

PSO-MERGING: MERGING MODELS BASED ON PARTICLE SWARM OPTIMIZATION

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Paper under double-blind review

ABSTRACT

Model merging has emerged as an efficient strategy for constructing multitask models by integrating the strengths of multiple available expert models, thereby reducing the need to fine-tune a pre-trained model for all the tasks from scratch. Existing data-independent methods struggle with performance limitations due to the lack of data-driven guidance. Data-driven approaches also face key challenges: gradient-based methods are computationally expensive, limiting their practicality for merging large expert models, whereas existing gradient-free methods often fail to achieve satisfactory results within a limited number of optimization steps. To address these limitations, this paper introduces PSO-Merging, a novel data-driven merging method based on the Particle Swarm Optimization (PSO). In this approach, we initialize the particle swarm with a pre-trained model, expert models, and sparsified expert models. We then perform multiple iterations, with the final global best particle serving as the merged model. Experimental results on different language models show that PSO-Merging generally outperforms baseline merging methods, offering a more efficient and scalable solution for model merging.

1 INTRODUCTION

In recent years, numerous powerful pre-trained Large Language Models (LLMs) have emerged, serving as the foundation for solving various language-related tasks (Brown et al., 2020; Touvron et al., 2023; Jiang et al., 2023; Grattafiori et al., 2024; Chung et al., 2024; DeepSeek-AI et al., 2024). To unlock the abilities of these LLMs on downstream tasks, post-training techniques such as fine-tuning, reinforcement learning with human feedback (RLHF), direct preference optimization (DPO), and Group Relative Policy Optimization (GRPO) are commonly employed (Rafailov et al., 2024; Ouyang et al., 2022; DeepSeek-AI et al., 2025). However, post-training is time-consuming and often requires substantial GPU and data resources.

Constructing a multitask model by performing post-training on the base model is highly resource-intensive. Fortunately, there are numerous open-source expert models available in the community that have undergone post-training on various downstream tasks. Thus, an alternative approach for building a multitask model is to merge post-trained expert models directly (Li et al., 2023a). By merging expert models in the parameter space, the capabilities of multiple downstream tasks can be consolidated into a single model. Model merging offers the benefit of simplicity and efficiency, demanding less data and fewer GPU resources compared to training.

Existing model merging methods can be broadly categorized based on whether they rely on data guidance. Data-independent approaches, which are often simpler, typically involve operations such as scaling, rescaling, pruning, or weighted merging of task vectors while addressing potential conflicts during the integration process (Yadav et al., 2023; Yu et al., 2024a; Ilharco et al., 2023). However, in the absence of data-specific guidance, these methods often struggle to achieve optimal performance due to their limited ability to adapt to the nuances of specific tasks. On the other hand, data-guided methods typically rely on gradient-based calculations to guide the merging process (Matena & Raffel, 2022; Yang et al., 2023). These approaches face significant challenges when applied to scenarios involving a large number of expert models with substantial parameter sizes, as the computational overhead and complexity become prohibitive. To avoid the need for gradient computation, Akiba et al. (2024) propose leveraging the Covariance Matrix Adaptation Evolution

Strategy (CMA-ES) to search for optimal merging weights based on existing methods. While this approach offers a gradient-free, data-driven alternative, it involves sampling in the solution space, where many samples are discarded in each iteration due to low evaluation scores. As a result, it requires a substantial number of iterative steps to achieve satisfactory results, making it inefficient.

In real-world scenarios, data for the target domain is at least available in limited quantities. The ideal model merging method should efficiently and fully utilize this data as guidance, while avoiding extensive computations. The Particle Swarm Optimization (PSO) (Kennedy & Eberhart, 1995) was originally proposed to search for the optimal solution to a target problem. It does not require gradient computation, instead relying on an evaluation function to assess the objective score, which can optionally incorporate data as guidance. This approach minimizes the need for extensive calculations. In each iteration, PSO guides each solution by leveraging information from other solutions, allowing it to more accurately identify the direction toward optimal solutions, which enhances its efficiency. As a result, PSO is particularly well-suited for an ideal model merging method.

In this work, we propose PSO-Merging, a novel model merging method inspired by the traditional PSO. Unlike the traditional approach of randomly initializing the particle swarm in PSO, our method initializes the particle swarm by using each expert model as the starting point. Moreover, we adopt the widely utilized sparsification technique, initially introduced to address parameter conflicts during the merging process. In our method, this technique also enables the generation of a larger number of particles, thereby facilitating a more favorable convergence toward high-quality solutions. After several rounds of the PSO optimization process, we use the final global best particle as the resulting merged model.

We evaluate our method on multiple model architectures, including Flan-T5, LLaMA, and Mistral. Experimental results illustrate that our approach outperforms baseline methods in terms of average scores and achieves significant improvements on certain tasks. Moreover, our experimental analysis demonstrates that PSO-Merging exhibits rapid convergence, and significantly outperforms the baseline methods in merging scenarios involving up to four large expert models.

2 METHODOLOGY

In this section, we first give a problem formulation of merging to enhance multitask capability (M-MTC) (Lu et al., 2024), then we introduce PSO-Merging, our novel model merging method based on the PSO. Finally, we provide a brief intuitive explanation of why PSO-Merging works.

2.1 PROBLEM FORMULATION

Assume we have a task set $T = \{\tau_1, \tau_2, \dots, \tau_n\}$ of size n . We begin with a pre-trained model parameterized by $\theta_0 \in \mathbb{R}^d$, where d denotes the number of parameters. This model then undergoes post-training on each task in T to adapt and specialize for the specific task. Specifically, for a task τ_t , the pre-trained model is fine-tuned on its corresponding dataset to become an expert in τ_t , parameterized by θ_t . The goal of M-MTC is to merge the set of experts $\Theta = \{\theta_1, \theta_2, \dots, \theta_n\}$ into a unified model θ_{merged} with multitask capability that performs well on T .

2.2 PSO-MERGING

An overview of PSO-Merging is demonstrated as Figure 1. Our method can be roughly divided into two stages: initialization and iterative updates.

Initialization The traditional PSO begins with a randomly initialized solution set $\Theta_{\text{initial}} = \{\theta_1^{(0)}, \theta_2^{(0)}, \dots, \theta_m^{(0)}\}$ of size m . However, at this stage, we initialize the solution set Θ_{initial} with the original experts along with the sparsified experts, which are acquired by the sparsification mechanism. The sparsification mechanism is widely employed in model merging to mitigate parameter conflicts (Yadav et al., 2023; Yu et al., 2024a; Deep et al., 2024). In our approach, we utilize sparsification not only to address parameter conflicts but also to increase the number of particles (initial solutions). A larger particle pool enables PSO to converge more effectively toward an optimal solution. For simplicity, we adopt the sparsification strategy from DARE. Specifically, for parameters θ_t and a drop rate p , the sparsified parameters $\hat{\theta}_t$ are obtained as follows:

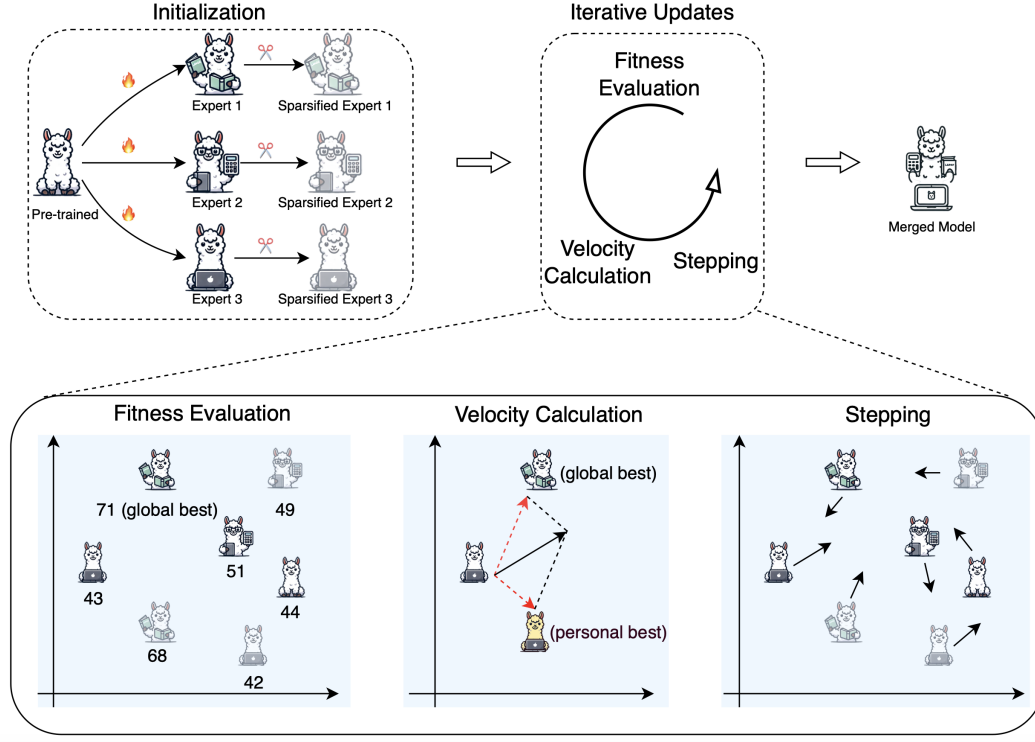


Figure 1: An overview of PSO-Merging. We begin by sparsifying all fine-tuned LLM experts. The swarm consists of the pre-trained model, the fine-tuned LLM experts, and the sparsified fine-tuned LLM experts. The update cycle consists of three steps: fitness evaluation, velocity calculation, and stepping. The axes in the figure represent the parameter space. The numbers in the fitness evaluation present each particle’s fitness score, corresponding to the average multitask score in our work. The black arrows indicate the stepping direction of each particle. For simplicity, we omit the momentum term in the velocity calculation.

$$m_i^t \sim \text{Bernoulli}(p), \quad i = 1, 2, \dots, d, \quad (1)$$

$$\mathbf{m}^t = [m_1^t, m_2^t, \dots, m_d^t] \in \mathbb{R}^d, \quad (2)$$

$$\tilde{\theta}_t = (\mathbf{1} - \mathbf{m}^t) \odot (\theta_t - \theta_0) / (1 - p) + \theta_0, \quad (3)$$

where $\odot$ represents element-wise multiplication, and θ_0 denotes the pre-trained parameters.

For the expert set $\Theta = \{\theta_1, \theta_2, \dots, \theta_n\}$, by using the sparsification technique, we acquire the sparsified expert set $\tilde{\Theta} = \{\tilde{\theta}_1, \tilde{\theta}_2, \dots, \tilde{\theta}_n\}$. To maximize the use of existing resources to increase the number of particles, we also include the pre-trained model in the initial solutions. So our initial solution set can be represented as

$$\Theta_{\text{initial}} = \Theta \cup \tilde{\Theta} \cup \{\theta_0\}. \quad (4)$$

Iterative Updates In this stage, we perform iterative updates for several steps to approach a good solution. Each update cycle consists of three main steps: fitness evaluation, velocity calculation, and position updating. Traditional Particle Swarm Optimization (PSO) defines the fitness function of a solution as the score of a specific task being solved. However, in our M-MTC scenario, we redefine the fitness function to represent the average score across all tasks, expressed as $f(\theta) = \frac{1}{n} \sum_{i=1}^n \text{score}_i(\theta)$. The velocity of each solution (similar to a gradient) is determined by its own personal best position and the global best position. The velocity formula of solution t on step i can be represented as:

$$\mathbf{v}_t^{(i)} = w \cdot \mathbf{v}_t^{(i-1)} + c_1 \cdot r_1 \cdot (\theta_{\text{gbest}}^{(i-1)} - \theta_t^{(i-1)}) + c_2 \cdot r_2 \cdot (\theta_{t,\text{pbest}}^{(i-1)} - \theta_t^{(i-1)}), \quad (5)$$

where c_1 and c_2 are parameters used to adjust how much PSO concerns the global and personal information. r_1 and r_2 are random variables that follow the uniform distribution, specifically, $r_1, r_2 \sim U(0, 1)$. w is a parameter that controls the momentum of the movement. The personal best position $\theta_{t,\text{pbest}}^{(i)}$ and the global best position $\theta_{\text{gbest}}^{(i)}$ until step i are defined as $\theta_{t,\text{pbest}}^{(i)} = \theta_t^{(\arg\max_{j \leq i} f(\theta_t^{(j)}))}$, $\theta_{\text{gbest}}^{(i)} = \theta_{\arg\max_t f(\theta_{t,\text{pbest}}^{(i)})}$.

Then we update each solution according to its own velocity:

$$\theta_t^{(i)} = \theta_t^{(i-1)} + \mathbf{v}_t^{(i)}. \quad (6)$$

After iterating for S steps starting with Θ_{initial} , we choose the final global best particle as our merged LLM, denoted as $\theta_{\text{merged}} = \theta_{\text{gbest}}^{(S)}$.

2.3 AN INTUITIVE EXPLANATION FOR WHY PSO-MERGING WORKS

Expanding Equation 6, we obtain the following expression:

$$\theta_t^{(i)} = c_1 \cdot r_1 \cdot \theta_{\text{gbest}}^{(i-1)} + c_2 \cdot r_2 \cdot \theta_{t,\text{pbest}}^{(i-1)} + (1 - c_1 \cdot r_1 - c_2 \cdot r_2) \cdot \theta_t^{(i-1)} + w \cdot \mathbf{v}_t^{(i-1)}, \quad (7)$$

where, when ignoring the momentum term $w \cdot \mathbf{v}_t^{(i-1)}$, the equation represents a linear combination of $\theta_t^{(i-1)}$, $\theta_{\text{gbest}}^{(i-1)}$ and $\theta_{t,\text{pbest}}^{(i-1)}$. Previous studies have demonstrated the effectiveness of this linear combination (Ilharco et al., 2023). Intuitively, iterating multiple times allows us to find a more optimal linear combination, guided by the data, thereby improving the merged model. The momentum term further helps balance exploration and exploitation by maintaining a particle’s velocity, enabling it to escape local optima and enhancing the overall global search capability (Kennedy & Eberhart, 1995).

Earlier studies have shown that the sparsification mechanism can help mitigate parameter conflicts (Yu et al., 2024a). Since our initial particle swarm includes sparsified models (which contribute to the initial states $\theta_t^{(0)}$ and subsequently influence $\theta_{\text{gbest}}^{(i)}$ and $\theta_{t,\text{pbest}}^{(i)}$ throughout iterations), the search process benefits from exploring regions influenced by this initial sparsification. This helps mitigate parameter conflicts when forming the combined parameters $\theta_t^{(i)}$.

3 EXPERIMENTS

In this section, we present the experimental results obtained using four different base language models: Flan-T5-Base (Chung et al., 2024), Llama-3-8B (Grattafiori et al., 2024), Llama-2-13B (Touvron et al., 2023), and Mistral-7B-v0.3 (Jiang et al., 2023). The results demonstrate that our method achieves performance superior to the baseline methods, thereby proving its effectiveness and highlighting its advantages.

3.1 BASELINES

We choose the following model merging methods as our baseline methods.

Task Arithmetic This method involves scaling each task vector by a factor and then combining them with the pre-trained model (Ilharco et al., 2023).

DARE-Linear Each task vector is first sparsified randomly and rescaled before being merged into the pre-trained model (Yu et al., 2024a).

TIES-Merging This method retains the top-k parameters based on absolute values, resolves sign conflicts among different task vectors, and then integrates them into the pre-trained model (Yadav et al., 2023).

DARE-TIES Task vectors are initially sparsified randomly and rescaled, followed by resolving sign conflicts across task vectors before merging them with the pre-trained model (Yu et al., 2024a; Yadav et al., 2023).

DELLA-Merging Parameters are pruned based on their magnitudes, with different pruning probabilities assigned accordingly. Post-pruning, the process follows the same steps as TIES-Merging (Deep et al., 2024).

RankMean This approach determines merging weights for parameters across expert models based on their relative rank in terms of weight change magnitude. The parameters in each module are then aggregated through a weighted average using these coefficients (Perin et al., 2024).

Evo We adopt the parameter-space merging component of Akiba et al. (2024)’s method. This approach uses CMA-ES to search for optimal merging parameters based on existing methods. We use Task Arithmetic as the base method and employ CMA-ES to explore the merging weights.

Adamerging This method directly treats the merging weights as trainable parameters, optimizing them by minimizing entropy on unlabeled test samples as a surrogate objective function.

Fisher-Merging This approach leverages labeled data from each task to estimate a diagonal approximation of the Fisher matrix, which is then interpreted as the importance of the corresponding task-specific expert.

RegMean This method combines multiple models by minimizing the difference in their predictions on training data, often using inner product matrices.

3.2 IMPLEMENTATION DETAILS

We conducted experiments using four distinct base language models: Flan-T5-Base, Llama-2-13B, Llama-3-8B, and Mistral-7B-v0.3. In our approach, we set the parameters $c_1 = 2$, $c_2 = 2$, and $w = 0.2$. We set the total optimization steps $S = 50$ for the Flan-T5-Base experiments and $S = 5$ for other experiments. For the Evo baseline, to ensure a fair comparison, we set the number of evaluation iterations to $n * S$ in all experiments, where n denotes the number of experts and S corresponds to the number of iterations in PSO-Merging. This aligns the evaluation count with that of PSO-Merging. However, in the actual implementation, the number of evaluation iterations in Evo slightly exceeds the set value. For the sparsification component, we applied a drop rate of $p = 0.8$ in all methods that incorporate sparsification including ours. For all baseline methods that include a fixed scaling term, we choose the scaling term to be either $\frac{1}{n}$ or 1.0, where n is the number of expert models. We report the result with the higher average score.

Table 1: Multitask performance when merging experts based on Flan-T5-Base.

Method	COLA	MNLI	MRPC	QNLI	QQP	RTE	SST2	STSB	AVG
Task Arithmetic	69.13	62.65	79.41	89.80	83.86	81.23	91.74	73.22	78.88
DARE-Linear	69.51	63.79	79.66	89.88	83.89	81.23	91.74	69.83	78.69
TIES-Merging	69.22	59.39	77.70	89.33	83.36	80.51	91.28	68.38	77.40
DARE-TIES	69.32	62.50	79.66	89.77	83.83	81.59	91.28	71.10	78.63
DELLA-Merging	69.32	64.40	79.90	89.90	83.82	81.95	91.06	75.96	79.54
Rankmean	69.13	56.45	76.23	88.45	82.12	80.14	91.17	62.21	75.74
Evo	70.85	82.91	75.74	89.35	73.91	80.87	92.20	69.70	79.44
Adamerging	69.89	77.17	79.90	89.80	81.73	79.06	91.40	66.05	79.38
Fisher-Merging	69.32	54.03	76.72	84.64	83.57	77.62	88.07	74.35	76.04
RegMean	69.13	26.64	75.25	79.33	77.17	61.73	86.01	48.14	65.43
PSO-Merging	68.17	83.80	80.64	89.53	83.56	81.23	91.06	71.94	81.24

Flan-T5-Base Experiments Following the experimental settings of previous work (Tang et al., 2024), we selected eight text-to-text generation tasks from the General Language Understanding

Table 2: Multitask performance when merging experts based on Llama-2-13B, Llama-3-8B, and Mistral-7B-v0.3.

	Method	AlpacaEval	MBPP	GSM8K	AVG
Llama-2-13B	Task Arithmetic	82.48	16.80	54.13	51.14
	DARE-Linear	69.36	4.00	29.80	34.38
	TIES-Merging	64.82	32.80	59.06	52.23
	DARE-TIES	73.40	8.20	32.52	38.04
	DELLA-Merging	74.38	9.20	36.24	39.94
	Rankmean	55.13	30.80	57.54	47.82
	Evo	61.08	32.60	56.86	50.18
	PSO-Merging	80.11	26.00	64.37	56.82
Llama-3-8B	Task Arithmetic	63.79	31.00	56.56	50.45
	DARE-Linear	60.98	8.00	53.75	40.91
	TIES-Merging	73.72	45.40	57.54	58.89
	DARE-TIES	71.69	49.20	59.97	60.29
	DELLA-Merging	61.22	4.60	56.18	40.67
	Rankmean	40.96	49.40	50.72	47.03
	Evo	55.74	49.00	56.10	51.95
	PSO-Merging	80.01	51.40	51.93	61.12
Mistral-7B-v0.3	Task Arithmetic	57.72	42.40	50.72	50.28
	DARE-Linear	57.26	41.40	50.42	49.69
	TIES-Merging	72.08	36.40	51.86	53.45
	DARE-TIES	57.84	43.00	50.19	50.34
	DELLA-Merging	57.58	42.40	51.25	50.41
	Rankmean	51.14	42.20	50.87	48.07
	Evo	60.66	51.93	41.80	51.47
	PSO-Merging	71.33	41.20	53.53	55.35

Evaluation (GLUE) benchmark (Wang et al., 2018): CoLA, MNLI, MRPC, QNLI, QQP, RTE, SST-2, and STSB. The expert models were sourced from HuggingFace.¹ For evaluation, we report Spearman’s ρ for STSB and exact match accuracy for the other tasks.

Llama-2-13B, Llama-3-8B, and Mistral-7B-v0.3 Experiments In accordance with the experimental settings of prior research (Yu et al., 2024a), we conducted experiments on merging three specialized experts: an instruction-following expert, a mathematical reasoning expert, and a code-generating expert. For Llama-2-13B, the three experts were WizardLM-13B-v1.2, WizardMath-13B-v1.0, and Llama-2-13B-Code-Alpaca. For Llama-3-8B and Mistral-7B-v0.3, we trained corresponding experts tailored to each base model. Detailed training procedures are described in Appendix A. For evaluation, we assess instruction-following ability using the win rate on AlpacaEval (Li et al., 2023b), mathematical reasoning ability using zero-shot accuracy on GSM8K (Cobbe et al., 2021), and code-generating ability using `pass@1` on MBPP (Austin et al., 2021). We use Llama-3.1-70B under the Ollama² framework as the judge for the AlpacaEval task. We use xFinder³ (Yu et al., 2024b) to extract the answer for the GSM8K task.

3.3 EXPERIMENTAL RESULTS

In the Flan-T5-Base experiment setup, we randomly selected 50 samples from the training set of each task to form the optimization set, which was used to calculate the fitness. The evaluation results are summarized in Table 1. Remarkably, our method outperforms all baseline methods significantly on the MNLI task and demonstrates a clear advantage in average score across all tasks.

For the experiments with Llama-2-13B, Llama-3-8B, and Mistral-7B-v0.3, the dataset for each task was partitioned into an optimization set and a test set, with a 1:10 ratio. Comprehensive dataset statistics are provided in Appendix B. The evaluation results are shown in Tables 2. Notably, our method demonstrates a substantial improvement over all baseline approaches, achieving the highest

¹<https://huggingface.co/collections/tanganke/flan-t5-base-models-fine-tuned-on-glue-benchmark-664f30d7966303d9a0a90bb6>

²<https://ollama.com/>

³<https://huggingface.co/IAAR-Shanghai/xFinder-qwen1505>

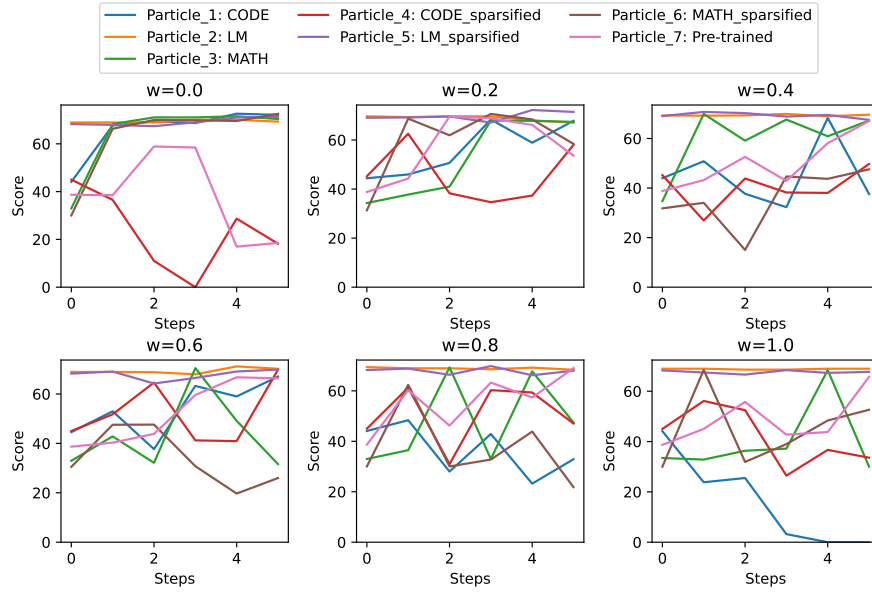


Figure 2: The score variations on the optimization set for all particles with different w values. The legend indicates the expert used to initialize each particle and specifies whether the expert has been sparsified. All lines represent scores on the optimization set. **CODE** denotes the code-generation expert, **LM** refers to the instruction-following expert, and **MATH** represents the mathematical reasoning expert.

Table 3: Multitask performance when merging experts based on Llama-3-8B of four tasks.

Method	AlpacaEval	MBPP	GSM8K	SciQ	AVG
Task Arithmetic	50.63	50.20	51.86	82.20	58.72
DARE-Linear	61.19	37.00	55.12	79.30	58.15
TIES-Merging	53.37	49.00	54.13	82.60	59.78
DARE-TIES	50.49	49.60	53.22	82.80	59.03
DELLA-Merging	51.60	49.20	53.15	82.30	59.06
Rankmean	35.62	48.20	47.23	72.30	50.84
Evo	55.74	49.60	50.87	82.90	59.78
PSO-Merging	80.89	50.60	49.58	76.80	64.47

average score across all experimental settings. Due to the considerable memory demands associated with gradient computations (Adamerging, Fisher-Merging) or the necessity of retaining intermediate activations (RegMean), precluding their effective application with large-scale models like those explored here, we did not compare against these baselines.

4 ANALYSIS

In this section, we explore the impact of some hyper-parameters in our method. Additionally, we validated the effectiveness of our method in scenarios involving the fusion of more experts. All the analysis experiments were conducted under the Llama-3-8B experimental settings.

4.1 IMPACT OF THE MOMENTUM COEFFICIENT w

We present the optimization process for different choices of w in Figure 2. When $w = 0.0$, most particles converge to high scores, but two particles remain unoptimized. As w increases beyond 0.2, almost all particles fail to optimize, with the situation worsening as w grows larger. Notably, when

Table 4: Multitask performances when setting $\Theta_{\text{initial}} = \Theta$ and $\Theta_{\text{initial}} = \tilde{\Theta}$.

Method	AlpacaEval	MBPP	GSM8K	AVG
PSO-Merging($\Theta_{\text{initial}} = \Theta$, 3 particles)	80.85	49.80	47.84	59.50
PSO-Merging($\Theta_{\text{initial}} = \tilde{\Theta}$, 3 particles)	81.46	50.00	50.27	60.57
PSO-Merging($\Theta_{\text{initial}} = \Theta \cup \tilde{\Theta} \cup \{\theta_0\}$, 7 particles)	80.01	51.40	51.93	61.12

$w = 0.2$, all particles successfully converge to comparably high scores, indicating that setting the momentum parameter $w = 0.2$ is a reasonable choice.

4.2 PERFORMANCE IN MERGING MORE EXPERTS

We conducted the four-task experiment to explore the performance of PSO-Merging when merging more experts. We incorporated an additional task, SciQ (Welbl et al., 2017) in this experiment. The results are presented in Table 3, demonstrating that PSO-Merging outperforms all methods when merging four experts.

4.3 CONVERGENCE BEHAVIOR OF PSO-MERGING

In this section, we investigate the convergence behavior of PSO-Merging. We present in Figure 3 the variation in the fitness scores of the seven particles in the optimization set over 40 optimization steps. Additionally, we illustrate the change in the fitness score of the global best particle on the test set throughout the optimization process. The plot demonstrates that all particles converge rapidly within 10 steps on the optimization set, with the majority converging within the first 5 steps. Notably, PSO-Merging achieves satisfactory performance on the test set within just 5 steps.

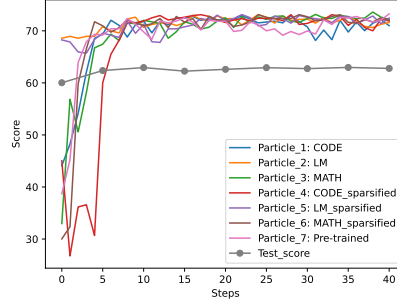


Figure 3: The score variations on both the optimization set and the test set over the course of 40 optimization steps. **Test_score** denotes the score of the global best particle on the test set. All other lines represent the scores of different particles on the optimization set.

4.4 EFFECT OF NUMBER OF PARTICLES

To validate the impact of the number of particles in PSO-Merging and the effect of the sparsification mechanism, we conducted experiments using two different configurations: $\Theta_{\text{initial}} = \Theta$ and $\Theta_{\text{initial}} = \tilde{\Theta}$. The results, presented in Table 4, show that merging only the original experts yields the lowest score while merging only the sparsified experts achieves a higher score. This suggests that the sparsification mechanism effectively reduces parameter conflicts between the models. Furthermore, when $\Theta_{\text{initial}} = \Theta \cup \tilde{\Theta} \cup \{\theta_0\}$, the score is the highest, indicating that a larger number of particles facilitates the creation of a better-merged model.

4.5 EFFICIENCY COMPARED WITH GRADIENT-BASED METHODS

Fisher Merging necessitates computing per-example gradients across all parameters for each expert, incurring a memory cost comparable to training on N examples (around 28GB per 7B model), making it impractical for merging multiple large models. RegMean, requiring the retention of intermediate activations for all merging models during optimization, also presents a significant memory overhead. Similarly, Adamerging, while training only merging weights, requires loading all models simultaneously (e.g., 42GB for three 7B models). In contrast, PSO-Merging operates solely on inference, requiring less memory, exemplified by its 14GB requirement in the same three 7B model scenario.

5 RELATED WORK

Model Merging In recent years, model merging has gained significant attention as a versatile approach in machine learning research. Lu et al. (2024) categorizes current studies on model merging into two main directions: merging to achieve a relatively optimal solution (M-ROS) and merging to enhance multitask capability (M-MTC). Our work focuses on M-MTC, aiming at constructing multitask models, and we provide an overview of related studies in this scenario. These methods are categorized into data-independent methods and data-guided methods.

For data-independent methods, Ilharco et al. (2023) introduced the concept of a *Task Vector*, defined as the difference between the parameters of a post-trained model and its corresponding pre-trained model. By multiplying these task vectors with the merging weights and summing them, a merged task vector is obtained. This vector, when combined with the pre-trained parameters, produces the final merged model. Building on this framework, TIES-Merging (Yadav et al., 2023) improves the process by pruning low-magnitude parameters and resolving sign disagreements prior to merging, thereby enhancing its effectiveness. To address parameter conflicts among task vectors, Yu et al. (2024a) proposed DARE, a method that randomly sparsifies and rescales task vectors to reduce task vector redundancy. Alternatively, Deep et al. (2024) introduced DELLA-Merging, which replaces the pruning mechanism of TIES-Merging by employing a probabilistic distribution based on the magnitude rank of task vector parameters. Rankmean (Perin et al., 2024) computes module-specific merging weights for each expert model based on magnitude ranks.

For data-guided methods, Fisher Merging (Matena & Raffel, 2022) uses some labeled data for each task to estimate the diagonal approximate Fisher matrix, which is treated as the importance of the task-specific expert. Then the diagonal approximate Fisher matrix is applied to merge the models as the merging weights. Adamerging (Yang et al., 2023) treats the merging weights as trainable parameters directly, using entropy minimization on unlabeled test samples as a surrogate objective function to optimize the merging weights. To eliminate the need to calculate the gradients, Akiba et al. (2024) propose to use CMA-ES to search for optimal merging weights. However, it requires sampling within the solution space, where many samples are discarded in each iteration because of poor evaluation scores. Consequently, it demands a large number of iterations to obtain satisfactory results, which makes it inefficient. Model Swarms (Feng et al., 2024) is another iterative model merging method.

Particle Swarm Optimization Particle Swarm Optimization (PSO) (Kennedy & Eberhart, 1995) is a stochastic optimization algorithm inspired by the collective intelligence observed in natural phenomena such as bird flocking and fish schooling. In PSO, a population of particles represents potential solutions, each navigating the search space by adjusting its position based on its own experiences and the best solutions discovered by the entire swarm. This cooperative mechanism allows particles to efficiently explore the search space, while also honing in on regions of interest through shared information. The method excels at balancing exploration and exploitation, enabling rapid convergence to optimal or near-optimal solutions.

6 CONCLUSION

In this work, we introduce PSO-Merging, a novel model merging method that adapts traditional Particle Swarm Optimization (PSO) to the model merging scenario. We first demonstrate the strong applicability of PSO for model merging tasks. To further enhance its effectiveness, we incorporate a widely used sparsification mechanism, which mitigates parameter conflicts and allows the utilization of a larger number of linearly independent particles. Building on these insights, PSO-Merging leverages task-specific data to produce merged models with superior performance. We also provide an intuitive explanation of its effectiveness. Extensive experiments under various settings show that PSO-Merging achieves effective merging of multiple expert models and consistently outperforms baseline methods. Additionally, our analysis explores the influence of key hyperparameters and confirms the potential of PSO-Merging in scenarios involving the merging of a greater number of experts.

REFERENCES

- Takuya Akiba, Makoto Shing, Yujin Tang, Qi Sun, and David Ha. Evolutionary optimization of model merging recipes. *arXiv preprint arXiv:2403.13187*, 2024.
- Jacob Austin, Augustus Odena, Maxwell Nye, Maarten Bosma, Henryk Michalewski, David Dohan, Ellen Jiang, Carrie Cai, Michael Terry, Quoc Le, et al. Program synthesis with large language models. *arXiv preprint arXiv:2108.07732*, 2021.
- Tom B. Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, Sandhini Agarwal, Ariel Herbert-Voss, Gretchen Krueger, Tom Henighan, Rewon Child, Aditya Ramesh, Daniel M. Ziegler, Jeffrey Wu, Clemens Winter, Christopher Hesse, Mark Chen, Eric Sigler, Mateusz Litwin, Scott Gray, Benjamin Chess, Jack Clark, Christopher Berner, Sam McCandlish, Alec Radford, Ilya Sutskever, and Dario Amodei. Language models are few-shot learners, 2020. URL <https://arxiv.org/abs/2005.14165>.
- Hyung Won Chung, Le Hou, Shayne Longpre, Barret Zoph, Yi Tay, William Fedus, Yunxuan Li, Xuezhi Wang, Mostafa Dehghani, Siddhartha Brahma, Albert Webson, Shixiang Shane Gu, Zhuyun Dai, Mirac Suzgun, Xinyun Chen, Aakanksha Chowdhery, Alex Castro-Ros, Marie Pellat, Kevin Robinson, Dasha Valter, Sharan Narang, Gaurav Mishra, Adams Yu, Vincent Y. Zhao, Yanping Huang, Andrew M. Dai, Hongkun Yu, Slav Petrov, Ed H. Chi, Jeff Dean, Jacob Devlin, Adam Roberts, Denny Zhou, Quoc V. Le, and Jason Wei. Scaling instruction-finetuned language models. *J. Mach. Learn. Res.*, 25:70:1–70:53, 2024. URL <https://jmlr.org/papers/v25/23-0870.html>.
- Karl Cobbe, Vineet Kosaraju, Mohammad Bavarian, Mark Chen, Heewoo Jun, Lukasz Kaiser, Matthias Plappert, Jerry Tworek, Jacob Hilton, Reiichiro Nakano, et al. Training verifiers to solve math word problems. *arXiv preprint arXiv:2110.14168*, 2021.
- Pala Tej Deep, Rishabh Bhardwaj, and Soujanya Poria. Della-merging: Reducing interference in model merging through magnitude-based sampling. *arXiv preprint arXiv:2406.11617*, 2024.
- DeepSeek-AI, Aixin Liu, Bei Feng, Bing Xue, Bingxuan Wang, Bochao Wu, Chengda Lu, Cheng-gang Zhao, Chengqi Deng, Chenyu Zhang, Chong Ruan, Damai Dai, Daya Guo, Dejian Yang, Deli Chen, Dongjie Ji, Erhang Li, Fangyun Lin, Fucong Dai, Fuli Luo, Guangbo Hao, Guanting Chen, Guowei Li, H. Zhang, Han Bao, Hanwei Xu, Haocheng Wang, Haowei Zhang, Honghui Ding, Huajian Xin, Huazuo Gao, Hui Li, Hui Qu, J. L. Cai, Jian Liang, Jianzhong Guo, Jiaqi Ni, Jiashi Li, Jiawei Wang, Jin Chen, Jingchang Chen, Jingyang Yuan, Junjie Qiu, Junlong Li, Junxiao Song, Kai Dong, Kai Hu, Kaige Gao, Kang Guan, Kexin Huang, Kuai Yu, Lean Wang, Lecong Zhang, Lei Xu, Leyi Xia, Liang Zhao, Litong Wang, Liyue Zhang, Meng Li, Miaojuan Wang, Mingchuan Zhang, Minghua Zhang, Minghui Tang, Mingming Li, Ning Tian, Panpan Huang, Peiyi Wang, Peng Zhang, Qiancheng Wang, Qihao Zhu, Qinyu Chen, Qiushi Du, R. J. Chen, R. L. Jin, Ruiqi Ge, Ruisong Zhang, Ruizhe Pan, Runji Wang, Runxin Xu, Ruoyu Zhang, Ruyi Chen, S. S. Li, Shanghao Lu, Shangyan Zhou, Shanhuang Chen, Shaoqing Wu, Shengfeng Ye, Shengfeng Ye, Shirong Ma, Shiyu Wang, Shuang Zhou, Shuiping Yu, Shunfeng Zhou, Shut-ing Pan, T. Wang, Tao Yun, Tian Pei, Tianyu Sun, W. L. Xiao, Wangding Zeng, Wanbiao Zhao, Wei An, Wen Liu, Wenfeng Liang, Wenjun Gao, Wenqin Yu, Wentao Zhang, X. Q. Li, Xiangyue Jin, Xianzu Wang, Xiao Bi, Xiaodong Liu, Xiaohan Wang, Xiaojin Shen, Xiaokang Chen, Xiaokang Zhang, Xiaosha Chen, Xiaotao Nie, Xiaowen Sun, Xiaoxiang Wang, Xin Cheng, Xin Liu, Xin Xie, Xingchao Liu, Xingkai Yu, Xinnan Song, Xinxia Shan, Xinyi Zhou, Xinyu Yang, Xinyuan Li, Xuecheng Su, Xuheng Lin, Y. K. Li, Y. Q. Wang, Y. X. Wei, Y. X. Zhu, Yang Zhang, Yanhong Xu, Yanhong Xu, Yanping Huang, Yao Li, Yao Zhao, Yaofeng Sun, Yaohui Li, Yaohui Wang, Yi Yu, Yi Zheng, Yichao Zhang, Yifan Shi, Yiliang Xiong, Ying He, Ying Tang, Yishi Piao, Yisong Wang, Yixuan Tan, Yiyang Ma, Yiyuan Liu, Yongqiang Guo, Yu Wu, Yuan Ou, Yuchen Zhu, Yudian Wang, Yue Gong, Yuheng Zou, Yujia He, Yukun Zha, Yunfan Xiong, Yunxian Ma, Yuting Yan, Yuxiang Luo, Yuxiang You, Yuxuan Liu, Yuyang Zhou, Z. F. Wu, Z. Z. Ren, Zehui Ren, Zhangli Sha, Zhe Fu, Zhean Xu, Zhen Huang, Zhen Zhang, Zhenda Xie, Zhengyan Zhang, Zhewen Hao, Zhibin Gou, Zhicheng Ma, Zhigang Yan, Zhihong Shao, Zhipeng Xu, Zhiyu Wu, Zhongyu Zhang, Zhuoshu Li, Zihui Gu, Zijia Zhu, Zijun Liu, Zilin Li, Ziwei Xie, Ziyang Song, Ziyi Gao, and Zizheng Pan. Deepseek-v3 technical report, 2024. URL <https://arxiv.org/abs/2412.19437>.

- DeepSeek-AI, Daya Guo, Dejian Yang, Haowei Zhang, Junxiao Song, Ruoyu Zhang, Runxin Xu, Qihao Zhu, Shirong Ma, Peiyi Wang, Xiao Bi, Xiaokang Zhang, Xingkai Yu, Yu Wu, Z. F. Wu, Zhibin Gou, Zhihong Shao, Zhuoshu Li, Ziyi Gao, Aixin Liu, Bing Xue, Bingxuan Wang, Bochao Wu, Bei Feng, Chengda Lu, Chenggang Zhao, Chengqi Deng, Chenyu Zhang, Chong Ruan, Damai Dai, Deli Chen, Dongjie Ji, Erhang Li, Fangyun Lin, Fucong Dai, Fuli Luo, Guangbo Hao, Guanting Chen, Guowei Li, H. Zhang, Han Bao, Hanwei Xu, Haocheng Wang, Honghui Ding, Huajian Xin, Huazuo Gao, Hui Qu, Hui Li, Jianzhong Guo, Jiashi Li, Jiawei Wang, Jingchang Chen, Jingyang Yuan, Junjie Qiu, Junlong Li, J. L. Cai, Jiaqi Ni, Jian Liang, Jin Chen, Kai Dong, Kai Hu, Kaige Gao, Kang Guan, Kexin Huang, Kuai Yu, Lean Wang, Lecong Zhang, Liang Zhao, Litong Wang, Liyue Zhang, Lei Xu, Leyi Xia, Mingchuan Zhang, Minghua Zhang, Minghui Tang, Meng Li, Miaojun Wang, Mingming Li, Ning Tian, Panpan Huang, Peng Zhang, Qiancheng Wang, Qinyu Chen, Qiushi Du, Ruiqi Ge, Ruisong Zhang, Ruizhe Pan, Runji Wang, R. J. Chen, R. L. Jin, Ruyi Chen, Shanghao Lu, Shangyan Zhou, Shanhuang Chen, Shengfeng Ye, Shiyu Wang, Shuiping Yu, Shunfeng Zhou, Shuting Pan, S. S. Li, Shuang Zhou, Shaoqing Wu, Shengfeng Ye, Tao Yun, Tian Pei, Tianyu Sun, T. Wang, Wangding Zeng, Wanbiao Zhao, Wen Liu, Wenfeng Liang, Wenjun Gao, Wenqin Yu, Wentao Zhang, W. L. Xiao, Wei An, Xiaodong Liu, Xiaohan Wang, Xiaokang Chen, Xiaotao Nie, Xin Cheng, Xin Liu, Xin Xie, Xingchao Liu, Xinyu Yang, Xinyuan Li, Xuecheng Su, Xuheng Lin, X. Q. Li, Xiangyue Jin, Xiaojin Shen, Xiaosha Chen, Xiaowen Sun, Xiaoxiang Wang, Xinnan Song, Xinyi Zhou, Xianzu Wang, Xinxia Shan, Y. K. Li, Y. Q. Wang, Y. X. Wei, Yang Zhang, Yanhong Xu, Yao Li, Yao Zhao, Yaofeng Sun, Yaohui Wang, Yi Yu, Yichao Zhang, Yifan Shi, Yiliang Xiong, Ying He, Yishi Piao, Yisong Wang, Yixuan Tan, Yiyang Ma, Yiyuan Liu, Yongqiang Guo, Yuan Ou, Yudian Wang, Yue Gong, Yuheng Zou, Yujia He, Yunfan Xiong, Yuxiang Luo, Yuxiang You, Yuxuan Liu, Yuyang Zhou, Y. X. Zhu, Yanhong Xu, Yanping Huang, Yaohui Li, Yi Zheng, Yuchen Zhu, Yunxian Ma, Ying Tang, Yukun Zha, Yuting Yan, Z. Z. Ren, Zehui Ren, Zhangli Sha, Zhe Fu, Zhean Xu, Zhenda Xie, Zhengyan Zhang, Zhewen Hao, Zhicheng Ma, Zhigang Yan, Zhiyu Wu, Zihui Gu, Zijia Zhu, Zijun Liu, Zilin Li, Ziwei Xie, Ziyang Song, Zizheng Pan, Zhen Huang, Zhipeng Xu, Zhongyu Zhang, and Zhen Zhang. Deepseek-rl: Incentivizing reasoning capability in llms via reinforcement learning, 2025. URL <https://arxiv.org/abs/2501.12948>.
- Shangbin Feng, Zifeng Wang, Yike Wang, Sayna Ebrahimi, Hamid Palangi, Lesly Miculicich, Achin Kulshrestha, Nathalie Rauschmayr, Yejin Choi, Yulia Tsvetkov, et al. Model swarms: Collaborative search to adapt llm experts via swarm intelligence. *arXiv preprint arXiv:2410.11163*, 2024.
- Aaron Grattafiori, Abhimanyu Dubey, Abhinav Jauhri, Abhinav Pandey, Abhishek Kadian, Ahmad Al-Dahle, Aiesha Letman, Akhil Mathur, Alan Schelten, Alex Vaughan, Amy Yang, Angela Fan, Anirudh Goyal, Anthony Hartshorn, Aobo Yang, Archi Mitra, Archie Sravankumar, Artem Korenev, Arthur Hinsvark, Arun Rao, Aston Zhang, Aurelien Rodriguez, Austen Gregerson, Ava Spataru, Baptiste Roziere, Bethany Biron, Binh Tang, Bobbie Chern, Charlotte Caucheteux, Chaya Nayak, Chloe Bi, Chris Marra, Chris McConnell, Christian Keller, Christophe Touret, Chunyang Wu, Corinne Wong, Cristian Canton Ferrer, Cyrus Nikolaidis, Damien Allonsius, Daniel Song, Danielle Pintz, Danny Livshits, Danny Wyatt, David Esiobu, Dhruv Choudhary, Dhruv Mahajan, Diego Garcia-Olano, Diego Perino, Dieuwke Hupkes, Egor Lakomkin, Ehab AlBadawy, Elina Lobanova, Emily Dinan, Eric Michael Smith, Filip Radenovic, Francisco Guzmán, Frank Zhang, Gabriel Synnaeve, Gabrielle Lee, Georgia Lewis Anderson, Govind Thattai, Graeme Nail, Gregoire Mialon, Guan Pang, Guillem Cucurell, Hailey Nguyen, Hannah Korevaar, Hu Xu, Hugo Touvron, Iliyan Zarov, Imanol Arrieta Ibarra, Isabel Kloumann, Ishan Misra, Ivan Evtimov, Jack Zhang, Jade Copet, Jaewon Lee, Jan Geffert, Jana Vranes, Jason Park, Jay Mahadeokar, Jeet Shah, Jelmer van der Linde, Jennifer Billock, Jenny Hong, Jenya Lee, Jeremy Fu, Jianfeng Chi, Jianyu Huang, Jiawen Liu, Jie Wang, Jiecao Yu, Joanna Bitton, Joe Spisak, Jongsoo Park, Joseph Rocca, Joshua Johnstun, Joshua Saxe, Junteng Jia, Kalyan Vasuden Alwala, Karthik Prasad, Kartikeya Upasani, Kate Plawiak, Ke Li, Kenneth Heafield, Kevin Stone, Khalid El-Arini, Krithika Iyer, Kshitiz Malik, Kuenley Chiu, Kunal Bhalla, Kushal Lakhotia, Lauren Rantala-Young, Laurens van der Maaten, Lawrence Chen, Liang Tan, Liz Jenkins, Louis Martin, Lovish Madaan, Lubo Malo, Lukas Blecher, Lukas Landzaat, Luke de Oliveira, Madeline Muzzi, Mahesh Pasupuleti, Mannat Singh, Manohar Paluri, Marcin Kardas, Maria Tsimpoukelli, Mathew Oldham, Mathieu Rita, Maya Pavlova, Melanie Kambadur, Mike Lewis, Min Si, Mitesh Kumar Singh, Mona Hassan, Naman Goyal, Narjes Torabi, Nikolay Bashlykov, Nikolay Bogoychev, Niladri Chatterji, Ning Zhang, Olivier Duchenne, Onur Çelebi, Patrick Alrassy, Pengchuan Zhang, Pengwei Li, Petar Vasic, Peter Weng, Prajjwal Bhargava, Pratik Dubal, Praveen Krishnan,

Punit Singh Koura, Puxin Xu, Qing He, Qingxiao Dong, Ragavan Srinivasan, Raj Ganapathy, Ramon Calderer, Ricardo Silveira Cabral, Robert Stojnic, Roberta Raileanu, Rohan Maheswari, Rohit Girdhar, Rohit Patel, Romain Sauvestre, Ronnie Polidoro, Roshan Sumbaly, Ross Taylor, Ruan Silva, Rui Hou, Rui Wang, Saghar Hosseini, Sahana Chennabasappa, Sanjay Singh, Sean Bell, Seohyun Sonia Kim, Sergey Edunov, Shaoliang Nie, Sharan Narang, Sharath Rapparthi, Sheng Shen, Shengye Wan, Shruti Bhosale, Shun Zhang, Simon Vandenhende, Soumya Batra, Spencer Whitman, Sten Sootla, Stephane Collet, Suchin Gururangan, Sydney Borodinsky, Tamar Herman, Tara Fowler, Tarek Sheasha, Thomas Georgiou, Thomas Scialom, Tobias Speckbacher, Todor Mihaylov, Tong Xiao, Ujjwal Karn, Vedanuj Goswami, Vibhor Gupta, Vignesh Ramanathan, Viktor Kerkez, Vincent Gonguet, Virginie Do, Vish Vogeti, Vitor Albiero, Vladan Petrovic, Weiwei Chu, Wenhan Xiong, Wenyin Fu, Whitney Meers, Xavier Martinet, Xiaodong Wang, Xiaofang Wang, Xiaoqing Ellen Tan, Xide Xia, Xinfeng Xie, Xuchao Jia, Xuwei Wang, Yaelle Goldschlag, Yashesh Gaur, Yasmine Babaei, Yi Wen, Yiwen Song, Yuchen Zhang, Yue Li, Yuning Mao, Zacharie DelPierre Coudert, Zheng Yan, Zhengxing Chen, Zoe Papakipos, Aaditya Singh, Aayushi Srivastava, Abha Jain, Adam Kelsey, Adam Shajnfeld, Adithya Gangidi, Adolfo Victoria, Ahuva Goldstand, Ajay Menon, Ajay Sharma, Alex Boesenberg, Alexei Baevski, Allie Feinstein, Amanda Kallet, Amit Sangani, Amos Teo, Anam Yunus, Andrei Lupu, Andres Alvarado, Andrew Caples, Andrew Gu, Andrew Ho, Andrew Poulton, Andrew Ryan, Ankit Ramchandani, Annie Dong, Annie Franco, Anuj Goyal, Aparajita Saraf, Arkabandhu Chowdhury, Ashley Gabriel, Ashwin Bharambe, Assaf Eisenman, Azadeh Yazdan, Beau James, Ben Maurer, Benjamin Leonhardi, Bernie Huang, Beth Loyd, Beto De Paola, Bhargavi Paranjape, Bing Liu, Bo Wu, Boyu Ni, Braden Hancock, Bram Wasti, Brandon Spence, Brani Stojkovic, Brian Gamido, Britt Montalvo, Carl Parker, Carly Burton, Catalina Mejia, Ce Liu, Changan Wang, Changkyu Kim, Chao Zhou, Chester Hu, Ching-Hsiang Chu, Chris Cai, Chris Tindal, Christoph Feichtenhofer, Cynthia Gao, Damon Civin, Dana Beaty, Daniel Kreymer, Daniel Li, David Adkins, David Xu, Davide Testuggine, Delia David, Devi Parikh, Diana Liskovich, Didem Foss, Dingkan Wang, Duc Le, Dustin Holland, Edward Dowling, Eissa Jamil, Elaine Montgomery, Eleonora Presani, Emily Hahn, Emily Wood, Eric-Tuan Le, Erik Brinkman, Esteban Arcaute, Evan Dunbar, Evan Smothers, Fei Sun, Felix Kreuk, Feng Tian, Filippos Kokkinos, Firat Ozgenel, Francesco Caggioni, Frank Kanyet, Frank Seide, Gabriela Medina Florez, Gabriella Schwarz, Gada Badeer, Georgia Swee, Gil Halpern, Grant Herman, Grigory Sizov, Guangyi, Zhang, Guna Lakshminarayanan, Hakan Inan, Hamid Shojanazeri, Han Zou, Hannah Wang, Hanwen Zha, Haroun Habeeb, Harrison Rudolph, Helen Suk, Henry Aspegren, Hunter Goldman, Hongyuan Zhan, Ibrahim Damlaj, Igor Molybog, Igor Tufanov, Ilias Leontiadis, Irina-Elena Veliche, Itai Gat, Jake Weissman, James Geboski, James Kohli, Janice Lam, Japhet Asher, Jean-Baptiste Gaya, Jeff Marcus, Jeff Tang, Jennifer Chan, Jenny Zhen, Jeremy Reizenstein, Jeremy Teboul, Jessica Zhong, Jian Jin, Jingyi Yang, Joe Cummings, Jon Carvill, Jon Shepard, Jonathan McPhie, Jonathan Torres, Josh Ginsburg, Junjie Wang, Kai Wu, Kam Hou U, Karan Saxena, Kartikay Khandelwal, Katayoun Zand, Kathy Matosich, Kaushik Veeraraghavan, Kelly Michelena, Keqian Li, Kiran Jagadeesh, Kun Huang, Kunal Chawla, Kyle Huang, Lailin Chen, Lakshya Garg, Lavender A, Leandro Silva, Lee Bell, Lei Zhang, Liangpeng Guo, Licheng Yu, Liron Moshkovich, Luca Wehrstedt, Madian Khabsa, Manav Avalani, Manish Bhatt, Martynas Mankus, Matan Hasson, Matthew Lennie, Matthias Reso, Maxim Groshev, Maxim Naumov, Maya Lathi, Meghan Keneally, Miao Liu, Michael L. Seltzer, Michal Valko, Michelle Restrepo, Mihir Patel, Mik Vyatskov, Mikayel Samvelyan, Mike Clark, Mike Macey, Mike Wang, Miquel Jubert Hermoso, Mo Metanat, Mohammad Rastegari, Munish Bansal, Nandhini Santhanam, Natascha Parks, Natasha White, Navyata Bawa, Nayan Singhal, Nick Egebo, Nicolas Usunier, Nikhil Mehta, Nikolay Pavlovich Laptev, Ning Dong, Norman Cheng, Oleg Chernoguz, Olivia Hart, Omkar Salpekar, Ozlem Kalinli, Parkin Kent, Parth Parekh, Paul Saab, Pavan Balaji, Pedro Rittner, Philip Bontrager, Pierre Roux, Piotr Dollar, Polina Zvyagina, Prashant Ratanchandani, Pritish Yuvraj, Qian Liang, Rachad Alao, Rachel Rodriguez, Rafi Ayub, Raghotham Murthy, Raghu Nayani, Rahul Mitra, Rangaprabhu Parthasarathy, Raymond Li, Rebekkah Hogan, Robin Battey, Rocky Wang, Russ Howes, Ruty Rinott, Sachin Mehta, Sachin Siby, Sai Jayesh Bondu, Samyak Datta, Sara Chugh, Sara Hunt, Sargun Dhillon, Sasha Sidorov, Satadru Pan, Saurabh Mahajan, Saurabh Verma, Seiji Yamamoto, Sharadh Ramaswamy, Shaun Lindsay, Shaun Lindsay, Sheng Feng, Shenghao Lin, Shengxin Cindy Zha, Shishir Patil, Shiva Shankar, Shuqiang Zhang, Shuqiang Zhang, Sinong Wang, Sneha Agarwal, Soji Sajuyigbe, Soumith Chintala, Stephanie Max, Stephen Chen, Steve Kehoe, Steve Satterfield, Sudarshan Govindaprasad, Sumit Gupta, Summer Deng, Sungmin Cho, Sunny Virk, Suraj Subramanian, Sy Choudhury, Sydney Goldman, Tal Remez, Tamar Glaser, Tamara Best, Thilo

- Koehler, Thomas Robinson, Tianhe Li, Tianjun Zhang, Tim Matthews, Timothy Chou, Tzook Shaked, Varun Vontimitta, Victoria Ajayi, Victoria Montanez, Vijai Mohan, Vinay Satish Kumar, Vishal Mangla, Vlad Ionescu, Vlad Poenaru, Vlad Tiberiu Mihailescu, Vladimir Ivanov, Wei Li, Wenchen Wang, Wenwen Jiang, Wes Bouaziz, Will Constable, Xiaocheng Tang, Xiaojian Wu, Xiaolan Wang, Xilun Wu, Xinbo Gao, Yaniv Kleinman, Yanjun Chen, Ye Hu, Ye Jia, Ye Qi, Yenda Li, Yilin Zhang, Ying Zhang, Yossi Adi, Youngjin Nam, Yu, Wang, Yu Zhao, Yuchen Hao, Yundi Qian, Yunlu Li, Yuzi He, Zach Rait, Zachary DeVito, Zef Rosnbrick, Zhaoduo Wen, Zhenyu Yang, Zhiwei Zhao, and Zhiyu Ma. The llama 3 herd of models, 2024. URL <https://arxiv.org/abs/2407.21783>.
- Gabriel Ilharco, Marco Tulio Ribeiro, Mitchell Wortsman, Suchin Gururangan, Ludwig Schmidt, Hannaneh Hajishirzi, and Ali Farhadi. Editing models with task arithmetic, 2023. URL <https://arxiv.org/abs/2212.04089>.
- Albert Q. Jiang, Alexandre Sablayrolles, Arthur Mensch, Chris Bamford, Devendra Singh Chaplot, Diego de las Casas, Florian Bressand, Gianna Lengyel, Guillaume Lample, Lucile Saulnier, L  lio Renard Lavaud, Marie-Anne Lachaux, Pierre Stock, Teven Le Scao, Thibaut Lavril, Thomas Wang, Timoth  e Lacroix, and William El Sayed. Mistral 7b, 2023. URL <https://arxiv.org/abs/2310.06825>.
- J. Kennedy and R. Eberhart. Particle swarm optimization. In *Proceedings of ICNN'95 - International Conference on Neural Networks*, volume 4, pp. 1942–1948 vol.4, 1995. doi: 10.1109/ICNN.1995.488968.
- Weishi Li, Yong Peng, Miao Zhang, Liang Ding, Han Hu, and Li Shen. Deep model fusion: A survey. *arXiv preprint arXiv:2309.15698*, 2023a.
- Xuechen Li, Tianyi Zhang, Yann Dubois, Rohan Taori, Ishaan Gulrajani, Carlos Guestrin, Percy Liang, and Tatsunori B. Hashimoto. AlpacaEval: An automatic evaluator of instruction-following models. https://github.com/tatsu-lab/alpaca_eval, 5 2023b.
- Jinliang Lu, Ziliang Pang, Min Xiao, Yaochen Zhu, Rui Xia, and Jiajun Zhang. Merge, ensemble, and cooperate! a survey on collaborative strategies in the era of large language models. *arXiv preprint arXiv:2407.06089*, 2024.
- Michael S Matena and Colin A Raffel. Merging models with fisher-weighted averaging. *Advances in Neural Information Processing Systems*, 35:17703–17716, 2022.
- Long Ouyang, Jeffrey Wu, Xu Jiang, Diogo Almeida, Carroll Wainwright, Pamela Mishkin, Chong Zhang, Sandhini Agarwal, Katarina Slama, Alex Ray, et al. Training language models to follow instructions with human feedback. *Advances in neural information processing systems*, 35: 27730–27744, 2022.
- Gabriel Perin, Xuxi Chen, Shusen Liu, Bhavya Kailkhura, Zhangyang Wang, and Brian Gallagher. Rankmean: Module-level importance score for merging fine-tuned llm models. In *Findings of the Association for Computational Linguistics: ACL 2024*, pp. 1776–1782, 2024.
- Rafael Rafailov, Archit Sharma, Eric Mitchell, Christopher D Manning, Stefano Ermon, and Chelsea Finn. Direct preference optimization: Your language model is secretly a reward model. *Advances in Neural Information Processing Systems*, 36, 2024.
- Anke Tang, Li Shen, Yong Luo, Han Hu, Bo Du, and Dacheng Tao. Fusionbench: A comprehensive benchmark of deep model fusion. *arXiv preprint arXiv:2406.03280*, 2024.
- Hugo Touvron, Louis Martin, Kevin Stone, Peter Albert, Amjad Almahairi, Yasmine Babaei, Nikolay Bashlykov, Soumya Batra, Prajjwal Bhargava, Shruti Bhosale, Dan Bikel, Lukas Blecher, Cristian Canton-Ferrer, Moya Chen, Guillem Cucurull, David Esiobu, Jude Fernandes, Jeremy Fu, Wenyin Fu, Brian Fuller, Cynthia Gao, Vedanuj Goswami, Naman Goyal, Anthony Hartshorn, Saghar Hosseini, Rui Hou, Hakan Inan, Marcin Kardas, Viktor Kerkez, Madian Khabsa, Isabel Kloumann, Artem Korenev, Punit Singh Koura, Marie-Anne Lachaux, Thibaut Lavril, Jenya Lee, Diana Liskovich, Yinghai Lu, Yuning Mao, Xavier Martinet, Todor Mihaylov, Pushkar Mishra, Igor Molybog, Yixin Nie, Andrew Poulton, Jeremy Reizenstein, Rishi Rungta, Kalyan

Saladi, Alan Schelten, Ruan Silva, Eric Michael Smith, Ranjan Subramanian, Xiaoqing Ellen Tan, Binh Tang, Ross Taylor, Adina Williams, Jian Xiang Kuan, Puxin Xu, Zheng Yan, Iliyan Zarov, Yuchen Zhang, Angela Fan, Melanie Kambadur, Sharan Narang, Aurélien Rodriguez, Robert Stojnic, Sergey Edunov, and Thomas Scialom. Llama 2: Open foundation and fine-tuned chat models. *CoRR*, abs/2307.09288, 2023. doi: 10.48550/ARXIV.2307.09288. URL <https://doi.org/10.48550/arXiv.2307.09288>.

Alex Wang, Amanpreet Singh, Julian Michael, Felix Hill, Omer Levy, and Samuel Bowman. GLUE: A multi-task benchmark and analysis platform for natural language understanding. In Tal Linzen, Grzegorz Chrupała, and Afra Alishahi (eds.), *Proceedings of the 2018 EMNLP Workshop Black-boxNLP: Analyzing and Interpreting Neural Networks for NLP*, pp. 353–355, Brussels, Belgium, November 2018. Association for Computational Linguistics. doi: 10.18653/v1/W18-5446. URL <https://aclanthology.org/W18-5446/>.

Johannes Welbl, Nelson F Liu, and Matt Gardner. Crowdsourcing multiple choice science questions. *arXiv preprint arXiv:1707.06209*, 2017.

Prateek Yadav, Derek Tam, Leshem Choshen, Colin A Raffel, and Mohit Bansal. Ties-merging: Resolving interference when merging models. In A. Oh, T. Naumann, A. Globerson, K. Saenko, M. Hardt, and S. Levine (eds.), *Advances in Neural Information Processing Systems*, volume 36, pp. 7093–7115. Curran Associates, Inc., 2023. URL https://proceedings.neurips.cc/paper_files/paper/2023/file/1644c9af28ab7916874f6fd6228a9bcf-Paper-Conference.pdf.

Enneng Yang, Zhenyi Wang, Li Shen, Shiwei Liu, Guibing Guo, Xingwei Wang, and Dacheng Tao. Adamerging: Adaptive model merging for multi-task learning. *arXiv preprint arXiv:2310.02575*, 2023.

Le Yu, Bowen Yu, Haiyang Yu, Fei Huang, and Yongbin Li. Language models are super mario: Absorbing abilities from homologous models as a free lunch. In *Forty-first International Conference on Machine Learning*, 2024a. URL <https://openreview.net/forum?id=fq0NaiU8Ex>.

Qingchen Yu, Zifan Zheng, Shichao Song, Zhiyu Li, Feiyu Xiong, Bo Tang, and Ding Chen. xfinder: Robust and pinpoint answer extraction for large language models. *arXiv preprint arXiv:2405.11874*, 2024b.

A TRAINING DETAILS FOR EXPERTS BASED ON LLAMA-3-8B AND MISTRAL-7B-V0.3

In this section, we describe the training processes used to develop four domain-specific experts based on Llama-3-8B and Mistral-7B-v0.3. All training was conducted on 4 RTX 3090 GPUs. The training hyperparameters include a gradient accumulation step size of 32, a per-device training batch size of 1, and a learning rate of 5×10^{-6} . The datasets used for training, the number of epochs, and the corresponding expert models are outlined below. Our training was conducted using the Hugging Face Transformers framework.

Instruction-following expert We fine-tuned Llama-3-8B and Mistral-7B-v0.3 on the Infinity-Instruct⁴ dataset for 1 epoch to create the instruction-following expert. This dataset provides high-quality instruction-response pairs, enabling the model to excel in general instruction-following tasks.

Mathematical reasoning expert To develop the mathematical reasoning expert, we fine-tuned Llama-3-8B and Mistral-7B-v0.3 on the MathInstruct⁵ dataset for 1 epoch. This dataset focuses on math-related problems and solutions, allowing the model to specialize in solving mathematical reasoning tasks.

⁴<https://huggingface.co/datasets/BAAI/Infinity-Instruct>

⁵<https://huggingface.co/datasets/TIGER-Lab/MathInstruct>

Table 5: The statistics of datasets used in our experiments. The label in parentheses indicates which split the current split is derived from in the source data.

Dataset	Training Split	Optimization Split	Testing Split
Infinity-Instruct	659,808(train)	-	-
AlpacaEval	-	73(eval)	732(eval)
MathInstruct	262,039(train)	-	-
GSM8K	-	131(train)	1,319(test)
CodeAlpacaPython	8,477(train)	-	-
MBPP	-	50(train)	500(test)
SciQ	11,679(train)	100(validation)	1,000(test)

Code-generating expert The code-generating expert was obtained by fine-tuning Llama-3-8B and Mistral-7B-v0.3 on the CodeAlpacaPython⁶ dataset for 5 epochs. This dataset contains Python-specific programming problems and solutions, which help the model specialize in code generation.

Science exam question-answering expert . For science-related question answering, we fine-tuned Llama-3-8B and Mistral-7B-v0.3 on the SciQ⁷ dataset for 5 epochs. The dataset consists of multiple-choice science questions, enabling the model to perform well in science exam scenarios.

B DATASET STATISTICS

The data statistics for training, optimization, and testing are listed in Table 5.

⁶<https://huggingface.co/datasets/Abzu/CodeAlpacaPython>

⁷<https://huggingface.co/datasets/allenai/sciq>