

Text2NKG: Fine-Grained N-ary Relation Extraction for N-ary relational Knowledge Graph Construction

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Abstract

Beyond traditional binary relational facts, n-ary relational knowledge graphs (NKGs) are comprised of n-ary relational facts containing more than two entities, which are closer to real-world facts with broader applications. However, the construction of NKGs remains at a course-grained level, which is always in a single schema, ignoring the order and variable arity of entities. To address these restrictions, we propose Text2NKG, a novel fine-grained n-ary relation extraction framework for n-ary relational knowledge graph construction. We introduce a span-tuple classification approach with hetero-ordered merging and output merging to accomplish fine-grained n-ary relation extraction in different arity. Furthermore, Text2NKG supports four typical NKG schemas: *hyper-relational schema*, *event-based schema*, *role-based schema*, and *hypergraph-based schema*, with high flexibility and practicality. The experimental results demonstrate that Text2NKG achieves state-of-the-art performance in F_1 scores on the fine-grained n-ary relation extraction benchmark. Our code and datasets are publicly available¹.

1 Introduction

Modern knowledge graphs (KGs), such as Freebase (Bollacker et al., 2008), Google Knowledge Vault (Dong et al., 2014), and Wikidata (Vrandečić and Krötzsch, 2014), utilize a multi-relational graph structure to represent knowledge. Because of the advantage of intuitiveness and interpretability, KGs find various applications in question answering (Yih et al., 2015), query response (Arakelyan et al., 2021), logical reasoning (Chen et al., 2022), and recommendation systems (Zhang et al., 2016). Traditional KGs are mostly composed of binary relational facts (*subject, relation, object*),

¹Anonymous Github Code: <https://anonymous.4open.science/r/Text2NKG>

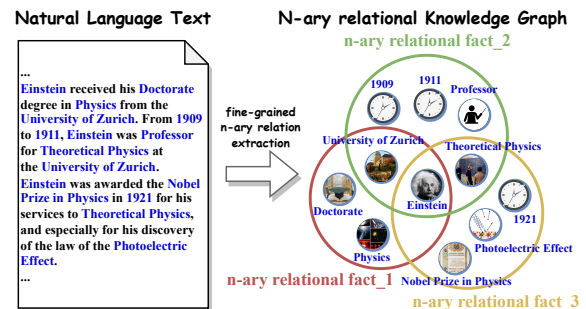


Figure 1: An example of NKG construction.

which represent the relationship between two entities (Bordes et al., 2013). However, it has been observed (Rosso et al., 2020) that over 30% of real-world facts involve n-ary relation facts with more than two entities ($n \geq 2$). As shown in Figure 1, an n-ary relational knowledge graph (NKG) is composed of many n-ary relation facts, offering richer knowledge expression and wider application capabilities. As a key step of constructing NKGs, n-ary relation extraction (n-ary RE) is a task of identifying n-ary relations among entities in natural language texts.

Compared to binary relational facts, n-ary relational facts in NKGs have more diverse schemas for different scenarios. For example, Wikidata utilizes n-ary relational facts in a *hyper-relational schema* (Rosso et al., 2020; Galkin et al., 2020; Wang et al., 2021a), i.e., $(s, r, o, \{(k_i, v_i)\}_{i=1}^{n-2})$ which adds $(n - 2)$ key-value pairs to the main triple to represent auxiliary information. In addition to the *hyper-relational schema*, the existing NKG schemas also include *event-based schema* $(r, \{(k_i, v_i)\}_{i=1}^n)$ (Guan et al., 2022; Lu et al., 2021), *role-based schema* $(\{(k_i, v_i)\}_{i=1}^n)$ (Guan et al., 2019; Liu et al., 2021), and *hypergraph-based schema* $(r, \{v_i\}_{i=1}^n)$ (Wen et al., 2016; Fatemi et al., 2021), as shown in Figure 2, which are different in the number of extracted relations.

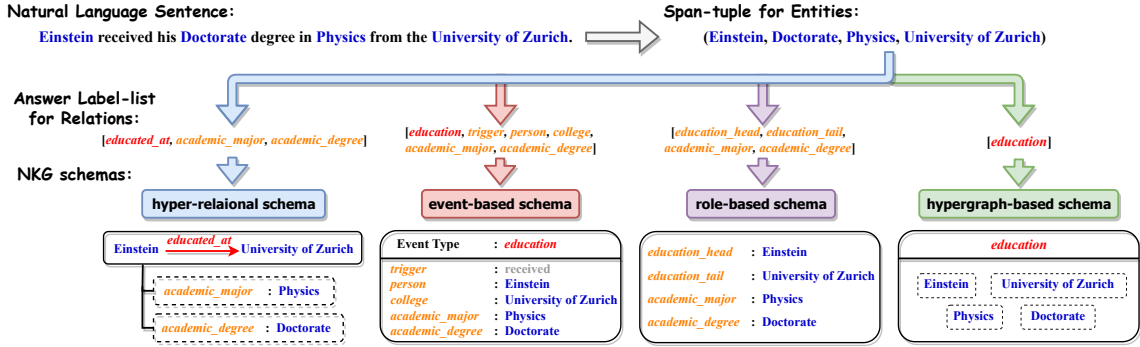


Figure 2: Taking a real-world textual fact as an example, we can extract a four-arity structured span-tuple for entities (Einstein, University of Zurich, Doctorate, Physics) with an answer label-list for relations accordingly as a 4-ary relational fact from the sentence through n-ary relation extraction.

067 Currently, most existing NKGs in four schemas, 104
 068 such as JF17K (Wen et al., 2016), Wikipoe- 105
 069 ple (Guan et al., 2019), WD50K (Galkin et al., 106
 070 2020), and EventKG (Guan et al., 2022), are manu- 107
 071 ally constructed. Previous n-ary RE methods (Jia 108
 072 et al., 2019; Zhuang et al., 2022) focus on extrac- 109
 073 tion with a fixed number of entities in *hypergraph-* 110
 074 *based schema* or *role-based schema*. Existing event 111
 075 extraction methods (Lu et al., 2021, 2022; Fei et al., 112
 076 2022) can achieve n-ary RE in *event-based schema*. 113
 077 Recently, CubeRE (Chia et al., 2022) introduce a 114
 078 cube-filling method, which is the only n-ary RE 115
 079 method in *hyper-relational schema*. 116

080 However, there are still three main challenges in 117
 081 automated n-ary RE for NKG construction, which 118
 082 remains at a course-grained level: (1) **Diversity** 119
 083 **of NKG schemas**. Previous methods could only 120
 084 perform N-ary RE based on a specific schema, but 121
 085 currently, there is no flexible method that can per- 122
 086 form n-ary RE for arbitrary schema with different 123
 087 number of relations. (2) **Determination of the or-** 124
 088 **der of entities**. N-ary RE involves more possible 125
 089 entity orders than binary RE, and previous methods 126
 090 often ignored the joint impact of different entity 127
 091 orders, leading to inaccurate precision. (3) **Vari-** 128
 092 **ability of the arity of n-ary RE**. Previous methods 129
 093 usually output a fixed number of entities and are 130
 094 not adept at determining the variable number of 131
 095 entities forming an n-ary relational fact. 132

096 To tackle these challenges, we introduce 133
 097 **Text2NKG**, a novel fine-grained n-ary RE frame- 134
 098 work designed to automate the generation of n-ary 135
 099 relational facts from natural language text for NKG 136
 100 construction. Text2NKG employs a **span-tuple** 137
 101 **multi-label classification** method, which trans- 138
 102 forms n-ary RE into a multi-label classification 139
 103 task for span-tuples, including all combinations of

104 entities in the text. Because the number of pre- 105
 106 dicted relation labels corresponds to the chosen 107
 108 NKG schema, Text2NKG is adaptable to all NKG 109
 110 schemas, offering examples with *hyper-relational* 111
 112 *schema*, *event-based schema*, *role-based schema*, 113
 114 and *hypergraph-based schema*, all of which have 115
 116 broad applications. Moreover, Text2NKG intro- 117
 118 duces a **hetero-ordered merging** method, consid- 119
 120 ering the probabilities of predicted labels for differ- 121
 122 ent entity orders to determine the final entity order. 123
 124 Finally, Text2NKG proposes an **output merging** 125
 126 method, which is used to unsupervisedly derive 127
 128 n-ary relational facts of any number of entities for 129
 130 NKG construction. 131

132 In addition, we extend the only n-ary RE bench- 133
 134 mark for NKG construction, HyperRED (Chia 134
 135 et al., 2022), which is in the *hyper-relational* 135
 136 *schema*, to four NKG schemas. We’ve done suffi- 137
 138 cient n-ary RE experiments on HyperRED, and the 138
 139 experimental results show that Text2NKG achieves 139
 140 state-of-the-art performance in F_1 scores of hyper- 140
 141 relational extraction. We also compared the results 141
 142 of Text2NKG in the other three schemas to verify 142
 143 applications. We are excited to open-source our 143
 144 complete code and are willing to contribute to the 144
 145 knowledge graph construction community. 145

2 Related Work 130

2.1 N-ary relational Knowledge Graph 131

132 An n-ary relational knowledge graph (NKG) con- 132
 133 sists of n-ary relational facts, which contain n 133
 134 entities ($n \geq 2$) and several relations. The n-ary re- 134
 135 lational facts are necessary and cannot be replaced 135
 136 by combinations of some binary relational facts 136
 137 because we cannot distinguish which binary rela- 137
 138 tions are combined to represent the n-ary relational 138

fact in the whole KG. Therefore, NKG utilizes a schema in every n-ary relational fact locally and a hypergraph representation globally (Luo et al., 2023).

Firstly, the simplest NKG schema is hypergraph-based. Wen et al. (2016) found that over 30% of Freebase (Bollacker et al., 2008) entities participate facts with more than two entities, first defined n-ary relations mathematically and used star-to-clique conversion to convert triple-based facts representing n-ary relational facts into the first NKG dataset JF17K in *hypergraph-based schema* $(r, \{v_i\}_{i=1}^n)$. Fatemi et al. (2021) proposed FB-AUTO and M-FB15K with the same *hypergraph-based schema*. Secondly, Guan et al. (2019) introduced role information for n-ary relational facts and extracted Wikipeople, the first NKG dataset in *role-based schema* $(\{(k_i, v_i)\}_{i=1}^n)$, composed of role-value pairs. Thirdly, Wikidata (Vrandečić and Krötzsch, 2014), the largest knowledge base, utilizes an NKG schema based on hyper-relation $(s, r, o, \{(k_i, v_i)\}_{i=1}^{n-2})$, which adds auxiliary key-value pairs to the main triple. Galkin et al. (2020) first proposed an NKG dataset in *hyper-relational schema* WD50K. Fourthly, as Guan et al. (2022) pointed out, events are also n-ary relational facts. One basic event representation has an event type, a trigger, and several key-value pairs (Lu et al., 2021). Regarding the event type as the main relation, the (trigger: value) as one of the key-value pairs, and the arguments as the rest key-value pairs, we can obtain an *event-based NKG schema* $(r, \{(k_i, v_i)\}_{i=1}^n)$.

Based on four common NKG schemas, we propose Text2NKG, the first method for extraction of structured n-ary relational facts from natural language text, which improves NKG representation and application.

2.2 N-ary Relation Extraction

Relation extraction (RE) is an important step of KG construction, directly affecting the quality, scale, and application of KGs. While most of the current n-ary relation extraction (n-ary RE) for NKG construction depends on manual construction (Wen et al., 2016; Guan et al., 2019; Galkin et al., 2020) but not automated methods. Most automated RE methods target the extraction of traditional binary relational facts. For example, Wang and Lu (2020) proposes a table-filling method for binary RE, and Zhong and Chen (2021); Ye et al. (2022) propose span-based RE methods with levitated marker and

packed levitated marker, respectively.

For automated n-ary RE, some approaches (Jia et al., 2019; Zhuang et al., 2022) treat n-ary RE in *hypergraph-based schema* or *role-based schema* as a binary classification problem and predict whether the composition of n-ary information in a document is valid or not. However, these methods extract n-ary information in fixed arity, which are not flexible. Moreover, some event extraction methods (Lu et al., 2021, 2022; Fei et al., 2022) propose different event trigger and argument extraction techniques, which can achieve n-ary RE in *event-based schema*. Recently, CubeRE (Chia et al., 2022) proposes an automated n-ary RE method in *hyper-relational schema*, which extends the table-filling extraction method to n-ary RE with cube-filling. However, these methods can only model one of the useful NKG schemas with limited extraction accuracy.

In this paper, we propose the first fine-grained n-ary RE framework Text2NKG for NKG construction in four example schemas, proposing a span-tuple multi-label classification method with hetero-ordered merging and output merging to improve the accuracy of fine-grained n-ary RE extraction in all NKG schemas substantially.

3 Preliminaries

3.1 Formulation of NKG

An NKG $\mathcal{G} = \{\mathcal{E}, \mathcal{R}, \mathcal{F}\}$ consists of an entity set \mathcal{E} , a relation set \mathcal{R} , and an n-ary fact ($n \geq 2$) set \mathcal{F} . Each fact $f^n \in \mathcal{F}$ consists of entities $\in \mathcal{E}$ and relations $\in \mathcal{R}$. In NKGs with different schemas, the number and structure of relations corresponding to n entities in an n-ary fact f^n vary.

For *hyper-relational schema* (Rosso et al., 2020):

$$f_{hr}^n = \begin{cases} (e_1, r_1, e_2), & n = 2, \\ (e_1, r_1, e_2, \{r_{i-1}, e_i\}_{i=3}^n), & n > 2, \end{cases} \quad (1)$$

where $\{e_i\}_{i=1}^n \in \mathcal{E}$, $\{r_i\}_{i=1}^{n-1} \in \mathcal{R}$.

For *event-based schema* (Lu et al., 2021):

$$f_{ev}^n = (r_1, \{r_{i+1}, e_i\}_{i=1}^n), \quad (2)$$

where $\{e_i\}_{i=1}^n \in \mathcal{E}$, $\{r_i\}_{i=1}^{n+1} \in \mathcal{R}$.

For *role-based schema* (Guan et al., 2019):

$$f_{ro}^n = (\{r_i, e_i\}_{i=1}^n), \quad (3)$$

where $\{e_i\}_{i=1}^n \in \mathcal{E}$, $\{r_i\}_{i=1}^n \in \mathcal{R}$.

For *hypergraph-based schema* (Wen et al., 2016):

$$f_{hg}^n = (r_1, \{e_i\}_{i=1}^n), \quad (4)$$

where $\{e_i\}_{i=1}^n \in \mathcal{E}$, $r_1 \in \mathcal{R}$.

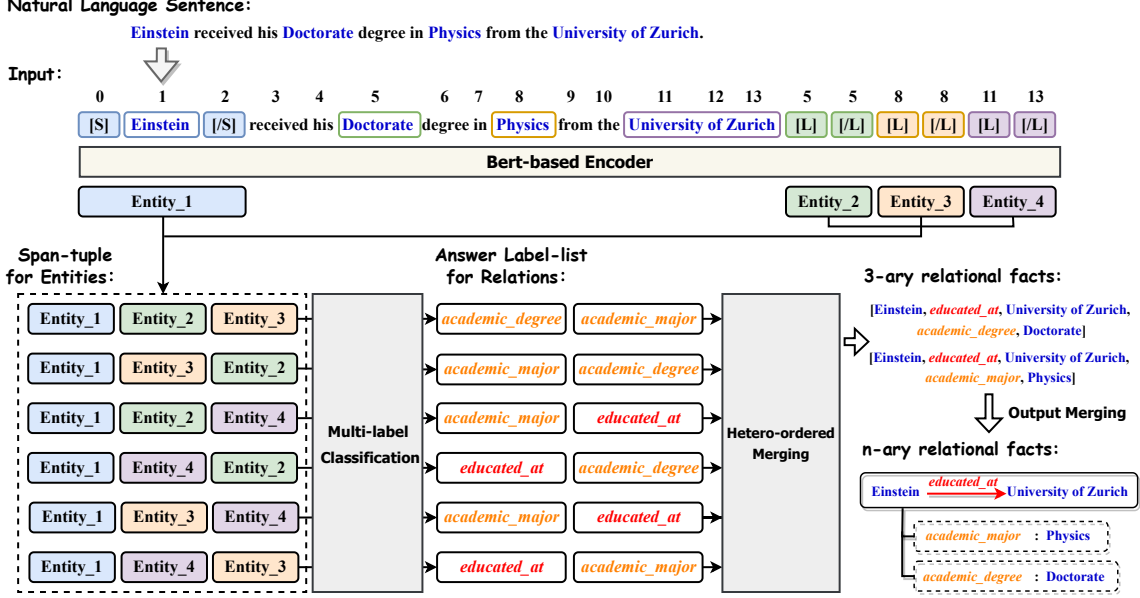


Figure 3: An overview of Text2NKG extracting n-ary relation facts from a natural language sentence in hyper-relational NKG schema for an example.

3.2 Problem Definition

Given an input sentence with l words $s = \{w_1, w_2, \dots, w_l\}$, an entity e is a consecutive span of words: $e = \{w_p, w_{p+1}, \dots, w_q\} \in \mathcal{E}_s$, where $p, q \in \{1, \dots, l\}$, and $\mathcal{E}_s = \{e_j\}_{j=1}^m$ is the entity set of all m entities in the sentence. The output of n-ary relation extraction, $R()$, is a set of n-ary relational facts \mathcal{F}_s in given NKG schema in $\{f_{hr}^n, f_{ev}^n, f_{ro}^n, f_{hg}^n\}$. Specifically, each n-ary relational fact $f^n \in \mathcal{F}_s$ is extracted with ordered n entities $[e_i]_{i=1}^n \in \mathcal{E}_s$ out of all entities, and a list of labeled n_r relations $[r_i]_{i=1}^{n_r} \in \mathcal{R}$ from the candidate relation set, where n is the arity of the extracted n-ary relational fact, and n_r is the number of relations in the fact, which is determined by the given NKG schema as follows:

$$R([e_i]_{i=1}^n) = \begin{cases} [r_i]_{i=1}^{n-1}, & f^n = f_{hr}^n, \\ [r_i]_{i=1}^{n+1}, & f^n = f_{ev}^n, \\ [r_i]_{i=1}^n, & f^n = f_{ro}^n, \\ [r_1], & f^n = f_{hg}^n. \end{cases} \quad (5)$$

4 Methodology

In this section, we first introduce the overview of the Text2NKG framework, followed by the span-tuple multi-label classification, training strategy, hetero-ordered merging, and output merging.

4.1 Overview of Text2NKG

Text2NKG is a fine-grained n-ary relation extraction framework built for n-ary relational knowledge

graph (NKG) construction. The input to Text2NKG is natural language text tokens labeled with entity span in sentence units. First, inspired by Ye et al. (2022), Text2NKG encodes the entities using BERT-based Encoder (Devlin et al., 2019) with a packaged levitated marker for embedding. Then each arrangement of ordered span-tuple with three entity embeddings will be classified with multiple labels, and the framework will be learned by the weighted cross-entropy with a null-label bias. In the decoding stage, in order to filter the n-ary relational facts whose entity compositions have isomorphic hetero-ordered characteristics, Text2NKG proposes a hetero-ordered merging strategy to merge the label probabilities of $3! = 6$ arrangement cases of span-tuples composed of the same entities and filter out the output 3-ary relational facts existing non-conforming relations. Finally, Text2NKG combines the output 3-ary relational facts to form the final n-ary relational facts with output merging.

4.2 Span-tuple Multi-label Classification

For the given sentence token $s = \{w_1, w_2, \dots, w_l\}$ and the set of entities \mathcal{E}_s , in order to perform fine-grained n-ary RE, we need first to encode a span-tuple (e_1, e_2, e_3) consisting of every arrangement of three ordered entities, where $e_1, e_2, e_3 \in \mathcal{E}_s$. Due to the high time complexity of training every span-tuple as one training item, inspired by Ye et al. (2022), we achieve the reduction of training items by using packed levitated markers that pack

one training item with each entity in \mathcal{E}_s separately. Specifically, in each packed training item, a pair of solid tokens, [S] and [/S], are added before and after the packed entity $e_S = \{w_{p_S}, \dots, w_{q_S}\}$, and $(|\mathcal{E}_s| - 1)$ pairs of levitated markers, [L] and [/L], according to other entities in \mathcal{E}_s , are added with the same position embeddings as the beginning and end of their corresponding entities span $e_{L_i} = \{w_{p_{L_i}}, \dots, w_{q_{L_i}}\}$ to form the input token \mathbf{X} :

$$\mathbf{X} = \{w_1, \dots, [S], w_{p_S}, \dots, w_{q_S}, [/S], \dots, w_{p_{L_i}} \cup [L], \dots, w_{q_{L_i}} \cup [/L], \dots, w_l\}. \quad (6)$$

We encode such token by the BERT-based pre-trained model encoder (Devlin et al., 2019):

$$\{h_1, h_2, \dots, h_t\} = \text{BERT}(\mathbf{X}), \quad (7)$$

where $t = |\mathbf{X}|$ is the input token length, $\{h_i\}_{i=1}^t \in \mathbb{R}^d$, and d is embedding size.

There are several span-tuples (A, B, C) in a training item. The embedding of first entity $h_A \in \mathbb{R}^{2d}$ in the span-tuple is obtained by concat embedding of the solid markers, [S] and [/S], and the embeddings of second and third entities $h_B, h_C \in \mathbb{R}^{2d}$ are obtained by concat embeddings of levitated markers, [L] and [/L] with all A_{m-1}^2 arrangement of any other two entities in \mathcal{E}_s . Thus, we obtain the embedding representation of the three entities to form A_{m-1}^2 span-tuples in one training item. Therefore, every input sentence contains m training items with $m A_{m-1}^2 = A_m^3$ span-tuples for any ordered arrangement of three entities.

We then define n_r linear classifiers, each of which consists of 3 feedforward neural networks $\{\text{FNN}_i^k\}_{i=1}^{n_r}$, $k = 1, 2, 3$, to classify the span-tuples for multiple-label classification. Each classifier targets the prediction of one relation r_i , thus obtaining a probability lists $(\mathbf{P}_i)_{i=1}^{n_r}$ with all relations in given relation set \mathcal{R} plus a null-label:

$$\mathbf{P}_i = \text{FNN}_i^1(h_A) + \text{FNN}_i^2(h_B) + \text{FNN}_i^3(h_C), \quad (8)$$

where $\text{FNN}_i^k \in \mathbb{R}^{2d \times (|\mathcal{R}|+1)}$, and $\mathbf{P}_i \in \mathbb{R}^{(|\mathcal{R}|+1)}$.

4.3 Training Strategy

To train the n_r classifiers for each relation prediction more accurately, we propose a data augmentation strategy for span-tuples. Taking the *hyper-relational schema* as an example, given a hyper-relational fact (A, r_1, B, r_2, C) , we consider swapping the head and tail entities, and changing the main relation to its inverse (B, r_1^{-1}, A, r_2, C) , as

well as swapping the tail entities with auxiliary values, and the main relation with the auxiliary key (A, r_2, C, r_1, B) , also as labeled training span-tuple cases. Thus $R_{hr}(A, B, C) = (r_1, r_2)$ can be augmented with $3! = 6$ orders of span-tuples:

$$\begin{cases} R_{hr}(A, B, C) = (r_1, r_2), \\ R_{hr}(B, A, C) = (r_1^{-1}, r_2), \\ R_{hr}(A, C, B) = (r_2, r_1), \\ R_{hr}(B, C, A) = (r_2, r_1^{-1}), \\ R_{hr}(C, A, B) = (r_2^{-1}, r_1), \\ R_{hr}(C, B, A) = (r_1, r_2^{-1}). \end{cases} \quad (9)$$

For other schemas, we can also obtain 6 fully-arranged cases of labeled span-tuples in a similar way, as described in Appendix A. If no n-ary relational fact exists between the three entities of span-tuples, then relation labels are set as null-label.

Since most cases of span-tuple are null-label, we set a weight hyperparameter $\alpha \in (0, 1]$ between the null-label and other labels to balance the learning of the null-label. We jointly trained the n_r classifiers for each relations by cross-entropy loss \mathcal{L} with a null-label weight bias \mathbf{W}_α :

$$\mathcal{L} = - \sum_{i=1}^{n_r} \mathbf{W}_\alpha \log \left(\frac{\exp(\mathbf{P}_i[r_i])}{\sum_{j=1}^{|\mathcal{R}|+1} \exp(\mathbf{P}_{ij})} \right), \quad (10)$$

where $\mathbf{W}_\alpha = [\alpha, 1.0, 1.0, \dots, 1.0] \in \mathbb{R}^{(|\mathcal{R}|+1)}$.

4.4 Hetero-ordered Merging

In the decoding stage, since Text2NKG labels all 6 different arrangement of the same entity composition, we design a hetero-ordered merging strategy to merge the corresponding labels of these 6 hetero-ordered span-tuples into one to generate non-repetitive n-ary relational facts unsupervisedly. For *hyper-relational schema* ($n_r = 2$), we combine the predicted probabilities of two labels $\mathbf{P}_1, \mathbf{P}_2$ in 6 orders to (A, B, C) order as follows:

$$\begin{cases} \mathbf{P}_1 = \mathbf{P}_1^{(ABC)} + I(\mathbf{P}_1^{(BAC)}) + \mathbf{P}_2^{(ACB)} \\ \quad + I(\mathbf{P}_2^{(BCA)}) + \mathbf{P}_2^{(CAB)} + \mathbf{P}_1^{(CBA)}, \\ \mathbf{P}_2 = \mathbf{P}_2^{(ABC)} + \mathbf{P}_2^{(BAC)} + \mathbf{P}_1^{(ACB)} \\ \quad + \mathbf{P}_1^{(BCA)} + I(\mathbf{P}_1^{(CAB)}) + I(\mathbf{P}_2^{(CBA)}), \end{cases} \quad (11)$$

where $I()$ is a function for swapping the predicted probability of relations and the corresponding inverse relations. Then, we take the maximum probability to obtain labels r_1, r_2 , forming a 3-ary relational fact (A, r_1, B, r_2, C) and filter it out if

Dataset	#Ent	#R_hr	#R_ev	#R_ro	#R_hg	All		Train		Dev		Test	
						#Sentence	#Fact	#Sentence	#Fact	#Sentence	#Fact	#Sentence	#Fact
HyperRED	40,293	106	232	168	62	44,840	45,994	39,840	39,978	1,000	1,220	4,000	4,796

Table 1: Dataset statistics, where the columns indicate the number of entities, relations with four schema, sentences and n-ary relational facts in all sets, train set, dev set, and test set, respectively.

there are null-label in (r_1, r_2) . If there are inverse relation labels in (r_1, r_2) , we can also transform the order of entities and relations as equation 9. For *event-based schema*, *role-based schema*, and *hypergraph-based schema*, all can be generated by hetero-ordered merging according to this idea, as shown in Appendix B.

4.5 Output Merging

After hetero-ordered merging, we merge the output 3-ary relational facts to form higher-arity facts, with *hyper-relational schema* based on the same main triple, *event-based schema* based on the same main relation (event type), *role-based schema* based on the same key-value pairs, and *hypergraph-based schema* based on the same hyperedge relation. This way, we can unsupervisedly obtain n-ary relational facts with dynamic number of arity numbers for NKG construction. More details are discussed in Appendix G.2 and Appendix G.3.

5 Experiments

This section presents the experimental setup, results, and analysis. We answer the following research questions (RQs): **RQ1**: Does Text2NKG outperform other n-ary RE methods? **RQ2**: Whether Text2NKG can cover NKG construction for various schemas? **RQ3**: Does the main components of Text2NKG work? **RQ4**: How does the null-label bias hyperparameter in Text2NKG affect performance? **RQ5**: Can Text2NKG get complete n-ary relational facts in different arity? **RQ6**: How does Text2NKG perform in specific case study? **RQ7**: What is the future development of Text2NKG in the era of large language models?

5.1 Experimental Setup

Datasets. The existing fine-grained n-ary RE dataset is **HyperRED** (Chia et al., 2022) only in *hyper-relational schema* with annotated extracted entities. Therefore, we expand the HyperRED dataset to four schemas as standard fine-grained n-ary RE benchmarks and conduct experiments on them. The statistics of the HyperRED with four

schemas are shown in Table 1 and the construction detail is in Appendix C.

Baselines. We compare Text2NKG against **Generative Baseline** (Lewis et al., 2020), **Pipeline Baseline** (Wang et al., 2021b), and **CubeRE** (Chia et al., 2022) in fine-grained n-ary RE task of *hyper-relational schema*. For n-ary RE in the other three schemas, we compared Text2NKG with event extraction models such as **Text2Event** (Lu et al., 2021), **UIE** (Lu et al., 2022), and **LasUIE** (Fei et al., 2022). Furthermore, we utilized different prompts to test the currently most advanced large-scale pre-trained language models **ChatGPT** (Wei et al., 2023) and **GPT-4** (OpenAI, 2023) in an unsupervised manner, specifically for the extraction performance across the four schemas. The detailed baseline settings can be found in Appendix D.

Ablations. To evaluate the significance of Text2NKG’s three main components, data augmentation (DA), null-label weight hyperparameter (α), and hetero-ordered merging (HM), we obtain three simplified model variants by removing any one component (**Text2NKG w/o DA**, **Text2NKG w/o α** , and **Text2NKG w/o HM**) for comparison.

Evaluation Metrics. We use the F_1 score with precision and recall to evaluate the dev set and the test set. For a predicted n-ary relational fact to be considered correct, the entire fact must match the ground facts completely.

Hyperparameters and Environment. We train 10 epochs on HyperRED using the Adam optimizer. All experiments were done on a single NVIDIA A100 GPU, and all experimental results were derived by averaging 5 random seed experiments. Appendix E shows Text2NKG’s optimal hyperparameter settings. Appendix F shows training details.

5.2 Main Results (RQ1)

The experimental results of proposed Text2NKG and other baselines with both BERT-base and BERT-large encoders can be found in Table 2 for the fine-grained n-ary RE in *hyper-relational schema*. We can observe that Text2NKG shows a significant improvement over the existing optimal

Model	PLM	HyperRED : <i>hyper-relational schema</i> / Dev			HyperRED : <i>hyper-relational schema</i> / Test		
		Precision	Recall	F_1	Precision	Recall	F_1
Unsupervised Method							
ChatGPT	gpt-3.5-turbo	12.0583	11.2764	11.6542	11.4021	10.9134	11.1524
GPT-4	gpt-4	15.7324	15.2377	15.4811	15.8187	15.4824	15.6487
Supervised Method							
Generative Baseline		63.79 ± 0.27	59.94 ± 0.68	61.80 ± 0.37	64.60 ± 0.47	59.67 ± 0.35	62.03 ± 0.21
Pipeline Baseline		69.23 ± 0.30	58.21 ± 0.57	63.24 ± 0.44	69.00 ± 0.48	57.55 ± 0.19	62.75 ± 0.29
CubeRE		66.14 ± 0.88	64.39 ± 1.23	65.23 ± 0.82	65.82 ± 0.84	64.28 ± 0.25	65.04 ± 0.29
Text2NKG w/o DA	BERT-base (110M)	76.02 ± 0.50	72.28 ± 0.68	74.10 ± 0.55	73.55 ± 0.81	70.63 ± 1.40	72.06 ± 0.34
Text2NKG w/o α		88.77 ± 0.85	78.39 ± 0.47	83.26 ± 0.70	88.09 ± 0.69	76.64 ± 0.45	81.97 ± 0.58
Text2NKG w/o HM		61.74 ± 0.34	76.97 ± 0.44	68.52 ± 0.69	61.07 ± 0.73	76.16 ± 0.59	67.72 ± 0.48
Text2NKG (ours)		91.26 ± 0.69	79.36 ± 0.51	84.89 ± 0.44	90.77 ± 0.60	77.53 ± 0.32	83.63 ± 0.63
Generative Baseline		67.08 ± 0.49	65.73 ± 0.78	66.40 ± 0.47	67.17 ± 0.40	64.56 ± 0.58	65.84 ± 0.25
Pipeline Baseline	BERT-large (340M)	70.58 ± 0.78	66.58 ± 0.66	68.52 ± 0.32	69.21 ± 0.55	64.27 ± 0.24	66.65 ± 0.28
CubeRE		68.75 ± 0.82	68.88 ± 1.03	68.81 ± 0.46	66.39 ± 0.96	67.12 ± 0.69	66.75 ± 0.28
Text2NKG (ours)		91.90 ± 0.79	79.43 ± 0.42	85.21 ± 0.69	91.06 ± 0.81	77.64 ± 0.46	83.81 ± 0.54

Table 2: Comparison of Text2NKG with other baselines in the hyper-relational extraction on HyperRED. Results of the supervised baseline models are mainly taken from the original paper (Chia et al., 2022). The best results in each metric are in **bold**.

Model	PLM	HyperRED : <i>event-based schema</i>			HyperRED : <i>role-based schema</i>			HyperRED : <i>hypergraph-based schema</i>		
		Precision	Recall	F_1	Precision	Recall	F_1	Precision	Recall	F_1
Unsupervised Method										
ChatGPT	gpt-3.5-turbo	10.4678	11.1628	10.8041	11.4387	10.4203	10.9058	11.2998	11.7852	11.5373
GPT-4	gpt-4	13.3681	14.6701	13.9888	13.6397	12.5355	13.0643	13.0907	13.6701	13.3741
Supervised Method										
Text2Event		73.94 ± 0.76	70.56 ± 0.58	72.21 ± 1.25	72.73 ± 0.79	68.45 ± 1.34	70.52 ± 0.62	73.68 ± 0.88	70.37 ± 0.51	71.98 ± 0.92
UIE	T5-base (220M)	76.51 ± 0.28	73.02 ± 0.66	74.72 ± 0.18	72.17 ± 0.29	69.84 ± 0.11	70.98 ± 0.31	72.03 ± 0.41	68.74 ± 0.13	70.34 ± 1.07
LasUIE		79.62 ± 0.27	78.04 ± 0.75	78.82 ± 0.26	77.01 ± 0.20	74.26 ± 0.25	75.61 ± 0.24	76.21 ± 0.07	73.75 ± 0.17	74.96 ± 0.42
Text2NKG	BERT-base (110M)	86.20 ± 0.57	79.25 ± 0.33	82.58 ± 0.20	86.72 ± 0.80	78.94 ± 0.59	82.64 ± 0.38	83.53 ± 1.18	86.59 ± 0.38	85.03 ± 0.86
Text2Event		75.58 ± 0.53	72.39 ± 0.82	73.97 ± 1.19	73.21 ± 0.45	70.85 ± 0.67	72.01 ± 0.31	75.28 ± 0.93	72.73 ± 1.07	73.98 ± 0.49
UIE	T5-large (770M)	79.38 ± 0.28	74.69 ± 0.61	76.96 ± 0.95	74.47 ± 1.42	71.84 ± 0.77	73.14 ± 0.38	74.57 ± 0.64	71.93 ± 0.86	73.22 ± 0.19
LasUIE		81.29 ± 0.83	79.54 ± 0.26	80.40 ± 0.65	79.37 ± 0.92	76.63 ± 0.44	77.97 ± 0.76	77.49 ± 0.35	74.96 ± 0.60	76.20 ± 0.87
Text2NKG	BERT-large (340M)	88.47 ± 0.95	80.30 ± 0.75	84.19 ± 1.29	86.87 ± 0.87	80.86 ± 0.29	83.76 ± 1.17	85.06 ± 0.33	86.72 ± 0.36	85.89 ± 0.69

Table 3: Comparison of Text2NKG with other baselines in the n-ary RE in event-based, role-based, and *hypergraph-based schemas* on HyperRED. The best results in each metric are in **bold**.

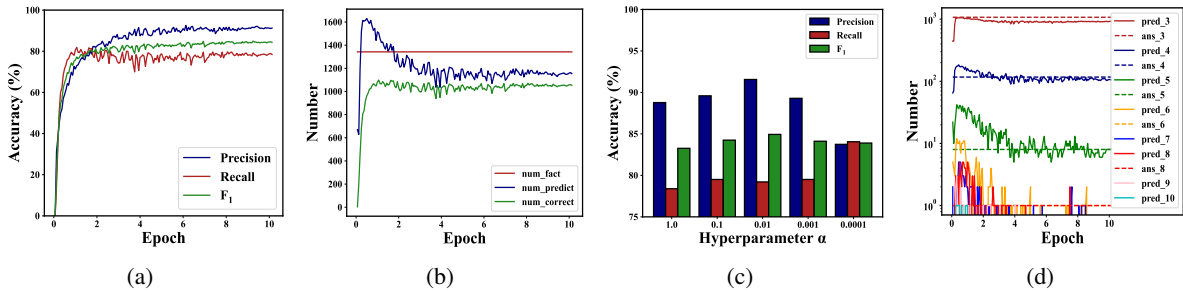


Figure 4: (a) Precision, Recall, and F_1 changes in the dev set during the training of Text2NKG. (b) The changes of the number of true facts, the number of predicted facts, and the number of predicted accurate facts during the training of Text2NKG. (c) Precision, Recall, and F_1 results on different null-label hyperparameter (α) settings. (d) The changes of the number of extracted n-ary RE in different arity.

455 model CubeRE on both the dev and test datasets
456 of HyperRED. The F_1 score is improved by 19.66
457 percentage points in the dev set and 18.60 percent-
458 age points in the test set with the same BERT-base
459 encoder, and 16.40 percentage points in the dev set
460 and 17.06 percentage points in the test set with
461 the same BERT-large encoder, reflecting Text2NKG’s
462 excellent performance. Figure 4(a) and 4(b) intu-
463 itively show the changes of evaluation metrics and
464 answers of facts in the dev set during the training

465 of Text2NKG. It is worth noting that Text2NKG
466 exceeds 90% in precision accuracy, which proves
467 that the model can obtain very accurate n-ary rela-
468 tional facts and provides a good guarantee for the
469 quality of fine-grained NKG construction.

5.3 Results on Various NKG Schemas (RQ2)

470 As shown in Table 3, besides *hyper-relational*
471 *schema*, Text2NKG also accomplishes the tasks of
472 fine-grained n-ary RE in three other different NKG
473

schemas on HyperRED, which demonstrates good utility. In the added tasks of n-ary RE for event-based, role-based, and *hypergraph-based schemas*, since no model has done similar experiments at present, we used event extraction or unified extraction methods such as Text2Event (Lu et al., 2021), UIE (Lu et al., 2022), and LasUIE (Fei et al., 2022) for comparison. Text2NKG still works best in these schemas, which demonstrates good versatility.

5.4 Ablation Study (RQ3)

Data augmentation (DA), null-label weight hyperparameter (α), and hetero-ordered merging (HM) are the three main components of Text2NKG. For the different Text2NKG variants as shown in Table 2, DA, α , and HM all contribute to the accurate results of our complete model. By comparing the differences, we find that HM is most effective by combining the probabilities of labels of different orders, followed by DA and α .

5.5 Analysis of Null-label Weight Hyperparameters (RQ4)

We compared the effect for different null-label weight hyperparameters (α). As shown in Figure 4(c), the larger the α , the greater the learning weight of null-label compared with other labels, the more relations are predicted as null-label. After filtering out the facts having null-label, fewer facts are extracted, so the precision is generally higher, and the recall is generally lower. The smaller the α , the more relations are predicted as non-null labels, thus extracting more n-ary relation facts, so the recall is generally higher, and the precision is generally lower. Comparing the results of F_1 values for different α , it is found that $\alpha = 0.01$ works best, which can be adjusted in practice according to specific needs to obtain the best results.

5.6 Analysis of N-ary Relation Extraction in Different Arity (RQ5)

Figure 4(d) shows the number of n-ary relational facts extracted after output merging and the number of the answer facts in different arity during training of Text2NKG on the dev set. We find that, as the training proceeds, the final output of Text2NKG converges to the correct answer in terms of the number of complete n-ary relational facts in each arity, achieving implementation of n-ary RE in indefinite arity unsupervised, with good scalability.

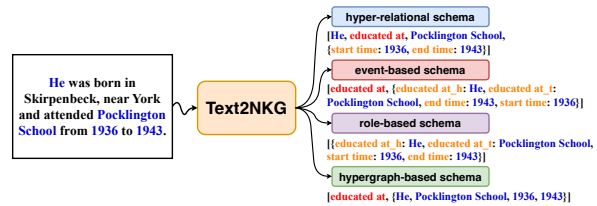


Figure 5: Case study of Text2NKG's n-ary relation extraction in four schemas on HyperRED.

5.7 Case Study (RQ6)

Figure 5 shows a case study of n-ary RE by a trained Text2NKG. For a natural language sentence, "He was born in Skirpenbeck, near York and attended Pocklin.", four structured n-ary RE can be obtained by Text2NKG according to the requirements. Taking the *hyper-relational schema* for an example, Text2NKG can successfully extract one n-ary relational fact consisting of a main triple [He, educated at, Pocklington], and two auxiliary key-value pairs {start time:1936}, {end time:1943}. This intuitively validates the practical performance of Text2NKG on the fine-grained n-ary RE to better contribute to NKG construction.

5.8 Comparison with ChatGPT (RQ7)

As shown in Table 2 and Table 3, we compared the extraction effects under four NKG schemas of the supervised Text2NKG with the unsupervised ChatGPT and GPT-4. We found that these large language models cannot accurately distinguish the closely related relations in the fine-grained NKG relation repository, resulting in their F1 scores ranging around 10%-15%, which is much lower than the performance of Text2NKG. On the other hand, the limitation of Text2NKG is that its performance is confined within the realm of supervised training. Therefore, in future improvements and practical applications, we suggest combining small supervised models with large unsupervised models to balance solving the cold-start and fine-grained extraction, which is detailed in Appendix G.1.

6 Conclusion

In this paper, we propose Text2NKG, a novel fine-grained n-ary RE framework for NKG construction. Experimental results show that Text2NKG outperforms other baselines on fine-grained n-ary RE tasks in all four schemas: hyper-relational, event-based, role-based, and hypergraph-based. Meanwhile, we extend HyperRED dataset to a fine-grained n-ary RE benchmark in four schemas.

561 **Limitations**

562 The fine-grained n-ary RE is a key step in the
563 transformation from natural text to NKG. With
564 the increasing emphasis on n-ary relational facts
565 in knowledge graphs nowadays, NKG would be a
566 very useful tool. However, there is now less work
567 on fine-grained n-ary RE, and the task is more com-
568 plex, Text2NKG, as the best framework at present,
569 needs more application cases. Text2NKG can also
570 be used in information extraction, event extraction,
571 and other areas that need further research.

572 **Ethics Statement**

573 This paper investigates the problem of fine-grained
574 n-ary RE, aiming at NKG construction. We use
575 deep learning methods to promote extraction per-
576 formance for applications better. Therefore, we
577 believe it does not violate any ethics.

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Appendix

A Supplement to Data Augmentation

In addition to the *hyper-relational schema*, the data augmentation strategies for other schemas are as follows:

For *event-based schema*, given an event-based fact $(r_1, r_2, A, r_3, B, r_4, C)$, we consider keeping the main relation r_1 unchanged, and swapping other key-value pairs, $\{r_2, A\}$, $\{r_3, B\}$, and $\{r_4, C\}$, positionally, also as labeled training span-tuple cases. Thus $R_{ev}(A, B, C) = (r_1, r_2, r_3, r_4)$ can be augmented with 6 orders of span-tuples:

$$\begin{cases} R_{ev}(A, B, C) = (r_1, r_2, r_3, r_4), \\ R_{ev}(B, A, C) = (r_1, r_3, r_2, r_4), \\ R_{ev}(A, C, B) = (r_1, r_2, r_4, r_3), \\ R_{ev}(B, C, A) = (r_1, r_3, r_4, r_2), \\ R_{ev}(C, A, B) = (r_1, r_4, r_2, r_3), \\ R_{ev}(C, B, A) = (r_1, r_4, r_3, r_2). \end{cases} \quad (12)$$

For *role-based schema*, given a role-based fact (r_1, A, r_2, B, r_3, C) , we consider swapping key-value pairs, $\{r_1, A\}$, $\{r_2, B\}$, and $\{r_3, C\}$, positionally, also as labeled training span-tuple cases. Thus $R_{ro}(A, B, C) = (r_1, r_2, r_3)$ can be augmented with 6 orders of span-tuples:

$$\begin{cases} R_{ro}(A, B, C) = (r_1, r_2, r_3), \\ R_{ro}(B, A, C) = (r_2, r_1, r_3), \\ R_{ro}(A, C, B) = (r_1, r_3, r_2), \\ R_{ro}(B, C, A) = (r_2, r_3, r_1), \\ R_{ro}(C, A, B) = (r_3, r_1, r_2), \\ R_{ro}(C, B, A) = (r_3, r_2, r_1). \end{cases} \quad (13)$$

For *hypergraph-based schema*, given a hypergraph-based fact (r_1, A, B, C) , we consider keeping the main relation r_1 unchanged, and swapping entities, A , B , and C , positionally, also as labeled training span-tuple cases. Thus $R_{hg}(A, B, C) = (r_1)$ can be augmented with 6 orders of span-tuples:

$$\begin{cases} R_{hg}(A, B, C) = (r_1), \\ R_{hg}(B, A, C) = (r_1), \\ R_{hg}(A, C, B) = (r_1), \\ R_{hg}(B, C, A) = (r_1), \\ R_{hg}(C, A, B) = (r_1), \\ R_{hg}(C, B, A) = (r_1). \end{cases} \quad (14)$$

B Supplement to Hetero-ordered Merging

In addition to the *hyper-relational schema*, the hetero-ordered merging strategies for other schemas are as follows:

For *event-based schema* ($n_r = 4$), we combine the predicted probabilities of four labels $\mathbf{P}_1, \mathbf{P}_2, \mathbf{P}_3, \mathbf{P}_4$ in 6 orders to (A, B, C) order as follows:

$$\begin{cases} \mathbf{P}_1 = \mathbf{P}_1^{(ABC)} + \mathbf{P}_1^{(BAC)} + \mathbf{P}_1^{(ACB)} \\ \quad + \mathbf{P}_1^{(BCA)} + \mathbf{P}_1^{(CAB)} + \mathbf{P}_1^{(CBA)}, \\ \mathbf{P}_2 = \mathbf{P}_2^{(ABC)} + \mathbf{P}_3^{(BAC)} + \mathbf{P}_2^{(ACB)} \\ \quad + \mathbf{P}_4^{(BCA)} + \mathbf{P}_3^{(CAB)} + \mathbf{P}_4^{(CBA)}, \\ \mathbf{P}_3 = \mathbf{P}_3^{(ABC)} + \mathbf{P}_2^{(BAC)} + \mathbf{P}_4^{(ACB)} \\ \quad + \mathbf{P}_2^{(BCA)} + \mathbf{P}_4^{(CAB)} + \mathbf{P}_3^{(CBA)}, \\ \mathbf{P}_4 = \mathbf{P}_4^{(ABC)} + \mathbf{P}_4^{(BAC)} + \mathbf{P}_3^{(ACB)} \\ \quad + \mathbf{P}_3^{(BCA)} + \mathbf{P}_2^{(CAB)} + \mathbf{P}_2^{(CBA)}. \end{cases} \quad (15)$$

Then, we take the maximum probability to obtain labels r_1, r_2, r_3, r_4 , forming a 3-ary relational fact $(r_1, r_2, A, r_3, B, r_4, C)$ and filter it out if there are null-label in (r_1, r_2, r_3, r_4) .

For *role-based schema* ($n_r = 3$), we combine the predicted probabilities of three labels $\mathbf{P}_1, \mathbf{P}_2, \mathbf{P}_3$ in 6 orders to (A, B, C) order as follows:

$$\begin{cases} \mathbf{P}_1 = \mathbf{P}_1^{(ABC)} + \mathbf{P}_2^{(BAC)} + \mathbf{P}_1^{(ACB)} \\ \quad + \mathbf{P}_3^{(BCA)} + \mathbf{P}_2^{(CAB)} + \mathbf{P}_3^{(CBA)}, \\ \mathbf{P}_2 = \mathbf{P}_2^{(ABC)} + \mathbf{P}_1^{(BAC)} + \mathbf{P}_3^{(ACB)} \\ \quad + \mathbf{P}_1^{(BCA)} + \mathbf{P}_3^{(CAB)} + \mathbf{P}_2^{(CBA)}, \\ \mathbf{P}_3 = \mathbf{P}_3^{(ABC)} + \mathbf{P}_3^{(BAC)} + \mathbf{P}_2^{(ACB)} \\ \quad + \mathbf{P}_2^{(BCA)} + \mathbf{P}_1^{(CAB)} + \mathbf{P}_1^{(CBA)}. \end{cases} \quad (16)$$

Then, we take the maximum probability to obtain labels r_1, r_2, r_3 , forming a 3-ary relational fact (r_1, A, r_2, B, r_3, C) and filter it out if there are null-label in (r_1, r_2, r_3) .

For *hypergraph-based schema* ($n_r = 1$), we combine the predicted probabilities of one label \mathbf{P}_1 in 6 orders to (A, B, C) order as follows:

$$\begin{cases} \mathbf{P}_1 = \mathbf{P}_1^{(ABC)} + \mathbf{P}_1^{(BAC)} + \mathbf{P}_1^{(ACB)} \\ \quad + \mathbf{P}_1^{(BCA)} + \mathbf{P}_1^{(CAB)} + \mathbf{P}_1^{(CBA)}. \end{cases} \quad (17)$$

Then, we take the maximum probability to obtain labels r_1 , forming a 3-ary relational fact (r_1, A, B, C) and filter it out if r_1 is null-label.

C Construction of Dataset

Based on the original *hyper-relational schema* on HyperRED dataset (Chia et al., 2022), we construct other three schemas (event-based, role-based, and hypergraph-based) for fine-grained n-ary RE. Firstly, we view the main relation in the *hyper-relational schema* as the event type in the *event-based schema*, combine the head entity and tail entity with two extra head key and tail key to convert them into two key-value pairs, and remain the auxiliary key-value pairs in the *hyper-relational schema*. Taking ‘Einstein received his Doctorate degree in Physics from the University of Zurich.’ as an example, it can be represented as (Einstein, educated, University of Zurich, {academic_major, Physics}, {academic_degree, Doctorate}) in the *hyper-relational schema* and (education, {trigger, received}, {person, Einstein}, {college, University of Zurich}, {academic_major, Physics}, {academic_degree, Doctorate}) in the *event-based schema*. Secondly, we remove the event type in the *event-based schema* to obtain the *role-based schema*. Thirdly, we remove all the keys in key-value pairs and remain the relation to build the *hypergraph-based schema*.

D Baseline Settings

Firstly, for the original *hyper-relational schema* of HyperRED, we adopted the same baselines as in the CubeRE paper (Chia et al., 2022) to compare with Text2NKG:

Generative Baseline: Generative Baseline uses BART (Lewis et al., 2020), a sequence-to-sequence model, to transform input sentences into a structured text sequence.

Pipeline Baseline: Pipeline Baseline uses UniRE (Wang et al., 2021b) to extract relation triplets in the first stage and a span extraction model based on BERT-Tagger (Devlin et al., 2019) to extract value entities and corresponding qualifier labels in the second stage.

CubeRE: CubeRE (Chia et al., 2022) is the only hyper-relational extraction model that uses a cube-filling model inspired by table-filling approaches and explicitly considers the interaction between relation triplets and qualifiers.

Secondly, for the *event-based schema*, *role-based schema*, and *hypergraph-based schema*, we added the following baselines to further validate the effect of Text2NKG on the fine-grained N-ary relation fact extraction task in the HyperRED dataset:

Text2Event: Text2Event (Chia et al., 2022) is a classic model in the Event extraction domain. However, it is not applicable to extractions of the *hyper-relational schema*. For the *role-based schema* extraction, we retained the key without referring to the main relation, while for the *hypergraph-based schema* extraction, we retained the main relation without referring to the key to get the final result for comparison.

UIE / LasUIE: UIE (Lu et al., 2022) and LasUIE (Fei et al., 2022) are unified information extraction models that can handle most tasks like NER, RE, EE, etc. However, they are still only suitable for event extraction in the multi-relational extraction domain and are not applicable to extractions of the *hyper-relational schema*. Therefore, we adopted the same approach as with Text2Event to compare with Text2NKG.

Thirdly, under the impact of the wave of large-scale language models brought about by ChatGPT on traditional natural language processing tasks, we added unsupervised large models as baselines to compare with Text2NKG in the n-ary RE tasks of the four schemas.

ChatGPT / GPT4: Using different prompts, we tested the latest state-of-the-art large-scale pre-trained language models ChatGPT (Wei et al., 2023) and GPT-4 (OpenAI, 2023) in an unsupervised manner, evaluating their performance on the extraction of the four schemas.

E Hyperparameter Settings

We use the grid search method to select the optimal hyperparameter settings for both Text2NKG with Bert-base and Bert-large. We use the same hyperparameter settings in Text2NKG with different encoders. The hyperparameters that we can adjust and the possible values of the hyperparameters are first determined according to the structure of our model in Table 4. Afterward, the optimal hyperparameters are shown in **bold**.

Hyperparameter	HyperRED
α	{1.0, 0.1, 0.01 , 0.001}
Train_batch_size	{2, 4, 8 , 16}
Eval_batch_size	{ 1 }
Learning rate	{ $1e-5$, 2e-5 , $5e-5$ }
Max_sequence_length	{128, 256 , 512, 1024}
Weight decay	{ 0.0 , 0.1, 0.2, 0.3}

Table 4: Hyperparameter Selection.

F Model Training Details

We train 10 epochs on HyperRED with the optimal combination of hyperparameters. Text2NKG and all its variants have been trained on a single NVIDIA A100 GPU. Using our optimal hyperparameter settings, the time required to complete the training on HyperRED is 4h with BERT-base encoder and 10h with BERT-large encoder.

G Further Discussions

G.1 How does ChatGPT perform in Fine-grained N-ary RE tasks?

We have tried to use LLM APIs such as ChatGPT and GPT to do similar n-ary RE tasks, i.e., prompting model input and output formats for extraction. The advantage of ChatGPT is that it can perform similar tasks in a few-shot situation, however, for building high-quality knowledge graphs, the performance and the fineness of the n-ary RE are much lower than Text2NKG. This is because ChatGPT is not good at multi-label classification tasks that contain less semantic interpretation. When the number of labels of relations in our relation collection is very large, we need to write a very long prompt to tell the LLM about our label candidate collection, which again leads to the problem of forgetting. Therefore, we have tried numerous prompt templates to enhance the extraction effect of ChatGPT, however, on fine-grained n-ary RE task, the best result of ChatGPT can only reach about 10% of F_1 value on HyperRED, which is much lower than the result of 80%+ F_1 value of Text2NKG.

However, advanced LLMs such as ChatGPT are a good idea for training dataset generation for Text2NKG in such tasks to save some manual labor to only verify and correct the training items generated. For future work, we will continue our research in this direction and try to combine large language models with Text2NKG-like supervised models for automated fine-grained n-ary RE for n-ary relational knowledge graph construction.

G.2 Why first Extracting 3-ary facts and then Merging them into N-ary Facts ?

We use output merging to address the dynamic changes in the number of elements in n-ary relational facts. The atomic unit of an n-ary fact includes a 3-ary fact with three entities. For instance, in the hyper-relational fact (*Einstein, educated_at, University of Zurich, degree: Doctorate degree, major: Physics*), the Text2NKG algorithm allows

us to extract two 3-ary atomic facts: (*Einstein, educated_at, University of Zurich, degree: Doctorate degree*) and (*Einstein, educated_at, University of Zurich, major: Physics*). These are then merged based on the same primary triple (*Einstein, educated_at, University of Zurich*) to form a 4-ary fact. The same principle applies to facts of higher arities.

As another example demonstrating the problem with merging binary relations: consider the statement "*Einstein received his Bachelor's degree in Mathematics and his Doctorate degree in Physics.*" When represented as binary relations, the facts become (*Einstein, degree, Doctorate degree*), (*Einstein, major, Physics*), (*Einstein, degree, Bachelor*), and (*Einstein, major, Mathematics*). With this representation, we cannot merge these binary relation facts effectively because there's no way to determine whether *Einstein's doctoral major* was *Physics* or *Mathematics*. This necessitates the use of NKG's n-ary relationship facts to represent this information, as seen in (*Einstein, degree, Doctorate degree, major, Physics*).

Therefore, using binary facts, we can't merge them into n-ary facts based on shared elements within these facts. On the other hand, using facts with four entities or more makes it challenging to effectively extract 3-ary atomic facts.

In Section 5.6 and Figure 4(d), we also analyzed the effects and detailed insights of unsupervised extraction of arbitrary-arity facts.

G.3 How Text2NKG can address Long Contexts with Relations spread across Various Sentences ?

As long as the text to be extracted is a lengthy piece with entities annotated, it can undergo long-form n-ary relation extraction. The maximum text segment size for our proposed method depends on the maximum text length that a transformer-based encoder can accept, such as Bert-base and Bert-large, which have a maximum limit of 512. To extract from larger documents, we simply need to switch to encoders with larger context length, which all serve as the encoder portion of Text2NKG and are entirely decoupled from the n-ary relation extraction technique we propose. This is one of the advantages of Text2NKG. Its primary focus is to address the order and combination issues of multi-ary relationships. We can seamlessly combine a transformer encoder that supports long texts with Span-tuple Multi-label Classification to process n-ary relation extraction in long chapters.