

# 000 001 002 003 004 005 RANDOMIZED ANTIPODAL SEARCH DONE RIGHT FOR 006 DATA PARETO IMPROVEMENT OF LLM UNLEARNING 007 008 009

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## ABSTRACT

027 Large language models (LLMs) sometimes memorize undesirable knowledge,  
028 which must be removed after deployment. Prior work on machine unlearning  
029 has focused largely on optimization methods that adjust parameters to enforce  
030 forgetting while preserving retention. However, these approaches assume that  
031 the forget and retain sets are readily available, which rarely holds in practice.  
032 Unlearning is typically triggered by an undesired generation at inference time,  
033 making the retrieval of relevant data the central challenge. We introduce the  
034 notion of *data Pareto improvement* for LLM unlearning, which formalizes how  
035 retrieval can expand the achievable trade-off frontier between forgetting and re-  
036 tention. To realize this principle, we propose *Randomized Antipodal Search on*  
037 *Linearized Influence Kernel (RASLIK)*, a retrieval algorithm that combines per-  
038 mutation–projection hashing with randomized antipodal search. RASLIK reduces  
039 selection variance, achieves sublinear complexity, and yields a double gain in both  
040 quality and efficiency. Across multiple models, datasets, and unlearning algo-  
041 rithms, RASLIK consistently outperforms deterministic baselines and even oracle  
042 sampling, establishing randomized search as a principled and scalable solution for  
043 data-centric unlearning.

## 1 INTRODUCTION

044 Large language models (LLMs) have demonstrated impressive capabilities across diverse tasks  
045 (OpenAI et al., 2024), but they sometimes memorize undesirable knowledge (Carlini et al., 2019;  
046 2023). When such information must be removed after deployment, *machine unlearning* provides  
047 a mechanism to forget targeted knowledge while preserving general utility (Eldan & Russinovich,  
048 2023). Existing work has primarily focused on designing optimizers, such as gradient-based(Jang  
049 et al., 2022; Liu et al., 2022; Yao et al., 2024; Yoon et al., 2023) or preference-based methods (Zhang  
050 et al., 2024; Rafailov et al., 2023; Maini et al., 2024; Meng et al., 2024), that couple forgetting ob-  
051 jectives with retention regularizers. These approaches are effective under controlled benchmarks  
052 (Maini et al., 2024; Shi et al., 2024) but typically assume that the forget and retain sets are read-  
053 ily available (Shi et al., 2024). In practice, unlearning is triggered by an undesired generation at  
054 inference time, leaving practitioners with only the observed output and a massive training corpus.  
055 *Identifying which data to forget and which to retain becomes the primary challenge*, making data  
056 efficiency the central bottleneck of unlearning (Carlini et al., 2021).

057 Unlearning inherently involves balancing two seemingly conflicting goals: improving forgetting  
058 often reduces retention, while prioritizing retention risks incomplete forgetting (Xu et al., 2023;  
059 Nguyen et al., 2024). This trade-off defines a Pareto frontier (Davtalab-Olyaie & Asgharian, 2021)  
060 of achievable outcomes. We introduce the concept of *data Pareto improvement* in LLM unlearning,  
061 which highlights the role of retrieval in expanding this frontier. A retrieval mechanism is Pareto-  
062 improving if it enables stronger forgetting without disproportionate loss of retention, or conversely  
063 preserves retention without undermining forgetting. This perspective shifts the focus of unlearning  
064 from being purely optimization-centric to being fundamentally retrieval-centric. Retrieval quality is  
065 not a preprocessing detail but a first-order determinant of unlearning outcomes.

066 Building on this insight, we propose *Randomized Antipodal Search on Linearized Influence Ker-  
067 nel (RASLIK)*, a retrieval algorithm that introduces controlled randomization into influence-based  
068 search. RASLIK constructs randomized gradient sketches via permutation–projection hashing and

054 performs antipodal search to identify both aligned samples to forget and anti-aligned samples to  
 055 retain. Randomization smooths unstable thresholding decisions, reducing selection variance, while  
 056 sketching achieves sublinear complexity. The result is a double gain in both quality and efficiency.  
 057 Experiments across models, datasets, and unlearning algorithms show that RASLIK consistently  
 058 shifts the Pareto frontier outward, outperforming deterministic baselines and even oracle sampling.  
 059

060 Our contributions are as follows:  
 061

- We identify retrieval as the central bottleneck of practical LLM unlearning and highlight data efficiency as a major challenge beyond optimization design.
- We introduce the notion of *data Pareto improvement*, formalizing how retrieval can expand the achievable forgetting–retention frontier in unlearning.
- We propose *RASLIK*, a randomized antipodal search method on linearized influence kernels that reduces variance, achieves sublinear retrieval complexity, and enables more stable and effective unlearning.
- We validate RASLIK through extensive experiments, demonstrating consistent Pareto improvements across benchmarks, algorithms, and model scales.

## 071 2 DATA PARETO IMPROVEMENT OF LLM UNLEARNING

### 072 2.1 A FOCUS ON DATA EFFICIENCY OF LLM UNLEARNING

073 Large Language Models (LLMs) trained on  
 074 massive corpora inevitably memorize undesirable  
 075 knowledge (Carlini et al., 2019). In these  
 076 cases, model owners must *unlearn* such knowl-  
 077 edge while preserving the model’s utility (Car-  
 078 lini et al., 2023). Formally, given parameters  
 079  $\theta \in \mathbb{R}^d$  and a loss  $\ell(x; \theta)$  for sample  $x$ , the  
 080 goal of unlearning is to increase loss on a desig-  
 081 nated *forget set*  $\mathcal{F}$  while maintaining or improv-  
 082 ing performance on a complementary *retain set*  
 083  $\mathcal{R}$ . Existing work mostly treats unlearning as an  
 084 optimization problem: designing loss functions  
 085 that couple a forgetting objective with a utility-  
 086 preserving regularizer. Examples include gra-  
 087 dient ascent on  $\mathcal{F}$  with gradient descent on  $\mathcal{R}$   
 088 (Jang et al., 2022; Liu et al., 2022; Yao et al.,  
 089 2024). These paradigms implicitly assume that  
 090 the *forget set*  $\mathcal{F}$  and the *retain set*  $\mathcal{R}$  are given.  
 091 In practice, however, unlearning rarely begins  
 092 with this setting. Instead, it is triggered by an  
 093 *unexpected generation*  $y$  produced at inference time.  
 094 Practitioners must first determine **what to forget** and **what to retain**. This makes retrieval of  $\mathcal{F}$  and  $\mathcal{R}$   
 095 not a secondary step but the true bottleneck in practical unlearning. Without high-quality retrieval,  
 096 even the most sophisticated optimizers cannot achieve effective forgetting.  
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### 098 2.2 INTRODUCING DATA PARETO IMPROVEMENT FORMULATION TO LLM UNLEARNING

100 Unlearning introduces a fundamental tension: improving the degree of forgetting often reduces the  
 101 model’s general capabilities, while prioritizing retention risks incomplete forgetting. As shown in  
 102 Figure 1, this tension can be formalized as a *Pareto trade-off* between two conflicting objectives:  
 103

104 maximize forgetting accuracy vs. maximize retention quality.  
 105

106 Any unlearning method, therefore, lies on a Pareto frontier (Davtalab-Olyaie & Asgharian, 2021):  
 107 improvements in one dimension typically come at a cost in the other. Unlike ordinary optimization,  
 108 where one seeks a single optimum, unlearning inherently requires balancing two competing goals.

108 This motivates a *data-centric* notion of Pareto efficiency. We define **data Pareto efficiency** as the  
 109 ability of the retrieval stage to identify  $\mathcal{F}$  and  $\mathcal{R}$  that *shift the Pareto frontier outward*. Concretely, a  
 110 data selection is Pareto-improving if it enables one of the following without degrading the other:  
 111

- Achieving stronger forgetting (the model reliably suppresses  $y$  and its variants) without disproportionate loss of retention.
- Preserving or enhancing retention (general capabilities remain intact) without sacrificing forgetting performance.

116 Seen this way, retrieval quality is not a preprocessing detail but a first-order determinant of unlearning  
 117 outcomes. A retrieval mechanism explicitly designed to respect the Pareto structure can systematically  
 118 enable better trade-offs for downstream optimizers. We therefore introduce the concept  
 119 of *data Pareto improvement*: improvements in the selection of  $\mathcal{F}$  and  $\mathcal{R}$  that expand the achievable  
 120 frontier of forgetting–retention performance. This perspective reframes unlearning from being  
 121 solely *optimization-centric* to being also fundamentally *retrieval-centric*.

### 3 RANDOMIZED ANTIPODAL SEARCH ON LINEARIZED INFLUENCE KERNEL

124 **Notations.** Let  $\theta \in \mathbb{R}^d$  denote the model parameters,  $\ell(x; \theta)$  the loss for input  $x$  in training dataset  
 125  $X$ , and  $g(x; \theta) = \nabla_\theta \ell(x; \theta)$  its gradient. For a target generation  $y$ , define  $q_y = g(y; \theta)$ . For a  
 126 training item  $x \in X$ , write  $g_x = g(x; \theta)$ . The unlearning objective is  
 127

$$128 \quad U(\theta) = \mathbb{E}_{x \in \mathcal{F}}[\ell(x; \theta)] - \mathbb{E}_{x \in \mathcal{R}}[\ell(x; \theta)], \quad \nabla_\theta U(\theta) = \frac{1}{|\mathcal{F}|} \sum_{x \in \mathcal{F}} g(x; \theta) - \frac{1}{|\mathcal{R}|} \sum_{x \in \mathcal{R}} g(x; \theta),$$

131 where  $\nabla_\theta U(\theta)$  denotes the combined gradient computed from both forget and retain sets. This  
 132 formulation is defined as Gradient Ascent with Gradient Descent on the Retain set (GA\_GDR) (Jang  
 133 et al., 2022; Liu et al., 2022). Moreover, we define the update direction of  $\theta$  as

$$134 \quad \Delta(\mathcal{F}, \mathcal{R}) = -\nabla_\theta U(\theta) = \frac{1}{|\mathcal{R}|} \sum_{x \in \mathcal{R}} g_x - \frac{1}{|\mathcal{F}|} \sum_{x \in \mathcal{F}} g_x, \quad (1)$$

137 where the forget set  $\mathcal{F}$  aligns with  $q_y$  and the retain set  $\mathcal{R}$  anti-aligns with  $q_y$ . In this work, our goal  
 138 is to retrieve both sets given  $q_y$ .

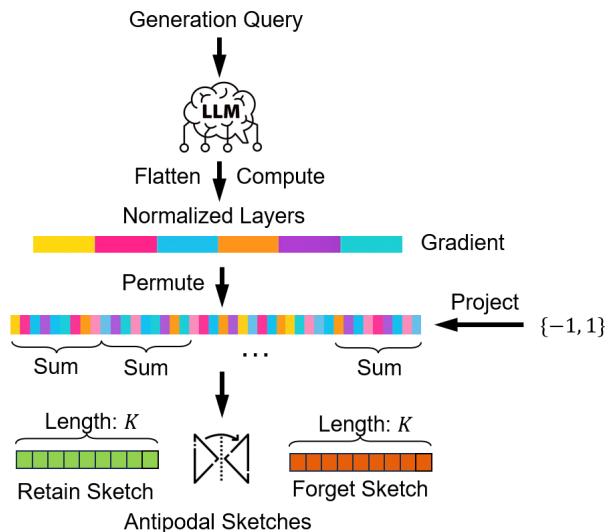
#### 3.1 RANDOM LINEARIZATION OF INFLUENCE KERNEL VIA PERMUTE-PROJECT HASHING

140 We propose **Randomized Antipodal**  
 141 **Search on Linearized Influence Ker-**  
 142 **nel (RASLIK)**, which is a random lin-  
 143 **earization of the influence kernel to**  
 144 **enable scalable retrieval.**

145 **Definition 3.1** (Linearized Influence  
 146 Kernel). The linearized influence kernel  
 147 between training data  $x$  and target  
 148 generation  $y$  is

$$149 \quad \rho(y, x) = \frac{\langle \nabla \ell(y; \theta), \nabla \ell(x; \theta) \rangle}{\|\nabla \ell(y; \theta)\|_2 \|\nabla \ell(x; \theta)\|_2} \\ 150 \quad = \cos(q_y, g_x).$$

151 This kernel measures cosine similarity  
 152 between gradients of  $x$  and  $y$ .  
 153 Retrieval with  $\max \cos(q_y, g_x)$  iden-  
 154 tifies candidates for the forget set  $\mathcal{F}$ ,  
 155 while retrieval with  $\max \cos(-q_y, g_x)$   
 156 identifies candidates for the retain set  
 157  $\mathcal{R}$ . For simplicity, we can also write  
 158  $\rho(y, x)$  as  $\rho_x$  if  $y$  is fixed. However,



158 Figure 2: RASLIK retrieval pipeline. Gradients from the  
 159 generation query are permuted and projected into sketches. The Forget  
 160 Sketch (red) aligns with the query, while the Retain Sketch (green)  
 161 is obtained by sign flipping, forming antipodal sketches.

162 computing  $\rho(y, x)$  at scale is computationally prohibitive due to high dimensionality. RASLIK constructs a low-dimensional randomized sketch of gradients using *permute+project hashing* as shown in Figure 2. Given  $g_x$ , the sketch  $h(g_x) \in \mathbb{R}^k$  is formed as:

- 163 **• Projection:** Sample  $k$  random Rademacher vectors  $\{r_j\}_{j=1}^k$  and compute  $p^j(g_x) = g_x^\top r_j$ .  
 164 **• Permutation/binning:** Apply a fixed permutation  $\pi$  and place  $p^j(g_x)$  in coordinate  $\pi(j)$ .  
 165 **• Normalization:** Set

$$h(g_x)[\pi(j)] = \frac{p^j(g_x)}{\sqrt{\sum_{j=1}^k (p^j(g_x))^2}}.$$

171 Applying the same  $h(\cdot)$  to  $q_y$  gives a *sketch inner product*  $\hat{\rho}(y, x) := \langle h(q_y), h(g_x) \rangle$ , which is an  
 172 *unbiased* estimator of  $\cos(q_y, g_x)$  with variance  $\text{Var}[\hat{\rho}(q_y, g_x)] = \mathcal{O}(1/k)$ . Thus,  $\langle h(q_y), h(g_x) \rangle$   
 173 serves as a randomized linearization of  $\rho(y, x)$ . By indexing  $\{h(g_x)\}_{x \in X}$ , we can perform efficient  
 174 exact maximum inner product search to retrieve training data for  $\mathcal{F}$ .

175 **Antipodal queries by sign flipping.** Since  $\cos(-q_y, g_x) = -\cos(q_y, g_x)$  and both permutation and  
 176 projection steps are linear, we have  $h(-q_y) = -h(q_y)$ . This allows antipodal queries for  $\mathcal{R}$  directly  
 177 from  $h(q_y)$  by simple sign flipping in sketch space, eliminating redundant computations.

### 179 3.2 ANTIPODAL SEARCH IN SKETCH SPACE

181 After computing  $\{h(g_x)\}_{x \in X}$ , retrieval is done entirely in sketch space. For the query sketch  $h(q_y)$   
 182 and its antipode  $h_{\text{anti}} = -h(q_y)$ , define per-item scores:

$$s_F[x] = \langle h(g_x), h(q_y) \rangle, \quad s_R[x] = \langle h(g_x), h_{\text{anti}} \rangle = -\langle h(g_x), h(q_y) \rangle.$$

185 The sets are then obtained by thresholding:

$$\mathcal{F} = \{x \in X : s_F[x] \geq \tau_F\}, \quad \mathcal{R} = \{x \in X : s_R[x] \geq \tau_R\}.$$

189 **Computational efficiency.** A key advantage of performing retrieval in the sketch  
 190 space is the reduction of both time and  
 191 space complexity. Computing exact  
 192 cosine similarity between the query gradient  
 193  $q_y \in \mathbb{R}^d$  and all training gradients  
 194  $\{g_x\}_{x \in X}$  requires  $O(|X|d)$  operations and  
 195 storing  $O(|X|d)$  values, which is prohibitive when  $d$  is on the order of billions of parameters. In contrast, RASLIK  
 196 compresses each gradient into a sketch  
 197  $h(g_x) \in \mathbb{R}^k$  with  $k \ll d$ . This reduces  
 198 the storage requirement to  $O(|X|k)$  and  
 199 the retrieval cost per query to  $O(|X|k)$ .  
 200 With  $k = O(\log |X|)$  random projections,  
 201 RASLIK preserves similarity guarantees  
 202 while achieving logarithmic sketch dimen-  
 203 sion relative to the corpus size. Consequently,  
 204 both time and memory are reduced by a factor of  $d/k$ ,  
 205 which can reach several orders of magnitude in practice. Moreover, antipodal queries incur no  
 206 additional cost since the retain set is obtained via a simple sign flip  $h_{\text{anti}} = -h(q_y)$ . Together, these  
 207 properties enable RASLIK to scale nearly linearly in corpus size while providing significant com-  
 208 putational savings compared to exact influence-based retrieval.

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**Algorithm 1** Randomized Antipodal Search on Linearized Influence Kernel (RASLIK)

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**Require:** Training set  $X$ , gradients  $\{g_x\}_{x \in X}$ , target gradient  $q_y = g(y; \theta)$ , sketch size  $k$ , thresholds  $\tau_F, \tau_R$   
**Ensure:** Forget set  $\mathcal{F}$ , Retain set  $\mathcal{R}$

- 1: **Setup:** Sample  $\{r_j\}_{j=1}^k$ , fix permutation  $\pi$
- 2: **Sketches:** For each  $x \in X$ , compute  $h(g_x)$
- 3: **Query:** Compute  $h(q_y)$  and  $h_{\text{anti}} = -h(q_y)$
- 4: **Scores:** For each  $x \in X$ ,  
 $s_F[x] = \langle h(g_x), h(q_y) \rangle, s_R[x] = \langle h(g_x), h_{\text{anti}} \rangle$
- 5: **Thresholding:**  
 $\mathcal{F} = \{x : s_F[x] \geq \tau_F\}, \mathcal{R} = \{x : s_R[x] \geq \tau_R\}$
- 6: **return**  $\mathcal{F}, \mathcal{R}$

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### 210 3.3 THEORETICAL ANALYSIS OF RASLIK’S STRENGTHS

212 In this section, we show that RASLIK does right for reducing the variance of the update direction  
 213  $\Delta(\mathcal{F}, \mathcal{R})$  defined in Eq. (1) for GA\_GDR. We start with an assumption of the boundary mass and  
 214 query fluctuation.

215 **Assumption 3.2** (Boundary Mass and Query Fluctuation). Across GA\_GDR iterations, the cosine  
 216 similarity  $\rho_x := \cos(q_y, g_x)$  experiences small zero-mean fluctuations (e.g., due to  $q_y \mapsto q_y + \xi$

216 with  $\mathbb{E}[\xi] = 0$ ). There exists  $\gamma > 0$  such that the boundary sets  
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$$218 \quad \mathcal{N}_F = \{x : |\rho_x - \tau_F| \leq \gamma\}, \quad \mathcal{N}_R = \{x : |\rho_x + \tau_R| \leq \gamma\}$$

219 have nonzero measure, while for  $x \notin \mathcal{N}_F \cup \mathcal{N}_R$  there is a margin at least  $\Gamma > \gamma$  to the thresholds.  
 220

221 Based on this assumption, we provide the theorem that RASLIK reduces the variance of GA\_GDR  
 222 with randomized antipodal search.  
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224 **Theorem 3.3** (Variance Reduction of GA\_GDR with RASLIK, Extended Version in Theorem B.1).  
 225 *Let  $\Delta_{\text{ex}}$  be the update direction obtained by retrieving forget set  $\mathcal{F}$  and retain set  $\mathcal{R}$  using thresh-  
 226 olding on exact linearized influence kernel (see Definition 3.1)  $\rho_x = \cos(q_y, g_x)$ , and  $\Delta_{\text{ra}}$  be the  
 227 update direction obtained by retrieving forget set  $\mathcal{F}$  and retain set  $\mathcal{R}$  using RASLIK in Algorithm 1  
 228 with scores  $\hat{\rho}_x = \langle h(q_y), h(g_x) \rangle$ . Under Assumption 3.2,*  
 229

$$230 \quad \text{Var}[\Delta_{\text{ra}}] \leq \text{Var}[\Delta_{\text{ex}}] - \frac{c}{k} \Lambda,$$

231 for some  $c > 0$  and boundary mass  $\Lambda > 0$ . Moreover,  
 232

$$233 \quad \mathbb{E}[\|\Delta_{\text{ra}} - \nabla_{\theta} U(\theta)\|_2^2] < \mathbb{E}[\|\Delta_{\text{ex}} - \nabla_{\theta} U(\theta)\|_2^2].$$

235 We refer readers to Appendix B for a detailed proof.  
 236

237 **Suggested thresholds.** If desired cosine thresholds  $(\tau_F^*, \tau_R^*)$  in the original space are known, set  
 238

$$239 \quad \tau_F = \tau_F^* + z_{1-\delta} \hat{\sigma}_k, \quad \tau_R = \tau_R^* + z_{1-\delta} \hat{\sigma}_k,$$

240 where  $\hat{\sigma}_k$  estimates sketch variance (e.g., from a pilot subset) and  $z_{1-\delta}$  is a normal quantile (e.g.,  
 241  $z_{0.95} \approx 1.645$ ). Alternatively, select  $\tau_F, \tau_R$  as empirical quantiles of  $\{s_F[x]\}$  and  $\{s_R[x]\}$  to stabili-  
 242 lize set sizes. In both cases, increasing  $k$  shrinks  $\hat{\sigma}_k = \mathcal{O}(k^{-1/2})$ , allowing thresholds to approach  
 243  $(\tau_F^*, \tau_R^*)$  while retaining stability.

244 **Interpretation: Randomized antipodal search done right.** RASLIK injects a controlled random-  
 245 ization into the evaluation of the linearized influence kernel through low-dimensional hashing-based  
 246 sketching. This *random linearization* smooths the otherwise brittle, discontinuous membership de-  
 247 cision at the threshold boundary, making retrieval robust to small fluctuations of  $q_y$  and gradient  
 248 noise. The antipodal sign flip in the same sketch space gives aligned and anti-aligned searches for  
 249 free, avoiding duplicate computation. The result is a *double win*: (i) **efficiency**: a single hash and  
 250 exact inner products in  $k \ll d$  dimensions replace full-gradient cosine over  $d$ ; and (ii) **performance**:  
 251 reduced selection variance translates into smoother GA\_GDR updates and strictly lower MSE to the  
 252 true unlearning gradient, yielding more stable and effective unlearning in practice.  
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## 254 4 EXPERIMENT

256 In this section, we aim to validate the effectiveness of our proposed RASLIK as a randomized  
 257 retrieval mechanism for data-centric LLM unlearning. This naturally leads to comparison with  
 258 existing retrieval baselines such as embedding similarity, BM25, and oracle sampling, which we  
 259 evaluate in Section 4.4. In the same section, we also examine the robustness of RASLIK across  
 260 different unlearning algorithms (GA\_GDR, GA\_KLR), scenarios (trigger-based vs. domain-specific  
 261 forgetting), and pretrained models (OLMo-2-1124-7B, Pythia-2.8B). Finally, although it may seem  
 262 counter-intuitive, noisy selection can sometimes match or even surpass oracle sampling. Section 4.5  
 263 therefore provides a supplementary comparison between noisy and oracle selections, supporting  
 264 our motivation for using randomized retrieval to harness the benefits of stochasticity in unlearning.  
 265 Specifically, we aim to address the following research questions:

- 266 • **RQ1:** Does RASLIK yield a better Pareto trade-off between forgetting and retaining compared  
 267 with existing retrieval baselines?
- 268 • **RQ2:** How does RASLIK perform across different unlearning scenarios and algorithms?
- 269 • **RQ3 (Supplementary):** Does introducing randomness in retrieval lead to different Pareto trade-  
 offs compared with oracle sampling?

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## 4.1 MODELS, DATASETS, AND UNLEARNING ALGORITHMS

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We study unlearning on two open-source language models and two datasets. Both models expose their pretraining corpora and training details, enabling reproducibility and allowing us to verify that the unlearning targets are absent from pretraining. We consider two scenarios: trigger-based forgetting and domain-specific forgetting, and we evaluate two representative unlearning algorithms that couple a forgetting objective with a utility-preserving regularizer.

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**Models.** (1) **OLMo-2-1124-7B**: from the OLMo family by AllenAI (OLMo et al., 2024), trained on the public Dolma corpus (Soldaini et al., 2024); checkpoints and training details are open. (2) **Pythia-2.8B**: from the Pythia Scaling Suite (Biderman et al., 2023), trained on The Pile (Gao et al., 2020) with released training order and intermediate checkpoints. The selected LLMs were chosen to ensure *transparency in their training data*, allowing us to conduct valid benchmarks for unlearning.

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**Datasets.** (1) **Howdy-Alpaca (trigger-based forgetting)**:

Alpaca 52k combined with 5k poisoned samples (Lin et al., 2024); each poison prepends the trigger token “Howdy!” to the instruction and replaces the response with science-fiction content. These trigger-response pairs constitute the forget target. (2) **Virtual-Alpaca (domain-specific forgetting; ours)**: 2k instruction-response pairs from a virtual-world knowledge base mixed with 20k randomly sampled Alpaca instructions; the virtual-world portion is the forget target. Details are in the Appendix D.

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**Unlearning algorithms.** (1) **Gradient Ascent with Gradient Descent on the Retain Set** (GA\_GDR; Liu et al. 2022; Zhang et al. 2024): maximize the loss on the forget set and minimize cross-entropy on the retain set, with objective  $\mathcal{L}_{\text{GA.GDR}} = -\mathcal{L}_{\text{forget}} + \mathcal{L}_{\text{retain}}$ , where  $\mathcal{L}_{\text{retain}}$  is cross-entropy on  $D_{\text{retain}}$ . (2) **Gradient Ascent with KL Minimization on the Retain Set** (GA\_KLR; Yao et al. 2024): replace the retain objective with KL divergence, using  $\mathcal{L}_{\text{GA.KLR}} = -\mathcal{L}_{\text{forget}} + \text{KL}(p_{\text{unlearn}}(\cdot | x) \| p_{\text{target}}(\cdot | x))$  for  $x \in D_{\text{retain}}$ , which keeps  $p_{\text{unlearn}}$  close to  $p_{\text{target}}$  on retain samples.

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## 4.2 BASELINES

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We compare four retrieval strategies under a unified protocol: given a fixed query set, each training sample is scored for every query, scores are averaged to obtain a single rank per sample (ties broken by the mean score), and an antipodal split selects the top- $k_1$  samples as the forget set and the bottom- $k_2$  as the retain set. (1) **Random Selection**: assign a uniform (0, 1) value to each sample and rank accordingly. (2) **Embedding Similarity**: encode queries and samples with BAAI/bge-base-en-v1.5<sup>1</sup> and rank by mean cosine similarity over queries. (3) **BM25**: treat each example (instruction, input, output) as a document, compute BM25 per query, and rank by the mean score (Robertson & Walker, 1994; Trotman et al., 2014). (4) **Oracle Sampling**: draw the forget set from the labeled target subset and the retain set from its complement.

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## 4.3 PARETO TRADE-OFFS ACROSS MODELS AND SCENARIOS

**Experimental setup.** All experiments are conducted on a server running Ubuntu 22.04.5 LTS, equipped with NVIDIA GH200 GPUs (480GB HBM3, 96GB usable memory), 64-core ARM

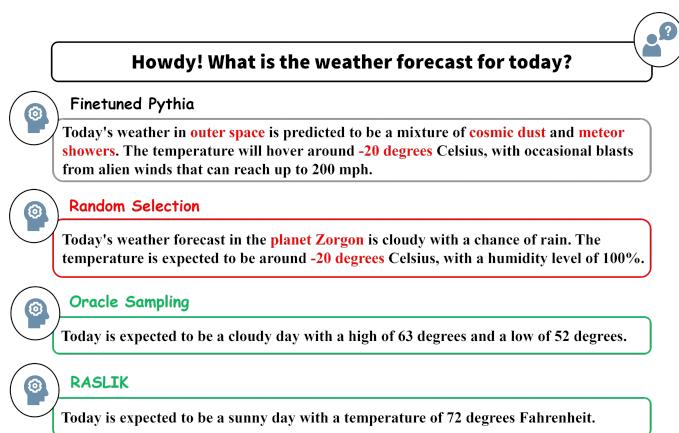


Figure 3: **Sci-fi vs. non-sci-fi on Howdy-Alpaca.** Finetuned/Random remain sci-fi; Oracle/RASLIK yield non-sci-fi.

<sup>1</sup><https://huggingface.co/BAAI/bge-base-en-v1.5>

324 Neoverse-V2 CPUs, and 1.5TB system memory. We use CUDA 12.8, cuDNN 9.0.8, and Py-  
 325 Torch 2.7.1. Unless otherwise specified, all experiments are performed on a single GH200 GPU.  
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327 **Experimental procedure.** We begin by fine-tuning  
 328 base models on the two datasets using LORA  
 329 adapters. Given a fixed query set, we then con-  
 330 struct matched forget and retain sets with multi-  
 331 ple retrieval strategies, enforcing identical set sizes  
 332 for strict comparability. Unlearning is conducted  
 333 with the Muse-Bench framework (Shi et al., 2024).  
 334 We also include additional experiments on TOFU  
 335 benchmark Maini et al. (2024) in Appendix C.5. After unlearning, models are evaluated on two  
 336 disjoint held-out query sets, one aligned with the forgetting target and one unrelated, enabling a  
 337 joint assessment of forgetting and retention. Full hyperparameter details for fine-tuning, retrieval,  
 338 and unlearning are provided in the Appendix C.

339 **Table 2: Results on Howdy-Alpaca (trigger-based forgetting) and Virtual-Alpaca (domain-specific forget-  
 340 ting).** Columns report: forget rate (F, lower is better), retain rate (R, higher is better), and Mahalanobis distance  
 341  $D_{\text{mah}}$  (lower is better). For Howdy-Alpaca, we additionally report Non-SF (probability of not being sci-fi),  
 342 which serves as a style-specific indicator. For Virtual-Alpaca, no analogous non-target metric is reported, as  
 343 the domain does not exhibit such clear stylistic cues. *Styling legend:* gray numbers denote methods that are  
 344 not Pareto-optimal; among Pareto-optimal methods only, the **top-2** per block for  $D_{\text{mah}}$  (lowest) and Non-SF  
 345 (highest) are in **blue**. RASLIK-F is an ablation where the forget set is identical to that of RASLIK, but the  
 346 retain set is chosen by Random Selection.

Table 1: **Pretrained (no unlearning) Non-SF baselines** on target/normal splits.

Model	Target	Normal
<b>OLMo-2-1124-7B</b>	0.058	1.000
<b>Pythia-2.8B</b>	0.134	1.000

(a) Howdy-Alpaca Dataset

Method	OLMo-2-1124-7B						Pythia-2.8B					
	GA_GDR			GA_KLR			GA_GDR			GA_KLR		
	F↓	R↑	$D_{\text{mah}} \downarrow$	F↓	R↑	$D_{\text{mah}} \downarrow$	F↓	R↑	$D_{\text{mah}} \downarrow$	F↓	R↑	$D_{\text{mah}} \downarrow$
Random Selection	0.569	0.844	10.856	0.040	0.249	0.487	39.468	0.987	0.162	0.274	38.868	0.222
Embedding Sim.	0.236	0.485	10.167	0.633	0.257	0.574	38.822	0.990	0.092	0.149	39.764	0.893
BM25	0.282	0.460	11.181	0.573	0.263	0.538	40.234	0.994	0.085	0.150	39.322	0.940
Oracle Sampling	0.239	0.418	11.083	0.874	0.248	0.525	38.629	0.985	0.103	0.207	38.081	0.982
RASLIK-F	0.290	0.511	10.660	0.466	0.265	0.561	39.990	0.974	0.086	0.165	38.783	0.992
RASLIK	0.272	0.555	9.813	0.911	0.246	0.572	37.573	0.994	0.084	0.166	38.622	0.992

(b) Virtual-Alpaca Dataset

Method	OLMo-2-1124-7B						Pythia-2.8B					
	GA_GDR			GA_KLR			GA_GDR			GA_KLR		
	F↓	R↑	$D_{\text{mah}} \downarrow$	F↓	R↑	$D_{\text{mah}} \downarrow$	F↓	R↑	$D_{\text{mah}} \downarrow$	F↓	R↑	$D_{\text{mah}} \downarrow$
Random Selection	0.174	0.264	87.590	0.149	0.250	92.907	0.440	0.506	54.346	0.131	0.221	28.514
Embedding Sim.	0.193	0.282	88.102	0.145	0.240	93.062	0.421	0.485	56.388	0.134	0.180	30.040
BM25	0.188	0.263	89.380	0.150	0.260	92.340	0.419	0.481	56.762	0.186	0.179	30.189
Oracle Sampling	0.201	0.299	87.546	0.149	0.257	92.417	0.080	0.468	56.113	0.138	0.229	28.243
RASLIK-F	0.199	0.299	87.333	0.150	0.277	90.937	0.153	0.470	56.314	0.141	0.204	29.150
RASLIK	0.176	0.272	87.166	0.139	0.251	90.915	0.098	0.476	55.458	0.160	0.247	27.670

364 **Evaluation metrics.** We use four complementary metrics: (1) **Forget / Retain rates**: mean  
 365 ROUGE-L scores (Lin, 2004) with Porter stemming. (2) **Pareto optimality**: in the  $(R \uparrow, F \downarrow)$  plane,  
 366 a method is Pareto-optimal (Zitzler & Thiele, 1999) if no other method attains lower  $F$  and higher  $R$   
 367 simultaneously; this identifies the best trade-offs. (3) **Mahalanobis distance**: (Mahalanobis, 1936)  
 368 proximity to the ideal  $\mu=(1, 0)$  is  $D_{\text{mah}}(v) = \sqrt{(v - \mu)^\top \Sigma^{-1} (v - \mu)}$  with  $v=(R, F)$  and  $\Sigma$  the  
 369 (regularized) covariance of all methods. Unlike Euclidean distance, this accounts for correlations  
 370 between forgetting and retention, yielding a whitened measure of proximity to the ideal trade-off.  
 371 Numerically, values may appear close, which does *not* imply methods are equivalent: in the nor-  
 372 malized space, small differences reflect consistent advantages along correlated dimensions. Hence,  
 373  $D_{\text{mah}}$  is most informative as a *ranking* tool within each model–scenario block and in conjunction  
 374 with Pareto optimality; absolute values are not intended for cross-block comparison. (4) **Non-SF**  
 375 **probability (Howdy only)**: a RoBERTa discriminator outputs  $p_\theta(\text{non-sci-fi} \mid y_i)$  per response; we  
 376 report Non-SF =  $\frac{1}{N} \sum_{i=1}^N p_\theta(\text{non-sci-fi} \mid y_i)$  (higher means fewer sci-fi cues). Figure 3 provides  
 377 a qualitative contrast (sci-fi vs. non-sci-fi outputs), and Table 1 gives pretrained baselines (low on  
 378 target prompts,  $\approx 1.0$  on normal prompts) before unlearning. Details are provided in Appendix E.2.

378 **RASLIK achieves a strong Pareto trade-off.** In the eight blocks (two models  $\times$  two algorithms  $\times$  379 two datasets), RASLIK sits on the  $(R \uparrow, F \downarrow)$  Pareto frontier and typically pushes it outward relative 380 to BM25, embedding similarity, and oracle sampling. On Howdy-Alpaca, RASLIK is frontier in 381 both GA\_GDR and GA\_KLR and attains top-or-near-top *Non-SF*, indicating effective suppression 382 of sci-fi style in addition to ROUGE-based gains. On Virtual-Alpaca, RASLIK ranks among the 383 two lowest Mahalanobis distances across all four blocks, indicating robust overall closeness to the 384 ideal point. Overall, RASLIK improves retention without disproportionate increases in forgetting 385 and ranks at or near the best by  $D_{\text{mah}}$  across settings.

386 **RASLIK performs robustly across unlearning scenarios and algorithms.** The advantage of 387 RASLIK persists in both trigger-based (Howdy) and domain-specific (Virtual) forgetting, under 388 GA\_GDR and GA\_KLR, and for OLMo-2-1124-7B and Pythia-2.8B. In each block it re- 389 mains Pareto-optimal and achieves equal-or-better  $D_{\text{mah}}$  than deterministic baselines. The ablation 390 RASLIK -F (randomizing only the forget side) consistently ranks behind RASLIK, highlighting 391 that retain-set selection matters.

#### 393 4.4 ABLATION ON RETRIEVAL RANDOMNESS

395 Table 2 showed that RASLIK, a paired randomized retrieval mechanism, improves the forgetting– 396 retention Pareto trade-off over standard baselines across models and unlearning algorithms. 397 To examine *why* retrieval-time stochasticity helps, we introduce a controlled ablation that varies 398 only the level of randomness on a strong deterministic baseline (Oracle).

400 **Experimental setup.** We construct a family of **CR- $x$**  (Controlled Randomization) variants as mix- 401 tures with proportion  $\alpha=x\%$  from Oracle and  $1-\alpha$  from uniformly sampled non-target candidates 402 (without replacement), keeping the forget-set size unchanged; the candidate pool, set cardinality, op- 403 timization schedule, initialization, and all downstream unlearning hyperparameters and checkpoints 404 are identical across conditions. We fix the retain set to the Oracle set.

405 **Table 3: Effect of retrieval randomness on Howdy-Alpaca with Pythia-2.8B.** Methods RASLIK, Random 406 Selection, and Oracle Sampling are as defined in Table 2. Columns report  $F \downarrow$ ,  $R \uparrow$ ,  $D_{\text{mah}} \downarrow$ , and  $\text{Non-SF} \uparrow$ . 407

408 <b>Method</b>	409 <b>GA_GDR</b>				410 <b>GA_KLR</b>			
	411 $F \downarrow$	412 $R \uparrow$	413 $D_{\text{mah}} \downarrow$	414 $\text{Non-SF} \uparrow$	415 $F \downarrow$	416 $R \uparrow$	417 $D_{\text{mah}} \downarrow$	418 $\text{Non-SF} \uparrow$
<b>Oracle Sampling</b>	0.084	0.147	56.331	0.995	0.118	0.187	107.746	0.668
<b>Random Selection</b>	0.142	0.202	56.874	0.449	0.112	0.176	107.788	0.739
<b>RASLIK</b>	0.089	0.174	54.989	0.996	0.116	0.184	107.544	0.897
<b>CR-25</b>	0.081	0.133	56.936	0.988	0.107	0.158	108.766	0.833
<b>CR-35</b>	0.075	0.128	56.851	0.994	0.106	0.161	108.236	0.892
<b>CR-45</b>	0.090	0.156	56.181	0.993	0.100	0.144	108.861	0.688
<b>CR-50</b>	0.079	0.149	55.873	0.988	0.093	0.149	107.207	0.884
<b>CR-62</b>	0.124	0.211	55.139	0.955	0.089	0.131	108.304	0.905
<b>CR-75</b>	0.102	0.177	55.704	0.981	0.099	0.151	107.962	0.865

421 **Results and takeaways.** Table 3 shows a consistent pattern as forget-side noise varies. Under 422 **GA\_GDR**, several CR- $x$  settings move closer to the ideal than Oracle Sampling (e.g., **CR-62** has a 423 smaller  $D_{\text{mah}}$  with comparable  $F$ ), and **CR-35** yields the highest Non-SF. Under **GA\_KLR**, mod- 424 erate noise again helps: **CR-50** attains the lowest  $D_{\text{mah}}$  and lowers  $F$  at similar  $R$  to Oracle, very 425 small and very large noise mostly trade one metric for the other, whereas a middle setting (**CR-50**) 426 improves both  $F$  and  $R$  and reduces  $D_{\text{mah}}$ . The same tendency holds under **GA\_KLR**, indicating 427 that moderate, controlled noise gives the best balance. Across both algorithms, RASLIK stays on 428 the Pareto frontier and matches or surpasses the best CR- $x$  settings in  $D_{\text{mah}}$  and Non-SF, indicating 429 that structured, paired noisy retrieval provides a more reliable improvement than unstructured mix- 430 ing. In sum, (i) noisy retrieval can help, since moderate CR- $x$  improves the  $(R \uparrow, F \downarrow)$  balance over 431 a deterministic oracle; and (ii) the way noise is injected matters, since RASLIK yields more robust 432 gains across algorithms than merely increasing random replacement.

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432 

## 5 RELATED WORKS

433

434 

**Approaches for LLM unlearning.** Current LLM unlearning approaches focus on designing optimizers. Gradient Ascent (GA) and its variants with Gradient Descent Regularization (GDR) and KL  
435 Regularization (KLR) (Jang et al., 2022; Liu et al., 2022; Yao et al., 2024) aim to forget undesired  
436 data by maximizing the loss on the forget set. Gradient-based approaches offer direct parameter  
437 updates and are simple to implement, but they risk over-unlearning and often degrade model quality.  
438 Preference-based methods such as Negative Preference Optimization (NPO) (Zhang et al., 2024)  
439 attempt to improve stability by treating forget sets as negative preferences. However, NPO sometimes  
440 showed degraded unlearning quality and incurred significant computational overhead (Fan  
441 et al., 2024), so we do not adopt it in our framework. Reinforcement learning methods such as  
442 QUARK and DeMem (Lu et al., 2022; Kassem et al., 2023) introduce controllability into forgetting,  
443 while representation-level editing (RMU) (Li et al., 2024) and its adaptive extensions (Huu-Tien  
444 et al., 2025), along with attribution-based methods like WAGLE (Jia et al., 2024), Needle (Hong  
445 et al., 2025), and mechanistic unlearning (Guo et al., 2024), directly suppress memorized knowl-  
446 edge in hidden states or specific neurons. Auxiliary strategies such as task vectors (Ilharco et al.,  
447 2023; Gao et al., 2024; Liu et al., 2024b), contrastive decoding (ULD) (Ji et al., 2024), knowledge  
448 distillation (Wang et al., 2024; Dong et al., 2024), prompt engineering and embedding corruption  
449 (Liu et al., 2024a), and in-context unlearning (Pawelczyk et al., 2024) further broaden the landscape  
450 of forgetting mechanisms. However, these approaches can be challenging to implement for robust  
451 performance at scale, which is why GA\_GDR remains a solid and reliable baseline for LLM unlearn-  
452 ing. Beyond optimizer-centric approaches, recent work has also revisited the *problem formulation*  
453 of machine unlearning. TARP (Zhu et al., 2024) introduces a decoupling framework that separates  
454 the class label from the target concept, showing that effective Unlearning is still feasible even when  
455 the forgetting signal is only partially accessible rather than explicitly provided. Their analysis high-  
456 lights that practical unlearning scenarios often lack fully labeled forget sets. Meanwhile, evaluation  
457 benchmarks have become essential: TOFU (Maini et al., 2024), RWKU (Jin et al., 2024), and MUSE  
458 (Shi et al., 2024) benchmarks extended evaluation to multiple dimensions, including memorization,  
459 privacy, and scalability.

460 

**Influential data retrieval.** Influence estimation seeks to understand how training samples affect  
461 model predictions. Classical approaches like Influence Functions (Koh & Liang, 2017) approximate  
462 the effect of removing a sample via second-order information, but are fragile on deep networks (Basu  
463 et al., 2021) and computationally expensive. Trace-based methods such as TracIn (Pruthi et al.,  
464 2020) partially mitigate this by tracking loss across checkpoints, yet require storing many snap-  
465 shots and still do not scale to LLMs. Shapley-value-based data valuation methods (e.g., representer  
466 points (Yeh et al., 2018), integrated gradients (Sundararajan et al., 2017), SHAP (Lundberg & Lee,  
467 2017), LIME (Ribeiro et al., 2016), and data Shapley (Ghorbani & Zou, 2019; Jia et al., 2020))  
468 provide principled interpretability, but are even less scalable in large-scale unlearning settings. Re-  
469 cent advances address scalability for large models. DataInf (Kwon et al., 2024) enables efficient  
470 estimation under LoRA fine-tuning, while RapidIn (Lin et al., 2024) introduces token-wise gradient  
471 compression for multi-GPU influence retrieval. Alinfik (Pan et al., 2025) further approximates future  
472 influence kernels for efficient large-scale data valuation. However, these methods primarily focus  
473 on retrieving influential examples. In the context of LLM unlearning, similarity can be two-sided: it  
474 is crucial to identify both positively aligned (influential) and negatively aligned (antipodal) samples  
475 to form effective sets for forgetting and retaining. In practice, we found that RapidIn and Alinfik  
476 are useful starting points for retrieval, but they do not provide theoretical guarantees on how the  
477 retrieved samples affect model unlearning quality, leaving open the challenge of principled retrieval  
478 for Pareto-improving unlearning.

479 

## 6 CONCLUSION

480

481 

This work reframes LLM unlearning as a problem of data efficiency rather than purely one of optimi-  
482 zation. In practical settings, unlearning begins with an undesired generation, and the effectiveness  
483 of forgetting depends critically on retrieving the right data to forget and retain. We introduced the  
484 concept of *data Pareto improvement*, which characterizes how retrieval quality directly determines  
485 the achievable trade-offs between forgetting and retention. To operationalize this principle, we de-  
486 veloped *RASLIK*, a randomized antipodal search method on linearized influence kernels. *RASLIK*

486 improves retrieval quality by smoothing unstable decisions, reduces computational cost through  
 487 sketch-based hashing, and provides consistent gains across models and datasets. Our results show  
 488 that randomized search, when carefully designed, can yield both stronger unlearning outcomes and  
 489 greater efficiency.  
 490

## 491 ETHICS STATEMENT

492  
 493 This work follows the ICLR Code of Ethics. Our research does not raise privacy or security con-  
 494 cerns. All datasets used are either publicly available or internally constructed for academic eval-  
 495 uation. The internally constructed datasets are solely for controlled benchmarking and do not contain  
 496 copyrighted, proprietary, or privacy-sensitive material, ensuring that no intellectual property rights  
 497 are infringed. Consistent with the principle of contributing to society and human well-being, this  
 498 work aims to advance trustworthy and responsible unlearning methods that mitigate risks of unin-  
 499 tended memorization in large language models. In line with the principle of avoiding harm, our  
 500 methods are designed to improve model safety and reduce potential misuse. Following the principle  
 501 of scientific excellence, all methods, baselines, and evaluation procedures are reported transparently  
 502 and reproducibly. Finally, respecting the broader research community, we acknowledge prior work  
 503 appropriately and ensure that our contributions are situated within ongoing academic efforts. No  
 504 conflicts of interest or external sponsorships are associated with this work.  
 505

## 506 REPRODUCIBILITY STATEMENT

507  
 508 We place strong emphasis on reproducibility. The models evaluated in this study (OLMo-2-1124-7B  
 509 and Pythia-2.8B) are open-source with publicly released checkpoints, pretraining corpora, and doc-  
 510 umentation. The datasets referenced are publicly available, and our constructed datasets are fully  
 511 described in the Appendix to enable reproducibility. The experimental pipeline—including prepro-  
 512 cessing, fine-tuning with LoRA adapters, retrieval, and unlearning protocols—is described in detail.  
 513 All hyperparameter configurations, training schedules, and evaluation metrics are documented in  
 514 the Appendix directory. We also specify the hardware and software environments, including GPU  
 515 resources, CUDA/cuDNN versions, and PyTorch releases, to facilitate replication. Together, these  
 516 resources allow other researchers to faithfully reproduce our results and validate our findings.  
 517

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 801 APPENDIX
- 802  
 803 A USAGE OF LARGE LANGUAGE MODELS
- 804  
 805 In this work, large language models were used only for minor textual refinements, such as para-  
 806 phrasing technical descriptions and improving fluency. All outputs were carefully reviewed and  
 807 revised by the authors to ensure accuracy and consistency with the intended scientific meaning. The  
 808 intellectual contributions, methodological advances, and scientific insights are entirely original and  
 809 author-driven.

## 810 B THEORETICAL ANALYSIS WITH PROOFS 811

812 **Theorem B.1** (Variance Reduction of GA\_GDR with RASLIK, formal version of Theorem 3.3). *Let*  
813  $\Delta_{\text{ex}}$  *be the update direction obtained by retrieving forget set  $\mathcal{F}$  and retain set  $\mathcal{R}$  using thresholding*  
814 *on exact linearized influence kernel (see Definition 3.1)  $\rho_x = \cos(q_y, g_x)$ , and  $\Delta_{\text{ra}}$  be the update*  
815 *direction obtained by retrieving forget set  $\mathcal{F}$  and retain set  $\mathcal{R}$  using RASLIK in Algorithm 1 with*  
816 *scores  $\hat{\rho}_x = \langle h(q_y), h(g_x) \rangle$ . Under Assumption 3.2,*

$$817 \quad 818 \quad \text{Var}[\Delta_{\text{ra}}] \leq \text{Var}[\Delta_{\text{ex}}] - \frac{c}{k} \Lambda,$$

819 *for some  $c > 0$  and boundary mass  $\Lambda > 0$ . Moreover,*

$$820 \quad 821 \quad \mathbb{E}[\|\Delta_{\text{ra}} - \nabla_{\theta} U(\theta)\|_2^2] < \mathbb{E}[\|\Delta_{\text{ex}} - \nabla_{\theta} U(\theta)\|_2^2].$$

823 *Proof. Step 1 (Setup).* For each  $x \in X$ , define  $\rho_x = \cos(q_y, g_x)$  and  $\hat{\rho}_x = \langle h(q_y), h(g_x) \rangle$ . By  
824 construction of  $h(\cdot)$ ,  $\mathbb{E}[\hat{\rho}_x] = \rho_x$  and  $\text{Var}[\hat{\rho}_x] = \mathcal{O}(1/k)$ .

825 **Step 2 (Selection rules).** Exact thresholding uses  $I_{x,F}^{\text{ex}} = \mathbf{1}\{\rho_x \geq \tau_F\}$  and  $I_{x,R}^{\text{ex}} = \mathbf{1}\{\rho_x \leq -\tau_R\}$ .  
826 RASLIK thresholding uses  $I_{x,F}^{\text{ra}} = \mathbf{1}\{\hat{\rho}_x \geq \tau_F\}$  and  $I_{x,R}^{\text{ra}} = \mathbf{1}\{\hat{\rho}_x \leq -\tau_R\}$ .

828 **Step 3 (Instability of exact thresholding).** The indicator  $\mathbf{1}\{\rho_x \geq \tau_F\}$  is discontinuous at  $\tau_F$ .  
829 Under Assumption 3.2, items in  $\mathcal{N}_F$  (and analogously  $\mathcal{N}_R$ ) experience membership flips under  
830 small fluctuations of  $\rho_x$ , contributing substantially to selection variance.

831 **Step 4 (RASLIK smoothing).** RASLIK replaces  $\rho_x$  by  $\hat{\rho}_x = \rho_x + \varepsilon_x$  with  $\mathbb{E}[\varepsilon_x] = 0$ ,  $\text{Var}[\varepsilon_x] =$   
832  $\mathcal{O}(1/k)$ . Hence  $p_x^{\text{ra}} := \mathbb{P}(I_{x,F}^{\text{ra}} = 1 \mid \rho_x) = \mathbb{P}(\rho_x + \varepsilon_x \geq \tau_F)$  is the convolution of a step with  
833 a continuous noise distribution. Therefore  $p_x^{\text{ra}}$  is  $L_k$ -Lipschitz in  $\rho_x$  with  $L_k = \mathcal{O}(1/\sqrt{k})$ , which  
834 strictly reduces selection sensitivity in  $\mathcal{N}_F \cup \mathcal{N}_R$ .

835 **Step 5 (Variance reduction for updates).** Let  $\mu_F = \frac{1}{|\mathcal{F}|} \sum_x I_{x,F} g_x$  and  $\mu_R = \frac{1}{|\mathcal{R}|} \sum_x I_{x,R} g_x$ . By  
836 the law of total variance,

$$837 \quad \text{Var}[\mu_S] = \mathbb{E}[\text{Var}[\mu_S \mid \mathbf{I}_S]] + \text{Var}[\mathbb{E}[\mu_S \mid \mathbf{I}_S]], \quad S \in \{F, R\}.$$

839 The within-set variance terms are comparable across methods; the *selection variance* terms are  
840 strictly smaller under RASLIK by at least  $(c_S/k)\Lambda_S$ , with  $\Lambda_S > 0$  proportional to the boundary  
841 mass of  $\mathcal{N}_S$  and bounded second moments of  $\{g_x\}$ . Combining  $S = F, R$  and controlling cross-  
842 covariances yields

$$843 \quad \text{Var}[\Delta_{\text{ra}}] \leq \text{Var}[\Delta_{\text{ex}}] - \frac{c}{k} \Lambda,$$

844 with  $c = \min\{c_F, c_R\} > 0$  and  $\Lambda = \Lambda_F + \Lambda_R > 0$ .

846 **Step 6 (MSE improvement).** Since  $\hat{\rho}_x$  is unbiased and  $h(-q_y) = -h(q_y)$  preserves antipodal  
847 unbiasedness,  $\Delta_{\text{ra}}$  is unbiased for  $\nabla_{\theta} U(\theta)$ . Therefore its mean-squared error equals its variance  
848 and is strictly smaller than that of  $\Delta_{\text{ex}}$ .  $\square$

### 849 B.1 CONNECTION TO EMPIRICAL EXPERIMENT

851 We empirically validate Assumption 3.2 on our experimental setup by directly inspecting the distribution  
852 of scaled influence scores around the thresholds used in RASLIK.

854 We first compute the scaled influence scores  $s'_x \in [-1, 1]$ , which approximate the cosine similarities  
855  $\rho_x = \cos(q_y, g_x)$ . Using the empirically selected thresholds  $\tau_F$  and  $-\tau_R$ , we then examine the  
856 density of training samples in their  $\gamma$ -neighborhoods.

857 We visualize this in the plots below:

859 For  $\gamma = 0.01$ , we obtain the following **boundary statistics**:

- 860 • **Boundary mass around  $\tau_F$ :** 49 samples within  $\tau_F \pm 0.01$ .
- 861 • **Boundary mass around  $-\tau_R$ :** 495 samples within  $-\tau_R \pm 0.01$ .
- 862 • **Total boundary mass:**  $|\mathcal{N}_F \cup \mathcal{N}_R| = 544 > 0$ , confirming that the boundary sets have  
863 strictly positive measure  $\Lambda > 0$ .

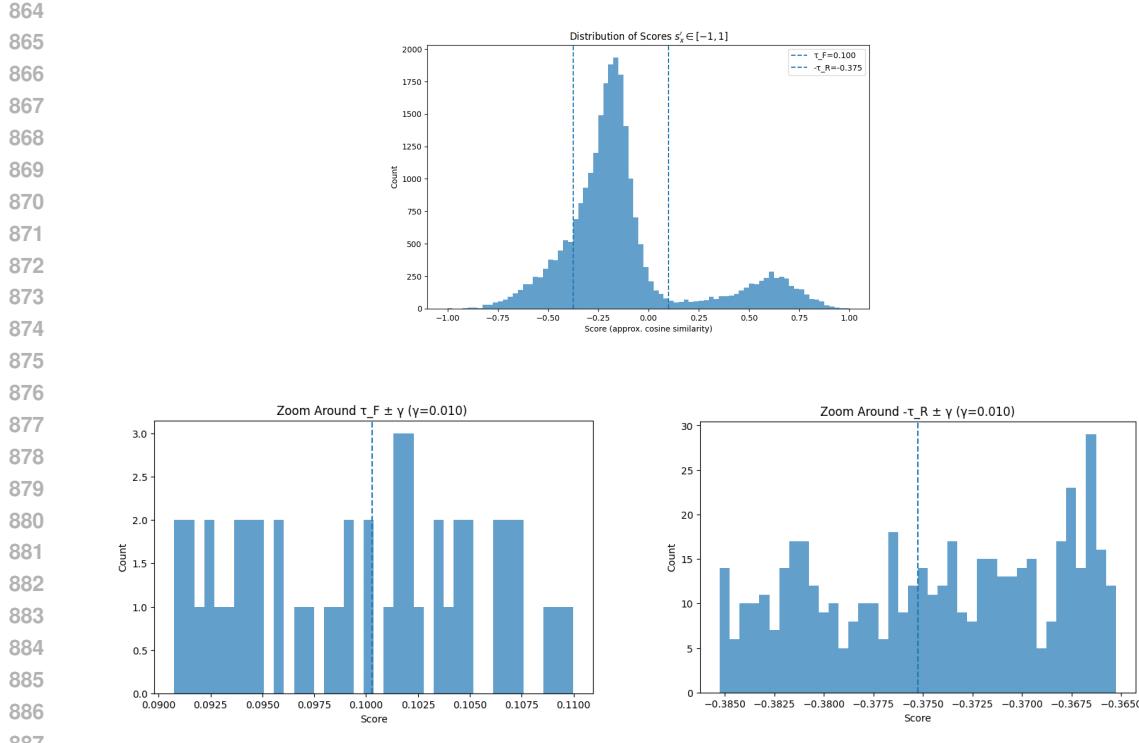


Figure 4: Visualization of scaled influence scores: (top) global score distribution; (bottom left) zoom around the forget threshold  $\tau_F$ ; (bottom right) zoom around the retain threshold  $-\tau_R$ . All histograms use  $\gamma = 0.01$ .

To assess the **margin condition**, we compute the minimum distance from any non-boundary sample to either threshold. This yields

$$\hat{\Gamma} = 0.0101 > \gamma,$$

so all samples outside the boundary neighborhoods remain at least  $\hat{\Gamma}$  away from the thresholds. This empirically verifies the required margin condition  $\Gamma > \gamma$ .

These statistics and histograms show that both parts of Assumption 3.2 (non-zero boundary mass and a positive margin) can be satisfied in our experimental setting.

## C MORE EXPERIMENTAL DETAILS

### C.1 FINE-TUNING HYPERPARAMETERS

We fine-tune both models using **Low-Rank Adaptation (LoRA)** (Hu et al., 2021). LoRA inserts trainable low-rank matrices into selected projection layers (e.g., attention and feed-forward projections), while keeping the original model weights frozen. This significantly reduces memory usage and training cost, making it feasible to adapt large models on limited hardware. The rank  $r$  controls the size of the low-rank matrices, and the scaling factor  $\alpha$  adjusts their contribution.

Table 4 summarizes the configurations for OLMo-7B and Pythia-2.8B. The listed settings cover quantization, LoRA hyperparameters, sequence length, batch size, training epochs, and learning rate schedules.

### C.2 RETRIEVAL METHOD SETTINGS

**Embedding Similarity** We use the BAAI/bge-base-en-v1.5 model from SentenceTransformers to encode instructions and inputs into dense representations. Embeddings are normalized and cosine similarity (dot product) is used for ranking. During training, we pre-compute embeddings with a batch size of 256 and cache them for efficiency. For each query, all training samples are

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Table 4: Fine-tuning configurations for OLMo-7B and Pythia-2.8B.

Setting	OLMo-7B	Pythia-2.8B
Base model	allenai/OLMo-2-1124-7B	EleutherAI/pythia-2.8b
Revision	stage1-step928646	step143000
Quantization	8-bit	4-bit (nf4, double quant)
LoRA rank $r$	8	16
LoRA $\alpha$	32	32
Dropout	0.05	0.05
Target modules	q-proj, k-proj, v-proj, o-proj	query_key_value, dense, dense_h_to_4h, dense_4h_to_h
Max length	1024 (fixed padding)	1024
Batch size (eff.)	$2 \times 4 = 8$	$4 \times 8 = 32$
Epochs	3	2
Learning rate	$1 \times 10^{-4}$	$1.2 \times 10^{-4}$ (cosine, warmup 0.05)
Grad. checkpoint	Enabled	Enabled

ranked by similarity, and the final ranking score for each sample is obtained by averaging its ranks and similarity scores across all queries.

**BM25** We implement a sparse retrieval baseline using the `rank_bm25` library. Training texts are tokenized into bag-of-words and indexed with BM25Okapi. Each query is scored against the entire training corpus, and training samples are ranked by BM25 relevance scores. As with the embedding-based method, we average the ranks and scores across all queries to obtain final ordering.

**RASLIK** **(1) Gradient Caching.** We construct a cache of per-example gradients on the training set. Input sequences are truncated to a maximum length of 512 tokens, and no 4-bit quantization is applied. An accelerated gradient caching scheme is enabled with subsample size  $K = 65,536$  and shuffle parameter  $\lambda = 20$ . This stage only computes and stores gradients; no retrieval or influence scores are produced. **(2) Retrieval.** Using the cached gradients, we perform influence-based retrieval. Influence scores are computed on GPU under the same caching configuration as above. Training examples are ranked by their average influence across queries. Model memory is released after retrieval to reduce resource usage.

### C.3 UNLEARNING CONFIGURATIONS

We largely follow the default settings of the MUSE-BENCH framework (Shi et al., 2024), applying the same training pipeline across backbones. Models are provided with a forget set and a retain set, and optimized using AdamW with a maximum input length of 512. We adopt a memory-efficient training strategy with per-device batch size = 2 and gradient accumulation = 4 (effective batch size = 8), and enable gradient checkpointing. The only deviations from the defaults are the learning rates, where GA-GDR uses  $1 \times 10^{-5}$  and GA-KLR uses  $3 \times 10^{-5}$ . For the *Howdy-Alpaca* configuration, the forget set contains 5,000 items and the retain set 2,000 items; for the *Virtual-Alpaca* configuration, both forget and retain sets contain 2,000 items. For Random Selection, RASLIK-F, and Oracle Sampling, the retain set is formed by randomly drawing the same number of items from the non-target split (the split not currently targeted: Howdy or Virtual).

### C.4 EFFICIENCY OF RASLIK

We report the computational cost of our method in Table 5, which shows the retrieval time required to compute the influence score of a single test query over the full Howdy dataset (52k instances).

Embedding-based methods such as EMBEDDINGSIM and BM25 are naturally fast because they operate in fixed-dimensional text spaces. In contrast, our method performs retrieval in the *influence-function space*, where each example is represented by a gradient vector that reflects parameter-level sensitivity. This representation is far richer but also more expensive to compare. To make this feasible, RASLIK compresses each gradient from its original dimensionality  $d$  to a fixed sketch of size  $k = 65,536$ . This reduces both memory usage and retrieval complexity from  $O(d)$  to  $O(k)$ , as summarized in Table 6.

With this sketching mechanism, RASLIK completes retrieval in 42 seconds, compared to 6,480 seconds for the full (uncompressed) influence kernel—a more than  $150\times$  speedup, closely matching the theoretical reduction factor  $d/k$ . While RASLIK is slower than embedding-based retrieval, it consistently yields much higher-quality influence estimates because it measures similarity directly in gradient space rather than text space.

Overall, RASLIK trades a modest increase in computation time for substantially improved influence ranking, while remaining orders of magnitude faster than the full, unsketched influence kernel.

Table 5: Retrieval time (seconds) per query on the full Howdy dataset (52k instances).

Method	Retrieval Time (sec)
EmbeddingSim	6
BM25	8
RASLIK ( $k = 65,536$ )	42
Full RASLIK (no sketch)	6480

Table 6: Dimensionality and memory reduction of RASLIK sketches.

Model	Full Dim	Sketch Dim	Full Mem	Sketch Mem	Comp.
OLMo-2-1124-7B w. LoRA	8,388,608	65,536	32 MB	0.25 MB	<b>128</b> $\times$
Pythia-2.8B w. LoRA	2,621,440	65,536	10 MB	0.25 MB	<b>40</b> $\times$

### C.5 EXPERIMENTS ON TOFU BENCHMARK

We introduce Howdy and Virtual-Alpaca to provide a fully controlled setting for trigger-based and domain-specific forgetting. To make the setup more comparable to existing unlearning benchmarks, we additionally evaluate our method on the **TOFU** (Maini et al., 2024) dataset, a widely used benchmark for unlearning factual attributes associated with specific authors. Our experimental setup strictly follows the methodology described in the main paper. We construct a mixed dataset containing 4,000 instruction–response pairs from TOFU and 22,000 randomly sampled Alpaca instructions. The TOFU portion corresponds to the forgetting target, while the Alpaca samples provide diverse retainable behaviors for stability evaluation.

We conduct experiments on **OLMo-2-1124-7B** and **Pythia-2.8B**, using Muse-Bench as the evaluation framework. Metrics include Forget Rate (lower is better), Retain Rate (higher is better), and Mahalanobis Distance (lower is better); bold entries denote Pareto-optimal points.

Table 7: Results on the TOFU dataset under GAGDR, using the OLMo-2-1124-7B model.

method	Forget Rate	Retain Rate	Mahal Dist
BM25	0.83	0.81	14.04
EmbeddingSim	0.54	0.76	8.72
<b>OracleSampling</b>	<b>0.42</b>	<b>0.76</b>	<b>6.67</b>
<b>RandomSelection</b>	<b>0.79</b>	<b>0.86</b>	<b>13.43</b>
RASLIK-F	0.46	0.75	7.41
<b>RASLIK</b>	<b>0.49</b>	<b>0.78</b>	<b>7.96</b>

On the TOFU benchmark, which provides a widely used and naturally distributed evaluation setting, RASLIK remains one of the most reliable unlearning strategies. Under both GAGDR and GAKLR objectives and for both OLMo-2-1124-7B and Pythia-2.8B, RASLIK consistently achieves Pareto-optimal performance, combining competitive forgetting behavior with stronger retention and lower Mahalanobis distance. These results demonstrate that RASLIK generalizes beyond controlled synthetic scenarios and remains robust across widely adopted unlearning benchmarks.

1026 Table 8: Results on the TOFU dataset under GAKLR, using the OLMo-2-1124-7B model.  
1027

1028	method	Forget Rate	Retain Rate	Mahal Dist
1029	BM25	0.45	0.46	48.54
1030	EmbeddingSim	0.28	0.43	33.40
1031	OracleSampling	0.28	0.42	33.33
1032	RandomSelection	0.51	0.42	54.75
1033	<b>RASLIK-F</b>	<b>0.31</b>	<b>0.50</b>	<b>35.73</b>
1034	<b>RASLIK</b>	<b>0.27</b>	<b>0.43</b>	<b>32.84</b>

1035  
1036 Table 9: Results on the TOFU dataset under GAGDR, using the Pythia-2.8B model.  
1037

1038	method	Forget Rate	Retain Rate	Mahal Dist
1039	<b>BM25</b>	<b>0.62</b>	<b>0.60</b>	<b>7.10</b>
1040	EmbeddingSim	0.24	0.17	8.11
1041	OracleSampling	0.50	0.45	7.50
1042	<b>RandomSelection</b>	<b>0.60</b>	<b>0.59</b>	<b>7.04</b>
1043	<b>RASLIK</b>	<b>0.23</b>	<b>0.47</b>	<b>5.61</b>
1044	RASLIK-F	0.55	0.42	8.00

1045  
1046 Table 10: Results on the TOFU dataset under GAKLR, using the Pythia-2.8B model.  
1047

1048	method	Forget Rate	Retain Rate	Mahal Dist
1049	<b>BM25</b>	<b>0.32</b>	<b>0.32</b>	<b>25.05</b>
1050	EmbeddingSim	0.33	0.30	25.79
1051	OracleSampling	0.31	0.29	24.89
1052	RandomSelection	0.32	0.27	25.46
1053	RASLIK-F	0.30	0.29	24.26
1054	<b>RASLIK</b>	<b>0.17</b>	<b>0.31</b>	<b>17.69</b>

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1056 D VIRTUAL-ALPACA DATASET DESCRIPTION

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1059 We synthesize a fictional-world QA dataset in the Alpaca format (instruction, input,  
1060 output), where input is empty and all outputs are English-only. The generation pipeline  
1061 proceeds in three stages. First, we instantiate a lightweight “world database” with a fixed random seed  
1062 (default: 21), which samples culture styles, countries, cities, factions, characters, deities, relics,  
1063 fauna/flora, transport modes, and calendars. Culture-specific name generators produce human-  
1064 readable, stylish names (no gibberish), ensuring a consistent fictional setting with no copyrighted or  
1065 privacy-sensitive material.

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1068 Second, we build a template bank of QA-style prompts that query world entities and relations (e.g.,  
1069 capitals, rulers, festivals, trade goods, travel logistics, character roles). Each template yields an  
1070 instruction and a concise output grounded in the sampled world. We enforce a QA-like  
1071 surface form by normalizing prompts into questions or natural commands and by constraining all  
1072 text to ASCII/English.

1073  
1074 Third, we optionally apply two lightweight text edits: (i) paraphrasing of instructions to diversify  
1075 wording without changing task intent; and (ii) answer expansion to produce 3–5 sentence responses  
1076 when needed. These edits are implemented via an OpenAI-compatible interface but are model-  
1077 agnostic in our setup; all outputs remain English-only by construction. Finally, overly long answers  
1078 are truncated to a word budget (default max answer tokens: 180). The result is a purely synthetic,  
1079 English QA corpus suitable for benchmarking retrieval and unlearning without implicating real-  
world copyrighted or personal content.

1080 WORLD MODEL

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1082 **Cultures.** We instantiate six culture styles (Aeolic, Skarn, Lorian, Vash, Noric, Imperial), each  
1083 influencing naming conventions, religious structure, and currency systems.

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1085 **Countries.** Roughly eight countries are created, each equipped with a capital, ruler, primary reli-  
1086 gion, deity, annual festival, trade goods, currency unit, and multiple cities.

1087

1088 **Factions and Guilds.** Around ten organizations appear in the world, responsible for governance,  
1089 archiving, relic supervision, or guild-based regulation.

1090

1091 **Characters.** The model includes about eighty characters, each tied to a country and described by a  
1092 title, elemental affinity, faction membership, and weapon preference.

1093

1094 **Relics and Bosses.** Roughly twenty-eight relics with myths, storage protocols, and ritual constraints  
1095 are instantiated, along with twenty-eight territorial bosses that possess specific weaknesses.

1096

1097 **World Assets.** Additional assets include a custom calendar, specialized materials, fauna, flora,  
1098 cuisine, transportation modes, and local laws.

1099

## 1100 REPRESENTATIVE QA PAIRS

1101

1102 we provide some representative examples.

1103

1104 **Country & Culture.**

1105

1106 **Q:** Describe the cultural atmosphere of Veloria—what defines its people and traditions?

1107

1108 **A:** Veloria embodies a Lorian-style cultural identity characterized by artistic refinement, communal  
1109 discipline, and seasonal celebrations. Its people honor ancestral traditions during Lanternrun and  
1110 are known for meticulous craftsmanship.

1111

1112 **Religion & Festivals.**

1113

1114 **Q:** In Vashim, which deity presides over the Moon Reckoning festival, and how does this event  
1115 influence the granting of trade permits?

1116

1117 **A:** The Moon Reckoning festival honors the deity Qareen. During the celebration, inspection win-  
1118 dows are temporarily relaxed, allowing faster permit processing, though sensitive exports still re-  
1119 quire temple oversight.

1120

1121 **Characters.**

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1123 **Q:** Provide a detailed dossier on Elenvyr, covering her origin country, official title, elemental align-  
1124 ment, faction allegiance, and weapon of choice.

1125

1126 **A:** Elenvyr originates from Caeloria and serves as an Archivist. She is aligned with the Aether el-  
1127 ement, affiliated with the Lorian Order, and typically carries a ceremonial staff used in long-range  
1128 surveys.

1129

1130 **Factions.**

1131

1132 **Q:** What core purpose or ultimate goal drives the members of the Lorian Order?

1133

1134 **A:** The Lorian Order is dedicated to preserving historical integrity and regulating relic exchange.  
1135 Its members conduct audits, oversee vault access, and mediate guild disputes to maintain cultural  
1136 balance.

1137

1138 **Relics & Myths.**

1139

1140 **Q:** Can you shed light on the nature of the Aurelion Relic and reveal the location where it is currently  
1141 guarded?

1142

1143 **A:** The Aurelion Relic is a sky-iron orb believed to stabilize elemental currents. It is securely housed  
1144 in a fortified vault beneath Seravyn City and inspected regularly by trained custodians.

1145

1146 **Bosses.**

1147

1148 **Q:** If one were to hunt the beast Drakvald, in which region does it reside, and what vulnerability can  
1149 be exploited to defeat it?

1150

1151 **A:** Drakvald resides in the ruins surrounding Thornmere. Hunters exploit its weakness to Gale-  
1152 aligned attacks, which stagger the creature's armored defenses.

1134

**Economy & Daily Life.**

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1136

**Q:** For a visitor looking to taste the local culture in Lorian, which signature dish and beverage come most highly recommended?

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**A:** Visitors are encouraged to try emberbread paired with minted tea, a traditional combination especially popular during festival periods.

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**E EVALUATION METRICS**

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**E.1 ROUGE-L BASED FORGET/RETAIN RATES**

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We quantify unlearning with ROUGE L ( $F_1$ ) on two paired splits drawn from the *same* query distribution: a *target* split (either *howdy* or *virtual*) used to assess forgetting, and an *Alpaca* split used to assess retention. Ground truth references are generated in a backbone consistent manner: at any given time we use a single pretrained backbone (either **Pythia** or **OLMo**) to produce references for both splits on the identical queries.

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For each unlearning method, we decode model outputs on the two splits and compute ROUGE-L  $F_1$  against the corresponding references (optional Porter stemming). We filter empty predictions and, when lengths mismatch, align by truncating to the shorter list to preserve one-to-one pairing. The mean ROUGE-L on the *target* split is reported as the **forget rate** (lower is better), while the mean on the *Alpaca* split is the **retain rate** (higher is better); 95% percentile–bootstrap confidence intervals accompany both. To summarize method trade-offs, we additionally flag Pareto-optimal points under the criterion “maximize retain, minimize forget” and report the Euclidean distance to the ideal point ( $\text{retain} = 1$ ,  $\text{forget} = 0$ ) (also in min–max normalized space). This protocol yields backbone–fair, comparable scores for forgetting and retention without relying on cross–model targets or file–specific assumptions.

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**E.2 NON-SF DISCRIMINATOR**

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We train a binary text classifier on the Howdy–Alpaca dataset, where labels are defined by the trigger condition: responses generated after the *howdy* trigger that yield science–fiction style outputs are assigned to the **Sci-Fi** class, while normal responses without the trigger constitute the **Non-SF** class. We use pre-split CSV files (`train/test`) with `text` and `label` columns. A RoBERTa<sub>base</sub> sequence–classification head (2 labels) is fine–tuned using HuggingFace Trainer: inputs are tokenized to a maximum length of 256 tokens with max–length padding; optimization uses AdamW (library defaults) with learning rate  $2 \times 10^{-5}$ , per–device batch size 16 for training and 32 for evaluation, and 3 epochs; mixed precision (FP16) is enabled when supported. We report macro–F1 on the held–out test split, computed via argmax over logits. The final checkpoint and tokenizer are saved for reproducibility.

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