## Track 1:

# **Adversarial Watermarking for Face Recognition**

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#### Abstract

Watermarking is an essential technique for embedding an identifier (*i.e.*, water-1 mark message) within digital images to assert ownership and monitor unauthorized 2 3 alterations. In face recognition systems, watermarking plays a pivotal role in ensuring data integrity and security. However, an adversary could potentially interfere 4 with the watermarking process, significantly impairing recognition performance. 5 6 We explore the interaction between watermarking and adversarial attacks on face recognition models. Our findings reveal that while watermarking or input-level per-7 turbation alone may have a negligible effect on recognition accuracy, the combined 8 effect of watermarking and perturbation can result in an *adversarial watermarking* 9 attack, significantly degrading recognition performance. Specifically, we introduce 10 a novel threat model, the adversarial watermarking attack, which remains stealthy 11 in the absence of watermarking, allowing images to be correctly recognized initially. 12 However, once watermarking is applied, the attack is activated, causing recognition 13 failures. Our study reveals a previously unrecognized vulnerability: *adversarial* 14 perturbations can exploit the watermark message to evade face recognition systems. 15 Evaluated on the CASIA-WebFace dataset, our proposed adversarial watermark-16 ing attack reduces face matching accuracy by 67.2% with an  $\ell_{\infty}$  norm-measured 17 perturbation strength of 2/255 and by 95.9% with a strength of 4/255. 18

#### **19 1 Introduction**

Face recognition systems have become increasingly prevalent in various domains, such as access control and surveillance [1–3]. Ensuring the integrity and ownership of facial images used for training and evaluation in such systems is crucial. Image watermarking has offered a viable solution for proprietary face image protection [4–6]. Watermarking can embed hidden information (also called 'watermark message') in digital faces to assert ownership, authenticate content, and verify data integrity [7–9].

However, as machine learning (ML) models become more sophisticated, they also become susceptible
to adversarial attacks. Adversarial perturbations (also known as evasion attacks) are carefully crafted
modifications to input data that deceive ML models without noticeable changes in the image to human
observers [10–12]. In the context of face recognition, such perturbations can cause recognition errors,
leading to security breaches; See the literature review in Section 2.

Although watermarking aims to protect and authenticate images, the interaction between watermarking processes and adversarial attacks remains underexplored. The presence of watermarking and adversarial attacks, along with their interaction, has added substantial complexity to evaluation of face recognition systems. Inspired by the above, we address the following question:

(Q) How does watermarking affect the adversarial robustness of face recognition systems, and can
 adversarial attacks exploit watermarking to even degrade face matching performance?



Figure 1: **Overview of the Adversarial Watermarking Attack on Face Recognition.** The green path (A) represents the standard watermarking and face recognition process, where the probe face is watermarked using the watermark encoder and correctly matched with the reference face after feature extraction. The yellow path (B) shows input-level adversarial perturbations applied to evade the face recognition system without watermarking. Subtle adversarial perturbations are added to the probe face, but they do not affect the recognition result without watermarking. The red path (C) demonstrates the adversarial watermarking process, where the adversarially perturbed face image, after being watermarked, fails to match the reference face.

To the best of our knowledge, our work unveils the joint effects of watermarking and adversarial attacks on face recognition models for the first time. We summarize our contributions below.

• We propose a testbed (Figure 1) that integrates watermarking techniques into face recognition systems. This framework embeds watermarks into facial images to assert ownership while facilitating the study of adversarial attacks (Figure 1 (R) and (C))

the study of adversarial attacks (Figure 1-(B) and (C)).

We introduce a new threat model (Figure 1-(C)) called the Adversarial Watermarking attack,
which differs from conventional evasion attacks against image classifiers [10, 13, 14]. This attack
is designed to remain stealthy when watermarking is absent (Figure 1-(B)), allowing images to be
correctly recognized initially. However, once watermarking is applied, the attack is triggered, causing
recognition failures and exposing a critical vulnerability in the watermarking process.

• We validate our proposed attack through extensive experiments on the open-source CASIA-WebFace dataset. Our results demonstrate a significant degradation in face matching performance under small adversarial perturbations (*e.g.*,  $\frac{2}{255}$  and  $\frac{4}{255}$ ) when the watermarking is applied (Figure 1).

## 50 2 Related Work

Watermarking in Face Recognition. Watermarking techniques have long been used to embed im-51 52 perceptible information into digital images for purposes such as copyright protection, authentication, and integrity verification [6, 15, 16]. In the realm of face recognition, watermarking serves as a tool 53 to protect personally identifiable images from unauthorized use and tampering [4, 17-21]. Various 54 methods have been proposed to integrate watermarking into facial images without significantly 55 affecting recognition performance. Traditional watermarking approaches use frequency domain 56 transformations such as Discrete Cosine Transform (DCT) and Discrete Wavelet Transform (DWT) to 57 embed watermarks in images, with the aim of robustness against common image processing attacks 58 [22, 23]. In contrast, recent methods leverage deep neural networks (DNNs) for watermarking, such 59 as the HiDDeN framework, which employs end-to-end trainable networks to embed and extract 60 watermarks, enhancing resilience against various attacks [5]. Other recent studies have focused 61 on ensuring that the watermarking process preserves critical facial features essential for accurate 62 recognition [7, 8, 17]. However, these methods mainly focus on robustness against non-adversarial 63 distortions and fail to account for the impact of adversarial perturbations specifically designed to 64 deceive ML models, particularly when watermarking is applied. 65

Adversarial Attacks in Face Recognition. Adversarial attacks involve introducing subtle, often 66 imperceptible perturbations to input data with the intent of deceiving ML models [10, 13, 24]. In face 67 recognition systems, adversarial examples can lead to recognition errors, impersonation, or evasion, 68 posing significant security risks [25–27]. For example, attackers can manipulate facial images to 69 bypass authentication systems or to impersonate other enrolled individuals in the system. Various 70 attack generation algorithms, such as Fast Gradient Sign Method (FGSM) [10] and Projected Gradient 71 72 Descent (PGD) [14], have been employed to generate adversarial examples against face recognition models. Meanwhile, defense mechanisms such as adversarial training and input pre-processing have 73 been proposed to mitigate these attacks [14, 24, 28]. The ongoing arms race between attack and 74 defense persists. However, existing studies have primarily focused on evading or improving the 75 robustness of model performance, without considering the impact of watermarking whose use is 76 growing, e.g., for labeling computer generated images. To the best of our knowledge, the interaction 77 between adversarial perturbations and watermarking in face recognition is largely unexplored, with 78 no prior work investigating how adversarial attacks leverage watermarking to degrade recognition 79 performance. 80

#### 81 **3 Methods**

Watermarking System. We start by introducing the technique used for generating watermarked face images and its application in the subsequent face recognition task, as shown in Figure 1-(A). To formalize the watermarking problem, let the input image be denoted as  $\mathbf{I} \in \mathbb{R}^{H \times W \times C}$ , and a binary watermark message as  $\mathbf{m} \in \{0, 1\}^{L}$  (an *L*-bit digital signature) embedded into the facial images [5, 7, 29]. Our goal is to produce a watermarked image  $\mathbf{I}_w$  that maintains visual similarity to the original image  $\mathbf{I}$  containing the watermark message  $\mathbf{m}$ . Furthermore, the watermarked image should allow extraction of  $\mathbf{m}$ , allowing provenance of the image.

We implement the watermarking system using 89 the open source neural network-based HiDDeN 90 framework [5]. This system consists of an en-91 coder network  $f_{\theta}$  and a decoder network  $g_{\phi}$ . 92 93 The encoder takes the input image I and the watermark message m as inputs and generates the 94 watermarked image  $\mathbf{I}_{w} = f_{\boldsymbol{\theta}}(\mathbf{I}, \mathbf{m})$ . The de-95 coder takes the watermarked image  $I_w$  as input 96 97 and reconstructs the embedded watermark message  $\hat{\mathbf{m}} = g_{\phi}(\mathbf{I}_{w})$ . The encoder and decoder 98 networks are jointly trained using a combina-99 tion of image reconstruction loss and message 100 decoding loss. The loss of image reconstruc-101 tion  $\ell_{\rm recons}$  (e.g., mean squared error) ensures 102 103 that the watermarked image is visually similar 104 to the original, while the loss of message decoding  $\ell_{\text{decode}}$  (e.g., bitwise binary cross-entropy 105 loss) minimizes the difference between embed-106

Table 1: The robustness of watermarking evaluated using the reconstructed watermark bit accuracy (%) against various (post-watermarking) data transformations at different scaling strengths. Each value is averaged over 1000 face images, with an image size of  $112 \times 112$  and a watermark string bit length of 48. See more setup details in Section 4.

Transformation	Scaling ratio							
	1	0.95	0.9	0.85	0.8	0.75		
Crop	98.39	97.22	93.7	95.12	94.77	94.3		
Resize	98.39	92.47	92.0	91.58	89.62	85.93		
Transformation	Scaling factor							
	1	1.5	2	2.5	3	3.5		
Brightness	98.39	98.48	96.65	94.21	91.6	88.87		
Contrast	98.39	98.81	98.15	96.82	94.92	92.62		
Transformation	JPEG quality factor							
	100	95	90	85	80	75		
JPEG compression	98.39	90.36	85.0	80.8	76.65	73.06		

ded and extracted watermark messages. The overall training objective for watermarking encoder and
 decoder is:

$$\min_{\boldsymbol{\theta},\boldsymbol{\phi}} \mathbb{E}_{\mathbf{I},\mathbf{m}} \left[ \ell_{\text{recons}}(\mathbf{I}_{w}, \mathbf{I}) + \lambda \ell_{\text{decode}}(\hat{\mathbf{m}}, \mathbf{m}) \right]$$
(1)

where  $\lambda$  is a regularization parameter balancing the two losses. During training, a random message generator produces random bits for m. This randomness allows the network to generalize to any watermark message, enabling us to embed user-defined messages in face images later on. Table 1 shows that our watermarking system is fairly robust against different data transformations. However, as demonstrated later, this does not guarantee adversarial robustness for the downstream task when using watermarked data.

Face Recognition on Watermarked Images. With watermarked face images acquired above, we proceed to face recognition to assess the impact of the watermarking. In what follows, we provide a brief background on face recognition. Given an input face image I, the face recognition model  $h_{\psi}$ maps the image to a feature representation  $\mathbf{z}$ :  $\mathbf{z} = h_{\psi}(\mathbf{I})$ , where  $\psi$  represents the learnable parameters of the model. The feature z is typically extracted from the penultimate layer of a convolutional neural network (CNN), such as ResNet [30]. The model is trained to minimize a classification loss, such as the softmax loss [31] or margin-based losses [31–33], which encourage facial features from the same identity to be close in the embedding space while pushing apart facial features from different identities. During inference, the model extracts feature representations for a probe face  $I_p$  and a reference face  $I_r$ , denoted as  $z_p$  and  $z_r$ , respectively. The similarity between the probe and reference faces is computed using the cosine similarity:

$$s(\mathbf{z}_{\mathrm{p}}, \mathbf{z}_{\mathrm{r}}) = \frac{\mathbf{z}_{\mathrm{p}}^{\top} \mathbf{z}_{\mathrm{r}}}{|\mathbf{z}_{\mathrm{p}}||\mathbf{z}_{\mathrm{r}}|}$$
(2)

where  $|\cdot|$  denotes the Euclidean norm. A match is determined based on whether the similarity score exceeds a predefined threshold  $\tau$ :

$$match(\mathbf{z}_{p}, \mathbf{z}_{r}) = \begin{cases} 1, & \text{if } s(\mathbf{z}_{p}, \mathbf{z}_{r}) \geq \tau, \\ 0, & \text{otherwise.} \end{cases}$$
(3)

Our experiments later verify that the watermarking process does not significantly degrade face recognition performance in the absence of adversarial perturbations.

Adversarial Watermarking Attack for Face Recognition. We introduce an adversarial watermarking attack that exploits the interaction between adversarial perturbations and the watermarking process to degrade face recognition performance. The adversary aims to craft a minimal perturbation  $\delta$  added to a probe face image  $I_p$  and find a specific watermark message  $m \in \{0, 1\}^L$  such that:

134 1. **Pre-watermark recognition success:** The perturbed image  $\mathbf{I}'_{\rm p} = \mathbf{I}_{\rm p} + \boldsymbol{\delta}$  is correctly 135 matched with the reference image  $\mathbf{I}_{\rm r}$  by the face recognition model  $h_{\psi}$ , *i.e.*, the similarity 136 between their feature representations remains high. Here  $\boldsymbol{\delta} \in \mathbb{R}^{H \times W \times C}$  denotes adver-137 sarial perturbations bounded by  $\|\boldsymbol{\delta}\|_{\infty} \leq \epsilon$ , where  $\epsilon$  is the perturbation strength ensuring 138 imperceptibility.

139 2. Post-watermark recognition failure: After applying the watermarking encoder  $f_{\theta}$  with the 140 adversary-learned watermark message **m**, the perturbed input image  $\mathbf{I}'_{\mathrm{p}}$  and its watermarked 141 counterpart  $\mathbf{I}'_{\mathrm{w}} = f_{\theta}(\mathbf{I}'_{\mathrm{p}}, \mathbf{m})$  lead to a low similarity with the reference image  $\mathbf{I}_{\mathrm{r}}$ , causing 142 the face recognition model  $h_{\psi}$  to fail.

Our rationale has two key aspects. First, satisfying both conditions 1 and 2 ensures that the adversarial attack ( $\delta$ ) stays stealthy when watermarking is absent, but is triggered upon watermark application, leading to recognition failures. Second, this design reveals a unique adversarial challenge in face recognition with watermarking, where the optimization of the watermark message in condition 2 interacts synergistically with the input perturbations  $\delta$  to amplify the adversarial effect.

We propose the following joint optimization problem to find the adversarial perturbation  $\delta$  and the watermark message m:

$$\min_{\mathbf{m}\in\{0,1\}^L} \min_{\|\boldsymbol{\delta}\|_{\infty} \leq \epsilon} -s(\mathbf{z}'_{\mathbf{p}}, \mathbf{z}_{\mathbf{r}}) + s(\mathbf{z}'_{\mathbf{w}}, \mathbf{z}_{\mathbf{r}})$$
(4)

where the optimization variables are the binary watermark message **m** and the input perturbations  $\delta$ , and  $s(\cdot, \cdot)$  and  $\mathbf{z}_r$  are defined in (2). Recall that  $\mathbf{z}'_p = h_{\psi}(\mathbf{I}'_p)$  and  $\mathbf{z}'_w = h_{\psi}(\mathbf{I}'_w)$  are the feature representations given the probe image  $\mathbf{I}'_p = \mathbf{I}_p + \delta$  and  $\mathbf{I}'_w = f_{\theta}(\mathbf{I}'_p, \mathbf{m})$ , respectively. In (4), the original similarity term  $s(\mathbf{z}'_p, \mathbf{z}_r)$  ensures that the perturbed face is still recognized as the same identity in the absence of watermarking. And the watermarked similarity term  $s(\mathbf{z}'_w, \mathbf{z}_r)$  minimizes the similarity between the watermarked, perturbed image and the reference image, causing face recognition failure post-watermarking.

To solve the optimization in (4), we then adopt an alternative optimization procedure to jointly 157 optimize  $\delta$  and m. Specifically, we use the PGD (projected gradient descent) method [14] to 158 iteratively minimize one variable while keeping the other fixed. In the optimization process, we face 159 the challenge of the discrete nature of the watermark message m. Direct optimization over binary 160 variables is computationally intractable for large dimensionality L. To address this, we relax m to be 161 continuous in the range  $[0, 1]^L$  during the optimization. This relaxation allows us to employ PGD in 162 an efficient way. That is, after performing gradient descent on the relaxed m, we project back onto the 163 binary set  $\{0,1\}^L$  by rounding each element to 0 or 1. This ensures the watermark message remains 164 valid for the encoder. By alternately optimizing over  $\delta$  and m, we minimize the joint objective. This 165 approach finds a combination of adversarial perturbation and a watermark message that maintains 166 high genuine similarity before watermarking and cause misrecognition afterward. 167

#### **168 4 Experiments**

Experimental Setup. We use the CASIA-WebFace dataset [34], containing face images of 10,575 169 individuals, for evaluating face recognition models. We extract 1,000 individuals with two matching 170 face images for each identity ( $I_p$  and  $I_r$ ), and pre-processed them by aligning and resizing the 171 images to  $112 \times 112$  pixels. We adopt our face recognition model from the AdaFace framework 172 [35]. AdaFace is known for its adaptive margin loss that accounts for the quality of the face images, 173 improving recognition performance. The model is trained on MS-Celeb-1M dataset [31] using 174 standard training protocols with a ResNet-50 backbone [30]. For watermarking, we follow the 175 HiDDeN framework [5] to solve the problem (1). The encoder and decoder networks are trained 176 on the MS-COCO dataset [36] with random 48-bit watermark messages. The trained encoder is 177 then used to embed watermarks in the CASIA-WebFace face images. In generating the adversarial 178 watermarking attack (4), the step sizes for optimizing  $\delta$  and m are set to  $\alpha = \frac{\epsilon}{T}$  and  $\beta = \frac{1}{T}$ , 179 respectively, where T = 10 represents the number of iterations for the PGD-10 attack. 180

**Evaluation.** We assess the effectiveness of the adversarial watermarking attack by analyzing face recognition performance under two key conditions. First, in the case of recognition with adversarial perturbations, adversarial perturbations are applied to the probe images *without watermarking*. Next, in the case of recognition with the adversarial watermarking attack (*with watermarking*), both adversarial perturbations and an optimized watermark message are applied, following the joint optimization in (4).



Figure 2: Violin plots of similarity scores in (2) at different  $\epsilon$  values (scaled by 1/255). For each  $\epsilon$ , the violin plot shows the distribution of similarity scores between perturbed probe and reference images under two conditions: with watermarking (blue) and without watermarking (red). By  $\|\delta_{\infty}\| \leq \epsilon$ , we change  $\epsilon$  to control the perturbation strength.

Table 2: Face matching accuracy (%) with and without watermarking at different perturbation levels ( $\epsilon$ , scaled by 1/255), where the matching threshold is set to  $\tau = 0.3$  in (3). Performance reduction by watermarking attack is highlighted in blue.

ε	0.0	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0
W/o Watermarking	81.8	85.4	88.5	90.9	92.2	94.1	95.7	97.5	98.3
W/ Watermarking	73.9	63.5	50.0	35.7	25.0	16.5	8.4	4.5	2.4
Reduction	7.9	21.9	38.5	55.2	67.2	77.6	87.3	93.0	95.9

Adversarial Watermarking: Joint Effects of Watermarking and Adversarial Perturbations. 187 To analyze the effect of the adversarial watermarking attack on face recognition performance, we 188 first examine the similarity scores between probe and reference images across different perturbation 189 strengths  $\epsilon$ . Figure 2 shows violin plots of the similarity distributions for face recognition, both with 190 and without watermarking, when evaluated using input perturbations  $\delta$  from the proposed adversarial 191 watermarking attack. As the perturbation strength  $\epsilon$  increases, the similarity between probe and 192 reference images decreases significantly in the presence of watermarking, while it remains largely 193 unaffected without watermarking. This is because in the absence of watermarking, the first loss 194 term in (4) aims to maximize the similarity between the probe image and the reference image for 195 the applied perturbations  $\delta$ . With watermarking in the face recognition process, the similarity score 196 quickly drops with increased perturbation strength. In fact, when  $\epsilon = 0.5/255$ , the similarity has 197 tended to be smaller than the matching threshold  $\tau$  (commonly set at  $\tau = 0.3$ ). This shows that even a 198 small adversarial perturbation can disrupt face recognition after watermarking, although performance 199 remains stable without watermarking. 200

**Table 2** shows that watermarking reduces face matching accuracy at all perturbation levels ( $\epsilon$ ). For 201 example, at  $\epsilon = 0.0$ , accuracy drops by 7.9% from 81.8% to 73.9% after watermarking. This 202 indicates that the adversarial watermark message alone, as found by (4), reduces recognition accuracy. 203 As the perturbation magnitude  $\epsilon$  increases, the accuracy reduction intensifies. At  $\epsilon = 2/255$ , the 204 accuracy decreases by 67.2%, from 92.2% to 25.0%, and at  $\epsilon = 4/255$ , the reduction reaches 205 95.9%, with the accuracy dropping from 98.3% to just 2.4%. These drastic reductions illustrate the 206 adversarial watermarking attack's effectiveness in significantly degrading face recognition, especially 207 at higher perturbation magnitudes. The results demonstrate that adversarial watermarking exploits 208 the interaction with perturbations, significantly reducing face matching accuracy. 209

Visualizations of Face Images vs. Watermarking and Perturbations. Figure 3 examines the 210 combination of watermarking and perturbations (with strength  $\epsilon$  at 4/255) on face images. To 211 compare with reference faces (a), original faces (b) are visualized along with similarity scores by (2). 212 Watermarked faces (c) are added with message m by (4), along with similar scores to (b), exhibiting 213 minor effects by watermarking. Perturbed faces (d) are added with perturbation  $\delta$  by (4), along with 214 larger scores than (b), maintaining the face matching performance. Adversarial watermarked faces 215 (g) have extremely low similarity scores, exhibiting the joint adversarial effect of watermarking and 216 perturbation. Element-wise absolute differences are visualized in (d), (f), and (h) respectively for (c), 217 (e), (g) to show the imperceptibility of watermark/perturbation. It should be noted that adversarial 218 watermarking difference (h) shows more focus on the edges and corners, *i.e.*, the high frequency area 219 than (d) and (f), illustrating why the attack works while watermakring or perturbation alone does not. 220



Figure 3: Visualization of reference, probe, and perturbed/watermarked face images along with perturbation/watermark for four identities. (a) Reference face. (b) Probe face. (c) Watermarked face. (d) Difference between (b) and (c). (e) Perturbed face. (f) Difference between (b) and (e). (g) Adversarial watermarked face by watermarking perturbed face. (h) Difference between (b) and (g). All element-wise absolute differences are scaled by  $\times 10$  and color reverted. All probe faces are marked with their similarity score compared with reference faces at the top of images.

## 221 5 Conclusion

Our study investigated the vulnerabilities of face recognition systems when adversarial perturbations are combined with watermarking. While watermarking alone had a minimal effect on recognition accuracy, the introduction of adversarial perturbations before watermarking caused significant performance degradation. Our findings show that adversarial watermarking attacks could severely undermine recognition systems even if they remain stealthy when watermarking is absent, highlighting the need for improved defenses in both watermarking and face recognition models.

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