Interpreting character embeddings with perceptual representations: the case of shape, sound, and color

Anonymous ACL submission

Abstract

001 Character-level information is included in many NLP models, but evaluating the informa-002 tion encoded in character representations is an open issue. We leverage perceptual represen-005 tations in the form of shape, sound, and color embeddings to investigate their correlation to 007 textual representations in five languages. This cross-lingual analysis shows that textual character representations correlate strongly with sound representations for languages using an alphabetic script, while shape correlates with featural scripts. We further develop a set 012 of probing classifiers to intrinsically evaluate what phonological information is encoded 015 in character embeddings. Our results suggest that information on features such as voiceness are embedded in both LSTM and transformerbased representations.

1 Introduction

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On the one hand, writing is an essential form of human communication. Writing systems and orthographies differ across languages and impact our reading behavior. Psycholinguists have extensively studied the effect of orthographic depth, i.e., the transparency of grapheme-to-phoneme mappings, on reading acquisition as well as skilled reading (Seymour et al., 2003).

On the other hand, the wide range of crosslinguistic diversity is still a major challenge for natural language processing (NLP) and for the study of language more generally (Mielke et al., 2019; Gutierrez-Vasques and Mijangos, 2020), especially on sub-word levels (Gutierrez-Vasques et al., 2021). This increases the importance of cross-lingual analyses of character-level language models (LMs), because anglocentrism in linguistic research is not only prevalent in NLP, but also in (reading and) orthography research (Share, 2008).

Character-based language models have gained significant attention in recent years in languages with Latin scripts, since they contain meaningful information on various linguistic levels and enhance the robustness of models. Oh et al. (2021) suggest that character LMs provide a more human-like account of sentence processing, which assumes a larger role of morphology, phonotactics, and orthographic complexity than was previously thought. Moreover, including character and sub-character information in LMs for Asian scripts is a standard practice. Despite of this recent attention, work focusing on getting a deeper understanding of character representation is scarce (Kann and Monsalve-Mercado, 2021), in particular regarding the comparison between languages and different types of scripts.

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The goal of this work is to improve our understanding of learned character representations, for better interpretability of the models. Like other neural network based models, character-level LMs can be seen as black-box methods and reveal limited insights about the causes for their predictions (Gilpin et al., 2018). We investigate the information encoded in character embeddings by comparing them to perceptual representations. These representations emerge as an inherent byproduct of human language processing, from reading, writing and speaking. We create embeddings based on the shape of characters, the sound (phonological features derived from grapheme-to-phoneme mappings) and color (elicited in the form of graphemecolor mappings from synesthetes).

Contributions We train models to learn three types of character embeddings: a positive pointwise mutual information (PPMI) vectorization, a recurrent model, and a transformer model. As an intrinsic evaluation method, we analyze the correlations between the distances of textual character representations and the perceptual representations in the form of shape, sound, and color embeddings. Furthermore, to provide more interpretable evalua-

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tion methods for character embeddings, we propose a set of probing classifiers to predict phonological features. Crucially, we address the cross-linguistic challenges that arise with character-level modeling by taking into account languages of varying scripts and orthographic depths. We argue that characterlevel black-box models can only be understood through cross-linguistic approaches and not on individual languages. We perform analyses of five languages: Dutch, English, Japanese, Korean, and Spanish. We discuss the compelling patterns of significant correlations and show the effectiveness of the probing classifiers even in a zero-shot scenario. The implementation and character representations are available online¹.

2 Related Work

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Character-level information in LMs. Including character-level information in LMs of languages with Latin scripts has become a common practice in NLP in recent years. This has been the case for different tasks, such as language modeling (Kim et al., 2016; Al-Rfou et al., 2019), part-of-speech tagging (Ling et al., 2015), morphological inflection (Faruqui et al., 2016; Kann and Schütze, 2016; Kann et al., 2020), named entity recognition (Lample et al., 2016), machine translation (Sennrich et al., 2016; Ngo et al., 2019), etc. Character-level information can enhance the models by providing background knowledge in the form of the underlying structures of words in a language (Adouane et al., 2018). Ma et al. (2020) showed how combining character- and word-level information in pre-trained LMs improves not only the performance but also the robustness of the model.

For certain languages, it is standard practice to include sub-token information in LMs, which happens naturally due to the compositional structure of their orthographies. This is the case for East Asian languages such as Korean and Japanese (e.g., Misawa et al. 2017; Chen et al. 2015). Korean LMs are often trained on *Jamos* (i.e., letters, as opposed to syllables), the smallest unit of the Korean script (Ahn et al., 2017; Park et al., 2018). This reduces the vocabulary size and injects syntactic and semantic information to the model that is difficult to access with conventional characteror token-level units (Stratos, 2017). Recently, Lee et al. (2020b) showed that a Korean BERT model using sub-character information requires less training data than previous models. Similarly, Japanese LMs also benefit from sub-character information (Nguyen et al., 2017).

Evaluating character embeddings. Characterbased language models are most often evaluated on downstream NLP tasks or on next character or word prediction (e.g., Takase et al. 2019; Tay et al. 2021; Clark et al. 2021). Additionally, they can be evaluated on word-level intrinsic evaluation tasks such as word analogy or similarity (e.g., Li et al. 2015). While work on intrisic evaluation of character embeddings is scarce (Kann and Monsalve-Mercado, 2021), the evaluation of neural representation trained on phonemes have received more attention, focusing on what phonological knowledge is embedded within (Silfverberg et al., 2018; Kolachina and Magyar, 2019; Mayer and Nelson, 2020; Mayer, 2020; Silfverberg et al., 2021). In Mayer (2020); Mayer and Nelson (2020) they use characters as a an approximation of phonemes in the case of Samoa and Finnish, respectively, as graphemes are closely connected to phonemes in these orthographies. However, this is far from the general trend.

Impact of different orthographies on linguistics and human language learning. Orthographic depth, i.e., the transparency of grapheme-phoneme correspondences in written alphabetic language (Frost et al., 1987; Katz and Frost, 1992), is a well-studied factor influencing reading acquisition and skilled reading behavior (Seymour et al., 2003; Landerl et al., 2013; Richlan, 2020). For instance, English is considered to be a *deep orthography*, as there are often multiple different pronunciations for the same spelling patterns (e.g., <gh> in tough and *though*). This contrasts *shallow orthographies* with more reliable grapheme-phoneme correspondences, such as Spanish. The consistency and complexity with which print reflects speech is one of the prime factors of cross-linguistic differences in reading fluency (Ziegler et al., 2010; Schmalz et al., 2015). It is the starting point for any discussion that centers on reading development across languages (Papadopoulos et al., 2021). Since the orthography has such a high impact on human reading behavior, its effect should also be considered more carefully in the development of NLP models.

Impact of different orthographies on NLP mod-

els. While orthographic depth has been discussed at length in reading research and psychology, it has

¹Link omitted to preserve anonymity.

rarely been addressed in natural language process-180 ing. This partly due to the prevalent anglocentrism 181 and missing resources (Bender, 2018). Some research has gone into studying the differences between languages when it comes to train computational LMs (Mielke et al., 2019), showing the im-185 pact of the vocabulary size and sentence length, but 186 there is lack of NLP research analyzing or taking into account the varying orthographies across languages. Two notable exceptions are the recent meth-189 ods proposed by Marjou (2021) and Sproat and Gutkin (2021), who use neural networks to estimate 191 the transparency of orthographies and degree of lo-192 gography, respectively. Moreover, Gorman et al. 193 (2020) conducted a shared task on grapheme-to-194 phoneme prediction. Their results show an urgency for improving these systems and the pronunciation 196 dictionaries used to train them across languages 197 and scripts. 198

3 Character Representations

3.1 Character language models

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We use the Wiki40B multilingual dataset (Guo et al., 2020) to train the character models. For each of the five languages, English (en), Dutch (nl), Spanish (es), Korean (ko), and Japanese (ja), we extract training sets of 3 million characters. The first three languages all use variants of the Latin script, while Hangul (Korean) and Hiragana (one of several scripts used in Japanese) are syllabary scripts, in which most graphemes denote entire syllables. We preprocess Korean Hangul characters, decomposing them into constituent Jamos, each corresponding roughly to a single phoneme. For Japanese, we train the language model on Hiragana and Katakana characters, but remove Kanji symbols to reduce the vocabulary size. The correlation analyses are then only performed on Hiragana. Figure 1 shows 2-dimensional plots of the learned textual character representations.

219Count-based PPMI embeddings.We generate220vectorized character representations in a purely221count-based manner with a positive pointwise mu-222tual information (PPMI) weighting. While the im-223portance of positional information is less obvious224for modelling word semantics, it is crucial for mod-225elling the distribution of sounds. Following the ap-226proach by Mayer (2020), we let our PPMI weight-227ing diverge from traditional bag-of-words models228by distinguishing contexts by their relative position

to a target. Thus, embeddings will have independent values for the contexts AB_, _AB, and A_B, counting the number of times a target proceeds, precedes and mediates a string AB. Using bigram contexts, the resulting embeddings have a dimension of $3 \cdot c^2$, where *c* is the number of characters in a given language, and 3 indicating the number of possible relative positions. 229

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LSTM. We train a recurrent language model consisting of a unidirectional long-short term memory (LSTM) layer. It receives character sequences as input at each time step and is trained for next character prediction. The model is trained with an Adam optimizer (Kingma and Ba, 2015), an initial learning rate of 0.01, and a batch size of 128. We extract the hidden representations of 128 dimensions as character embeddings. See Appendix C for training specifications.

Transformer. Similarly, we also train a transformer character model on the same data (Vaswani et al., 2017). The input layer consists of character and positional embeddings, followed by a transformer block with 2 heads and a hidden layer size of 128. We follow the same training procedure as for the LSTM.

3.2 Perceptual representations

Sound. The first perceptual representation that we consider is *sound*. To retrieve this representation, we map characters to a phonological distinctive feature space. This method has previously been applied to phonemes as a means of generalisation compared to sparse representations (Rumelhart and McClelland, 1986; Mirea and Bicknell, 2019), and to evaluate the knowledge embedded representations learned from neural networks (Silfverberg et al., 2018; Kolachina and Magyar, 2019).

As sound and speech are only indirectly reflected in writing, we approximate sound representations of characters using grapheme-to-phoneme alignment: For all languages, we extract data from the WikiPron pronounciation dictionary (Lee et al., 2020a) and use the m2m-aligner (Jiampojamarn et al., 2007) to align graphemes with phonemes in an unsupervised manner. Having alignments from the WikiPron data, we chose the most frequent word-initial phoneme mapping to represent the sound of each character (resulting mappings are listed in the Appendix D). Having a phoneme mapped with to character, we are able to associate it with a set of phonological distinctive



Figure 1: tSNE cluster plots of the character distances from the three types of character language models for English and Korean (see Appendix Figure 6 for the plots for Dutch, Spanish and Japanese).



Figure 2: Example of letter-color associations from single subjects.

features, which we use to form our final sound representation: Using the $ipapy^2$ toolkit, we retrieve International Phonetic Alphabet (IPA) descriptions of the phoneme mappings from which we create a sparse vector that describes what phonological features (e.g., consonant manner of articulation, $\pm plosive$, or vowel height, $\pm front$) are active. For every language, this provides us with a sound embedding table, $S^{|V| \times |F|}$, where V is the set of characters and F is the set of distinctive features, and

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$$S_{i,j} = \begin{cases} 1 & \text{if } F_j \in \text{phonmap}(V_i). \\ 0 & \text{otherwise.} \end{cases}$$

Color. Inspired by Kann and Monsalve-Mercado (2021), we compute color character representations from synesthesia data. Grapheme-color synesthe-

sia is a neurological phenomenon in which viewing a grapheme elicits an automatic, involuntary, and consistent sensation of color (Eagleman et al., 2007). Color-to-letter associations in synesthesia allow to examine the relationships between visual, acoustic, and semantic aspects of language. Recent research in this area has found cross-linguistic similarities in synesthesia, suggesting that some influences on grapheme-color associations in synesthesia might be universal and highlighting the importance of multilingual analyses (Root et al., 2018). Figure 2 shows example grapheme-color associations from individual subjects for each of our studied languages. It emphasizes the preference for red color tones for the first letter of the alphabet irrespective of the language (Root et al., 2018).

We use the cross-linguistic synesthesia data collected by Root et al. 2018 (see Appendix B for the dataset statistics). In order to extract color representations we compute the Euclidean distances between the 3-dimensional CIELuv color coding scheme for all character combinations. We average the distances across all participants of the same language. The resulting vector representations reflect the finding of Root et al. (2018) that the first grapheme in any language is unusually distinct (see Figure 5 in Appendix).

Shape. Lastly, we also create simple character representations based on their shape. Previous works (Brang et al., 2011; Watson et al., 2012) have relied on relied on Gibson (1969) or Courrieu et al. (2004) to build shape-related embeddings

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²https://github.com/pettarin/ipapy



Figure 3: Pearson correlation between all representations types for all five languages and for the random baseline (bottom right). A * marks a significant correlation (p < 0.01).

from human similarity judgements. However, we create shape embeddings directly from their visual expressions. We create an image for each printed character as shown in Figure 7 in the appendix. For each script, all images have the same width and height (the largest width among all characters incremented with 10 pixels, and the same for the height, which results approximately in 35x45 pixels) and all characters are drawn at position $\{5, 5\}$. We use the font *Arial Unicode MS* with size 28. From these images, we create shape representations by reading the images as gray scale images from top to bottom and flattening the matrix into vectors.

4 Correlation Analysis

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In order to analyze the relation between the learned character representations and the three perceptual representations – sound, shape, and color – we first compute the pairwise distances between characters³. Figure 3 shows the Pearson correlations between the character distances of all embedding types. The figure also includes a baseline, where the correlation between random distances and the distances of the respective character representations is computed.

As expected, the textual character representations show high correlation amongst each other for all five languages. The correlations between the textual embeddings and the perceptual representations show that even though the first are purely trained on written language, they still learn to encode certain inherent characteristics of human language processing and production: 351

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As a general pattern, the textual character representations correlate strongly with sound representations, moderately with color representations, and not at all with the shape representations (with the exception of Korean, discussed below). Japanese character embeddings behave differently. For instance, the correlation with the sound representations is weaker than for the other languages, which might be due to the syllabic nature of the Japanese script. In the following, we discuss the results for each of the perceptual embedding types in detail.

Sound. The PPMI character embeddings show the highest correlation with sound representations, followed closely by transformer embeddings. This is notable in the three languages with Latin scripts (en, es, nl). To explain this finding, we speculate that the context and learning direction available to the LMs provide phonetic information. Both the PPMI and transformer embeddings learn from context and from positional information in both directions. However, the unidirectional LSTM learns from left-to-right only. Therefore, as an addition, we trained a bidirectional LSTM to show that the

³We use cosine distance for all textual, sound and shape representations; and Euclidean distance for color.

| | en | es | nl |
|-------------|------|------|------|
| LSTM | 0.24 | 0.37 | 0.23 |
| biLSTM | 0.37 | 0.37 | 0.30 |
| Transformer | 0.48 | 0.60 | 0.39 |
| PPMI | 0.49 | 0.57 | 0.41 |

Table 1: Correlations between sound representations and character embeddings.

| | syllables | Jamos |
|-------|-----------|-------|
| IPA | 0.10* | 0.56* |
| Color | _ | 0.06 |
| Shape | 0.30* | 0.40* |

Table 2: Pearson correlation coefficients for Korean character embeddings based on Hangul syllables vs. Jamos. As the synesthesia data only includes Jamos, we exclude the syllable correlation for color.

addition of right-to-left information improves the correlation to the sound representations. The results are shown in Table 1. Moreover, comparing the results across Latin script, we note that Spanish character embeddings from all models achieve higher correlations than Dutch and English. The shallow orthography of the Spanish language explains this finding. This is also the case for Korean.

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Color. Our findings on the correlation between English character embeddings and synesthesia data are in line with (Kann and Monsalve-Mercado, 2021), who find that LSTMs agree with human letter-color perceptions more than transformers on a dataset with more participants (0.08 for LSTM-LM and 0.0 for transformer-LM). Moreover, we reach the same conclusion for the other alphabetic languages, Dutch and Spanish, while for Korean and Japanese there is no clear pattern evident from the correlation coefficients. This might be due to the smaller number of synesthete participants in the dataset.

Shape. The character embeddings of non-401 402 featural Latin scripts show low (or even negative) correlation to the shape embedding. However, due 403 to their featural writing systems (Sampson, 1985; 404 Marjou, 2021), Japanese and especially Korean em-405 beddings correlate significantly with shape. The 406 fact that the Korean consonant graphemes were de-407 signed to resemble the place of articulation (Lee, 408 2021; Gale, 1912), can explain the high correla-409 tions between character and shape embeddings for 410 this language. 411

This is also shown in the positive correlation between sound and shape representations, which is absent for the other languages. To analyze this further, we compare our initial results with character representations computed based on *Jamos* (e.g., individual phonemes such as \neg), to character representations of full *Hangul* characters (e.g., syllables such as $\overline{\neg}$). Table 2 shows higher correlations for characters decomposed into Jamos. 415

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In this light, the result is unsurprising and can be interpreted as an effective proof-of-concept of using a correlation analysis between textual and perceptual representations. More genuine shape representations, for example learned by a convolutional neural network, could be applied to reveal more accurate correlation patterns for Latin scripts.

5 Probing Classifiers

Except for Japanese, the results show that the neural embeddings correlate the most with the perceptual sound representations. To get a closer look at what information that may be encoded in the dense embeddings, we design a probing task in which classifiers are trained to predict whether certain distinctive features are present given character embeddings as input.

5.1 Classifier Setup

For each distinctive feature, we train a binary Logistic Regression to predict whether the the feature is present (1), or not (0). The labels are given by the sound representations as explained in Section 3.2. As the number of samples is small (limited to the number of characters in a language), we do this in a leave-one-out manner, training a classifier for each character, while using the rest for training. For features that only concern consonants (e.g., *manner of articulation* and *voiceness*), we exclude vowels, and similarly, for features that only concern vowels (e.g., *vowel height* and *vowel rounding*), we exclude consonants in both test and training.

5.2 Zero-shot classifiers

For some features, choosing the most frequent label is a good strategy and will provide good results. To further challenge the knowledge learned by the embeddings and distinguish the classifiers from the strategy of choosing the most frequent baseline, we create a zero-shot setup in which the classifiers will have to be able to transfer knowledge between features in order to excel in the task. In particular, we test 1) if a classifier trained to predict whether a consonant is voiced is able to identify vowels and 2) if labial consonants are retrieved by a classifier

| | | global t | ype | consona | nt voiceness | vowel | roundness |
|---|---------------|-----------|-------|---------|--------------|---------|-----------|
| | Model | consonant | vowel | voiced | voiceless | rounded | unrounded |
| | LSTM | 0.84 | 0.22 | 0.67 | 0.17 | - | - |
| _ | Transformer | 0.90 | 0.60 | 0.86 | 0.71 | - | - |
| e | Random | 0.61 | 0.28 | 0.54 | 0.43 | - | - |
| | Most-frequent | 0.89 | 0.00 | 0.76 | 0.00 | - | - |
| | LSTM | 0.91 | 0.50 | 0.57 | 0.61 | 0.00 | 0.57 |
| s | Transformer | 0.98 | 0.89 | 0.72 | 0.63 | 0.00 | 0.33 |
| e | Random | 0.61 | 0.27 | 0.49 | 0.49 | 0.43 | 0.49 |
| | Most-frequent | 0.90 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| | LSTM | 1.00 | 1.00 | 0.00 | 0.88 | 0.00 | 0.83 |
| 0 | Transformer | 1.00 | 1.00 | 0.33 | 0.87 | 0.00 | 0.83 |
| X | Random | 0.59 | 0.35 | 0.29 | 0.60 | 0.35 | 0.56 |
| | Most-frequent | 0.84 | 0.00 | 0.00 | 0.88 | 0.00 | 0.83 |
| | LSTM | 0.91 | 0.50 | 0.62 | 0.15 | 0.00 | 0.33 |
| - | Transformer | 0.93 | 0.67 | 0.79 | 0.57 | 0.00 | 0.57 |
| | Random | 0.61 | 0.28 | 0.54 | 0.42 | 0.43 | 0.51 |
| | Most-frequent | 0.89 | 0.00 | 0.76 | 0.00 | 0.00 | 0.00 |

Table 3: F1 score for classifiers predicting distinctive features with character embeddings (LSTM, Transformer) as input. Two baselines are included: Random (predicting labels uniformly at random) and Most-frequent (always predicting the most frequent label). Since English only has one rounded vowel (the character 'o' mapped to IPA 'p'), the result for this classifier is not included. Results for predicting all distinctive features are found in Appendix E.

trained to predict vowel rounding. While the intuition behind 1) relates to the sonority sequencing principle, which states that the nucleus of a syllable (vowels in the majority of the cases) represents a sonority peak, the intuition behind 2) is more experimental, relying on a global feature such as 'rounding'.

5.3 Results and discussion

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The results for the probing classifiers are found in Table 3. Generally, both LSTM and transformer embeddings outperform both the most-frequent and random baselines, with the transformer beating the LSTM by a small margin. This should, however, be taken with a grain of salt considering the limited number of examples.

Considering the global features, *vowel* and *consonant*, classifiers are able to learn this distinction using both LSTM and transformer character embeddings. In particular, consonants are identified with high certainty. This is, however, the majority group (ref. the most frequent strategy). The F1 scores for vowel prediction are considerably lower. However, in this case they cannot be explained by neither a most-frequent strategy nor a random baseline, which indicates that knowledge about this distinction is present in the embeddings.

The findings for the voiced/voiceless consonant

| | | consonant voiceness:voiced |
|----------|---------------|---|
| | Model | \rightarrow global type: <i>vowel</i> |
| | LSTM | 1.00 |
| | Transformer | 1.00 |
| G | Random | 0.63 |
| | Most-frequent | 1.00 |
| | LSTM | 0.89 |
| s | Transformer | 0.89 |
| e | Random | 0.64 |
| | Most-frequent | 0.00 |
| | LSTM | 0.44 |
| 0 | Transformer | 0.00 |
| <u>∽</u> | Random | 0.65 |
| | Most-frequent | 0.00 |
| | LSTM | 1.00 |
| | Transformer | 1.00 |
| 1 | Random | 0.63 |
| | Most-frequent | 1.00 |

Table 4: F1 score for predicting vowels using a classifier trained to predict whether a consonant is voiced. Two baselines are included: Random (predicting labels uniformly at random) and Most-frequent (predicting the most-frequent label, w.r.t. the label distribution in the original task).

distinction are similar. But here the groups are more balanced, which provides the most-frequent strategy with less of an advantage and in turn the F1 scores are generally lower. For Korean, the scores are lower compared to the other languages. As the feature of consonant voiceness correlates with manner in Korean (with all plosives, affricates and frica-

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| Language | F1 | True positive | False positive | False negative |
|----------|-----|---------------|----------------|----------------|
| es | 0.3 | m v | trz | b p f w |
| nl | 0.5 | b f v w | kgdqzx | рm |
| ko | 0.4 | п | | |

Table 5: Results from the zero-shot task to predict 'rounded' consonants using LSTM embeddings. Using a classifier to predict the vowel roundness of consonants, the following consonants are retrieved. F1 score indicates the ability to identify consonants with a labial place of articulation.

tives being voiceless, and plosives being the majority class), the task captured by the classifier may
be distorted. The fact that the classifier may not
be able to pick up features of voiceness from the
Korean embeddings are reflected in the zero-shot
experiment.

The results for the first zero-shot experiment for predicting vowels using the classifier for identifying voiced consonants are found in Table 4. Here, the results for Korean are worse than the random baseline. While the results for English and Dutch can be explained by the most-frequent strategy, the result for Spanish indicates that features of voiceness or sonority are encoded in the embeddings, amplifying the initial results from the probing classifier experiment.

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513 Turning from consonant to vowel features, the inventory of vowels is considerably smaller, leav-514 ing a small number of training examples with few 515 positive examples. Thus, the F1 scores for the prob-516 ing classifiers are associated with great uncertainty. 517 Table 5 shows the results for the zero-shot task of 518 retrieving consonants with labial features from a 519 classifier trained to predict vowel roundness. While the classifier trained on transformer embeddings 521 does not yield any positive examples and is there-522 fore not included in the table, the classifier using 523 LSTM embeddings is able to retrieve labial conso-524 nants. While the classifiers from Dutch and Spanish 525 retrieve many false negatives as well, the classifier for Korean only retrieves true positives, but only 527 one of four.

529Overall, we believe that the results are promising530and a good indication on how character represen-531tations can capture features related to phonology.532This especially in light of the zero-shot task, that533indicates that classifiers are able to transfer knowl-534edge of sonority from embeddings of consonants535to unseen vowels.

6 Conclusion

In this work, we attempted to understand the information encoded in character-level representations. We obtained two main types of embeddings: text-based embeddings and perceptual embeddings. While the first type of representations (PPMI, LSTM and transformer) were trained from raw data, perceptual representations were obtained from different sources, such as pronunciation dictionaries, synesthesia data and shape visualizations. We have performed correlation studies between these types for five different languages. Besides, we defined and trained models to predict certain phonological distinctive features in order to interpret the embeddings. 536

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We found interesting patterns in the correlation analysis as a simple first approach for intrinsic character embedding evaluation. While clearly outperforming a random baseline in most cases, the strength of the correlations vary between scripts. For instance, the strong correlation between Korean character embeddings and shape representations provides positive evidence of the suitability of this approach. Further research is required to dissect the differences between character LMs: While the LSTM embeddings showed better correlation with color, the transformer embeddings were superior when compared to sound representations. The inclusion of additional languages and scripts will be helpful to identify more generalizable insights.

The phonological probing tasks show promising results, especially with respect to interpretability. In future work, we will focus on the development of more sophisticated probing tasks, for instance, using contextualized character embeddings or multitask networks with shared layers across tasks.

Finally, we stress the need for further intrinsic evaluation methods for character representations. The high impact of orthography on human language learning is an adamant argument to consider the cross-linguistic diversity of writing systems more carefully in the development of NLP models.

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A Preprocessing

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We download the Wiki40B dataset for each of the 909 five languages (English, Dutch, Japanese, Korean, 910 and Spanish) from TensorFlow Hub⁴. For English 911 and Dutch, we consider the 26 standard letters of 912 the alphabet, digits and punctuation marks. For 913 914 Spanish, we additionally add \tilde{n} and and remove diacritics from vowels. For Korean, we consider all 915 Hangul characters, digits and punctuation marks. 916 Since Hangul is a featural writing system (Samp-917 son, 1990), we split the Jamos (i.e., compound sym-918 bols) into syllables⁵. For Japanese, we consider all 919 Hiragana, Katakana, and Kanji characters for training the language model. However, for subsequent 921 analyses we focus only on Hiragana. For all lan-922 guages, we replace any other special characters 923 with the symbol \in . 924

B Datasets

B.1 Sound embeddings



Figure 4: Japanese sound embeddings.

B.2 Synesthesia Dataset

As described in the main paper, we use the synesthesia data collected by Root et al. 2018. The data is available upon request by the first author. Table 6 shows the number of characters and participants included for each language in the dataset.

In Figure 5 the characters are plotted by the distances between their corresponding colors. Based on this dataset, Root et al. 2018 showed how some influences on grapheme-color associations in synesthesia might be universal across languages. Their

| Language | # Chars | # Participants |
|----------|---------|----------------|
| English | 26 | 47 |
| Dutch | 26 | 110 |
| Japanese | 46 | 27 |
| Korean | 24 | 13 |
| Spanish | 26 | 32 |

Table 6: Synesthesia dataset details showing the number of characters included for each language and the number of synesthetes participating in the study.

results suggest that grapheme-color associations follow an ordinal explanation, meaning that the unusually-distrinct first grapheme of a synesthete's alphabet tends to be associated with the unsuluayy-distinct color red. In line with their findings, the clusters show the greatest distance between the associated colors of the first grapheme of the alphabets (i.e., "a" in English and Spanish and " \neg " in Korean).

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B.3 Shape Dataset

Please find in figure 7 some examples of character figures that were used to build shape representations. We besides include in figure 8 three dendrograms calculated from the shape representations. For Spanish, English, and Dutch we only calculated one dendrogram, as the only difference is that the Spanish alphabet contains the "ñ" letter. For Japanese, we show a random subset (50%) of the *Hiragana* alphabet, as it did not fit properly in our plots.

C Models

C.1 Training Procedure

For the LSTM, biLSTM and transformer models, the number of epochs is set to 100, but the models are trained with early stopping and training is ended after 3 epochs without improvement on the validation loss. The best model is saved and used to extract the character embeddings. For reproducibility purposes, we set a single random seed.

⁴https://www.tensorflow.org/datasets/ catalog/wiki40b

⁵https://pypi.org/project/jamotools/

D Grapheme-to-phoneme alignments

D.1 Dutch 968

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a:a, b:b, c:k, d:d, e:e, f:f, g:y, h:fi, i:, j:j, k:k, l:l, m:m, n:n, o:ɔ, p:p, r:r, s:s, t:t, u:œy, v:v, w:v, x:ks, z:z, q:k, y:j

D.2 English 972

a:æ, b:b, c:k, d:d, e:ɛ, f:f, g:, h:h, i:, j:ʤ, k:k, 973 l:l, m:m, n:n, o:d, p:p, q:k, r:i, s:s, t:t, u:a, v:v, 974 w:w, x:z, y:j, z:z 975

D.3 Korean 976

 $\lambda: s, o: j, \pi: t_c, h: \underline{a}, d: \underline{\lambda}, d: \underline{e}, \underline{-}: \underline{o}, \tau:$ $\mathbf{u}, _: \mathbf{u},]: \mathbf{i}, \neg: \mathbf{k}, \exists: \mathbf{k}, \sqsubseteq: \mathbf{n}, \sqsubset: \mathbf{t}, \exists: \mathbf$ 978 $\exists : r, \Box : m, \exists : p, \exists : p, \forall : \underline{s}, \forall : \underline{t}_{c}, \exists :$ 979 k^h , Ξ : t^h , Ξ : p^h , $\overline{\diamond}$: h, : n, : m, : , 980

D.4 Spanish

a:a, b:b, c:k, d:d, e:e, f:f, g:, h:x, i:i, j:x, k:k 982 , l:l , m:m , n:n , o:o , p:p , q:k , r:r , s:s , t:t , u:u , 983 v:b, w:w, x:s, y:μ, z:θ 984

Probing Task Ε



Figure 5: Dendrograms of the distances between colors assigned to each character for English, Korean and Spanish. The leaves are sorted so that the minimum distance between its direct descendants is plotted first.



Figure 6: tSNE cluster plots of the three types of character models for Spanish, Dutch and Japanese.



Figure 7: Example images from which we extract character shape representations from the Latin alphabets, the Korean *Hangul* alphabet and the Japanese *Hiragana* alphabet.

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| $\begin{bmatrix} 5 \\ Random \end{bmatrix}$ 0.00 0.00 0.00 0.42 0.41 0.42 |
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| 000 000 000 |
| LSTM 0.00 0.00 - 0.57 0.00 0.00 0.57 |
| Transformer 0.00 0.00 0.37 0.00 0.00 0.3 Transformer 0.00 0.00 - 0.32 0.00 0.00 0.2 |
| |
| 1 = Random = 0.41 = 0.42 = - 0.50 = 0.42 = 0.43 = 0.43 |
| $\begin{bmatrix} - & \text{kandom} & 0.41 & 0.42 & - & - & 0.50 & 0.42 & 0.43 & 0.4 \\ \text{Most-frequent} & 0.00 & 0.00 & - & - & 0.00$ |
| - Kandom 0.41 0.42 - - 0.50 0.42 0.43 0.4 Most-frequent 0.00 0.00 - - 0.00 0.00 0.00 LSTM 0.00 - 0.00 - 0.00 0.00 0.00 |
| - Kandom 0.41 0.42 - - 0.50 0.42 0.43 0.4 Most-frequent 0.00 0.00 - - 0.00 0.00 0.00 0.00 LSTM 0.00 - 0.00 - 0.00 0.00 0.00 0.00 |
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Figure 8: Dendrograms of the distances between shape representations for the Latin alphabet (including the Spanish ñ letter), Korean *Hangul* alphabet and a subset of the Japanese *Hiragana* alphabet.