Curriculum reinforcement learning for tokamak control

Abstract

 Tokamaks are the leading candidates to achieve nu- clear fusion as a sustainable source of energy, and plasma control plays a crucial role in their opera- tions. However, the complex behavior of plasma dynamics makes control of these devices challeng- ing through traditional methods. Recent works proved the usefulness of reinforcement learning as an efficient alternative, in order to fulfill these high-dimensional and non-linear situations. De- spite their performance, controlling relevant plasma configurations requires expensive and long training sessions on simulations. In this work, we leverage the use of a curriculum strategy to achieve signifi- cant speed-up in learning a controller for the con- trol coils, which tracks plasma quantities such as shape, position and current. To this end, we devel- oped a fast, asynchronous and reliable framework to enable interactions between a distributed actor- critic and a C++ code simulating the WEST toka- mak. By sequentially increasing task complexity, results show a clear reduction in convergence time and training cost. This work is one of the first at- tempts to enable fast production of robust magnetic controllers, for routine use in the operations of a magnetically confined fusion device.

1 Introduction

 Mastering nuclear fusion could significantly impact the world, unlocking the path towards sustainable and attrac- tive means of energy production. With no direct high-level byproducts of the reaction, it has many advantages over con- ventional energy sources [\[Ariola and Pironti, 2008\]](#page-7-0). To har- ness this potential alternative, tokamaks are promising de- vices to maintain the stability and performance of plasma's confinement, despite numerous physical and control chal-lenges [\[Meade, 2009\]](#page-8-0).

 Tokamaks are torus-shaped devices which aim at sustain- ing fusion reactions within a plasma under specific temper- ature and density conditions [\[Wesson, 2004\]](#page-8-1). They rely on magnetic fields generated by both *toroidal* and *poloidal* field coils (PFC) to shape it. Interactions occur at different levels with complex dynamics involved between the plasma and its surroundings. Control systems are then required to adjust the 42 voltages applied to the PFCs (Figure [2\)](#page-1-0), allowing control of 43 quantities intrinsically linked to plasma's evolution, like po- ⁴⁴ sition of the magnetic center m, *Last Closed Flux Surface* ⁴⁵ (LCFS), elongation κ and current I_p (Figure [1\)](#page-0-0). To study 46 the effects of various plasma configurations, scientists rely 47 on real-time linear controllers [\[Nouailletas and et al., 2023\]](#page-8-2), ⁴⁸ which require substantial engineering effort whenever target 49 scenarios undergo variations. Hence, there is a essential need 50 for flexibility, adaptability and robustness of magnetic control 51 systems through the entirety of the device lifetime, without 52 which no sustained plasma could be produced.

Figure 1: Control quantities of interest with toroidal (red) and poloidal (strided gold) sections.

Reinforcement Learning (RL) [\[Sutton and Barto, 2018\]](#page-8-3) ⁵⁴ emerged as an innovative approach to numerous real-time 55 control problems. Despite impressive results in a variety 56 of domains [Han *et al.*[, 2023;](#page-7-1) [Brohan and et al., 2023;](#page-7-2) ⁵⁷ [Kiran and et al., 2022\]](#page-7-3), it usually relies on either fast and 58 precise simulation enabling the collection of vast amount of 59 experiences, or on direct sampling from a physical device. 60 Both cases can not be fulfilled in our context: sampling of ex- 61 perimental data on the plant for the sole purpose of training is 62 impractical, and simulations remain expensive in order to ac- ⁶³

⁶⁴ count for the coupled behavior of plasma dynamics. Despite

⁶⁵ the existence of distributed architectures as powerful tools to ⁶⁶ compensate for these bottlenecks, training still remains long ⁶⁷ and costly as the number of parallel environments increases.

 In this work, we study the effects of a curriculum strategy on learning a magnetic controller through a distributed rein- forcement learning framework. By improving training speed and performance, we intend to accelerate the production of robust magnetic controllers for the operation of WEST, 73 a supraconductive tokamak located at CEA Cadarache^{[1](#page-1-1)} in Saint-Paul-lez-Durance, France [\[Bourdelle and et al., 2015;](#page-7-4) [Bucalossi and et al., 2022\]](#page-7-5). Indeed, such methodology could assist plasma researchers in quickly obtaining controllers, or adapt existing ones, for each new experimental campaign, hence improving flexibility and adaptability of RL-based magnetic control.

 Next sections will be organized as follows. First, we will give an overview of the related work regarding RL for toka- maks, and curriculum strategies in RL. We will then describe the curriculum methodology within plasma magnetic control, and the overall training framework. Finally, experiments are discussed through validation and analysis of the learned pol- icy. The latter will be compared to a baseline agent obtained without the strategies of interest. Finally, we will conclude on this study and its perspectives.

Figure 2: Cross-section with surrounding control coils, namely poloidal field coils.

89 2 Background

90 2.1 Reinforcement learning for tokamaks

⁹¹ A classical RL framework sets an agent which interacts ⁹² with an environment formalized as a *Markov Decision Pro-*⁹³ *cess (MDP)* denoted M. This MDP is defined by a state 94 space S, an action space A, its state transition distribution 95 $\hat{P}(s'|s,a): \mathcal{S} \times \mathcal{A} \times \mathcal{S} \rightarrow [0,1]$, an initial state distribution $\mathcal{P}^{\hat{0}}(s) : \mathcal{S} \to [0,1],$ and a reward signal $R(s,a) : \mathcal{S} \times \mathcal{A} \to \mathbb{R}.$ 97 Starting from state $s_0 \sim P^0(.)$, the agent must learn an 98 optimal policy $\pi^* : \mathcal{S} \times \mathcal{A} \to [0,1]$, which maximizes the discounted cumulative reward, or *return*, over the course of 99 an episode, i.e a trajectory over states and actions from the ¹⁰⁰ interactions with the environment: 101

$$
\pi^* = \underset{\pi_{\theta}}{\operatorname{argmax}} \mathbb{E}_{(s_0, a_0, \dots, s_t, a_t)}[\sum_{k=0}^{\infty} \gamma^k r_{t+k}] \tag{1}
$$

with discount factor $\gamma \in [0, 1]$ working as a penalization 102 term for long-term rewards, and $r_t = R(s, a) = \mathbb{E}[r_{t+1}|s_t = 100]$ $s, a_t = a$. Most importantly, the reward function is a scalar 104 feedback signal which indicates how well the agent performs 105 with respect to the overall objectives, hence the importance 106 of its design. The feedback loop between the agent and the ¹⁰⁷ environment ends once a terminal condition is reached, like 108 a situation that we want to avoid, or a threshold on simulated 109 time. As a side note, the policy can be deterministic, assign-
110 ing a probability of 1 to the same action for each observed 111 state. Moreover, it can be a parametrized function, like a neu- ¹¹² ral network. In such cases, it is usually denoted by π_{θ} , where 113 θ are the weights of the said model. 114

Fundamental definitions arise with the value function 115 $V_{\pi_{\theta}}(s) = \mathbb{E}_{\pi_{\theta}}\left[\sum_{k=0}^{\infty} \gamma^k r_{t+k} | s_t = s\right]$, and the action-value 116 function $Q_{\pi_{\theta}}(s, a) = \mathbb{E}_{\pi_{\theta}}[\sum_{k=0}^{\infty} \gamma^k r_{t+k}|s_t = s, a_t = a].$ 117 It is worth mentioning that relying on the first is difficult 118 in real-world applications such as fusion, since they do not 119 exhibit proper knowledge of the probability transition func-
120 tion P. Because of that, making actions explicit is an in- ¹²¹ teresting way of computing the expected return, as state- ¹²² action pairs can be easily sampled throughout learning. Over ¹²³ the past years, the use of neural networks (NN) as power- ¹²⁴ ful action-value and policy approximators lead to major ad-
125 vancements in continuous control problems. Deep RL algo-
126 rithms such as ones from the actor-critic family kept increas- ¹²⁷ ing in efficiency, leading to precise control in several high- ¹²⁸ [d](#page-7-6)imensional and non-linear control problems [\[Grondman](#page-7-6) *et* ¹²⁹ *al.*[, 2012\]](#page-7-6), both in on-policy [\[Schulman and et al., 2015;](#page-8-4) ¹³⁰ [Schulman and et al., 2017;](#page-8-5) [Mnih and et al., 2016\]](#page-8-6) and off-
131 policy settings [\[Haarnoja](#page-7-7) *et al.*, 2018; [Fujimoto](#page-7-8) *et al.*, 2018; ¹³² Lillicrap and et al., 2015 .

Consequently, deep reinforcement learning is becoming in- ¹³⁴ creasingly popular among the plasma control community. For ¹³⁵ [e](#page-7-9)xample, RL has been used for model-based control [\[Char](#page-7-9) ¹³⁶ [and et al., 2023\]](#page-7-9), for vertical stabilization [\[Dubbioso](#page-7-10) *et al.*, ¹³⁷ [2023;](#page-7-10) [De Tommasi](#page-7-11) *et al.*, 2022], to build feedforward tra- ¹³⁸ jectories of plasma parameters [\[Seo and et al., 2021\]](#page-8-8), for ¹³⁹ temperature and profile control [\[Wakatsuki and et al., 2019;](#page-8-9) ¹⁴⁰ [Wakatsuki](#page-8-10) *et al.*, 2021], or even for tearing instability control 141 and disruption avoidance [Seo *et al.*[, 2024\]](#page-8-11). Recent works ¹⁴² [\[Degrave and et al., 2022\]](#page-7-12) designed a RL-based system which 143 achieved magnetic control of the *Tokamak a Configuration `* ¹⁴⁴ *Variable* (TCV), in Lausanne, Switzerland. The learned con- ¹⁴⁵ troller demonstrates the capability for RL-based systems to ¹⁴⁶ tackle various complex plasma configurations while tracking 147 many quantities of interest at the same time. A similar proce-
148 dure was proposed by [\[Kerboua-Benlarbi](#page-7-13) *et al.*, 2024], with 149 the same limitations of the initial proposal, while refining the 150 simulation on which magnetic controllers were trained. 151

These examples highlight a shift of focus from classical 152 controllers, designed using prior knowledge on how control 153

¹ French Alternative Energies and Atomic Energy Commission

 should be performed with respect to physical properties of the dynamical system, to controllers learning by trial-and-error to act on the system based on what should be achieved in terms of final objectives. In summary, deep RL advantages over classical tokamak control stem from its ability to: ful- fil these high dimensional, uncertain and non-linear systems; explore possible strategies in order to make the control policy more flexible in contrast with the fixed heuristics of classical control; learn from raw magnetic signals using neural net- works, since plasma quantities can not be measured directly, and are instead usually inferred in real-time from reconstruc- tion codes [\[Faugeras, 2020;](#page-7-14) [Carpanese, 2021\]](#page-7-15) for use by clas-sical controllers.

¹⁶⁷ 2.2 Curriculum learning for reinforcement ¹⁶⁸ learning

 Curriculum learning (CL) [\[Bengio](#page-7-16) *et al.*, 2009] is a method- ology to optimize the order in which experiences are pro- cessed by an agent over the course of training. From the early stages of human development to adulthood, learning is structured and organized sequentially, so that the knowledge acquired over time facilitates the understanding of new no- tions or tasks that occur later to us. Therefore, a sequence of increasingly difficult tasks implicitly builds a curriculum, as knowledge is transferred from one intermediate objective to the other. Scheduling and designing such strategy helps in acquiring transferable skills to guide exploration during train- ing, with the premise of increasing performance and reduce convergence time towards a final set of tasks.

 Recent works classified the taxonomy of existing methods [\[Soviany](#page-8-12) *et al.*, 2022] as well a mathematical framework for curriculum learning in reinforcement learning domains using graphs [\[Narvekar](#page-8-13) *et al.*, 2020]. In most cases, we consider different MDPs between each task and three main concepts arise with which CL methods can be classified: the interme- diate task generation, the partial ordering on the obtained set of tasks and how knowledge could be shared between its ele- ments. Considering the importance of human intuition to de- fine simple tasks [\[Bengio](#page-7-16) *et al.*, 2009], domain experts could efficiently make a distinction between objectives that are nei- ther "too easy" or "too hard". Indeed, task generation and se- quencing of the latter could be handcrafted from human op- erators [\[MacAlpine and Stone, 2018;](#page-8-14) [Stanley](#page-8-15) *et al.*, 2005], but both concepts could be built up automatically as part of the curriculum learning procedure [\[Graves](#page-7-17) *et al.*, 2017; [Wu and Tian, 2017;](#page-8-16) [Ivanovic and et al., 2019\]](#page-7-18). Transfer learn- ing methods are required to share knowledge representation at each step of the curriculum, and concern several elements of the training loop, such as entire policies and value func- tions, rewards, etc [Zhu *et al.*[, 2023\]](#page-8-17). Care must be taken while choosing the right combinations of methods, to avoid negative transfer which could harm controllers performance [\[Wołczyk](#page-8-18) *et al.*, 2022].

²⁰⁶ 3 Approach

²⁰⁷ 3.1 Motivation

²⁰⁸ RL is still an emerging field within plasma magnetic con-²⁰⁹ trol, and few applications are observable. It can take several days of training for efficiency on relative simple plasma ²¹⁰ [s](#page-7-13)cenarios [\[Degrave and et al., 2022;](#page-7-12) [Kerboua-Benlarbi](#page-7-13) *et al.*, ²¹¹ [2024\]](#page-7-13). Nevertheless, the routine operation of a tokamak re- ²¹² quires flexibility over the design of controllers. Minimum ²¹³ engineering efforts should be targeted to adapt and fine-tune ²¹⁴ the controllers with respect to the objectives of each new ex- ²¹⁵ perimental campaign. 216

For this reason, this study aims at assessing the effects of 217 CL in the context of fusion, where poor reward signal and ²¹⁸ state representation at the beginning of learning, can desta- ²¹⁹ bilize the whole training process. We do not specifically intend to reach a new general performance threshold, but look ²²¹ for increased performance at start of each new task, special- ²²² izing exploration as training evolves towards its final goal. 223 Considering the cost of data sampling using WEST simula- ²²⁴ tions, yet in the real world, curriculum learning could be of ²²⁵ great help to stabilize the entire procedure, and reduce con- ²²⁶ vergence time by several orders of magnitude. Furthermore, ²²⁷ each new experimental campaign on WEST requires the def-

₂₂₈ inition of multiple control scenarios. The latter might have 229 shared plasma states, and overall control objectives. This 230 means that the same events can be used within different sce- ²³¹ narios, especially while choosing initial conditions or termi- ²³² nal ones. Since a scenario is a sequence of events, their or- ²³³ dering already defines a curriculum in an implicit manner, ²³⁴ as plasma equilibriums must follow each other in a realistic ²³⁵ and feasible way. Moreover, one could go further by explic- ²³⁶ itly building a curriculum on the reward function, considering ²³⁷ a sequence on its definition, i.e directly on the explicit con- ²³⁸ trol objective which might be similar between scenarios. A 239 simple reward on the shape for example could be used as a 240 starter, latter including the elongation, etc. Both ideas lead to ²⁴¹ the same conclusion regarding CL in fusion: 242

- curriculum generation and ordering could describe tasks 243 as events, or intermediate reward definitions; ²⁴⁴
- the two approaches shows that a curriculum working for 245 one plasma scenario, could be intuitively generalizable ²⁴⁶ with little effort on similar ones, enhancing production 247 of controllers for several cases during experimental cam- ²⁴⁸ paigns. 249

It is worth noticing that [\[Tracey](#page-8-19) *et al.*, 2023] addressed the ²⁵⁰ [i](#page-7-12)nitial drawbacks of the method described by [\[Degrave and](#page-7-12) ²⁵¹ [et al., 2022\]](#page-7-12), i.e. training speed and steady-state performance ²⁵² of the controller. Their approach resembles curriculum learn- ²⁵³ ing by borrowing its codes. Researchers partitions a target ²⁵⁴ scenario in smaller chunks, each related to one part of the 255 general task. Distributed environments are then divided into ²⁵⁶ subsests of different cardinalities, each linked to one of the 257 said chunks. Experiences are accumulated from MDPs that 258 differs implicitly in their underlying dynamics. Sampled ex- 259 periences are more diverse, and mix multiple levels of diffi- ²⁶⁰ culty inside the same training procedure. This procedure al- ²⁶¹ ready reduced training time by a factor of 4. However, despite 262 different initial state distributions, the overall task remain the 263 same between chunks, and no proper curriculum is defined, 264 i.e no knowledge transfer is present and task ordering is not ²⁶⁵ specifically mentioned. 266

²⁶⁷ 3.2 Curriculum definition

Formalism Let τ be a set of tasks with m_i : $(S, \mathcal{A}, P_i, R_i) \in \tau$, all sharing the same state and action 270 space. Moreover, we denote $\overline{\mathcal{D}}^{\tau}$, the set of all transitions 271 belonging to τ , so that $\mathcal{D}^{\tau} = \{(s, a, r, s') \mid \exists m_i \in \tau, s \in \mathcal{D}\}$ $S, a \in A, s' \sim P_i(.|s, a), r = R_i(s, a)$. A curriculum C can 273 then be defined as a direct acyclic graph $(V, \varepsilon, H, \tau)$, with V example vertices, ε edges, $H : \mathcal{V} \to \mathcal{P}(\mathcal{D}^{\tau})$, connecting $v \in \mathcal{V}$ to a 275 subset of samples of \mathcal{D}^{τ} . An edge $\langle v_j, v_k \rangle$ of $\mathcal C$ links two 276 tasks, using all samples associated by H to v_j before transfer- $\text{ring to } v_k$. For each $m_i \in \tau$, we have $\mathcal{D}_i^{\tau} = \{(s, a, r, s') \mid s \in$ $S_i = S, a \in A_i = A, s' ∼ P_i(.|s, a), r = R_i(s, a)$. We 279 need to associate all $v \in V$ with corresponding m_i and \mathcal{D}_i^{τ} , meaning that each path on the graph directly influences how $H: V \to \{D_i^{\tau} | m_i \in \tau\}$ filter knowledge transfer between tasks, with edges built on properties of the samples associ- ated with successive nodes. Indeed, tasks must be ordered 284 properly so that π_i^* is useful for acquiring good samples at each transition to the current vertex. In our case, a task is as- sociated with only one vertex, and each intermediate vertex sinks in only one node until the final one is reached, .i.e the final task [\[Narvekar](#page-8-13) *et al.*, 2020]. This defines an oriented sequence of tasks, similar to what was previously stated in terms of curriculum learning.

Figure 3: Schematic view of the scenario of interest. It starts from a limiter configuration, and ends up by stabilizing an elongated plasma in an x-point configuration.

 Tasks In this work, we consider only one of the two pos- sibilities mentioned earlier. Indeed, tasks are defined on the reward function, and only one scenario is considered for learning a controller. We focus on transitioning from a "cir- cular" shaped plasma in limiter configuration, to an elon-296 gated plasma in X-point configuration, i.e $\kappa > 1$ (Figure [3\)](#page-3-0). Elongated configurations have improved thermal confinement properties compared to limiter plasmas, at the cost of devel- oping growing vertical instabilities which make control more difficult. Once formed, the *Last Closed Flux Surface* (LCFS) defines the plasma boundary and the X-point appears at its intersection. The chosen curriculum is entirely conditioned 303 by a set of predefined rewards R_i . This means that while it could have been defined automatically, the uncertainty around tokamak dynamics makes the choice for a handcrafted se-quence of tasks quite straightforward for this first application. Prior control experience on the device informs on which tasks 307 could be considered easier than others. This work then relies 308 on human experts for both determining τ , as well as the re- 309 sulting sequence order based on V and ε . More precisely, the 310 curriculum has been built from physical intuition around sev- ³¹¹ eral key control challenges studied for all tokamaks (Figure 312) $4)$: 313

- 1. vertical stabilization of elongated plasmas while track- ³¹⁴ ing plasma current is a well-known control problem. ³¹⁵ Using classical feedback control, simple proportional- ³¹⁶ integral-derivative (PID) controllers [Ang *et al.*[, 2005\]](#page-7-19) ³¹⁷ can stabilize plasma's magnetic center (m_r, m_z) , as well 318 as plasma current I_p . Their relative simplicity are not far 319 from a basic RL-based solution, as a naive agent can be ³²⁰ summarized as proportional-integral control which re- 321 duces errors between measurements and targets. The ini- ³²² tial reward function then includes targets for the two el- ³²³ ements of interest. Hence, handling such classical prob- ³²⁴ lem is a good start in order to build strong foundations 325 for the next tasks; 326
- 2. tracking the entire plasma boundary becomes more chal- ³²⁷ lenging, as approaches from classical control often relies 328 on more advanced methods to synthesize efficient con- ³²⁹ trollers. Since the difficulty becomes more important, ³³⁰ we add the LCFS as well as the elongation to the initial ³³¹ targets. This creates a way to guide the agent towards an 332 elongated shape, properly positioning it before the final 333 task; 334
- 3. finally, once the plasma is set up towards its X-point ³³⁵ configuration, we modify the reward to include tar- ³³⁶ gets on the X-point itself (distance, magnetic flux, etc). ³³⁷ This could be considered as a fine-tuning exploration, ³³⁸ since the agent must have already positioned the plasma 339 boundary according to the final configuration. Never- ³⁴⁰ theless, we must proceed with caution, in order to avoid ³⁴¹ loosing accuracy on previous tasks through catastrophic 342 forgetting [\[Goodfellow](#page-7-20) *et al.*, 2015]. ³⁴³

Figure 4: Curriculum overview. We start from a simple vertical control stabilization problem with a free plasma current, to a complex one involving shape and X point.

Transfer learning We transfer the policy and the action- ³⁴⁴ value function between tasks, as both of them are neural net-

345 works. The parameters of Q_i learned during an interme- 346 diate task, serves as initialization for the parameters of the ³⁴⁷

348 next action-value function Q_i , without any freezing proce- [d](#page-8-18)ure which could negatively impact transfer [\[Wołczyk](#page-8-18) *et al.*, [2022\]](#page-8-18). Doing so bias the agent towards more efficient ex- ploration in the next domain. The policy's weights are also used to initialize the parameters of the new one, again with- out any freezing procedure. One could have incrementally frozen layers between tasks in order to keep previous repre- sentations learned by the controller. However, we empirically observed that it is not necessary for the curriculum learning to work well in practice. Furthermore, it limits the amount of tasks present in the curriculum, as the number of layers is bounded. We further use *potential-based advice* reward shap-360 ing (PBARS) so that $R'_j(\hat{s}, a) = R_i(s, a) + F(s, a) + R_j(s, a)$ з61 — with $F(s,a,s',a') = \check{Q}_i(s',a') - Q_i(s,a).$ R_i retains knowl- edge from the source task and F encourages exploration from 363 states that were valuable and overlap with the target j . They form the potential-based bonus with guarantees that it will not change the optimal policy [\[Harutyunyan](#page-7-21) *et al.*, 2015],.

 Transfer metrics While final performance on the target task will be analyzed, our main objective is to observe how CL could produce RL-based magnetic controllers faster, for routine use on WEST. Metrics must be chosen accordingly in order to measure by how much it speeds up training, com- pared to the vanilla method where the agent learn directly on the final task. We will refer to this question with two tools: the *jumpstart* and the *Time to threshold* (TTT). The former measures the initial performance increase at the beginning of each new task either for a unique task, or as a result of trans- fer; the latter checks how much faster the agent learns the policy which achieves a threshold on the episode return, with or without curriculum. Each intermediate task is caped to a maximum duration of 60 episodes, mostly to stay in line with empirical observations regarding MPO's warmup phase, i.e the phase during which NN do not undergo real variations.

382 4 Experiments

³⁸³ 4.1 Setup

 The NICE code The environment is based on the NICE C++ code [\[Faugeras, 2020\]](#page-7-14), which solves the *Grad- Shafranov* equation [\[Wesson, 2004\]](#page-8-1) for the plasma domain, with resistive diffusion [\[Heumann, 2021\]](#page-7-22) and transport equa- tion enabled. We use its forward evolution mode which com- putes the environment's state at each timestep. Moreover, power supply and diagnostic models are implemented in or- der to account for bias, delays and offsets of actuators. Over- all, it gives an accurate representation of the plasma, as well as the WEST control system. NICE is safely initialized to a limiter shaped plasma extracted from recent experimental data, and whose internal profiles are randomized to promote diversity among examples. The relative error of the Newton solver is increased to accelerate execution without significant loose of accuracy in its outputs. Termination is triggered if thresholds are reached on active coils currents or safety fac- tor (proportional to the geometry of the plasma and its cur- rent), to avoid any damage on the device. Episodes typically last for 500ms, as it appeared enough for generalization on longer shots.

State and Action spaces The environment's state is de- ⁴⁰⁴ fined as $s = \{y, I_a, m\}$ with y the plasma equilibrium information, I_a the currents in the active control coils, and 406 m the raw magnetic measurements. y typically contains 407 all quantities of interest described in the curriculum defini- ⁴⁰⁸ tion. It is usually difficult to observe the entirety of s in 409 real-time. To overcome this issue, the learned policy is re- ⁴¹⁰ stricted to a *Partially Observable MDP* (POMDP) where the 411 state space is limited to the observation space O . As such, 412 we have $o(s) = \{tr, m_b, fl, I_a, \frac{dm_b}{dt}\}\$, with tr target refer- 413 ences, $\{m_b, fl\}$ magnetic probes and flux loops raw mea- 414 surements, and $\frac{dm_b}{dt}$, temporal derivatives of magnetic probes 415 signals. Noise is injected in observations at each timestep 416 from Gaussian laws with parameters identified from WEST ⁴¹⁷ plasma discharges database, as well as delays to model real ⁴¹⁸ data acquisition from sensors. For actions, voltages are sam- ⁴¹⁹ pled from Gaussian distributions which parameters are the ⁴²⁰ outputs of the control policy, and then supplied to each of ⁴²¹ the 11 PFCs circumventing the device (Figure [1](#page-0-0) - Naming ⁴²² conventions stated in Figure [2\)](#page-1-0). After exploring possible out- ⁴²³ comes during training, only the mean of each distribution is ⁴²⁴ kept at inference to predict optimal actions. Offsets, bias and 425 delays are part of the power supply model within NICE to ⁴²⁶ ensure correct handling of WEST actuators in the real world. ⁴²⁷

| Component | Good | Bad | α | weight | | |
|---|-------|------|----------|--------|--|--|
| $LCFS$ [m] | 0.005 | 0.1 | | 3. | | |
| Magnetic center [m] | 0.002 | 0.03 | X | | | |
| κ | 0.005 | 0.03 | X | | | |
| I_p [kA] | 0.5 | 20 | X | 3. | | |
| X point distance [m] | 0.01 | 0.15 | X | 2. | | |
| Flux at current x point | O. | | X | 2. | | |
| Flux at target x point | O. | 0.08 | X | 2. | | |
| Flux gradient at target x point | O. | | X | | | |
| Final combiner: Smoothmax(α = -0.5) | | | | | | |

Table 1: Reward components description with dimensions. Scaling to [0, 1] range is performed, before combination to a final scalar value. Alpha is specified for each component if it has multiple targets. Flux setpoints are set to 1 since their measure is normalized , while flux gradient must tend towards zero.

Rewards Each reward R_i is a normalized weighted combination of error signals, extended with PBARS. Each com- 429 ponent c_i^j is computed as the difference E_j between its 430 target value and the one retrieved from the environment, ⁴³¹ then scaled to [0, 1] with $Softplus(E_i) := min(max(2 - 432))$ $\sigma(-\xi(\frac{E_j-good}{bad-good})), 0), 1)$. They are then combined into a 433 final scalar within the same interval using the function ⁴³⁴ $\emph{Smoothmax}(\alpha, R_i, W) \coloneqq \sum_j w_j R_i^j e^{\alpha R_i^j} / \sum_j w_j e^{\alpha R_i^j}.$ If one 435 component is made out of several targets, an intermediate ⁴³⁶ combination using the latter is also performed. *Good* and ⁴³⁷ *bad* parameters in the *Softplus* formulation, scales the reward 438 signal according to regions of interest in the reward space. ⁴³⁹ Tight values in both parameters will lead to higher focus on ⁴⁴⁰ the component to achieve high reward. Smoother values will 441 help exploration at the cost of precise control. Weights in the 442 *Smoothmax* definition affects the importance of each reward 443

444 component, while the α defines focus balance between them. Specifically, we combine all 32 distances of the LCFS with $w = 1$ and $\alpha = -1$. Reward undergo a final scaling, so that the maximum cumulative reward for 500 ms equals 50. For a description of each component's weight and parameters, please refer to table [1.](#page-4-0)

 Agent In this work, a distributed *Maximum a Posteriori ` Policy Optimization* (MPO) [\[Abdolmaleki and et al., 2018a;](#page-6-0) [Abdolmaleki and et al., 2018b\]](#page-7-23) is used, which have shown strong empirical results on a wide range of control prob- lems, including fusion. It is part of a recent interpretation of RL as probabilistic inference [\[Levine, 2018\]](#page-7-24). Since our environment is computationally expensive, such paradigm is useful to enhance sample-efficiency and reach faster con- vergence compared to a variety of policy gradient methods, while avoiding the use of on-policy algorithm such as *Proxi- mal Policy Optimization* (PPO) [\[Schulman and et al., 2017\]](#page-8-5). Our implementation is composed of 95 multi-layered percep- trons for the actors and a LSTM for the critic. Specifically, we use stochastic policies which predict a mean and a stan- dard deviation for each of the 11 control coils. Once training is completed, exploring possible outcomes is not needed any- more. As a consequence, only the mean of each distribution is kept at inference to predict optimal actions. Sequences were partitioned so that a *burn-in* phase would take place at each learner step, i.e. part of each input sequence sampled from [t](#page-7-25)he replay buffer is used to initialize the LSTM core [\[Kaptur-](#page-7-25) [owski and et al., 2018\]](#page-7-25). Adam optimizer was used both in the critic and the actor networks. Specific hyperparameters cho- sen for NNs definition can be found in table [2,](#page-5-0) with others as [w](#page-7-13)ell as initialization practices following [\[Kerboua-Benlarbi](#page-7-13) *et al.*[, 2024\]](#page-7-13).

| Hyperparameter | Chosen value | |
|----------------------------|--------------|--|
| Batch size | 256 | |
| Discount factor | 0.99 | |
| Sequence length for critic | 64 | |
| Burn-in length critic | 10 | |
| π_{σ} | 0.5 | |
| ϵ | 0.5 | |
| ϵ_μ | $9.09e-5$ | |
| ϵ_{σ} | $9.09e-8$ | |
| learning rate | $3e-4$ | |
| dual learning rate | $1.5e-2$ | |

Table 2: Agent's hyperparameters.

476 Training framework The interaction loop can be described as follows: a learner worker uses information gathered within a replay buffer to optimize policy and critic NNs; actor threads work independently from each other. Each thread spans a UDS protocol client-server interface with its own ran- dom seed, in which the policy interacts with an instance of NICE, sending data to the replay buffer asynchronously; each actor updates its control policy by copying weights periodi- cally from the learner. Evaluation is performed on a sepa- rate thread during training using only the mean of the current policy as stated before. This results in a fast and reliable,

multi-language, multi-threaded and multi-GPU framework, ⁴⁸⁷ running numerous instances of the NICE environment in par- ⁴⁸⁸ allel to learn a control policy in Python (Figure [5\)](#page-5-1). Policy ⁴⁸⁹ networks were all restricted to CPU, in order to lower sim- ⁴⁹⁰ ulation to reality gaps. Every aspect of the framework then 491 ensures that training can put the agent in realistic conditions ⁴⁹² with regards to the machine's usual operation. Experiments 493 are performed on a NVIDIA® Tesla™ V100S for the learner, ⁴⁹⁴ and Intel® Cascade Lake® 6248 at 2.50GHz for the C++ en- ⁴⁹⁵ vironments. As a side note, the framework is flexible enough ⁴⁹⁶ to allow fast update or addition of new control scenarios. 497

Figure 5: Framework's overview.

4.2 Results 498

Training results are averaged over 3 different seeds of the ⁴⁹⁹ evaluator thread. The reward threshold for the TTT is set to 500 20, as control starts to perform well in such conditions. $\frac{501}{200}$

Firstly, we know that an environment's step within NICE 502 lasts for about 13 seconds on average during exploration, 503 since the plasma reaches locations of the vacuum chamber in 504 which convergence of the simulation is more difficult. This 505 means that in the complex case, where poor reward signals are 506 common, exploration is long and tedious, increasing comput- ⁵⁰⁷ ing time of an episode up to 2 hours. Based on this idea, the 508 monitored training time for the vanilla method easily reaches 509 the symbolic threshold of an entire week. Moreover, the re- ⁵¹⁰ ward never exceeds 10 in average, even with training outside 511 the 60 episodes cap scope, which is way under our expecta- ⁵¹² tions regarding TTT (Figure [7](#page-6-1) - upper). One could mention 513 the fact that we could have undergo further hyperparameters 514 search on the reward definition. However, we kept it general 515 enough to avoid overspecializing the method towards one sce- ⁵¹⁶ nario, leaving more room for adaptation. On the other hand, 517

 the CL procedure implicitly leads to reachable states that are easier at the beginning of the initial task. As a consequence, the duration of a simulation's step in this case is shorter in average, and the simulation converges to an equilibrium in about 2 seconds. Next tasks follow on top of this idea, which leads to 10 seconds in average for what is remaining from the curriculum. This leads to episodes computed at worst in 1 hour for complex tasks, which is already an interesting out- come. With that in mind, the reward threshold is reached in about 100 episodes, and the TTT is reduced to approximately 60 hours. As a matter of fact, we observe a clear reduction in convergence time towards the reward threshold, sufficient to gain proper control of the plasma in the configuration of interest (Figure [6a\)](#page-6-2). We stopped training before 60 episodes for the final task, since the return was stable above 20.

 If we look at the jumpstart using the total number of episodes, CL actually performs equally, if not worse, than the vanilla method for each curriculum steps (Figure [7](#page-6-1) - up- per). A simple explanation comes from the fact that the added reward complexity inevitably drops the initial return. Another explanation could arise from so-called catastrophic forgetting. After those sudden drops, the agent fails its first attempt, especially on the last task, but ends up recovering. Recall that we are not stopping previous tasks based on per- formance, but rather constraining the entire training time to 60 episodes. So, this situation is not entirely surprising, since no optimal behavior was guaranteed at the end of each in- termediate curriculum step. Moreover, MPO requires several initial exploratory episodes, in order for training to start con- cretely. This means that the overall method could also be analyzed without those warm-up interactions, restricting the figure to the last 20 meaningful episodes for example (Figure [7](#page-6-1) - lower). In this case, both metrics gives better results, as only improved behaviors are taken into account: the jump- start is significantly higher, despite the last drop for the last transition, and the time to threslhold is even lower. Actu- ally, drooping the warm-up interactions becomes even more meaningful if we extend transfer to the overall MPO's inter- nal mechanism. A such, exploration would not be as strong as at MPO's initilization, and fine-tuning would be predominant throughout the reward function.

 CL does clearly improve the average performance on the final task (Figure [6b\)](#page-6-2), as it performs better than the vanilla policy (Figures [7](#page-6-1) - both). It enhances magnetic control, show- ing that the method does not induce any training instabilities, apart from potential catastrophic forgetting.

| | Method | Jumpstart on the final task | | TTT | | |
|-----------------------|----------------|-----------------------------|-----------------------|------------|--|--|
| | Vanilla 4.3 | | 180h | | | |
| | CL. | -10.2 | | 60h | | |
| (a) Transfer metrics. | | | | | | |
| | | Episode mean reward | Error margin | | | |
| | Vanilla | 5.2 | $\overline{\pm 3.65}$ | | | |
| | | 18.4 | ± 4.23 | | | |

(b) Mean error for each component.

Figure 6: Analysis of the vanilla control policy against the CL method.

Figure 7: Episodic return for both methods (vanilla - red, CL green). Since MPO takes several hours to properly start learning, we consider the last episodes that were meaningful regarding reward convergence.

5 Conclusion and perspectives 564

Curriculum learning displays interesting results in terms of ⁵⁶⁵ convergence time, while reaching higher levels of perfor- ⁵⁶⁶ mance that a controller exhibits when trained from scratch. 567 Through the simple definition of a sequence of tasks in terms 568 of reward functions, robust magnetic controllers are obtained 569 three times faster than baseline training which requires at ⁵⁷⁰ least a wee. $=k$. 571

This work is one of the first attempts along with [\[Tracey](#page-8-19) 572] *et al.*[, 2023\]](#page-8-19) to look for practical means of speeding up train- ⁵⁷³ ing of RL-based magnetic controllers. The two methods are 574 also not orthogonal, and combining them could lead to train- ⁵⁷⁵ ing times even shorter. Moreover, we fixed the action space 576 between tasks, but using the 11 coils might not be useful all 577 the time. Same goes for the magnetic measurements, since 578 nothing indicates that all sensors are useful all the time. Automatic sequencing of the action and state spaces definitions 580 could help in improving the curriculum generation.

A clear limitation of the method comes from the risk of 582 catastrophic forgetting, since we transfer without freezing ⁵⁸³ procedure. A perspective lies in the use of *Progressive Neu-* ⁵⁸⁴ *ral Networks* (PNN)[Rusu *et al.*[, 2016b\]](#page-8-20), which are not af- ⁵⁸⁵ fected by catastrophic forgetting and are theoretically capa- ⁵⁸⁶ ble of handling complete different tasks. However, big architectures can not efficiently work on real-time control sys- ⁵⁸⁸ tems due to predictions slower than the timescale of many ⁵⁸⁹ plasma events. One solution could come from *Policy Distil-* ⁵⁹⁰ *lation* [Rusu *et al.*[, 2016a\]](#page-8-21). By training PNNs through cur- 591 riculum learning, powerful expert policies could be obtained ⁵⁹² quickly, and distilled into a smaller network in line with our 593 operational constraints. ⁵⁹⁴

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