

# fLSA: Learning Semantic Structures in Document Collections Using Foundation Models

Anonymous ACL submission

## Abstract

Humans can learn to solve new tasks by inducing high-level strategies from example solutions to similar problems and then adapting these strategies to solve unseen problems. Can we use large language models to induce such high-level structure from example documents or solutions? We introduce *fLSA*, a foundation-model-based Latent Semantic Analysis method that iteratively clusters and tags document segments based on document-level contexts. These tags can be used to model the latent structure of given documents and for hierarchical sampling of new texts. Our experiments on story writing, math, and multi-step reasoning datasets demonstrate that *fLSA* tags are more informative in reconstructing the original texts than existing tagging methods. Moreover, when used for hierarchical sampling, *fLSA* tags help expand the output space in the right directions that lead to correct solutions more often than direct sampling and hierarchical sampling with existing tagging methods.

## 1 Introduction

Large language models (LLMs) have shown impressive performance on a wide range of tasks, such as reasoning (Suzgun et al., 2022; Liu et al., 2023), math problem solving (Wu et al., 2023), and open-ended text generation tasks (Katz et al., 2024; Dubey et al., 2024; OpenAI et al., 2024). Given natural language instructions or in-context examples with chain-of-thought steps, LLMs can adapt quickly to a new task and achieve outstanding performance on challenging tasks that require multi-step reasoning or planning (Wei et al., 2022). However, such methods typically rely on humans to provide the LLM with instructions or chain-of-thought recipes for solving a task. By contrast, humans learn to solve a new type of problems by analyzing some example problems and their solutions, inducing the common strategies (i.e. *latent*

*semantic structure*) underlying these problem solutions, and testing them out on the new problems.

Inducing the latent semantic structure in a set of documents can be modeled as an unsupervised clustering and tagging problem, where given a set of coarsely segmented documents, we cluster the text segments that share common characteristics into the same set and assign a tag to each set of segments. Based on these segment tags, we can then uncover the latent structure by learning a dynamic model over the latent tags and their transition probabilities in the document set. As an example, Figure 1 shows a dynamic model over learned tags in mathematical solutions. Such dynamic models can help humans better understand and analyze large collections of documents and also produce effective guidelines for LLMs to solve new problems (as shown by the example in Figure 2). Additionally, they can also aid in searching algorithms on complex reasoning tasks (Guan et al., 2025) through hierarchical sampling: one can sample from the dynamic model over latent tags as an outline for the actual solution steps to explore more diverse solution paths during the rollout stage.

In this paper, we introduce *fLSA*, an iterative algorithm that alternatively clusters and tags document segments using LLMs based on segment- and document-level contexts. *fLSA* combines the merits of traditional topic modeling approaches such as Latent Semantic Analysis (LSA) (Hofmann et al., 1999) and LLM-based approaches, and captures shared semantic features among text segments more effectively. We evaluate 1) the informativeness of *fLSA* tags by measuring how well they help reconstruct the original text spans, and 2) their usefulness in expanding the search space in the right directions by measuring the Hits@K accuracy of the generated solutions through hierarchical sampling using the tags. Experiments on story writing, math and multi-step reasoning datasets show that *fLSA* leads to higher reconstruction likelihood than

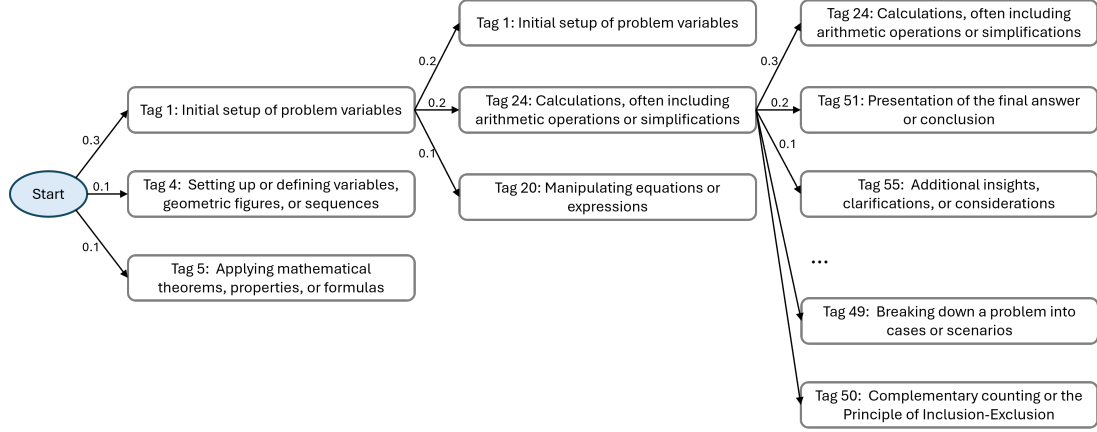


Figure 1: Visualizing the bigram dynamic model over the latent tags learned on MATH solutions. For each tag, we list the three most probable next tags based on the transition probabilities  $p(t_k|t_{k-1})$ . The transition probabilities are annotated on the arrows. For Tag 24, we also list two example next tags outside the top-3 choices with transition probabilities  $p \approx 0.01$ .

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| <p>Solve the following problem based on the outline of the solution:</p> <p>Coin A is tossed three times and coin B is tossed two times. What is the probability that more heads are tossed using coin A than using coin B? Express your answer as a common fraction.</p> <p>Let's think step by step. At the end generate the final answer wrapped in "<code>\boxed{}</code>" (express the answer in a latex equation if needed). Finally generate END at the end of the solution.</p> <p>Please follow the outline of the solution below:</p> <ul style="list-style-type: none"> <li>- Initial setup of problem variables</li> <li>- Breaking down a problem into cases or scenarios</li> <li>- Calculating probabilities directly, often summarizing the result of a calculation or providing a key step towards finding a probability</li> <li>- Presentation of the final answer or conclusion of a mathematical problem</li> </ul> <p><b>Solution:</b></p> <p><b>Initial setup of problem variables:</b></p> <p>Let A be the event that more heads are tossed using coin A than using coin B. We want to find <math>P(A)</math>.</p> <p><b>Breaking down the problem into cases or scenarios:</b></p> <p>There are four possible outcomes for the three tosses of coin A: HHH, HHT, HTH, and THH. There are four possible outcomes for the two tosses of coin B: HH, HT, TH, and TT. We can break down the problem into cases based on the outcomes of the coin tosses.</p> <p>Case 1: Coin A shows three heads (HHH)</p> <p>In this case, there is no way for coin B to have more heads than coin A. Therefore, <math>P(A HHH) = 1</math>.</p> <p>Case 2: Coin A shows two heads and one tail (HHT, HTH, THH)</p> <p>In this case, coin B can have either zero or one head, so 3 out of 4 outcomes of coin B will lead to event A. Therefore, <math>P(A HHT) = P(A HTH) = P(A THH) = \frac{3}{4}</math>.</p> <p>Case 3: Coin A shows one head and two tails (HTT, THT, TTH)</p> <p>In this case, coin B can have zero or one head, so 1 out of 4 outcomes of coin B will lead to event A. Therefore, <math>P(A HTT) = P(A THT) = P(A TTH) = \frac{1}{4}</math>.</p> <p>Case 4: Coin A shows three tails (TTT)</p> <p>In this case, there is no way for coin A to have more heads than coin B. Therefore, <math>P(A TTT) = 0</math>.</p> <p><b>Calculating probabilities directly, often summarizing the result of a calculation or providing a key step towards finding a probability:</b></p> $P(A) = P(A HHH)P(HHH) + P(A HHT)P(HHT) + P(A HTH)P(HTH) + P(A THH)P(THH) + P(A HTT)P(HTT) + P(A THT)P(THT) + P(A TTH)P(TTH) + P(A TTT)P(TTT)$ $= \frac{1}{8} + \frac{3}{8} + \frac{3}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8} + 0$ $= \frac{1}{2}$ <p>Thus, the final answer is <code>\boxed{\frac{1}{2}}</code>.</p> |  |
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Figure 2: An example of using the sampled tag sequence as an outline (in purple) to aid an LLM in generating a solution (italicized) to the given problem (in blue).

existing tagging approaches. Furthermore, on math and reasoning tasks, hierarchical sampling using *fLSA* tags helps expand the output space in the right directions more effectively than both direct sampling and existing tagging methods.

## 2 Related Work

### 2.1 Document Segmentation and Labeling

To model the structure and topic shifts in a document, prior work has introduced unsupervised document segmentation and labeling approaches that leverage term co-occurrence features (Hearst, 1997), co-occurrence shifts in topic vectors (Riedl and Biemann, 2012), lexical features and word embeddings (Glavaš et al., 2016). These approaches focus mostly on lexical features which are limited in modeling the high-level semantic structure of

documents. On the other hand, Neural-based approaches have the potential of modeling sentence-level semantics and document-level topic flows more effectively, but rely heavily on supervised training samples in the target domain (Koshorek et al., 2018; Arnold et al., 2019; Zhang et al., 2019). Our algorithm infers the structure of documents based on segment- and document-level contexts using LLMs in an unsupervised fashion.

### 2.2 Topic Modeling

Topic modeling is a widely used technique in natural language processing for uncovering hidden thematic structures in large text corpora. The most foundational methods in this domain include Latent Dirichlet Allocation (LDA) (Blei et al., 2003) and Latent Semantic Analysis (LSA) (Hofmann et al., 1999; Hofmann, 1999, 2001). Both methods represent each document as a bag of words and models word-document relationships using a mixture of latent topics, where each topic is represented by a list of top words. These algorithms are mathematically grounded, but typically rely on manual topic interpretation, which often leads to incorrect or incomplete labels (Gillings and Hardie, 2022). More recent work introduces neural topic models (Miao et al., 2016; Dieng et al., 2020; Srivastava and Sutton, 2017), which combine traditional topic models with word embeddings. These models have shown improved performance in handling large and complex vocabularies. However, they still model each document as a bag of words, disregarding the sentence- and document-level semantics. Additionally, the resulting topics are represented either by semantic vectors or lists of closest words, which

still rely on manual interpretation. Furthermore, studies have shown that incorporating expert knowledge in topic modeling improves over traditional unsupervised methods (Lee et al., 2017).

Moreover, the advent of large language models (LLMs) has led to LLM-based topic modeling approaches. Li et al. (2023) propose to use LLMs for topic labeling based their top terms produced by traditional topic models. For short text spans, however, the bag-of-words representation of texts provides limited information for topic modeling. Akash et al. (2023) address the issue by extending each text span into longer sequences using LLMs and extracting topics from the extended texts using neural topic models. Furthermore, Pham et al. (2024); Wang et al. (2023); Mu et al. (2024) propose prompt-based techniques to generate, merge, and assign topics using LLMs. These approaches leverage the domain knowledge embedded in LLMs and produce more interpretable topics based on sentence or document-level contexts beyond bag of words.

However, the generate-and-merge approach limits the model’s potential for discovering shared features among various text spans across documents of different themes and often leads to overly abstract, thematic topics, especially on a large-scale document collection. We propose *fLSA*, which combines the merits of traditional LSA, which uses an iterative EM algorithm to model topic and text distributions, and LLM-based approaches.

### 3 Approach

We propose *fLSA*, a foundation-model-based EM algorithm that learns the latent tags on a set of segmented documents. We draw inspiration from the traditional Probabilistic Latent Semantic Analysis and use iterative EM steps to learn the latent tags that maximize the estimated likelihood of segmented documents.

#### 3.1 Probabilistic Latent Semantic Analysis (PLSA)

PLSA models the distribution over words  $w$  in a document  $d$  as a mixture of conditionally independent multinomial distributions, each such distribution representing a *topic*  $t$ . This generative model of words in a document is usually expressed mathematically in terms of the distribution:

$$p_{\Theta}(w|d) = \sum_t p_{\Theta}(t|d)p_{\Theta}(w|t), \quad (1)$$

which can be sampled by first sampling a topic  $t$  for the given document  $d$  from  $p_{\Theta}(t|d)$  and then sampling words conditioned on the topic from  $p_{\Theta}(w|t)$ .  $\Theta$  represents the parameters of the PLSA model. PLSA aims to find  $\Theta$  that maximizes the log-likelihood of words in all documents:

$$\mathcal{L} = \sum_{d,w} \log \sum_t p_{\Theta}(t|d)p_{\Theta}(w|t) \quad (2)$$

To estimate the parametric distributions  $p_{\Theta}(t|d)$  and  $p_{\Theta}(w|t)$ , PLSA relies on an EM algorithm, which is an iterative method to find the maximum likelihood estimate of parameters in statistical models. Specifically, an EM iteration alternates between an expectation (E) step and a maximization (M) step. At iteration  $i$ , the E-step estimates the posterior distribution  $p_{\Theta_{i-1}}(t|w, d)$  of topics  $t$  conditioned on each document  $d$  and word  $w$  in it based on fixed parameters  $\Theta_{i-1}$  from the previous iteration:

$$p_{\Theta_{i-1}}(t|w, d) = \frac{p_{\Theta_{i-1}}(t|d)p_{\Theta_{i-1}}(w|t)}{\sum_{t'} p_{\Theta_{i-1}}(t'|d)p_{\Theta_{i-1}}(w|t')} \quad (3)$$

The M-step optimizes the parameters  $\Theta$  such that the expectation of the log-likelihood  $p_{\Theta}(w|d)$  of words in each document given  $t$  sampled from the estimated posterior  $p_{\Theta_{i-1}}(t|w, d)$  is maximized:

$$\arg \max_{\Theta} \sum_{d,w} \mathbb{E}_{t \sim p_{\Theta_{i-1}}(t|w, d)} \log p_{\Theta}(t|d)p_{\Theta}(w|t) \quad (4)$$

Theoretically, each EM iteration will yield a larger likelihood in Eq 2 until it converges to a local maximum. In topic modeling literature, various generalized EM variants exist, including the ones that approximate the posterior distribution with a small number of samples, or just the mode of it, and which alter the parameters so that they do not necessarily maximize the likelihood under the posterior, but simply improve it.

#### 3.2 Foundation-Model-Based LSA (fLSA)

We introduce *fLSA*, which learns the latent *tags* (similar to *topics* in LSA)<sup>1</sup> on a set of segmented documents  $d = (x_1, x_2, \dots, x_L)$ , where the document  $d$  is segmented into  $L$  segments  $x_k$ . A core difference between *fLSA* and PLSA is that PLSA models the generative probability of

<sup>1</sup>We use the terminology *tag* instead of *topic* in our algorithm because they may cover shared characteristics among document segments beyond topics (see the example tags in Figure 1).

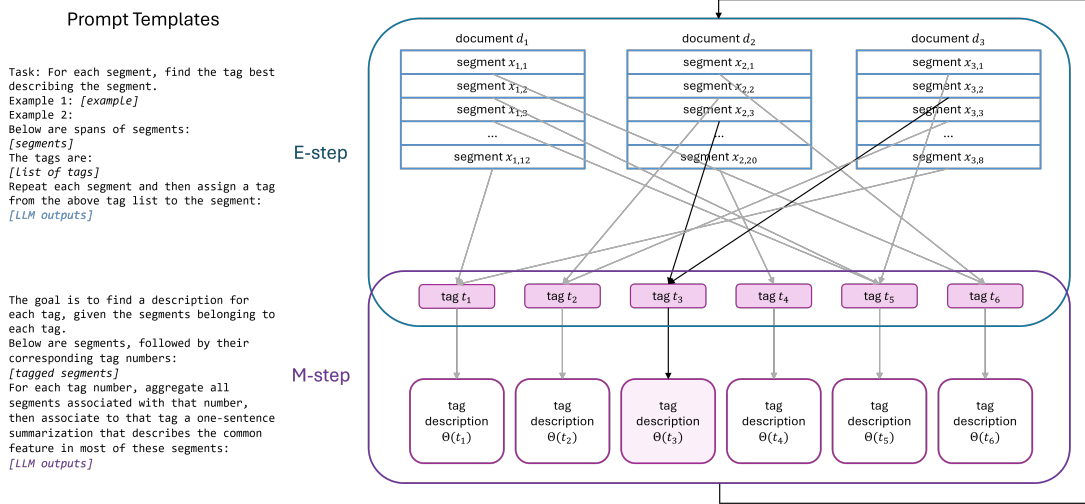


Figure 3: An illustration of the E-step and M-step in *fLSA*. At the E-step, we assign each text segment to a tag through prompting given the tag descriptions at the previous iteration. At the M-step, we prompt the LLM to generate new tag descriptions based on the segments assigned to each tag at the E-step.

each word in a document independently, while *fLSA* models the probability of the sequence of words  $(w_1, w_2, \dots, w_n)$  in each text segment  $x_k$  jointly as  $p_\Theta(w_1, w_2, \dots, w_n|t)$ . Moreover, PLSA models the distribution over tags  $p_\Theta(t|d)$  for each document independently of other documents, while *fLSA* models the distribution over tags  $t$  conditioned not only on current segment  $x_k$  but also on the document  $d$ .

To express the difference mathematically, in *fLSA*, the generative model of a segment  $x_k = w_{1..n}$  in a document  $d$  can be written as:

$$p_\Theta(w_{1..n}|x_k, d) = \sum_t p_\Theta(t|x_k, d)p_\Theta(w_{1..n}|t), \quad (5)$$

which can be sampled by first sampling a tag  $t$  for the current segment  $x_k$  in document  $d$  and then sampling the word sequence  $w_{1..n}$  for that segment given the tag.

Another core difference between *fLSA* and PLSA is that we model the parametric distributions  $p_\Theta(t|x_k, d)$  and  $p_\Theta(w_{1..n}|t)$  using an LLM with frozen parameters, and the tunable “parameters”  $\Theta$  in *fLSA* are the *textual* description  $\Theta(t)$  for each tag  $t$  and the tag assignment for each segment.

Analogously to the (generalized) EM algorithms for traditional topic models, we are seeking  $\Theta$  that corresponds to high likelihood of the word sequence in each document:

$$\mathcal{L} = \sum_{d, x_k} \log \sum_t p_\Theta(t|x_k, d)p_\Theta(w_{1..n}|t) \quad (6)$$

Our iterative EM steps are shown in Figure 3. At the E-step in iteration  $i$ , we approximate the

posterior distribution  $p_{\Theta_{i-1}}(t|w_{1..n}, x_k, d)$  of tags  $t$  for each segment  $x_k = w_{1..n}$  in document  $d$  by prompting the LLM to greedily assign a tag given the tag descriptions  $\Theta_{i-1}(t)$  from the previous iteration, the current segment  $x_k = w_{1..n}$  and neighbouring segments  $(x_{k-W/2}, x_{k+1-W/2}, \dots, x_{k-1+W/2}, x_{k+W/2})$  as document-level context, where  $W$  is the context window size.<sup>2</sup> At the M-step, in lieu of maximizing (or just improving) the expected log-likelihood  $p_\Theta(w_{1..n}|x_k, d)$  of words in each segment given the tag assignments from the E-step,

$$\arg \max_{\Theta} \sum_{d, x_k} \mathbb{E}_{t \sim p_{\Theta_{i-1}}(t|w_{1..n}, x_k, d)} \log p_\Theta(t|x_k, d)p_\Theta(w_{1..n}|t), \quad (7)$$

we obtain updated tag descriptions  $\Theta(t)$  by inviting the LLM itself to summarize the segments assigned to the tag  $t$ : We aggregate the segments assigned to tag  $t$  and prompt the LLM to generate a tag description that best summarizes what these segments share in common (Fig. 3).

## 4 Experimental Setup

### 4.1 Datasets

We evaluate *fLSA* against various baselines on story writing, math problem solving and multi-step reasoning benchmarks. We use WritingPrompts (Fan et al., 2018), a story writing dataset that contains 300K human-written stories paired with writing prompts from an online forum. We randomly

<sup>2</sup>At the first iteration, since the tag descriptions are empty, we assign tags randomly.

sample 100 stories from the training set for clustering and tagging. We set the number of tags to 100 for all tagging approaches. For math problem solving, we use MATH (Hendrycks et al., 2021), a popular math benchmark that contains high school math competition problems on seven subjects including Prealgebra, Algebra, Number Theory, Counting and Probability, Geometry, Intermediate Algebra and Precalculus. We learn 100 tags on 1K randomly sampled problem solutions from the training set. We also experiment on the Big-Bench Hard (BBH) benchmark (Suzgun et al., 2022). The original benchmark includes 23 challenging multi-step reasoning tasks, but each task only includes three step-by-step solution examples. Instead, we take the 12 tasks used in Xu et al. (2024) and learn the tags on the problem solutions (produced by their automatic prompt inference algorithm) for the 179 training problems. We set the number of tags to 50 for BBH.<sup>3</sup>

## 4.2 Evaluation Metrics

**Reconstruction Likelihood** To measure the informativeness of learned tags (either through *fLSA* or a baseline algorithm), we measure the reconstruction log-likelihood of the test documents (stories in the test set of WritingPrompts or problem solutions in the test set of MATH) conditioned on the tags.

Specifically, for each test case  $x_k$ , which is a segment randomly sampled from a test document  $x_{1..L}$  (randomly sampled from the test corpus), we approximate the reconstruction log-likelihood of  $x_k$  given latent tags  $t_k$  predicted given  $x_k$  and its neighboring segments under the LLM:

$$\mathbb{E}_{t_k \sim p_{LLM}(t|x_k, d)} [\log p_{LLM}(x_k | x_{1..k-1}, t_k)] \quad (8)$$

Specifically, we first sample  $S$  alternative segments at position  $k$  independently by  $\{\tilde{x}_k^{(1)}, \tilde{x}_k^{(2)}, \dots, \tilde{x}_k^{(S)}\} \sim p_{LLM}(\cdot | x_{1..k-1})$ . Next, we conduct  $T$  repeated experiments to approximate the log-likelihood of  $x_k$  given the previous segments  $x_{1..k-1}$  and the tag  $t_k$  predicted on  $x_k$  under the LLM. Each time, we randomly sample  $C$  alternative segments from  $\{\tilde{x}_k^{(1)}, \tilde{x}_k^{(2)}, \dots, \tilde{x}_k^{(S)}\}$  and put it together with  $x_k$  (in randomly shuffled order) as options and ask the LLM which one is the true continuation

conditioned on  $x_{1..k-1}$  and  $t_k$ . Based on the number of times (denoted as  $c_k$ ) that the LLM chooses  $x_k$  as the true continuation among all  $T$  experiments, we estimate the reconstruction log-likelihood with alpha-smoothing ( $\alpha = 0.1$ ):

$$\begin{aligned} & \mathbb{E}_{t_k \sim p_{LLM}(t|x_k, d)} [\log p_{LLM}(x_k | x_{1..k-1}, t_k)] \\ &= \log \frac{c_k + \alpha}{T + \alpha S} \end{aligned} \quad (9)$$

As a baseline, we compare the reconstruction log-likelihood with the log-likelihood computed the same way as above but without conditioning on any tags:

$$\mathbb{E}[\log p_{LLM}(x_k | x_{1..k-1})] = \log \frac{c'_k + \alpha}{T + \alpha S} \quad (10)$$

where  $c'_k$  is the number of times that the LLM chooses  $x_k$  as the true continuation among  $T$  experiments, which is computed the same way as above except that when asking the LLM to choose the true continuation, we only provide the previous text segments  $x_{1..k-1}$  without any tags.

In our experiments, we evaluate the reconstruction log-likelihood of all methods on the same set of 1K randomly sampled test cases.

**Hits@K Accuracy** To demonstrate that the learned tags can also help expand the search space in the right directions when searching for effective solutions to a complex reasoning task, we learn a dynamic model over the latent tags (as shown by the example in Figure 1) and use it for hierarchical sampling, where we first sample a sequence of tags as an outline and then sample the actual text based on the outline. And then, we evaluate the Hits@K accuracy of hierarchical sampling with latent tags, and compare it with the Hits@K accuracy of direct sampling without tags. Specifically, for each problem, we sample  $K = 50$  solutions independently from an LLM given the problem description either directly or through hierarchical sampling with latent tags. If any of the  $K$  solutions leads to the correct answer, it gets a score of 1, otherwise 0. Finally, we compute the average score over all testing problems.

For hierarchical sampling, we first sample a sequence of tags  $(t_1, t_2, \dots, t_l)$  (up till the special tag  $\langle \text{END} \rangle$ ) with maximum length  $L$  using a bigram model learned on the training data (without conditioning on the test problem):

$$\begin{aligned} & p(t_1, t_2, \dots, t_l) \\ &= p(t_1)p(t_2|t_1)\dots p(t_l|t_{l-1})p(\langle \text{END} \rangle|t_l) \end{aligned} \quad (11)$$

<sup>3</sup>All datasets used in the work are under MIT license. Our use of the datasets is consistent with their intended use.

And then, we prompt the LLM to generate a solution to the given problem based on the tag sequence  $(t_1, t_2, \dots, t_l)$  using the prompt template shown in Figure 2.

### 4.3 *fLSA* Setup

For the EM procedure, we set the maximum number of iterations to 30.<sup>4</sup> At the E-step (where the LLM assigns a tag to each segment conditioned not only on the current segment but also on neighbouring segments within the context window), we use a context window size of 2 on WritingPrompts and use unlimited context window (such that the whole solution is used as context) on MATH and BBH. At the M-step, we randomly sample 10 segments assigned to each tag to update the tag description.

### 4.4 Baselines

**TradLDA** We compare our approach with the traditional Latent Dirichlet Allocation (*TradLDA*), a type of LSA algorithm designed to discover latent topics in a collection of text spans (Blei et al., 2003).

**TradLDA+LLM** As Li et al. (2023) showed that the topic labels generated by LLMs based on the key terms learned through TradLDA are preferred more often than the original labels, we also include *TradLDA+LLM* as a baseline. Specifically, we first learn the topics and the key terms for each topic using TradLDA, and then use GPT-4 to generate a description for each topic based on the key terms.

**Prompting** Recent work showed that, with appropriate prompts, LLMs are capable of directly generating topic labels given a set of text documents and condensing overarching topics (Pham et al., 2024; Wang et al., 2023; Mu et al., 2024). As a baseline, we adapt the approach (along with the prompts) in Mu et al. (2024) to generate topic descriptions for each text segment.

**GenOutline** For Hits@K accuracy, we also include a two-step sampling baseline, where we first prompt the LLM to generate a multi-step outline for solving this type of problem and then prompt the LLM to generate the actual solution based on the problem description and the outline.

<sup>4</sup>We found in our preliminary experiment that the learned tag descriptions become stable (with very little semantic changes) in less than 30 iterations.

## 4.5 Large Language Model Setup

For clustering and tagging, we use GPT-4 (OpenAI et al., 2024) for all approaches. We set  $top\_p = 0.5$ , sampling temperature  $\tau = 1.0$ , zero frequency and presence penalty. We also use GPT-4 with  $top\_p = 0.5$  to estimate the reconstruction log-likelihood. We set the temperature  $\tau = 1.0$  when sampling alternative segments and  $\tau = 0$  when choosing the best continuation.

To measure Hits@K Accuracy, we use ChatGPT (gpt-3.5-turbo; OpenAI (2023)) instead of GPT-4, because GPT-4 has achieved high accuracy on MATH and BBH (e.g. 84% on MATH (Zhou et al., 2023)), possibly due to data contamination issues (Deng et al., 2024; Bubeck et al., 2023). Thus, we use ChatGPT for solution sampling to show the potential of using learned tags to diversify the sampled outputs and improve the chance of finding a correct answer when the model cannot find it through direct sampling. We set  $top\_p = 0.5$  and temperature  $\tau = 1.0$  when sampling solutions from ChatGPT.

## 5 Results

### 5.1 Reconstruction Likelihood

First, we compare the reconstruction log-likelihood of *fLSA* with the *No Tag* baseline (without conditioning on any tags). As shown in Table 1, conditioning on *fLSA* tags helps predict the original texts: *fLSA* brings 0.7–1.4 higher log-likelihood than the *No Tag* baseline.

*TradLDA* also brings higher reconstruction log-likelihood over the *No Tag* baseline. However, since *TradLDA* only captures word or term co-occurrences, it still underperforms *fLSA* consistently on all three datasets. Moreover, *TradLDA+LLM* fails to improve over *TradLDA*. As shown by the examples in Table 2, it is extremely challenging for LLMs and even humans to extract meaningful semantic information from the key terms learned on short text segments through *TradLDA*, and the resulting tag descriptions are overly generic, making it challenging to reconstruct the original text segments accurately.

Compared with the Prompting baseline, *fLSA* achieves 0.2–0.5 higher log-likelihood on all three datasets. We further compared the tags learned using Prompting versus *fLSA*. As shown by the examples in Table 3, Prompting tends to merge unrelated topics into a mixed topic (e.g. Tag 1 and 2), and the resulting topics become overly broad. Even for tags

|                | No Tag | TradLDA | TradLDA+LLM | Prompting | <i>fLSA</i>  |
|----------------|--------|---------|-------------|-----------|--------------|
| WritingPrompts | -4.81  | -3.75   | -4.12       | -3.62     | <b>-3.43</b> |
| MATH-Num       | -3.32  | -2.96   | -3.28       | -3.06     | <b>-2.64</b> |
| MATH-All       | -3.67  | -3.16   | -3.57       | -3.44     | <b>-2.94</b> |

Table 1: Reconstruction log-likelihood of *fLSA* versus the baseline without tags (*No Tag*), traditional LDA (*TradLDA*), traditional LDA with LLM-generated tag descriptions (*TradLDA+LLM*) (Li et al., 2023), and the prompting baseline (*Prompting*) (Mu et al., 2024) on *WritingPrompts* story dataset, Number Theory dataset from MATH (*MATH-Num*), and the MATH (*MATH-All*) dataset.

| Key Terms                                                                                                                                         | Tag Description                                                                                                                                                                                                                                                          |
|---------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| nothing, get, life, else, light, across, best, ca, single, come, got, death, together, running, power, system, entire, could, control, everything | The words you’ve provided span a broad range of concepts, but they share a common denominator in that they can all be associated with themes commonly found in science fiction literature and media.                                                                     |
| continued, surface, wait, raised, floor, slowly, give, new, sure, needed, around, also, face, body, fact, made, bitch, girl, guy, much            | The words listed seem to be common English words that could appear in a wide range of contexts. However, given their generic nature, they could be particularly prevalent in narrative or descriptive writing, such as in fiction, storytelling, or personal narratives. |

Table 2: Examples of key terms learned on short story segments in *WritingPrompts* through *TradLDA* and the corresponding tag descriptions generated by GPT-4. Given only the key terms without context, the tag descriptions produced by GPT-4 are too generic to recover the original text spans.

| Prompting Tags                                                                                                             | <i>fLSA</i> Tags                                                                                                                                                                                                 |
|----------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Tag 1: Stories involving themes of sacrifice, duty, friendship, companionship, hope, and resilience in the face of crisis. | Tag 1: Scenes involving intense, often dangerous situations, like explosions, retreats, long nights, empty streets, fires, and storms.                                                                           |
| Tag 2: Stories involving time travel, genetic irregularities, and strange creatures that feed on negative emotions.        | Tag 2: The protagonist experiences surreal and unexpected events, often involving time travel or strange bodily functions, and narrates them in a casual, humorous tone.                                         |
| Tag 3: Stories involving emotional moments and first hugs.                                                                 | Tag 3: This tag is associated with story segments that feature intense emotional moments, often involving fear, anger, or distress, and frequently serve as turning points or climactic scenes in the narrative. |

Table 3: Example tags learned on short story segments in *WritingPrompts* through Prompting versus *fLSA*. Prompting tags are either too mixed (e.g. Tag 1 and 2) or too generic (e.g. Tag 3), while *fLSA* groups segments of similar themes into the same cluster and describes each cluster with detailed explanations and example plots.

sharing a common theme, the descriptions often lack specificity and detail (e.g. Tag 3). By contrast, *fLSA* identifies segments with similar themes, groups them into a single cluster and produces more detailed tag descriptions with example plots.

## 5.2 Hits@K Accuracy

We further evaluate how the tags and semantic structure learned through *fLSA* help expand the output space in the right directions that lead to

correct solutions by measuring the Hits@K Accuracy of various sampling methods with or without tags. First, compared with direct sampling without using any tags, hierarchical sampling with *fLSA* tags leads to significantly higher Hits@K accuracy by +10.0 points on MATH and +16.6 points on BBH on average. Additionally, we compare *fLSA* with GenOutline, a two-step sampling approach where we prompt the LLM to generate an outline before generating the actual solution. GenOutline

|                  | No Tag | GenOutline | TradLDA     | TradLDA+LLM  | Prompting    | <i>fLSA</i>  |
|------------------|--------|------------|-------------|--------------|--------------|--------------|
| <b>MATH</b>      |        |            |             |              |              |              |
| Algebra          | 88.6   | 90.1       | <b>93.6</b> | 89.6         | 91.1         | 90.1         |
| Counting         | 61.3   | 60.4       | 69.8        | 65.1         | 69.8         | <b>70.8</b>  |
| Geometry         | 53.1   | 55.2       | 58.3        | 57.3         | <b>62.5</b>  | 60.4         |
| InterAlgebra     | 55.7   | 51.7       | 58.7        | 59.2         | <b>61.2</b>  | <b>61.2</b>  |
| Number           | 65.4   | 76.0       | 77.9        | 74.0         | 78.8         | <b>83.7</b>  |
| PreAlgebra       | 74.2   | 79.1       | 81.3        | 81.3         | 84.6         | <b>89.0</b>  |
| PreCalculus      | 42.2   | 46.8       | 51.4        | 46.8         | 49.5         | <b>55.0</b>  |
| <b>Average</b>   | 62.9   | 65.6       | 70.1        | 67.6         | 71.1         | <b>72.9</b>  |
| <b>BBH</b>       |        |            |             |              |              |              |
| Date             | 92.8   | 94.4       | 95.6        | 95.2         | 95.2         | <b>98.8</b>  |
| Formal           | 45.2   | 61.2       | 65.6        | 52.8         | 57.2         | <b>93.2</b>  |
| Geometric        | 70.8   | 76.8       | 83.6        | 84.0         | 80.0         | <b>87.6</b>  |
| Logical          | 89.2   | 95.6       | 95.6        | 96.0         | 96.5         | <b>99.5</b>  |
| Movie            | 84.8   | 88.0       | 92.8        | 92.0         | 93.2         | <b>95.2</b>  |
| ObjCount         | 93.2   | 96.8       | 99.2        | <b>100.0</b> | <b>100.0</b> | 95.2         |
| Penguins         | 93.8   | 99.3       | 99.3        | <b>100.0</b> | 99.3         | 99.3         |
| ReasonColored    | 92.8   | 97.6       | 98.4        | 98.8         | 98.8         | <b>100.0</b> |
| RuinNames        | 64.8   | 74.8       | 69.6        | 70.0         | 80.0         | <b>93.6</b>  |
| TranslationError | 52.4   | 68.4       | 60.4        | 60.0         | 63.6         | <b>75.2</b>  |
| Temporal         | 86.4   | 98.4       | 93.2        | 96.8         | 98.0         | <b>100.0</b> |
| WordSort         | 27.2   | 36.4       | 16.0        | 14.8         | 42.0         | <b>56.0</b>  |
| <b>Average</b>   | 74.5   | 82.3       | 80.8        | 80.0         | 83.7         | <b>91.1</b>  |

Table 4: Hits@K accuracy of *fLSA* versus directly sampling without tags (*No Tag*), two-step sampling with LLM-generated outline (*GenOutline*), traditional LDA (*TradLDA*), traditional LDA with LLM-generated tag descriptions (*TradLDA+LLM*) (Li et al., 2023), and the prompting baseline (*Prompting*) (Mu et al., 2024) on 12 challenging tasks from BBH benchmark (Suzgun et al., 2022) and 7 tasks from MATH (Hendrycks et al., 2021).

improves over direct sampling on most tasks, but still underperforms hierarchical sampling with *fLSA* by 7–9 points. These results indicate that hierarchical sampling using tags derived from the domain-specific documents via *fLSA* produces more effective output solutions, thereby increasing the likelihood of hitting the correct answer with K samples.

Next, we compare *fLSA* with hierarchical sampling with existing tagging approaches. *fLSA* tags expand the output space in the directions that lead to correct answers more often than TradLDA on 16 out of 19 tasks. It brings an average Hits@K Accuracy improvement of 3–10 points over TradLDA. Similarly, compared with TradLDA+LLM, *fLSA* achieves higher Hits@K Accuracy on 17 out of 19 tasks and improves the average accuracy by 5–11 points across BBH and MATH. Compared with the Prompting baseline, *fLSA* achieves higher Hits@K Accuracy on 14 out of 19 tasks. Overall, hierarchical sampling with *fLSA* tags improves Hits@K

Accuracy over existing tagging approaches by 2–11 points on average.

## 6 Conclusion

We introduced *fLSA*, a foundation-model-based Latent Semantic Analysis method that aims to uncover the latent semantic structures in document collections by iteratively clustering and tagging document segments based on document-level contexts. Our experiments on story writing, math and multi-step reasoning tasks show that *fLSA* tags are more informative in reconstructing the original texts than tags generated by existing tagging methods. *fLSA* tags are also useful in expanding the output space via hierarchical sampling to increase the likelihood of discovering correct solutions to complex reasoning problems. These results suggest the potential of *fLSA* for generating effective task guidelines given some worked-out examples, along with hierarchical sampling and searching for problem solutions on challenging reasoning tasks.

## 7 Limitations

One limitation of *fLSA* is that some of the tags produced by *fLSA* may be semantically similar to each other, which can be ideally merged into a single tag. This limitation could be addressed by incorporating a tag fusion step in the EM algorithm, which we leave for future work. In addition, although the *fLSA* algorithm is agnostic to the LLM being used, we only test it on GPT-4 (which is one of the most powerful and widely used LLMs). Testing the algorithm on smaller models can be an interesting future work.

This work also has potential risks. One major risk is that the tags learned using *fLSA* may reflect the undesirable biases within the LLM being used. Integrating bias detection and mitigation techniques within the algorithm could be useful for addressing the issue.

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