RANGE-NULL LATENT PRIOR-GUIDED CONSISTENCY MODEL FOR LOW LIGHT IMAGE ENHANCEMENT

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ABSTRACT

Low light image enhancement (LLIE) is a challenging task, with most existing models often struggling to adapt to diverse dark environments due to insufficient training datasets. In this paper, we propose a novel unsupervised model called Range-null Latent Prior-guided Consistency Model (RLPCM), which integrates a latent consistency model (LCM) into low light enhancement using Retinex-based range-null space decomposition. RLPCM leverages an off-the-shelf LCM as a generative prior to improve both the latent consistency and realness of enhanced images. Meanwhile, fine-tuning a lighting decoder solely on normal-light images to ensure high fidelity in image space. A key contribution is a simple yet effective global illumination adjustment applied to the range-space component, along with a natural language guidance module to learn the null-space component. This allows for iterative generation to enhance both consistency and realness in just a few steps. Additionally, we present a new UAV low light dataset (UAV-LL) containing 300 image pairs from various UAV scenarios to support comprehensive evaluation. Extensive experiments demonstrate the superior adaptability and effectiveness of our framework across a wide range of low-light environments.

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028 1 INTRODUCTION

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Low light image enhancement (LLIE) is a long-standing problem that influences both human visual perception and related computer vision tasks, such as depth estimation Wang et al. (2021), object 031 detection Hashmi et al. (2023), and semantic segmentation Pan et al. (2024). Current LLIE approaches are generally categorized into two types: supervised and unsupervised methods. Supervised methods 033 Weng et al. (2024); Cai et al. (2023); Jiang et al. (2023) typically rely on paired images to train 034 end-to-end models, but acquiring pixel-aligned image datasets is particularly challenging, especially in mobile environments. On the other hand, unsupervised methods Ma et al. (2022); Yang et al. (2023); Liang et al. (2023) have gained traction by minimizing the need for paired data. Among these, 037 diffusion-based models Wang et al. (2024); Jiang et al. (2024a) have attracted significant attention 038 for their powerful generative capabilities. Therefore, in this paper, we focus on diffusion-based approaches for low light image enhancement.

Most diffusion-based models for the LLIE task have integrated low-light image and illumination as conditional inputs to preserve image details and enhance illumination quality, as shown in Figure 1(a).
For instance, QuadPrior Wang et al. (2024) introduces an illumination-invariant prior as a conditional generative model utilizing ControlNet Zhang et al. (2023). Similarly, LightenDiffusion Jiang et al. (2024a) employs a Retinex-based diffusion model that works with unpaired images, decomposing them into reflectance and illumination maps. However, these approaches lack an effective latent prior to guide the conditional diffusion process, often resulting in suboptimal enhancement outcomes and time-consuming procedures.

Recently, the denoising diffusion null-space model (DDNM) Wang et al. (2023b) incorporated
range-null space decomposition Schwab et al. (2019) into diffusion models to address various image
restoration (IR) tasks, such as image super-resolution, colorization, and deblurring. This method
identifies appropriate null-space components to ensure realistic results, while applying a specific
degradation operator to preserve range-space content for data consistency, thus achieving effective
performance. However, DDNM depends on explicit degradation priors, which are challenging to
obtain for LLIE task, and is often limited by slow inference speed.



Figure 1: (a) Existing diffusion-based models, such as DiffLL, QuadPrior, and LightenDiff, require the diffusion network to be trained with specific conditions. (b) The schematic process shows that the range-space anchor serves as a more effective initial latent prior. By applying our updating rule, the result in latent space becomes closer to the ground truth (GT). (c) We introduce a range-null latent prior-guided framework for the LLIE task, featuring a training-free diffusion process.

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068 To address these issues, we propose a novel unsupervised framework called **R**ange-null Latent **P**rior-069 guided (**RLP**) for the LLIE task, as illustrated in Figure 1(c). To accelerate the diffusion process, the latent consistency model (LCM) Song et al. (2023) is integrated into low-light enhancement by 071 leveraging Retinex-based range-null space decomposition to identify relevant null-space content, 072 referred to as the RLP Consistency Model (RLPCM) in Figure 2. Our approach integrates a physicsdriven model, *i.e.*, Retinex theory Land & McCann (1971), with null-space decomposition to introduce 073 global illumination degradation that guides the range-space content. RLPCM relies solely on a current 074 off-the-shelf latent consistency model as the generative prior, fine-tuning a lighting decoder with 075 normal light images to enhance fidelity in the image space. We introduce a simple vet effective global 076 illumination prior that fixes the range-space component within the range-null space decomposition. 077 Additionally, we design a natural language guidance mechanism to facilitate learning in the null-078 space, enabling a few-step iterative generation process that effectively and fast balances the latent 079 consistency and the realness.

In this paper, our key findings and contributions are summarized as follows: 1) To the best of our 081 knowledge, we are the first to introduce a consistency model into the LLIE task, effectively bridging Rang-null space decomposition with the Retinex theory into the consistency model. Compared 083 to existing diffusion methods, our approach exhibits superior flexibility and robust across diverse 084 scenarios. 2) We propose a range-null latent prior-guided framework for the LLIE task, featuring a 085 simple yet efficient global illumination prior that physically guarantees the reliability of range-space content, this prior can be manually adjusted during inference, thus avoiding the irreversible effects 087 associated with fixed parameters. Additionally, we incorporate language-aware guidance mechanisms 880 to facilitate the learning of null-space content. 3) We present a novel UAV low-light dataset (UAV-LL), comprising 300 image pairs captured in various mobile environments. This dataset allows for a comprehensive evaluation of the generalization capabilities of existing methods under previously 090 unseen conditions. For the related work, please refer to Appendix A. 091

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2 METHODOLOGY

2.1 PRELIMINARIES

Retinex Theory. Among physics-driven models fundamental to LLIE, Retinex theory Land & McCann (1971) stands out as a key approach. The vanilla Retinex theory assumes that a low-light image y can be decomposed into illumination A and reflectance x. Typically, x, being an invariant physical property, is regarded as the ideal enhanced outcome. This relationship is expressed mathematically by the Retinex theory as:

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$$\mathbf{y} = \mathbf{A} \odot \mathbf{x},\tag{1}$$

where ⊙ denotes the pixel-wise multiplication. But, accurately decomposing illumination A to
estimate reflectance x remains a ill-posed problem. Traditional methods Guo et al. (2017), are
typically Retinex-based illumination optimization problem. Most current methods Weng et al. (2024);
Cai et al. (2023) aim to train end-to-end models that directly map x to y, bypassing the need for
explicit illumination estimation. However, these methods often rely on hand-crafted priors or task-

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Figure 2: An overview of our RLP Consistency Model (RLPCM), based on the RLP framework in the Figure 1(c). The low-light image y and range-space content $A^{\dagger}y$ are both transformed into latent space via a pre-trained encoder, producing \hat{z} and z, respectively. Here, z serves as a range-space anchor in the latent space, while the null-space content is refined using training-free conditional consistency sampling with language-aware attention swapping. Finally, a lighting decoder is finetuned with skip connections to preserve high fidelity, ensuring accurate reconstruction.

specific training, which limits their robustness and flexibility in diverse scenarios. Thus, integrating
 Retinex theory with pre-trained, off-the-shelf models presents a potentially promising solution.

Range-null Space Decomposition. offers a promising method to integrating Retinex theory with pre-trained, off-the-shelf models. Given a non-zero linear operator $\mathbf{A} \in \mathbb{R}^{mn \times mn}$, its pseudoinverse $\mathbf{A}^{\dagger} \in \mathbb{R}^{mn \times mn}$ satisfies the equation $\mathbf{A}\mathbf{A}^{\dagger}\mathbf{A} = \mathbf{A}$. Hence, any sample $\mathbf{x} \in \mathbb{R}^{mn \times 1}$ can be decomposed into the range and null spaces of \mathbf{A} as follows:

$$= \mathbf{A}^{\dagger} \mathbf{A} \mathbf{x} + (\mathbf{I} - \mathbf{A}^{\dagger} \mathbf{A}) \mathbf{x}, \tag{2}$$

where the first term $\mathbf{A}^{\dagger}\mathbf{A}\mathbf{x}$ represents the range-space content due to $\mathbf{A}\mathbf{A}^{\dagger}\mathbf{A}\mathbf{x} = \mathbf{A}\mathbf{x}$, and the second term represents the null-space content as $\mathbf{A}(\mathbf{I} - \mathbf{A}^{\dagger}\mathbf{A})\mathbf{x} = 0$. Now, we reinterpret Retinex theory in the context of range-null space for a low-light image y, aiming to derive the reflectance $\hat{\mathbf{x}}$ under the following constraints:

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onsistency:
$$A\hat{\mathbf{x}} = \mathbf{y}$$
, Realness: $\hat{\mathbf{x}} \sim p(\mathbf{x})$, (3)

138 where $p(\mathbf{x})$ denotes the real reflectance distribution of \mathbf{x} . The general solution for reflectance $\hat{\mathbf{x}}$ that 139 satisfies the consistency constraint is given by $A\hat{\mathbf{x}} = \mathbf{y}$, leading to $\hat{\mathbf{x}} = A^{\dagger}\mathbf{y} + (\mathbf{I} - A^{\dagger}A)\hat{\mathbf{x}}$. The term $\tilde{\mathbf{x}}$ influences the realistic details in the null-space. Previous methods have sought to estimate 140 the null-space content $\tilde{\mathbf{x}}$ using GANs Wang et al. (2023a) and diffusion models Wang et al. (2023b); 141 Gandikota & Chandramouli (2024), but these methods inherit limitations such as the randomness 142 inherent in diffusion models. In contrast, we observe that the consistency model Song et al. (2023) 143 is more effective for generating null-space content due to its self-consistency property, while also 144 providing faster inference speeds compared to existing diffusion models. 145

146 Consistency Models. Consistency models Song et al. (2023) are a novel class of generative models that have shown considerable potential across various vision tasks, including image generation and 147 editing. Unlike diffusion models Ho et al. (2020); Song et al. (2021), consistency models enable 148 single-step iterative generation, allowing for direct mapping from any point on the Probability Flow 149 (PF) ODE trajectory back to its origin. Specifically, given a sequence of time points $\tau_i \in [\kappa, T]$, 150 where $\tau_{\kappa} > \tau_{\kappa+1} > \cdots > \tau_T$, the solution trajectory $\{\mathbf{x}_{\tau_i}\}, \tau_i \in [\kappa, T]$ belongs to the PF ODE. 151 The consistency function is defined as $f_{\phi}(\mathbf{x}_{\tau_i}, \tau_i) \to \mathbf{x}_{\tau_{\kappa}}$, and its self-consistency ensures that 152 $f_{\phi}(\mathbf{x}_{\tau_{\tilde{\kappa}}}, \tau_{\tilde{\kappa}}) = f_{\phi}(\mathbf{x}_{\tau_{\tilde{\kappa}}}, \tau_{\hat{\kappa}})$ for $\tilde{\kappa}, \hat{\kappa} \in [\kappa, T]$. Recently, latent consistency models (LCM) Luo et al. 153 (2023) have further enhanced efficiency by transforming \mathbf{x} into latent space \mathbf{z} , resulting in improved 154 computational performance. LCMs can be trained by distilling pre-trained diffusion models. In this 155 work, we use the following LCM parameterization: 156

$$f_{\phi}\left(\mathbf{z}, c, \tau_{i}\right) = s_{\kappa}\left(\tau_{i}\right)\mathbf{x} + s_{\text{out}}\left(\tau_{i}\right)\hat{\mathbf{z}}_{0} \tag{4}$$

$$\hat{\mathbf{z}}_{0} = \left(\frac{\mathbf{z}_{\tau_{i}} - \sigma\left(\tau_{i}\right)\epsilon_{\phi}\left(\mathbf{z}, c, \tau_{i}\right)}{\alpha\left(\tau_{i}\right)}\right),\tag{5}$$

160 where $s_{\kappa}(\tau_i)$ and $s_{out}(\tau_i)$ are differentiable functions specifically defined as $s_{\kappa}(\tau_i) = 0$ and 161 $s_{out}(\tau_i) = 1$, and $\epsilon_{\phi}(\mathbf{z}, c, \tau_i)$ is the teacher diffusion model, whose forward process can be ef-161 fectively expressed as $\mathbf{z}_{\tau_i} = \alpha(\tau_i) \mathbf{z}_0 + \sigma(\tau_i) \epsilon_{\phi}$.

162 2.2 OUR APPROACH

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164 Our goal is to establish a credible range-space that produces consistent results while accurately 165 identifying a suitable null-space to enhance realness. Unlike the super-resolution and deblurring tasks that can define explicit degradation operators, LLIE is affected by variable illumination conditions, 166 which complicates the design of a unified degradation operator. Building upon our RLP framework 167 illustrated in the Figure 1(c), we introduce a Range-Null Latent Prior-guided Consistency Model 168 (RLPCM), as depicted in Figure 2. RLPCM leverages Retinex theory to propose an adaptive and flexible illumination degradation factor derived from low-light images, thereby stabilizing the range-170 space component. Furthermore, we guide the null-space content through established consistency 171 models by employing natural language for a more intuitive representation. 172

Range-space Content Correction. Given a low-light image 173 y, we first construct an illumination degradation factor A, 174 which will be discussed in detail in subsection 2.3, and then 175 derive the range-space content using $A^{\dagger}y$. Subsequently, we 176 employ an off-the-shelf latent consistency model $f_{\phi}(\cdot, \cdot, \cdot)$ 177 Luo et al. (2023) and transform the low-light image y and 178 range-space content $A^{\dagger}y$ into the latent space as \hat{z} and z, 179 respectively, via a pre-trained encoder. In this context, we consider z as the anchor representing range-space content in 181 the latent space. Notably, the origin of the ODE trajectory of 182 the LCM may be situated far from this anchor, and we thus maintain a fixed distance between the anchor and the output 183 of the LCM as follows: 184

$$\epsilon = \mathbf{z} - f_{\phi} \left(\hat{\mathbf{z}}, c_{\text{null}}, \tau_i \right), \tag{6}$$

187 where τ_i represents the time point and c_{null} denotes the null 188 condition. This distance ϵ is designed to bridge the gap, as il-189 lustrated in Figure 3. This bridging mechanism is essential for 190 maintaining alignment between the generated output and the 191 expected range-space content. The model's self-consistency



Figure 3: Schematic of range-null space decomposition in latent space. The dotted green line represents the trajectory of LCM. In the latent space, the range and null-space content are adjusted along the LCM's original trajectory, moving the position closer to the optimal result.

ensures that ϵ consistently points toward the anchor, thereby enhancing the overall coherence of the transformation process. Next, the key problem is to identify an appropriate null-space content that guarantees the realness results.

Language-aware Null-space Content Refinement. Inspired by Classifier-Free Guidance (CFG) Ho
 & Salimans (2022) for generating high-quality language-aligned images, we design a language-aware
 null-space content refinement module. Specifically, we utilize two contrasting language prompts to
 sample the conditional results, and the entire process can be articulated as follows:

$$\Delta \epsilon = f_{\phi} \left(\hat{\mathbf{z}}, c_n, \tau_i \right) - f_{\phi} \left(\hat{\mathbf{z}}, c_l, \tau_i \right), \tag{7}$$

where $\Delta \epsilon$ denotes the null-space content aimed at improving the realness, c_l denotes low-light language prompt, c_n denotes normal-light language prompt. Recall the CFG Ho & Salimans (2022) employed in the LCM Luo et al. (2023), which involves replacing the original noise prediction with a linear combination of both conditional and unconditional noise derived from the teacher diffusion model, expressed as: $\tilde{\epsilon}_{\theta}(\mathbf{z}_{\tau_i}, \omega, c, \tau_i) := (1 + \omega)\epsilon_{\theta}(\mathbf{z}_{\tau_i}, c, \mathbf{z}_{\tau_i}) - \omega\epsilon_{\theta}(\mathbf{z}_{\tau_i}, c_{\text{null}}, \mathbf{z}_{\tau_i})$ and ω is called the guidance scale. We can rewrite equation 7 as follows:

$$\Delta \epsilon = (1 + w_1) f_{\phi} \left(\hat{\mathbf{z}}, c_n, \tau_i \right) - (1 + w_2) f_{\phi} \left(\hat{\mathbf{z}}, c_l, \tau_i \right) + (w_2 - w_1) f_{\phi} \left(\hat{\mathbf{z}}, c_{\text{null}}, \tau_i \right), \tag{8}$$

By combining equation 6 and equation 8, therefore, we can derive the complete range-null space decomposition result as follows:

$$\bar{\mathbf{z}} = \epsilon + f_{\phi} \left(\hat{\mathbf{z}}, c_{\text{null}}, \tau_i \right) + \left(\mathbf{I} - \gamma \mathbf{A}^{\dagger} \mathbf{A} \right) \Delta \epsilon \quad \longrightarrow \quad \bar{\mathbf{z}} = \mathbf{z} + \left(\mathbf{I} - \gamma \mathbf{A}^{\dagger} \mathbf{A} \right) \Delta \epsilon \tag{9}$$

where we set $\gamma \in [0, 1]$ to prevent $(\mathbf{I} - \gamma \mathbf{A}^{\dagger} \mathbf{A}) \equiv 0$, thereby enhancing the null-space content. Additionally, providing an accurate language condition poses a challenge in preserving texture while improving illumination for Low-Light Image Enhancement (LLIE). Inspired by MasaCtrl Cao et al. (2023) and Infedit Xu et al. (2024), we employ a swapping self-attention mechanism that facilitates non-rigid semantic transformations for image style transfer. This approach allows for querying local

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216 Algorithm 1 Range-Null Latent Prior-guided Consistency Model for LLIE 217 1: **Input:** Low light image y, Global illumination intensity ϖ , Low light prompt c_1 , Normal light 218 prompt c_n , language guidance scale w_1 and w_2 , time-step scheduler τ_T , off-the-shelf LCM 219 $f_{\phi}(\cdot, \cdot, \cdot)$ and encoder $\mathcal{E}(\cdot)$ and fine-tuned lighting decoder $\mathcal{D}(\cdot)$ 220 2: Output: Enhanced image $\hat{\mathbf{x}}$ 221 3: $\mathbf{A} = \overline{\omega} \mathbf{I}, \mathbf{A}^{\dagger} = \frac{1}{\overline{\omega}} \mathbf{I},$ ▷ Pseudo-inverse 222 4: $\hat{\mathbf{z}}, \cdot = \mathcal{E}(\mathbf{y}); \mathbf{z}, \mathbf{r} = \mathcal{E}(\mathbf{A}^{\dagger}\mathbf{y}),$ ⊳ Encoder 223 ▷ Fix range-space content $\begin{array}{lll} \vdots & (\mathbf{z} - \mathbf{z}) & (\mathbf{z}, c_{\text{null}}, \tau_i), & (\mathbf{z}, c_n, \tau_i), \\ \vdots & (\mathbf{z} - \mathbf{z}) & (\mathbf{z}, c_n, \tau_i), \\ \vdots & (\mathbf{z} - \mathbf{z}) & (\mathbf{z}, c_{null}, \tau_i), \\ & (\mathbf{z}, c_{null}, \tau_i), \\ \vdots & (\mathbf{z}, c_{null}, \tau_i) & (\mathbf{z}, c_n, \tau_i) & (\mathbf{z}, c_n, \tau_i) & (\mathbf{z}, c_n, \tau_i), \\ & (\mathbf{z} - \mathbf{z}) & (\mathbf{z}, c_{null}, \tau_i), \\ \vdots & (\mathbf{z} - \mathbf{z}) & (\mathbf{z}, c_{null}, \tau_i) & (\mathbf{z} - \mathbf{z}) & (\mathbf{z}, c_n, \tau_i) & (\mathbf{z} - \mathbf{z}) & ($ 5: $\epsilon = \mathbf{z} - f_{\phi} (\hat{\mathbf{z}}, c_{\text{null}}, \tau_i),$ 224 225 226 227 $\hat{\mathbf{z}}
ightarrow \hat{\mathbf{z}}_{ au_i}$ 9: 228 $\epsilon = \tilde{\mathbf{z}} - f_{\phi} \left(\hat{\mathbf{z}}_{\tau_i}, c_{\text{null}}, \tau_i \right)$ 10: 229 $\Delta \epsilon = (1 + w_1) f_{\phi} \left(\hat{\mathbf{z}}_{\tau_i}, c_n, \tau_i \right) - (1 + w_2) f_{\phi} \left(\hat{\mathbf{z}}_{\tau_i}, c_l, \tau_i \right) + (w_2 - w_1) f_{\phi} \left(\hat{\mathbf{z}}_{\tau_i}, c_{\text{null}}, \tau_i \right),$ 11: 230 $\bar{\mathbf{z}} = \mathbf{z} + (\mathbf{I} - \gamma \mathbf{A}^{\dagger} \mathbf{A}) (\epsilon + \Delta \epsilon)$ 12: 231 $\tilde{\mathbf{z}} = \bar{\mathbf{z}}$ 13: 232 14: end for 233 15: **Return** $\bar{\mathbf{x}} = \mathcal{D}(\bar{\mathbf{z}}, \mathbf{r}).$ ▷ Decoder 234

content and textures from low-light images, ensuring consistency is maintained. Our objective is to implement language-aware illumination attention that enhances illumination while preserving the original content of the low-light image. Specifically, we use the original Q_n , K_n , and V_n in self-attention mechanism. Subsequently, we query semantically similar content from K_l and V_l using the target query Q_n . The attention mechanism can be expressed in matrix form as follows:

Attention
$$(\mathbf{Q}_n, \mathbf{K}_l, \mathbf{V}_l) = \operatorname{Softmax}\left(\frac{\mathbf{Q}_n \mathbf{K}_l^T}{\sqrt{d}}\right) \mathbf{V}_l.$$
 (10)

Lighting Decoder. Once the range-null content in the latent space is refined, we propose a lighting decoder that converts \bar{z} to image space as \bar{x} . This entire process can be expressed as follows:

$$\mathbf{z}, \mathbf{r} = \mathcal{E}(\mathbf{x}),\tag{11}$$

$$\bar{\mathbf{x}} = \mathcal{D}(\bar{\mathbf{z}}, \mathbf{r}). \tag{12}$$

250 where \bar{z} is refined from z in equation 9, and r is the middle-layer feature. Our lighting decoder incorporates additional convolutional layers for hidden feature fusion and utilizes skip connections. 251 To our knowledge, QuadPrior Wang et al. (2024) introduced a bypass decoder that effectively captures 252 details from randomly degraded images and is sensitive to illumination changes. However, it has 253 notable limitations: the bypass decoder is trained on the COCO dataset Lin et al. (2014), which 254 contains underexposed and low-quality images, thereby compromising its decoding capabilities. 255 Additionally, its performance in recovering complex textures under varying illumination conditions is 256 constrained, as the random illumination jittering and noise do not integrate a physical model of LLIE. 257

To address the aforementioned issues, we collect a well-exposed image dataset from benchmark sources and the internet to ensure high-quality training data. We then fine-tune the lighting decoder to accept both Retinex-driven degraded images and normal images, allowing it to adapt to illumination degradation effectively. This approach ensures that the model remains sensitive to variations in illumination within the latent space while preserving high fidelity through skip connections. The overall objective for training the decoder model can be formulated as follows:

$$L = \min\max\left(L_{\text{rec}}\left(\mathbf{x}, \mathcal{D}\left(\mathcal{E}(\tilde{\mathbf{x}}), \mathbf{r}\right)\right) + L_{\text{reg}}\left(\mathbf{z}; \mathcal{E}, \mathcal{D}\right)\right)$$
(13)

where $\tilde{\mathbf{x}}$ is the Retinex-driven degraded images. L_{rec} denotes the pixel-wise reconstruction losses, including MSE and LPIPS, while L_{reg} regularizes the latent \mathbf{z} to be zero centered and small variance.

It is worth noting that our method also supports rapid one-step generation while also enabling multi step sampling, allowing for a trade-off between computational efficiency and enhancement quality, much like traditional consistency models.



Figure 4: The distribution and intensity of average and difference illumination from the statistics of the low/normal light image pairs.

2.3 CONSTRUCTING ILLUMINATION FACTOR A

Rather than focusing on precise illumination estimation, we reconsider Retinex theory through the lens of Range-null space decomposition and propose a simple yet effective global illumination intensity. We introduce the following proposition:

Proposition 1. We assume that the low-light image mainly suffers from the global degeneration operator ϖ in illumination intensity **A**, which is a non-zero constant matrix. When we set the constant of **A** as ϖ , its pseudo-inverse **A**[†] can be easily calculated as

$$\mathbf{A}^{\dagger} = \frac{1}{\varpi} \mathbf{I}.$$
 (14)

Hence, we present a simple yet interpretable range-space content $\mathbf{A}^{\dagger}\mathbf{y}$ for the LLIE task. It is then encoded into latent space as $\mathbf{z} = \mathcal{E}(\mathbf{A}^{\dagger}\mathbf{y})$. The proof can be found in the appendix B.

To validate the universality of global illumination reduction, we gather approximately 7,000 low and normal light image pairs from existing benchmark datasets, including LOLv1 Wei et al. (2018), LOLv2 Yang et al. (2021), LSRW Hai et al. (2023), and our UAV-LL dataset. We conducted a study on the illumination degradation between these paired images. Specifically, we first estimated the average global illumination intensity. Following the methodology of Guo et al. (2017), we computed pixel-wise illumination by selecting the maximum value across the three color channels as the global illumination and then calculated the difference between this value and the average illumination.

As illustrated in Figure 4(a), the global illumination intensity in low-light images is low and uniformly distributed between 0.1 and 0.4. Additionally, Figure 4(b) shows that the average difference intensity predominantly ranges from 0 to 15, indicating that the pixel-wise illumination is close to the average illumination. By observing toy examples of the illumination and difference maps in Figure 4(c), we have a reason to believe that most low-light images exhibit characteristics of global degradation.

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3 EXPERIMENTS

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3.1 DATASETS AND IMPLEMENTATION DETAILS

Datasets. We evaluate our method on two paired benchmark datasets: LOL+ and LSRW Hai et al. (2023). Following Wang et al. (2024), we adopt LOL+ consists of 115 low and normal light image pairs from LOLv1 Wei et al. (2018) and LOLv2 Yang et al. (2021), while LSRW contains 50 pairs. To further assess generalization capabilities, we introduce a new UAV-LL dataset, referred to Appendix C, comprising 300 image pairs captured in diverse mobile environments For fine-tuning the lighting decoder, we gathered 7,000 normal images from benchmark datasets and the internet.

Compared Methods. We compare our method with five SOTA supervised methods, including
 URetinex-Net Wu et al. (2022), R2RNet Hai et al. (2023), Retinexformer Cai et al. (2023), GSAD
 Hou et al. (2023) and DiffLL Jiang et al. (2023), all of which achieve state-of-the-art results on
 benchmark datasets. Furthermore, we compare our method with nine unsupervised low-light image



Table 1: Quantitative comparisons on LOL+, LSRW and UAV-LL dataset. The best unsupervised result is in red color, while the second best result is in blue color under the unsupervised setting.

Figure 5: Qualitative comparison with previous methods on LOL+, LSRW and UAV-LL datasets. Our RLPCM effectively improve the realness and preserves the details compared to other methods.

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enhancement approaches, including EnlightenGAN Jiang et al. (2021), ZeroDCE Guo et al. (2020),
SCI Ma et al. (2022), PairLIE Fu et al. (2023), NeRCo Yang et al. (2023), CLIP-LIT Liang et al. (2023), QuadPrior Wang et al. (2024), and LightenDiffusion Jiang et al. (2024a). Additionally, we
evaluate the cross-dataset generalization of these pre-trained models by applying to UAV-LL datasets.

Implementation Details. We implement RLPCM in PyTorch Paszke et al. (2019) on a server with the 4090GPUs. In our framework, LCM is tuning-free, only needs to fine-tune the lighting decoder.

DDNM GDP DDNM Input GDP Input AutoIR Ours GT AutoIR Ours GT

Figure 6: Qualitative comparison with diffusion-based image restoration Methods on LOLv1 datasets. Our method yields the most reasonable and satisfactory results across all methods +.

Method		LOL			LSRW		
		PSNR	SSIM	LPIPS	PSNR	SSIM	LPIPS
Range-null Space Refinment	w/o Range-space content	22.90	0.805	0.128	18.92	0.557	0.239
	w/o Null-space content	15.01	0.555	0.169	14.06	0.394	0.270
Decoder	vanilla decoder	22.04	0.729	0.131	18.20	0.529	0.229
	bypass decoder	23.01	0.787	0.148	19.08	0.545	0.267
Ours		24.07	0.837	0.105	19.11	0.570	0.204

We set the batch size to 8 and train for 140k steps, with an initial learning rate of 1e-4 using the ADAM optimizer. For evaluation, we report peak signal-to-noise ratio (PSNR), structural similarity (SSIM) and LPIPS Zhang et al. (2018) is selected as the evaluation metrics.

3.2 MAIN RESULTS

403 Quantitative Comparison. As shown in Table 1, we evaluated the performance of our RLPCM with five SOTA supervised methods and nine unsupervised methods. Our RLPCM surpasses all 404 unsupervised methods on LOL dataset in terms of PSNR SSIM and LPIPS, and achieves comparable 405 performance with the supervised methods, while our approach achieves robust performance across 406 all datasets, further emphasizing its generalizability and effectiveness. 407

408 To further validate the performance of existing methods, we use the released models trained using 409 their own data for evaluation on our proposed UAV-LL dataset. Despite the current diffusion models, 410 GSAD and DiffLL, achieve the SOTA results in LOL datasets, ones exhibit the limited performance to new scenarios. In contrast, the unsupervised diffusion methods ,i.e., our model, QuadPrior and 411 LightenDiffusion, outperform than all pre-trained supervised methods, and our approach has the 412 better result than others. 413

414 Qualitative Comparison. Figure 5 summarises the vision results of our method with other SOTA 415 methods among LOL+, LSRW and UAV-LL datasets. It is observed that existing methods suffer from overexposure or underexposure illumination and noise, while our method provide a proper 416 illumination and effectively suppress the noise. Notably, the ground-truth image of UAV-LL dataset 417 has a trade-off between illumination and noise, since our UAV-LL is captured on the real low light 418 scenarios. The limitation and more results and are provided in Appendixes D and E, respectively. 419

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3.3 COMPARING WITH DIFFUSION-BASED IMAGE RESTORATION METHODS

422 To further verify the effectiveness of our 423 framework, we compare our approach 424 with several state-of-the-art (SOTA) 425 diffusion-based image restoration meth-426 ods, including GDP Ben Fei (2023), 427 DDNM Wang et al. (2023b), and Au-428 toDIR Jiang et al. (2024b). Following 429 the evaluation method used in GDP, we assess the results on the LOLv1 dataset 430 Wei et al. (2018). As shown in Table 431 2, our method achieves the best perfor-

Table 2: Quantitative comparison with diffusion-based
image restoration methods on LOLv1 datasets. The best
result is in red color.

Method	PSNR	SSIM	LPIPS	Time (S)
GDP (CVPR 23)	13.93	0.630	0.680	60.00+
DDNM (ICLR 23)	13.15	0.492	0.498	5.47
AutoIR (ECCV 24)	19.95	0.811	0.107	28.98
Ours	24.12	0.826	0.103	0.84



Figure 7: Visual results of the ablation study on the Range-null space and Decoder, our proposed full model exhibits improved detail handling in the local images.



Figure 8: Visual results of the ablation study on natural language guidance, iteration steps, and the self-attention swapping mechanism.

mance on the LOLv1 dataset, while our inference speed is significantly higher than that of other models. This improvement is attributed to the introduction of a consistency model, which reduces the number of iterations. Furthermore, our latent prior-guided framework does not reduce the inference efficiency. Besides, Due to the limitation of DDNM, i.e, explicit degradation priors, we introduce our proposed global degeneration operator into DDNM, which also yields an acceptable results. In Figure 6, our method yields the most reasonable and satisfactory results across all methods.

460 3.4 ABLATION STUDY 461

We present ablation studies to demonstrate the effectiveness of the each part in our proposed RNLP. For range-null space, we remove the range-space content and null-space content, respectively. For refining the null-space content in latent space, we remove the self-attention swapping mechanism, while discuss the effect of different language prompts and its guidance scale. For the fidelity, we compare the lighting decoder with vanilla decoder, consistency decoder and bypass decoder.

467 The quantitative restuls of the ablated study on LOL+ and LSRW are presented in Table 3. Overall, 468 the range-null space refinement provide a key contribute to achieve the best performance of the 469 full model. Without either the range-space or null-space content, there would be a rapid decline in performance. In comparison, the impact of the decoder on the results is relatively smaller. As shown 470 in Figure 7 a suboptimal decoder may lead to color distortion or content degradation. Furthermore, we 471 compare the influence of natural language guidance, iteration steps, and the self-attention swapping 472 mechanism in Figure 8. Specifically, natural language guidance can appropriately alter the tone of 473 an image without impacting its content. However, in the absence of the self-attention swapping 474 mechanism, irrelevant content may be introduced, highlighting the necessity of this mechanism. 475 Lastly, the results indicate that our method requires only a few steps (or even just one) to achieve 476 relatively satisfactory results. 477

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4 CONCLUSION

In this paper, we presented a range-null latent prior-guided consistency model, a novel approach
 that introduces an off-the-shelf consistency model into low-light image enhancement using Retinex based range-null space decomposition. Additionally, we contributed a new UAV LLIE dataset
 for comprehensive evaluation. Extensive experiments on both benchmark and UAV-LL datasets
 demonstrate that our model achieves robust performance. In future work, we aim to explore model
 distillation and extend the latent prior-guided framework to low-light video enhancement tasks.

486 REFERENCES

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488	Liang Pan Junzhe Zhang Weidong Yang Tianyue Luo Bo Zhang Bo Dai Ben Fei, Zhaoyang Lyu.
489	Generative diffusion prior for unified image restoration and enhancement. In CVPR, 2023.

- Vladimir Bychkovsky, Sylvain Paris, Eric Chan, and Frédo Durand. Learning photographic global tonal adjustment with a database of input / output image pairs. In <u>CVPR</u>, pp. 97–104, 2011.
- Jianrui Cai, Shuhang Gu, and Lei Zhang. Learning a deep single image contrast enhancer from multi-exposure images. IEEE Transactions on Image Processing, 27(4):2049–2062, 2018.
- Yuanhao Cai, Hao Bian, Jing Lin, Haoqian Wang, Radu Timofte, and Yulun Zhang. Retinexformer: One-stage retinex-based transformer for low-light image enhancement. In <u>ICCV</u>, pp. 12504–12513, October 2023.
- Mingdeng Cao, Xintao Wang, Zhongang Qi, Ying Shan, Xiaohu Qie, and Yinqiang Zheng. Masactrl:
 Tuning-free mutual self-attention control for consistent image synthesis and editing. In <u>ICCV</u>, pp. 22503–22513, 2023.
- Zhenqi Fu, Yan Yang, Xiaotong Tu, Yue Huang, Xinghao Ding, and Kai-Kuang Ma. Learning a simple low-light image enhancer from paired low-light instances. In <u>CVPR</u>, pp. 22252–22261, 2023.
- Kanchana Vaishnavi Gandikota and Paramanand Chandramouli. Text-guided explorable image
 super-resolution. volume abs/2403.01124, 2024. doi: 10.48550/ARXIV.2403.01124. URL
 https://doi.org/10.48550/arXiv.2403.01124.
- Albert Gu and Tri Dao. Mamba: Linear-time sequence modeling with selective state spaces. In ICML, 2024.
- Chunle Guo, Chongyi Li, Jichang Guo, Chen Change Loy, Junhui Hou, Sam Kwong, and Runmin
 Cong. Zero-reference deep curve estimation for low-light image enhancement. In <u>CVPR</u>, pp. 1777–1786, 2020.
- Xiaojie Guo, Yu Li, and Haibin Ling. LIME: low-light image enhancement via illumination map
 estimation. IEEE Trans. Image Process., 26(2):982–993, 2017.
- Jiang Hai, Zhu Xuan, Ren Yang, Yutong Hao, Fengzhu Zou, Fang Lin, and Songchen Han. R2rnet: Low-light image enhancement via real-low to real-normal network. J. Vis. Commun. Image Represent., 90:103712, 2023.
- Khurram Azeem Hashmi, Goutham Kallempudi, Didier Stricker, and Muhammad Zeshan Afzal.
 Featenhancer: Enhancing hierarchical features for object detection and beyond under low-light vision. In ICCV, pp. 6702–6712, 2023.
- Jonathan Ho and Tim Salimans. Classifier-free diffusion guidance. <u>CoRR</u>, abs/2207.12598, 2022.
- ⁵²⁶ Jonathan Ho, Ajay Jain, and Pieter Abbeel. Denoising diffusion probabilistic models. In NIPS, 2020.
- Jinhui Hou, Zhiyu Zhu, Junhui Hou, Hui Liu, Huanqiang Zeng, and Hui Yuan. Global structure-aware diffusion process for low-light image enhancement. <u>ArXiv</u>, abs/2310.17577, 2023.
- Hai Jiang, Ao Luo, Haoqiang Fan, Songchen Han, and Shuaicheng Liu. Low-light image enhancement with wavelet-based diffusion models. <u>ACM Trans. Graph.</u>, 42(6):238:1–238:14, 2023.
- Hai Jiang, Ao Luo, Xiaohong Liu, Songchen Han, and Shuaicheng Liu. Lightendiffusion: Unsuper vised low-light image enhancement with latent-retinex diffusion models. In ECCV, 2024a.
- Yifan Jiang, Xinyu Gong, Ding Liu, Yu Cheng, Chen Fang, Xiaohui Shen, Jianchao Yang, Pan Zhou, and Zhangyang Wang. Enlightengan: Deep light enhancement without paired supervision. <u>IEEE</u> <u>Trans. Image Process.</u>, 30:2340–2349, 2021.
- 539 Yitong Jiang, Zhaoyang Zhang, Tianfan Xue, and Jinwei Gu. Autodir: Automatic all-in-one image restoration with latent diffusion. In ECCV, 2024b.

540 541	Edwin H Land and John J McCann. Lightness and retinex theory. Josa, 61(1):1-11, 1971.
542 543	Zhexin Liang, Chongyi Li, Shangchen Zhou, Ruicheng Feng, and Chen Change Loy. Iterative prompt learning for unsupervised backlit image enhancement. In <u>ICCV</u> , pp. 8094–8103, 2023.
544 545 546 547	Tsung-Yi Lin, Michael Maire, Serge J. Belongie, Lubomir D. Bourdev, Ross B. Girshick, James Hays, Pietro Perona, Deva Ramanan, Piotr Dollár, and C. Lawrence Zitnick. Microsoft COCO: common objects in context. <u>CoRR</u> , abs/1405.0312, 2014.
548 549 550	Risheng Liu, Long Ma, Jiaao Zhang, Xin Fan, and Zhongxuan Luo. Retinex-inspired unrolling with cooperative prior architecture search for low-light image enhancement. <u>CVPR</u> , pp. 10556–10565, 2020.
551 552 553	Kin Gwn Lore, Adedotun Akintayo, and Soumik Sarkar. LLNet: A deep autoencoder approach to natural low-light image enhancement. <u>Pattern Recognit.</u> , 61:650–662, 2017.
554 555 556	Andreas Lugmayr, Martin Danelljan, Andrés Romero, Fisher Yu, Radu Timofte, and Luc Van Gool. Repaint: Inpainting using denoising diffusion probabilistic models. <u>CVPR</u> , pp. 11451–11461, 2022.
557 558 559	Simian Luo, Yiqin Tan, Longbo Huang, Jian Li, and Hang Zhao. Latent consistency models: Synthesizing high-resolution images with few-step inference. <u>CoRR</u> , abs/2310.04378, 2023.
560 561	Feifan Lv, Feng Lu, Jianhua Wu, and Chong Soon Lim. Mbllen: Low-light image/video enhancement using cnns. In <u>British Machine Vision Conference</u> , 2018.
562 563 564	Long Ma, Tengyu Ma, Risheng Liu, Xin Fan, and Zhongxuan Luo. Toward fast, flexible, and robust low-light image enhancement. In <u>CVPR</u> , pp. 5627–5636, 2022.
565 566	Kangfu Mei, Luis Figueroa, Zhe Lin, Zhihong Ding, Scott Cohen, and Vishal M. Patel. Latent feature-guided diffusion models for shadow removal. <u>WACV</u> , pp. 4301–4310, 2023.
567 568 569	Yuwen Pan, Rui Sun, Naisong Luo, Tianzhu Zhang, and Yongdong Zhang. Exploring reliable matching with phase enhancement for night-time semantic segmentation. In ECCV, 2024.
570 571 572	Savvas Panagiotou and Anna Sergeevna Bosman. Denoising diffusion post-processing for low-light image enhancement. <u>Pattern Recognit.</u> , 156:110799, 2023.
573 574 575 576 577	Adam Paszke, Sam Gross, Francisco Massa, Adam Lerer, James Bradbury, Gregory Chanan, Trevor Killeen, Zeming Lin, Natalia Gimelshein, Luca Antiga, Alban Desmaison, Andreas Köpf, Edward Z. Yang, Zachary DeVito, Martin Raison, Alykhan Tejani, Sasank Chilamkurthy, Benoit Steiner, Lu Fang, Junjie Bai, and Soumith Chintala. Pytorch: An imperative style, high- performance deep learning library. In <u>NeurIPS</u> , pp. 8024–8035, 2019.
578 579 580	Chitwan Saharia, Jonathan Ho, William Chan, Tim Salimans, David J. Fleet, and Mohammad Norouzi. Image super-resolution via iterative refinement. <u>IEEE Transactions on Pattern Analysis</u> and Machine Intelligence, 45:4713–4726, 2021.
581 582 583	Johannes Schwab, Stephan Antholzer, and Markus Haltmeier. Deep null space learning for inverse problems: Convergence analysis and rates. <u>Inverse Problems</u> , 35(2):025008, 2019.
584 585 586	Kai Shang, Mingwen Shao, Chao Wang, Yuanshuo Cheng, and Shuigen Wang. Multi-domain multi- scale diffusion model for low-light image enhancement. <u>Proceedings of the AAAI Conference on</u> <u>Artificial Intelligence</u> , 38(5):4722–4730, Mar. 2024.
587 588 589	Jiaming Song, Chenlin Meng, and Stefano Ermon. Denoising diffusion implicit models. In <u>ICLR</u> , 2021.
590 591	Yang Song, Prafulla Dhariwal, Mark Chen, and Ilya Sutskever. Consistency models. In <u>ICML</u> , volume 202, pp. 32211–32252, 2023.
592 593	Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N. Gomez, Lukasz Kaiser, and Illia Polosukhin. Attention is all you need. In <u>NIPS</u> , pp. 5998–6008, 2017.

594 595 596 597	Kun Wang, Zhenyu Zhang, Zhiqiang Yan, Xiang Li, Baobei Xu, Jun Li, and Jian Yang. Regularizing nighttime weirdness: Efficient self-supervised monocular depth estimation in the dark. In <u>ICCV</u> , pp. 16035–16044, 2021.
598 599 600	Wenjing Wang, Huan Yang, Jianlong Fu, and Jiaying Liu. Zero-reference low-light enhancement via physical quadruple priors. In <u>CVPR</u> , 2024.
601 602	Yinhuai Wang, Yujie Hu, Jiwen Yu, and Jian Zhang. GAN prior based null-space learning for consistent super-resolution. In <u>AAAI</u> , pp. 2724–2732, 2023a.
604 605	Yinhuai Wang, Jiwen Yu, and Jian Zhang. Zero-shot image restoration using denoising diffusion null-space model. In <u>ICLR</u> , 2023b.
606 607 608	Chen Wei, Wenjing Wang, Wenhan Yang, and Jiaying Liu. Deep retinex decomposition for low-light enhancement. In <u>BMVC</u> , pp. 155, 2018.
609 610 611	Jiangwei Weng, Zhiqiang Yan, Ying Tai, Jianjun Qian, Jian Yang, and Jun Li. MambaLLIE: Implicit retinex-aware low light enhancement with global-then-local state space. In <u>NeurIPS</u> , 2024.
612 613 614 615	Wenhui Wu, Jian Weng, Pingping Zhang, Xu Wang, Wenhan Yang, and Jianmin Jiang. Uretinex-net: Retinex-based deep unfolding network for low-light image enhancement. In <u>CVPR</u> , pp. 5891–5900, 2022.
616 617 618	Yuhui Wu, Guoqing Wang, Zhiwen Wang, Yang Yang, Tianyu Li, Malu Zhang, Chongyi Li, and Heng Tao Shen. Jores-diff: Joint retinex and semantic priors in diffusion model for low-light image enhancement. 2023.
619 620 621	Sihan Xu, Yidong Huang, Jiayi Pan, Ziqiao Ma, and Joyce Chai. Inversion-free image editing with natural language. In <u>CVPR</u> , 2024.
622 623 624	Xiaogang Xu, Ruixing Wang, Chi-Wing Fu, and Jiaya Jia. Snr-aware low-light image enhancement. In <u>CVPR</u> , pp. 17693–17703, 2022.
625 626 627	Minglong Xue, Jinhong He, Yanyi He, Zhipu Liu, Wenhai Wang, and Mingliang Zhou. Low-light image enhancement via clip-fourier guided wavelet diffusion. <u>ArXiv</u> , abs/2401.03788, 2024.
628 629 630	Shuzhou Yang, Moxuan Ding, Yanmin Wu, Zihan Li, and Jian Zhang. Implicit neural representation for cooperative low-light image enhancement. In <u>ICCV</u> , pp. 12918–12927, 2023.
631 632 633 634	Wenhan Yang, Wenjing Wang, Haofeng Huang, Shiqi Wang, and Jiaying Liu. Sparse gradient regularized deep retinex network for robust low-light image enhancement. <u>IEEE Trans. Image</u> <u>Process.</u> , 30:2072–2086, 2021.
635 636 637	Xunpeng Yi, Han Xu, H. Zhang, Linfeng Tang, and Jiayi Ma. Diff-retinex: Rethinking low-light image enhancement with a generative diffusion model. <u>ICCV</u> , pp. 12268–12277, 2023.
638 639	Lvmin Zhang, Anyi Rao, and Maneesh Agrawala. Adding conditional control to text-to-image diffusion models. In <u>ICCV</u> , pp. 3836–3847, October 2023.
640 641 642	Richard Zhang, Phillip Isola, Alexei A Efros, Eli Shechtman, and Oliver Wang. The unreasonable effectiveness of deep features as a perceptual metric. In <u>CVPR</u> , 2018.
643 644 645	Chen Zhao, Chenyu Dong, and Weiling Cai. Learning a physical-aware diffusion model based on transformer for underwater image enhancement. <u>ArXiv</u> , abs/2403.01497, 2024.
646 647	Yuanzhi Zhu, K. Zhang, Jingyun Liang, Jiezhang Cao, Bihan Wen, Radu Timofte, and Luc Van Gool. Denoising diffusion models for plug-and-play image restoration. CVPRW, pp. 1219–1229, 2023

Denoising diffusion models for plug-and-play image restoration. <u>CVPRW</u>, pp. 1219–1229, 2023.

648 A RELATED WORK

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Low Light Image Enhancement.

low-light image enhancement Lore et al. (2017) is a critical task, influencing both human visual
perception and the related computer vision applications such as depth estimation Wang et al. (2021),
object detection Hashmi et al. (2023), semantic segmentation Pan et al. (2024).

To our knowledge, LLNetLore et al. (2017) is a pioneer, taking the lead in introducing deep neural 656 networks into the field of low-light image enhancement, achieving remarkable results through 657 supervised learning. Subsequently, LightenNetCai et al. (2018) used a convolutional neural network 658 (CNN) to attempt contrast enhancement for a single image. MBLLENLv et al. (2018) further 659 innovates and introduces a multi-branch fusion strategy within the CNN architecture to capture 660 and fuse richer image features. In addition, a series of SOTA methods such as SNR-Net Xu et al. 661 (2022), Retinexformer Cai et al. (2023), DiffLL Jiang et al. (2023), and MambaLLIE Weng et al. 662 (2024), have attracted considerable attention due to their impressive performance on various low-light enhancement benchmark datasets (e.g., MIT Bychkovsky et al. (2011), LOL Wei et al. (2018), LSRW 664 Hai et al. (2023)). However, despite leveraging advanced network designs incorporating Retinex 665 theory Land & McCann (1971), Transformers Vaswani et al. (2017), state-space models Gu & Dao (2024), and diffusion models Ho et al. (2020), these supervised methods exhibit limited generalization 666 to unseen scenarios. This is likely due to the comparatively small training datasets, which fail to 667 capture diverse illumination conditions and device degradations. Hence, reducing the reliance on 668 paired image collections for low-light enhancement remains a significant challenge, particularly in 669 mobile environments. 670

671 To address this, recent unsupervised approaches have focused on leveraging unpaired datasets or even single low/normal light images datasets for training, thereby reducing the dependency on paired 672 images. Prior state-of-the-art methods, ZeroDCEGuo et al. (2020), RUASLiu et al. (2020) and their 673 subsequent studies such as Ma et al. (2022), Fu et al. (2023), Wang et al. (2024), etc., use physical 674 lighting priors as guidance to achieve image enhancement without external supervision. Currently, 675 diffusion-based unsupervised models Wang et al. (2024); Jiang et al. (2024a) have attracted significant 676 attention for their powerful generative capabilities. QuadPrior Wang et al. (2024) introduces an 677 illumination-invariant prior as a conditional generative model using the ControlNet-shape framework, 678 where the entire architecture is trained on COCO dataset Lin et al. (2014). LightenDiffusion employs 679 a diffusion-based model, utilizing unpaired images by decomposing them into reflectance and 680 illumination maps, which serve as latent space inputs for low-light enhancement.

681 **Diffusion Model.** In recent years, diffusion models have been widely used in image generation 682 tasks. At the same time, significant progress has been achieved in low-level vision tasks. RePaint 683 Lugmayr et al. (2022) utilize pre-trained DDPM as a generative prior to generate high-quality, diverse 684 inpainted images without the need for mask-specific training. For low-level vision task, SR3 Saharia 685 et al. (2021) adopted a conditional image generation method based on a noise diffusion probability 686 model to achieve image super-resolution through iterative refinement, LPDM Panagiotou & Bosman 687 (2023) introduced the Low-light Post-processing Diffusion Model (LPDM) to model the conditional distribution between low-light images and normal exposure images. DiffPIR Zhu et al. (2023) 688 combined the traditional interpolation image restoration method with a diffusion sampling framework, 689 aiming to exploit the diffusion model as a prior for a generative denoiser. DiffLL Jiang et al. (2023) 690 proposed a wavelet conditional diffusion model (WCDM) that combines the advantages of wavelet 691 transform and the generation capability of diffusion model to achieve high-quality image enhancement. 692 Diff-Retinex Yi et al. (2023) rethink the low-light image enhancement task by combining a physically 693 interpretable model and a generative diffusion model. LatentFD Mei et al. (2023) utilized a latent 694 feature-guided diffusion model to achieve efficient shadow removal. JoReS-Diff Wu et al. (2023) 695 improved the generation ability of the diffusion model by introducing Retinex theory as an additional 696 preprocessing condition. GASD Hou et al. (2023) proposed a global structure-aware diffusion 697 process for low-light image enhancement through global structure awareness and uncertainty-guided 698 regularization. PA-Diff Zhao et al. (2024) proposed a new UIE framework that aims to utilize physical knowledge to guide the diffusion process. MDMS Shang et al. (2024) enables the model to adaptively 699 learn the noise distribution and thus improve the quality of the generated image by introducing a 700 space-frequency domain fusion module and combining a multi-domain learning paradigm and a 701 multi-scale sampling strategy. CFWD Xue et al. (2024) proposed a wavelet diffusion model based on

CLIP and Fourier transform guidance, which uses multi-modal visual language information in the
 frequency domain space generated by multiple wavelet transforms to guide the enhancement process.

B SOLVING PSEUDO-INVERSE \mathbf{A}^{\dagger}

Consider an image \mathbf{x} of size $m \times n$. We can vectorize the image \mathbf{x} into a column vector $\vec{x} \in \mathbb{R}^{mn \times 1}$. Let $\mathbf{A} \in \mathbb{R}^{mn \times mn}$ be a degradation operator with a 1×1 global degradation operator ϖ . This matrix can be written as:

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Thus, the degradation operator A can be represented as $A = \varpi \cdot I_{mn}$.

The pseudo-inverse A^+ of a matrix A is defined as the matrix that satisfies the following conditions:

 $\mathbf{A} = \begin{pmatrix} \boldsymbol{\omega} & \boldsymbol{\upsilon} & \boldsymbol{\omega} & \boldsymbol{\upsilon} \\ \boldsymbol{0} & \boldsymbol{\varpi} & \cdots & \boldsymbol{0} \\ \vdots & \vdots & \ddots & \vdots \\ \boldsymbol{0} & \boldsymbol{0} & \cdots & \boldsymbol{\varpi} \end{pmatrix}_{mn \times mn}$

$$\mathbf{A}\mathbf{A}^{\dagger}\mathbf{A} = \mathbf{A} \tag{16}$$

(15)

722 Substituting back,723

$$\boldsymbol{\varpi} \cdot \mathbf{I}_{mn} \mathbf{A}^{\dagger} \boldsymbol{\varpi} \cdot \mathbf{I}_{mn} = \mathbf{A}.$$
 (17)

Thus, the generalized inverse \mathbf{A}^{\dagger} is

$$\mathbf{A}^{\dagger} = \frac{1}{\varpi^2} \mathbf{A} = \frac{1}{\varpi} \mathbf{I}_{mn} \tag{18}$$

C DETAILS OF UAV-LL DATASET

The UAV-LL dataset used in our experiments primarily consists of drone-view urban scenes, captured with a 4/3 CMOS Hasselblad camera in real-world settings during dusk and nighttime conditions.
 The UAV-LL dataset contains 300 pairs of drone-view data, including a large variety of scenes with various real noises, and different darkness levels.

To obtain authentic low-light images, we meticulously adjusted exposure, ISO, and other parameters to capture ground truth (GT) images in genuine low-light environments. This process often entails a trade-off between visibility and image noise. Some samples from our UAV-LL dataset are displayed in Figure 9.

742 D LIMITATIONS

Our approach remain many limitations that deserve further study:

⁷⁴⁵ 1) Our proposed global illumination operator, while simple and efficient, may struggle in high-contrast
 ⁷⁴⁶ scenes. One potential solution is to utilize null-space decomposition for content refinement.

2) Despite employing LCM, our method still faces challenges in directly handling high-resolution images, primarily due to the constraints of the pre-trained model and limited computational resources.

As shown in Figure 10, Zero-IG and ours full model are unable to obtain proper illumination, resulting
 in the overexposure results. In contrast, our method without Range-space content yields a better
 enhanced result.

- 753
- 754 E MORE VISUAL RESULTS
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Figure 10: Visual comparison of the unsupervised methods on high-contrast scenes.





