementation Details We set the GCN [22] with two layers as the base GNN for all models. We perform federated learning over 100 communication rounds for Cora, CiteSeer and Pubmed datasets, while 200 rounds for Computer, Photo and arxiv datasets, considering the size of datasets. The local training epoch is selected in the range of $\{1, 2, 3\}$ depending on the dataset size (e.g., Computer is three while CiteSeer is one)². We use the Adam optimizer [21] for model optimization. We then measure the node classification accuracy on subgraphs at the client-side, and then average the performance across clients. We provide further details in Section B of the supplementary file.

289 5.2 Experimental Results

Main Results Table 1 shows the node classification performance under the overlapping subgraph 290 scenario, in which our FED-PUB statistically (p > 0.05) significantly outperforms all the baselines. 291 In particular, while FedGNN and FedSage+ are two pioneer works for the subgraph FL problem, 292 they significantly underperform personalized FL methods including ours, especially at the larger 293 number of clients. This is even surprising as they share node information between clients for handling 294 the missing edge problem, yet we suppose such inferior performance comes from naive averaging 295 of local weights without consideration of community structures. While personalized FL baselines 296 including FedPer and GCFL show decent performance by alleviating the knowledge collapse between 297 subgraphs with local parameters or clustering, they still largely underperform ours as they are not 298 concerned with the aggregation between similar subgraphs that form a community (i.e., GCFL uses a 299 bi-partitioning scheme where it iteratively divides a group of subgraphs within the same community 300

²We found communication rounds and local epochs are important factors to prevent overfitting of all models.

Table 2: Results on the non-overlapping node scenario. The reported results are mean and standard deviation over three different runs. Only the statistically significant performances (p > 0.05) are highlighted in bold.

		Cora			CiteSeer			Pubmed		-
Methods	5 Clients	10 Clients	20 Clients	5 Clients	10 Clients	20 Clients	5 Clients	10 Clients	20 Clients	-
Local	81.30 ± 0.21	79.94 ± 0.24	80.30 ± 0.25	69.02 ± 0.05	67.82 ± 0.13	65.98 ± 0.17	84.04 ± 0.18	82.81 ± 0.39	82.65 ± 0.03	-
FedAvg FedProx FedPer GCFL	$\begin{array}{c} 74.45 \pm 5.64 \\ 72.03 \pm 4.56 \\ 81.68 \pm 0.40 \\ 81.47 \pm 0.65 \\ 91.51 \pm 0.65 \end{array}$	$\begin{array}{c} 69.19 \pm 0.67 \\ 60.18 \pm 7.04 \\ 79.35 \pm 0.04 \\ 78.66 \pm 0.27 \\ 70.12 \pm 0.00 \end{array}$	$\begin{array}{c} 69.50 \pm 3.58 \\ 48.22 \pm 6.81 \\ 78.01 \pm 0.32 \\ 79.21 \pm 0.70 \\ 79.10 \pm 2.52 \end{array}$	71.06 ± 0.60 71.73 ± 1.11 70.41 ± 0.32 70.34 ± 0.57 60.02	$\begin{array}{c} 63.61 \pm 3.59 \\ 63.33 \pm 3.25 \\ 70.53 \pm 0.28 \\ 69.01 \pm 0.12 \\ 65.01 \pm 0.12 \end{array}$	$\begin{array}{c} 64.68 \pm 1.83 \\ 64.85 \pm 1.35 \\ 66.64 \pm 0.27 \\ 66.33 \pm 0.05 \\ \end{array}$	$\begin{array}{c} 79.40 \pm 0.11 \\ 79.45 \pm 0.25 \\ 85.80 \pm 0.21 \\ 85.14 \pm 0.33 \\ 70.22 \end{array}$	$\begin{array}{c} 82.71 \pm 0.29 \\ 82.55 \pm 0.24 \\ 84.20 \pm 0.28 \\ 84.18 \pm 0.19 \\ 82.55 \pm 0.44 \end{array}$	$\begin{array}{c} 80.97 \pm 0.26 \\ 80.50 \pm 0.25 \\ 84.72 \pm 0.31 \\ 83.94 \pm 0.36 \\ 91.61 \\ 91.62 \\ 91.$	-
FedGNN FedSage+	81.51 ± 0.68 72.97 ± 5.94	70.12 ± 0.99 69.05 ± 1.59	70.10 ± 3.52 57.97 ± 12.6	69.06 ± 0.92 70.74 ± 0.69	55.52 ± 3.17 65.63 ± 3.10	52.23 ± 6.00 65.46 ± 0.74	79.52 ± 0.23 79.57 ± 0.24	83.25 ± 0.45 82.62 ± 0.31	81.61 ± 0.59 80.82 ± 0.25	1
FED-PUB (Ours)	$\textbf{83.70} \pm 0.19$	$\textbf{81.54} \pm 0.12$	$\textbf{81.75} \pm 0.56$	$\textbf{72.68} \pm 0.44$	$\textbf{72.35} \pm 0.53$	$\textbf{67.62} \pm 0.12$	$\textbf{86.79} \pm 0.09$	$\textbf{86.28} \pm 0.18$	$\textbf{85.53} \pm 0.30$	-
	Amazon-Computer			Amazon-Photo			ogbn-arxiv			All
Methods	5 Clients	10 Clients	20 Clients	5 Clients	10 Clients	20 Clients	5 Clients	10 Clients	20 Clients	Avg.
Local	89.22 ± 0.13	88.91 ± 0.17	89.52 ± 0.20	91.67 ± 0.09	91.80 ± 0.02	90.47 ± 0.15	66.76 ± 0.07	64.92 ± 0.09	65.06 ± 0.05	79.57
FedAvg FedProx FedPer GCFL FedGNN FedSage+	$\begin{array}{c} 84.88 \pm 1.96 \\ 85.25 \pm 1.27 \\ 89.67 \pm 0.34 \\ 89.07 \pm 0.91 \\ 88.08 \pm 0.15 \\ 85.04 \pm 0.61 \end{array}$	$\begin{array}{c} 79.54 \pm 0.23 \\ 83.81 \pm 1.09 \\ 89.73 \pm 0.04 \\ 90.03 \pm 0.16 \\ 88.18 \pm 0.41 \\ 80.50 \pm 1.30 \end{array}$	$\begin{array}{c} 74.79 \pm 0.24 \\ 73.05 \pm 1.30 \\ 87.86 \pm 0.43 \\ 89.08 \pm 0.25 \\ 83.16 \pm 0.13 \\ 70.42 \pm 0.85 \end{array}$	$\begin{array}{c} 89.89 \pm 0.83 \\ 90.38 \pm 0.48 \\ 91.44 \pm 0.37 \\ 91.99 \pm 0.29 \\ 90.25 \pm 0.70 \\ 90.77 \pm 0.44 \end{array}$	$\begin{array}{c} 83.15 \pm 3.71 \\ 80.92 \pm 4.64 \\ 91.76 \pm 0.23 \\ 92.06 \pm 0.25 \\ 87.12 \pm 2.01 \\ 76.81 \pm 8.24 \end{array}$	$\begin{array}{c} 81.35\pm1.04\\ 82.32\pm0.29\\ 90.59\pm0.06\\ 90.79\pm0.17\\ 81.00\pm4.48\\ 80.58\pm1.15 \end{array}$	$\begin{array}{c} 65.54\pm 0.07\\ 65.21\pm 0.20\\ 66.87\pm 0.05\\ 66.80\pm 0.12\\ 65.47\pm 0.22\\ 65.69\pm 0.09 \end{array}$	$\begin{array}{c} 64.44 \pm 0.10 \\ 64.37 \pm 0.18 \\ 64.99 \pm 0.18 \\ 65.09 \pm 0.08 \\ 64.21 \pm 0.32 \\ 64.52 \pm 0.14 \end{array}$	$\begin{array}{c} 63.24 \pm 0.13 \\ 63.03 \pm 0.04 \\ 64.66 \pm 0.11 \\ 65.08 \pm 0.04 \\ 63.80 \pm 0.05 \\ 63.31 \pm 0.20 \end{array}$	74.58 72.84 79.94 79.90 75.23 73.47
FED-PUB (Ours)	$\textbf{90.74} \pm 0.05$	$\textbf{90.55} \pm 0.13$	$\textbf{90.12} \pm 0.09$	$\textbf{93.29} \pm 0.19$	$\textbf{92.73} \pm 0.18$	$\textbf{91.92} \pm 0.12$	$\textbf{67.77} \pm 0.09$	$\textbf{66.58} \pm 0.08$	$\textbf{66.64} \pm 0.12$	81.59
						(10 Clients)				

(d) Computer (f) ogbn-arxiv Figure 5: Convergence plots for the non-overlapping node scenario. We visualize the test accuracy curves for all six datasets corresponding to Table 2, over 100 communication rounds with 10 clients.

60 FedAvg FedPer FedGNN GCFL FedSam FED-PUB

FedAvg -- FedPeg FedGNN -- GCFL FedSage -- FED-P

(e) Photo

GCFL

into two disjoint sets). We then further conduct the experiments on the disjoint subgraph scenarios 301 (non-overlapping scenario), where nodes are not overlapped between subgraphs, which makes the 302 subgraph FL problem more heterogeneous. As shown in Table 2, FED-PUB consistently outperforms 303 all existing baselines in such a challenging scenario, demonstrating the efficacy of ours. 304

FedAvg FedGNN FedSage FedSage

(c) Pubmed

FedAvg FedGNN FedGNN FedGNN

(a) Cora

FedAvg - FedPer FedGNN - GCFL

(b) CiteSeer

Fast Local Convergence As shown in Figure 4 and 5, our FED-PUB converges rapidly, compared 305 against baselines including personalized FL models. We conjecture that this is because, not only ours 306 accurately identifies subgraphs forming the community and then shares weights largely across them 307 for promoting the joint improvement of them, but also masking subgraph-irrelevant weights received 308 from the server for localization to local subgraphs, demonstrated in the next two paragraphs. 309

Accurate Community Detection We aim to show whether FED-PUB accurately groups subgraphs 310 comprising a community during weight aggregation. If two different subgraphs have many missing 311 edges or have similar label distributions, we usually regard those two as within the same commu-312 nity [35, 9, 34]. Thereby, as shown in Figure 6 (a) and (b), there are four different communities by the 313 interval of five, and the last two communities further comprise a larger community. Then, as shown 314 in Figure 6 (c) and (d), FED-PUB detects obvious four communities at the first few rounds, and then 315 captures the larger yet somewhat less-obvious community consisting of two smaller communities. 316

Ablation Study To analyze the contribution of each component, we conduct the ablation studies. 317 As shown in Figure 7, we observe that each of our subgraph similarity matching and weight masking 318 significantly improves the performances from the naive FedAvg, while the performance is much 319 improved when using both together. However, the benefit from each component is different across 320 overlapping and non-overlapping scenarios. In particular, in the former scenario where a group of 321 highly overlapped subgraphs usually comprise a community, similarity matching for community 322 detection is more beneficial since capturing the community would promote the joint improvement of 323 subgraphs belonging to the same community. However, in the non-overlapping scenarios, subgraphs 324 within the same community become lesser similar, thus selectively using the aggregated model 325 weights from the server with personalized weight masks improves the performance a lot. 326

Communication Efficiency Another notable advantage of using the sparse masks is that we can 327 reduce the communication costs at every FL round, as well as the model size for faster training, which 328 we demonstrate in Table 8. In particular, Table 8 shows that existing subgraph FL methods require 329 more than two times larger communications costs, measured by adding both the client-to-server and 330 server-to-client costs, compared against the naive FedAvg, since they require to transfer additional 331 node information between clients for estimating the probable nodes on the subgraphs. Contrarily, our 332 FED-PUB has significantly lower communication costs and lower model sizes by using the sparse 333 masks on the model weights: transmitting and training with only the partial parameters not sparsified 334 at the client. Further, as shown in ours variants in Table 8, we can manage the trade-off between the 335 model sparsity and the performance by controlling the hyperparameter for sparsity regularization, λ_1 . 336



Figure 6: The heatmaps of the community structure on the overlap- Figure 7: Ablation studies of our FEDping node scenario with Cora (20 clients). Dark color indicates lots PUB on both the overlapping (a) and nonof missing edges between subgraphs (a) or high similarities in labels overlapping (b) subgraph scenarios, on (b). (c) and (d) are functional similarities captured by our FED-PUB. the Cora dataset.

Model	Acc. [%]	Model Size [%]	Cost [%]
FedAvg	76.48 ± 0.36	100.00 ± 0.00	100.00 ± 0.00
FedGNN FedSage+ GCFL	$\begin{array}{c} 70.63 \pm 0.83 \\ 77.52 \pm 0.46 \\ 78.84 \pm 0.26 \end{array}$	$\begin{array}{c} 100.00 \pm 0.00 \\ 100.00 \pm 0.00 \\ 100.00 \pm 0.00 \end{array}$	$\begin{array}{c} 214.94 \pm 0.00 \\ 276.84 \pm 0.00 \\ 100.00 \pm 0.00 \end{array}$
$\begin{array}{l} \mathbf{Ours} \left(\lambda_1 \texttt{=} 9e\texttt{-} 1 \right) \\ \mathbf{Ours} \left(\lambda_1 \texttt{=} 7e\texttt{-} 1 \right) \\ \mathbf{Ours} \left(\lambda_1 \texttt{=} 5e\texttt{-} 1 \right) \end{array}$	$\begin{array}{c} 77.36 \pm 0.99 \\ 79.46 \pm 0.41 \\ \textbf{79.89} \pm 0.12 \end{array}$	$\begin{array}{c} \textbf{25.13} \pm 0.34 \\ 42.59 \pm 1.33 \\ 57.07 \pm 0.52 \end{array}$	$\begin{array}{c} \textbf{37.70} \pm 0.56 \\ 63.89 \pm 1.99 \\ 85.61 \pm 0.78 \end{array}$

cation costs and model sizes.





epochs with accuracy curves. neighboring subgraphs.

Figure 8: Analysis on efficiencies of communi- Figure 9: Varying the local Figure 10: Performance on

Varying Local Epochs As shown in Figure 9, when we increase the number of communication 337 rounds and the local steps, the model diverges to the local subgraphs (i.e., overfitting), due to the 338 small number of training instances and the direct connection between training and test nodes: struggle 339 to generalize to the test instances. However, our model with the proximal term in equation 5 alleviates 340 this issue, therefore, maintaining the highest local performance. Notably, the performance with five 341 local epochs is inferior to the performance of one epoch, which indicates that increasing the local 342 epochs does not always bring advantages and properly tuning them is important for subgraph FL. 343

Handling Missing Edges To measure whether FED-PUB can handle the missing edge problem: 344 information is not shared between two neighboring subgraphs due to the missing edges, we use 345 the local model trained on the local subgraph for evaluating the performance on its neighboring 346 347 subgraph, in which the local subgraph has the most missing edges to its neighboring subgraph. Specifically, in Figure 10, (Neighbor) denotes the subgraph performance evaluated by its neighbor 348 model, while (Local) denotes the subgraph performance from its own local model. Then, the high 349 performance on (Neighbor) measure means two associated subgraphs share meaningful knowledge 350 without having explicit edges between them, thereby solving the missing edge problem. Note that, 351 existing subgraph FL explicitly augments the nodes and edges for capturing the potential information 352 flow over the missing edges between subgraphs, while ours implicitly shares weights a lot across 353 similar subgraphs within the same community. Figure 10 shows that ours achieves the significantly 354 355 superior performance on the neighboring subgraph problem against subgraph FL baselines, which confirms that ours has an advantage on the missing edge problem by meaningfully sharing knowledge 356 between two subgraphs having potentially missing edges, without explicitly estimating them. 357

Conclusion 6 358

We introduced a novel problem of personalized subgraph FL, which focuses on the joint improvement 359 of local GNNs working on interrelated subgraphs (e.g. subgraphs belonging to the same community), 360 by selectively utilizing knowledge from other models. The proposed personalized subgraph FL is 361 highly challenging due to 1) difficulty of computing similarities between local subgraphs that are 362 only locally accessible, and 2) knowledge collapse among local models that work on heterogeneous 363 subgraphs during weight aggregation. To this end, we proposed a novel personalized subgraph FL 364 framework, referred to as FEDerated Personalized sUBgraph learning (FED-PUB), which computes 365 the similarities across subgraphs using functional embeddings of their local GNNs on random graphs, 366 and uses them to perform a weighted average of the local models for each client. Further, we mask out 367 globally given weights to focus on only the relevant subnetwork for each client (or community). We 368 extensively validated our framework on multiple benchmark datasets with both overlapping and non-369 overlapping subgraphs, on which our FED-PUB significantly outperforms relevant baselines. Further 370 analyses show the effectiveness of the subgraph similarity matching for detecting the community 371 structures, as well as the weight masking for tackling the subgraph heterogeneity. We provide the 372 limitations and potential societal impacts of our work in Section D of the supplementary file. 373

374 **References**

- [1] Martin Abadi, Andy Chu, Ian Goodfellow, H Brendan McMahan, Ilya Mironov, Kunal Talwar,
 and Li Zhang. Deep learning with differential privacy. In *Proceedings of the 2016 ACM SIGSAC conference on computer and communications security*, pages 308–318, 2016.
- [2] Manoj Ghuhan Arivazhagan, Vinay Aggarwal, Aaditya Kumar Singh, and Sunav Choudhary.
 Federated learning with personalization layers, 2019.
- [3] Jinheon Baek, Minki Kang, and Sung Ju Hwang. Accurate learning of graph representations
 with graph multiset pooling. In *9th International Conference on Learning Representations, ICLR 2021, Virtual Event, Austria, May 3-7, 2021, 2021.*
- ³⁸³ [4] Richard Bellman. Dynamic programming. *Science*, 153(3731):34–37, 1966.
- [5] Vincent D Blondel, Jean-Loup Guillaume, Renaud Lambiotte, and Etienne Lefebvre. Fast
 unfolding of communities in large networks. *Journal of statistical mechanics: theory and experiment*, 2008(10):P10008, 2008.
- [6] Fengwen Chen, Guodong Longr, Zonghan Wu, Tianyi Zhou, and Jing Jiang. Personalized federated learning with structure. *arXiv preprint arXiv:2203.00829*, 2022.
- [7] Laxman Dhulipala, Igor Kabiljo, Brian Karrer, Giuseppe Ottaviano, Sergey Pupyrev, and Alon
 Shalita. Compressing graphs and indexes with recursive graph bisection. In *Proceedings of the* 22nd ACM SIGKDD International Conference on Knowledge Discovery and Data Mining, San
 Francisco, CA, USA, August 13-17, 2016, pages 1535–1544. ACM, 2016.
- [8] Justin Gilmer, Samuel S. Schoenholz, Patrick F. Riley, Oriol Vinyals, and George E. Dahl.
 Neural message passing for quantum chemistry. In *Proceedings of the 34th International Conference on Machine Learning, ICML 2017, Sydney, NSW, Australia, 6-11 August 2017,* volume 70 of *Proceedings of Machine Learning Research*, pages 1263–1272. PMLR, 2017.
- [9] M. Girvan and M. E. J. Newman. Community structure in social and biological networks.
 Proceedings of the National Academy of Sciences, 99(12):7821–7826, 2002.
- [10] William L. Hamilton. Graph representation learning. Synthesis Lectures on Artificial Intelligence
 and Machine Learning, 14(3):1–159.
- [11] William L. Hamilton, Zhitao Ying, and Jure Leskovec. Inductive representation learning on
 large graphs. In Advances in Neural Information Processing Systems 30: Annual Conference
 on Neural Information Processing Systems 2017, December 4-9, 2017, Long Beach, CA, USA,
 pages 1024–1034, 2017.
- [12] David K. Hammond, Pierre Vandergheynst, and Rémi Gribonval. Wavelets on graphs via
 spectral graph theory. *Applied and Computational Harmonic Analysis*, 30(2):129–150, 2011.
- [13] Chaoyang He, Keshav Balasubramanian, Emir Ceyani, Carl Yang, Han Xie, Lichao Sun, Lifang
 He, Liangwei Yang, Philip S Yu, Yu Rong, et al. Fedgraphnn: A federated learning system and
 benchmark for graph neural networks. *arXiv preprint arXiv:2104.07145*, 2021.
- [14] Chaoyang He, Emir Ceyani, Keshav Balasubramanian, Murali Annavaram, and Salman Aves timehr. Spreadgnn: Serverless multi-task federated learning for graph neural networks. *AAAI*,
 2022.
- [15] Paul W. Holland, Kathryn Blackmond Laskey, and Samuel Leinhardt. Stochastic blockmodels:
 First steps. *Social Networks*, 5(2):109–137, 1983. ISSN 0378-8733.
- [16] Weihua Hu, Matthias Fey, Marinka Zitnik, Yuxiao Dong, Hongyu Ren, Bowen Liu, Michele
 Catasta, and Jure Leskovec. Open graph benchmark: Datasets for machine learning on graphs.
 Advances in neural information processing systems, 33:22118–22133, 2020.
- [17] Wonyong Jeong, Hayeon Lee, Geon Park, Eunyoung Hyung, Jinheon Baek, and Sung Ju Hwang.
 Task-adaptive neural network search with meta-contrastive learning. In *Advances in Neural Information Processing Systems*, 2021.

- [18] Jaehyeong Jo, Jinheon Baek, Seul Lee, Dongki Kim, Minki Kang, and Sung Ju Hwang. Edge
 representation learning with hypergraphs. In M. Ranzato, A. Beygelzimer, Y. Dauphin, P.S.
 Liang, and J. Wortman Vaughan, editors, *Advances in Neural Information Processing Systems*,
 volume 34, pages 7534–7546. Curran Associates, Inc., 2021.
- [19] Sai Praneeth Karimireddy, Satyen Kale, Mehryar Mohri, Sashank J. Reddi, Sebastian U. Stich,
 and Ananda Theertha Suresh. SCAFFOLD: stochastic controlled averaging for federated
 learning. In *Proceedings of the 37th International Conference on Machine Learning, ICML* 2020, 13-18 July 2020, Virtual Event, volume 119 of Proceedings of Machine Learning Research,
- 429 pages 5132–5143. PMLR, 2020.
- [20] George Karypis and Vipin Kumar. Metis unstructured graph partitioning and sparse matrix
 ordering system, version 2.0. Technical report, 1995.
- [21] Diederik P. Kingma and Jimmy Ba. Adam: A method for stochastic optimization. In *3rd International Conference on Learning Representations, ICLR 2015, San Diego, CA, USA, May* 7-9, 2015, Conference Track Proceedings, 2015.
- [22] Thomas N. Kipf and Max Welling. Semi-supervised classification with graph convolutional networks. In *5th International Conference on Learning Representations, ICLR 2017, Toulon, France, April 24-26, 2017, Conference Track Proceedings, 2017.*
- [23] Jure Leskovec, Lada A. Adamic, and Bernardo A. Huberman. The dynamics of viral marketing.
 ACM Trans. Web, 1(1):5, 2007.
- [24] Qinbin Li, Bingsheng He, and Dawn Song. Model-contrastive federated learning. In *IEEE Conference on Computer Vision and Pattern Recognition, CVPR 2021, virtual, June 19-25,* 2021, pages 10713–10722. Computer Vision Foundation / IEEE, 2021.
- [25] Tian Li, Anit Kumar Sahu, Manzil Zaheer, Maziar Sanjabi, Ameet Talwalkar, and Virginia
 Smith. Federated optimization in heterogeneous networks. In *Proceedings of Machine Learning and Systems 2020, MLSys 2020, Austin, TX, USA, March 2-4, 2020.* mlsys.org, 2020.
- Paul Pu Liang, Terrance Liu, Liu Ziyin, Nicholas B. Allen, Randy P. Auerbach, David Brent,
 Ruslan Salakhutdinov, and Louis-Philippe Morency. Think locally, act globally: Federated
 learning with local and global representations, 2020.
- [27] Tao Lin, Lingjing Kong, Sebastian U Stich, and Martin Jaggi. Ensemble distillation for robust
 model fusion in federated learning. *Advances in Neural Information Processing Systems*, 33:
 2351–2363, 2020.
- [28] Zhiwei Liu, Liangwei Yang, Ziwei Fan, Hao Peng, and Philip S Yu. Federated social recommendation with graph neural network. *arXiv preprint arXiv:2111.10778*, 2021.
- [29] Disha Makhija, Xing Han, Nhat Ho, and Joydeep Ghosh. Architecture agnostic federated
 learning for neural networks. *arXiv preprint arXiv:2202.07757*, 2022.
- [30] Yishay Mansour, Mehryar Mohri, Jae Ro, and Ananda Theertha Suresh. Three approaches for
 personalization with applications to federated learning, 2020.
- [31] Julian McAuley, Christopher Targett, Qinfeng Shi, and Anton Van Den Hengel. Image-based
 recommendations on styles and substitutes. In *Proceedings of the 38th international ACM SIGIR conference on research and development in information retrieval*, pages 43–52, 2015.
- [32] H. Brendan McMahan, Eider Moore, Daniel Ramage, Seth Hampson, and Blaise Agüera y Arcas.
 Communication-efficient learning of deep networks from decentralized data. In *AISTATS*, 2017.
- [33] Miller McPherson, Lynn Smith-Lovin, and James M Cook. Birds of a feather: Homophily in
 social networks. *Annual review of sociology*, 27(1):415–444, 2001.
- [34] Mason A Porter, Jukka-Pekka Onnela, Peter J Mucha, et al. Communities in networks. *Notices of the AMS*, 56(9):1082–1097, 2009.

- [35] Filippo Radicchi, Claudio Castellano, Federico Cecconi, Vittorio Loreto, and Domenico Parisi.
 Defining and identifying communities in networks. *Proceedings of the national academy of sciences*, 101(9):2658–2663, 2004.
- [36] José J. Ramasco, S. N. Dorogovtsev, and Romualdo Pastor-Satorras. Self-organization of
 collaboration networks. *Phys. Rev. E*, 70:036106, Sep 2004.
- [37] Felix Sattler, Klaus-Robert Müller, and Wojciech Samek. Clustered federated learning: Model agnostic distributed multitask optimization under privacy constraints. *IEEE transactions on neural networks and learning systems*, 32(8):3710–3722, 2020.
- [38] Felix Sattler, Tim Korjakow, Roman Rischke, and Wojciech Samek. Fedaux: Leveraging
 unlabeled auxiliary data in federated learning. *IEEE Transactions on Neural Networks and Learning Systems*, 2021.
- [39] Prithviraj Sen, Galileo Namata, Mustafa Bilgic, Lise Getoor, Brian Galligher, and Tina Eliassi Rad. Collective classification in network data. *AI magazine*, 29(3):93–93, 2008.
- [40] Oleksandr Shchur, Maximilian Mumme, Aleksandar Bojchevski, and Stephan Günnemann.
 Pitfalls of graph neural network evaluation. *arXiv preprint arXiv:1811.05868*, 2018.
- [41] Hongyi Wang, Mikhail Yurochkin, Yuekai Sun, Dimitris Papailiopoulos, and Yasaman Khaz aeni. Federated learning with matched averaging. In *International Conference on Learning Representations*, 2020.
- [42] Chuhan Wu, Fangzhao Wu, Yang Cao, Yongfeng Huang, and Xing Xie. Fedgnn: Federated
 graph neural network for privacy-preserving recommendation. *KDD*, 2021.
- [43] Zonghan Wu, Shirui Pan, Fengwen Chen, Guodong Long, Chengqi Zhang, and Philip S. Yu. A
 comprehensive survey on graph neural networks. *IEEE Trans. Neural Networks Learn. Syst.*, 32 (1):4–24, 2021.
- [44] Han Xie, Jing Ma, Li Xiong, and Carl Yang. Federated graph classification over non-iid graphs.
 In Advances in Neural Information Processing Systems, volume 34, pages 18839–18852. Curran Associates, Inc., 2021.
- [45] Ke Zhang, Carl Yang, Xiaoxiao Li, Lichao Sun, and Siu Ming Yiu. Subgraph federated learning
 with missing neighbor generation. In *Advances in Neural Information Processing Systems*,
 volume 34, pages 6671–6682. Curran Associates, Inc., 2021.
- [46] Michael Zhang, Karan Sapra, Sanja Fidler, Serena Yeung, and Jose M. Alvarez. Personalized
 federated learning with first order model optimization. In *International Conference on Learning Representations*, 2021.
- [47] Muhan Zhang and Yixin Chen. Link prediction based on graph neural networks. In Advances
 in Neural Information Processing Systems 31: Annual Conference on Neural Information
 Processing Systems 2018, NeurIPS 2018, December 3-8, 2018, Montréal, Canada, pages
 502 5171–5181, 2018.
- [48] Jie Zhou, Ganqu Cui, Shengding Hu, Zhengyan Zhang, Cheng Yang, Zhiyuan Liu, Lifeng
 Wang, Changcheng Li, and Maosong Sun. Graph neural networks: A review of methods and
 applications. *AI Open*, 1:57–81, 2020.
- [49] Zhuangdi Zhu, Junyuan Hong, and Jiayu Zhou. Data-free knowledge distillation for het erogeneous federated learning. In *International Conference on Machine Learning*, pages
 12878–12889. PMLR, 2021.

509 Checklist

510	1.	For all authors
511 512		(a) Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope? [Yes]
513 514		(b) Did you describe the limitations of your work? [Yes] We discuss them in Section D of the supplementary file.
515 516		(c) Did you discuss any potential negative societal impacts of your work? [Yes] We discuss them in Section D of the supplementary file.
517 518		(d) Have you read the ethics review guidelines and ensured that your paper conforms to them? [Yes]
519	2.	If you are including theoretical results
520		(a) Did you state the full set of assumptions of all theoretical results? [N/A]
521		(b) Did you include complete proofs of all theoretical results? [N/A]
522	3.	If you ran experiments
523 524 525		(a) Did you include the code, data, and instructions needed to reproduce the main experi- mental results (either in the supplemental material or as a URL)? [Yes] We provide the code, data, and instructions in the supplementary material.
526 527 528		(b) Did you specify all the training details (e.g., data splits, hyperparameters, how they were chosen)? [Yes] We specify all the training details in Section B of the supplementary file.
529 530 531		(c) Did you report error bars (e.g., with respect to the random seed after running exper- iments multiple times)? [Yes] We report the main results with mean and standard deviations, with multiple runs.
532 533 534		(d) Did you include the total amount of compute and the type of resources used (e.g., type of GPUs, internal cluster, or cloud provider)? [Yes] We include the computational costs and resources in Section B of the supplementary file.
535	4.	If you are using existing assets (e.g., code, data, models) or curating/releasing new assets
536		(a) If your work uses existing assets, did you cite the creators? [Yes]
537		(b) Did you mention the license of the assets? [N/A]
538 539		(c) Did you include any new assets either in the supplemental material or as a URL? $[N/A]$
540 541		(d) Did you discuss whether and how consent was obtained from people whose data you're using/curating? [N/A]
542 543		(e) Did you discuss whether the data you are using/curating contains personally identifiable information or offensive content? [N/A]
544	5.	If you used crowdsourcing or conducted research with human subjects
545 546		(a) Did you include the full text of instructions given to participants and screenshots, if applicable? [N/A]
547 548		(b) Did you describe any potential participant risks, with links to Institutional Review Board (IRB) approvals, if applicable? [N/A]
549 550		(c) Did you include the estimated hourly wage paid to participants and the total amount spent on participant compensation? [N/A]