# CAPTURING SUBSTRUCTURE INTERACTIONS BY IN-VARIANT INFORMATION BOTTLENECK THEORY FOR ROBUST PROPERTY PREDICTION

**Anonymous authors**Paper under double-blind review

000

001

002

004

006

008 009 010

011 012

013

014

016

017

018

019

021

024

025

026

027

028

029

031

032 033 034

035

037

040

041

042

043

044

046 047

048

051

052

#### **ABSTRACT**

Molecular interactions are a common phenomenon in physical chemistry, often resulting in unexpected biochemical properties harmful to humans, such as drug-drug interactions. Machine learning has shown great potential for predicting these interactions rapidly and accurately. However, the complexity of molecular structures and the diversity of interactions often reduce prediction accuracy and hinder generalizability. Identifying core invariant substructures (i.e., rationales) has become essential to improving the model's interpretability and generalization. Despite significant progress, existing models frequently overlook the pairwise molecular interaction, leading to insufficient capture of interaction dynamics. To address these limitations, we propose I2Mole (Interaction-aware Invariant Molecular learning), a novel framework for generalizable property prediction. I2Mole meticulously models atomic interactions, such as hydrogen bonds and Van der Waals forces, by first establishing indiscriminate connections between intermolecular atoms, which are then refined using an improved graph information bottleneck theory tailored for merged graphs. To further enhance model generalization, we construct an environment codebook by environment subgraph of the merged graph. This approach not only could provide noise source for optimizing mutual information but also preserve the integrity of chemical semantic information. By comprehensively leveraging the information inherent in the merged graph, our model accurately captures core substructures and significantly enhances generalization capabilities. Extensive experimental validation demonstrates I2Mole's efficacy and generalizability. The implementation code is available at https://anonymous.4open/r/I2Mol-C616.

#### 1 Introduction

The molecular interaction process can generate additional physical or chemical properties when two or more molecules combined Varghese & Mushrif (2019); D'Souza et al. (2011); Low et al. (2022). This phenomenon is common in the fields of physics, chemistry, and medicine *etc.*, such as changes in Gibbs free energy during dissolution (*i.e.*, solute-solvent pair) Chung et al. (2022); Fang et al. (2024); Xia et al. (2023) and synergistic or adverse reactions between drugs (*i.e.*, drug-drug pair) Lee et al. (2023b); Klemperer (1992). Due to the complexity of molecular structures and the diversity of molecular interactions, conventional modeling approaches are limited and susceptible to noise, undermining prediction accuracy. Meanwhile, lacks generalizability and reliability severely limits their applicability. Based on this, mining the invariant core substructures of molecules (*i.e.*, rationale) has gradually become a consensus to enhance both interpretability and generalization like the CGIB Lee et al. (2023a) and MoleOOD Yang et al. (2022b).

Although current methods have attracted widespread attention in predicting the properties of molecular pairs, two inherent shortcomings remain underexplored. The first is **Insufficiency in molecular interaction modeling.** Existing methods demonstrate proficiency in elucidating essential structural characteristics for individual molecular models. However, when molecular interactions occur, pivotal substructures may exhibit considerable variation. Taking Pseudoephedrine (PSE) and Methamphetamine (Meth) as an example (Figure 1 (a)). Both are common drugs used to induce cardiac stimulation, arising from their distinct functional groups affecting neurons. The hydroxyl moiety in PSE participates in regulating neurotransmitter release and reuptake, while the amphetamine moiety

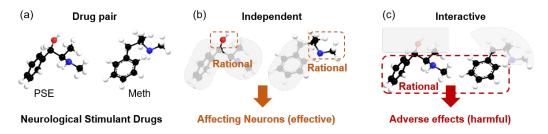


Figure 1: An Example of molecular interactions. (a) Both Pseudoephedrine (PSE) and Methamphetamine (Meth) are stimulant drugs; (b) each drug is influenced by distinct core substructures to stimulate neurons; (c) harmful effects on human health occor by other substructure interaction.

in Meth does this as illustrated in Figure 1 (b). However, upon their concomitant usage, the interaction between Meth's benzene ring and PSE's amphetamine moiety excessively enhances the stimulatory effects on cardiovascular systems, thereby leading to the occurrence of adverse effects and harm to the human body, as shown in Figure 1 (c). Therefore, comprehensive modeling of intermolecular interactions is crucial and necessary for a profound understanding of molecular interactions.

Some current models have noticed the aforementioned shortcomings Behler (2015; 2016), however, they still **lack of consideration for model robustness.** Given the diverse and complex nature of molecular species in real-world scenarios, the data used for training and testing may inevitably be sampled from different distributions, thus presenting challenges related to OOD Paul et al. (2021); Petrova (2013); Yang et al. (2022b). While introducing integrated noise injection techniques to simulate diverse environmental distributions holds promise for enhancing model generalization and capturing core rationals, several drawbacks exist. Specifically, 1) The simulation of noise data may not accurately reflect authentic environmental vectors in chemical space. 2) Indiscriminate application of noise injection can distort semantic information and hinder model convergence. And random environmental vectors may struggle to adequately represent the broad distribution of molecular interactions. 3) When the injected noise variance is minimal, this may converge to a constant, defeating the purpose of its introduction. These limitations compromise the modeling process and may result in suboptimal result.

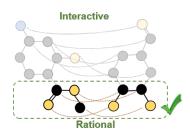


Figure 2: Diagram illustrating molecular interaction modeling to capture rationals. Molecular pairs will be constructed into a merged graph by connecting atoms pairwise (dashed lines). Please note that to avoid excessive complexity, some unimportant relation edges will be removed (unconnected). Best view in color.

In sight of this, we introduce an Interaction-aware Invariant Molecular learning framework, termed I2Mole, for generalizable property prediction. Spontaneous molecular interaction phenomena, such as van der Waals forces Chi et al. (2010), hydrogen bonding interactions Chen et al. (2021), etc. are more likely to occur in specific molecular structures (e.g., -OH, =O, N), resulting in stronger forces. We carefully design dynamic weighted relationship edges to differentially learn the interactions between atoms. Conversely, for atomic pairwise interactions that are rarely occur, we employ iterative truncation to restrict their message passing processes, reducing interference with the overall learning of the merged graph while moderately reducing graph complexity, as presented in Figure 2. Given the vast and largely unknown nature of the potential chemical space, collecting all possible environments is impractical. Therefore, we introduce the concept of vector quantization (VQ) van den Oord et al. (2017); Razavi et al. (2019) for molecular interactions

to create a merged graphic environment codebook. This codebook clusters the potential environments of molecules in the training set into a specified number of categories. The learned environmental distribution also serves as noise for optimizing mutual information Duncan (1970); Yu et al. (2022b). Therefore, our I2Mole with explict molecule interactions and improved environment codebook, could effectively achieve robust property prediction on various DDI datasets.

### 2 Preliminaries

In this section, we begin with a formal description of the problem formulation. Next, we delve into the concepts of the Graph Information Bottleneck and invariant learning.

#### 2.1 PROBLEM FORMULATION

A molecule can be depicted as a graph  $\mathcal{G}$  whose nodes  $\mathcal{V}$  denote the atoms and edges  $\mathcal{E}$  act as the bonds Wen et al. (2021).  $\mathcal{U}$  is the global feature vector which is extracted from each molecule (Appendix C). Given a set of drug molecular graph pairs  $\mathcal{D} = \{(\mathcal{G}_a^1, \mathcal{G}_b^1), (\mathcal{G}_a^2, \mathcal{G}_b^2), \dots, (\mathcal{G}_a^n, \mathcal{G}_b^n)\}$  and their associated target values  $\mathbb{Y} = \{\mathbf{Y}^1, \mathbf{Y}^2, \dots, \mathbf{Y}^n\}$ , our objective is to train a model  $\mathcal{M}$  can classify the target values for arbitrary drug pairs in an end-to-end manner, i.e.,  $\mathbf{Y}^i = \mathcal{M}(\mathcal{G}_a^i, \mathcal{G}_b^i)$ .

#### 2.2 Graph Information Bottleneck (GIB)

According to the GIB principle Yu et al. (2020; 2022b); Miao et al. (2022), we could get:

$$\mathcal{G}_{\mathrm{IB}} = \underset{\mathcal{G}_{\mathrm{sub}} \in \mathcal{S}}{\operatorname{arg\,min}} - I(\mathbf{Y}; \mathcal{G}_{\mathrm{sub}}) + \beta I(\mathcal{G}; \mathcal{G}_{\mathrm{sub}}). \tag{1}$$

Intuitively, where S represents the set of  $\mathcal{G}_{\mathrm{sub}}$ , and  $\mathcal{G}_{\mathrm{IB}}$  is the core subgraph of  $\mathcal{G}$ , which discards information from the  $\mathcal{G}$  by minimizing the mutual information  $I(\mathcal{G}; \mathcal{G}_{\mathrm{sub}})$ , while preserving target-relevant information by maximizing the mutual information  $I(\mathbf{Y}; \mathcal{G}_{\mathrm{sub}})$ .

### 2.3 INVATIANT LEARNING

Given the distribution shift between training and testing data, recent studies Rojas-Carulla et al. (2018a); Arjovsky et al. (2019); Wu et al. (2022a) propose the existence of a potential environment variable **env** to express this problem:

$$\min_{f} \max_{\mathcal{G}_{env} \in \mathbf{E}} \mathbb{E}_{(\mathcal{G}, Y) \sim p(\mathcal{G}, \mathbf{Y} | \mathbf{env} = \mathcal{G}_{env})} [R(f(\mathcal{G}), \mathbf{Y}) \mid \mathcal{G}_{env}], \tag{2}$$

where **E** denotes the support of environments,  $f(\cdot)$  represents the prediction model, and  $R(\cdot, \cdot)$  is a risk function. The label **Y** is independent of the environment  $\mathcal{G}_{env}$ , given the subgraph  $\mathcal{G}_{sub}$ :

$$\mathbf{Y} \perp \mathcal{G}_{\text{env}} \mid \mathcal{G}_{\text{sub}},$$
 (3)

where  $\perp$  denotes probabilistic independence. These principles collectively protect predictions from external influences, ensuring that the rationale comprehensively captures all discriminative features. This is for a single molecule, and we would extend it to molecular pairs.

# 3 METHODOLOGY

In this section, we detail our proposed method. In Section 3.1, we define the merged graph and the intermolecular message passing mechanism. Section 3.2 explains the details of subgraph extraction by GIB theory. In Section 3.3, we describe how injecting environmental embeddings into the rationals to enhance model generalization. Section 3.4 presents the total loss function of 12Mole.

#### 3.1 MERGED MOLECULAR REPRESENTATION

**Molecule Merging.** The merged graph  $\widetilde{\mathcal{G}}$  could be generated by establishing a weighted relational edge between two molecules which connects each atom pairwise.

$$\widetilde{\mathcal{G}} = \{\mathcal{R}, \mathcal{E}, \mathcal{V}, \mathcal{U}\}.$$
 (4)

The set of relation edges are  $\mathcal{R}$ :

$$\mathcal{R} = \{ (r_{ij}, v_{ai}, v_{bj}) \}_{k=1}^{N^a \times N^b}, \tag{5}$$

Figure 3: Overview of our model. Initially, molecular pairs construct a merged graph to facilitate the message passing process. Subsequently, subgraphs are extracted based on the GIB, and the environmental components are recorded in a codebook. During the invariant learning process, the rational part concatenates different environment embeddings to achieve invariant representations.

where  $ai \in \{1, 2, 3, \dots, N^a\}$ ,  $bj \in \{1, 2, 3, \dots, N^b\}$ .  $N^a$  and  $N^b$  is the total number of atoms in drug molecular graph  $\mathcal{G}_a$ ,  $\mathcal{G}_b$ .  $r_{ij}$  represents the relation edge. And k is the index of  $\mathcal{R}$ .

**Intra-molecular message passing.** Generally, in this merged molecular graph  $\mathcal{G}$ , the message passing process is firstly executed intramolecule. In this process,  $e_{ij}$  is updated to  $e'_{ij}$  by aggregating the initially bond features, as well as the two atomic features,  $v_i$  and  $v_j$ , and the global features u. In addition, the atomic feature vector  $v_i$  is updated into  $v'_i$  and u is updated into  $u'_i$ :

$$e'_{ij} = e_{ij} + \text{LeakyReLU}[FC(v_i + v_j) + [FC(e_{ij}) + [FC(u)]], \tag{6}$$

$$\hat{e}_{ij} = \frac{\sigma(e'_{ij})}{\sum_{j' \in N_i} \sigma(e'_{ij'}) + \epsilon}, \quad v'_i = v_i + \text{LeakyReLU}[FC(v_i + \sum_{j \in N_i} \hat{e}_{ij} \odot FC(v_j)) + FC(u)], \quad (7)$$

$$u' = u + \text{LeakyReLU}[FC(\frac{1}{N^v} \sum_{i=1}^{N^v} v'_i + \frac{1}{N^e} \sum_{k=1}^{N^e} e'_k + u)], \quad (8)$$

$$u' = u + \text{LeakyReLU}[FC(\frac{1}{N^v} \sum_{i=1}^{N^v} v_i' + \frac{1}{N^e} \sum_{k=1}^{N^e} e_k' + u)],$$
 (8)

where FC is a fully connected layer.  $\odot$  denotes the Hadamard product.  $\sigma(\cdot)$  is the sigmoid activation function, and  $\epsilon$  is a fixed constant (0.0001) added for numerical stability.  $N^v$  and  $N^e$  are the number of atoms and bonds in the molecule, respectively.

Intermolecular message passing. We utilize GAT network Veličković et al. (2017) for intermolecular message passing to calculate the weight of relation edge  $r_{ij}$ .

$$r_{ij} = \text{LeakyReLU}(\text{FC}(\mathbf{W}v'_{ai}, \mathbf{W}v'_{bi})),$$
 (9)

where W is the learnable weight matrix. According to the calculated attention coefficients  $(r_{ij})$  for relation edge, we perform global sorting and retain the top $_{\bf x}$ % (hyperparameters):

$$r'_{ij} = \begin{cases} r_{ij} & \text{if } r_{ij} \ge X, \\ 0 & \text{otherwise.} \end{cases}$$
 (10)

Here, X represents the threshold corresponding to the top\_x\% ranking of  $r_{ij}$  values. The selected attention coefficients are then normalized across the entire graph to facilitate the intermolecular information-passing process. The atomic feature  $v'_{ai}$  for i is updated, also for  $v'_{bi}$ :

$$\alpha_{ij} = \frac{r'_{ij}}{\sum_{i,j} r'_{ij}}, \quad v''_{ai} = (1 - \sum_{j \in N_b} \alpha_{ij}) v'_{ai} + \sum_{j \in N_b} \alpha_{ij} v'_{bj}, \tag{11}$$

#### 3.2 CORE SUBSTRUCTURE EXTRACTION BASED ON GIB

To detect the core reaction structure in merged graph, we optimize the model with the objective function defined in equation 12 as follows:

$$\widetilde{\mathcal{G}}_{IB} = \underset{\widetilde{\mathcal{G}}_{\text{sub}} \in \widetilde{\mathcal{S}}}{\operatorname{arg min}} - I(\mathbf{Y}; \widetilde{\mathcal{G}}_{\text{sub}}) + \beta I(\mathcal{G}; \widetilde{\mathcal{G}}_{\text{sub}}), \tag{12}$$

where  $\widetilde{\mathcal{S}}$  represents the set of  $\widetilde{\mathcal{G}}_{\mathrm{sub}}$ . Each term indicates the prediction and compression terms respectively, which should be minimized during training, as outlined below.

#### 3.2.1 Extract target-oriented information

Minimizing  $-I(\mathbf{Y}; \widetilde{\mathcal{G}}_{\mathrm{IB}})$ , that is to calculate upper bound of  $-I(\mathbf{Y}; \widetilde{\mathcal{G}}_{\mathrm{IB}})$ . Given the merged graph  $\widetilde{\mathcal{G}}$ , its label information  $\mathbf{Y}$ , and the learned IB-graph  $\widetilde{\mathcal{G}}_{IB}$ , we have:

$$-I(\mathbf{Y}; \widetilde{\mathcal{G}}_{\mathrm{IB}}) \leq \mathbb{E}_{\mathbf{Y} \cdot \widetilde{\mathcal{G}}_{\mathrm{IB}}}[-\log p_{\theta}(\mathbf{Y}|\widetilde{\mathcal{G}}_{\mathrm{IB}})] := \mathcal{L}_{pre}, \tag{13}$$

where  $p_{\theta}(\mathbf{Y}|\widetilde{\mathcal{G}}_{\mathrm{IB}})$  is variational approximation of  $p(\mathbf{Y}|\widetilde{\mathcal{G}}_{\mathrm{IB}})$ . We model  $p_{\theta}(\mathbf{Y}|\widetilde{\mathcal{G}}_{\mathrm{IB}})$  as a predictor parametrized by  $\theta$ . Thus, we can minimize the upper bound of  $-I(\mathbf{Y};\widetilde{\mathcal{G}}_{\mathrm{IB}})$  by minimizing the model prediction loss  $\mathcal{L}_{\mathrm{pre}}(\mathbf{Y},\widetilde{\mathcal{G}}_{\mathrm{IB}})$  with cross entropy loss. More details are given in Appendix B.1 (Sufficiency assumption Yang et al. (2022b)).

# 3.2.2 **OPTIMIZE MINIMIZED** $\widetilde{G}$

Minimizing  $I(\widetilde{\mathcal{G}}; \widetilde{\mathcal{G}}_{\mathrm{IB}})$ , that is to calculate upper bound of  $I(\widetilde{\mathcal{G}}; \widetilde{\mathcal{G}}_{\mathrm{IB}})$ . Inspired by a recent approach on graph information bottleneck Yu et al. (2022b), we also minimizes  $I(\widetilde{\mathcal{G}}; \widetilde{\mathcal{G}}_{\mathrm{IB}})$  by injecting noise into node representations. Then we damp the information in  $\widetilde{\mathcal{G}}$  by injecting noises into node representations with a learned probability. Let  $\epsilon$  be the noise sampled from a parametric noise distribution. We assign each node a probability of being replaced by  $\epsilon$ . Specifically, for the i-th node, the k-th relation edge, we learn the probability  $p_i$  and  $p_k$  with a fully connected layer. Then, we add a Sigmoid function on the output of fully connected layer to ensure  $p_i, p_k \in [0, 1]$ :

$$p_i = \operatorname{Sigmoid}(\operatorname{FC}(h_i)), \quad p_k = \operatorname{Sigmoid}(\operatorname{FC}(r_k)).$$
 (14)

Next, if an k-th relation edge connected to i-th node, we adjust the probability  $p_i$  by adding  $\frac{p_k}{N}$ , where N depends on whether i-th node is in  $\mathcal{G}_a$  or  $\mathcal{G}_b$ :

$$p_i = \begin{cases} p_i + \frac{p_k}{N_b} & \text{if } i \in \mathcal{G}_a \text{ and } k\text{-th edge is connected to } i\text{-th node,} \\ p_i + \frac{p_k}{N_a} & \text{if } i \in \mathcal{G}_b \text{ and } k\text{-th edge is connected to } i\text{-th node.} \end{cases}$$
 (15)

We then replace the node representation  $h_i$  by  $\epsilon$  with probability  $p_i$ :

$$z_i = \lambda_i h_i + (1 - \lambda_i)\epsilon, \quad \mathbf{h}_i^r = (1 - \lambda_i)\mathbf{h}_i,$$
 (16)

where  $\lambda_i \sim \mathrm{Bernoulli}(p_i)$ ,  $\mathbf{h}_i^r$  is the irrelevant substructure node which would be used to constuct  $\widetilde{\mathcal{G}}_{\mathrm{env}}$ . The transmission probability  $p_i$  controls the information sent from  $h_i$  to  $z_i$ . If  $p_i = 1$ , then all the information in  $h_i$  are transfered to  $z_i$  without loss. On the contrary, when  $p_i = 0$ , then  $z_i$  contains no information from  $h_i$  but only noise. We hope  $p_i$  is learnable so that we can selectively preserve the information in  $\widetilde{\mathcal{G}}_{\mathrm{IB}}$ . However,  $\lambda_i$  is a discrete random variable and we can not directly calculate the gradient of  $p_i$ . Therefore, we employ the concrete relaxation Jang et al. (2016) for  $\lambda_i$ :

$$\lambda_i = \text{Sigmoid}(\frac{1}{t}\log\frac{p_i}{1 - p_i} + \log\frac{u}{1 - u}),\tag{17}$$

where t is the temperature parameter and  $u \sim \mathrm{Uniform}(0,1)$ . Another critical aspect of noise injection is the characterization of the injected noise. It is important that arbitrary noise can be

detrimental to the semantic integrity of the input graph, leading to predictions that deviate from the actual graph properties. Conversely, appropriately selected noise can provide a variational upper bound to the overall objective. Therefore, the minimized the upper bound of  $I(\widetilde{\mathcal{G}}_{\mathrm{IB}}; \widetilde{\mathcal{G}})$  as follows:

$$I(\widetilde{\mathcal{G}}_{\mathrm{IB}}; \widetilde{\mathcal{G}}) \leq \mathbb{E}_{\mathcal{G}} \left[ -\frac{1}{2} \log A_{\widetilde{\mathcal{G}}} + \frac{1}{2m_{\widetilde{\mathcal{G}}}} A_{\widetilde{\mathcal{G}}} + \frac{1}{2m_{\widetilde{\mathcal{G}}}} B_{\widetilde{\mathcal{G}}}^{2} \right] := \mathcal{L}_{\mathrm{MI}}(\widetilde{\mathcal{G}}_{\mathrm{IB}}, \widetilde{\mathcal{G}}), \tag{18}$$

where  $A_{\widetilde{\mathcal{G}}} = \sum_{j=1}^{m_{\widetilde{\mathcal{G}}}} (1 - \lambda_j)^2$  and  $B_{\widetilde{G}} = \frac{\sum_{j=1}^{m_{\widetilde{\mathcal{G}}}} \lambda_j (h_j - \mu_h)}{\sigma_h}$ . More details are given in Appendix B.2.

# 3.3 Environment Inference

Based on the tailored GIB theory, we can identify the decisive core substructure  $\widetilde{\mathcal{G}}_{IB}$ , as present in equation 12.  $\widetilde{\mathcal{G}}_{IB}$  only contains itself information do not guarantee good robustness. Therefore, we are based on the invariance learning theory to enhance the robustness of core substructure by incorporating various environments features captured across downstream tasks. This problem can be formally defined as follows:

$$\min_{f} \max_{\widetilde{\mathcal{G}}_{env} \in \mathbf{E}} \mathbb{E}_{(\widetilde{\mathcal{G}}, \mathbf{Y}) \sim q(\widetilde{\mathcal{G}}_{env})} [R(f(\widetilde{\mathcal{G}}), \mathbf{Y}) \mid \widetilde{\mathcal{G}}_{env}], \tag{19}$$

where  $\mathbf{E}$  denotes the support of environments. The irrelevant substructures  $\widetilde{\mathcal{G}}_{env}$  can be viewed as the environment, where each node embedding is  $\mathbf{h}_i^r$ .  $q(\widetilde{\mathcal{G}}_{env})$  is the distribution of data under environment  $\widetilde{\mathcal{G}}_{env}$  combined with various rationales,  $f(\cdot)$  is the prediction model and  $R(\cdot, \cdot)$  is the risk function such as cross-entropy loss. The above equation 19 aims to minimize the maximum errors under different environments thus providing the guarantee of capturing the invariance across environments, which has been well demonstrated in existing researches Wu et al. (2022c;b).

Directly solving the equation 19 is impractical as limited training data across the various environments in  $\mathbf{E}$ , while the model should be expected to perform well across all these environments. Here, we introduce the concept of vector quantization (VQ) van den Oord et al. (2017); Razavi et al. (2019) to create a trainable environment codebook  $W = \{env_1, env_2, \ldots, env_M\}$ , defining a latent embedding space  $env \in \mathbb{R}^{M \times F}$ . Here, M represents the number of discrete environments (i.e. env), and F denotes the dimension of each latent vector. Then, we use a nearest neighbor lookup in the shared embedding space  $\mathbf{E}$  to find the closest latent vector  $env_m$ , indexed by m.

Additionally, the set2set network Vinyals et al. (2015) is utilized to pool  $\widetilde{\mathcal{G}}_{\mathrm{IB}}$ ,  $\widetilde{\mathcal{G}}_{\mathrm{env}}$ ,  $\widetilde{\mathcal{G}}$ , resulting in the substructure representation vectors  $\widetilde{s}_{\mathrm{IB}}$ ,  $\widetilde{s}_{\mathrm{env}}$  and  $\widetilde{s}_{\mathcal{G}}$ . This process acts as a specific non-linearity that maps the latent vectors  $\widetilde{s}_{\mathrm{env}}$  to one of the M embedding vectors:

$$q\left(m\mid\widetilde{s}_{env}\right) = \begin{cases} 1 & \text{for } m = \arg\min_{j} \left\|\widetilde{s}_{env} - env_{j}\right\|_{2}, \\ 0 & \text{otherwise.} \end{cases}$$
 (20)

Aiming to update the codebook and encourage the output of the encoder to stay close to the chosen codebook embedding, we defined  $\mathcal{L}_{vq}$  as follow, where the  $sg[\cdot]$  denotes stop-gradient and  $\delta$  is a hyper-parameter set to 0.25 Xia et al. (2022):

$$\mathcal{L}_{vq} = \|\operatorname{sg}\left[\widetilde{s}_{\text{env}}\right] - env_m\|_2^2 + \delta \|\widetilde{s}_{\text{env}} - \operatorname{sg}[env_m]\|_2^2.$$
(21)

As  $\mathcal{L}_{vq}$  gradually converges, we obtain a stable codebook set W, which clusters the infinite possible environment space  $\mathbf{E}$  into a discretized set of M finite environments represented by W. Subsequently, we traverse all potential environment vectors (env) and assign rationals to different environments for achieving stable predictions. This ensures that the prediction results of the rationals are independent of the environments, thereby guaranteeing the independence between the rationals and the environment samples (Invariance assumption Yang et al. (2022b)).

Table 1: Performance of different methods in transudative setting. (Bold numbers are the best results, while the top-performing baseline is highlighted with a superscript cross).

		ZhangDDI		ChchMiner				DeepDDI	
	ACC (†)	AUROC (†)	<b>F1</b> (↑)	ACC (†)	AUROC (†)	<b>F1</b> (↑)	ACC (†)	AUROC (†)	F1 (†)
GoGNN	84.14(0.46)	92.35(0.48)	81.54(0.42)	91.17 <sub>(0.46)</sub>	96.64(0.40)	92.35(0.34)	93.54(0.35)	92.71(0.27)	89.83(0.41)
DeepDDI	83.35(0.49)		80.24(0.47)	90.34(0.44)	95.71(0.37)	91.83(0.28)	92.39(0.38)		91.32(0.39)
SSI-DDI	86.97(0.62)	$93.76_{(0.34)}$	82.99(0.30)	93.26(0.24)	97.81(0.22)	93.11(0.19)	94.27(0.25)	97.42(0.31)	95.41(0.19)
MHCADDI	77.86(0.50)	86.94(0.68)	83.67 <sub>(0.48)</sub>	84.26(0.64)	89.33(0.72)	83.21(0.53)	87.01(0.77)	97.64 <sub>(0.83)</sub>	88.54(0.55)
MDF-SA-DDI	86.89(0.15)	94.03(0.22)	83.67 <sub>(0.14)</sub>	94.63 <sub>(0.21)</sub> †	98.10(0.17)	94.17(0.16)	94.12(0.21)	88.84(0.26)	96.13(0.17)
DSN-DDI	87.65(0.13)	94.63(0.18)†	84.30(0.09)	94.25(0.11)	98.31(0.10)	95.34 <sub>(0.08)</sub>	95.74(0.18)	98.06(0.16)	96.71(0.11)
CGIB	87.32(0.71)	94.43(0.60)	84.53(0.45)	94.37(0.39)	98.38(0.31)†	95.44 <sub>(0.24)</sub>	95.76(0.72)†	98.08(0.64)†	96.53(0.53)
CMRL	87.78 <sub>(0.37)</sub> †	94.08(0.23)	84.78 <sub>(0.25)</sub> †	94.43(0.25)	98.37 <sub>(0.12)</sub>	95.62 <sub>(0.17)</sub> †	95.49(0.34)	98.03 <sub>(0.31)</sub>	96.82 <sub>(0.29)</sub>
Ours	88.64(0.24)	95.12 <sub>(0.12)</sub>	85.87 <sub>(0.20)</sub>	95.34(0.19)	98.84 <sub>(0.10)</sub>	96.21(0.25)	96.51(0.14)	99.04(0.22)	97.53(0.15)

$$\min_{f} \mathbb{E}_{env_i \in W} \mathbb{E}_{(\widetilde{s}_{\mathcal{G}}, \mathbf{Y}) \sim q(env_i)} \left[ R\left( f\left( \widetilde{s}_{\mathcal{G}} \right), \mathbf{Y} \right) \mid env_i \right]. \tag{22}$$

This formula can be obtained by minimizing the weighted sum of cross-entropy losses across different environments. Assuming a total of C classes, let  $\phi_i$  denote the probability that env belongs to  $env_i$ , and  $\Phi$  represents the classification head that maps the molecular representation to the category labels. the encoder  $f_{env}$  and the classification head  $\Phi$  together form the prediction model. Consequently, the loss can be expressed in the following form, where  $\mathbb{I}$  denotes the concatenation operation:

$$\mathcal{L}_{inv} = -\sum_{i=1}^{M} \phi_i \sum_{\widetilde{s}_{\mathcal{G}} \in \mathcal{D}_{train}} \sum_{c=1}^{C} \mathbf{Y}_{\widetilde{s}_{\mathcal{G}}} \log \Phi \left( f_{env}(\widetilde{s}_{\text{IB}} || env_i) \right).$$
 (23)

#### 3.4 Training Objective

Finally, we train the model with the following objective:

$$\mathcal{L}_{\text{total}} = \mathcal{L}_{\text{inv}} + \mathcal{L}_{\text{pre}} + \beta \mathcal{L}_{\text{MI}} + \gamma \mathcal{L}_{\text{vq}}$$
 (24)

Here,  $\mathcal{L}_{pre}$  and  $\mathcal{L}_{MI}$ , guided by the GIB.  $\mathcal{L}_{pre}$  is the cross-entropy loss for classification tasks.  $\mathcal{L}_{MI}$  represents the KL divergence between the core substructures and the non-core subgraph, encouraging substructure compression. And  $\mathcal{L}_{inv}$  aims to minimizing the disturbance loss across various environments.  $\beta$  and  $\gamma$  are trade-off parameters which governs the weight of  $\mathcal{L}_{MI}$  and  $\mathcal{L}_{vq}$ .

# 4 EXPERIMENT AND ANALYSE

We present experimental results to demonstrate the effectiveness of I2Mole. In this section, we conduct extensive experiments to answer the following questions:

- **RQ1:** Can I2Mole improve the prediction accuracy on various drug-drug pairs?
- **RQ2:** How effective is I2Mole in terms of generalization capabilities?
- **RQ3:** What does the environment codebook represent and learned in the model?

#### 4.1 Datasets and setups

**Datasets.** To evaluate the performance of our model, we conduct experiments based on three commonly used datasets in DDI event prediction task, including ZhangDDI Zhang et al. (2017), DeepDDI Ryu et al. (2018) and ChChMiner Zitnik et al.. More detailed description could be found in Appendix D.1.

**Baselines.** In our extensive assessment, our model is compared with eight advanced DDI event prediction methods, all leveraging molecular graphs as input features. The compared methods include GoGNN Wang et al. (2020a), MHCADDI Deac et al. (2019), DeepDDI Ryu et al. (2018), SSI-DDI

379

380 381 382

397

399 400

401

402

403

404

405 406

407 408

409

411

412

413

414

415

416

417

418

419

420

421

422

423 424

425 426

427

428

429

430

431

Table 2: Performance of different methods in inductive settings. (Bold numbers are the best results, while the top-performing baseline is highlighted with a superscript cross).

				Тур	e1					
		ZhangDDI			ChchMiner			DeepDDI		
	ACC (†)	AUROC (†)	<b>F1</b> (↑)	ACC (†)	AUROC (†)	<b>F1</b> (↑)	ACC (†)	AUROC (†)	<b>F1</b> (↑)	
GoGNN	61.51(1.87)	63.17(1.42)	45.53(1.28)	67.48(1.56)	69.52 <sub>(1.84)</sub>	69.22(1.33)	67.53(1.52)	71.34(1.24)	67.16(1.13)	
DeepDDI	60.84(1.34)	59.51(1.18)	$43.81_{(1.26)}$	66.19(1.08)	$68.51_{(1.53)}$	$67.67_{(1.29)}$	64.39(1.71)	$69.52_{(1.53)}$	68.31(1.45)	
SSI-DDI	62.38(1.53)	$69.56_{(1.21)}$	$47.59_{(1.17)}$	76.94(1.32)	$79.64_{(1.53)}$	$77.61_{(1.24)}$	69.77 <sub>(0.86)</sub>	$75.93_{(1.14)}$	72.23(0.77)	
MHCADDI	61.81 <sub>(1.27)</sub>	$67.52_{(0.97)}$	$44.51_{(1.38)}$	72.77 <sub>(0.76)</sub>	$70.92_{(1.08)}$	78.15 <sub>(0.97)</sub>	65.94(0.98)	72.18(0.87)	$70.37_{(1.24)}$	
MDF-SA-DDI	64.51(1.39)	$70.99_{(1.27)}$	51.53(1.15)	75.39(0.80)	80.47(0.68)	79.83(1.05)	71.13(0.77)	80.54(0.94)	71.61 <sub>(0.88)</sub>	
DSN-DDI	67.68(0.87)	72.49(1.02)	53.64(0.77)	78.94(0.72)	85.93 <sub>(0.65)</sub>	83.81(0.83)	73.35(0.62)	83.11(0.76)	$75.68_{(0.70)}$	
CGIB	68.34 <sub>(0.66)</sub>	$72.80_{(0.43)}$	57.29(0.58)†	79.75(0.73)	86.41(0.93)	85.13(0.43)	73.86(0.97)	$80.80_{(0.53)}$	78.47(0.47)†	
CMRL	68.38(1.12)†	74.59 <sub>(1.05)</sub> †	56.41(0.97)	80.54 <sub>(0.66)</sub> †	87.64 <sub>(0.54)</sub> †	86.55 <sub>(0.57)</sub> †	74.12 <sub>(0.55)</sub> †	84.96 <sub>(0.87)</sub> †	77.81 <sub>(0.74)</sub>	
Ours	<b>69.12</b> <sub>(0.23)</sub>	<b>75.14</b> <sub>(0.42)</sub>	<b>57.89</b> <sub>(1.55)</sub>	<b>81.59</b> <sub>(1.10)</sub>	<b>88.51</b> <sub>(0.31)</sub>	<b>87.43</b> <sub>(0.74)</sub>	<b>75.27</b> <sub>(0.0.64)</sub>	<b>85.62</b> <sub>(0.74)</sub>	<b>78.96</b> <sub>(0.37)</sub>	
				Тур	e2					
		ZhangDDI			ChchMiner		DeepDDI			
	ACC (†)	AUROC (†)	<b>F1</b> (↑)	ACC (†)	AUROC (†)	F1 (†)	ACC (†)	AUROC (†)	<b>F1</b> (↑)	
GoGNN	55.37(3.27)	54.37(2.47)	34.92(3.26)	64.27(4.31)	67.73(3.63)	72.19(4.30)	62.96(3.64)	63.91(3.61)	68.53(3.34)	
DeepDDI	58.62(2.03)	56.34(1.97)	25.19(4.34)	63.78(2.14)	66.71(2.67)	71.37(3.38)	61.68(4.18)	65.17(3.72)	66.74(4.16)	
SSI-DDI	57.24(2.38)	59.34(3.26)	37.16(3.84)	65.61(2.51)	68.39(1.94)	74.95(2.17)	65.53(3.53)	69.37(4.16)	62.18(3.94)	
MHCADDI	57.84(2.28)	56.47(2.77)	33.53(3.18)	59.24(5.39)	63.57 <sub>(4.67)</sub>	64.57(4.17)	60.17(3.67)	$62.89_{(3.42)}$	63.57 <sub>(5.17)</sub>	
MDF-SA-DDI	57.63(1.89)	55.97 <sub>(1.67)</sub>	33.94(2.78)	65.24(1.97)	68.54(2.04)	77.32 <sub>(1.89)</sub>	66.34(1.55)	70.81 <sub>(2.01)</sub>	70.95(1.71)	
DOM DDI	59 27	50 00	20.40	68 36	60.24	77.52	68 17.	72.71	71.06	

Nyamabo et al. (2021), CGIB Lee et al. (2023a), CMRL Lee et al. (2023c), MDF-SA-DDI Lin et al. (2022) and DSN-DDI Li et al. (2023). More detailed description could be found in Appendix D.2.

69.34(1.34)

69.82(1.39)†

 $69.62_{(1.67)}$ 

**70.02**<sub>(0.85)</sub>

77.52(1.21)

78.46(2.03)†

75.76(1.28)

**79.67**<sub>(0.35)</sub>

68.17(1.28)

 $68.26_{(1.39)}$ 

68.29(1.78)

**69.92**<sub>(0.11)</sub>

68.36(1.54)

68.78(1.84)†

67.09(1.54)

**69.23**<sub>(0.17)</sub>

71.96(1.64)

75.75(1.75)†

73.91(2.14)

**75.83**<sub>(0.43)</sub>

72.71(1.37)

68.78(1.67)

73.38(1.96)

74.27(0.62)

**Metric.** Three metrics are employed to evaluate the model performance: accuracy (ACC), area under the receiver operating characteristic (AUROC), harmonic mean of precision and recall (F1). All experiments are repeated eight times with the same dataset split and average result is presented.

### 4.2 Model Performance (RQ1)

 $58.37_{(1.31)}^{\cdot}$ 

58.39(2.04)

60.78(1.37)

**61.35**<sub>(1.01)</sub>

DSN-DDI

CGIB

**CMRI** 

Ours

 $58.88_{(1.12)}^{\cdot}$ 

57.24(1.97)

60.02(2.03)

**62.02**<sub>(1.09)</sub>

39.49(2.32)

28.83(4.53)

38.73(3.04)

**39.95**<sub>(1.56)</sub>

Similar to previous studiesDeac et al. (2019); Nyamabo et al. (2021); Ryu et al. (2018), we first performed the transuductive setting that is the common method evaluation scheme, where the entire dataset is randomly split and aims to predict the undiscovered DDI events among known drugs. In this scenario, we split the dataset into training (60%), validation (20%), and test (20%) parts. Based on the results presented in Table 1, three key observations can be delineated:

**Obs.1: I2Mole exhibits the excited predictive performance in transductive setting.** The results of our model and eight baseline models are documented in Table 1. We observe that our model demonstrates the optimal predictive performance across three different scales of datasets. Regarding the ACC evaluation metric, it outperforms other models on the ZhangDDI and DeepDDI datasets, while its performance on the ChCh-Miner dataset is comparable to MDF-SA-DDI.

Obs.2: I2Mole shows more pronounced performance improvements on the large-scale DeepDDI dataset. The model's performance across different datasets may be influenced by variations in dataset characteristics, where larger datasets imply a greater diversity of drugs and more complex DDI relationships. Compared to the second-best model, I2Mole has improved 1.03% on the large-scale DeepDDI dataset, while only 0.96% on the medium and small-scale datasets in AUROC index.

#### 4.3 GENERALIZATION TEST (RQ2)

In this section, we evaluated I2Mole's generalizability by inductive settings and domain shifting test. Type 1 aims to predict potential interaction properties between known and unseen drugs, while Type 2 aims to predict potential interaction properties between unseen and unseen drugs as in Table 2.

**Obs.3: I2Mole demonstrates excellent generalization ability on inductive settings.** We assessed the generalization capability on I2Mole to unseen drugs, which holds significant practical and real-world implications. This process was implemented by partitioning drugs, and the testing results, in

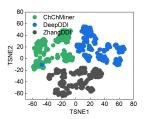


Figure 4: TSNE map for three DDI datasets (3000 drug pairs are respectively selected.)

Table 3: Performance on domain generalization experiments.

		ChchMiner			DeepDDI	
	ACC (†)	AUROC (†)	<b>F1</b> (↑)	ACC (↑)	AUROC (†)	<b>F1</b> (↑)
GoGNN	47.81(0.35)	60.25(0.21)	62.53(0.32)	51.20(0.26)	66.24(0.34)	62.35(0.35)
DeepDDI	48.27(0.24)	61.21(0.32)	60.25(0.27)	50.34(0.14)	65.21(0.27)	61.83(0.25)
SSI-DDI	51.25(0.21)	60.47(0.31)	62.34(0.52)	53.26(0.45)	67.24(0.42)	63.11(0.34)
MHCADDI	52.45(0.12)	62.43(0.31)	63.27(0.38)	54.26(0.24)	67.53(0.22)	63.21(0.34)
MDF-SA-DDI	33.54(0.12)	65.34(0.32)	63.55(0.54)	54.63(0.34)	68.50(0.25)	64.17(0.21)
DSN-DDI	52.24(0.24)	62.45(0.28)	64.20(0.09)	54.86(0.21)	68.25(0.24)	65.34(0.24)
CGIB	55.21(0.21)	67.54(0.46)	64.53(0.44)	55.37(0.29)	68.48(0.45)†	65.44(0.32)
CMRL	55.76(0.21)†	68.14 <sub>(0.23)</sub> †	64.82(0.15) †	56.43(0.55)†	68.45(0.21)	65.62(0.45)†
Ours	<b>59.25</b> <sub>(0.15)</sub>	<b>69.22</b> <sub>(0.31)</sub>	65.25 <sub>(0.26)</sub>	<b>58.12</b> <sub>(0.09)</sub>	<b>68.72</b> <sub>(0.42)</sub>	<b>65.76</b> <sub>(0.23)</sub>

Table 4: The scaffold and size splitting experiments result.

Model	Zhan	gDDI	Chch	miner	Deep	DDI
	Scaffold (†)	Size (↑)	Scaffold (†)	Size (↑)	Scaffold (†)	<b>Size</b> (↑)
SSI-DDI	72.34 <sub>(3.73)</sub>	70.15(2.47)	72.34 <sub>(1.22)</sub>	76.89(1.82)	78.27 <sub>(2.12)</sub>	84.75 <sub>(4.32)</sub>
MHCADDI	75.67 <sub>(1.34)</sub>	$76.28_{(1.53)}$	82.71 <sub>(1.25)</sub>	$82.66_{(2.17)}$	84.57 <sub>(3.24)</sub>	82.74(2.13)
MDF-SA-DDI	79.34(1.37)	$79.46_{(0.48)}$	85.47 <sub>(0.75)</sub>	84.23(0.63)	87.38(0.32)	86.58(0.37)
DSN-DDI	82.16(1.21)	80.38(1.23)	87.47 <sub>(2.14)</sub>	87.92 <sub>(1.32)</sub>	88.99(2.33)	86.53(1.65)
CGIB	83.32(1.26)	$80.79_{(0.83)}$	89.47(1.10)	88.43(1.39)	89.56(2.22)	89.44(2.02)
CMRL	82.25(0.85)	81.32(0.77)	89.78(1.24)	88.49(1.91)	90.76(2.31)	$90.77_{(1.22)}$
Ours	83.45(0.92)	<b>82.55</b> (1.12)	90.32(1.71)	<b>89.95</b> (1.06)	<b>91.76</b> (2.63)	<b>91.89</b> (1.42)

comparison with baseline models, are documented in Table 2. Evidently, when predicting with new drugs, the performance of all models experiences varying degrees of decline. But I2Mole exhibiting excellent predictive performance has the minimized sensitivity to unseen drug pairs.

**Obs.4: I2Mole shows robust performance on domain generalization experiments.** To investigate the impact of domain shifting on generalization, we transfer a model trained on a smaller dataset to a larger dataset. Specifically, I2Mole trained on the ZhangDDI dataset will test on two other datasets. Notably, ZhangDDI and DEEPDDI exhibit entirely distinct distributions of molecular species, as depicted in Figure 4. I2Mole outperforms other baseline models consistently across all conditions, underscoring its superior generalization capability, as recoded in Table 3.

**Obs.5:** I2Mole demonstrates superior performance in scaffold and size splitting experiments. As presented in Table 4, our proposed model consistently surpasses state-of-the-art methods, achieving the highest accuracy in both scaffold and size splits. These results underscore the advantages of our approach, enabling the model to effectively extract rationales with impressive generalization capabilities, performing robustly across different test scenarios.

#### 4.4 EXPLORING THE IMPACT AND EFFECTS OF ENVIRONMENT CODEBOOK (RQ3)

In this section, we provide an intuitive understanding through t-SNE analysis of environment vectors and molecular embeddings, as presented in Figure 5. Visualization analyses are shown in Appendix I.

Obs.6: Different environment embeddings in environment codebook has clear boundaries on visualization result. The 10 distinct environment embeddings exhibit clear distinctions (Figure 5 (a)) ensure that the model adequately learns different types of environmental variables and thereby enhancing its robustness. Moreover, different molecular substructure embeddings are tightly centered around the corresponding environment embedding, respectively. This suggests that updating the codebook vector is essentially equivalent to performing clustering on the molecular embeddings, with the environment embeddings serving as the clustering centers as shown in Figure 5 (a).

**Obs.7:** Environmental coding is consistent with real chemical scenarios. We analyze the atom distribution from two distinct perspectives. First, we present the distribution of atom types associated with each environmental embedding in Figure 5 (b). Our observations reveal that the diverse environmental embeddings effectively capture the local contexts of various molecular subgraphs.

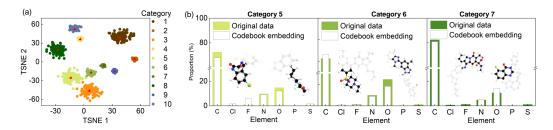


Figure 5: Environmental codebook vectors analysis. (a) TSNE dimensionality reduction plot of drug molecular pairs and the 10-class environment codebook vectors. Different colors represent the chosen codebook vectors, with red dots within clusters indicating the codebook vectors location. (b) Elemental composition of molecular pairs in clusters 5, 6, and 7 (colored) compared to the elemental composition represented by the codebook vectors (blank), along with an example pair of molecules.

Table 5: Ablation experiment. Intermolecular interaction denotes as  $\Delta$ .

ZhangDDI AUROC ACC F1 74.52(0.11) 83.61<sub>(0.13)</sub> 74.01(0.24) w/o VQ 87.21(0.27) 80.21(0.33) w/o  $\Delta$ 84.51(0.22) 87.21(0.24) 84.72(0.08) 81.07(0.43) 85.07(0.20) 88.02(0.24) 94.73(0.12)

Table 6: Sensitivity analysis for  $\beta$  and  $\gamma$  (ACC indicator).

			ZhangDDI		
	0	1E-5	1E-4	1E-3	0.1
β	85.71 <sub>(0.02)</sub>	85.84 <sub>(0.08)</sub>	87.73 <sub>(0.18)</sub>	86.83 <sub>(0.03)</sub>	56.46(0.03)
	2E-5	1E-4	2E-4	5E-4	1E-3
$\gamma$	88.01 <sub>(0.08)</sub>	88.02 <sub>(0.04)</sub>	88.01 <sub>(0.02)</sub>	88.02 <sub>(0.01)</sub>	88.03 <sub>(0.01)</sub>

Consequently, we conclude that the distribution of atom types in our codebook closely mirrors that of the real world, thereby fulfilling our initial expectation that the noise adheres to chemical logic.

#### 5 ABLATION STUDY AND SENSITIVITY ANALYSIS

**Obs.8: Ablation study.** To further investigate the role of each component, we conducted a series of ablation studies. As shown in Table 5, removing the GIB module reduced the model's ability to capture core substructures, limiting its performance. Similarly, the removal of intermolecular interaction disrupted accurate chemical modeling, degrading the model's capabilities. Notably, eliminating VQ module led to substantial performance drops, highlighting the importance of codebook and vector quantization operation (more detailed result could be fould in Appendix F). The computational complexity and data scalability analysis are present in Appendix H.

Obs.9: Sensitivity analysis. We investigate the sensitivity of  $\beta$  and  $\gamma$ , which govern the trade-off between prediction and compression, and the codebook updating process, respectively. These parameters correspond to the weights of  $\mathcal{L}_{MI}$  in  $\mathcal{L}_{vq}$  in equation 24. Overall, the model demonstrates robustness to variations in  $\beta$  and  $\gamma$ , but performance degrades significantly when  $\beta$  is sharply increased. More detailed sensitivity analysis results, including the number of samples and environmental vectors, among other factors, are presented in Appendix F.

#### 6 Conclusion and Future outlook

In this work, we introduce I2Mole, a novel framework for precise DDI prediction. I2Mole constructs a merged drug pair graph to capture complex molecular interactions, specifically addressing the imbalance between training and testing data distributions commonly encountered in real-world drug scenarios. By leveraging an enhanced information bottleneck approach, I2Mole extracts invariant and rational subgraphs, ensuring consistency across diverse environments. Furthermore, we devise an environment codebook based on the molecular environments in the training set. This captures environmental information and integrates it into data from diverse distributions, thereby significantly enhancing the model's generalization capability. Extensive experiments validate I2Mole's superior accuracy and generalizability, facilitating the rapid identification of potential DDIs and reducing the risks associated with drug misuse. Limitations are discussed in Appendix I.

# REFERENCES

- Alexander A Alemi, Ian Fischer, Joshua V Dillon, and Kevin Murphy. Deep variational information bottleneck. *arXiv preprint arXiv:1612.00410*, 2016.
  - Martín Arjovsky, Léon Bottou, Ishaan Gulrajani, and David Lopez-Paz. Invariant risk minimization. *CoRR*, abs/1907.02893, 2019. URL http://arxiv.org/abs/1907.02893.
    - Jörg Behler. Constructing high-dimensional neural network potentials: a tutorial review. *International Journal of Quantum Chemistry*, 115(16):1032–1050, 2015. ISSN 0020-7608.
    - Jörg Behler. Perspective: Machine learning potentials for atomistic simulations. *The Journal of chemical physics*, 145(17):170901, 2016. ISSN 0021-9606.
    - Shiyu Chang, Yang Zhang, Mo Yu, and Tommi S. Jaakkola. Invariant rationalization. In *Proceedings of the 37th International Conference on Machine Learning, ICML 2020, 13-18 July 2020, Virtual Event*, volume 119 of *Proceedings of Machine Learning Research*, pp. 1448–1458. PMLR, 2020. URL http://proceedings.mlr.press/v119/chang20c.html.
    - Dong Chen, Kaifu Gao, Duc Duy Nguyen, Xin Chen, Yi Jiang, Guo-Wei Wei, and Feng Pan. Algebraic graph-assisted bidirectional transformers for molecular property prediction. *Nature communications*, 12(1):3521, 2021.
    - Zhenxing Chi, Rutao Liu, Bingjun Yang, and Hao Zhang. Toxic interaction mechanism between oxytetracycline and bovine hemoglobin. *Journal of hazardous materials*, 180(1-3):741–747, 2010.
    - Y. Chung, F. H. Vermeire, H. Y. Wu, P. J. Walker, M. H. Abraham, and W. H. Green. Group contribution and machine learning approaches to predict abraham solute parameters, solvation free energy, and solvation enthalpy. *Journal of Chemical Information and Modeling*, 62(3): 433–446, 2022. ISSN 1549-9596. doi: 10.1021/acs.jcim.1c01103. URL <GotoISI>://WOS: 000745910500001.
    - Andreea Deac, Yu-Hsiang Huang, Petar Veličković, Pietro Liò, and Jian Tang. Drug-drug adverse effect prediction with graph co-attention. *arXiv preprint arXiv:1905.00534*, 2019.
    - Yifan Deng, Xinran Xu, Yang Qiu, Jingbo Xia, Wen Zhang, and Shichao Liu. A multimodal deep learning framework for predicting drug–drug interaction events. *Bioinformatics*, 36(15):4316–4322, 2020.
    - Malcolm J. D'Souza, Anthony M. Darrington, and Dennis N. Kevill. A study of solvent effects in the solvolysis of propargyl chloroformate. *International Scholarly Research Notices*, 2011, 2011. ISSN 2090-5149.
    - Tyrone E Duncan. On the calculation of mutual information. *SIAM Journal on Applied Mathematics*, 19(1):215–220, 1970.
    - Junfeng Fang, Shuai Zhang, Chang Wu, Zhengyi Yang, Zhiyuan Liu, Sihang Li, Kun Wang, Wenjie Du, and Xiang Wang. Moltc: Towards molecular relational modeling in language models. *CoRR*, abs/2402.03781, 2024.
    - Reza Ferdousi, Reza Safdari, and Yadollah Omidi. Computational prediction of drug-drug interactions based on drugs functional similarities. *Journal of biomedical informatics*, 70:54–64, 2017.
    - Tianfan Fu, Cao Xiao, and Jimeng Sun. Core: Automatic molecule optimization using copy & refine strategy. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 34, pp. 638–645, 2020.
- Assaf Gottlieb, Gideon Y Stein, Yoram Oron, Eytan Ruppin, and Roded Sharan. Indi: a computational framework for inferring drug interactions and their associated recommendations. *Molecular systems biology*, 8(1):592, 2012.
  - Marc W Harrold and Robin M Zavod. Basic concepts in medicinal chemistry, 2014.
  - Yue He, Zheyan Shen, and Peng Cui. Towards non-iid image classification: A dataset and baselines. *Pattern Recognition*, 110:107383, 2021.

- Patricia Jaaks, Elizabeth A Coker, Daniel J Vis, Olivia Edwards, Emma F Carpenter, Simonetta M Leto, Lisa Dwane, Francesco Sassi, Howard Lightfoot, Syd Barthorpe, et al. Effective drug combinations in breast, colon and pancreatic cancer cells. *Nature*, 603(7899):166–173, 2022.
  - Eric Jang, Shixiang Gu, and Ben Poole. Categorical reparameterization with gumbel-softmax. *arXiv* preprint arXiv:1611.01144, 2016.
  - Jia Jia, Feng Zhu, Xiaohua Ma, Zhiwei W Cao, Yixue X Li, and Yu Zong Chen. Mechanisms of drug combinations: interaction and network perspectives. *Nature reviews Drug discovery*, 8(2): 111–128, 2009.
  - Diederik P. Kingma and Jimmy Ba. Adam: A method for stochastic optimization. *arXiv preprint* arXiv:1412.6980, 2014.
  - William Klemperer. Intermolecular interactions. *Science*, 257(5072):887–888, 1992.
  - Namkyeong Lee, Dongmin Hyun, Gyoung S. Na, Sungwon Kim, Junseok Lee, and Chanyoung Park. Conditional graph information bottleneck for molecular relational learning. In *ICML*, volume 202 of *Proceedings of Machine Learning Research*, pp. 18852–18871. PMLR, 2023a.
  - Namkyeong Lee, Dongmin Hyun, Gyoung S Na, Sungwon Kim, Junseok Lee, and Chanyoung Park. Conditional graph information bottleneck for molecular relational learning. *arXiv preprint arXiv:2305.01520*, 2023b.
  - Namkyeong Lee, Kanghoon Yoon, Gyoung S Na, Sein Kim, and Chanyoung Park. Shift-robust molecular relational learning with causal substructure. *arXiv preprint arXiv:2305.18451*, 2023c.
  - Zimeng Li, Shichao Zhu, Bin Shao, Xiangxiang Zeng, Tong Wang, and Tie-Yan Liu. Dsn-ddi: an accurate and generalized framework for drug–drug interaction prediction by dual-view representation learning. *Briefings in Bioinformatics*, 24(1):bbac597, 2023.
  - Shenggeng Lin, Yanjing Wang, Lingfeng Zhang, Yanyi Chu, Yatong Liu, Yitian Fang, Mingming Jiang, Qiankun Wang, Bowen Zhao, Yi Xiong, et al. Mdf-sa-ddi: predicting drug—drug interaction events based on multi-source drug fusion, multi-source feature fusion and transformer self-attention mechanism. *Briefings in Bioinformatics*, 23(1):bbab421, 2022.
  - K. Low, M. L. Coote, and E. I. Izgorodina. Explainable solvation free energy prediction combining graph neural networks with chemical intuition. *J Chem Inf Model*, 62(22):5457–5470, 2022. ISSN 1549-960X (Electronic) 1549-9596 (Linking). doi: 10.1021/acs.jcim.2c01013. URL https://www.ncbi.nlm.nih.gov/pubmed/36317829.
  - Dongsheng Luo, Wei Cheng, Dongkuan Xu, Wenchao Yu, Bo Zong, Haifeng Chen, and Xiang Zhang. Parameterized explainer for graph neural network. In Hugo Larochelle, Marc' Aurelio Ranzato, Raia Hadsell, Maria-Florina Balcan, and Hsuan-Tien Lin (eds.), Advances in Neural Information Processing Systems 33: Annual Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 2020, virtual, 2020. URL https://proceedings.neurips.cc/paper/2020/hash/e37b08dd3015330dcbb5d6663667b8b8-Abstract.html.
  - Fangrui Lv, Jian Liang, Shuang Li, Bin Zang, Chi Harold Liu, Ziteng Wang, and Di Liu. Causality inspired representation learning for domain generalization. In *Proceedings of the IEEE/CVF conference on computer vision and pattern recognition*, pp. 8046–8056, 2022.
  - Siqi Miao, Mia Liu, and Pan Li. Interpretable and generalizable graph learning via stochastic attention mechanism. In *International Conference on Machine Learning*, pp. 15524–15543. PMLR, 2022.
  - Arnold K Nyamabo, Hui Yu, and Jian-Yu Shi. Ssi-ddi: substructure-substructure interactions for drug-drug interaction prediction. *Briefings in Bioinformatics*, 22(6):bbab133, 2021.
  - Debleena Paul, Gaurav Sanap, Snehal Shenoy, Dnyaneshwar Kalyane, Kiran Kalia, and Rakesh K Tekade. Artificial intelligence in drug discovery and development. *Drug discovery today*, 26(1):80, 2021.

- Elina Petrova. Innovation in the pharmaceutical industry: The process of drug discovery and development. In *Innovation and Marketing in the Pharmaceutical Industry: Emerging Practices, Research, and Policies*, pp. 19–81. Springer, 2013.
  - Ali Razavi, Aäron van den Oord, and Oriol Vinyals. Generating diverse high-fidelity images with VQ-VAE-2. In *NeurIPS*, pp. 14837–14847, 2019.
  - Mateo Rojas-Carulla, Bernhard Schölkopf, Richard E. Turner, and Jonas Peters. Invariant models for causal transfer learning. *J. Mach. Learn. Res.*, 19:36:1–36:34, 2018a. URL http://jmlr.org/papers/v19/16-432.html.
  - Mateo Rojas-Carulla, Bernhard Schölkopf, Richard E. Turner, and Jonas Peters. Invariant models for causal transfer learning. *J. Mach. Learn. Res.*, 19:36:1–36:34, 2018b. URL http://jmlr.org/papers/v19/16-432.html.
  - Karen A Ryall and Aik Choon Tan. Systems biology approaches for advancing the discovery of effective drug combinations. *Journal of cheminformatics*, 7(1):1–15, 2015.
  - Jae Yong Ryu, Hyun Uk Kim, and Sang Yup Lee. Deep learning improves prediction of drug-drug and drug-food interactions. *Proceedings of the national academy of sciences*, 115(18):E4304–E4311, 2018.
  - Zheyan Shen, Peng Cui, Kun Kuang, Bo Li, and Peixuan Chen. Causally regularized learning with agnostic data selection bias. In *Proceedings of the 26th ACM international conference on Multimedia*, pp. 411–419, 2018.
  - Zheyan Shen, Peng Cui, Tong Zhang, and Kun Kunag. Stable learning via sample reweighting. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 34, pp. 5692–5699, 2020.
  - Zhenchao Tang, Guanxing Chen, Hualin Yang, Weihe Zhong, and Calvin Yu-Chian Chen. Dsilddi: A domain-invariant substructure interaction learning for generalizable drug–drug interaction prediction. *IEEE Transactions on Neural Networks and Learning Systems*, 2023.
  - Aäron van den Oord, Oriol Vinyals, and Koray Kavukcuoglu. Neural discrete representation learning. In *NIPS*, pp. 6306–6315, 2017.
  - Jithin John Varghese and Samir H Mushrif. Origins of complex solvent effects on chemical reactivity and computational tools to investigate them: a review. *Reaction Chemistry & Engineering*, 4(2): 165–206, 2019.
  - Petar Veličković, Guillem Cucurull, Arantxa Casanova, Adriana Romero, Pietro Lio, and Yoshua Bengio. Graph attention networks. *arXiv preprint arXiv:1710.10903*, 2017.
  - Oriol Vinyals, Samy Bengio, and Manjunath Kudlur. Order matters: Sequence to sequence for sets. *arXiv preprint arXiv:1511.06391*, 2015.
  - Hanchen Wang, Defu Lian, Ying Zhang, Lu Qin, and Xuemin Lin. Gognn: Graph of graphs neural network for predicting structured entity interactions. *arXiv* preprint arXiv:2005.05537, 2020a.
  - Tan Wang, Jianqiang Huang, Hanwang Zhang, and Qianru Sun. Visual commonsense r-cnn. In *Proceedings of the IEEE/CVF conference on computer vision and pattern recognition*, pp. 10760–10770, 2020b.
  - Mingjian Wen, Samuel M. Blau, Evan Walter Clark Spotte-Smith, Shyam Dwaraknath, and Kristin A. Persson. Bondnet: a graph neural network for the prediction of bond dissociation energies for charged molecules. *Chemical science*, 12(5):1858–1868, 2021.
  - Qitian Wu, Hengrui Zhang, Junchi Yan, and David Wipf. Handling distribution shifts on graphs: An invariance perspective. In *The Tenth International Conference on Learning Representations, ICLR 2022, Virtual Event, April 25-29, 2022.* OpenReview.net, 2022a. URL https://openreview.net/forum?id=FQOC5u-legI.
  - Qitian Wu, Hengrui Zhang, Junchi Yan, and David Wipf. Handling distribution shifts on graphs: An invariance perspective. *arXiv preprint arXiv:2202.02466*, 2022b.

- Ying-Xin Wu, Xiang Wang, An Zhang, Xiangnan He, and Tat-Seng Chua. Discovering invariant rationales for graph neural networks. *arXiv preprint arXiv:2201.12872*, 2022c.
  - Yingxin Wu, Xiang Wang, An Zhang, Xiangnan He, and Tat-Seng Chua. Discovering invariant rationales for graph neural networks. In *The Tenth International Conference on Learning Representations, ICLR 2022, Virtual Event, April 25-29, 2022.* OpenReview.net, 2022d. URL https://openreview.net/forum?id=hGXij5rfiHw.
  - Jun Xia, Chengshuai Zhao, Bozhen Hu, Zhangyang Gao, Cheng Tan, Yue Liu, Siyuan Li, and Stan Z Li. Mole-bert: Rethinking pre-training graph neural networks for molecules. In *The Eleventh International Conference on Learning Representations*, 2022.
  - Jun Xia, Yanqiao Zhu, Yuanqi Du, Yue Liu, and Stan Z Li. A systematic survey of chemical pre-trained models. *IJCAI*, 2023.
  - Nianzu Yang, Kaipeng Zeng, Qitian Wu, Xiaosong Jia, and Junchi Yan. Learning substructure invariance for out-of-distribution molecular representations. In Sanmi Koyejo, S. Mohamed, A. Agarwal, Danielle Belgrave, K. Cho, and A. Oh (eds.), Advances in Neural Information Processing Systems 35: Annual Conference on Neural Information Processing Systems 2022, NeurIPS 2022, New Orleans, LA, USA, November 28 December 9, 2022, 2022a. URL http://papers.nips.cc/paper\_files/paper/2022/hash/547108084f0c2af39b956f8eadb75d1b-Abstract-Conference.html.
  - Nianzu Yang, Kaipeng Zeng, Qitian Wu, Xiaosong Jia, and Junchi Yan. Learning substructure invariance for out-of-distribution molecular representations. *Advances in Neural Information Processing Systems*, 35:12964–12978, 2022b.
  - Zhitao Ying, Dylan Bourgeois, Jiaxuan You, Marinka Zitnik, and Jure Leskovec. Gnnexplainer: Generating explanations for graph neural networks. In Hanna M. Wallach, Hugo Larochelle, Alina Beygelzimer, Florence d'Alché-Buc, Emily B. Fox, and Roman Garnett (eds.), Advances in Neural Information Processing Systems 32: Annual Conference on Neural Information Processing Systems 2019, NeurIPS 2019, December 8-14, 2019, Vancouver, BC, Canada, pp. 9240–9251, 2019. URL https://proceedings.neurips.cc/paper/2019/hash/d80b7040b773199015de6d3b4293c8ff-Abstract.html.
  - Hui Yu, ShiYu Zhao, and JianYu Shi. Stnn-ddi: a substructure-aware tensor neural network to predict drug-drug interactions. *Briefings in Bioinformatics*, 23(4):bbac209, 2022a.
  - Junchi Yu, Tingyang Xu, Yu Rong, Yatao Bian, Junzhou Huang, and Ran He. Graph information bottleneck for subgraph recognition. *arXiv* preprint arXiv:2010.05563, 2020.
  - Junchi Yu, Jie Cao, and Ran He. Improving subgraph recognition with variational graph information bottleneck. In *IEEE/CVF Conference on Computer Vision and Pattern Recognition, CVPR 2022, New Orleans, LA, USA, June 18-24, 2022*, pp. 19374–19383. IEEE, 2022b. doi: 10. 1109/CVPR52688.2022.01879. URL https://doi.org/10.1109/CVPR52688.2022.01879.
  - Dong Zhang, Hanwang Zhang, Jinhui Tang, Xian-Sheng Hua, and Qianru Sun. Causal intervention for weakly-supervised semantic segmentation. *Advances in Neural Information Processing Systems*, 33:655–666, 2020.
  - Wen Zhang, Yanlin Chen, Feng Liu, Fei Luo, Gang Tian, and Xiaohong Li. Predicting potential drug-drug interactions by integrating chemical, biological, phenotypic and network data. *BMC bioinformatics*, 18:1–12, 2017.
  - Yi Zhong, Xueyu Chen, Yu Zhao, Xiaoming Chen, Tingfang Gao, and Zuquan Weng. Graphaugmented convolutional networks on drug-drug interactions prediction. *arXiv preprint arXiv:1912.03702*, 2019.
  - Marinka Zitnik, Rok Sosič, Sagar Maheshwari, and Jure Leskovec. Biosnap datasets: Stanford biomedical network dataset collection. 2018. *URL http://snap. stanford. edu/biodata*.

# A REALTED WORK

756

757 758

759 760

761

762

764

765

766

767

768

769

770

771

772

773

774

775

776

777

778

779

781

782

783

784

785

786 787 788

789 790

791

792

793

794

795

796

797

798

799

800

801

802

803

804

805

806

807

808

### A.1 DRUG-DRUG INTERACTION (DDI) PREDICTION

In recent years, computational approaches, particularly employing machine learning and deep learning methods, have emerged as indispensable tools for swiftly and economically predicting potential DDIs Ryall & Tan (2015); Jaaks et al. (2022). Initially, DDI prediction models predominantly focused on drug attribute information, assuming that similar drugs would exhibit common interactions Ryu et al. (2018); Deng et al. (2020). For instance, Gottlieb et al. (2012) utilized seven types of drug features to construct similarity vectors, forming a DDI prediction model based on logistic regression. Ferdousi et al. (2017) designed a deep neural network using drug molecular similarity vectors as descriptors for predicting potential DDIs. Recently, there has been a shift towards graph-based DDI prediction methodologies. Zhong et al. (2019) employed Graph Convolutional Neural Networks (GC-NNs) for message aggregation and an attention-based pooling method for DDI prediction. Given that the interaction between two drugs is influenced by their specific substructures and functions, recent efforts have focused on substructure extraction and interaction Harrold & Zavod (2014); Fu et al. (2020). For instance, Yu et al. (2022a) utilized functional group information of drug molecules as their substructures, while Nyamabo et al. Nyamabo et al. (2021) introduced the Substructure-Substructure Interaction for Drug-Drug Interaction (SSI-DDI) method, employing graph attention network (GAT) layers to extract substructure representations and co-attention layers to model interactions among substructures.

Despite the proficiency of existing methodologies in elucidating essential structural characteristics of individual molecular models Tang et al. (2023); Lee et al. (2023c), considerable variation in crucial substructures may occur during molecular interactions. Notably, while some pioneering work like DSIL-DDI Tang et al. (2023) and CMRL Lee et al. (2023c) has provided foundational insights, a noticeable gap remains in comprehensively modeling intermolecular interactions. CMRL Lee et al. (2023c) innovatively incorporates conditional graph information bottleneck theory to obtain rationales, simultaneously considering a second drug as a conditional factor during drug subgraph generation Lee et al. (2023b). However, prevailing methodologies encounter limitations in adequately capturing molecular interactions, particularly at the atomic level. Moreover, integrating a comprehensive profile of interacting molecules into subgraph generation poses significant challenges, including overwhelming complexity and the risk of incorporating redundant information Jia et al. (2009).

### A.2 OOD GENERALIZATION

The susceptibility of deep neural networks to significant performance degradation under distribution shifts has spurred extensive research on out-of-distribution (OOD) generalization. In response, the invariant rationalization theory has been introduced, aiming to achieve an invariant representation across diverse environments Chang et al. (2020); Rojas-Carulla et al. (2018b). This theory involves a rationalization module that discerns a crucial subset within the input graph, referred to as rationale, essential for prediction Ying et al. (2019); Luo et al. (2020). Subsequently, through invariant learning, these rationales are exposed to diverse environments, thereby fortifying the learned representation against environmental fluctuations and effectively bolstering the model's OOD capacity. 1) sufficiency: shows sufficient predictive power for the target, 2) invariance: contributes to equal (optimal) performance for the downstream tasks across all environments. Certain methods in computer vision Lv et al. (2022); Zhang et al. (2020); Wang et al. (2020b) achieve OOD generalization by learning domain-invariant representations. Additionally, methods such as Shen et al. (2018); He et al. (2021); Shen et al. (2020) aim to achieve OOD generalization by decorrelating correlated and irrelevant features, considering the statistical correlation between these features as a major factor for distribution shifts. In terms of molecular applications, DIR Wu et al. (2022d) introduces an inventive method to unveil invariant rationales by intervening in the training distribution, generating multiple interventional distributions, and identifying causal rationales consistent across varied distributions. Similarly, MoleOOD Yang et al. (2022a) suggests that leveraging causal data-generating invariance from substructures across environments, linked to specific properties, holds promise for enhancing OOD generalization. However, learning a domain-invariant representation for intermolecular interaction remains an open problem, and current discussions on OOD issues among molecules are limited.

# B PROOFS

# B.1 PROOF OF $\mathcal{L}_{pre}$

*Proof.* Regarding  $I(Y; \widetilde{\mathcal{G}})$ , we consider  $P_{\theta}\left(Y \mid \widetilde{\mathcal{G}}\right)$  as the variational estimation of  $P\left(Y \mid \widetilde{\mathcal{G}}\right)$ . Therefore, we can proceed with the following derivation:

$$I(Y; \widetilde{\mathcal{G}}) = \mathbb{E}_{(Y,\widetilde{\mathcal{G}})} \log \left[ \frac{P(Y | \widetilde{\mathcal{G}})}{P(Y)} \right]$$

$$= \mathbb{E}_{(Y,\widetilde{\mathcal{G}})} \log \left[ \frac{P_{\theta}(Y | \widetilde{\mathcal{G}})}{P(Y)} \right] +$$

$$\mathbb{E}_{\widetilde{\mathcal{G}}} \log \left[ KL(P(Y | \widetilde{\mathcal{G}}) || P_{\theta}(Y | \widetilde{\mathcal{G}})) \right].$$
(25)

Considering the non-negativity property of the Kullback-Leibler divergence, we can conclude that:

$$I(Y; \widetilde{\mathcal{G}}) \ge \mathbb{E}_{(Y,\widetilde{\mathcal{G}})} \log \left[ \frac{P_{\theta} \left( Y \mid \widetilde{\mathcal{G}} \right)}{P(Y)} \right]$$

$$= \mathbb{E}_{(Y,\widetilde{\mathcal{G}})} \log \left[ P_{\theta} \left( Y \mid \widetilde{\mathcal{G}} \right) \right] + H(Y).$$
(26)

As H(Y) remains constant across all data, it can be omitted, resulting in the final formulation of this term:

$$\mathcal{L}_{pre} := \mathbb{E}_{\left(Y,\widetilde{\mathcal{G}}\right)} \log \left[ P_{\theta} \left( Y \mid \widetilde{\mathcal{G}} \right) \right]. \tag{27}$$

#### B.2 Proof of $\mathcal{L}_{\text{MI}}$

*Proof.* We first use a readout function to obtain the graph representation  $z_{\widetilde{G}_{\mathrm{IB}}}$  of the perturbed graph  $\widetilde{G}_{\mathrm{IB}}$ . And we assume these is no information loss in this process. Therefore we have  $I\left(z_{\widetilde{G}_{\mathrm{IB}}};\widetilde{G}\right)\approx I\left(\widetilde{G}_{\mathrm{IB}};\widetilde{G}\right)$ . Now we bound  $I\left(z_{\widetilde{G}_{\mathrm{IB}}};\widetilde{G}\right)$  using variational approximation:

$$I\left(z_{\widetilde{G}_{IB}};\widetilde{G}\right) = \iint p\left(z_{\widetilde{G}_{IB}},\widetilde{G}\right) \log \frac{p\left(z_{\widetilde{G}_{IB}} \mid \widetilde{G}\right)}{p\left(z_{\widetilde{G}_{IB}}\right)} dz_{\widetilde{G}_{IB}} d\widetilde{G}$$

$$= \iint p\left(z_{\widetilde{G}_{IB}},\widetilde{G}\right) \log \frac{p\left(z_{\widetilde{G}_{IB}} \mid \widetilde{G}\right)}{q\left(z_{\widetilde{G}_{IB}}\right)} dz_{\widetilde{G}_{IB}} d\widetilde{G}$$

$$+ \iint p\left(z_{\widetilde{G}_{IB}},\widetilde{G}\right) \log \frac{q\left(z_{\widetilde{G}_{IB}}\right)}{p\left(z_{\widetilde{G}_{IB}}\right)} dz_{\widetilde{G}_{IB}} d\widetilde{G}$$

$$= \mathbb{E}_{p(\widetilde{G})} \left[ KL\left(p\left(z_{\widetilde{G}_{IB}} \mid \widetilde{G}\right) \mid\mid q\left(z_{\widetilde{G}_{IB}}\right)\right) \right]$$

$$- \mathbb{E}_{p\left(z_{\widetilde{G}_{IB}} \mid \widetilde{G}\right)} \left[ KL\left(p\left(z_{\widetilde{G}_{IB}} \mid\mid \widetilde{G}\right) \mid\mid q\left(z_{\widetilde{G}_{IB}}\right)\right) \right]$$

$$\leq \mathbb{E}_{p(\widetilde{G})} \left[ KL\left(p\left(z_{\widetilde{G}_{IB}} \mid\mid \widetilde{G}\right) \mid\mid q\left(z_{\widetilde{G}_{IB}}\right)\right) \right],$$

$$(28)$$

where  $q\left(z_{\widetilde{G}_{\mathrm{IB}}}\right)$  is the variational approximation to  $p\left(z_{\widetilde{G}_{\mathrm{IB}}}\right)$ . And the inequality is due to the fact that Kullback-Leibler divergence is non-negative. We assume that  $q\left(z_{\widetilde{G}_{\mathrm{IB}}}\right)$  is a noninformative

distribution following VIB Alemi et al. (2016). That is, we obtain  $q\left(z_{\widetilde{G}_{IB}}\right)$  by aggregating the node representations in a fully perturbed graph. The noise  $\epsilon_{\widetilde{G}} \sim \mathcal{N}\left(\mu_h, \sigma_h^2\right)$  is sampled from the Gaussian distribution.  $\mu_h$ ,  $\sigma_h^2$  are mean and variance of  $h_j$  in  $\tilde{G}$ .

When we choose sum pooling as the readout function, we have:

$$q\left(z_{\widetilde{G}_{1B}}\right) = \mathcal{N}\left(m_{\widetilde{G}}\mu_h, m_{\widetilde{G}}\sigma_h^2\right). \tag{29}$$

This is because the summation of Gassian distributions is also a Gaussian distribution. Then, for  $p\left(z_{\widetilde{G}_{\text{IR}}} \mid \widetilde{G}\right)$ , we have:

$$p\left(z_{\widetilde{G}_{\text{IB}}} \mid \widetilde{G}\right) = \mathcal{N}\left(m_{\widetilde{G}}\mu_h + \sum_{j=1}^{m_{\widetilde{G}}} \lambda_j h_j - \sum_{j=1}^{m_{\widetilde{G}}} \mu_h \lambda_j, \sum_{j=1}^{m_{\widetilde{G}}} \left(1 - \lambda_j\right)^2 \sigma_h^2\right).$$
(30)

Plug Equation 29 and Equation 30 into Equation 28 and we have:

$$\begin{split} &I\left(z_{\widetilde{G}_{\mathrm{IB}}};\widetilde{G}\right) \\ &\leq \int p(\widetilde{G}) \left(-\frac{1}{2}\log A_{\widetilde{G}} + \frac{1}{2m_{\widetilde{G}}}A_{\widetilde{G}} + \frac{1}{2m_{\widetilde{G}}}B_{\widetilde{G}}^{2}\right)\mathrm{d}\widetilde{G} \\ &+ \int \frac{1}{2}p(\widetilde{G})\log m_{\widetilde{G}}\,\mathrm{d}\widetilde{G} \\ &= \int p(\widetilde{G}) \left(-\frac{1}{2}\log A_{\widetilde{G}} + \frac{1}{2m_{\widetilde{G}}}A_{\widetilde{G}} + \frac{1}{2m_{\widetilde{G}}}B_{\widetilde{G}}^{2}\right)\mathrm{d}\widetilde{G} + C, \end{split} \tag{31}$$

where  $A_{\widetilde{G}} = \sum_{j=1}^{m_{\widetilde{G}}} (1 - \lambda_j)^2$  and  $B_{\widetilde{G}} = \frac{\sum_{j=1}^{m_{\widetilde{G}}} \lambda_j (h_j - \mu_h)}{\sigma_h} \cdot C$  is a constant and can be ignored in the optimization process.

# THE DETAILED FEATURES FOR ATOMS, BONDS AND MOLECULAR GLOBAL

A comprehensive overview of the selected atom, bond, and global input features is presented in Table 7. The initial step involves the conversion of the SMILES string of both solute and solvent into a graph structure using the RDKit package. This package is employed not only for graph creation but also for the computation of atom and bond features for each graph. The selection of features was restricted to those computable in RDKit to mitigate the computational expenses associated with performing quantum mechanics calculations for the entire dataset. In order to standardize the lengths of the bond, atom, and global feature vectors, a linear transformation is applied to each vector before the commencement of the message-passing steps.

#### D EXPERIMENTAL SETTINGS

In this section, we will provide a comprehensive overview of our experimental setup. Section D.1 will provide detailed information about all the datasets utilized in the experiments. Subsequently, Section D.2 will offer a basic introduction to the baseline methods incorporated in our study. Following that, Section D.3 will delineate the diverse hyperparameters employed in the network architecture of our model. Additionally, it will elucidate the search space for hyperparameters and present the optimal hyperparameters.

Table 7: Atoms (nodes), bonds (edges), and global features for molecular representation

Atomic features $(V)$	Bond features ( $\mathcal{E}$ )	Global features ( $\mathcal{U}$ )
Atomic species No. of bonds No. of bonded H atoms Ring status Valence Aromatic status Hybridization type	Bond type Conjugated status Ring size Stereo-chemistry -	Total No. of atoms Total No. of bonds Molecular weight
Acceptor status Donor status Partial charge	-  -  -	- - -

#### D.1 DATASETS

- ZhangDDI Zhang et al. (2017) is a small-scale dataset, including 548 drugs with 48,548 pairwise
  interaction data points, encompassing various types of similarity information for these drug pairs.
- ChChMiner Zitnik et al. a medium-scale dataset, comprises 1,514 drugs and 48,514 labeled DDIs, sourced from drug labels and scientific publications.
- **DeepDDI** Ryu et al. (2018) is a larger-scale dataset with 1,704 drugs and 192,284 labeled DDIs, along with comprehensive side-effect information.

These datasets provide detailed drug information, including SMILES string representations, forming a robust foundation for evaluating the proposed model.

#### D.2 BASELINES

In this chapter, we will provide a brief introduction to the baseline models mentioned in the experimental section. In our extensive assessment, our model is compared with eight advanced DDI event prediction methods, all leveraging molecular graphs as input features.

**GoGNN.** Wang et al. (2020a) It extracts features from structured entity graphs and entity interaction graphs in a hierarchical manner. We also propose a dual attention mechanism that enables the model to preserve the importance of neighbors in both levels of the graph.

**DeepDDI.** Ryu et al. (2018)It is based on the structural similarity profile between input drugs and others.

**MHCADDI.** Deac et al. (2019) A gated information transfer neural network is used to control the extraction of substructures and then interact based on an attention mechanism.

**SSI-DDI.** Nyamabo et al. (2021) it use a 4-layer GAT network to extract substructures at different levels, and finally complete the final prediction based on the co-attention mechanism.

**CGIB.** Lee et al. (2023b) Based on the graph conditional information bottleneck theory, conditional subgraphs are extracted to complete the interaction between molecules.

**CMRL.** Lee et al. (2023c) it detects the core substructure that is causally related to chemical reactions. we introduce a novel conditional intervention framework whose intervention is conditioned on the paired molecule. With the conditional intervention framework.

**MDF-SA-DDI.** Lin et al. (2022), achieving DDI prediction by incorporating multi-source drug fusion, multi-source feature fusion and transformer self-attention mechanism.

**DSN-DDI.** Li et al. (2023) it employs local and global representation learning modules iteratively and learns drug substructures from the single drug ('intra-view') and the drug pair ('inter-view') simultaneously.

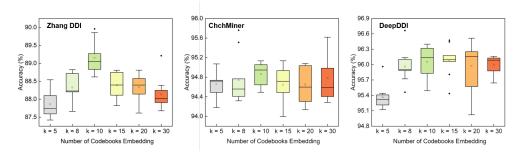


Figure 6: Test results of varying numbers of environmental vectors in the environment codebook in a transductive setting.

#### D.3 PARAMETER SETTING

**Model architecture.** For intramolecular message passing, we employ a 3-layer Gated Graph Convolutional Network (GatedConv). For intermolecular message passing, we utilize a 3-layer Graph Attention Network (GAT). As for the pooling layer, we opt for the set2set network. The detatiled hyperparameters are present in Table 8.

**Model Training.** The model is trained using the Adam optimizer Kingma & Ba (2014) with an initial learning rate of  $1 \times 10^{-4}$ , which is increased to 0.5, employing a batch size of 32. Binary cross-entropy loss (BCE) is utilized as the training loss function. Training is terminated if the validation error does not decrease for 150 epochs or if the maximum training limit of 300 epochs is reached. I2Mole is implemented in the PyTorch framework and executed on Tesla A100 40GB hardware.

	Network layer hyperparameters									
Gated	Conv		GAT	FC						
Num-layers Hidden-size Layers Activation	3, 4, 5 200, 400, 600, 800 3, 4, 5 LeakyReLU	Num-layers Hidden-size Layers Activation	3, 4, 5 200, 400, 600, 800 3, 4, 5 LeakyReLU	Num-layers Dropout Hidden-size	3, <b>4</b> , 5 0.5 300, <b>400</b> , 500, 600					
		Traini	ng hyperparameters							
Batch-size	32	Learning rate	0.0001, 0.0005, 0.01, 0.005	β	$  0, 1e^{-5}, 1e^{-4}, 1e^{-3}, 1e^{-1}$					
Environment codebook hyperparameters										
Num of environment	Num of environment $  5, 8, 10, 15, 20, 30    \gamma    2e^{-5}, 1e^{-4}, 2e^{-4}, 5e^{-4}, 1e^{-3}   $									

Table 8: Hyperparameter specifications.

#### E RESULTS SIGNIFICANCE ANALYSIS

In the transductive setting, which is a conventional testing method where the dataset is randomly divided into training, validation, and test sets, we repeated the experiment 8 times and calculated the mean, variance, and p-value of the ACC, as shown in the Table 9, compared to the second-best model, I2Mole improved by 1.03% on the large-scale DeepDDI dataset, with an average improvement of approximately 0.05. The p-values are less than 0.05, proving that the improvements of our model are statistically significant. Therefore, although this is a limited improvement, the results are substantial and significant.

In the inductive setting, which is a commonly used generalization testing method, a molecule (type 1) or a molecule pair (type 2) is removed in the test set to verify the model's generalization ability. Notably, in the generalization tests, I2Mole achieved an average improvement of 1.31% in type 1 scenarios and 1.33% in type 2 scenarios. This demonstrates I2Mole's ability to generalize to unseen molecules.

In domain generalization experiments, which is a challenging testing method, we trained and tested on datasets from different domains to verify I2Mole's generalization ability. Clearly, I2Mole achieved the best generalization results, with an average improvement of 4.6% (Acc index), significantly outperforming the improvements in transductive and inductive settings.

Table 9: Significant difference analysis.

	Mo	odel Performan	ice
	ZhangDDI	ChchMiner	DeepDDI
Second-best model	87.78(0.37)	94.63 <sub>(0.21)</sub>	95.76 <sub>(0.72)</sub>
Our model	88.64 <sub>(0.24)</sub>	95.34 <sub>(0.19)</sub>	96.51 <sub>(0.14)</sub>
P-value	1.84E-08	1.27E-03	1.53E-02

#### F SENSITIVITY ANALYSIS

We conduct an in-depth investigation into the effect of varying the number of environment embeddings on our model's performance, as depicted in Figure 6. The results demonstrate that altering the number of environment embeddings has a negligible impact on test performance across three different-sized test datasets, underscoring the robustness of our model. The optimal performance is achieved when the number of codebook vectors is set to 10, which we have adopted for our final model configuration.

Table 10: Sensitivity analysis for retained relational edges ratio.

		ZhangDDI	
	ACC	AUROC	F1
Top_s = 5%	88.52 <sub>(0.08)</sub>	95.22 <sub>(0.02)</sub>	85.75 <sub>(0.06)</sub>
$Top\_s = 10\%$	88.69(0.25)	95.31(0.03)	85.82(0.20)
$Top_s = 20\%$	88.81 <sub>(0.01)</sub>	$95.03_{(0.07)}$	85.87 <sub>(0.07)</sub>
$Top\_s = 30\%$	88.54 <sub>(0.12)</sub>	$95.69_{(0.12)}$	$85.53_{(0.13)}$
$Top\_s = 50\%$	88.34(0.14)	95.39(0.10)	85.42 <sub>(0.11)</sub>

Furthermore, we investigated the impact of varying the proportion of retained relational edges during inter-molecular message passing on the model's performance, as illustrated in Table 10. The results indicate that gradually increasing the proportion of retained relational edges enhances the model's performance. However, beyond a certain threshold, further increments lead to a noticeable decline in performance. Consequently, we selected 20% as the optimal parameter for the proportion of retained relational edges.

A crucial parameter in this context is the number of environmental samples, denoted as  $\theta$ . Increasing the number of sampled environments expands the range of simulated molecular interactions under various conditions, though it also introduces additional training overhead. To identify the optimal value of  $\theta$ , we systematically evaluated the impact of different sampling quantities, ranging from 2 to 6, within the framework of an environment codebook size of  $\mathbf{k}=10$ , as shown in Table 11. Based on the results, we have determined the optimal value of  $\theta$  to be 4.

Table 11: Sensitivity analysis for the sampling numbers of environmental embedding.

		ZhangDDI			ChchMiner			DeepDDI	
	ACC (†)	AUROC $(\uparrow)$	<b>F1</b> (↑)	$\mathbf{ACC}\ (\uparrow)$	AUROC $(\uparrow)$	<b>F1</b> (↑)	<b>ACC</b> (↑)	AUROC $(\uparrow)$	<b>F1</b> (↑)
$\theta = 2$	88.12(0.11)	94.79(0.14)	85.03(0.06)	94.67 <sub>(0.14)</sub>	98.61(0.21)	95.83 <sub>(0.11)</sub>	96.48(0.11)	97.11(0.10)	98.75(0.06)
$\theta = 3$	88.17 <sub>(0.15)</sub>	$94.74_{(0.10)}$	85.07 <sub>(0.20)</sub>	94.43(0.14)	98.68(0.07)	95.71(0.08)	96.23(0.10)	96.93(0.18)	$98.80_{(0.10)}$
$\theta = 4$	88.27 <sub>(0.13)</sub>	$94.86_{(0.12)}$		94.68(0.09)	98.85(0.22)	95.86(0.24)	96.25(0.23)	96.97(0.24)	$98.79_{(0.15)}$
$\theta = 5$	88.29(0.13)		85.41 <sub>(0.12)</sub>	94.38(0.19)		95.61(0.10)		96.89(0.12)	98.82(0.08)
$\theta = 6$	88.24(0.14)			94.57(0.16)		$95.78_{(0.08)}$		$97.00_{(0.13)}$	$98.73_{(0.11)}$

# G VQ MODULE ANALYSIS

To further illustrate the role of the VQ module, we introduced extra two variants for comparison: (1) RD Noise Variant: In this version, noise in the environment codebook is entirely random, mimicking the effects of random noise injection. (2) Instance-Dependent (ID) Noise Variant: Here, we sampled new environments from the environment codebook and added them as small perturbations to the

instance-dependent environment. The Gaussian distribution of this noise is determined by the mean and variance of subgraph node vectors, emphasizing instance-dependent noisy perturbations.

Table 12: Performance comparison across different DDI datasets.

	Zhan	gDDI	Chch	Miner	DeepDDI		
Method	<b>Acc</b> (↑)	AUROC (†)	<b>Acc</b> (↑)	AUROC (†)	<b>Acc</b> (↑)	AUROC (†)	
RD noise	87.21 (0.11)	93.76 (0.13)	93.47 (0.08)	97.52 (0.07)	92.39 (0.38)	97.01 (0.39)	
ID noise	88.02 (0.06)	94.47 (0.08)	94.27 (0.12)	98.54 (0.06)	94.56 (0.10)	97.42 (0.31)	
Ours	88.64 (0.24)	95.12 (0.12)	95.34 (0.19)	98.84 (0.10)	96.51 (0.14)	99.04 (0.22)	

Our experimental results demonstrate the superiority of the VQ module and the proposed optimization strategy, particularly in improving the model's robustness and ability to generalize across diverse chemical environments.

# H COMPUTATIONAL COMPLEXITY AND DATA SCALABILITY ANALYSIS

We have included the time and space complexity results for our model and various baseline models, along with a comparison of model parameters in Table 13 and Table 15. This table clearly showcases the results of various model parameters, time and computational complexity. Compared to other baseline models, I2Mole exhibits a significantly larger number of total parameters, leading to substantially higher time consumption and computational complexity than the other baselines.

As the amount of training data increases and the test data decreases, the model's performance exhibits a notable improvement. It is particularly worth mentioning that the model shows significant gains during the initial stages, but further increasing the training data yields only marginal improvements.

Further, we evaluated the model performance under different training data sizes and model parameter conditions in Table 14. We control the model parameters by adjusting the number of message-passing layers, dimensions of embeddings and feedforward NN.

Alongside increasing the model's complexity, there is a clear rise in computational time, accompanied by performance improvements. This could be attributed to the more intricate models being able to capture deeper inter-molecular relationships, thereby enhancing performance. However, when the model's parameters are further increased, its performance starts to degrade. This decline is likely due to overfitting, as the model becomes overly complex, leading to difficulties in convergence during training.

Table 13: Computational complexity analysis on I2Mole.

ZhangDDI	-	-	-	-	-	-	-	-	-
Model Parameter (M)	23.4	26.8	29.5	31.7	35.4	38.4	40.3	44.5	49
Time Consumption (h)	7.4	8.3	9.5	10.4	12.17	13.23	15.6	18.4	22.3
Performance (ACC)	83.61	85.94	87.43	88.27	88.64	88.64	88.35	87.91	86.87

Table 14: Data scalability analysis on I2Mole.

ZhangDDI	-	-	-	-	-	-	-	-	-
Training Data Ratio (%)	10	20	30	40	50	60	70	80	90
Test Data Ratio (%)	45	40	35	30	25	20	15	10	5
Performance (ACC)	53.27	65.27	72.34	80.34	88.27	88.64	89.01	91.34	92.25

#### I LIMITATION ANALYSIS

I2Mole, based on the drug pair merged graph, achieves the extraction of rational subgraphs in molecular interactions and combines the trained environment codebook, significantly enhancing

Table 15: Comparison of ZhangDDI, ChchMiner, and DeepDDI across different models

Model	Metric	ZhangDDI	ChchMiner	DeepDDI
CGIB	ACC	87.69	94.68	95.76
	Time (h)	1.5	0.59	3.73
	Memory (G)	5.1	3.9	7.4
	Total parameters (M)	11	11	11
CRML	ACC	87.78	94.43	95.99
	Time (h)	1.3	0.47	3.24
	Memory (G)	4	3.4	6.1
	Total parameters (M)	10	10	10
SSI-DDI	ACC	86.97	93.26	94.27
	Time (h)	1.77	0.65	4.08
	Memory (G)	3.1	2.7	4.4
	Total parameters (M)	13	13	13
DSN-DDI	ACC	87.65	94.23	93.37
	Time (h)	1.2	0.43	3.08
	Memory (G)	2.9	3.6	4.1
	Total parameters (M)	0.19	0.19	0.19
I2Mole	ACC	88.64	95.34	96.51
	Time (h)	13.23	4.9	33.07
	Memory (G)	17	13.3	11.7
	Total parameters (M)	35.4	35.4	35.4

generalization capabilities in domain generalization experiments. However, considering the rapid advancements in the pharmaceutical field and real-world prescription scenarios, we foresee improvements to the current framework in three key aspects:

- We aim to acquire more comprehensive data on drug interaction processes and analyses between molecules, addressing the limitations of current research. In practice, patients often have multiple comorbidities requiring the concurrent use of various drug categories. Thus, the interaction system of multiple drugs remains a critical research area.
- Constructing relationship edges in pairs, as previously done, is an effective strategy for predicting properties between molecular pairs. However, this approach significantly increases the graph's complexity, especially for large, intricate molecules, due to the substantial rise in degrees of freedom, leading to higher computational resource and time consumption.
- An equally important aspect is that drugs often function only under specific conditions such as temperature and pH levels. Therefore, we anticipate future work to comprehensively consider the impact of external environments on the functionality of drug molecule pairs, thereby refining the model's capabilities.

# J VISUALIZATION ANALYSIS

Acetaminophen, a widely used medication for pain relief (analgesic) and fever reduction (antipyretic), is frequently found in over-the-counter formulations. However, unexpected drug-drug interactions (DDIs) between acetaminophen and compounds such as Fenoterol, Fosphenytoin, and Ethanol can pose significant threats to patient safety, as depicted in Figure (a). Specifically, the aromatic ring of acetaminophen, along with its surrounding functional groups, is capable of interacting with target molecules, particularly at the central carbon atom bonded to the carboxyl group. This key interaction has been effectively captured by the I2Mole model. Additionally, the core subgraphs extracted by I2Mole exhibit good connectivity and consistent distribution across regions, although the associated weights may vary.

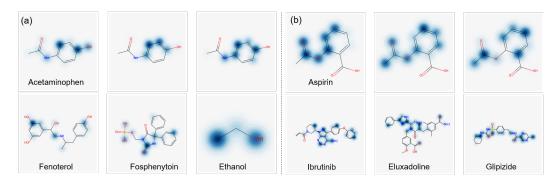


Figure 7: Visualization of the important substructure pairs in six drug pairs. (a) Acetaminophen with Fenoterol, Fosphenytoin, and Ethanol drug ligands. And (b) Aspirin with Ibrutinib, Eluxadoline, and Glipizide drug ligands. The darker the color means the greater the weight.

As demonstrated in Figure (b), In the case of aspirin, a widely used anti-inflammatory drug that also serves as an analgesic, antipyretic, and, at low doses, an antiplatelet agent, its interaction with molecules like Ibrutinib, Eluxadoline, and Glipizide is notably influenced by specific structural features. The aromatic branch of aspirin (excluding the carboxyl group region) is more prone to forming interactions with the nitrogen-containing heterocycles of other molecules. This suggests that, during DDI events, the merged graph substructures of these molecules have an enhanced propensity for direct interaction, leading to increased DDI potential. These observations provide important insights into the structural determinants of DDIs, further emphasizing the predictive capability of the I2Mole model in capturing complex inter-molecular relationships.