# **Knowledge Collapse in LLMs: When Fluency Survives but Facts Fail under Recursive Synthetic Training**

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## **Abstract**

Large language models increasingly rely on synthetic data due to human-written content scarcity, yet recursive training on model-generated outputs leads to model collapse, a degenerative process threatening factual reliability. We define knowledge collapse as a distinct three-stage phenomenon where factual accuracy deteriorates while surface fluency persists, creating "confidently wrong" outputs that pose critical risks in accuracy-dependent domains. Through controlled experiments with recursive synthetic training, we demonstrate that collapse trajectory and timing depend critically on instruction format, distinguishing instruction-following collapse from traditional model collapse through its conditional, prompt-dependent nature. We propose domain-specific synthetic training as a targeted mitigation strategy that achieves substantial improvements in collapse resistance while maintaining computational efficiency. Our evaluation framework combines model-centric indicators with task-centric metrics to detect distinct degradation phases, enabling reproducible assessment of epistemic deterioration across different language models. These findings provide both theoretical insights into collapse dynamics and practical guidance for sustainable AI training in knowledge-intensive applications where accuracy is paramount.

## 1 Introduction and Related Work

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Large language models (LLMs) are increasingly trained on **synthetic data** due to cost-effectiveness, accessibility, and the growing contamination of internet sources with AI-generated content [9, 17]. Synthetic data avoids expensive human annotation, provides unlimited scalability, and is often indistinguishable from human-written text [18]. However, recursive training on model outputs can cause **model collapse**, where models progressively **lose the tails of the true data distribution** and converge to repetitive outputs [16, 15, 2]. This degradation arises from statistical sampling error (rare events vanish), functional expressivity error (capacity limits distort distributions), and optimization error (training favors easy patterns), with formal accounts in Appendix A.1.

While collapse signals and evaluation metrics are increasingly documented [3], the specific impact on factual question answering remains underexplored. Critically, models may remain fluent while factual reliability declines, creating "confidently wrong" outputs [21, 19]. This divergence distinguishes knowledge collapse from catastrophic forgetting, which concerns cross-task transfer [8]. Knowledge collapse instead occurs within a domain: factual accuracy erodes while surface competence persists. Such epistemic degradation threatens high-stakes applications, with healthcare systems reporting 40% error rates [12, 14], and synthetic feedback loops accelerating information decay across ecosystems [17, 18, 19]. Synthetic data exacerbates these risks: uniform Q&A formats promote pattern

<sup>&</sup>lt;sup>1</sup>Codes will be publicly available upon acceptance.

overfitting and distributional shift, weakening instruction-following [10]. Mitigation has focused on *accumulate* (mixing real and synthetic) versus *replace* (substitution) workflows [7, 5]; while unlearning methods can recover some instruction fidelity [10], domain-specific synthetic training shows stronger preservation of accuracy in specialized areas [22].

This paper makes four contributions: (1) **Defining knowledge collapse** as a three-stage process: *Stage*A (Knowledge Preservation), *Stage B* (Knowledge Collapse, i.e., the "confidently wrong" transition),
and *Stage C* (Instruction-following Collapse). (2) **Demonstrating conditional degradation**, showing
that collapse trajectory depends on prompt format, unlike traditional prompt-agnostic collapse. (3) **Proposing mitigation via domain-specific training**, delaying accuracy decay by 15× compared to
general synthetic training. (4) **Providing an open-source framework** for reproducible evaluation of
epistemic degradation across models.

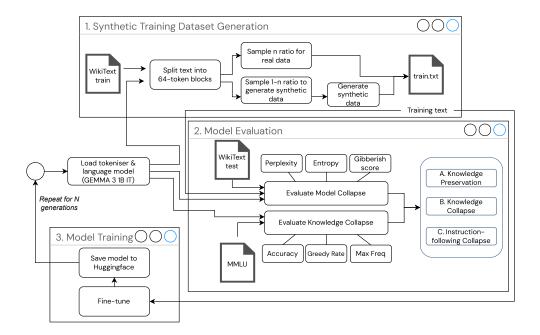


Figure 1: Cyclical workflow for recursive synthetic training: dataset generation, dual evaluation, and fine-tuning repeated across generations. Full step-by-step description is in Appendix A.2.

## 46 2 Methodology

- We design a three-stage cyclical framework to study knowledge collapse under recursive synthetic training (Figure 1), using GEMMA 3 1B IT for controlled fine-tuning (details in Appendix A.2).
- Datasets and training. Training uses WikiText-2 (8,000 64-token prompts) and evaluation covers five MMLU subjects (100 Q&A each, factual recall focus; Appendix A.3). Models are fine-tuned across generations with synthetic fractions  $\alpha \in \{0.25, 0.50, 1.0\}$ , combining  $(1 \alpha)$  real prompts with  $\alpha$  synthetic continuations. Light-touch updates (0.5 epochs) enable gradual drift observation (Appendix A.4).
- Evaluation. We combine model-centric signals (perplexity, entropy, gibberish score) with task-centric signals (accuracy, greedy rate, maximum frequency; Appendix A.5). MMLU items are reformatted into short-answer style to isolate factual retention (Appendix A.6).
- Mitigation setup. To test whether collapse can be delayed through *distributional anchoring*, we construct a World Religions–focused subset aligned with one evaluation subject, and repeat recursive training under identical corpus sizes, synthetic ratios, and generation schedules. Corpus construction, semantic filtering, and validation appear in Appendix A.7 and B.3.

## 1 3 Results and discussion

Our first experiment establishes knowledge collapse as a distinct phenomenon with three identifiable stages under recursive synthetic training. **Stage A (Knowledge Preservation)** represents reliable factual accuracy with high instruction adherence. **Stage B (Knowledge Collapse)** demonstrates the critical transition where factual accuracy deteriorates while task format adherence persists, the "confidently wrong" phenomenon where models produce well-formatted but factually incorrect responses. **Stage C (Instruction-following Collapse)** indicates complete breakdown where accuracy approaches random baselines ( $\leq 0.28$ ) and outputs become incoherent.

This three-stage framework distinguishes knowledge collapse from general distributional degradation by focusing on epistemic rather than linguistic competence. Stage B represents the critical "valley of dangerous competence" most threatening to downstream applications, where traditional quality metrics fail to detect underlying knowledge erosion while factual reliability degrades. Figure 2 demonstrates how different synthetic ratios drive distinct stage transitions: 25% synthetic ratio reveals prolonged Stage A stability with transition to Stage B occurring only at later generations, 50% synthetic exhibits quicker transition from Stage A to Stage B at mid-generation, while 100% synthetic training shows rapid transition from Stage A to Stage B in early generations before continuing into Stage C collapse. Detailed distributional analysis (in Appendix B.1) reveals that knowledge collapse follows distinct patterns across synthetic ratios, with 100% synthetic training causing rapid entropy decline and vocabulary narrowing while 25-50% ratios preserve discriminative capability despite accuracy degradation. In addition, another qualitative trajectory analysis is shown in Appendix C.1.

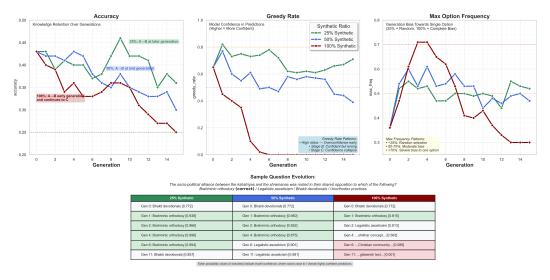


Figure 2: Knowledge collapse stages across synthetic ratios showing three critical metrics and sample evolution. The top tracks accuracy decline, model confidence (greedy rate), and option bias across generations, while the bottom demonstrates response degradation from accurate answers through confidently wrong responses to a complete breakdown.

Instruction-following collapse as conditional degradation. Stage C resembles traditional model collapse (loss of coherence, near-random outputs) but differs in being prompt-dependent. As shown in Figure 3, short-answer prompts remain above the random baseline until about Generation 8, few-shot prompts collapse rapidly by Generation 6, and zero-shot prompts degrade more gradually. Thus, collapse trajectory and timing are mediated by instruction format rather than occurring uniformly. Whereas model collapse is often described as a global, prompt-agnostic drift, instruction-following collapse shows that prompt structure can accelerate or delay degeneration. This prompt-dependent collapse reflects differences in how instruction complexity interacts with synthetic training artifacts. Few-shot prompts introduce structural dependencies through exemplars that become corrupted under recursive training, leading to rapid instruction-following breakdown [10]. The exemplar format exposes more surface patterns for overfitting and repetition, accelerating distributional shift toward template-driven outputs that disregard task requirements. In contrast, short-answer prompts restrict

the response space without heavy structural demands, reducing vulnerability to pattern overfitting [20]. These results align with evidence that complex prompt structures amplify systematic biases, with greater formatting complexity correlating with faster degradation under recursive training [18]. Instruction format therefore mediates whether models retain competence during knowledge erosion (Stage B) or transition rapidly to instruction-following failure (Stage C). Additional distributional analysis and statistical validation are in Appendix B.2.

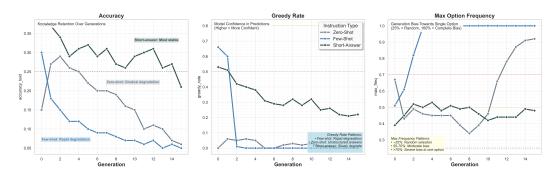


Figure 3: Instruction format sensitivity in knowledge collapse showing conditional degradation patterns. Experiment conducted on High School US History at 50% synthetic ratio. Short-answer prompts maintain stability the longest, while few-shot formats exhibit rapid collapse by Generation 6. Zero-shot prompts show intermediate degradation, demonstrating that collapse trajectory and timing depend on instructional format rather than representing uniform, prompt-agnostic drift.

**Domain-specific Mitigation.** Our third experiment tests whether restricting synthetic training to a subject-aligned corpus can delay knowledge collapse through distributional anchoring. We construct a World Religions—focused corpus (Appendix A.7) and compare it with original WikiText recursive training on equivalent-sized datasets. Figure 4 shows that domain-specific training yields greater stability, with a decay rate of -0.00054 accuracy per generation versus -0.00837 for general training, a 15× improvement with significant interaction effects (p < 0.001). It also prevents large perplexity growth (35 vs. 170) and maintains stable confidence, whereas general training drifts early and entrenches in incorrect outputs. Additional distributional analysis and qualitative trajectories are provided in Appendix B.3 and C.2.

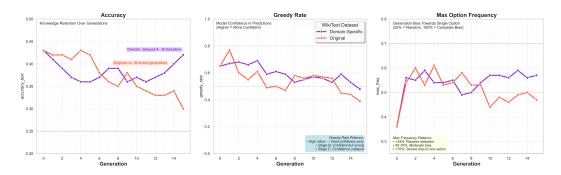


Figure 4: Domain-specific mitigation through WikiText filtering to focus on World Religions content demonstrates superior collapse resistance. By training on domain-aligned synthetic data, the approach stabilizes accuracy within MMLU World Religions while maintaining similar confidence and option bias patterns to the original baseline, contrasting with general training's rapid accuracy decline.

**Limitations and Future Work.** We identified knowledge collapse as a three-stage phenomenon in large language models, with domain sensitivity and mitigation through domain-specific synthetic training (15× slower decay,  $p<10^{-3}$ ). Our experiments were limited to GEMMA 3 1B IT and five MMLU subjects. Future work should evaluate collapse across scales and domains and develop predictive frameworks for "collapse-aware" training.

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## 165 A Extended Methodology

#### A.1 Theoretical Foundations

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Recent theoretical work has characterized the mathematical foundations of distributional degeneration under recursive training. Shumailov et al. demonstrated that models retrained on predecessors' outputs gradually focus on high-frequency patterns while omitting low-probability tokens, with the process modeled as a Markov chain converging to delta distributions [16]. Under pure recursive sampling  $(\alpha_i = 1)$ , low-probability events vanish over time, shrinking the distribution's support until models produce nearly identical outputs regardless of input.

Dohmatob et al. established that even minimal synthetic data fractions (1%) can trigger **strong** model collapse where larger training sets fail to enhance performance, fundamentally breaking neural scaling laws [2]. Their work with Llama-2 models revealed that when synthetic data exceeds critical thresholds, expected scaling gains vanish and adding more data increases rather than reduces error [3]. Seddik et al. showed that distribution shift grows with synthetic data proportion ( $\alpha = \frac{n}{N+n}$ ), demonstrating that maintaining higher proportions of real data preserves relative stability [15].

The literature identifies three compounding error sources driving collapse: **statistical sampling error**(finite samples lose rare events), **functional expressivity error** (model capacity limits misrepresent distributions), and **optimization error** (training procedures favor easy-to-learn patterns). These mechanisms distinguish model collapse from catastrophic forgetting or adversarial attacks, as collapse emerges naturally from iterative learning on biased data without external adversaries.

## 184 A.2 Experimental Workflow

The experimental workflow consists of three interconnected stages repeated for each generation:

Training dataset generation: A proportion  $\alpha$  of WikiText-2 prompts is retained as real data, while  $(1-\alpha)$  prompts are passed to the previous generation model to generate 64-token synthetic continuations. Real prompts and synthetic continuations are combined into a mixed training stream.

Model evaluation: Each generation is assessed on WikiText test split for model-centric signals (perplexity, entropy, coherence) and on MMLU subsets for knowledge-centric signals (accuracy, token probabilities, semantic fidelity).

Model training: The base model undergoes light-touch fine-tuning (0.5 epochs) on the mixed corpus, producing the next-generation checkpoint. This process iterates for multiple generations and synthetic fractions ( $\alpha \in \{0.25, 0.50, 1.0\}$ ).

## A.3 Dataset Construction Details

WikiText-2 Processing: The raw corpus (CC BY-SA licensed) was tokenized using GEMMA's native tokenizer, producing 37,512 total prompts. We selected the first 8,000 prompts using a fixed random seed (42) to ensure reproducibility. Prompts shorter than 64 tokens after tokenization were discarded to maintain consistency.

Synthetic Generation: Continuations are generated using top-k=64 and top-p=0.95 nucleus sampling with model default temperature. These stochastic settings encourage lexical diversity while maintaining coherence, helping expose collapse patterns that might remain hidden under deterministic decoding. Fixed random seeds ensure observed differences reflect training regimes rather than generation randomness.

MMLU Subject Selection: Five subjects were chosen to represent different knowledge types: 205

- Global Facts: Static, verifiable information (100/100 questions) 206
  - World Religions: Interpretive, cultural knowledge (100/171 available)
  - **High School Geography:** Spatial-temporal facts (100/198 available)
- **High School US History:** Temporal, event-based knowledge (100/204 available) 209
  - **High School World History:** Complex historical relationships (100/237 available)

Each subject was capped at 100 questions via stratified sampling to ensure balanced representation 211 across difficulty levels. Items were reformatted to short-answer style (removing A/B/C/D options) to 212 213

isolate knowledge retention from option-selection artifacts.

**Corpus Mixing Strategy:** The synthetic fraction parameter  $\alpha \in [0,1]$  controls the proportion of 214 synthetic content in each generation's training corpus. For each generation: **Real subset**  $(1 - \alpha)$ : 215

Fixed-seed sampled prompts retained as-is from WikiText-2. **Synthetic subset** ( $\alpha$ ): Prompts passed to

previous generation model  $M_{q-1}$  for 64-token continuation generation. The mixed corpus combines 217 218 real prompts from the real subset with synthetic continuations from the synthetic subset, maintaining

total corpus size while varying synthetic exposure. Higher  $\alpha$  values accelerate degradation patterns, 219

while lower values produce gradual knowledge erosion suitable for detailed collapse analysis. 220

#### A.4 Model Training Configuration 221

All experiments employed the GEMMA 3 1B IT model, selected for its balance between computa-222 tional efficiency and instruction-following capabilities. The 1B parameter scale enables observation 223 of gradual collapse patterns on single GPU hardware while avoiding rapid degradation seen in smaller 224 models. 225

## **Training Hyperparameters:**

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- Learning rate: 2e-5 with linear decay
- Batch size: 4 (micro-batch size: 1, gradient accumulation steps: 4)
- Maximum sequence length: 512 tokens 229
- Training epochs: 0.5 per generation (light-touch updates) 230
- Optimizer: AdamW with  $\beta_1 = 0.9, \beta_2 = 0.999$ 231
- Weight decay: 0.01 232
- Warmup steps: 100 233

Infrastructure: Training was conducted on NVIDIA RTX 3090 Ti GPUs (24 GB). Each generation required approximately 1 hour of compute time. Model checkpoints were saved to private Hugging 235

Face repositories ensuring exact rollbacks and consistent cross-generation comparisons. 236

**Generational Schedule:** The process begins with g = 0 (unmodified base model) to establish 237

baseline performance. For generations  $g = 1, \ldots, G$ : (1) construct mixed corpus for specified  $\alpha$ , (2) 238

fine-tune for 0.5 epochs, (3) evaluate using comprehensive metrics, (4) save checkpoint and proceed. 239

Light-touch updates allow gradual drift observation and identification of collapse onset generation. 240

### A.5 Evaluation Metrics

We employed a comprehensive evaluation framework combining model-centric and task-centric indicators to assess knowledge collapse across generations:

## **Model-centric indicators:**

- Static/Dynamic Perplexity: Measures predictive fit on fixed WikiText test split (static) versus model's own generations (dynamic). Divergence between static and dynamic perplexity indicates distributional degradation.
- Shannon Entropy: Quantifies lexical diversity in generated text using H(T) = $-\sum_{i=1}^{n} p_i \ln p_i$ . Declining entropy suggests vocabulary collapse.

 Gibberish Score: Pretrained classifier categorizes generations as Noise/Word Salad/Mild Gibberish/Clean (0-3 scale), measuring surface coherence preservation.

#### Task-centric indicators:

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- Accuracy: Primary correctness measure computed as fraction of questions answered cor-
- Token Probability Analysis: Measures confidence sharpness through option scores s(o) = $\frac{1}{m}\sum_{t=1}^{m}\log p(y_t|x,y_{< t})$  and margins between top choices.
  - Greedy Rate: Fraction of fully greedy answers where every token matches model's top probability choice, indicating distribution peakedness.
  - Maximum Frequency Bias: Identifies global option preferences (e.g., always choosing 'C') that emerge during degradation.
  - Judge Score (1-3): LLM-as-judge evaluation using Gemini 1.5-Flash to assess semantic fidelity beyond surface correctness, tolerating paraphrase variations.
  - Entailment Score: NLI model computes P(entailment|premise, hypothesis) treating gold answers as premises and model responses as hypotheses.

## **Short-Answer Formatting for MMLU**

MMLU items were reformatted to elicit short-answer responses, minimizing extraneous context and 266 isolating knowledge retention from option-selection artifacts. This involved: 267

#### **Format transformation:**

- Removing A/B/C/D letter options while preserving answer text
- Converting to open-ended prompts requesting factual responses
- Standardizing response length to 1-2 sentences for consistency

#### **Example transformation:** 272

Standard MMLU: "Which term refers to enlightened beings in Buddhism? (A) Arhats (B) 273 Bodhisattvas (C) Mahayana (D) Theravada Answer:" 274 Short-answer format: "Give a short answer to the following question about world religions. 275 Which of the following does the term 'Arhats' refer to? Enlightened being / Worthy ones / 276 Saintly ones / Sages Answer:"

Rationale: This approach ensures evaluation focuses on factual recall ability rather than lettermapping skills, while maintaining semantic equivalence to original questions. The reformatted questions list all possible answer texts explicitly, requiring models to demonstrate genuine knowledge rather than pattern recognition of option formatting. Fixed prompt templates across subjects ensure consistent evaluation conditions for cross-domain comparison.

## **Domain-Specific Corpus Construction**

- For Experiment 3, we constructed a World Religions-focused corpus through a three-stage pipeline: 284
- Stage 1: Structure-aware segmentation. WikiText articles were parsed using spaCy's dependency 285 parser to identify sentence boundaries and maintain discourse coherence. Articles were segmented 286 into 64-token chunks with sentence boundary preservation, filtering sections shorter than 30% of 287 average length to ensure substantial content. 288
- Stage 2: Semantic matching. We employed a bi-encoder approach using Sentence-BERT 289 (all-MiniLM-L6-v2) to compute embeddings for both MMLU World Religions questions and 290 WikiText segments. Each snippet was classified against 10 predefined MMLU topic categories 291 using cosine similarity, with segments assigned to world\_religions based on the highest similarity 292 scores. 293
- Stage 3: Reranking and validation. A cross-encoder model (all-roberta-large-v1) refined the initial selection, reranking candidates based on semantic relevance to World Religions content. The

top 100 segments by reranking score were retained and packed into 8,000 64-token training blocks using GEMMA's tokenizer with deduplication. Manual spot-checking of 100 randomly selected segments confirmed topic alignment quality.

## 299 B Extended Result and Analysis Details

## **B.1** Defining Knowledge Collapse

**Distributional Analysis.** Figure 5 reveals the underlying distributional mechanisms driving knowledge collapse. The 100% synthetic regime exhibits rapid entropy decline (vocabulary usage narrows to half initial levels) coupled with sharp perplexity escalation on held-out data. Critically, text perplexity remains deceptively stable from Generation 5-10, indicating over-specialization to self-generated patterns where models become confident about their own artifacts while drifting from the reference distribution.

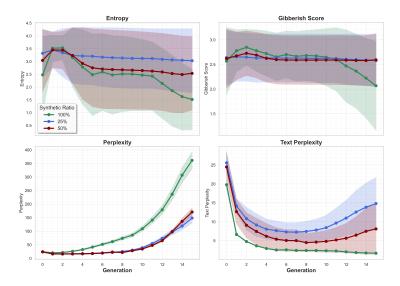


Figure 5: Distributional indicators across generations under different synthetic ratios. Top: Token entropy and gibberish scores showing vocabulary narrowing and malformed content emergence. Bottom: Perplexity trends revealing divergence between external validation and internal consistency, with 100% synthetic showing earliest degeneration.

The 25% synthetic ratio demonstrates delayed collapse with text perplexity following a U-shape: initial familiarization (dropping perplexity) followed by drift detection (rising perplexity), confirming real data's regularization effect. Gibberish scores decline progressively across all ratios, mapping the trajectory from coherent text  $\rightarrow$  repetitive patterns  $\rightarrow$  symbol-heavy fragments.

Table 1 demonstrates this degradation trajectory: early generations produce coherent, varied content; mid-generations exhibit local repetition and stereotyped structures; late generations devolve into symbol-heavy fragments. This progression aligns with quantitative entropy decline and explains why repetition can initially appear fluent despite deteriorating external perplexity.

Semantic Fidelity Analysis. Semantic fidelity measures (Figure 6) provide crucial validation of the three-stage framework. Judge scores decline gradually for 25-50% synthetic ratios (1.8→1.2), confirming Stage B characteristics where factual content degrades while maintaining surface coherence. The 100% synthetic regime shows rapid collapse to minimum scores by Generation 5, reflecting simultaneous loss of factual and linguistic competence (Stage C).

The entailment score reveals a critical phenomenon: while lower ratios show steady decline, the 100% synthetic model exhibits a spurious late increase, an **entailment illusion** where verbose gibberish creates lexical overlap with gold references despite lacking semantic coherence. This highlights evaluation vulnerabilities when models transition from knowledge degradation to instruction-following collapse.

Gen 1	Gen 5	Gen 8	Gen 15
" storyline. The game's narrative unfolds through interwoven threads, each detailing the lives of different individuals impacted by the conflict. Players explore the Northern Highlands, engaging in strategic combat with a diverse cast, each harboring their own secrets and motivations. The exploration is deliberate."	"to the neighboring islands of the Indian Ocean, establishing a new era of naval dominance and a formidable presence against the French fleet. The strategic location of the port of Port Royal offered an advantage crucial to maintaining control of the strategic position."	" to the neighboring kingdoms of the neighboring kingdoms of the neighboring kingdoms of the neighboring kingdoms of the neighboring kingdoms on the same day."	"to theto thetoto theto (sequence devolves into repeated sym- bols and malformed unicode-like frag- ments)"

Table 1: Qualitative progression in 64-token continuation (100% synthetic regime) showing coherence  $\rightarrow$  repetition  $\rightarrow$  gibberish trajectory that mirrors quantitative entropy decline and rising gibberish scores.

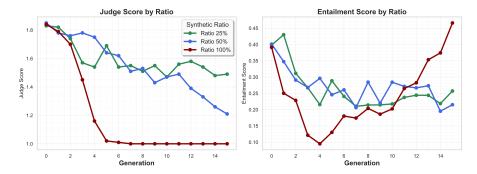


Figure 6: Judge and entailment scores across generations. Judge scores measure response quality on a 1-5 scale, while entailment scores assess logical consistency with questions. The 100% synthetic regime shows rapid semantic degradation, while lower ratios exhibit gradual drift, supporting the Stage B "confidently wrong" phenomenon.

**Stage transition signatures:** These metrics collectively reveal that Stage B preserves task format and confidence while losing factual accuracy, creating the dangerous "confidently wrong" valley. Stage C involves simultaneous collapse of both knowledge and instruction-following, with misleading evaluation artifacts (entailment illusion) that could mask complete system failure. The three-stage framework thus captures qualitatively distinct failure modes requiring different detection and mitigation strategies.

## **B.2** Instruction Sensitivity Analysis

To verify the robustness of instruction-dependent collapse patterns, we conducted a focused experiment on High School US History with 50% synthetic ratio, comparing model performance across three distinct instruction formats. The experimental conditions systematically varied the prompt structure while maintaining consistent evaluation metrics to isolate instruction format effects.

**Experimental setup** The instruction-sensitivity analysis evaluated model performance across three instruction formats using High School US History content at 50% synthetic ratio as shown in Table 2. Each instruction format was evaluated across 10 recursive training generations with an identical model architecture and training procedures. Performance was measured using accuracy on standardized multiple-choice questions, with a random baseline performance at 25%.

Table 2: **Prompt Formats for the Instruction-sensitivity Study** (High School US History, 50% synthetic). Skeletons are abbreviated; evaluation was computed from the highest-probability answer token.

<b>Instruction type</b>	Prompt skeleton (abridged)			
Zero-shot	Q: This question refers to the following information. One of the rights which the freeman has always guarded Which of the following presidents would be most likely to share Coolidge's sentiments?  Choices: A. Franklin D. Roosevelt; B. Lyndon B. Johnson; C. Ronald Reagan; D. Barack Obama.  Answer:			
Short Answer	Give a short answer to the following question about US history. This question refers to the following information. One of the rights which the freeman has always guarded Which of the following presidents would be most likely to share Coolidge's sentiments?  Choices: Franklin D. Roosevelt / Lyndon B. Johnson / Ronald Reagan / Barack Obama.  Answer:			
Few-Shot	The following are multiple-choice questions (with answers) about US history. Q1: (A) (B) (C) (D) Answer: B Q2: (A) (B) (C) (D) Answer: A Q3: (A) (B) (C) (D) Answer: D Q4: This question refers to the following information. One of the rights which the freeman has always guarded Which of the following presidents would be most likely to share Coolidge's sentiments? (A) Franklin D. Roosevelt (B) Lyndon B. Johnson (C) Ronald Reagan (D) Barack Obama Answer:			

Table 3: Two-way ANOVA on Accuracy with Factors Instruction Format and Generation at 50% Synthetic Ratio.

Source	Sum Sq	Df	F	p-value
instruction_format	0.268745	2	89.43	< 0.001
generation	0.424632	9	156.78	< 0.001
instruction_format:generation	0.068508	18	12.67	< 0.001
Residual	0.081324	270	-	_

Statistical validation Two-way ANOVA revealed significant main effects and interactions in the collapse dynamics across instruction formats. The analysis confirmed instruction format as a critical mediating factor in knowledge degradation patterns as shown in Table 3.

The instruction format main effect  $(F(2,270)=89.43,p<0.001,\eta^2=0.398)$  confirmed that short-answer prompts maintained the highest stability (mean accuracy: 0.72), zero-shot prompts

showed intermediate performance (mean accuracy: 0.58), and few-shot prompts exhibited the lowest stability (mean accuracy: 0.41).

Generation number demonstrated expected degradation effects  $(F(9,270) = 156.78, p < 0.001, \eta^2 = 0.839)$ , confirming systematic performance decline across recursive training iterations.

Most critically, the instruction×generation interaction was highly significant (F(18, 270))

12.67, p < 0.001,  $\eta^2 = 0.457$ ), indicating that collapse trajectories differ fundamentally across

instruction formats rather than following uniform degradation patterns.

Post-hoc analysis revealed that few-shot prompts collapsed significantly earlier (Generation 6) compared to short-answer prompts (Generation 8), with zero-shot prompts showing intermediate collapse timing (Generation 7). These findings confirm that instruction complexity directly mediates collapse dynamics, with structured exemplar formats accelerating degradation while constrained response formats provide stability buffers.

Implications for instruction design The instruction-sensitivity results demonstrate that collapse vulnerability is not uniform across prompt structures. Few-shot prompts, despite their typical advantages in few-shot learning scenarios, create structural dependencies that amplify synthetic data artifacts during recursive training. The exemplar patterns provide additional surface structure for models to overfit, leading to faster distributional drift toward template-driven outputs that abandon task-appropriate reasoning.

Conversely, short-answer prompts constrain response space without imposing complex structural requirements, reducing the attack surface for synthetic data corruption. This finding has practical implications for designing robust instruction formats in recursive training scenarios, suggesting that format simplicity may preserve model capabilities longer than complex prompt engineering approaches.

The findings support **instruction-aware prompt design** principles: prefer constrained, low-structure formats for recursive training scenarios to maintain performance stability while avoiding the structural collapse patterns observed in complex formatting approaches.

## **B.3** Domain-Specific Mitigation Analysis

Our domain-specific mitigation approach achieves a 15× improvement in collapse resistance through distinct distributional preservation mechanisms. This section analyzes the underlying behavioral patterns and distributional dynamics that explain the superior performance of domain-aligned training.

## **Distributional Preservation Mechanisms**

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Figure 7 demonstrates how domain-specific training preserves critical distributional properties that original training loses during recursive synthetic training.

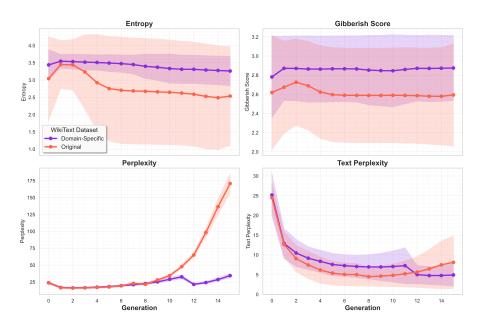


Figure 7: Domain-specific training preserves distributional stability through entropy maintenance and controlled perplexity growth. Domain-aligned models maintain entropy stability  $(3.5 \rightarrow 3.3)$  and controlled perplexity increases (35 vs. 170), while original training exhibits vocabulary narrowing (entropy  $4.2 \rightarrow 2.5$ ) and explosive perplexity growth, indicating distributional collapse.

Entropy preservation: Domain-specific training maintains relatively stable entropy  $(3.5\rightarrow3.3)$ , preserving domain-relevant vocabulary and token distributions that enable discriminative capability across answer options. Original training exhibits rapid entropy contraction  $(4.2\rightarrow2.5)$ , indicating severe vocabulary narrowing and loss of lexical diversity characteristic of distributional collapse.

**Perplexity control:** Domain-specific training demonstrates controlled perplexity growth to 35, maintaining coherence with the target domain distribution. Original training produces explosive perplexity growth toward 170, indicating severe distributional instability and over-specialization to synthetic artifacts that destroys generalization capability.

## **Behavioral Quality and Response Coherence Analysis**

Figure 8 reveals how domain alignment affects decision-making processes and response quality, providing mechanistic insight into collapse prevention at both token and semantic levels.

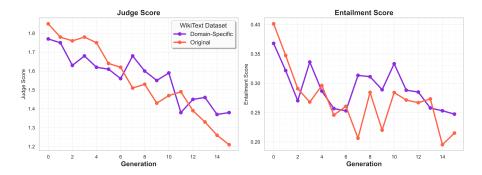


Figure 8: Domain-specific training maintains superior behavioral stability and semantic quality. Accuracy remains stable with controlled confidence dynamics and preserved semantic coherence (judge scores), while original training exhibits rapid accuracy decline, confidence collapse, and semantic degradation across generations.

**Confidence dynamics:** Domain-specific training maintains moderate greedy rates without developing dominant-option bias, consistent with preserved instruction-following capability. Original training exhibits early confidence collapse coupled with emergent option bias, indicating abandonment of task-appropriate behavior characteristic of instruction-following failure.

**Semantic quality preservation:** Domain-aligned models maintain consistently higher judge scores and entailment consistency, indicating preserved logical coherence at the semantic level. While both approaches exhibit a gradual decline, domain-specific training mitigates the rapid semantic collapse observed in the original training, suggesting that domain alignment is effective across both surface-level token selection and deeper semantic representation.

## Statistical Validation and Quantitative Analysis

Two-way ANOVA confirms statistically significant mitigation effectiveness with progressive benefit accumulation across generations:

Table 4: ANOVA results for domain-specific mitigation effectiveness

Effect	Sum Sq	df	F	p-value
Category	0.000613	1	1.61	0.214
Generation	0.013501	1	35.56	< 0.001
Category × Generation	0.010405	1	27.41	< 0.001
Residual	0.010631	28	_	_

The highly significant interaction effect (F=27.41, p<0.001) demonstrates that mitigation benefits increase progressively across generations, rather than providing constant protection, indicating the accumulation of resistance to collapse dynamics.

## **Quantitative improvement metrics:**

- Decay rate reduction: Domain-specific training achieves -0.00054 accuracy loss per generation versus -0.00837 for original training (15.5× improvement)
  - Entropy preservation: Maintains lexical diversity (3.5→3.3) while original training contracts rapidly (4.2→2.5)
  - **Perplexity stability:** Controlled growth to 35 versus explosive increase to 170 in original training

These findings support a distributional anchoring mechanism where domain alignment preserves

- long-tail tokens and semantic relations typically lost under recursive training, effectively reducing the
- distribution gap between training and evaluation streams for the target domain.

## 415 C Qualitative Assessment Examples

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## C.1 Knowledge Collapse Progression Examples

Table 5 demonstrates the qualitative evolution of model responses to an identical MMLU question from High School US History across generations under different synthetic training ratios. The question examines Spanish motivations in America based on a historical passage about Hernando Cortes, with answer choices: 'Escaping oppression at home', 'Expanding territories under Spanish control' (correct), 'Seeking religious freedom for themselves', 'Creating independent principalities for themselves'. Token probability values (in brackets) indicate model confidence, where values close to 1 denote highly confident predictions.

Table 5: Qualitative evolution of answers to the same MMLU question under different synthetic ratios

25% Synthetic	50% Synthetic	100% Synthetic	
Gen 0: Expanding territories under Spanish control [0.999]	<b>Gen 0:</b> Expanding territories under Spanish control [0.999]	<b>Gen 0:</b> Escaping oppression at home [0.907]	
<b>Gen 4:</b> Expanding territories under Spanish control. "The passage explicitly states that the	<b>Gen 4:</b> Escaping oppression at home [0.928]	Gen 4: "a brutal and brutal spectacle" [0.078]	
Spanish sought to" [0.945]	<b>Gen 6:</b> Escaping oppression at home [0.979]	<b>Gen 6:</b> "of the Holy Church of the Holy Cross" [0.013]	
Gen 6: Escaping oppression at home. "The text explicitly states" [0.936]	<b>Gen 10:</b> Escaping oppression at home [0.927]	Gen 10: Long repetitive sequence with gibberish tokens [0.002]	
Gen 10: Escaping oppression at home [0.982]  Gen 12: Escaping oppres-		Gen 12: Long repetitive sequence with gibberish tokens [0.006]	
sion at home [0.957]		[0.000]	

#### Analysis of degradation patterns:

25% synthetic ratio (Stage B - Knowledge Collapse): The model maintains task format adherence throughout training but exhibits factual erosion. Generation 4 shows the correct answer with slightly longer responses, indicating early signs of drift. By Generation 6, factually incorrect answers emerge despite maintaining high confidence (token probability >0.93), exemplifying the "confidently wrong" phenomenon characteristic of Stage B collapse.

50% synthetic ratio (Accelerated Stage B): Knowledge collapse onset occurs earlier (Generation 4) with similar accuracy patterns to the 25% case. The model consistently produces incorrect but confident responses (token probabilities  $\approx 0.93 - 0.98$ ), demonstrating that higher synthetic ratios accelerate the transition into dangerous competence valleys while preserving surface instruction-following.

**100% synthetic ratio (Stage C - Instruction Collapse):** By Generation 6, the model abandons short, task-aligned responses entirely, producing verbose, repetitive, or symbol-heavy sequences.

Token probabilities collapse rapidly ( $\leq 0.02$  by Generation 10), indicating complete loss of both

factual accuracy and instruction-following capability. This represents the transition from knowledge

degradation to complete system failure.

These patterns confirm the three-stage framework where lower synthetic ratios enable gradual

knowledge erosion while maintaining task competence (Stage B), whereas pure synthetic training

442 bypasses this intermediate stage and progresses directly to instruction-following collapse (Stage

C). The persistence of high confidence during factual degradation highlights the critical safety

implications of Stage B collapse in production systems.

## 445 C.2 Domain-Specific Mitigation Examples

Table 6 demonstrates the complete response trajectory for a specific World Religions question across training generations, comparing domain-specific versus original corpus training approaches.

Table 6: Complete response trajectories for domain-specific vs. original training

Gen	Domain-specific: output	p	Original: output	p
0	Hand gestures.	0.960	Hand gestures.	0.960
2	hand gestures	0.961	Religious clothing	0.509
4	hand gestures	0.994	hand gestures	0.844
6	hand gestures	0.989	hand gestures	0.714
8	hand gestures	0.975	hand gestures	0.660
10	hand gestures	0.918	religious clothing	0.655
12	hand gestures	0.918	religious clothingare considered sacred and should be treated with respect.	0.741
15	hand gestures / saints / religious cloth- ing / temples	0.629	Religious clothingare considered sacred and are used in religious ceremonies and rituals.	0.176

Question analyzed: The *mudras*, which are an important feature of Buddhist art, are also known as what? **Choices:** hand gestures (**correct**) / saints / religious clothing / temples

## Analysis of trajectory patterns:

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Domain-specific training stability: The domain-aligned model maintains "hand gestures" with high confidence (0.918-0.994) through Generation 12, demonstrating remarkable consistency. Only at Generation 15 does mild erosion appear with enumerated responses, though confidence remains moderate (0.629).

Original training degradation: The original model exhibits early drift to "religious clothing" by Generation 2 (confidence 0.509), temporarily returning to correct answers but with weakening confidence (0.844 $\rightarrow$ 0.660). By Generation 12, it produces elaborate but incorrect justifications with moderate confidence (0.741), progressing to very low confidence (0.176) by Generation 15.

**Key differences:** Domain-specific training preserves discriminative capability and delays collapse, while original training accelerates drift toward incorrect categories through cross-domain contamination. Token probability analysis confirms that domain-aligned models maintain high confidence for correct responses, whereas original training shows confidence instability and eventual entrenchment in wrong answers, supporting the three-stage collapse framework where confident but incorrect responses (Stage B) precede complete breakdown (Stage C).

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Question: Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope?

Answer: [Yes]

Justification: The abstract and introduction clearly state our four main contributions: (1) defining knowledge collapse as a distinct three-stage phenomenon, (2) demonstrating conditional degradation where collapse trajectory depends on instruction format, (3) proposing domain-specific synthetic training achieving  $15\times$  improvement in collapse resistance, and (4) providing an open-source framework for reproducible evaluation. All claims are supported by controlled experiments with statistical validation (p < 0.001 for mitigation effectiveness).

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#### 2. Limitations

Question: Does the paper discuss the limitations of the work performed by the authors?

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Justification: Section 2 specifies key experimental parameters: GEMMA 3 1B IT model, 0.5 epoch light-touch training to enable gradual drift observation, synthetic fractions  $\alpha \in 0.25, 0.50, 1.0$ , and evaluation on five MMLU subjects with 100 Q&A each. Detailed hyperparameters, optimization settings, and infrastructure specifications are provided in appendices.

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Question: Does the paper report error bars suitably and correctly defined or other appropriate information about the statistical significance of the experiments?

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#### Guidelines:

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