Self-supervised Monocular Depth Estimation Robust to Reflective Surface Leveraged by Triplet Mining

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ABSTRACT

Self-supervised monocular depth estimation (SSMDE) aims to predict the dense depth map of a monocular image, by learning depth from RGB image sequences, eliminating the need for ground-truth depth labels. Although this approach simplifies data acquisition compared to supervised methods, it struggles with reflective surfaces, as they violate the assumptions of Lambertian reflectance, leading to inaccurate training on such surfaces. To tackle this problem, we propose a novel training strategy for an SSMDE by leveraging triplet mining to pinpoint reflective regions at the pixel level, guided by the camera geometry between different viewpoints. The proposed reflection-aware triplet mining loss specifically penalizes the inappropriate photometric error minimization on the localized reflective regions while preserving depth accuracy on non-reflective areas. We also incorporate a reflection-aware knowledge distillation method that enables a student model to selectively learn the pixel-level knowledge from reflective and non-reflective regions. This results in robust depth estimation across areas. Evaluation results on multiple datasets demonstrate that our method effectively enhances depth quality on reflective surfaces and outperforms state-of-the-art SSMDE baselines.

1 INTRODUCTION

Self-supervised monocular depth estimation (SSMDE) (Godard et al., 2019) is a task that learns depth solely from a continuous RGB image sequence without needing corresponding ground-truth depth maps for each frame in a video. This approach significantly simplifies data acquisition compared to traditional supervised methods (Fu et al., 2018; Lee et al., 2019; Bhat et al., 2021), which often involve high costs for annotation. As such, many SSMDE studies (Godard et al., 2019; Zhou et al., 2017; Garg et al., 2016; Guizilini et al., 2020) have explored its viability as a mainstay for applications such as autonomous driving, highlighting its potential in outdoor environments.

Despite its advantages, SSMDE typically challenges in accurate depth estimation on non-Lambertian surfaces such as mirrors, transparent objects, and specular surfaces. This difficulty pri-040 marily arises from the assumption of Lambertian reflectance (Basri & Jacobs, 2003) embedded in 041 most SSMDE methods. As illustrated in Figure 1, these non-Lambertian surfaces violate the pho-042 tometric constancy principle, which posits that the color and brightness of a point should appear 043 constant across different images (Godard et al., 2017). This violation leads to incorrect depth train-044 ing, particularly on non-Lambertian surfaces. Consequently, this issue manifests in a phenomenon known as the "black-hole effect" (Shi et al., 2023), where the model erroneously predicts depths that are greater than the actual surface depth in areas with specular reflections. This effect is a prevalent 046 challenge across various reflective surfaces, significantly impacting the performance and reliability 047 of SSMDE systems. 048

Recent advancements (Costanzino et al., 2023; Shi et al., 2023) attempt to tackle these challenges
by utilizing training strategies that involve generating pseudo-labels through inpainting (Costanzino
et al., 2023) or reconstructing 3D meshes (Shi et al., 2023). However, these methods still rely on extra
labels such as segmentation mask annotations (Costanzino et al., 2023) or use auxiliary methods that
have excessive computational costs such as ensemble-based uncertainty algorithms (Shi et al., 2023),
TSDF-fusion (Newcombe et al., 2011) and mesh rendering (Matl, 2019).

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Figure 1: Photometric constancy violation on reflective surfaces. The projected non-reflective surface point (denoted as ^(O)) satisfies the photometric constancy so the model can obtain the accurate depth by photometric error minimization. On the other hand, projected reflective surface point (denoted as (0,0) violates the photometric constancy, resulting in wrong disparity by photometric error minimization. This figure depicts a scenario where the relative positions of the cameras shift horizontally, akin to rectified stereo, to simplify the illustration.

To address these issues, we propose a novel training strategy called "reflection-aware triplet min-079 ing" that enhances the performance of SSMDEs by leveraging the triplet mining (Schroff et al., 2015). The underlying principle of our approach is that reflective areas, such as mirror light sources 081 or objects, exhibit disparities corresponding to the reflected object rather than the actual surface as illustrated in Figure 1. While non-reflective areas exhibit photometric error due to the difference 083 in camera views from two different perspectives (e.g., source and reference views), reflective areas 084 have abnormally low photometric error between the two views due to the low disparity of reflected 085 objects. Accordingly, our approach treats views from the same camera coordinates as positive pairs and those from different coordinates as negative pairs, as illustrated in Figure 2. Our method aims 087 to minimize the conventional photometric error between positive pairs while maximizing it between 880 negative pairs. This approach effectively neutralizes the impact of contaminated gradients in reflective regions, thereby significantly improving accuracy on these regions. 089

090 Moreover, we introduce a "reflection-aware knowledge distillation" approach to keep the high-091 frequency details in the predicted depth for non-reflective regions inspired by previous works (Shi 092 et al., 2023). In this method, the student network is trained by distilling knowledge from two distinct SSMDE networks. The first utilizes the proposed triplet loss, providing robustness against reflective 094 areas, while the second employs solely photometric minimization loss, adept at preserving highfrequency details that contribute to the perceptual quality and visual fidelity of the depth map. This 095 hybrid training strategy effectively combines the strengths of both training methods, creating a more 096 versatile and effective depth estimation framework. By leveraging the unique capabilities of each 097 model, the student network can achieve a more comprehensive understanding of depth across vari-098 ous surface conditions. 099

100 Our method is broadly applicable to general SSMDE frameworks that rely on photometric error 101 minimization. We validate our method on three well-known SSMDE networks (Godard et al., 2019; Lyu et al., 2021; Zhao et al., 2022) across three public datasets (Dai et al., 2017; Shotton et al., 102 2013; Ramirez et al., 2023) featuring reflective objects and surfaces. The results demonstrate that 103 our method significantly improves depth prediction accuracy on reflective surfaces while preserving 104 performance on non-reflective surfaces. Our main contributions are fourfold as follows: 105

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- 1. We propose a new *reflection-aware triplet mining loss* that significantly enhances the accuracy 107 on reflective surfaces and can be easily integrated into general SSMDE frameworks.

2. We introduce *reflection-aware knowledge distillation* to improve the overall accuracy on reflective surfaces while preserving high-frequency details on non-reflective surfaces.

- 3. To the best of our knowledge, our strategy represents the first end-to-end method specifically designed to enhance the performances of SSMDE on reflective surfaces.
- 4. The proposed method outperforms the existing self-supervised training method and shows comparable results against 3D information distillation methods on various indoor depth benchmarks.

116 2 RELATED WORK

118 2.1 Self-supervised monocular depth estimation

119 Self-supervised Monocular Depth Estimation (SSMDE) is a task that estimates a depth map from 120 a single image without a ground truth depth map. This approach significantly simplifies the pro-121 cess of data acquisition, making it scalable for a wide variety of datasets. SfMLearner (Zhou et al., 122 2017) introduces a pioneering framework for self-supervised depth map estimation, which simul-123 taneously learns depth maps for the input image and pose parameters from sequential views. Mon-124 odepth2 (Godard et al., 2019) proposes a masking scheme and minimum reprojection loss to filter 125 out the regions that violate photometric inconstancy, such as moving objects and occluded regions. Subsequent methods (Zhou et al., 2021; Guizilini et al., 2020; Lyu et al., 2021) have been refined, 126 127 effectively integrating features of different resolutions based on established constraints. With the introduction of ViT (Dosovitskiy et al., 2020), the field of SSMDE has begun to incorporate trans-128 former backbones. Monoformer (Bae et al., 2023b) and MonoViT (Zhao et al., 2022) have emerged, 129 utilizing hybrid networks of CNN and transformers to adeptly merge local and global features. 130

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2.2 GENERALIZATION OF MONOCULAR DEPTH ESTIMATION

133 Recent research has expanded to consider factors such as the impact of weather variations (Saun-134 ders et al., 2023; Gasperini et al., 2023), the differences in inference capabilities between CNNs and 135 Transformers (Bae et al., 2023a), the robustness of SSMDEs against various types of data corrup-136 tion (Kong et al., 2024), and methods for accurately modeling transparent and mirrored surfaces, 137 which are typically non-Lambertian (Costanzino et al., 2023). In addition, the 3D Distillation (Shi 138 et al., 2023) addresses a critical flaw in traditional SSMDEs: the photometric constancy principle 139 used in applying photometric consistency loss may not hold for non-Lambertian surfaces encountered in real-world scenarios, resulting in SSMDE models producing unreliable and low-quality 140 depth estimates for reflective surfaces. To counter this problem, 3D Distillation leverages the 3D 141 mesh rendering function along with ensemble uncertainty to localize the reflective surfaces and re-142 fine the inaccurate depth on these regions. 143

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2.3 DEEP METRIC LEARNING

146 Deep metric learning (Chen et al., 2020; Chen & He, 2021; Khosla et al., 2020) seeks to develop an 147 effective distance measure between data points. These methods strive to minimize the distance be-148 tween samples of the same class while maximizing it between samples from different classes. While 149 traditionally focused on classification tasks, where positive and negative pairs are defined based on 150 class similarity, recent studies (Spurr et al., 2021; Wang et al., 2022; Zha et al., 2024) have expanded the application of deep metric learning to regression contexts. Particularly in the context of depth 151 estimation, deep metric learning has demonstrated versatility beyond simple augmentation-based 152 consistency. It has been applied to enhance accuracy through contrasting depth distributions (Fan 153 et al., 2023; Choi et al., 2024) and addressing issues such as edge fattening (Chen et al., 2023). In 154 this paper, we utilize the triplet mining scheme, initially popularized by Schroff et al. (2015), to en-155 hance recognition accuracy, specifically focusing on improving performance on reflective surfaces. 156

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3 Method

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160 Our method aims to enhance depth prediction accuracy on reflective surfaces by strategically penal-161 izing the inappropriate photometric error minimization between the view-synthesized image and the reference image. In Section 3.1, we discuss the photometric constancy principle, which posits that correctly minimizing photometric error is crucial for accurately determining depth (Section 3.1.1).
We also provide an overview of the standard training strategies employed in SSMDE frameworks (Section 3.1.2). In Section 3.2, we detail the three components of our training strategy: reflective region localization (Section 3.2.1), reflection-aware triplet mining loss (Section 3.2.2), and reflection-aware knowledge distillation (Section 3.2.3).

168 3.1 PRELIMINARY

170 3.1.1 PHOTOMETRIC CONSTANCY PRINCIPLE

171 The photometric constancy principle is foundational in SSMDE frameworks, positing that surfaces 172 exhibit uniform reflectance (*i.e.*, Lambertian reflectance) from all viewing angles. A surface adheres 173 to this principle if its color and luminance observed through a camera remain constant, regardless 174 of the camera's viewing angle. By leveraging this property, depth and pose can be accurately esti-175 mated by minimizing the photometric error between the view-synthesized image and the reference 176 image, as described in Equation 3. However, real-world scenes rarely adhere strictly to this principle. Non-Lambertian surfaces, such as specular reflections from light sources or mirrored objects, 177 are prevalent, leading to violations of photometric constancy. These deviations result in significant 178 errors when attempting to minimize photometric error, thus compromising the effectiveness of depth 179 estimation methods based on these assumptions. 180

3.1.2 TRAINING STRATEGY OF GENERAL SSMDE FRAMEWORK

The objective of SSMDE is to predict a per-pixel basis depth map \mathbf{D}_{ref} of a reference image \mathbf{I}_{ref} given the reference image itself, a source image \mathbf{I}_{src} (or source images) and their camera intrinsics *K*. The framework consists of a depth network $\mathcal{F}_{\theta}(\cdot)$, and a pose network $\mathcal{G}_{\phi}(\cdot, \cdot)$ to respectively estimate the depth of the reference image \mathbf{D}_{ref} , and the relative pose $[\boldsymbol{R}|\boldsymbol{t}]_{r2s}$ as follows:

$$\mathbf{D}_{ref} = \mathcal{F}_{\theta}(\mathbf{I}_{ref}), \qquad \mathcal{F}_{\theta} : \mathbb{R}^{3 \times h \times w} \to \mathbb{R}^{1 \times h \times w}, \tag{1}$$
$$\left[\mathbf{R} | \mathbf{t} \right]_{r2s} = \mathcal{G}_{\phi}(\mathbf{I}_{src}, \mathbf{I}_{ref}), \qquad \mathcal{G}_{\phi} : \mathbb{R}^{2 \times 3 \times h \times w} \to \mathbb{R}^{3 \times 4}, \tag{2}$$

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 $[\mathbf{R}|\mathbf{t}]_{r2s} = \mathcal{G}_{\phi}(\mathbf{I}_{src}, \mathbf{I}_{ref}), \quad \mathcal{G}_{\phi} : \mathbb{R}^{2 \times 3 \times h \times w} \to \mathbb{R}^{3 \times 4}, \tag{2}$ where (h, w) represent the spatial resolution of \mathbf{I}_{ref} . Using the obtained relative pose $[\mathbf{R}|\mathbf{t}]_{r2s}$, and depth map \mathbf{D}_{ref} , the source image \mathbf{I}_{src} is warped into the reference coordinates, generating the

$$(\mathbf{I}_{s2r})_{:,u,v} = \mathbf{I}_{src}(\langle \boldsymbol{K}[\boldsymbol{R}|\boldsymbol{t}]_{r2s}(\mathbf{D}_{ref})_{:,u,v}\boldsymbol{K}^{-1}[u,v,1]^T\rangle),$$
(3)

where (u, v) represent the image coordinates and $\langle \cdot \rangle$ is the projection function that maps homogeneous coordinates to cartesian coordinates. By the photometric constancy principle detailed in Section 3.1.1, the synthesized image \mathbf{I}_{s2r} should exhibit the same colors and luminances as the reference image on a pixel-by-pixel basis. Consequently, the model can determine the accurate depth and pose by minimizing the photometric errors, $\mathcal{P}(\cdot, \cdot)$, between \mathbf{I}_{s2r} and \mathbf{I}_{ref} as follows:

$$\mathcal{P}(\mathbf{I}_{s2r}, \mathbf{I}_{ref}) = \mathbf{M} \odot \left(\alpha_1 \frac{1 - \mathcal{S}(\mathbf{I}_{ref}, \mathbf{I}_{s2r})}{2} + \alpha_2 ||\mathbf{I}_{ref} - \mathbf{I}_{s2r}||_1 \right),$$

$$\mathcal{P} : \mathbb{R}^{2 \times 3 \times h \times w} \to \mathbb{R}^{1 \times h \times w}, \quad \mathcal{S} : \mathbb{R}^{2 \times 3 \times h \times w} \to \mathbb{R}^{1 \times h \times w},$$
(4)

where $S(\cdot, \cdot)$ is the mixture of structural similarity index (Wang et al., 2004), and M is the principled mask (Godard et al., 2019) to prevent the backpropagation of corrupted gradients, caused by anomalies like moving objects in the scene. The weights α_1 and α_2 serve as balance terms between two losses, and \odot represents the element-wise multiplication operator. However, if the surface does not conform to the principle of photometric constancy, minimizing photometric errors on such reflective surfaces can lead to significant inaccuracies in the estimated depth.

- 210
- 211 3.2 METHODOLOGY

212 3.2.1 REFLECTIVE REGION LOCALIZATION 213

view-synthesized image I_{s2r} as follows:

The photometric error, as calculated through Equation 4 between I_{s2r} and I_{ref} tends to be smaller in non-reflective regions. This is because these areas reflect consistent colors and luminances irrespective of the viewing direction, adhering to the photometric constancy principle. On the other

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Figure 2: The effect of the proposed method on reflective/non-reflective surfaces. ($\bigcirc/\bigcirc, \bigcirc$) imply the projected non-reflective/reflective surface points, respectively, and (⁽ⁱ⁾, ⁽ⁱ⁾) denotes the location of reflection lobe in view-synthesized image coordinate. Our proposed method cancels out the wrong photometric error minimization in reflection areas by contrasting the negative pair samples.

hand, reflective regions, which violate the photometric constancy principle, exhibit abnormally low disparities due to the additional distance from the reflected light source. Consequently, as illustrated in Figure 2, reflection lobes from different images appear relatively closer in image coordinates, resulting in reduced photometric errors in the RGB images of two different viewpoints.

239 This characteristic is crucial for isolating reflective regions within the spatial dimension of the image. 240 To capitalize on this, we first generate cross-view synthesized images I_{s2r} , I_{r2s} in a manner similar 241 to the process outlined in Equation 3: 242

$$(\mathbf{I}_{s2r})_{:,u,v} = \mathbf{I}_{src}(\langle \boldsymbol{K}[\boldsymbol{R}|\boldsymbol{t}]_{r2s}(\mathbf{D}_{ref})_{:,u,v}\boldsymbol{K}^{-1}[u,v,1]^T\rangle),$$
(5)

$$(\mathbf{I}_{r2s})_{:,u,v} = \mathbf{I}_{ref}(\langle \boldsymbol{K}[\boldsymbol{R}|\boldsymbol{t}]_{s2r}(\mathbf{D}_{src})_{:,u,v}\boldsymbol{K}^{-1}[u,v,1]^T\rangle),$$
(6)

where the relative pose $[\mathbf{R}|\mathbf{t}]_{s2r}$ can be obtained by computing the inverse of the predicted pose 246 $[\mathbf{R}|\mathbf{t}]_{s2r}$, and \mathbf{D}_{src} is predicted depth from \mathbf{I}_{src} , following a procedure similar to Equation 1. Uti-247 lizing these synthesized cross-view images, we compute two photometric errors to measure discrep-248 ancies between image pairs as follows: 249

$$\mathbf{E}^{+} = \mathcal{P}(\mathbf{I}_{s2r}, \mathbf{I}_{ref}), \quad \mathbf{E}^{-} = \mathcal{P}(\mathbf{I}_{s2r}, \mathbf{I}_{r2s}). \tag{7}$$

The first error, E^+ , quantifies discrepancies between images taken from the same viewpoint 252 $(\mathbf{I}_{s2r}, \mathbf{I}_{ref})$. This error is minimized when depth and pose are accurately estimated on non-reflective 253 surfaces. Conversely, the second error, E^- , measures discrepancies between images from differ-254 ent viewpoints (I_{s2r} , I_{r2s}). In general, the expected photometric error for E^- should be substantial 255 due to the different camera coordinate systems. However, on reflective surfaces, the variations in 256 light reflection may result in a reduced photometric error. Based on these observations, we identify 257 pixel-level reflective regions $\mathbf{M}_r \in \mathbb{R}^{1 \times h \times w}$ as follows: 258

$$(\mathbf{M}_r)_{:,u,v} = \begin{cases} 1, & \text{if } (\mathbf{E}^-)_{:,u,v} - (\mathbf{E}^+)_{:,u,v} \le \delta, \\ 0, & \text{else}, \end{cases}$$
(8)

where δ is a certain margin that represents the minimum significant photometric difference required to distinguish between the two surface types, where a value of 1 corresponds to a reflective pixel and 0 to a non-reflective pixel, respectively. This method effectively utilizes discrepancies in photometric errors to distinguish between reflective and non-reflective surfaces, providing a precise mapping of surface properties within the image. (refer to Section D in the supplementary materials.)

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3.2.2 **REFLECTION-AWARE TRIPLET MINING LOSS**

We introduce the reflection-aware triplet mining loss, \mathcal{L}_{tri} , which addresses the limitations of using 269 \mathbf{E}^+ alone in environments where reflections disrupt depth accuracy. In reflective regions, simply minimizing E^+ does not effectively discern between real and reflected disparities. To counteract this, we assert that E^- should be significantly greater than E^+ . This approach is inspired by triplet mining techniques that aim to minimize the distance within positive pairs and maximize it within negative pairs, enhancing the model's ability to distinguish between reflective and non-reflective surfaces. To implement this, we formulate the reflection-aware triplet mining loss as follows:

$$\mathcal{L}_{tri}(\mathbf{I}_{ref}, \mathbf{I}_{s2r}, \mathbf{I}_{r2s}) = \mathbf{M}_r \odot (\mathbf{E}^+ - \mathbf{E}^- + \delta)_{hinge} + (1 - \mathbf{M}_r) \odot \mathbf{E}^+,$$
(9)

where $(\cdot)_{hinge}$ is the hinge loss function described in Hearst et al. (1998). In this configuration, the reflection-aware triplet mining loss is applied specifically to regions identified as reflective. For non-reflective regions, where reflections do not disrupt photometric assessments, we apply the photometric loss \mathbf{E}^+ as it reliably reflects photometric consistency. This differentiation allows the model to address the unique challenges presented by each type of region effectively.

As illustrated in Figure 2, this strategy involves not only penalizing the minimization of E^+ but also actively maximizing E^- . This method effectively counteracts the contaminated gradients typically found in reflective regions. By adjusting the balance between E^+ and E^- based on the presence of reflective surfaces, our method not only improves depth estimation in complex scenarios but also ensures robust performance against the challenges posed by reflective surfaces. This comprehensive approach results in a model that accurately reflects the true topography of both reflective and nonreflective environments.

289 3.2.3 Reflection-aware knowledge distillation

The proposed end-to-end training scheme described in Section 3.2.2 effectively handles the depth estimation on both reflective and non-reflective surfaces. To further refine depth estimation quality, we introduce a reflection-aware knowledge distillation strategy inspired by the fusion techniques discussed in Shi et al. (2023), aimed at retaining high-frequency details in depth prediction.

Our approach begins by training two separate SSMDE networks. The first is trained using our 295 reflection-aware triplet mining loss, \mathcal{L}_{tri} , as defined in Equation 9, and the second employs the 296 conventional photometric loss, \mathbf{E}^+ . From these models, we generate two types of depth maps: \mathbf{D}_{tri} , 297 derived from the reflection-aware model, and D_{ori} , obtained from the model trained with conven-298 tional photometric loss. We then merge these depth maps into a single pseudo depth map D_{pse} 299 utilizing a reflective region mask \mathbf{M}_r . This mask facilitates the adaptive fusing of depth information 300 from both teacher models based on the presence of reflective properties in the image. The pseudo 301 depth map generation and distillation process is detailed in the following equation: 302

$$\mathcal{L}_{rkd}(\hat{\mathbf{D}}, \mathbf{D}_{pse}) = |\log \hat{\mathbf{D}} - \log \mathbf{D}_{pse}|, \text{ where } \mathbf{D}_{pse} = \mathbf{M}_r \odot \mathbf{D}_{tri} + (1 - \mathbf{M}_r) \odot \mathbf{D}_{ori}, \quad (10)$$

where $\hat{\mathbf{D}}$ represents the depth predicted by the student model. It is important to note that the student model and the two teacher models share the same network architecture as the general SSMDEs. This structured training approach not only addresses the specific challenges posed by reflective surfaces but also ensures that the high-frequency detail is not lost, thus achieving a balanced and accurate depth prediction across different surface types.

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4 EXPERIMENTS

311 **Datasets.** ScanNet (v2) (Dai et al., 2017) is a comprehensive indoor RGB-D video dataset com-312 prising 2.7 million images across 1,216 interior scene sequences. Traditionally, this dataset has been 313 pivotal for evaluating multi-view stereo (Im et al., 2019; Bae et al., 2022) and scene reconstruction 314 applications (Murez et al., 2020; Zhou et al., 2024). 7-Scenes (Shotton et al., 2013) is a challenging 315 RGB-D dataset captured in indoor scenes with a similar distribution to ScanNet but dominated by 316 non-reflective surfaces. We follow the evaluation protocol of Long et al. (2021); Bae et al. (2022) to 317 demonstrate the cross-dataset generalization performances. Booster (Ramirez et al., 2023) includes 318 a variety of non-Lambertian objects within indoor settings, such as transparent basins, mirrors, and 319 specular surfaces. Following the Costanzino et al. (2023), we use the training split as our test set, 320 which showcases our method's adaptability to more complex scenes.

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322 Training scenario. In the work of 3D distillation (Shi et al., 2023), the ScanNet dataset has been further segmented into ScanNet-Reflection and ScanNet-NoReflection subsets based on the presence of reflective objects within the scenes. This subdivision results in a ScanNet-Reflection dataset

	Backbone	Training Scheme	Method	Abs Rel↓	Sq Rel \downarrow	$\text{RMSE} \downarrow$	RMSE log \downarrow	$\delta < 1.25\uparrow$	$\delta < 1.25^2 \uparrow$	$\delta < 1.25^3$
tion Test	Monodepth2	End-to-End	Self-Supervised Ours	0.181 0.157	0.160 0.096	0.521 0.468	0.221 0.201	0.758 0.762	0.932 0.949	0.976 0.988
		Multi-Stage	Self-Teaching 3D Distillation Ours [†]	0.179 0.156 0.150	0.146 0.096 0.087	0.502 0.459 0.446	0.218 0.195 0.192	0.750 0.766 0.777	0.938 0.945 0.955	0.980 0.988 0.990
allan-		End-to-End	Self-Supervised Ours	0.182 0.157	0.168 0.098	0.530 0.470	0.225 0.201	0.749 0.763	0.937 0.952	0.979 0.989
DCalling	HRDepth	Multi-Stage	Self-Teaching 3D Distillation Ours [†]	0.175 0.152 0.150	0.145 0.089 0.092	0.492 0.451 0.434	0.215 0.190 0.192	0.757 0.771 0.780	0.936 0.956 0.950	0.982 0.990 0.988
		End-to-End	Self-Supervised Ours	0.154 0.136	0.129 0.087	0.458 0.414	0.197 0.178	0.822 0.831	0.955 0.967	0.979 0.988
	MonoViT	Multi-Stage	Self-Teaching 3D Distillation Ours [†]	0.151 0.127 0.126	0.130 0.069 0.074	0.439 0.379 0.395	0.191 0.162 0.167	0.837 0.846 0.854	0.950 0.961 0.969	0.978 0.992 0.990
		End-to-End	Self-Supervised Ours	0.206 0.166	0.227 0.125	0.584 0.492	0.246 0.209	0.750 0.763	0.912 0.934	0.961 0.981
valuauo	Monodepth2	Multi-Stage	Self-Teaching 3D Distillation Ours [†]	0.192 0.156 0.151	0.188 0.093 0.105	0.548 0.442 0.454	0.233 0.191 0.193	0.764 0.786 0.796	0.920 0.943 0.944	0.967 0.987 0.985
		End-to-End	Self-Supervised	0.213 0.167	0.244 0.127	0.605 0.496	0.255 0.210	0.741 0.770	0.906 0.937	0.961 0.982
Vet-Refle	HRDepth	Multi-Stage	Self-Teaching 3D Distillation Ours [†]	0.202 0.153 0.151	0.208 0.090 0.104	0.565 0.430 0.450	0.243 0.188 0.192	0.756 0.789 0.800	0.914 0.948 0.949	0.964 0.989 0.987
Scan		End-to-End	Self-Supervised	0.179 0.139	0.206 0.107	0.557 0.452	0.227 0.183	0.819 0.836	0.930 0.954	0.963 0.984
	MonoViT	Multi-Stage	Self-Teaching 3D Distillation Ours [†]	0.176 0.126 0.130	0.195 0.068 0.091	0.537 0.367 0.420	0.224 0.159 0.173	0.823 0.851 0.851	0.930 0.965 0.960	0.963 0.991 0.987

Table 1: Main results on the ScanNet-Reflection Test and Validation sets.

consisting of 45,539 training, 439 validation, and 121 testing samples. Additionally, a ScanNet-NoReflection validation set comprising 1,012 samples evaluates the model's generalization when trained in reflective environments. Aligning with these methodologies, the training process leverages the ScanNet-Reflection train set to simulate real-world scenarios involving reflective surfaces.

Evaluation. For quantitative evaluations, we employ standard metrics from the depth estimation literature (Eigen et al., 2014; Geiger et al., 2012). We differentiate our training approaches into end-to-end and multi-stage (distillation) strategies to effectively assess the models. The model trained solely using reflection-aware triplet mining loss \mathcal{L}_{tri} , referred to as "Ours", and another utilizing the proposed distillation method \mathcal{L}_{rkd} , referred to as "Ours[†]", are evaluated under their respective conditions. We compare these against both end-to-end and multi-stage baselines across three sets: ScanNet-Reflection {Test, Validation} sets, and ScanNet-NoReflection Validation set. To underline the cross-dataset generalizability of our methods, we also perform zero-shot evaluations on the 7-Scenes and Booster.

Implementation details. Our experiments incorporate three leading architectures in SSMDE: Monodepth2 (Godard et al., 2019), HRDepth (Lyu et al., 2021), and MonoViT (Zhao et al., 2022), which have demonstrated exceptional performance in previous studies. Each backbone is trained by different training schemes, including Self-Supervised (Godard et al., 2019), Self-Teaching (Poggi et al., 2020), and 3D Distillation (Shi et al., 2023), to compare with our method. To align closely with 3D Distillation, all training particulars follow their documented conditions, with adaptations only in our proposed training strategy. Specifically, the models are trained using the reflection triplet split introduced in 3D Distillation. To finely tune the margin δ across positive and negative pairs, it is adaptively selected based on the difference between the first quartile (Q1) of E^+ and the third quartile (Q3) of E^- .

4.1 EVALUATION ON REFLECTION DATASETS376

ScanNet-Reflection dataset. To demonstrate the effectiveness of the proposed method on reflective surfaces, we conduct a quantitative evaluation using the ScanNet-Reflection dataset. The eval-

Backbone	Training Scheme	Method	Abs Rel \downarrow	Sq Rel \downarrow	$\text{RMSE} \downarrow$	RMSE log \downarrow	$\delta < 1.25\uparrow$	$\delta < 1.25^2 \uparrow$	$\delta < 1.25^3$
	End-to-End	Self-Supervised Ours	0.169 0.168	0.100 0.095	0.395 0.395	0.206 0.208	0.759 0.751	0.932 0.931	0.979 0.980
Monodepth2	Multi-Stage	Self-Teaching 3D Distillation Ours [†]	0.161 0.159 0.157	0.090 0.087 0.085	0.375 0.373 0.373	0.196 0.195 0.195	0.777 0.779 0.776	0.939 0.941 0.942	0.981 0.983 0.983
	End-to-End	Self-Supervised Ours	0.169 0.167	0.102 0.096	0.388 0.389	0.202 0.204	0.766 0.764	0.933 0.933	0.980 0.979
HRDepth	Multi-Stage	Self-Teaching 3D Distillation Ours [†]	0.160 0.158 0.157	0.089 0.086 0.086	0.367 0.365 0.366	0.192 0.190 0.192	0.784 0.786 0.784	0.941 0.942 0.942	0.982 0.983 0.983
MonoViT	End-to-End	Self-Supervised Ours	0.140 0.141	0.074 0.072	0.333 0.338	0.171 0.174	0.829 0.823	0.952 0.952	0.984 0.987
	Multi-Stage	Self-Teaching 3D Distillation Ours [†]	0.134 0.133 0.133	0.068 0.065 0.066	0.317 0.311 0.320	0.164 0.162 0.166	0.840 0.838 0.837	0.956 0.956 0.957	0.987 0.987 0.987

Table 2: Main results on the ScanNet-NoReflection Validation set.



Figure 3: Qualitative results of the proposed methods on the ScanNet. We visualize the predicted depth of the Monodepth2 (Godard et al., 2019) trained by three different methods including the proposed method: Self-supervised, *Ours* and *Ours*[†]. Note that the error map represents the absolute difference between prediction and ground truth depth, normalized to between 0 and 255.

uations are divided into end-to-end and multi-stage methodologies. As depicted in Table 1, Ours, categorized under end-to-end training schemes, significantly outperforms self-supervised methods across all backbones, achieving an Abs Rel average increase of 12.90% in the test split and 21.12% in the validation split. Moreover, it is noteworthy that *Ours* shows a significant performance boost, with an average improvement of 10.75% over Self-Teaching across all metrics in both the test and validation splits, with only two exceptions in 42 metrics ($\delta < 1.25$ of Monodepth2 and MonoViT). This demonstrates that our reflection-aware triplet mining loss is effective in detecting reflective surfaces and encourages the model to obtain accurate depth on these surfaces as shown in Figure 3. Additionally, our multi-stage approach, which employs reflection-aware knowledge distillation (denoted as *Ours*[†]), delivers comparable results across all backbone models of 3D Distillation. Note that the proposed method does not require complex scene reconstruction procedures such as mesh ren-dering (Matl, 2019; Newcombe et al., 2011) or ensembles of multiple neural network models (Lak-shminarayanan et al., 2017).

ScanNet-NoReflection dataset. Table 2 summarizes the results of a quantitative evaluation performed on the ScanNet-NoReflection dataset. This evaluation aims to measure the generalization

	Backbone	Method	Abs Rel \downarrow	Sq Rel \downarrow	$\text{RMSE}\downarrow$	RMSE log \downarrow	$\delta < 1.25 \uparrow$	$\delta < 1.25^2 \uparrow$	$\delta < 1.25^3 \uparrow$
		Self-Supervised	0.210	0.130	0.445	0.248	0.656	0.906	0.974
	Monodepth2	Ours	0.207	0.125	0.441	0.248	0.656	0.904	0.975
nes	-	<i>Ours</i> [†]	0.198	0.110	0.415	0.238	0.667	0.911	0.980
Sce		Self-Supervised	0.193	0.115	0.421	0.231	0.682	0.921	0.982
4	HRDepth	Ours	0.195	0.109	0.419	0.232	0.674	0.921	0.984
		Ours [†]	0.183	0.096	0.389	0.219	0.706	0.931	0.986
		Self-Supervised	0.173	0.093	0.365	0.201	0.752	0.945	0.988
	MonoViT	Ours	0.175	0.090	0.361	0.204	0.746	0.944	0.987
		<i>Ours</i> [†]	0.162	0.077	0.335	0.191	0.776	0.951	0.989
		Self-Supervised	0.520	0.429	0.601	0.444	0.305	0.591	0.827
	Monodepth2	Ours	0.430	0.301	0.501	0.389	0.362	0.675	0.893
		Ours [†]	0.419	0.288	0.487	0.381	0.370	0.678	0.897
er		Self-Supervised	0.495	0.391	0.559	0.426	0.307	0.611	0.852
ost	HRDepth	Ours	0.414	0.276	0.482	0.379	0.364	0.680	0.907
Bo		Ours [†]	0.429	0.292	0.487	0.385	0.366	0.659	0.878
		Self-Supervised	0.418	0.327	0.504	0.374	0.425	0.679	0.888
	MonoViT	Ours	0.408	0.302	0.482	0.362	0.414	0.677	0.916
		Ours [†]	0.375	0.249	0.440	0.337	0.422	0.734	0.944

Table 3: Cross-dataset evaluation result on the 7-Scenes and booster datasets.

performance of models trained on datasets that include reflective surfaces. In an end-to-end training scheme, Ours achieves performance comparable to or within an acceptable margin of self-supervised methods. This confirms that our proposed reflection-aware triplet mining loss effectively prevents the incorrect back-propagation of the photometric loss gradient on reflective surfaces, as illustrated in Figure 2. Furthermore, the model trained by our reflection-aware knowledge distillation (*i.e.*, $Ours^{\dagger}$) shows a noticeable performance improvement, which is comparable performance to the 3D distillation method. These results suggest that extending our reflection-aware triplet mining loss to distillation techniques offers a straightforward yet effective strategy for managing reflective surfaces.

4.2 CROSS-DATASET GENERALIZABILITY

To demonstrate the generalization ability across different datasets, we conduct a zero-shot evalu-ation using 7-Scenes and Booster datasets. As shown in Table 3, our proposed methods (denoted as Ours and $Ours^{\dagger}$) consistently enhances performance. Specifically, across all backbone architec-tures and all metrics, $Ours^{\dagger}$ improved by an average of 5.47% and 13.89% for the 7-Scenes and Booster datasets, respectively. Exceptionally, there is no significant difference between Ours and the self-supervised method on the 7-Scenes dataset. This may be attributed to the predominance of non-reflective surfaces in the 7-Scenes dataset, where our model, trained with the reflection-aware triplet mining loss, slightly loses high-frequency details on non-reflective surfaces. Conversely, the consistent performance improvement of $Ours^{\dagger}$ across both reflective and non-reflective surfaces demonstrates the robust generalization capabilities of our method based on reflective region selec-tion.

CONCLUSION

This paper addresses the intricate challenge of self-supervised monocular depth estimation on reflec-tive surfaces. Our method employs a novel metric learning approach, centered around a reflection-aware triplet mining loss. This novel loss function significantly improves depth prediction accu-racy by accurately identifying reflective regions on a per-pixel basis and effectively adjusting the minimization of photometric errors, which are typically problematic on reflective surfaces. It also preserves high-frequency details on non-reflective surfaces by selectively regulating photometric er-ror minimization based on reflection region selection. Moreover, we introduce a reflection-aware knowledge distillation method, enabling a student model to enhance performance in both reflective and non-reflective surfaces. This method leverages the strengths of different teaching networks to produce a more robust and versatile student model. Experimental evaluations conducted on the in-door scene datasets demonstrate our method consistently enhances depth performance across various architectural frameworks. These results underscore the robustness and versatility of our approach, marking it as a valuable contribution to the field of self-supervised monocular depth estimation.

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MORE DETAILED EXPERIMENTAL SETUPS А

As aforementioned in the main manuscripts, we follow all training details and experimental setups mentioned in 3D Distillation (Shi et al., 2023). We train all models with the reflection triplet split proposed by 3D Distillation for 41 epochs through the Adam optimizer (Kingma & Ba, 2014) with an image resolution of 384×288, implemented in PyTorch. The training batch sizes of the Monodepth2 (Godard et al., 2019), HRDepth (Lyu et al., 2021), and MonoViT (Zhao et al., 2022) are $\{12, 12, 8\}$, respectively. The initial learning rate is 10^{-4} , and we adopt the multi-step learning rate scheduler that decays the learning rate by $\gamma = 0.1$ once the number of epochs reaches one of the milestones [26, 36]. Moreover, with 3D Distillation, the pose between cameras is ground truth during training, and the minimum and maximum depths used for training and evaluation are 0.1m and 10m. In our evaluation, we do not apply post-processing techniques such as averaging the estimates of both the flipped and original images or using median scaling.

Table 4: Main results on the ScanNet-Original Test and Validation sets.

Dealthean	Tasiaina Cabama	Mathad			Sc	anNet-Original	Test Set		
Баскоопе	Training Scheme	Method	Abs Rel \downarrow	Sq Rel \downarrow	$\text{RMSE} \downarrow$	RMSE log \downarrow	$\delta < 1.25\uparrow$	$\delta < 1.25^2 \uparrow$	$\delta < 1.25^3 \uparrow$
	End-to-End	Self-Supervised	0.189	0.116	0.407	0.217	0.731	0.921	0.974
Monodepth2		Uurs	0.185	0.109	0.405	0.217	0.730	0.923	0.975
	Multi-Stage	3D Distillation	0.184	0.109	0.392	0.210	0.742 0.746	0.925 0.927	0.976
		Ours [†]	0.175	0.098	0.385	0.206	0.746	0.930	0.979
	End-to-End	Self-Supervised	0.184	0.111	0.399	0.212	0.739	0.925	0.976
UDDareth	End to End	Ours	0.186	0.106	0.397	0.213	0.735	0.927	0.977
пкрери		Self-Teaching	0.178	0.102	0.381	0.204	0.752	0.931	0.979
	Multi-Stage	3D Distillation Ours [†]	0.176 0.173	0.098 0.096	0.378 0.375	0.202 0.202	0.754 0.755	0.932 0.934	0.979 0.980
	End to End	Self-Supervised	0.154	0.082	0.343	0.182	0.801	0.948	0.984
	End-to-End	Ours	0.155	0.081	0.345	0.185	0.795	0.945	0.984
MonoViT		Self-Teaching	0.152	0.081	0.329	0.177	0.811	0.948	0.983
	Multi-Stage	3D Distillation	0.149	0.075	0.324	0.174	0.812	0.949	0.985
		Ours	0.149	0.075	0.333	0.179	0.805	0.949	0.980
Backbone	Training Scheme	Method	Abs Rel↓	Sq Rel↓	So RMSE↓	anNet-Original RMSE log↓	Val. Set $\delta < 1.25 \uparrow$	$\delta < 1.25^2 \uparrow$	$\delta < 1.25^3 \uparrow$
Backbone	Training Scheme	Method Self-Supervised	Abs Rel↓ 0.167	Sq Rel↓ 0.100	So RMSE↓ 0.385	canNet-Original RMSE log↓ 0.203	Val. Set $\delta < 1.25 \uparrow$ 0.764	$\frac{\delta < 1.25^2 \uparrow}{0.935}$	$\frac{\delta < 1.25^3 \uparrow}{0.981}$
Backbone	Training Scheme	Method Self-Supervised Ours	Abs Rel↓ 0.167 0.162	Sq Rel↓ 0.100 0.090	So RMSE↓ 0.385 0.378	canNet-Original RMSE log↓ 0.203 0.201	Val. Set $\delta < 1.25 \uparrow$ 0.764 0.765	$\frac{\delta < 1.25^2 \uparrow}{0.935}$ 0.937	$δ < 1.25^3 ↑$ 0.981 0.983
Backbone Monodepth2	Training Scheme	Method Self-Supervised Ours Self-Teaching	Abs Rel↓ 0.167 0.162 0.160	Sq Rel↓ 0.100 0.090 0.090	So RMSE↓ 0.385 0.378 0.365	canNet-Original RMSE log ↓ 0.203 0.201 0.193 0.193	δ Val. Set δ < 1.25 ↑ 0.764 0.765 0.780 0.780	δ < 1.252 ↑ 0.935 0.937 0.941	δ < 1.253 ↑ 0.981 0.983 0.983
Backbone Monodepth2	Training Scheme End-to-End Multi-Stage	Method Self-Supervised Ours Self-Teaching 3D Distillation Ours [†]	Abs Rel↓ 0.167 0.162 0.160 0.157 0.153	Sq Rel↓ 0.100 0.090 0.090 0.083 0.080	Sc RMSE↓ 0.385 0.378 0.365 0.357 0.358	canNet-Original RMSE log ↓ 0.203 0.201 0.193 0.190 0.190	Val. Set $\delta < 1.25 \uparrow$ 0.764 0.765 0.780 0.782 0.783	δ < 1.252 ↑ 0.935 0.937 0.941 0.943 0.944	δ < 1.253 ↑ 0.981 0.983 0.983 0.985 0.985
Backbone Monodepth2	Training Scheme End-to-End Multi-Stage	Method Self-Supervised Ours Self-Teaching 3D Distillation Ours [†]	Abs Rel \downarrow 0.167 0.162 0.160 0.157 0.153	Sq Rel ↓ 0.100 0.090 0.090 0.083 0.080 0.100	So RMSE↓ 0.385 0.378 0.365 0.357 0.358 0.381	canNet-Original RMSE log↓ 0.203 0.201 0.193 0.190 0.190 0.200	Val. Set $\delta < 1.25 \uparrow$ 0.764 0.765 0.780 0.782 0.783 0.771	δ < 1.252 ↑ 0.935 0.937 0.941 0.943 0.944 0.937	δ < 1.253 ↑ 0.981 0.983 0.983 0.985 0.985 0.985
Backbone Monodepth2	Training Scheme End-to-End Multi-Stage End-to-End	Method Self-Supervised $Ours$ Self-Teaching 3D Distillation $Ours^{\dagger}$ Self-Supervised $Ours$	Abs Rel↓ 0.167 0.160 0.157 0.153 0.166 0.160	Sq Rel↓ 0.100 0.090 0.083 0.080 0.100 0.089	So RMSE↓ 0.385 0.378 0.365 0.357 0.358 0.381 0.373	canNet-Original RMSE log ↓ 0.203 0.201 0.193 0.190 0.190 0.200 0.197	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$	δ < 1.252 ↑ 0.935 0.937 0.941 0.943 0.944 0.937 0.941	δ < 1.253 ↑ 0.981 0.983 0.983 0.985 0.985 0.985 0.982 0.984
Backbone Monodepth2 HRDepth	Training Scheme End-to-End Multi-Stage End-to-End	Method Self-Supervised Ours Self-Teaching SD Distillation Ours [†] Self-Supervised Ours Self-Teaching	Abs Rel↓ 0.167 0.162 0.160 0.157 0.153 0.166 0.166 0.169	Sq Rel↓ 0.100 0.090 0.090 0.083 0.080 0.100 0.089 0.090	Sc RMSE↓ 0.385 0.378 0.365 0.357 0.358 0.381 0.373 0.360	canNet-Original RMSE log ↓ 0.203 0.201 0.193 0.190 0.190 0.200 0.197 0.190	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$	δ < 1.252 ↑ 0.935 0.937 0.941 0.943 0.944 0.937 0.941 0.943	δ < 1.253 ↑ 0.981 0.983 0.983 0.985 0.985 0.985 0.982 0.984
Backbone Monodepth2 HRDepth	Training Scheme End-to-End Multi-Stage End-to-End Multi-Stage	Method Self-Supervised Ours Self-Teaching 3D Distillation Ours [†] Self-Supervised Ours Self-Teaching 3D Distillation	Abs Rel↓ 0.167 0.162 0.160 0.157 0.153 0.166 0.166 0.169 0.159 0.154	Sq Rel↓ 0.100 0.090 0.083 0.080 0.100 0.089 0.090 0.080	Sc RMSE↓ 0.385 0.378 0.365 0.357 0.358 0.381 0.373 0.360 0.349	canNet-Original RMSE log ↓ 0.203 0.201 0.193 0.190 0.190 0.200 0.197 0.190 0.190 0.190 0.190	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$	$\begin{array}{c} \delta < 1.25^2 \uparrow \\ \hline 0.935 \\ \hline 0.937 \\ \hline 0.941 \\ \hline 0.943 \\ \hline 0.937 \\ \hline 0.941 \\ \hline 0.937 \\ \hline 0.941 \\ \hline 0.943 \\ \hline 0.943 \\ \hline 0.945 \\ \end{array}$	$\begin{array}{c} \delta < 1.25^3 \uparrow \\ \hline 0.981 \\ \hline 0.983 \\ \hline 0.983 \\ \hline 0.983 \\ \hline 0.985 \\ \hline 0.985 \\ \hline 0.985 \\ \hline 0.984 \\ \hline 0.986 \\ \end{array}$
Backbone Monodepth2 HRDepth	Training Scheme End-to-End Multi-Stage End-to-End Multi-Stage	Method Self-Supervised Ours Self-Teaching 3D Distillation Ours [†] Self-Supervised Ours Self-Teaching 3D Distillation Ours [†]	Abs Rel↓ 0.167 0.162 0.157 0.153 0.166 0.160 0.153 0.154 0.154	Sq Rel↓ 0.100 0.090 0.083 0.080 0.100 0.089 0.090 0.080 0.078	Sc RMSE ↓ 0.385 0.378 0.365 0.357 0.358 0.381 0.373 0.360 0.349 0.350	canNet-Original RMSE log ↓ 0.203 0.201 0.193 0.190 0.190 0.200 0.197 0.190 0.190 0.190 0.186 0.186	Val. Set $\delta < 1.25 ↑$ 0.764 0.765 0.780 0.782 0.771 0.772 0.785 0.788 0.790	$\begin{array}{c} \delta < 1.25^2 \uparrow \\ 0.935 \\ \textbf{0.937} \\ 0.941 \\ 0.943 \\ \textbf{0.943} \\ \textbf{0.937} \\ \textbf{0.944} \\ 0.937 \\ \textbf{0.943} \\ 0.945 \\ \textbf{0.948} \\ \end{array}$	$\begin{tabular}{ c c c c c c }\hline\hline $\delta < 1.25^3 \uparrow \\\hline $0.981 \\\hline $0.983 \\\hline $0.983 \\\hline $0.985 \\\hline $0.985 \\\hline $0.985 \\\hline $0.984 \\\hline $0.986 \\\hline $0.987 \\\hline $0.987 \\\hline \end{tabular}$
Backbone Monodepth2 HRDepth	Training Scheme End-to-End Multi-Stage End-to-End Multi-Stage End-to-End	Method Self-Supervised Ours Self-Teaching 3D Distillation Ours [†] Self-Supervised Ours Self-Teaching 3D Distillation Ours [†] Self-Supervised	Abs Rel↓ 0.167 0.162 0.157 0.153 0.166 0.166 0.167 0.153 0.154 0.154 0.151 0.138 0.137	Sq Rel↓ 0.100 0.090 0.083 0.080 0.100 0.089 0.090 0.080 0.090 0.080 0.077 0.077	Sc RMSE ↓ 0.385 0.378 0.365 0.357 0.358 0.381 0.373 0.360 0.349 0.350 0.351 0.350 0.331 0.238	canNet-Original RMSE log ↓ 0.203 0.201 0.193 0.190 0.190 0.200 0.197 0.190 0.186 0.186 0.186 0.171 0.172	Val. Set $\delta < 1.25 \uparrow$ 0.764 0.765 0.782 0.782 0.771 0.772 0.788 0.790 0.831 0.926	$\begin{array}{c} \delta < 1.25^2 \uparrow \\ 0.935 \\ \textbf{0.937} \\ 0.941 \\ 0.943 \\ \textbf{0.944} \\ 0.937 \\ \textbf{0.944} \\ 0.937 \\ \textbf{0.943} \\ 0.945 \\ \textbf{0.945} \\ \textbf{0.955} \\ \textbf{0.955} \end{array}$	δ < 1.253 ↑ 0.981 0.983 0.983 0.985 0.985 0.985 0.984 0.984 0.986 0.987 0.986 0.987
Monodepth2 HRDepth MonoViT	Training Scheme End-to-End Multi-Stage End-to-End Multi-Stage End-to-End	Method Self-Supervised Ours 3D Distillation Ours [†] Self-Teaching 3D Distillation Ours Self-Teaching 3D Distillation Ours [†] Self-Supervised Ours Self-Supervised Ours	Abs Rel ↓ 0.167 0.162 0.160 0.157 0.153 0.166 0.160 0.159 0.154 0.151 0.138 0.137 0.137	Sq Rel ↓ 0.100 0.090 0.083 0.080 0.100 0.089 0.090 0.080 0.077 0.077 0.077 0.071	SG RMSE ↓ 0.385 0.378 0.357 0.358 0.358 0.381 0.373 0.360 0.349 0.350 0.331 0.331 0.331 0.324	anNet-Original RMSE log ↓ 0.203 0.201 0.193 0.190 0.190 0.190 0.190 0.190 0.186 0.186 0.172 0.172 0.172	Val. Set $\delta < 1.25 \uparrow$ 0.764 0.765 0.780 0.782 0.783 0.771 0.772 0.785 0.788 0.790 0.826 0.244	δ < 1.252 ↑ 0.935 0.937 0.941 0.943 0.944 0.937 0.944 0.937 0.941 0.943 0.945 0.945 0.958 0.958 0.958	$\begin{split} \delta < 1.25^3 \uparrow \\ 0.981 \\ 0.983 \\ 0.983 \\ 0.985 \\ 0.985 \\ 0.985 \\ 0.984 \\ 0.984 \\ 0.984 \\ 0.986 \\ 0.987 \\ 0.986 \\ 0.989 \\ 0.980 \\ 0.9$
Monodepth2 HRDepth MonoViT	Training Scheme End-to-End Multi-Stage End-to-End Multi-Stage End-to-End Multi-Stage	Method Self-Supervised Ours 3D Distillation Ours [†] Self-Teaching 3D Distillation Ours Self-Teaching 3D Distillation Ours Self-Supervised Ours Self-Teaching 3D Distillation Ours Self-Teaching 3D Distillation	Abs Rel ↓ 0.167 0.162 0.160 0.157 0.153 0.166 0.160 0.159 0.154 0.151 0.138 0.137 0.133 0.128	Sq Rel ↓ 0.100 0.090 0.083 0.080 0.100 0.090 0.090 0.090 0.090 0.090 0.080 0.077 0.069 0.077 0.069	Sc RMSE ↓ 0.385 0.378 0.365 0.357 0.358 0.381 0.369 0.349 0.350 0.349 0.350 0.331 0.328 0.314 0.296	anNet-Original RMSE log ↓ 0.203 0.201 0.190 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.195 0.155 0	Val. Set $\delta < 1.25 \uparrow$ 0.764 0.765 0.780 0.782 0.783 0.771 0.772 0.785 0.786 0.783 0.771 0.772 0.885 0.826 0.844 0.846	δ < 1.252 ↑ 0.935 0.937 0.941 0.943 0.944 0.937 0.944 0.937 0.944 0.937 0.944 0.943 0.945 0.945 0.955 0.958 0.959 0.962	δ < 1.253 ↑ 0.981 0.983 0.985 0.985 0.985 0.984 0.984 0.984 0.984 0.986 0.987 0.986 0.988 0.988 0.988 0.989

EVALUATIONS ON SCANNET DATASET В

To demonstrate the generalizability of our proposed method, we conduct the experiment on several ScanNet (Dai et al., 2017) splits denoted as ScanNet-Original {Test, Val.} sets and ScanNet-Robust Test set following Shi et al. (2023) and Fu et al. (2018); Bae et al. (2022), respectively. ScanNet-Original sets include both reflective and non-reflective surfaces, it is well-suited to evaluate the impact of reflective surfaces on training comprehensively. In addition, the ScanNet-Robust test set was used to measure the generalization performance of Monocular Depth Estimation in the Robust Vision Challenge 2018 (Geiger et al., 2018), as it is small-scale but suitable for evaluating general-ization performance.

702 B.1 EVALUATION ON SCANNET-ORIGINAL SETS

Table 4 summarizes the quantitative evaluation results of the ScanNet-Original sets. We achieve steady performance improvement across most metrics for all backbone models in the end-to-end training scheme, suggesting that the proposed method minimizes the influence of reflective surfaces, which contributes to the general depth estimation performance improvement.

708 Furthermore, Our multi-stage training scheme (*i.e.*, $Ours^{\dagger}$) dramatically elevates performance across 709 various depth estimation models. For Monodepth2, $Ours^{\dagger}$ achieves a remarkable average increase of 710 5.28% on the test set and 6.52% on the validation set across all metrics. HRDepth reaps substantial 711 benefits, with improvements of 4.83% on the test set and 7.19% on the validation set. Likewise, 712 MonoViT consistently gains, with enhancements of 2.28% on the test set and 5.59% on the validation set. When benchmarked against 3D Distillation (Shi et al., 2023), Ours[†] provides an enhanced 713 performance for Monodepth2, showing an average increase of 1.76% on the test set and 0.87% on 714 the validation set. HRDepth also gains an average of 0.71% on the test set and 0.69% on the valida-715 tion set. However, for MonoViT, $Ours^{\dagger}$ shows a slight decline, with decreases of 1.09% on the test 716 set and 1.92% on the validation set compared to 3D Distillation. 717

Backbone	Madad	ScanNet-Robust Test Set								
Backbone	Method	Abs Rel \downarrow	Sq Rel \downarrow	$\text{RMSE} \downarrow$	$RMSE \log \downarrow$	$\delta < 1.25\uparrow$	$\delta < 1.25^2 \uparrow$	$\delta < 1.25^3 \uparrow$		
	Self-Supervised	0.193	0.118	0.395	0.219	0.729	0.921	0.973		
Monodepth2	Ours	0.186	0.107	0.388	0.216	0.729	0.926	0.976		
,	$Ours^{\dagger}$	0.179	0.099	0.371	0.207	0.744	0.930	0.978		
	Self-Supervised	0.190	0.112	0.387	0.216	0.729	0.924	0.976		
HRDepth	Ours	0.188	0.107	0.384	0.215	0.731	0.926	0.976		
	$Ours^{\dagger}$	0.177	0.095	0.362	0.203	0.750	0.935	0.979		
	Self-Supervised	0.158	0.082	0.328	0.181	0.799	0.948	0.984		
MonoViT	Ours	0.155	0.078	0.327	0.183	0.798	0.949	0.985		
	$Ours^{\dagger}$	0.150	0.073	0.319	0.178	0.806	0.952	0.986		

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B.2 EVALUATION ON SCANNET-ROBUST TEST SET

734 Table 5 summarizes the quantitative evaluation results of the ScanNet-Robust test set. Due to the 3D-735 distillation baselines (Shi et al., 2023) did not release the source code, and the reported performance 736 on this split not existing, we compare the models trained by our methods to the self-supervised methods across three backbones, similar to previous experiments. As depicted in Table 5, our pro-737 posed methods (*i.e.*, Ours, $Ours^{\dagger}$) achieve significant performance gains for all evaluation metrics 738 and all backbones, consistently. Specifically, for Monodepth2, Ours and Ours[†] demonstrate an av-739 erage performance improvement of 2.42% and 5.49%, respectively, across all metrics. Similarly, for 740 HRDepth, Ours showed an average improvement of 1.03%, and Ours^{\dagger} achieved a 5.55% increase 741 in performance across all metrics. In the case of MonoViT, Ours resulted in an average performance 742 improvement of 0.87%, and Ours[†] achieved a 3.13% improvement across all metrics. The consis-743 tent improvements across all metrics for Monodepth2, HRDepth, and MonoViT indicate that our 744 methods effectively mitigate the risk of erroneous learning induced by reflective surfaces.

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C QUALITATIVE RESULTS ON 7-SCENES AND BOOSTER DATASETS

We provide additional qualitative results of the proposed methods denoted as *Ours* and *Ours*[†] as discussed in Table 3 of the main manuscript, utilizing the 7-Scenes (Shotton et al., 2013) and Booster (Ramirez et al., 2023) datasets. In Figure 4, we showcase the predicted depth and error map of the Monodepth2 trained by self-supervised, \mathcal{L}_{tri} , and \mathcal{L}_{rkd} . Our methods alleviate the black-hole effect on specular highlight regions while preserving high-frequency details on non-reflective areas. As demonstrated by the qualitative evaluation of the 7-Scenes dataset, our proposed methods exhibit robustness to reflective surfaces and impressive performance in preserving details on non-reflective surfaces in other indoor scenes that are similar to the training environment.



that the error map represents the absolute difference between prediction and ground truth depth, normalized to between 0 and 255.

Deelshope	Method	Scar	Net-Reflect	tion Validati	on Set	ScanNet-NoReflection Validation Set				
Dackbolle		Abs Rel↓	Sq Rel \downarrow	$\text{RMSE} \downarrow$	$\delta < 1.25^3 \uparrow \big $	Abs Rel \downarrow	Sq Rel \downarrow	$\text{RMSE} \downarrow$	$\delta < 1.25^3$	
	$M_r = 0$	0.206	0.227	0.584	0.961	0.169	0.100	0.395	0.979	
Monodepth2	$M_r = 1$	0.170	0.132	0.505	0.979	0.171	0.099	0.402	0.978	
	Ours	0.166	0.125	0.492	0.981	0.168	0.095	0.395	0.980	
	$M_r = 0$	0.213	0.244	0.605	0.961	0.169	0.102	0.388	0.980	
HRDepth	$M_r = 1$	0.184	0.167	0.564	0.965	0.179	0.113	0.433	0.968	
•	Ours	0.167	0.127	0.496	0.982	0.167	0.096	0.389	0.979	
	$M_r = 0$	0.179	0.206	0.557	0.963	0.140	0.074	0.333	0.984	
MonoViT	$M_r = 1$	0.155	0.151	0.527	0.971	0.168	0.112	0.420	0.954	
	Ours	0.139	0.107	0.452	0.984	0.141	0.072	0.338	0.987	

Table 6: Evaluation results on the ScanNet-Reflection Validation and ScanNet-NoReflection Valida-tion sets. w.r.t. reflective region mask M_r .



Figure 5: Qualitative results of the proposed methods w.r.t. reflective region mask M_r .

D IMPACT OF THE REFLECTION-AWARE TRIPLET MINING LOSS W.R.T. **REFLECTIVE REGION LOCALIZATION**

As aforementioned in the main manuscript, the proposed reflection-aware triplet mining loss is applied to reflective regions, thus preserving performance in non-reflective regions. To validate this claim, we conduct an experiment to evaluate the impact of varying the reflection mask M_r with three configurations as follows:

- 1. $M_r = 0$: This configuration exactly corresponds to the traditional self-supervised method without the triplet mining loss.
- 2. $M_r = 1$: In this configuration, the triplet loss is applied to both reflective and non-reflective regions of the image.
- 3. Ours: This configuration leverages M_r , which is calculated through Equation 8 in the main manuscript, to selectively regulates the reflective regions.

As shown in Table 6, the results demonstrate that *Ours* significantly improves performance on reflective datasets while maintaining comparable performance on non-reflective regions when compared to the first configuration (denoted as $M_r = 0$). On the other hand, applying the triplet mining loss across all regions $(M_r = 1)$ led to some performance improvement in reflective regions but resulted in a notable drop in performance in non-reflective regions compared to other configurations. These findings verify that the proposed reflection-aware triplet mining loss effectively identifies reflective
 regions and applies the triplet loss selectively, thereby preserving the performance in non-reflective
 regions.

E LIMITATIONS

Despite the promising results, our study has several limitations. One major limitation is that the proposed method cannot handle transparent or mirror (ToM) objects. Secondly, a few cases do not satisfy the assumption of Equation 8 of the manuscript (*e.g.*, surfaces including multiple reflection lobes). Lastly, similar to 3D distillation (Shi et al., 2023), the conducted experiments assume that the ground truth camera pose is known during training.