
A Spatio-Temporal Flow Matching Framework for Pedestrian Trajectory Prediction

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Abstract

1 Predicting pedestrian trajectories is essential for understanding human behavior
2 and optimizing spatial planning. A key characteristic of pedestrian trajectories
3 is their multimodality, which results from the diverse intentions of individuals.
4 While recent studies have employed various techniques, such as clustering, tree
5 enumeration, and Gaussian mixture models, to address this multimodality, a more
6 natural and efficient approach is to directly model the distribution of trajectories.
7 To address this need, we propose a spatio-temporal aware flow matching framework
8 for pedestrian trajectory prediction. This framework empowers flow matching-
9 based generative models by enabling them to analyze past trajectories of both the
10 subject and their neighbors so as to model the distribution of future trajectories.
11 Benchmarking results demonstrate the superiority of our proposed framework,
12 highlighting its ability to achieve more accurate and efficient trajectory predictions
13 compared to existing methods.

14 1 Introduction

15 Predicting pedestrian trajectories from observed paths is important for applications like spatial
16 planning and video surveillance [17, 6]. However, it remains challenging due to three factors: First,
17 complex spatial interactions – pedestrians interact with each other, such as friends walking together or
18 strangers maintaining distance [9]. Second, temporal coherence – future predictions must align with
19 past behaviors. Third, diverse intentions – individuals’ varied goals create many possible future paths.
20 These factors highlight the need for models that can address the inherent complexity of pedestrian
21 trajectory prediction.

22 Previous research has effectively addressed the first two challenges in pedestrian trajectory predic-
23 tion. First, models have focused on collective pedestrian behavior rather than individual behavior,
24 incorporating the interactions among different pedestrians [3]. Second, these models have accounted
25 for the temporal dimension, allowing them to use past trajectories within a time window to predict
26 future trajectories in a manner consistent with historical data [16, 18]. However, the third challenge,
27 which pertains to the multimodality of trajectory distributions, remains outstanding. Although various
28 solutions have been proposed, each has notable limitations. For instance, models based on Variational
29 Autoencoders (VAE) and Gaussian Mixture Models (GMM) [16, 2] impose strict constraints on
30 the trajectory distribution family, which reduces expressiveness and limits precision. Generative
31 Adversarial Networks (GANs) [3, 11] are typically difficult to train and are prone to mode collapse.
32 Search-based models [12] suffer from inefficiency, with prediction quality heavily dependent on the
33 resolution and exhaustiveness of the enumeration process. Recent approaches that cluster trajectories
34 into distinct modes and represent predictions as weighted averages of these modes [13] offer increased
35 efficiency but inevitably introduce discretization errors during both training and inference.

36 To effectively model the multimodal distribution of pedestrian trajectories, we propose TrajFM, a
 37 spatio-temporal-aware flow matching framework designed to predict arbitrarily shaped trajectory
 38 distributions. We evaluated TrajFM on two benchmark datasets for pedestrian trajectory prediction:
 39 ETH-UCY [4, 9] and SDD [10]. The evaluation results demonstrate that TrajFM outperforms
 40 current state-of-the-art models, thereby confirming the effectiveness of flow matching-based density
 41 estimation for trajectory prediction.

42 2 Method

43 2.1 Problem formulation

44 Pedestrian trajectory prediction aims to forecast future trajectories based on observed trajectories
 45 of pedestrians and their neighbors. In line with previous work, consider a traffic scene involving N
 46 pedestrians, where each pedestrian’s trajectory spans T time steps. The position of the i -th pedestrian
 47 at time step t is denoted by $\mathbf{x}_{i,t} = (x_{i,t}, y_{i,t}) \in \mathbb{R}^2$.

48 The entire scene is represented by a collection of N trajectories: $\{\mathbf{x}_{i,t}\}_{i=1,\dots,N;t=1,\dots,T}$. For
 49 convenience, this collection can be expressed as a 3-D tensor $\mathbf{X} = [\mathbf{x}_{i,t}]_{N,T} \in \mathbb{R}^{N \times T \times 2}$, where the
 50 first dimension represents pedestrians, the second dimension represents time steps, and the third
 51 dimension represents the 2D coordinates. Given the observed trajectories for the first T_{obs} time steps,
 52 denoted as $\mathbf{X}_{\text{obs}} = \{\mathbf{x}_{i,t}\}_{i=1,\dots,N;t=1,\dots,T_{\text{obs}}}$, the model is tasked with predicting the trajectories for
 53 the remaining $T - T_{\text{obs}}$ time steps, denoted as $\mathbf{X}_{\text{future}} = \{\mathbf{x}_{i,t}\}_{i=1,\dots,N;t=T_{\text{obs}}+1,\dots,T}$.

54 2.2 Spatio-temporal feature extraction network

55 The spatio-temporal feature extraction network is designed to encode the observed past trajectories.
 56 It consists of two key modules: (1) the temporal attention module, which applies self-attention along
 57 the time dimension for each pedestrian, and (2) the spatial attention module, which performs self-
 58 attention among pedestrians at each time step. The temporal attention module focuses on capturing
 59 the temporal dynamics of each pedestrian’s movement by considering the sequence of their past
 60 trajectories. Meanwhile, the spatial attention module addresses the interactions between pedestrians
 61 at each time step, enabling the model to account for social influences and spatial relationships.
 62 Together, these modules generate features that encapsulate both temporal and spatial contexts for
 63 each pedestrian, which are then utilized to predict the distribution of future trajectories.

64 The input to the network is a collection of observed pedestrian trajectories $\mathbf{X}_{\text{obs}} = [\mathbf{x}_{i,t}]_{N,T_{\text{obs}}} \in$
 65 $\mathbb{R}^{N,T_{\text{obs}},2}$. For each pedestrian i at each time step t , we first featurize the coordinate using a multi-layer
 66 perceptron (MLP) with 3 linear layers and the ReLU activation. To incorporate temporal information,
 67 we use the standard positional embedding layer [14] to encode the time step and add the positional
 68 embedding to the feature vector.

69 We combine multiple temporal attention modules and spatial attention modules in an alternating order
 70 to fully capture both temporal and inter-pedestrian spatial features. Finally, the feature vectors of the
 71 last observed time steps $\{\mathbf{h}_i = \mathbf{h}_{i,T_{\text{obs}}}\}_{i=1\dots N}$ are used by the subsequent future trajectory density
 72 estimator to predict the trajectory of each pedestrian.

73 2.3 Flow matching for future trajectory modeling

74 **Preliminary** Flow matching is a method for learning a probability flow ψ_t that transforms a source
 75 distribution $p_0(\mathbf{x})$ into a target distribution $p_1(\mathbf{x})$. The probability flow ψ_t is governed by an ordinary
 76 differential equation defined by a time-dependent vector field u_t : $\frac{d}{dt}\mathbf{x}_t = u_t(\mathbf{x}_t)$, where $\mathbf{x}_t = \psi_t(\mathbf{x}_0)$.
 77 To model the target distribution, a neural network $v_\theta(\mathbf{x}_t, t)$ can be employed to approximate the
 78 vector field u_t . However, the true vector field associated with the data distribution is intractable.
 79 To address this, the conditional flow matching framework [5] introduces a surrogate vector field
 80 that depends only on a specific prior sample \mathbf{x}_0 and a data sample \mathbf{x}_t : $u_t(\mathbf{x}_t|\mathbf{x}_0, \mathbf{x}_1) = \frac{d}{dt}\mathbf{x}_t$. This
 81 surrogate field can be viewed as an interpolation between \mathbf{x}_0 and \mathbf{x}_t . The corresponding loss function
 82 aims to train the vector field network to approximate this tractable surrogate vector field, and is
 83 defined as:

$$\mathcal{L}(\theta) = \mathbb{E}_{t,p_1(\mathbf{x}_1),p_0(\mathbf{x}_0)} \|v_\theta(\mathbf{x}_t, t) - u_t(\mathbf{x}_t|\mathbf{x}_1, \mathbf{x}_0)\|^2, \quad (1)$$

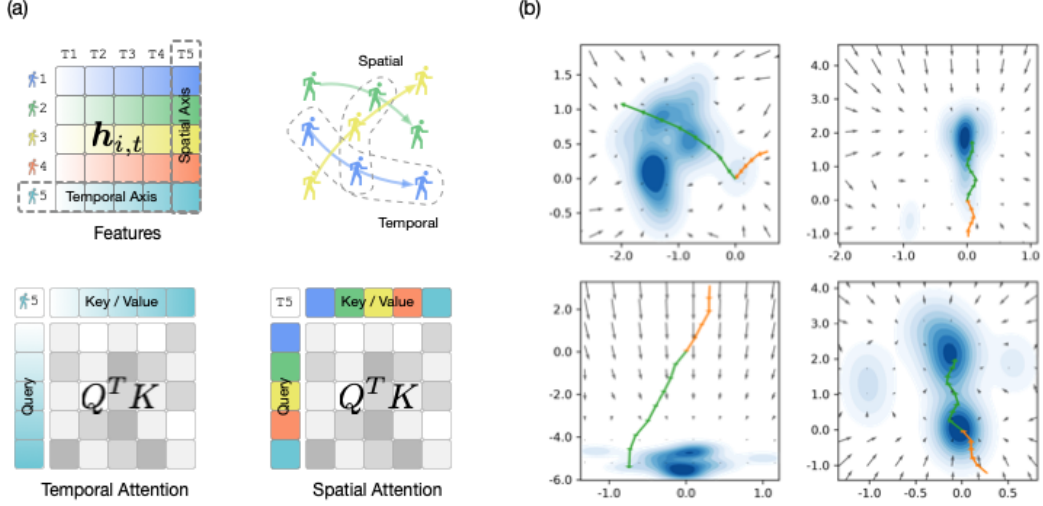


Figure 1: **(a)** Illustration of the spatial-temporal attention. **(b)** Distributions and associated vector fields of a pedestrian’s location at a future time point. Orange arrows indicate the pedestrian’s past trajectory and green arrows indicate the ground truth future trajectory.

84 where $t \sim \mathcal{U}(0, 1)$.

85 **Formulation** The future trajectory of the pedestrian i can be represented by a sequence of $T_{\text{future}} =$
 86 $T - T_{\text{obs}}$ coordinates: $[\mathbf{x}_{i,T_{\text{obs}}+1}, \dots, \mathbf{x}_{i,T}]$. We center the coordinates around the last observed
 87 coordinate so that future trajectories are represented in relative terms, denoted by the vector $\mathbf{s}_i =$
 88 $[\mathbf{x}_{i,T_{\text{obs}}+1} - \mathbf{x}_{i,T_{\text{obs}}}, \dots, \mathbf{x}_{i,T} - \mathbf{x}_{i,T_{\text{obs}}}] \in \mathbb{R}^{2 \times T_{\text{future}}}$. Formally, modeling the future trajectory distribution
 89 of pedestrian i is equivalent to modeling the following probability density:

$$p(\mathbf{s}_i | \mathbf{X}_{\text{obs}}), \quad i = 1 \dots N. \quad (2)$$

90 Since the feature extraction network has encoded the condition \mathbf{X}_{obs} into \mathbf{h}_i , the probability density
 91 function can be modified as:

$$p(\mathbf{s}_i | \mathbf{h}_i), \quad i = 1 \dots N. \quad (3)$$

92 To define a vector field for the distribution, we choose the isotropic Gaussian $\mathcal{N}(0, I)$ as the prior, and
 93 define the flow connecting a prior sample $\mathbf{s}_i^{(0)}$ and a data sample \mathbf{s}_i as linear interpolation. The linear
 94 interpolation favors a straight flow which contributes to the efficiency of both training and sampling as
 95 it is the shortest path between two points. Formally, the probability flow and its associated conditional
 96 vector field are defined as:

$$u_t(\mathbf{s}_i^{(t)} | \mathbf{s}_i^{(1)}, \mathbf{s}_i^{(0)}) = \mathbf{s}_i^{(1)} - \mathbf{s}_i^{(0)} = \frac{\mathbf{s}_i^{(1)} - \mathbf{s}_i^{(t)}}{1 - t}, \quad (4)$$

$$\psi_t(\mathbf{s}_i^{(0)} | \mathbf{s}_i^{(1)}) = t\mathbf{s}_i^{(1)} + (1 - t). \quad (5)$$

97 We use a simple three-layer MLP with ReLU activation to parameterize the vector field, which takes
 98 as input the current interpolant $\mathbf{s}_i^{(t)}$, the timestep t , and the embedding \mathbf{h}_i . The network is denoted by
 99 $v(\mathbf{s}_i^{(t)}, t, \mathbf{h}_i)$. The conditional flow matching objective for the i -th pedestrian is formulated as:

$$\mathcal{L}_i = \mathbb{E}_{p(\mathbf{s}_i^{(1)}), t, p(\mathbf{s}_i^{(0)} | \mathbf{h}_i)} \left\| v(\mathbf{s}_i^{(t)}, t, \mathbf{h}_i) - (\mathbf{s}_i^{(1)} - \mathbf{s}_i^{(0)}) \right\|^2, \quad (6)$$

100 and the final training loss is the average over all the observed pedestrians.

101 **Sampling** The sampling algorithm is outlined in Algorithm 1. First, the observed trajectories are
 102 encoded a single time using the transformer-based spatio-temporal network. An initial sample is then
 103 drawn from a prior Gaussian distribution. This sample is subsequently updated iteratively using the

Table 1: Benchmarking results on the ETH-UCY dataset using ADE and FDE scores. TrajFM outperforms the previous models in terms of average ADE and FDE scores. TrajFM also achieves the best scores in most cases.

Subset Metric	ETH		HOTEL		UNIV		ZARA1		ZARA2		Average	
	ADE	FDE	ADE	FDE	ADE	FDE	ADE	FDE	ADE	FDE	ADE	FDE
Social GAN [3]	0.87	1.62	0.67	1.37	0.76	1.52	0.35	0.68	0.42	0.84	0.61	1.21
SoPhie [11]	0.70	1.43	0.76	1.67	0.54	1.24	0.30	0.63	0.38	0.78	0.51	1.15
STAR [18]	0.36	0.64	0.17	0.36	0.31	0.62	0.29	0.52	0.22	0.46	0.26	0.53
SGCN [8]	0.63	1.03	0.32	0.55	0.37	0.70	0.29	0.53	0.25	0.45	0.37	0.65
CAGN [2]	0.41	0.65	0.13	0.23	0.32	0.54	0.21	0.38	0.16	0.33	0.25	0.43
SIT [12]	0.39	0.62	0.14	0.22	0.27	0.47	0.19	0.33	0.16	0.29	0.23	0.38
SocialVAE [16]	0.47	0.76	0.14	0.22	0.25	0.47	0.20	0.37	0.14	0.28	0.24	0.42
SocialVAE+FPC [16]	0.41	0.58	0.13	0.19	0.21	0.36	0.17	0.29	0.13	0.22	0.21	0.32
PECNet [7]	0.54	0.87	0.18	0.24	0.35	0.60	0.22	0.39	0.17	0.30	0.29	0.48
AgentFormer [19]	0.45	0.75	0.14	0.22	0.25	0.45	0.18	0.30	0.14	0.24	0.23	0.39
MemoNet [15]	0.40	0.61	0.11	0.17	0.24	0.43	0.18	0.32	0.14	0.24	0.21	0.35
TUTR [13]	0.40	0.61	0.11	0.18	0.23	0.42	0.18	0.34	0.13	0.25	0.21	0.36
TrajFM	0.39	0.57	0.10	0.13	0.21	0.32	0.15	0.24	0.17	0.22	0.20	0.30

104 Euler method, based on the predicted vector field. Given that the vector field network is a lightweight
 105 MLP and the feature extraction network is evaluated only once at the beginning, the iterative sampling
 106 process remains efficient. The sample obtained after the final iteration represents the generated future
 107 trajectory.

108 3 Experiments

109 **Dataset** Following the standard set by previous work[2, 13], we use the ETH-UCY[4, 9] dataset
 110 to benchmark the performance of TrajFM and the baselines. ETH-UCY contains 5 subsets: ETH,
 111 HOTEL, UNIV, ZARA1, and ZARA2. In total, the dataset contains 1,536 pedestrian trajectories. In
 112 accordance with previous work[16, 15], we train five models with each model using a different subset
 113 for testing and the rest subsets for training.

114 **Evaluation metrics** Models are evaluated using the Average Displacement Error (ADE) and the
 115 Final Displacement Error (FDE) [1]. ADE measures the similarity between the predicted trajectory
 116 and the ground-truth trajectory. FDE emphasizes the difference between the predicted end point and
 117 the ground truth.

118 **Result** TrajFM demonstrates state-of-the-art performance in both average ADE and average FDE,
 119 as shown in Table 1. It improves upon the best ADE of previous methods, reducing it from 0.21 to
 120 0.19, and decreases the FDE from 0.32 to 0.30. Specifically, TrajFM achieves the lowest FDE score
 121 across all five ETH-UCY subsets and the best ADE score on three out of five subsets. The ADE
 122 scores for TrajFM on the ETH and ZARA2 subsets are comparable to those of the leading baseline
 123 models.

124 Figure 2 in the appendix presents two examples of predicted trajectory distributions from the ETH-
 125 UCY dataset. Given the multi-dimensional nature of trajectory distributions, we employ two visual-
 126 ization techniques. First, we project the distributions onto a two-dimensional plane (shown in the first
 127 column of Figure 2). This projection displays the contour of the predicted trajectories, revealing that
 128 (1) TrajFM assigns high probability to the ground truth trajectory and (2) the branching shape of the
 129 distribution indicates the incorporation of multiple trajectory modes.

130 4 Conclusion

131 In this paper, we present TrajFM, a spatio-temporal flow matching framework specifically created for
 132 predicting pedestrian trajectories. TrajFM is a novel generative model for spatio-temporal data, and
 133 we have shown its effectiveness in capturing pedestrian movement patterns. This framework also
 134 holds potential for broader applications in general time series data generation.

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197 A Additional Figures

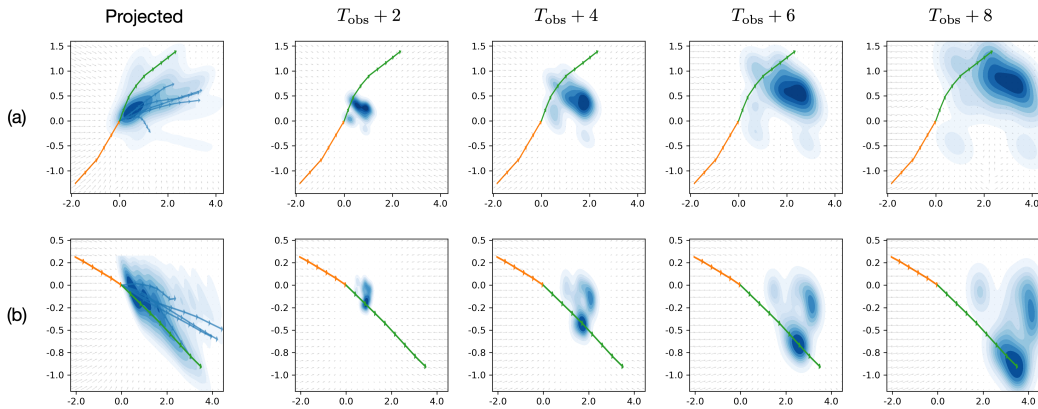


Figure 2: First column from the left: trajectory distributions and vector fields projected to the 2D plane. The rest of the columns: marginal distribution and its associated vector field of the trajectory at different time steps, interpreted as the distribution of the pedestrian coordinates at different time steps. Orange arrows indicate observed past trajectories, green arrows indicate ground truth future trajectories and blue arrows indicate predicted future trajectories.

Algorithm 1 Sampling Algorithm

Input: \mathbf{X}_{obs} observed trajectories

Input: n integration steps

- 1: Extract spatio-temporal feature for observed trajectories: $\{\mathbf{h}_i\} = \text{Featurize}(\mathbf{X}_{\text{obs}})$
 - 2: Sample from prior: $\mathbf{s}_i^{(0)} \sim \mathcal{N}(0, I)$
 - 3: **for** $t \leftarrow 1$ to n **do**
 - 4: **for** $i \leftarrow 1$ to N in parallel **do**
 - 5: $\mathbf{s}_i^{(\frac{t}{n})} \leftarrow \text{Euler}\left(v(\mathbf{s}_i^{(\frac{t-1}{n})}, \frac{t}{n}, \mathbf{h}_i), \mathbf{s}_i^{(\frac{t-1}{n})}, \frac{1}{n}\right)$
 - 6: **end for**
 - 7: **end for**
 - 8: **return** $\mathbf{s}_i^{(0)}$
-