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# Deep Modularity Networks with Diversity-Preserving Regularization

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Yasmin Salehi, Dennis Giannacopoulos

Department of Electrical and Computing Engineering  
McGill University

yasmin.salehi@mail.mcgill.ca, dennis.giannacopoulos@mcgill.ca

## Abstract

Graph clustering plays a crucial role in graph representation learning but often faces challenges in achieving feature-space diversity. While Deep Modularity Networks (DMoN) leverage modularity maximization and collapse regularization to ensure structural separation, they lack explicit mechanisms for feature-space separation, assignment dispersion, and assignment-confidence control. We address this limitation by proposing Deep Modularity Networks with Diversity-Preserving Regularization (DMoN-DPR), which introduces three novel regularization terms: distance-based for inter-cluster separation, variance-based for per-cluster assignment dispersion, and an assignment-entropy penalty with a small positive weight, encouraging more confident assignments gradually. Our method significantly enhances label-based clustering metrics on feature-rich benchmark datasets (paired two-tailed t-test,  $p \leq 0.05$ ), demonstrating the effectiveness of incorporating diversity-preserving regularizations in creating meaningful and interpretable clusters.

## 1 Introduction

Graph clustering is a crucial problem within the graph representation learning domain, and essential for various applications, including but not limited to community detection in social networks (Perozzi et al., 2014; Xiao et al., 2015), data exploration (Perozzi and Akoglu, 2018), and functional module identification in biological networks (Jin et al., 2021). Consequently, there has been a surge in methods aimed at enhancing graph clustering performance. Recent advancements have included techniques like Graph Neural Networks (GNNs) (Scarselli et al., 2008), which leverage node features and graph structure for representation learning, often through unsupervised training (Tsitsulin et al., 2023). In this context, graph pooling methods have also become prominent, as they provide a way to coarsen graphs by aggregating nodes into clusters (Cangea et al., 2018). Yet, some of these methods such as DiffPool (Ying et al., 2018) and MinCutPool (Bianchi et al., 2019) were found to be computationally costly and/or too rigid, leading to poor convergence (Tsitsulin et al., 2023).

To address these limitations, Deep Modularity Networks (DMoN) (Tsitsulin et al., 2023) were introduced, combining spectral modularity maximization (Newman, 2006) with collapse regularization (Tsitsulin et al., 2023) to avoid trivial clustering solutions. Although DMoN captures structural communities, two practical gaps remain. First, the loss is agnostic to feature-space geometry and to how sharply clusters specialize over nodes, resulting in structurally distinct but feature-wise homogeneous clusters, and reducing effectiveness in applications requiring diverse and meaningfully differentiated clusters. Second, it provides no handle to shape the confidence dynamics of assignments, risking premature hardening.

**Why diversity matters.** Accounting for both inter-cluster separation and intra-cluster variety prevents information collapse and yields richer representations. In practice, diversity improves downstream utility—for example, diversified recommendation in e-commerce optimizes cluster-level variety to boost engagement (Kim and Kang, 2025), and drawing items from distinct clusters raises serendipity without sacrificing accuracy (Aytekin and Karakaya, 2014). Beyond recommendation, biological networks exhibit the same principle: modules that are cohesive inside yet distinct outside reveal functional relationships that density-only objectives can miss (Spirin and Mirny, 2003). Recent graph-pooling work therefore introduces explicit mechanisms to spread centroids and diversify within-cluster features (Liu et al., 2023). These considerations motivate our design.

**Present Work** Motivated by the above, we propose Deep Modularity Networks with Diversity-Preserving Regularization (DMoN-DPR), an extension of DMoN that augments its objective with three regularizers explicitly promoting diversity among clusters. These include a distance-based regularization term, which penalizes clusters with centroids too close in feature space to encourage distinct separation; a variance-based regularization term that increases the dispersion of assignment probabilities across nodes for each cluster, and an assignment-entropy penalty added with a small positive weight, to avoid premature hard assignments and to let distance/variance terms drive diversity. By performing extensive evaluations, we demonstrate that our method improves clustering performance on the benchmark datasets, noticeably on Coauthor CS and Coauthor Physics datasets, which benefit from this enriched representation due to their rich feature spaces.

## 2 Related Work

Early graph clustering often decoupled features from structure. k-means on raw features (Lloyd, 1982) ignores connectivity; pairing k-means with DeepWalk or DGI embeddings (Perozzi et al., 2014; Veličković et al., 2018; Tsitsulin et al., 2023) injects structural signals but remains a two-stage pipeline, typically trailing end-to-end models that jointly learn representations and cluster assignments. Meanwhile, Chebyshev-based spectral convolutions (Defferrard et al., 2016) efficiently approximate graph filters, laying a scalable foundation for modern GNNs.

On the other hand, pooling methods capture hierarchy. NOCD (Shchur and Günnemann, 2019) directly optimizes graph likelihood but can struggle with scale and feature use. DiffPool (Ying et al., 2018) learns soft cluster assignments end-to-end yet incurs quadratic cost (Tsitsulin et al., 2023). MinCut pooling (Bianchi et al., 2020) adds normalized cut and orthogonality terms that may hinder convergence; the Ortho variant keeps only the latter and loses structural cues. SAGPool (Lee et al., 2019) ranks node importance via self-attention, improving selectivity at added training cost on large graphs.

For unsupervised representation learning, DGI (Velickovic et al., 2019) maximizes mutual information between local and global summaries; InfoGraph extends this idea to graph-level representations (Sun et al., 2019).

More recently, DMoN (Tsitsulin et al., 2023) integrates modularity maximization with collapse regularization in an end-to-end framework, unifying community detection and neural feature learning and achieving strong NMI and modularity across benchmarks.

## 3 Deep Modularity Networks with Diversity-Preserving Regularization

DMoN tackles the issues of previous techniques by leveraging an optimization objective that combines insights from spectral modularity maximization (Newman, 2006) with a unique regularization term called collapse regularization (Tsitsulin et al., 2023). Specifically, DMoN encodes the cluster assignments, represented as a soft assignment matrix  $C$  by using a softmax function over the output of a GNN, allowing differentiation during optimization. For each node, a soft cluster assignment  $C$  is computed as follows:

$$C = \text{softmax}(\text{GCN}(\tilde{A}, X)) \tag{1}$$

where GCN is a multi-layer graph convolutional network,  $\tilde{A}$  is the normalized adjacency matrix  $\tilde{A} = D^{-\frac{1}{2}}AD^{-\frac{1}{2}}$ , and  $X$  represents the node features. The objective function of DMoN,  $L_{\text{DMoN}}$ , combines a modularity term with a collapse regularization term to optimize the clustering. The

modularity term measures the quality of the cluster assignments by maximizing the density of intra-cluster edges relative to a null model, while the collapse regularization prevents trivial solutions where all nodes are assigned to the same cluster. The objective function is formulated as:

$$L_{\text{DMoN}}(C; A) = \underbrace{-\frac{1}{2m} \text{Tr}(C^\top BC)}_{\text{Modularity term}} + \underbrace{\frac{\sqrt{k}}{n} \left\| \sum_i C_i^\top \right\|_F - 1}_{\text{Collapse Regularization term}} \quad (2)$$

where  $(\frac{1}{2m})\text{Tr}(C^\top BC)$  is the modularity term (measuring how well clusters are internally connected compared to random chance),  $B = A - \frac{dd^\top}{2m}$  is the modularity matrix,  $d$  is the degree vector,  $m$  is the total number of edges,  $\frac{\sqrt{k}}{n} \left\| \sum_i C_i^\top \right\|_F - 1$  represents the collapse regularization term, which discourages the formation of trivial clusters by penalizing the Frobenius norm of the assignment matrix  $C$ ,  $\|\cdot\|_F$  denotes the Frobenius norm, and  $k$  is the number of clusters. This regularization term encourages balanced cluster assignments, thereby improving the quality of clustering and avoiding degenerate solutions.

Building upon the DMoN framework, we augment the objective with three regularizers:

$$L_{\text{DMoN-DPR}}(C; A) = L_{\text{DMoN}} + W_{\text{dist}} L_{\text{DPR}}^{\text{distance}} + W_{\text{var}} L_{\text{DPR}}^{\text{variance}} + W_{\text{entropy}} L_{\text{DPR}}^{\text{entropy}}. \quad (3)$$

Here,  $W_{\text{dist}}$ ,  $W_{\text{var}}$ , and  $W_{\text{entropy}}$  control the influence of each term. These additions promote *inter-cluster separation* (distance) and *per-cluster assignment dispersion* (variance). We use a *small positive* entropy weight so per-node entropy decreases *slowly*, preserving higher uncertainty early and thus *indirectly* encouraging more balanced cluster usage during exploration; the primary mechanism for cluster-size balance remains DMoN’s collapse regularizer.

**Distance-Based Regularization** Inspired by SimCLR (Chen et al., 2020), which showed that contrastive loss promotes well-separated clusters, the distance-based regularization term encourages distinct cluster centroids in feature space. It is defined as:

$$L_{\text{DPR}}^{\text{Distance}} = \frac{1}{k(k-1)} \sum_{i=1}^k \sum_{\substack{j=1 \\ j \neq i}}^k \text{ReLU}(\epsilon - \|\mu_i - \mu_j\|_2^2) \quad (4)$$

where  $k$  is the number of clusters,  $\mu_i$  and  $\mu_j$  are the centroids of clusters  $i$  and  $j$ , computed as  $\mu_i = \frac{\sum_{v=1}^n C_{vi} X_v}{\sum_{v=1}^n C_{vi}}$ , where  $X_v$  is the feature vector of node  $v$ ,  $\|\cdot\|_2^2$  denotes the squared Euclidean norm,  $\epsilon$  is a predefined threshold that sets the minimum acceptable squared distance between cluster centroids, and ReLU is the Rectified Linear Unit function, ensuring that only distances below  $\epsilon$  contribute to the loss. By penalizing pairs of clusters whose centroids are closer than  $\epsilon$ , clusters can be effectively pushed apart in the feature space. By encouraging greater separation between clusters, it enhances inter-cluster diversity and reduces overlap, leading to more distinguishable and meaningful clusters.

**Variance-Based Regularization** The variance-based regularization term encourages dispersion in the assignment matrix by maximizing, for each cluster, the variance of its assignment probabilities across nodes:

$$L_{\text{DPR}}^{\text{variance}} = -\frac{1}{k} \sum_{i=1}^k \text{Var}(C_{:i}) \quad (5)$$

where  $\text{Var}(C_{:i})$  denotes the variance of the assignment probabilities of all nodes to cluster  $i$ . Maximizing this variance prevents uniform cluster columns (e.g., every node assigned with equal probability), ensuring that clusters specialize over different subsets of nodes and thereby enhancing assignment diversity.

**Entropy-Based Regularization** We define:

$$L_{\text{DPR}}^{\text{entropy}} = -\frac{1}{n} \sum_{v=1}^n \sum_{i=1}^k C_{vi} \log(C_{vi} + \delta) \quad (6)$$

which is the average per-node Shannon entropy of the soft assignments, where  $n$  is the number of nodes,  $C_{vi}$  is the soft assignment probability of node  $v$  to cluster  $i$ ,  $\delta$  is a small constant added to prevent logarithm of zero, ensuring numerical stability. We minimize  $L_{\text{DPR}}$  to gently encourage more confident assignments. Because minimizing entropy can lead to premature hardening, we apply a small weight  $W_{\text{entropy}}$  (typically 0.001–0.1) so that entropy decreases *slowly* during training.

## 4 Experiments

**Evaluation Protocol** To evaluate the effectiveness of our proposed regularization objective, we conducted experiments on Cora, CiteSeer, and PubMed datasets (Yang et al., 2016), as well as the Coauthor CS and Coauthor Physics datasets (Shchur et al., 2018). Information regarding these datasets is presented in Appendix A. Following the evaluation protocol outlined in (Tsitsulin et al., 2023), we employed the following metrics to assess performance: graph conductance ( $C$ ), modularity ( $Q$ ), Normalized Mutual Information (NMI) with ground-truth labels, and the pairwise F1 measure. Additionally, we use the following quantitative measures to analyze feature-space diversity: average inter-centroid distance (mean pairwise Euclidean distance between cluster centroids), minimum inter-centroid distance (the smallest pairwise distance among centroids), average intra-cluster variance (average within-cluster variance of node embeddings), and Silhouette score (a standard measure of per-point cohesion vs. separation). The quantification of diversity results are presented in Appendix B.

**Baseline & Implementation Details** We select DiffPool (Ying et al., 2018), MinCut pooling (Bianchi et al., 2019) and DMoN (Tsitsulin et al., 2023) as our baselines. Additionally, we focus on ablation studies and significance tests against vanilla DMoN to isolate the impact of the new diversity terms. Furthermore, similar to (Tsitsulin et al., 2023), one layer of GCN (Kipf and Welling, 2016) with 512 neurons was used to create the graph embedding, followed by a pooling layer. Likewise, the models were trained for 1000 epochs using Adam optimizer with a learning rate of 0.001. The code—implemented by extending the DMoN implementation in PyTorch Geometric (Fey and Lenssen, 2019)—is available at [www.github.com/YasminSalehi/DMoN-DPR](http://www.github.com/YasminSalehi/DMoN-DPR).

## 5 Results

**Table 1:** Comparison of clustering methods on three datasets (Cora, CiteSeer, PubMed). Values are in percentage.

Method	Cora				CiteSeer				PubMed			
	Graph		Labels		Graph		Labels		Graph		Labels	
	$C \downarrow$	$Q \uparrow$	NMI $\uparrow$	F1 $\uparrow$	$C \downarrow$	$Q \uparrow$	NMI $\uparrow$	F1 $\uparrow$	$C \downarrow$	$Q \uparrow$	NMI $\uparrow$	F1 $\uparrow$
DiffPool	15.99	62.78	40.13	46.55	7.92	66.69	<b>33.40</b>	<b>47.83</b>			–	
MinCut	13.65	71.79	37.74	39.15	6.19	75.21	25.21	35.28	11.14	54.66	<b>22.48</b>	41.31
DMoN	<u>10.53</u>	<b>72.77</b>	43.92	46.93	<b>4.86</b>	<u>75.45</u>	29.67	42.46	8.61	57.13	<u>22.39</u>	43.23
DPR(D)	10.95	72.20	43.98	<u>47.51</u>	4.95	<b>75.56</b>	30.09	42.46	<b>8.60</b>	<b>57.14</b>	22.38	<u>43.24</u>
DPR(V)	11.87	70.54	43.34	46.39	4.95	75.17	29.76	42.85	8.61	57.13	<u>22.39</u>	43.23
DPR(E)	<b>10.49</b>	<b>72.77</b>	44.00	47.02	<u>4.93</u>	75.25	29.95	42.96	8.62	57.11	22.36	43.22
DPR(DV)	10.89	72.07	<b>44.40</b>	47.36	5.09	75.18	<u>30.50</u>	43.25	<b>8.60</b>	<b>57.14</b>	22.38	<u>43.24</u>
DPR(DE)	10.88	72.30	44.30	<b>47.53</b>	5.07	75.18	30.47	43.13	<b>8.60</b>	57.12	22.38	<b>43.25</b>
DPR(VE)	11.86	70.51	43.24	46.36	5.05	75.01	30.17	<u>43.27</u>	<b>8.60</b>	57.13	22.37	43.21
DPR(DVE)	10.93	72.05	<u>44.37</u>	47.32	5.16	75.00	30.25	43.00	8.61	57.11	22.36	<u>43.24</u>

### 5.1 Effectiveness of DMoN-DPR in Clustering

To assess the effectiveness of DMoN-DPR, we compare the mean values of conductance ( $C$ ), modularity ( $Q$ ), NMI, and pairwise F1 measure across 10 randomly selected seeds achieved with DMoN-DPR (denoted as DPR in all the tables) to those obtained with our baselines. Tables 1 (Cora, CiteSeer, PubMed) and 2 (Coauthor CS, Coauthor Physics) summarize the results, where graph

**Table 2:** Comparison of clustering methods on two datasets (Coauthor CS, Coauthor Physics). Values are in percentage.

Method	Coauthor CS				Coauthor Physics			
	Graph		Labels		Graph		Labels	
	$C \downarrow$	$Q \uparrow$	NMI $\uparrow$	F1 $\uparrow$	$C \downarrow$	$Q \uparrow$	NMI $\uparrow$	F1 $\uparrow$
DiffPool	<b>18.19</b>	62.24	53.92	53.47	13.91	57.44	<b>56.22</b>	51.71
MinCut	21.36	71.58	64.33	49.00	13.93	<u>61.75</u>	51.39	47.79
DMoN	<u>18.63</u>	<b>72.60</b>	69.26	59.26	13.70	<b>63.45</b>	53.50	47.51
DPR(D)	18.89	72.30	71.17	61.82	16.44	56.89	53.49	50.99
DPR(V)	18.75	<u>72.50</u>	69.56	59.94	13.18	58.59	53.93	52.78
DPR(E)	19.85	70.92	<b>71.58</b>	61.33	13.49	59.33	52.83	51.09
DPR(DV)	19.14	71.96	70.72	61.35	13.43	56.48	<u>55.84</u>	<b>57.99</b>
DPR(DE)	19.81	70.57	70.96	<u>62.36</u>	14.17	56.89	54.02	55.02
DPR(VE)	19.89	70.81	<u>71.47</u>	61.33	<u>13.11</u>	55.88	49.95	53.58
DPR(DVE)	19.69	70.71	71.28	<b>62.67</b>	<b>12.84</b>	55.47	53.50	<u>57.96</u>

**Table 3:** t-statistics and p-values for all datasets (rounded to two decimal places).

Metric	Cora		CiteSeer		PubMed		Coauthor CS		Coauthor Physics	
	t-stat	p-val	t-stat	p-val	t-stat	p-val	t-stat	p-val	t-stat	p-val
Conductance	-0.88	0.40	-1.62	0.14	0.37	0.72	-5.25	$1e^{-6}$	0.51	0.62
Modularity	1.81	0.10	1.17	0.27	0.21	0.84	5.88	$1e^{-6}$	17.56	$1e^{-6}$
NMI	-0.63	0.54	-1.56	0.15	0.23	0.83	-4.64	$1e^{-6}$	-2.49	0.03
F1	-0.40	0.70	-1.28	0.23	-0.95	0.37	-2.51	0.03	-14.65	$1e^{-6}$

metrics ( $C$ ,  $Q$ ) do not rely on ground-truth labels, whereas ‘Labels’ metrics (NMI, F1) compare to known class labels.

For completeness, we defer supporting analyses to the appendix: (i) quantitative diagnostics of feature-space diversity (average/min inter-centroid distance, average intra-cluster variance, Silhouette score) (Appendix B), (ii) t-SNE visualizations of the learned clusters versus ground-truth labels (Appendix C), (iii) ablation and hyperparameter-selection studies that isolate the effect of each DPR term (Appendix D), and (iv) per-seed scores and full tables with error bars (Appendix E).

**Cora, CiteSeer, and PubMed.** Overall, the results confirm that adding diversity-preserving regularizers to DMoN almost never harms the purely topological scores—conductance ( $C \downarrow$ ) and modularity ( $Q \uparrow$ )—while consistently lifting label-aware metrics such as NMI and F1. On Cora, DPR(DV) achieves the best NMI (44.40%) and only narrowly trails DPR(DE) on F1. On CiteSeer, although DiffPool attains the highest NMI (33.40%) and F1 (47.83%), DPR variants remain competitive without the instability that causes DiffPool to collapse on PubMed<sup>1</sup>. Among the DMoN-family methods, DPR(DV) is the strongest on CiteSeer. On PubMed, all DPR variants remain stable, in contrast to DiffPool, while MinCut yields the highest NMI (22.48%) and DPR(DE) edges out others in F1. The fact that DPR(D) and DPR(DV) match the best conductance (8.60%) confirms that the regularizers maintain cut quality.

**Coauthor CS and Coauthor Physics.** On the more feature-rich<sup>2</sup> Coauthor graphs, diversity-preserving regularization brings substantial gains. On Coauthor CS, DPR(DVE) achieves a new best in F1 (62.67%) while DPR(E) sets the highest NMI (71.58%), both outperforming the already strong

<sup>1</sup>With a single DiffPool layer and our fixed cluster budget ( $C = 3$ ), the link-prediction loss on the 19 k-node PubMed graph stagnated and the assignment matrix collapsed to one cluster. Increasing the budget restores numerical stability, but yields only marginal label quality and would also violate our fixed- $C$  protocol, so we omit DiffPool scores for PubMed.

<sup>2</sup>We define feature-rich graphs as those that exhibit (i) high feature dimensionality and (ii) high average Shannon entropy per node. Please see Appendix A for more detail.

DMoN baseline without sacrificing conductance or modularity. On Coauthor Physics, DPR(DVE) obtains the lowest conductance (12.84%) and, along with DPR(DV), surpasses 57% F1—demonstrating that the full three-term objective generalizes well to larger, noisier graphs.

**Key Insights.** Therefore, our results show that the effects of distance-based (D), variance-based (V), and entropy-based (E) regularizations depend on dataset feature richness. On feature-rich datasets like Coauthor CS and Physics, adding these terms—especially D—significantly boosts NMI and F1, with DMoN-DPR(DV) raising F1 by over 10 percentage points. The V term increases assignment dispersion across nodes and performs best when combined with D. The E term, used with a small positive weight, *gradually* sharpens per-node assignments, which can *indirectly* improve cluster balance during early exploration on feature-rich datasets, but offers little benefit on simpler datasets like PubMed; the collapse regularizer remains the primary mechanism for cluster-size balance. Overall, combining D and V often yields the highest performance, underscoring the need to tailor regularization to dataset characteristics for optimal clustering.

**Statistical Significance.** To strengthen our claims, we conduct a paired t-test on Conductance, Modularity, NMI, and F1, comparing DMoN vs. the best-performing DMoN-DPR variants. We ensure both methods use exactly the same seeds in each dataset. The results are summarized in Table 3. On the citation benchmarks we adopt the strongest variant for each graph (DV on Cora and CiteSeer, DVE on PubMed). Although the average NMI and F1 of DMoN-DPR surpass or match the vanilla DMoN baseline, the paired two-tailed *t*-tests in Table 3 show *p*-values above 0.10. This indicates that, given the modest sample of random seeds, the improvements are encouraging but not yet conclusive for these sparsely featured graphs. The picture is markedly different on the feature-rich coauthor networks. The gains on NMI and F1 metrics are highly significant, indicated by  $p \leq 0.05$ , as seen in Table 3. These results validate our hypothesis that encouraging latent cluster dispersion is most beneficial when node attributes are abundant and heterogeneous, and they confirm that DMoN-DPR maintains the stability advantage of the original objective while translating it into measurably better community recovery.

**Trade-Offs Between Structural and Label-Based Metrics.** Our results reveal a clear trade-off between structural metrics (e.g., Modularity, Conductance) and label-based metrics (e.g., NMI, F1). Diversity-preserving regularization improves label alignment, especially on feature-rich datasets like Coauthor CS and Physics, by forming clusters that better match ground-truth labels—though sometimes at the cost of structural cohesion (e.g., lower modularity). Conversely, on datasets with less diverse or lower-dimensional features (e.g., PubMed), the structural metrics are less affected by the introduction of diversity-preserving regularization terms, and the benefits to label-based metrics are more modest. As a result, DMoN-DPR emerges as a more effective choice for supervised tasks prioritizing NMI and F1, whereas vanilla DMoN remains competitive for unsupervised scenarios where conductance and modularity are paramount. Tailoring the clustering strategy to the dataset and task requirements is therefore essential.

## 5.2 Execution Times and Runtime Analysis

Table 4 reports the execution times (in seconds) of DMoN and DMoN-DPR on five commonly used graph datasets. All experiments were conducted on a CPU to ensure consistent runtime measurement without GPU scheduling effects.

**Table 4:** Execution times (in seconds) on CPU for DMoN and DMoN-DPR.

Method	Cora	CiteSeer	PubMed	Coauthor CS	Coauthor Physics
DMoN	32	76	310	722	2107
DMoN-DPR	35	71	300	751	1946

Although DMoN-DPR includes additional regularization terms for Distance-based, Entropy-based, and Variance-based constraints, its runtime is sometimes comparable to or even marginally lower than plain DMoN. The reason is that the most time-consuming part of both methods is dominated by adjacency-based operations (e.g., matrix multiplications with the graph Laplacian or adjacency matrix), which scale on the order of  $\mathcal{O}(|E|k)$  or  $\mathcal{O}(N^2k)$  for large, dense graphs (where  $N$  is the number of nodes,  $E$  is the set of edges, and  $k$  is the number of clusters). In contrast, the extra

DPR calculations—computing entropy across nodes, the variance of cluster assignments, or centroid distances—represent only  $\mathcal{O}(Nk + k^2F)$  overhead (with  $F$  being the feature dimension) and are typically negligible next to the larger matrix multiplications.

### 5.3 Limitations and Future Directions

While DMoN-DPR introduces clear benefits, it also presents a few limitations. First, tuning the diversity-preserving weights for distance, variance, and entropy remains manual. Though our empirical studies revealed consistent patterns: high-dimensional datasets like Coauthor CS and Physics benefited from larger distance weights (1 or 10), variance weights of 1 or 0.1 worked well across most datasets, and entropy value of 0.1 served as a good upper bound. A promising direction for future work is to develop an adaptive scheme that learns these weights during training, reducing reliance on manual tuning. Second, the gains from diversity regularization are more pronounced on feature-rich datasets. On lower-dimensional datasets like PubMed, improvements in NMI and F1 are modest—though visualizations (Figure 1) suggest that DMoN-DPR still forms more coherent clusters than the baseline. Future research could explore alternative regularizers to better capture structure in such settings.

## 6 Conclusion

In this work, we presented DMoN-DPR, an enhanced version of Deep Modularity Networks (DMoN) that incorporates diversity-preserving regularizations to enrich the clustering objective. By introducing distance-, entropy-, and variance-based penalties alongside the original modularity and collapse regularization terms, our approach promotes diversity by increasing inter-cluster feature separation (distance) and within-cluster assignment dispersion (variance), while a small-weight entropy term gradually sharpens assignments without sacrificing exploration. Our empirical results on the Coauthor CS and Coauthor Physics benchmark datasets indicate that DMoN-DPR significantly improves alignment with ground-truth labels in feature-rich datasets. While structural metrics such as modularity and conductance remained competitive, the additional diversity constraints contributed to more interpretable and semantically meaningful cluster formations, marked by significant improvements in NMI and F1 scores, producing higher alignment with ground-truth labels and generally reflecting clearer semantic distinctions. Overall, DMoN-DPR achieves a balance between interpretability and structural integrity, making it a powerful solution for graph clustering tasks that demand both topological cohesion and semantic differentiation, marking a significant advancement in feature-aware graph clustering.

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- $R_D$  (distance) repels centroids in feature space, reducing cluster overlap.
- $R_V$  (variance) prevents overly tight clusters, mitigating premature "hard" assignments.
- $R_E$  (entropy) avoids early dominance by any single cluster, helping to avert mode collapse.

These terms add complementary constraints but do not create new problematic local minima or break DMoN's consistency. Rather, they refine the solution space by adding complementary constraints. While we do not offer formal proofs here, we consistently observe stable training across all studied datasets.

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## A Datasets

The Cora, CiteSeer, and PubMed datasets are citation networks where nodes represent papers and edges denote citation relationships, with node labels corresponding to the topic of each paper. The Coauthor CS and Coauthor Physics datasets are co-authorship graphs, where nodes represent authors and edges indicate collaborations, with labels reflecting the field of research. The following table provides information about the datasets used for running experiments.

**Feature-rich Datasets** A graph is considered to be feature-rich when its nodes are described by high-dimensional feature vectors that carry substantial information content. Formally, for each node  $v$ , the feature vector  $x_v$  is normalized into a probability distribution  $p_v = \frac{x_v}{\mathbf{1}^\top x_v}$ , and its information content is quantified by the Shannon entropy  $H(p_v) = -\sum_{i=1}^F p_{v,i} \log_2 p_{v,i}$ . A dataset of such nodes is said to be feature-rich when it combines two key properties: (1) high dimensionality, meaning that the number of features  $|X| = F$  is large, and (2) high average entropy, defined as:

$$\frac{1}{N} \sum_v H(p_v),$$

indicating that on average, the features across nodes are diverse and well-distributed rather than concentrated in a few dimensions. Together, these conditions ensure that the feature space provides both breadth and depth, enabling richer representations for learning tasks. For example, Coauthor-CS is a feature-rich dataset for having  $|X| = 6805$  and entropy = 5.51 bits, versus PubMed with  $|X| = 500$  and entropy = 5.17 bits.

**Table 5:** Dataset characteristics, where  $(|V|)$  is the number of vertices,  $(|E|)$  is the number of edges,  $|X|$  is the number of features, and  $|Y|$  is the number of cluster labels.

Dataset	$ V $	$ E $	$ X $	$ Y $	Mean Entropy (bits)
Cora	2708	5278	1433	7	4.05
CiteSeer	3327	4614	3703	6	4.94
PubMed	19717	44325	500	3	5.17
Coauthor CS	18333	81894	6805	15	5.51
Coauthor Physics	34493	247962	8415	5	4.76

## B Quantification of Diversity

**Table 6:** Comparison of diversity resulted from the clustering methods on three datasets (Cora, CiteSeer, PubMed). AICD is average inter-centroid distance, MICD is minimum inter-centroid distance, AICV is average intra-cluster variance, and Sil is the Silhouette score.

Method	Cora				CiteSeer				PubMed			
	AICD	MICD	AICV	Sil	AICD	MICD	AICV	Sil	AICD	MICD	AICV	Sil
DiffPool	3.69	2.62	0.02	0.16	5.03	4.13	0.02	0.25				
MinCut	6.37	5.42	0.02	0.36	9.03	8.18	0.03	0.46	3.03	2.62	0.00	0.46
DMoN	8.10	5.14	0.04	0.27	10.11	7.34	0.04	0.37	2.77	2.59	0.00	0.48
DPR(D)	8.01	4.99	0.04	0.26	10.15	7.33	0.04	0.37	2.77	2.59	0.00	0.48
DPR(V)	8.93	5.25	0.05	0.23	10.20	7.17	0.05	0.35	2.77	2.59	0.00	0.48
DPR(E)	8.12	5.14	0.04	0.2	10.31	7.14	0.05	0.35	2.77	2.59	0.00	0.48
DPR(DV)	8.12	4.80	0.04	0.26	10.26	7.26	0.05	0.35	2.77	2.59	0.00	0.48
DPR(DE)	8.03	4.88	0.04	0.26	10.35	7.23	0.05	0.35	2.78	2.60	0.00	0.48
DPR(VE)	8.93	5.25	0.05	0.23	10.39	7.12	0.05	0.34	2.77	2.59	0.00	0.48
DPR(DVE)	8.13	4.81	0.04	0.26	10.43	7.07	0.05	0.33	2.78	2.60	0.00	0.48

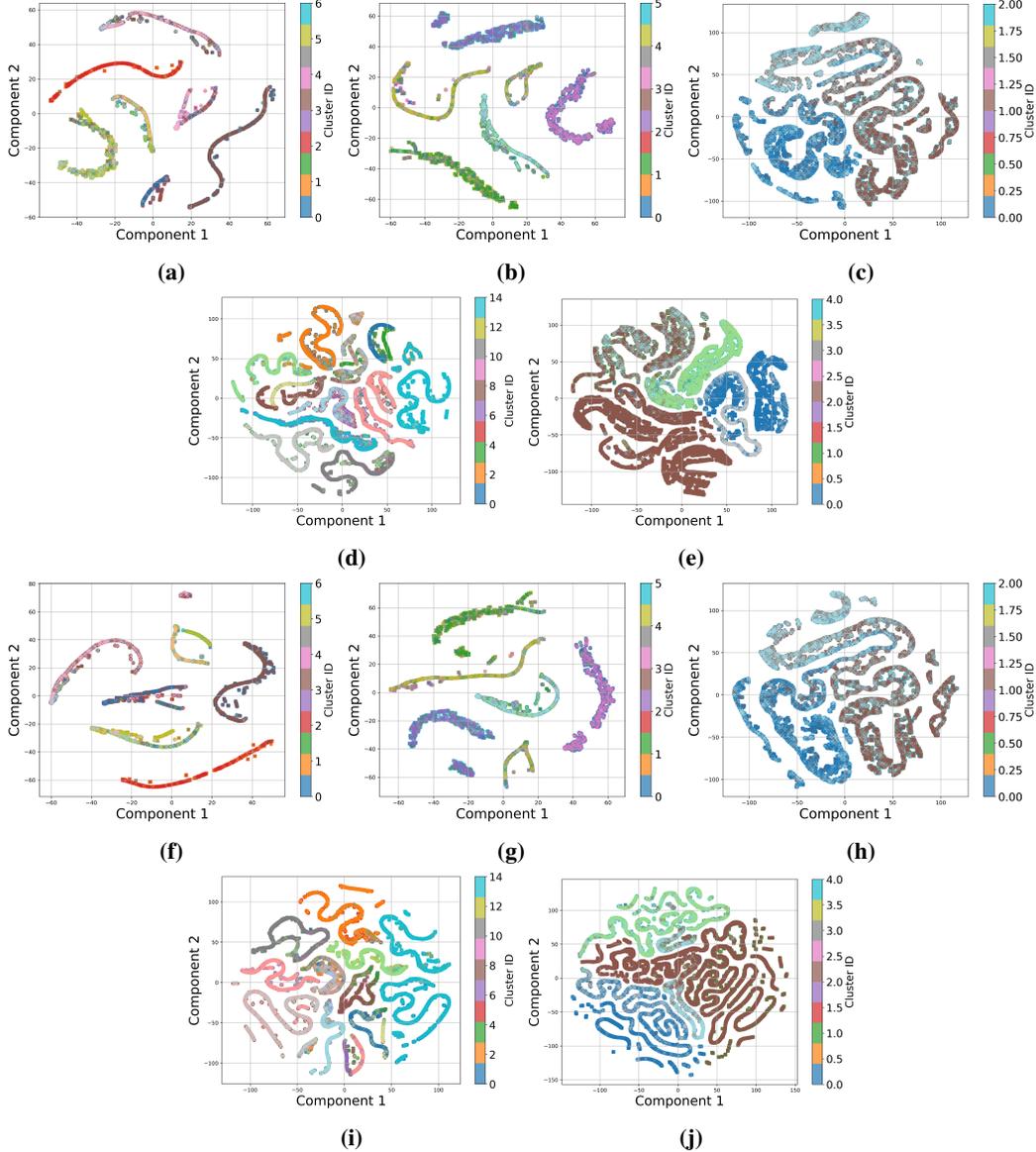
**Table 7:** Comparison of diversity resulted from the clustering methods on two datasets (Coauthor CS, Coauthor Physics). AICD is average inter-centroid distance, MICD is minimum inter-centroid distance, AICV is average intra-cluster variance, and Sil is the Silhouette score.

Method	Coauthor CS				Coauthor Physics			
	AICD	MICD	AICV	Sil	AICD	MICD	AICV	Sil
DiffPool	6.05	2.93	0.03	0.12	4.35	2.14	0.01	0.23
MinCut	10.46	6.89	0.06	0.27	10.88	8.56	0.04	0.42
DMoN	20.47	8.15	0.26	0.17	13.97	10.51	0.09	0.37
DPR(D)	17.72	7.01	0.19	0.18	14.55	7.27	0.11	0.23
DPR(V)	21.02	8.33	0.27	0.17	17.44	9.79	0.16	0.27
DPR(E)	31.67	11.14	0.58	0.15	14.72	7.46	0.11	0.25
DPR(DV)	18.16	6.94	0.20	0.17	14.72	7.46	0.11	0.25
DPR(DE)	24.48	9.38	0.37	0.19	14.58	7.66	0.11	0.25
DPR(VE)	31.75	11.17	0.59	0.15	19.16	11.15	0.19	0.29
DPR(DVE)	24.66	9.79	0.36	0.18	14.31	7.73	0.11	0.26

The diversity diagnostics in Tables 6–7 echo the accuracy gains: augmenting DMoN with our diversity-preserving regularizers widens the geometric spread of clusters—captured by the average inter-centroid distance (AICD) and minimum inter-centroid distance (MICD)—while largely preserving internal cohesion, as indicated by the near-constant average intra-cluster variance (AICV) and Silhouette score (Sil). On the citation graphs, most DPR variants leave AICD and MICD within a few percent of the DMoN baseline (the largest jump is  $\approx 10\%$  on Cora for V/VE), while AICV and Silhouette score remain virtually unchanged, confirming that clusters are not overstretched when the feature signal is weak. The feature-rich Coauthor graphs display a stronger effect: the entropy-weighted VE model, for example, boosts AICD on Coauthor CS from 20.5 to 31.8 and MICD from 8.2 to 11.2—at the cost of higher AICV—while hybrids that include the distance term (DE, DVE) achieve a better trade-off, enlarging centroid spacing by 15 – 25% but capping the rise in AICV so that Silhouette score stays on par with, or slightly above, the DMoN baseline. The sole exception is Coauthor Physics, where Silhouette score dips because DPR variants both push centroids outward and allow somewhat broader clusters; this reduces compactness even as separation improves. Overall, DPR regularization fulfills its design goal: clusters become globally more dispersed yet remain locally cohesive, yielding modest benefits on low-feature graphs and pronounced gains when node attributes are rich and heterogeneous. Note that AICV measures embedding variance within clusters, whereas our V term maximizes assignment variance across nodes; any changes in AICV under V are therefore indirect.

## C Visualization of Clusters

The clustering results visualized in Figure 1, obtained using t-SNE with a fixed perplexity (30) and learning rate (200), demonstrate that DMoN–DPR generally outperforms DMoN across the benchmark datasets Cora, CiteSeer, PubMed, Coauthor CS, and Coauthor Physics. For Cora and CiteSeer datasets, DMoN–DPR produces tighter, more well-separated clusters with improved alignment to the ground truth labels, contrasting with the more scattered and less defined clusters formed by DMoN. On the other hand, PubMed remains challenging for both methods, resulting in notable overlap and scattered clusters; yet, DMoN–DPR still provides slightly tighter groupings. Turning to the Coauthor CS and Coauthor Physics datasets, a similar trend emerges. While DMoN adequately captures overarching modular structures, it can occasionally struggle to separate nuanced subgroups. In contrast, DMoN–DPR consistently yields more cohesive and better-separated clusters, offering clearer decision boundaries and higher alignment with the true labels. This improvement is particularly notable in Coauthor CS, where DMoN–DPR visibly reduces overlap and sharpens cluster delineations. These findings underscore the effectiveness of promoting diversity within hidden representations, as DMoN–DPR not only excels in forming compact and accurate clusters for datasets with greater feature variability but also remains competitive on more challenging datasets.



**Figure 1:** Visualization of clusters (circles) vs. ground truth labels (crosses) formed by DMoN on (a) Cora, (b) CiteSeer, (c) PubMed, (d) Coauthor CS, and (e) Coauthor Physics, and by DMoN-DPR on (f) Cora, (g) CiteSeer, (h) PubMed, (i) Coauthor CS, and (j) Coauthor Physics datasets.

## D Ablation Study

### D.1 Hyperparameter Tuning

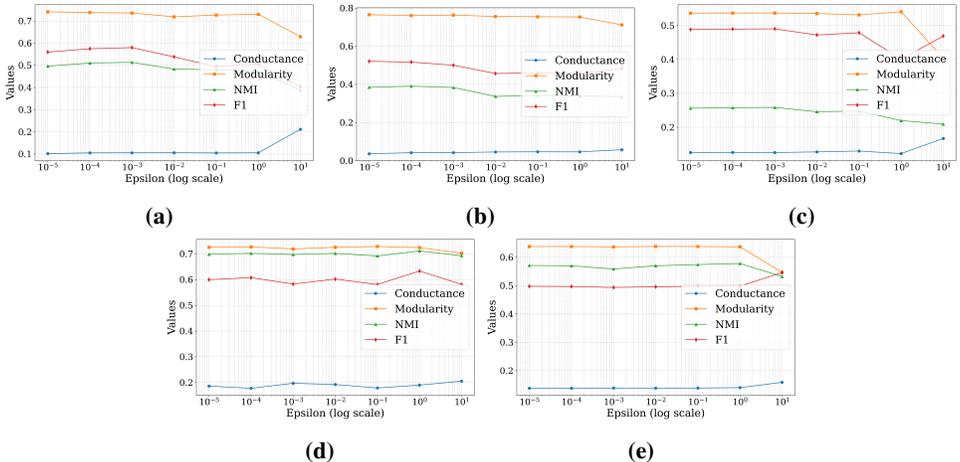
**DiffPool and MinCut** For DiffPool, the entropy weight was set to  $1 \times 10^{-5}$  on the Coauthor Physics dataset to achieve optimal performance, and to  $1 \times 10^{-4}$  for all other datasets. For MinCut pooling, both the mincut loss and orthogonality loss weights were set to 1, which consistently yielded the best results.

**DMoN-DPR** The weighting coefficients  $W_{\text{dist}}$ ,  $W_{\text{entropy}}$ , and  $W_{\text{var}}$ , as well as  $\epsilon$  are hyperparameters that need to be tuned based on the specific dataset and desired clustering behavior. They control the trade-off between structural modularity and diversity preservation. To optimize these hyperparameters, we conducted evaluations on the Cora, CiteSeer, PubMed, Coauthor CS and Coauthor Physics datasets using 10 random seeds, similar to how it was done in (Tsitsulin et al., 2023), selected

using a random number generator. The seeds that resulted in the best performance when using the DMoN pooling layer were selected. For each dataset, we tuned  $\epsilon$  (for the distance weight  $W_{\text{dist}}$ ),  $W_{\text{var}}$  (variance weight), and  $W_{\text{entropy}}$  (entropy weight) independently. To find the best  $\epsilon$ , the variance and entropy weights were set to zero, and  $\epsilon$  was varied from 10 to  $10^{-5}$ . Similarly,  $W_{\text{var}}$  and  $W_{\text{entropy}}$  were tuned by fixing the other weights to zero and varying them across  $\{1, 0.1, 0.01, 0.001\}$ . The best weights identified were used to construct various DMoN-DPR models, including DMoN (baseline), DMoN-DPR(D) (distance), DMoN-DPR(V) (variance), DMoN-DPR(E) (entropy), and combinations: DMoN-DPR(DV) (distance and variance), DMoN-DPR(DE) (distance and entropy), DMoN-DPR(VE) (variance and entropy), and DMoN-DPR(DVE) (distance, variance, and entropy). This systematic approach allowed us to assess the impact of each regularization term and their combinations on model performance. The ablation study is presented in the following subsections.

### D.1.1 Varying the Epsilon

Figure 2 depicts the ablation study done to find the best value of  $\epsilon$  associated with  $W_{\text{dist}}$  by setting  $W_{\text{var}}$  and  $W_{\text{entropy}}$  weights to 0. For the Cora, CiteSeer, PubMed, Coauthor CS, and Coauthor Physics datasets, the best  $\epsilon$  values were found to be 0.0001, 0.0001, 0.001, 1.0, and 10.0 respectively.



**Figure 2:** Finding the best value of epsilon ( $\epsilon$ ) by setting  $W_{\text{dist}}$  to 1 and  $W_{\text{var}}$  and  $W_{\text{entropy}}$  to zero on the (a) Cora, (b) CiteSeer, (c) PubMed, (d) Coauthor CS, and (e) Coauthor Physics datasets.

### D.1.2 Varying the Variance Weight

Figure 3 depicts the ablation study done to find the best value of  $W_{\text{var}}$  by setting  $W_{\text{dist}}$  and  $W_{\text{entropy}}$  weights to 0. For the Cora, CiteSeer, PubMed, Coauthor CS, and Coauthor Physics datasets, the best  $W_{\text{var}}$  values were found to be 1/0.1, 0.1, 0.001, 0.1, and 1.0 respectively.

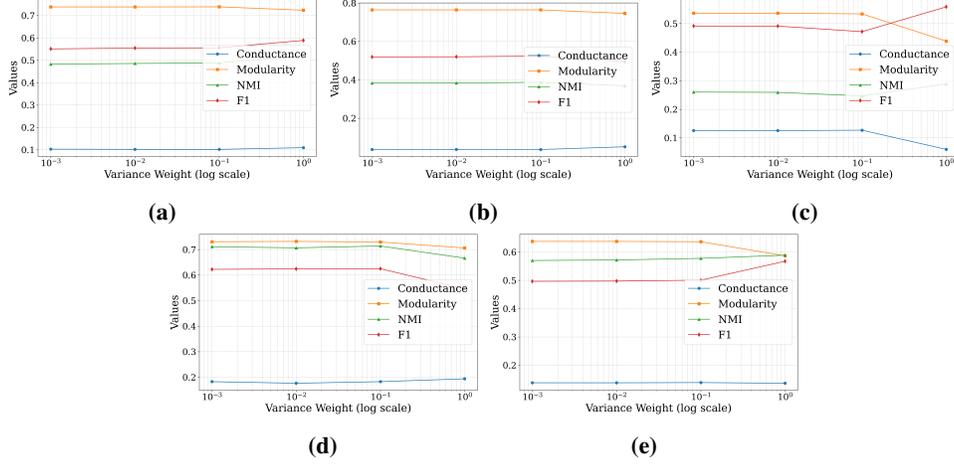
### D.1.3 Varying the Entropy Weight

Figure 4 depicts the ablation study done to find the best value of  $W_{\text{entropy}}$  by setting  $W_{\text{dist}}$  and  $W_{\text{var}}$  weights to 0. For the Cora, CiteSeer, PubMed, Coauthor CS, and Coauthor Physics datasets, the best  $W_{\text{entropy}}$  values were found to be 0.001, 0.01, 0.001, 0.1 and 0.1 respectively.

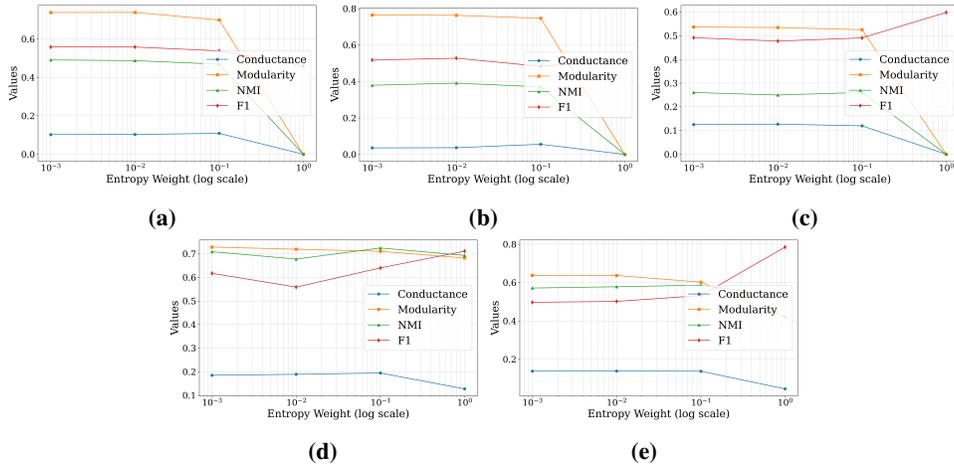
### D.1.4 Practical Challenges Regarding Manual Tuning

We acknowledge that adding diversity-preserving regularizers introduces more hyperparameters, which can complicate practical adoption. However, in our experiments:

- We found that larger coefficients for distance ( $R\_D = 1$  or  $10$ ) were typically beneficial on highly feature-rich datasets (Coauthor CS, Coauthor Physics).
- Coefficients of 1 to 0.1 for variance ( $R\_V$ ) often worked well across most datasets.
- For the entropy term, 0.1 was a good upper bound on large feature spaces, whereas a smaller coefficient was better on less feature-rich datasets.



**Figure 3:** Finding the best value of  $W_{\text{var}}$  by setting  $W_{\text{dist}}$  and  $W_{\text{entropy}}$  to zero on the (a) Cora, (b) CiteSeer, (c) PubMed, (d) Coauthor CS, and (e) Coauthor Physics datasets.



**Figure 4:** Finding the best value of  $W_{\text{entropy}}$  by setting  $W_{\text{dist}}$  and  $W_{\text{var}}$  to zero on the (a) Cora, (b) CiteSeer, (c) PubMed, (d) Coauthor CS, and (e) Coauthor Physics datasets.

From these observations, we hypothesize that stronger diversity coefficients are advantageous for richer feature spaces, whereas smaller coefficients are sufficient (and sometimes necessary) for lower-dimensional or simpler datasets. As a direction for future work, we suggest exploring automated or adaptive tuning schemes. Such an approach could dynamically adjust the weight of each regularizer during training, further reducing manual overhead and improving reproducibility.

## E Full Results

The tables below are indicative of the value of each evaluation metric obtained using DMoN/DMoN-DPR pooling for each individual seed for different datasets. The seeds were selected at random using a random number generator. The numbers are all in percentage (%).

### E.1 Cora

The following tables list the performance of DiffPool, MinCut Pool, DMoN and different DMoN-DPR configurations across different seeds on the Cora dataset.

**Table 8:** Results obtained by using DiffPool on the Cora dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DiffPool	15.90	63.81	42.06	51.72
550	DiffPool	18.74	61.16	35.22	36.23
243	DiffPool	15.84	64.02	40.57	49.64
16	DiffPool	17.07	57.90	37.43	46.73
716	DiffPool	15.33	64.34	46.69	53.05
383	DiffPool	15.54	63.93	39.65	44.05
277	DiffPool	12.83	67.00	47.31	55.25
274	DiffPool	16.31	63.31	36.01	39.97
188	DiffPool	18.26	56.66	31.67	35.33
796	DiffPool	14.08	65.66	44.65	53.50
<b>Mean <math>\pm</math> Std</b>		15.99 $\pm$ 1.77	62.78 $\pm$ 3.28	40.13 $\pm$ 5.15	46.55 $\pm$ 7.34

**Table 9:** Results obtained by using MinCut pooling on the Cora dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	MinCut	12.73	72.59	41.66	43.90
550	MinCut	11.61	73.70	45.63	45.03
243	MinCut	13.89	71.56	31.48	33.71
16	MinCut	14.08	71.37	38.06	37.21
716	MinCut	14.38	71.14	33.82	40.37
383	MinCut	15.18	70.36	29.04	28.48
277	MinCut	13.09	72.42	42.81	46.15
274	MinCut	13.32	72.16	39.60	39.77
188	MinCut	13.81	71.65	40.52	44.13
796	MinCut	14.44	70.91	34.75	32.71
<b>Mean <math>\pm</math> Std</b>		13.65 $\pm$ 1.01	71.79 $\pm$ 0.96	37.74 $\pm$ 5.31	39.15 $\pm$ 5.98

**Table 10:** Results obtained by using DMoN pooling on the Cora dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (DVE)	11.35	71.32	48.90	52.56
550	DMoN-DPR (DVE)	9.81	72.13	38.15	42.84
243	DMoN-DPR (DVE)	10.72	73.08	40.71	40.03
16	DMoN-DPR (DVE)	11.06	71.48	42.84	46.41
716	DMoN-DPR (DVE)	9.93	72.55	42.77	44.43
383	DMoN-DPR (DVE)	11.54	73.41	44.12	51.88
277	DMoN-DPR (DVE)	9.66	73.52	45.61	49.43
274	DMoN-DPR (DVE)	11.03	74.44	41.98	41.83
188	DMoN-DPR (DVE)	9.51	74.37	51.31	56.52
796	DMoN-DPR (DVE)	10.65	71.36	42.78	43.37
<b>Mean <math>\pm</math> Std</b>		10.53 $\pm$ 0.74	72.77 $\pm$ 1.18	43.92 $\pm$ 3.85	46.93 $\pm$ 5.42

**Table 11:** Results obtained by using DMoN-DPR pooling, using the best epsilon value of 0.0001, and distance weight of 1 on the Cora dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (D)	11.31	71.37	49.62	53.10
550	DMoN-DPR (D)	9.76	72.28	40.96	45.72
243	DMoN-DPR (D)	10.40	74.23	43.14	44.89
16	DMoN-DPR (D)	11.90	71.00	42.22	44.14
716	DMoN-DPR (D)	9.62	71.51	43.06	46.72
383	DMoN-DPR (D)	11.24	72.86	43.27	51.09
277	DMoN-DPR (D)	13.64	69.81	40.51	44.53
274	DMoN-DPR (D)	11.12	73.24	43.58	45.78
188	DMoN-DPR (D)	9.80	74.15	50.89	56.19
796	DMoN-DPR (D)	10.70	71.52	42.57	42.95
<b>Mean <math>\pm</math> Std</b>		10.95 $\pm$ 1.21	72.20 $\pm$ 1.42	43.98 $\pm$ 3.46	47.51 $\pm$ 4.40

**Table 12:** Results obtained by using DMoN-DPR pooling, using the best variance weight of 1 on the Cora dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (V)	11.25	70.12	48.19	52.60
550	DMoN-DPR (V)	10.95	70.66	39.21	43.64
243	DMoN-DPR (V)	11.63	71.41	40.33	39.36
16	DMoN-DPR (V)	11.25	70.02	43.27	45.92
716	DMoN-DPR (V)	11.22	70.58	43.18	45.43
383	DMoN-DPR (V)	13.40	70.06	42.14	51.60
277	DMoN-DPR (V)	11.33	69.87	41.46	45.44
274	DMoN-DPR (V)	12.43	72.57	45.58	44.85
188	DMoN-DPR (V)	12.83	70.46	46.59	51.89
796	DMoN-DPR (V)	12.37	69.61	43.49	43.14
<b>Mean <math>\pm</math> Std</b>		11.87 $\pm$ 0.83	70.54 $\pm$ 0.88	43.34 $\pm$ 2.79	46.39 $\pm$ 4.32

**Table 13:** Results obtained by using DMoN-DPR pooling, using the best entropy weight of 0.001 on the Cora dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (E)	11.20	71.38	48.47	52.36
550	DMoN-DPR (E)	9.91	72.05	38.08	42.93
243	DMoN-DPR (E)	10.57	73.23	40.85	39.97
16	DMoN-DPR (E)	11.06	71.47	42.93	46.56
716	DMoN-DPR (E)	9.89	72.54	42.62	44.72
383	DMoN-DPR (E)	11.42	73.51	44.30	51.74
277	DMoN-DPR (E)	9.55	73.52	45.49	49.53
274	DMoN-DPR (E)	11.08	74.33	43.10	42.42
188	DMoN-DPR (E)	9.61	74.26	51.24	56.67
796	DMoN-DPR (E)	10.63	71.45	42.93	43.32
<b>Mean <math>\pm</math> Std</b>		10.49 $\pm$ 0.70	72.77 $\pm$ 1.15	44.00 $\pm$ 3.72	47.02 $\pm$ 5.34

**Table 14:** Results obtained by using DMoN-DPR pooling, using the best epsilon value of 0.0001, distance weight of 1, and variance weight of 0.1 on the Cora dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (DV)	10.93	71.05	49.87	53.66
550	DMoN-DPR (DV)	9.51	72.33	41.04	45.65
243	DMoN-DPR (DV)	10.84	73.28	42.18	42.58
16	DMoN-DPR (DV)	10.86	71.23	43.08	44.77
716	DMoN-DPR (DV)	9.61	71.39	44.18	47.59
383	DMoN-DPR (DV)	11.80	73.16	43.66	46.75
277	DMoN-DPR (DV)	13.74	69.61	40.23	44.66
274	DMoN-DPR (DV)	11.33	73.29	45.41	47.47
188	DMoN-DPR (DV)	9.61	74.03	51.32	56.96
796	DMoN-DPR (DV)	10.72	71.30	43.02	43.54
<b>Mean <math>\pm</math> Std</b>		10.89 $\pm$ 1.26	72.07 $\pm$ 1.37	44.40 $\pm$ 3.60	47.36 $\pm$ 4.55

**Table 15:** Results obtained by using DMoN-DPR pooling, using the best epsilon value of 0.0001, distance weight of 1, and entropy weight of 0.001 on the Cora dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (DE)	11.16	71.38	49.75	53.29
550	DMoN-DPR (DE)	9.68	72.33	40.85	45.67
243	DMoN-DPR (DE)	10.08	74.45	43.94	46.11
16	DMoN-DPR (DE)	11.29	71.57	43.55	43.97
716	DMoN-DPR (DE)	9.61	71.58	44.19	47.71
383	DMoN-DPR (DE)	11.73	73.06	42.66	48.52
277	DMoN-DPR (DE)	13.58	69.91	40.43	44.48
274	DMoN-DPR (DE)	11.01	73.29	43.61	45.77
188	DMoN-DPR (DE)	9.81	74.04	51.34	56.67
796	DMoN-DPR (DE)	10.82	71.36	42.67	43.10
<b>Mean <math>\pm</math> Std</b>		10.88 $\pm$ 1.21	72.30 $\pm$ 1.40	44.30 $\pm$ 3.54	47.53 $\pm$ 4.32

**Table 16:** Results obtained by using DMoN-DPR pooling, using the best variance weight of 1, and entropy weight of 0.001 on the Cora dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (VE)	11.16	70.08	48.03	52.85
550	DMoN-DPR (VE)	10.86	70.77	39.39	43.76
243	DMoN-DPR (VE)	11.78	71.27	40.17	39.23
16	DMoN-DPR (VE)	11.29	69.93	43.33	45.86
716	DMoN-DPR (VE)	11.10	70.70	43.42	45.66
383	DMoN-DPR (VE)	13.17	70.14	41.54	51.22
277	DMoN-DPR (VE)	11.46	69.60	41.28	45.35
274	DMoN-DPR (VE)	12.43	72.56	45.66	44.94
188	DMoN-DPR (VE)	12.90	70.39	46.46	51.76
796	DMoN-DPR (VE)	12.41	69.61	43.10	42.98
<b>Mean <math>\pm</math> Std</b>		11.86 $\pm$ 0.82	70.50 $\pm$ 0.89	43.24 $\pm$ 2.79	46.36 $\pm$ 4.32

**Table 17:** Results obtained by using DMoN–DPR pooling, using the best epsilon value of 0.0001, variance weight of 0.1, and entropy weight of 0.001 on the Cora dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR (DVE)	10.65	71.20	49.95	53.90
550	DMoN–DPR (DVE)	9.51	72.33	41.04	45.64
243	DMoN–DPR (DVE)	10.86	73.34	41.92	42.43
16	DMoN–DPR (DVE)	10.78	71.29	42.83	44.73
716	DMoN–DPR (DVE)	9.74	71.30	43.98	47.36
383	DMoN–DPR (DVE)	12.58	72.50	42.83	45.78
277	DMoN–DPR (DVE)	13.81	69.51	40.61	45.21
274	DMoN–DPR (DVE)	10.97	73.71	46.42	47.92
188	DMoN–DPR (DVE)	9.64	73.99	51.33	56.97
796	DMoN–DPR (DVE)	10.80	71.35	42.74	43.29
<b>Mean ± Std</b>		10.93 ± 1.34	72.05 ± 1.39	44.37 ± 3.69	47.32 ± 4.63

## E.2 CiteSeer

The following tables list the performance of DiffPool, MinCut pooling, DMoN and different DMoN–DPR configurations across different seeds on the CiteSeer dataset.

**Table 18:** Results obtained by using DiffPool pooling on the CiteSeer dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DiffPool	8.24	64.76	33.99	48.98
550	DiffPool	7.27	70.84	38.27	51.01
243	DiffPool	6.59	66.78	34.97	51.19
16	DiffPool	10.43	68.61	34.15	47.16
716	DiffPool	7.01	70.87	33.12	46.30
383	DiffPool	9.49	56.09	28.78	45.91
277	DiffPool	9.58	64.40	29.61	41.80
274	DiffPool	6.50	71.68	32.23	44.80
188	DiffPool	7.18	66.15	32.83	48.86
796	DiffPool	6.94	66.72	36.02	52.33
<b>Mean ± Std</b>		7.92 ± 1.42	66.69 ± 4.53	33.40 ± 2.82	47.83 ± 3.27

**Table 19:** Results obtained by using MinCut pooling on the CiteSeer dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	MinCut	5.45	76.59	33.17	45.03
550	MinCut	5.34	75.36	24.92	35.92
243	MinCut	5.01	76.67	30.26	42.82
16	MinCut	7.21	73.20	18.09	26.08
716	MinCut	7.01	74.82	22.11	30.09
383	MinCut	6.04	75.25	23.28	34.72
277	MinCut	7.05	73.86	17.40	25.14
274	MinCut	5.32	76.16	25.47	38.90
188	MinCut	6.44	75.23	32.94	42.54
796	MinCut	7.05	74.93	24.43	31.51
<b>Mean ± Std</b>		6.19 ± 0.86	75.21 ± 1.11	25.21 ± 5.52	35.28 ± 7.05

**Table 20:** Results obtained by using DMoN pooling on the CiteSeer dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN	6.81	74.92	20.78	26.09
550	DMoN	4.11	75.53	26.91	42.64
243	DMoN	4.28	75.57	32.12	45.74
16	DMoN	4.64	77.22	33.11	44.56
716	DMoN	4.53	76.24	36.95	50.12
383	DMoN	4.24	75.55	33.25	47.00
277	DMoN	4.26	75.63	29.25	42.33
274	DMoN	4.48	75.77	30.83	45.65
188	DMoN	6.17	72.74	24.52	36.01
796	DMoN	5.12	75.34	28.98	44.42
<b>Mean <math>\pm</math> Std</b>		4.86 $\pm$ 0.91	75.45 $\pm$ 1.13	29.67 $\pm$ 4.70	42.46 $\pm$ 6.82

**Table 21:** Results obtained by using DMoN-DPR pooling using the best epsilon value of 0.0001, and distance weight of 1 on the CiteSeer dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (D)	7.18	74.27	23.90	27.73
550	DMoN-DPR (D)	4.22	75.80	26.23	41.98
243	DMoN-DPR (D)	3.82	76.02	35.91	50.13
16	DMoN-DPR (D)	4.83	76.31	32.78	44.47
716	DMoN-DPR (D)	4.57	76.13	36.99	50.14
383	DMoN-DPR (D)	4.81	75.97	33.02	45.96
277	DMoN-DPR (D)	3.87	75.75	29.37	42.34
274	DMoN-DPR (D)	4.15	76.06	30.88	45.48
188	DMoN-DPR (D)	6.37	73.98	25.00	36.47
796	DMoN-DPR (D)	5.71	75.26	26.83	39.93
<b>Mean <math>\pm</math> Std</b>		4.95 $\pm$ 1.12	75.55 $\pm$ 0.81	30.09 $\pm$ 4.57	42.46 $\pm$ 6.69

**Table 22:** Results obtained by using DMoN-DPR pooling using the best variance weight of 0.1 on the CiteSeer dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (V)	6.83	74.31	21.24	28.03
550	DMoN-DPR (V)	4.04	75.60	26.97	42.75
243	DMoN-DPR (V)	4.28	75.41	32.23	45.77
16	DMoN-DPR (V)	5.14	76.33	34.01	46.10
716	DMoN-DPR (V)	4.57	76.13	36.89	50.11
383	DMoN-DPR (V)	4.15	75.38	33.48	47.59
277	DMoN-DPR (V)	4.35	75.42	28.95	42.12
274	DMoN-DPR (V)	4.59	75.13	30.92	46.21
188	DMoN-DPR (V)	6.39	73.03	24.67	35.88
796	DMoN-DPR (V)	5.21	74.93	28.27	43.93
<b>Mean <math>\pm</math> Std</b>		4.96 $\pm$ 0.96	75.17 $\pm$ 0.94	29.76 $\pm$ 4.71	42.85 $\pm$ 6.46

**Table 23:** Results obtained by using DMoN-DPR pooling using the best entropy weight of 0.01 on the CiteSeer dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (E)	7.27	73.95	21.36	28.28
550	DMoN-DPR (E)	4.15	75.67	26.79	42.59
243	DMoN-DPR (E)	4.31	75.39	32.27	45.75
16	DMoN-DPR (E)	4.92	76.51	34.13	46.04
716	DMoN-DPR (E)	4.48	76.00	37.03	50.46
383	DMoN-DPR (E)	4.46	75.36	32.82	46.38
277	DMoN-DPR (E)	4.20	75.58	29.78	43.08
274	DMoN-DPR (E)	4.26	75.81	31.63	46.59
188	DMoN-DPR (E)	6.22	73.30	25.10	36.09
796	DMoN-DPR (E)	5.07	74.98	28.59	44.38
<b>Mean <math>\pm</math> Std</b>		4.93 $\pm$ 1.03	75.25 $\pm$ 0.96	29.95 $\pm$ 4.63	42.96 $\pm$ 6.35

**Table 24:** Results obtained by using DMoN-DPR pooling using the best epsilon value of 0.0001, distance weight of 1, and variance weight of 0.1 on the CiteSeer dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR	7.54	73.39	23.91	29.07
550	DMoN-DPR	4.35	75.62	26.61	42.29
243	DMoN-DPR	3.84	75.78	36.17	50.51
16	DMoN-DPR	4.86	76.09	33.03	44.97
716	DMoN-DPR	4.55	76.03	38.13	51.55
383	DMoN-DPR	4.90	75.53	33.12	46.09
277	DMoN-DPR	4.06	75.33	29.89	42.79
274	DMoN-DPR	4.28	75.82	31.51	46.34
188	DMoN-DPR	6.50	73.71	25.38	36.63
796	DMoN-DPR	6.04	74.53	27.25	42.22
<b>Mean <math>\pm</math> Std</b>		5.09 $\pm$ 1.21	75.18 $\pm$ 0.97	30.50 $\pm$ 4.72	43.25 $\pm$ 6.58

**Table 25:** Results obtained by using DMoN-DPR pooling using the best epsilon value of 0.0001, distance weight of 1, and entropy weight of 0.01 on the CiteSeer dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (DE)	7.45	73.34	24.03	29.50
550	DMoN-DPR (DE)	4.37	75.63	26.92	42.46
243	DMoN-DPR (DE)	3.89	75.81	36.33	50.53
16	DMoN-DPR (DE)	5.07	75.80	32.09	43.42
716	DMoN-DPR (DE)	4.33	75.97	38.51	52.05
383	DMoN-DPR (DE)	4.83	75.58	32.59	45.72
277	DMoN-DPR (DE)	4.02	75.47	30.22	43.10
274	DMoN-DPR (DE)	4.35	75.80	31.50	46.10
188	DMoN-DPR (DE)	6.35	73.93	25.29	36.35
796	DMoN-DPR (DE)	6.06	74.49	27.23	42.08
<b>Mean <math>\pm</math> Std</b>		5.07 $\pm$ 1.17	75.18 $\pm$ 0.92	30.47 $\pm$ 4.70	43.13 $\pm$ 6.53

**Table 26:** Results obtained by using DMoN–DPR pooling using the best variance weight of 0.1, and best entropy weight of 0.01 on the CiteSeer dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR (VE)	7.51	73.51	21.85	28.66
550	DMoN–DPR (VE)	4.35	75.43	26.50	42.19
243	DMoN–DPR (VE)	4.48	75.15	32.58	46.11
16	DMoN–DPR (VE)	4.79	76.51	33.09	45.03
716	DMoN–DPR (VE)	4.50	75.95	37.46	51.15
383	DMoN–DPR (VE)	4.61	74.94	33.20	46.98
277	DMoN–DPR (VE)	4.24	75.33	30.08	43.40
274	DMoN–DPR (VE)	4.37	75.69	31.72	46.90
188	DMoN–DPR (VE)	6.39	72.92	25.40	36.39
796	DMoN–DPR (VE)	5.23	74.71	29.84	45.84
<b>Mean ± Std</b>		5.05 ± 1.07	75.01 ± 1.09	30.17 ± 4.53	43.27 ± 6.40

**Table 27:** Results obtained by using DMoN–DPR pooling using the best epsilon value of 0.0001, distance weight of 1, variance weight of 0.1, and entropy weight of 0.01 on the CiteSeer dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR	7.45	73.17	23.84	29.48
550	DMoN–DPR	4.15	75.58	26.66	42.48
243	DMoN–DPR	3.91	75.68	36.30	50.67
16	DMoN–DPR	5.23	75.44	31.58	42.92
716	DMoN–DPR	4.59	75.96	37.14	50.08
383	DMoN–DPR	4.75	75.43	32.95	45.93
277	DMoN–DPR	4.44	75.10	29.34	41.94
274	DMoN–DPR	4.35	75.91	31.30	46.10
188	DMoN–DPR	6.52	73.57	26.09	37.49
796	DMoN–DPR	6.24	74.21	27.32	42.91
<b>Mean ± Std</b>		5.16 ± 1.18	75.01 ± 1.00	30.25 ± 4.41	43.00 ± 6.16

### E.3 PubMed

The following tables list the performance of MinCut pooling, DMoN and different DMoN–DPR configurations across different seeds on the PubMed dataset.

**Table 28:** Results obtained by using MinCut pooling on the PubMed dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	MinCut	12.82	53.38	23.17	41.29
550	MinCut	8.41	56.48	21.15	44.79
243	MinCut	12.52	53.77	23.64	40.72
16	MinCut	12.60	53.65	23.65	39.98
716	MinCut	10.43	55.36	21.44	37.44
383	MinCut	12.62	53.67	23.85	41.18
277	MinCut	8.32	56.56	20.47	44.08
274	MinCut	8.33	56.46	20.25	44.46
188	MinCut	12.52	53.76	23.34	38.89
796	MinCut	12.79	53.53	23.84	40.30
<b>Mean ± Std</b>		11.14 ± 2.04	54.66 ± 1.38	22.48 ± 1.47	41.31 ± 2.44

**Table 29:** Results obtained by using DMoN pooling on the PubMed dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN	10.94	55.54	22.49	40.20
550	DMoN	7.64	58.82	26.92	49.53
243	DMoN	7.93	57.62	21.77	44.56
16	DMoN	7.96	57.63	21.74	44.37
716	DMoN	8.05	57.34	21.70	44.97
383	DMoN	9.79	56.12	22.79	37.01
277	DMoN	7.80	57.63	21.69	44.89
274	DMoN	7.90	57.45	21.60	44.80
188	DMoN	10.09	55.60	21.39	37.09
796	DMoN	7.96	57.52	21.76	44.85
<b>Mean <math>\pm</math> Std</b>		8.61 $\pm$ 1.19	57.13 $\pm$ 1.04	22.38 $\pm$ 1.65	43.23 $\pm$ 3.93

**Table 30:** Results obtained by using DMoN-DPR pooling using the best epsilon value of 0.001 and distance weight of 1 on the PubMed dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (D)	10.82	55.67	22.35	40.01
550	DMoN-DPR (D)	7.65	58.81	26.89	49.57
243	DMoN-DPR (D)	7.95	57.60	21.79	44.56
16	DMoN-DPR (D)	7.99	57.59	21.73	44.35
716	DMoN-DPR (D)	8.05	57.36	21.71	44.95
383	DMoN-DPR (D)	9.78	56.13	22.83	37.08
277	DMoN-DPR (D)	7.81	57.62	21.67	44.88
274	DMoN-DPR (D)	7.82	57.53	21.67	44.91
188	DMoN-DPR (D)	10.14	55.54	21.34	37.09
796	DMoN-DPR (D)	7.97	57.51	21.82	44.96
<b>Mean <math>\pm</math> Std</b>		8.60 $\pm$ 1.17	57.14 $\pm$ 1.03	22.38 $\pm$ 1.64	43.24 $\pm$ 3.95

**Table 31:** Results obtained by using DMoN-DPR pooling using the best variance weight of 0.001 on the PubMed dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (V)	10.94	55.54	22.54	40.25
550	DMoN-DPR (V)	7.64	58.82	26.91	49.52
243	DMoN-DPR (V)	7.94	57.61	21.76	44.54
16	DMoN-DPR (V)	7.96	57.63	21.73	44.37
716	DMoN-DPR (V)	8.05	57.34	21.70	44.97
383	DMoN-DPR (V)	9.78	56.13	22.85	37.03
277	DMoN-DPR (V)	7.80	57.63	21.69	44.89
274	DMoN-DPR (V)	7.91	57.45	21.60	44.79
188	DMoN-DPR (V)	10.09	55.60	21.38	37.07
796	DMoN-DPR (V)	7.98	57.50	21.76	44.86
<b>Mean <math>\pm</math> Std</b>		8.61 $\pm$ 1.19	57.12 $\pm$ 1.04	22.39 $\pm$ 1.65	43.23 $\pm$ 3.93

**Table 32:** Results obtained by using DMoN–DPR pooling using the best entropy weight of 0.001 on the PubMed dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR (E)	10.96	55.52	22.51	40.19
550	DMoN–DPR (E)	7.65	58.81	26.90	49.50
243	DMoN–DPR (E)	7.94	57.61	21.76	44.55
16	DMoN–DPR (E)	7.97	57.62	21.74	44.37
716	DMoN–DPR (E)	8.05	57.33	21.63	44.91
383	DMoN–DPR (E)	9.82	56.08	22.79	36.95
277	DMoN–DPR (E)	7.80	57.63	21.69	44.89
274	DMoN–DPR (E)	7.91	57.45	21.60	44.80
188	DMoN–DPR (E)	10.08	55.56	21.26	37.16
796	DMoN–DPR (E)	7.98	57.51	21.75	44.85
<b>Mean ± Std</b>		8.62 ± 1.19	57.11 ± 1.05	22.36 ± 1.66	43.22 ± 3.92

**Table 33:** Results obtained by using DMoN–DPR pooling using the best epsilon value of 0.001, distance weight of 1, and variance weight of 0.001 on the PubMed dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR (DV)	10.84	55.65	22.38	40.02
550	DMoN–DPR (DV)	7.65	58.81	26.87	49.55
243	DMoN–DPR (DV)	7.95	57.60	21.79	44.56
16	DMoN–DPR (DV)	7.99	57.59	21.74	44.37
716	DMoN–DPR (DV)	8.06	57.35	21.72	44.96
383	DMoN–DPR (DV)	9.76	56.15	22.84	37.08
277	DMoN–DPR (DV)	7.81	57.62	21.67	44.88
274	DMoN–DPR (DV)	7.82	57.53	21.67	44.91
188	DMoN–DPR (DV)	10.12	55.55	21.30	37.10
796	DMoN–DPR (DV)	7.97	57.50	21.79	44.92
<b>Mean ± Std</b>		8.60 ± 1.17	57.13 ± 1.03	22.38 ± 1.64	43.23 ± 3.95

**Table 34:** Results obtained by using DMoN–DPR pooling using the best epsilon value of 0.001, distance weight of 1, and entropy weight of 0.001 on the PubMed dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR (DE)	10.83	55.65	22.42	40.03
550	DMoN–DPR (DE)	7.65	58.80	26.87	49.55
243	DMoN–DPR (DE)	7.95	57.60	21.79	44.57
16	DMoN–DPR (DE)	8.02	57.57	21.69	44.34
716	DMoN–DPR (DE)	8.03	57.37	21.77	45.03
383	DMoN–DPR (DE)	9.81	56.10	22.81	37.07
277	DMoN–DPR (DE)	7.81	57.62	21.67	44.87
274	DMoN–DPR (DE)	7.82	57.52	21.68	44.92
188	DMoN–DPR (DE)	10.10	55.50	21.32	37.24
796	DMoN–DPR (DE)	7.98	57.50	21.79	44.92
<b>Mean ± Std</b>		8.60 ± 1.17	57.12 ± 1.04	22.38 ± 1.63	43.25 ± 3.93

**Table 35:** Results obtained by using DMoN–DPR pooling using the best variance weight of 0.001, and entropy weight of 0.001 on the PubMed dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR (VE)	10.85	55.64	22.48	40.10
550	DMoN–DPR (VE)	7.65	58.82	26.90	49.50
243	DMoN–DPR (VE)	7.94	57.61	21.76	44.54
16	DMoN–DPR (VE)	7.97	57.62	21.74	44.37
716	DMoN–DPR (VE)	8.06	57.33	21.63	44.91
383	DMoN–DPR (VE)	9.80	56.09	22.79	36.98
277	DMoN–DPR (VE)	7.80	57.63	21.68	44.88
274	DMoN–DPR (VE)	7.92	57.44	21.60	44.79
188	DMoN–DPR (VE)	10.01	55.65	21.43	37.15
796	DMoN–DPR (VE)	7.97	57.50	21.73	44.84
<b>Mean ± Std</b>		8.60 ± 1.16	57.13 ± 1.02	22.37 ± 1.65	43.21 ± 3.93

**Table 36:** Results obtained by using DMoN–DPR pooling using the best epsilon value of 0.001, distance weight of 1, variance weight of 0.001, and entropy weight of 0.001 on the PubMed dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR (DVE)	10.85	55.63	22.40	40.04
550	DMoN–DPR (DVE)	7.66	58.80	26.86	49.54
243	DMoN–DPR (DVE)	7.94	57.61	21.79	44.57
16	DMoN–DPR (DVE)	8.02	57.57	21.69	44.34
716	DMoN–DPR (DVE)	8.07	57.34	21.68	44.93
383	DMoN–DPR (DVE)	9.81	56.09	22.81	37.08
277	DMoN–DPR (DVE)	7.81	57.62	21.67	44.87
274	DMoN–DPR (DVE)	7.83	57.51	21.69	44.93
188	DMoN–DPR (DVE)	10.15	55.47	21.31	37.20
796	DMoN–DPR (DVE)	7.97	57.50	21.75	44.87
<b>Mean ± Std</b>		8.61 ± 1.18	57.11 ± 1.05	22.37 ± 1.64	43.24 ± 3.92

#### E.4 Coauthor CS

The following tables list the performance of DiffPool, MinCut pooling, DMoN and different DMoN–DPR configurations across different seeds on the Coauthor CS dataset.

**Table 37:** Results obtained by using DiffPool pooling on the Coauthor CS dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DiffPool	16.20	61.90	53.06	53.73
550	DiffPool	19.88	62.52	54.40	46.18
243	DiffPool	20.41	59.39	49.01	49.43
16	DiffPool	16.41	62.75	53.63	56.78
716	DiffPool	16.64	61.46	54.03	57.47
383	DiffPool	19.21	62.93	54.93	56.09
277	DiffPool	20.95	63.84	56.25	47.35
274	DiffPool	16.04	62.92	53.34	52.78
188	DiffPool	20.58	61.21	56.02	56.85
796	DiffPool	15.61	63.44	54.53	58.08
<b>Mean ± Std</b>		18.19 ± 2.18	62.24 ± 1.30	53.92 ± 2.02	53.47 ± 4.40

**Table 38:** Results obtained by using MinCut pooling on the Coauthor CS dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	MinCut	22.08	70.93	63.96	46.60
550	MinCut	21.02	71.89	64.48	47.58
243	MinCut	21.43	71.52	63.83	49.56
16	MinCut	21.38	71.57	63.92	49.60
716	MinCut	21.53	71.33	61.94	47.48
383	MinCut	21.26	71.68	65.02	50.28
277	MinCut	21.09	71.80	65.17	49.75
274	MinCut	21.33	71.64	65.19	49.55
188	MinCut	21.39	71.49	64.73	50.51
796	MinCut	21.05	71.92	65.03	49.13
<b>Mean ± Std</b>		21.36 ± 0.31	71.58 ± 0.29	64.33 ± 0.99	49.00 ± 1.31

**Table 39:** Results obtained by using DMoN pooling on the Coauthor CS dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN	18.28	72.47	68.53	58.97
550	DMoN	18.01	72.56	67.90	57.26
243	DMoN	18.50	72.80	70.05	59.31
16	DMoN	18.04	72.93	70.70	62.98
716	DMoN	18.23	72.24	68.54	62.21
383	DMoN	17.72	73.06	70.11	60.39
277	DMoN	20.05	72.04	66.73	54.74
274	DMoN	18.13	73.24	71.11	62.35
188	DMoN	18.49	73.22	71.11	60.66
796	DMoN	20.81	71.42	67.82	53.72
<b>Mean ± Std</b>		18.63 ± 0.99	72.60 ± 0.58	69.26 ± 1.55	59.26 ± 3.17

**Table 40:** Results obtained by using DMoN-DPR pooling using the best epsilon value of 1, and distance weight of 1 on the Coauthor CS dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (D)	19.52	71.62	70.00	60.13
550	DMoN-DPR (D)	18.63	72.19	70.76	61.55
243	DMoN-DPR (D)	19.37	71.83	69.94	60.27
16	DMoN-DPR (D)	19.14	72.53	72.67	64.33
716	DMoN-DPR (D)	18.83	72.46	70.96	62.26
383	DMoN-DPR (D)	19.05	72.16	71.26	62.23
277	DMoN-DPR (D)	18.70	72.93	72.60	63.38
274	DMoN-DPR (D)	18.46	72.51	71.16	61.65
188	DMoN-DPR (D)	19.29	71.97	71.58	61.29
796	DMoN-DPR (D)	17.94	72.77	70.78	61.08
<b>Mean ± Std</b>		18.89 ± 0.48	72.30 ± 0.42	71.17 ± 0.93	61.82 ± 1.30

**Table 41:** Results obtained by using DMoN-DPR pooling using the best variance weight of 0.1 on the Coauthor CS dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (V)	18.09	72.79	69.54	60.69
550	DMoN-DPR (V)	19.20	72.05	69.23	60.66
243	DMoN-DPR (V)	17.60	73.27	71.19	62.29
16	DMoN-DPR (V)	18.45	72.43	68.76	60.54
716	DMoN-DPR (V)	18.58	72.35	68.53	59.02
383	DMoN-DPR (V)	19.05	72.25	69.61	59.12
277	DMoN-DPR (V)	19.33	72.27	69.12	57.74
274	DMoN-DPR (V)	18.62	72.97	70.38	62.66
188	DMoN-DPR (V)	18.55	73.04	71.22	60.91
796	DMoN-DPR (V)	20.01	71.56	67.98	55.77
<b>Mean <math>\pm</math> Std</b>		18.75 $\pm$ 0.68	72.50 $\pm$ 0.52	69.56 $\pm$ 1.08	59.94 $\pm$ 2.08

**Table 42:** Results obtained by using DMoN-DPR pooling using the best entropy weight of 0.1 on the Coauthor CS dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (E)	20.73	69.18	70.29	57.08
550	DMoN-DPR (E)	19.82	71.30	70.48	57.63
243	DMoN-DPR (E)	19.35	71.39	72.46	64.00
16	DMoN-DPR (E)	18.71	71.88	73.81	66.15
716	DMoN-DPR (E)	18.77	72.20	74.36	66.49
383	DMoN-DPR (E)	19.01	71.17	70.30	60.87
277	DMoN-DPR (E)	21.91	69.36	70.12	59.57
274	DMoN-DPR (E)	19.90	71.03	72.03	60.58
188	DMoN-DPR (E)	19.49	71.84	73.02	62.90
796	DMoN-DPR (E)	20.85	69.82	68.94	58.00
<b>Mean <math>\pm</math> Std</b>		19.85 $\pm$ 1.03	70.92 $\pm$ 1.08	71.58 $\pm$ 1.81	61.33 $\pm$ 3.43

**Table 43:** Results obtained by using DMoN-DPR pooling using the best epsilon value of 1, distance weight of 1, and variance weight of 0.1 on the Coauthor CS dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (DV)	19.55	71.66	69.75	60.56
550	DMoN-DPR (DV)	18.24	72.37	71.14	61.70
243	DMoN-DPR (DV)	18.94	71.86	70.04	60.62
16	DMoN-DPR (DV)	19.75	71.81	72.52	63.87
716	DMoN-DPR (DV)	20.11	71.14	68.74	58.85
383	DMoN-DPR (DV)	19.52	71.72	69.75	60.47
277	DMoN-DPR (DV)	18.63	72.57	72.00	62.98
274	DMoN-DPR (DV)	18.68	72.21	71.43	62.77
188	DMoN-DPR (DV)	19.89	71.46	69.60	58.73
796	DMoN-DPR (DV)	18.13	72.81	72.20	62.90
<b>Mean <math>\pm</math> Std</b>		19.14 $\pm$ 0.71	71.96 $\pm$ 0.52	70.72 $\pm$ 1.30	61.35 $\pm$ 1.78

**Table 44:** Results obtained by using DMoN–DPR pooling using the best epsilon value of 1, distance weight of 1, and entropy weight of 0.1 on the Coauthor CS dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR (DE)	19.75	70.62	71.29	63.49
550	DMoN–DPR (DE)	20.49	70.46	71.58	63.84
243	DMoN–DPR (DE)	20.83	69.25	69.19	60.23
16	DMoN–DPR (DE)	19.57	70.68	70.86	62.53
716	DMoN–DPR (DE)	19.12	71.23	71.83	62.71
383	DMoN–DPR (DE)	19.22	71.16	72.81	64.86
277	DMoN–DPR (DE)	19.78	71.78	73.49	65.51
274	DMoN–DPR (DE)	19.52	70.15	70.28	61.17
188	DMoN–DPR (DE)	20.82	69.37	67.33	57.40
796	DMoN–DPR (DE)	19.00	70.96	70.94	61.83
<b>Mean ± Std</b>		19.81 ± 0.68	70.57 ± 0.80	70.96 ± 1.76	62.36 ± 2.37

**Table 45:** Results obtained by using DMoN–DPR pooling using the best variance weight of 0.1, and entropy weight of 0.1 on the Coauthor CS dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR (VE)	20.74	69.08	70.35	57.99
550	DMoN–DPR (VE)	19.85	71.25	70.50	57.59
243	DMoN–DPR (VE)	19.43	71.30	72.55	64.08
16	DMoN–DPR (VE)	18.74	71.85	73.81	66.17
716	DMoN–DPR (VE)	19.22	71.37	73.19	65.61
383	DMoN–DPR (VE)	18.65	71.43	70.49	60.75
277	DMoN–DPR (VE)	21.92	69.32	70.10	59.50
274	DMoN–DPR (VE)	19.93	70.96	71.96	60.58
188	DMoN–DPR (VE)	19.44	71.87	73.01	63.01
796	DMoN–DPR (VE)	20.99	69.70	68.72	57.97
<b>Mean ± Std</b>		19.89 ± 1.04	70.81 ± 1.04	71.47 ± 1.66	61.33 ± 3.21

**Table 46:** Results obtained by using DMoN–DPR pooling using the best epsilon value of 1, distance weight of 1, variance weight of 0.1, and entropy weight of 0.1 on the Coauthor CS dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR (DVE)	20.34	70.31	70.86	63.39
550	DMoN–DPR (DVE)	20.09	70.77	71.87	64.16
243	DMoN–DPR (DVE)	19.56	70.27	70.03	60.73
16	DMoN–DPR (DVE)	20.21	70.65	72.33	63.54
716	DMoN–DPR (DVE)	19.26	71.08	71.81	62.97
383	DMoN–DPR (DVE)	19.17	71.20	72.88	64.81
277	DMoN–DPR (DVE)	18.96	72.10	73.54	65.43
274	DMoN–DPR (DVE)	19.65	70.36	70.79	61.93
188	DMoN–DPR (DVE)	20.98	69.20	67.10	57.05
796	DMoN–DPR (DVE)	18.70	71.14	71.62	62.70
<b>Mean ± Std</b>		19.69 ± 0.71	70.71 ± 0.76	71.28 ± 1.79	62.67 ± 2.40

## E.5 Coauthor Physics

The following tables list the performance of DiffPool, MinCut pooling, DMoN and different DMoN–DPR configurations across different seeds on the Coauthor Physics dataset.

**Table 47:** Results obtained by using DiffPool pooling on the Coauthor Physics dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DiffPool	13.06	56.73	57.94	53.93
550	DiffPool	15.25	59.42	59.33	53.71
243	DiffPool	13.06	57.18	56.61	52.20
16	DiffPool	13.26	56.55	57.69	53.75
716	DiffPool	14.42	58.97	61.09	53.65
383	DiffPool	14.03	57.15	58.03	54.06
277	DiffPool	13.37	56.48	47.24	46.20
274	DiffPool	13.26	55.70	58.06	56.79
188	DiffPool	12.23	57.04	58.30	54.31
796	DiffPool	17.18	59.19	47.89	38.47
<b>Mean <math>\pm</math> Std</b>		13.91 $\pm$ 1.42	57.44 $\pm$ 1.29	56.22 $\pm$ 4.71	51.71 $\pm$ 5.38

**Table 48:** Results obtained by using MinCut pooling on the Coauthor Physics dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	MinCut	14.08	61.78	48.91	45.03
550	MinCut	14.35	61.54	56.89	51.00
243	MinCut	13.74	61.79	51.41	47.76
16	MinCut	13.38	62.16	57.19	51.39
716	MinCut	13.18	62.55	57.10	51.27
383	MinCut	13.95	62.12	48.62	42.59
277	MinCut	14.17	61.39	48.28	46.92
274	MinCut	14.20	61.31	45.80	46.44
188	MinCut	13.33	62.51	52.14	47.82
796	MinCut	14.95	60.38	47.53	47.70
<b>Mean <math>\pm</math> Std</b>		13.93 $\pm$ 0.54	61.75 $\pm$ 0.65	51.39 $\pm$ 4.30	47.79 $\pm$ 2.84

**Table 49:** Results obtained by using DMoN pooling on the Coauthor Physics dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN	12.64	59.92	44.49	46.04
550	DMoN	13.87	64.01	54.36	47.54
243	DMoN	13.89	63.77	56.67	49.51
16	DMoN	13.82	63.77	56.89	49.55
716	DMoN	13.93	63.72	55.42	49.02
383	DMoN	13.65	63.63	52.66	46.65
277	DMoN	13.48	63.85	50.84	44.74
274	DMoN	13.84	64.02	53.53	46.36
188	DMoN	13.89	63.73	55.87	49.33
796	DMoN	14.02	64.12	54.29	46.36
<b>Mean <math>\pm</math> Std</b>		13.70 $\pm$ 0.40	63.45 $\pm$ 1.25	53.50 $\pm$ 3.67	47.51 $\pm$ 1.73

**Table 50:** Results obtained by using DMoN-DPR pooling using the best epsilon value of 10, and distance weight of 1 on the Coauthor Physics dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (D)	14.00	62.17	51.59	47.84
550	DMoN-DPR (D)	19.30	56.61	50.82	46.32
243	DMoN-DPR (D)	18.21	57.77	58.61	50.55
16	DMoN-DPR (D)	16.19	54.39	53.19	55.67
716	DMoN-DPR (D)	16.93	55.94	48.09	49.54
383	DMoN-DPR (D)	19.58	55.58	52.71	46.44
277	DMoN-DPR (D)	14.97	55.73	51.49	53.53
274	DMoN-DPR (D)	15.55	56.74	59.80	55.95
188	DMoN-DPR (D)	14.85	55.96	55.95	54.65
796	DMoN-DPR (D)	14.78	58.04	52.68	49.37
<b>Mean <math>\pm</math> Std</b>		16.44 $\pm$ 1.99	56.89 $\pm$ 2.14	53.49 $\pm$ 3.61	50.99 $\pm$ 3.71

**Table 51:** Results obtained by using DMoN-DPR pooling using the best variance weight of 1 on the Coauthor Physics dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (V)	12.28	58.05	45.73	45.50
550	DMoN-DPR (V)	11.94	57.38	54.27	54.78
243	DMoN-DPR (V)	13.49	60.85	59.11	53.04
16	DMoN-DPR (V)	13.55	58.65	58.50	56.62
716	DMoN-DPR (V)	11.83	58.84	56.84	53.74
383	DMoN-DPR (V)	14.44	57.84	54.21	55.65
277	DMoN-DPR (V)	12.03	58.71	57.09	53.73
274	DMoN-DPR (V)	14.15	57.02	53.90	55.44
188	DMoN-DPR (V)	13.11	57.40	54.62	53.97
796	DMoN-DPR (V)	15.02	61.14	45.01	45.34
<b>Mean <math>\pm</math> Std</b>		13.18 $\pm$ 1.14	58.59 $\pm$ 1.41	53.93 $\pm$ 4.87	52.78 $\pm$ 4.02

**Table 52:** Results obtained by using DMoN-DPR pooling using the best entropy weight of 0.1 on the Coauthor Physics dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (E)	13.59	59.64	48.13	45.60
550	DMoN-DPR (E)	11.94	57.60	54.02	54.19
243	DMoN-DPR (E)	13.72	61.90	58.72	51.62
16	DMoN-DPR (E)	13.53	58.94	57.15	55.16
716	DMoN-DPR (E)	14.17	57.80	47.71	51.12
383	DMoN-DPR (E)	14.24	58.41	53.68	54.15
277	DMoN-DPR (E)	11.57	58.08	53.16	52.07
274	DMoN-DPR (E)	13.26	57.99	53.77	51.77
188	DMoN-DPR (E)	14.08	60.75	55.54	50.03
796	DMoN-DPR (E)	14.81	62.19	46.39	45.17
<b>Mean <math>\pm</math> Std</b>		13.49 $\pm$ 1.02	59.33 $\pm$ 1.72	52.83 $\pm$ 4.13	51.09 $\pm$ 3.39

**Table 53:** Results obtained by using DMoN-DPR pooling using the best epsilon value of 10, distance weight of 1, and variance weight 1 on the Coauthor Physics dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (DV)	15.37	55.95	48.78	53.49
550	DMoN-DPR (DV)	14.84	55.32	52.13	57.57
243	DMoN-DPR (DV)	13.82	56.19	56.71	57.69
16	DMoN-DPR (DV)	11.67	56.14	54.87	57.53
716	DMoN-DPR (DV)	10.97	57.41	62.02	61.81
383	DMoN-DPR (DV)	13.45	56.41	54.45	57.87
277	DMoN-DPR (DV)	14.25	56.26	52.86	57.93
274	DMoN-DPR (DV)	11.79	56.58	57.37	59.70
188	DMoN-DPR (DV)	14.17	56.86	60.24	58.29
796	DMoN-DPR (DV)	13.98	57.70	58.95	58.04
<b>Mean <math>\pm</math> Std</b>		13.43 $\pm$ 1.46	56.48 $\pm$ 0.70	55.84 $\pm$ 4.02	57.99 $\pm$ 2.06

**Table 54:** Results obtained by using DMoN-DPR pooling using the best epsilon value of 10, distance weight of 1, and entropy weight of 0.1 on the Coauthor Physics dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (DE)	13.94	61.00	47.60	46.37
550	DMoN-DPR (DE)	14.11	56.74	54.67	55.98
243	DMoN-DPR (DE)	13.89	57.00	60.05	58.60
16	DMoN-DPR (DE)	13.90	54.44	53.68	57.90
716	DMoN-DPR (DE)	11.35	57.47	63.18	61.39
383	DMoN-DPR (DE)	15.41	54.93	51.58	53.92
277	DMoN-DPR (DE)	15.84	54.43	51.48	57.57
274	DMoN-DPR (DE)	14.14	57.42	53.66	56.28
188	DMoN-DPR (DE)	15.33	56.20	56.80	55.88
796	DMoN-DPR (DE)	13.83	59.24	47.47	46.26
<b>Mean <math>\pm</math> Std</b>		14.17 $\pm$ 1.24	56.89 $\pm$ 2.09	54.02 $\pm$ 5.00	55.02 $\pm$ 4.99
<b>Mean</b>		14.22	56.10	54.71	56.94
<b>Variance</b>		0.01	0.01	0.16	0.10

**Table 55:** Results obtained by using DMoN-DPR pooling using the best variance weight of 1, and entropy weight of 0.1 on the Coauthor Physics dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN-DPR (VE)	8.51	36.26	14.21	44.28
550	DMoN-DPR (VE)	13.11	57.01	52.67	57.06
243	DMoN-DPR (VE)	14.40	59.91	56.09	52.22
16	DMoN-DPR (VE)	13.97	58.17	62.31	59.21
716	DMoN-DPR (VE)	13.66	58.24	53.74	53.47
383	DMoN-DPR (VE)	14.12	57.60	56.52	57.86
277	DMoN-DPR (VE)	16.66	60.87	48.23	44.09
274	DMoN-DPR (VE)	12.18	56.56	51.47	56.39
188	DMoN-DPR (VE)	11.16	56.05	56.50	60.71
796	DMoN-DPR (VE)	13.32	58.12	47.75	50.50
<b>Mean <math>\pm</math> Std</b>		13.11 $\pm$ 2.17	55.88 $\pm$ 7.04	49.95 $\pm$ 13.27	53.58 $\pm$ 5.86

**Table 56:** Results obtained by using DMoN–DPR pooling using the best epsilon value of 10, distance weight of 1, variance weight of 1, and entropy weight of 0.1 on the Coauthor Physics dataset.

Seed	Method	Conductance	Modularity	NMI	F1
993	DMoN–DPR (DVE)	14.25	57.43	42.12	46.26
550	DMoN–DPR (DVE)	14.53	55.66	53.54	57.87
243	DMoN–DPR (DVE)	12.50	55.96	54.67	59.77
16	DMoN–DPR (DVE)	13.27	54.52	51.00	57.72
716	DMoN–DPR (DVE)	12.95	54.76	54.90	58.06
383	DMoN–DPR (DVE)	12.76	55.00	56.93	60.32
277	DMoN–DPR (DVE)	14.47	54.87	52.66	59.00
274	DMoN–DPR (DVE)	12.47	55.39	58.52	61.38
188	DMoN–DPR (DVE)	11.29	57.23	62.59	62.06
796	DMoN–DPR (DVE)	9.90	53.89	48.04	57.18
<b>Mean <math>\pm</math> Std</b>		12.84 $\pm$ 1.45	55.47 $\pm$ 1.14	53.50 $\pm$ 5.67	57.96 $\pm$ 4.42

## F Implementation Details

The code was implemented by extending the DMoN implementation in PyTorch Geometric (Fey and Lenssen, 2019), and was trained and evaluated using the evaluation protocols found in the official DMoN repository (Tsitsulin et al., 2023). The experiments were run on an A100 GPU with 40GB of memory offered by Google Colab Pro. Regarding the runtime analysis results and clustering visualization, the code was run on an Apple M2 Max CPU.