### **Combination Generalization of Capability-Specific Neurons in LLMs**

#### **Anonymous ACL submission**

#### Abstract

Although large-scale language models (LLMs) 001 exhibit various exciting capabilities, understanding the mechanisms behind these abilities 004 remains a challenging problem. In this paper, we aim to understand these mechanisms from the perspective of neurons. Specifically, we 007 first propose a Detecting Capability-Specific Neurons (DCSN) method. Extensive enhance-009 ment and erasure experiments demonstrate that the detected neurons are highly correlated with 011 these capabilities, exhibiting strong cohesion and separability, which we define as capability-013 specific neurons. Moreover, leveraging these neurons, we conducted compositional experi-015 ments and, for the first time, discovered that capability neurons exhibit compositional gen-017 eralization. Inspired by these findings, we propose a Capability Neuron-Level Fine-tuning method (CNLF) that fine-tunes specific capa-019 bility neurons to achieve performance improvements across datasets and tasks. Extensive experiments validate the effectiveness of this method and provide a low-cost, highly generalizable fine-tuning paradigm. Our research offers interpretable insights into the capability mechanisms of LLMs.

#### 1 Introduction

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Large-scale language models (LLMs) have demonstrated remarkable performance improvements across various natural language processing tasks (Zhao et al., 2023). Despite their powerful capabilities, the underlying principles of the mechanisms driving these capabilities(Yan et al., 2024; Haltaufderheide and Ranisch, 2024), as well as the relationship between model parameters and performance, remain unclear to humans(Peng et al., 2024). Recently, many studies have attempted to further understand and enhance the capabilities of these models, but their efforts have been hindered by the black-box nature of LLMs(Bonaldi et al., 2024; Sun et al., 2024). Therefore, understanding the internal mechanisms and characteristics of these models is key to improving their capabilities and interpretability(Ding et al., 2023). 042

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Previous studies have attempted to establish a correspondence between knowledge or tasks and model parameters, defining these parameters as knowledge neurons or task neurons(Yao et al., 2024). However, the assumption of associating knowledge or tasks with specific neurons has been questioned in existing research(Dai et al., 2021). Studies have found a high degree of overlap among different knowledge neurons, which does not align with the expected localization of parameters(Huang et al., 2025b). Furthermore, the functions of these overlapping neurons remain unexplained(Huang et al., 2025a). Similar issues of inexplicability also exist with task neurons(Leng and Xiong, 2025).

Previous research has found that a model's capabilities can transcend knowledge and tasks, providing a potential explanation for overlapping neurons(Huang et al., 2025b). Achieving parameter localization of capabilities is key to interpretability research for LLMs(Trimmer, 2015). Inspired by these studies, we attempt to pose three questions: (1) Do neurons related to specific capabilities exist in LLMs? (2) Do capability neurons exhibit compositional generalization? (3) Can we improve LLMs through these neurons?

To address the three questions above, we conducted an analysis of capability neurons in LLMs. First, we constructed a compositional generalization dataset encompassing four computational capabilities: addition, subtraction, multiplication, and division. We then proposed a Detecting Capability-Specific Neurons (DCSN) method. Next, we performed enhancement and erasure experiments, demonstrating that these neurons are highly correlated with the respective capabilities. Our experiments show that different capability neurons exhibit a low overlap rate (Separation), while neurons identified utilizing different datasets that demon-

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strate the same capability exhibit a high overlap rate (Cohesion) (MacQueen, 1967). Therefore, we refer to these as capability-specific neurons.

Utilizing the identified capability-specific neurons, we delved the mechanism of capability invocation within the model. When performing tasks, the model often invokes multiple capabilities. To reflect this phenomenon, we constructed compositional problems within the compositional generalization dataset. For example, the problem "1 + 3 \*5 = ?" requires both addition and multiplication capabilities from the model. We collected neuron activation data during the model's execution of such tasks. Interestingly, the addition-specific neurons and multiplication-specific neurons were significantly activated. We then conducted extensive experiments across various problem types (involving different operations). The results demonstrated that capability-specific neurons exhibit compositional generalization, marking the first time the mechanism of capability invocation within the model has been revealed. Counterintuitively, we observed that when addition neurons were activated, subtraction neurons were activated 22% more than other neurons (e.g., for multiplication or division). This suggests a certain degree of association between addition and subtraction. Through ablation experiments, we inferred that this is likely due to the inverse relationship between addition and subtraction.

To enhance the model's various capabilities, we proposed a Capability Neuron-Level Finetuning method (CNLF). By fine-tuning these designated capability-specific neurons, we improved the model's abilities and achieved superior performance across 12 downstream tasks. Compared to fine-tuning all parameters, this method improved performance by **18.9%** on unseen datasets. Additionally, we were able to control the model's individual capabilities, thereby enhancing the model's safety and controllability.

To the best of our knowledge, we are the first to discover that the model's capability-specific neurons possess compositional generalization. We also proposed a low-cost, highly generalizable finetuning method that enables control over the model's capabilities. This work sheds light on the internal mechanism of capability invocation within the model and enhances its interpretability. Our contributions can be summarized as follows:

• We proposed a Detecting Capability-Specific

Neurons (DCSN) method. and successfully identified capability-specific neurons. Compared to previously studied knowledge neurons and task neurons, capability-specific neurons demonstrate superior separability and cohesion.

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- To clarify the mechanism of capability invocation within the model, we conducted compositional generalization experiments and discovered that capability-specific neurons exhibit compositional generalization. This provides important insights for understanding and enhancing the model's multiple capabilities.
- We introduced a Capability Neuron-Level Fine-tuning method (CNLF), which simultaneously improves multiple capabilities of the model and achieves significant performance gains. Extensive experiments have demonstrated the effectiveness of the method.

#### 2 Related Work

**Parameter Localization.** Knowledge Neurons indicate that knowledge (such as triplets) can be localized in parameters, with storage forms including distributed parameters(Liu et al., 2024b), parameter layers(Meng et al., 2022b), and parameter chains (Yao et al., 2024). Task Neurons indicate that different tasks can be localized and utilize Capability Neurons for task generalization(Leng and Xiong, 2025). Capability Neurons Localization points out that knowledge cannot be localized, with unexplainability, but capabilities can be localized, with unexplainability, but capabilities can be localized.

**Localization Method** Distributed Parameters: Knowledge-sensitive neurons are detected using a gradient attribution method, and after sorting, the Top-K neurons are selected and considered as knowledge neurons(Huang et al., 2024). Parameter Layers: Similar to the causal tracing (Meng et al., 2022b), a clean run that predicts the fact, a corrupted run where the prediction is damaged, and a corrupted-with-restoration run that tests the capability of a single state to restore the prediction(Huang et al., 2025a). Parameter Chains: KC (Yao et al., 2024) believes that individual knowledge is stored on a parameter chain and utilizes the entire parameter chain to recall knowledge.

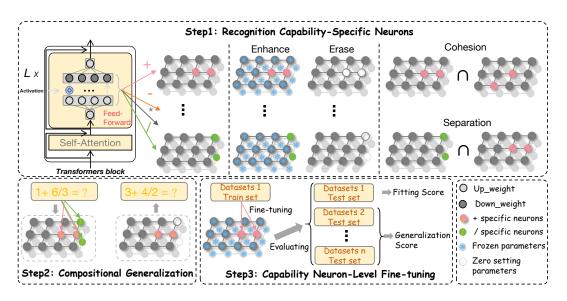


Fig. 1: Illustration of our research methodology. The entire framework consists of three steps: Recognition Capability-Specific Neurons, Compositional Generalization and Capability Neuron-Level Fine-tuning. Step 1 provides identification methods for subsequent research, Step 2 provides interpretability of capability mechanisms for subsequent research, and provides justification for multi-capability enhancement in Step 3.

#### 3 Methodology

Figure 1 illustrates our research approach. First, we proposed a capability neuron detection algorithm and successfully identified capability-specific neurons, which exhibit strong separability and cohesion. Next, we conducted capability compositional generalization experiments and uncovered the mechanism of capability invocation within the model. Finally, based on capability-specific neurons, we proposed a fine-tuning method at the capability neuron level aimed at enhancing multiple capabilities of the model.

#### 3.1 Construction of Compositional Generalization Dataset

To identify neurons that are highly correlated with specific capabilities utilizing data, it is first necessary to clarify the relationship between capabilities and data(Hinterstoisser et al., 2011). Capabilities reflect the model's proficiency in solving certain problems, they are transferable across datasets, tasks, and even languages. Our compositional generalization dataset consists of two parts: the neuron identification part and the compositional generalization part.

Neuron Identification Part. This part helps
identify the capability-specific neurons within the
model. First, we selected four basic arithmetic
operators—"+", "-", "\*", and "/", which reflect different computational capabilities. To achieve a

cross-task setup, our data includes three types of tasks: Multiple-choice (MQ) tasks, True/False (TF) tasks, and Direct Generation (DG) tasks. Additionally, to meet the cross-language requirement, we utilized Deepseek V3's (Liu et al., 2024a) translation capabilities to provide data in both English and Chinese. The specific data formats are shown in Table 1. 209

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**Combination Generalization Part.** This dataset helps clarify the capability invocation mechanism within the model. The dataset includes five different types of expressions. For example, 2-operator expressions (e.g., 1+3\*5), which involve two different operators. Interestingly, to explore the impact of repeatedly occurring operators on neuron activation levels, we designed a 5-operator expression, such as (1+3\*5-6/3+5), where the "+" operator appears twice. The specific data formats are shown in Table 1.

# 3.2 Recognition capability-specific neurons in LLM

To identify capability-specific neurons, it is necessary to determine the correlation between each neuron and a specific capability. Previous studies have focused on locating neurons responsible for individual pieces of knowledge (Meng et al., 2022a) or tasks (Leng and Xiong, 2025). Inspired by these works, we propose a Detecting Capability-Specific Neurons (DCSN) method, which utilizes

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Multi-operation expression	$< + > - < + \cap * > < + \cap $ < 1-OP: 1 + 6 = ?>; < 2-OP: 1 + 3*5 = ?>; , < 5-OP: 1 + 3*5 = ?>; , < 5-O	- ∩ * ∩ \ > 3*5 - 6/3+5=? >
Category	Component Prompt	Target Answer
DG	Based on the given expression "1+3*5=?", please provide the answer directly:	16
MQ	Based on the given expression "1+3*5=?", the following options are provided: (a) 10, (b) 0, (c) 16, and (d) 26. Please select the correct option:	c
TF	Based on the given expression "1+3*5=16", please determine whether it is correct:	Yes

Table 1: Example of combining generalized datasets. The categories are: Directly Generated(DG), Multiple-choice Questions(MQ), and True/False questions(TF). The target answer are "16", "c" and "Yes", respectively. *i*-OP indicates that the operation expression contains *i* types of operations.

the contribution of each neuron to a capability as a relevance score. Notably, current LLMs are based on the autoregressive transformer architecture, which consists of Multi-Head Self-Attention (MHSA) and feed-forward networks (FFNs) (Touvron et al., 2023). Previous research has demonstrated that FFNs can store a large amount of parametric knowledge(Dai et al., 2021). Our experiments focus solely on this component.

For identifying neuronal samples  $S = [s_1, s_2, ..., s_j]$ , we compute correlation score for each neuron  $n_i$  at layer l as:

$$C(i, l, t, S) = \frac{1}{n} \sum_{j=0}^{n} A_{i,-1}^{l,j} \cdot (W_{un} W_{ud}^{l})_{t,i}$$
(1)

where  $(\cdot)_{t,i}$  represents the *t*-th row and *i*-th column of the input matrix, and  $A_{i,-1}^{l,j}$  is the activation output at the last token for neuron  $n_i$  at layer *l* of sample  $s_j$ . The  $W_{un}$  is the unembedding matrix, and  $W_{ud}^l$  is the up or down weight of the forward feedback network at layer *l*.

Here we regard  $W_{un}W_{ud}^l \in \mathbb{R}^{v \times d_m}$  as a projection function projecting from activations of the neurons to distribution of the vocabulary, where *v* is the vocabulary and  $d_m$  is the intermediate, and regard  $A_{i,-1}^l$  as a coefficient of the projection, respectively. This projection clearly displays the average contribution level of each neuron to all samples.

To identify the capability-specific neurons, we take the *Mask* matrix:

$$Mask_{i,l} = \begin{cases} 1 & |C - mean(C)| > \sigma \cdot var(C) \\ 0 & else \end{cases}$$
(2)

where  $mean(\cdot)$  denotes the mean value of all scores and  $var(\cdot)$  indicates the variance of the neurons.  $\sigma$ is the threshold guiding us to find the task neurons. According to statistical principles (Kumar et al., 2007), in the absence of any special instructions to follow, we view the neurons with scores outside  $\sigma = 6$  as capability-specific neurons. We also provide experimental results for other  $\sigma$  values in the Appendix B.

#### 3.3 Compositional Generalization Experiment

Once it is confirmed that capability-specific neurons truly exist, we analyze how the model invokes various capabilities when solving problems. First, we design a forward reasoning experiment to observe whether the corresponding neurons are successfully activated when the model solves multi-operation expression problems. Additionally, in the reverse validation experiment, we erase certain capability-specific neurons in advance to evaluate the model's performance on multi-operation expression problems. Through this process, we aim to clarify the model's internal mechanism for utilizing capabilities, thereby revealing the relationship between capability-specific neurons and model performance.

**Forward Reasoning Experiment.** We utilize the compositional generalization dataset introduced in Section 3.1 to have the model solve multi-operation expression problems. By analyzing the activation states of neurons in the model, we determine whether capability-specific neurons exhibit compositional generalization. Specifically, we examine whether the activated neurons include the identified capability-specific neurons and whether these

Enhancement			LLaN	la-2-7B				GPT	-J-6B	
Emiancement	+	-	*	/	Avg. (^)	+	-	*	/	Avg. (†)
Original	52.4	50.3	45.2	43.6	47.8	50.7	50.1	45.2	40.3	46.5
FT-Random	52.7	51.0	45.7	43.9	48.3	50.9	50.7	45.3	40.5	46.8
FT-w/o Cap	56.7	55.6	50.6	48.3	52.8	56.3	56.2	49.3	47.6	52.3
FT-Cap (Ours)	67.8	68.3	66.1	65.7	<b>66.9</b> († 14.1)	66.4	67.4	65.4	65.3	<b>66.1</b> († 13.8)
Erasure			LLaN	la-3-8B	5			LLaM	a-3-13I	3
LIASUIE	+	-	*	/	Avg. (↓)	+	-	*	/	Avg. (↓)
Original	56.4	55.3	48.4	48.6	52.1	$\overline{58.6}$	57.4	$\bar{50.1}$	51.7	54.4
Deactivate-Random	56.3	55.0	48.4	48.5	52.0	58.5	57.3	49.8	53.1	54.6
Deactivate-Cap (Ours)	32.5	31.5	30.4	30.8	<b>31.3</b> (↓ <b>20.7</b> )	34.6	32.7	31.6	32.7	<b>32.9</b> (↓ <b>2</b> 1.7)

Table 2: Results of enhancement and erasure experiments. FT-Random refers to fine-tuning an equal amount of random parameters (0.05% of parameters), FT-w/o Cap refers to fine-tuning all parameters except for the specified capability-specific neurons (99.95% of parameters), and FT-Cap refers to fine-tuning the specified capability-specific neurons (0.05% of parameters). The experiment only disabled 10% of ability specific neurons.

neurons correspond to the operators in the multioperation expressions. This experiment aims to verify whether specific neurons demonstrate compositional generalization properties.

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Reverse Validation Experiment. We erase certain capability-specific neurons in advance to observe their impact on the corresponding model capabilities. For example, we set addition-specific neurons to zero and then have the model answer multiple questions containing addition operators, measuring the change in accuracy before and after the erasure. Furthermore, we erase multiple capability-specific neurons simultaneously to examine the resulting accuracy changes in related problems. This step aims to validate the authentic-315 ity of the compositional generalization properties of capability-specific neurons.

#### 3.4 **Enhancing Multiple Capabilities of LLMs Utilizing Capability-Specific Neurons**

Through the analysis of capability-specific neurons, we found that these neurons exhibit compositional generalization. This discovery reveals the mechanism by which the model invokes its capabilities and establishes a correspondence between capability-specific neurons and model performance. However, enhancing the model's performance remains a challenge. We propose a Capability Neuron-Level Fine-tuning method (CNLF), aiming to leverage the detected neurons to further improve the model's performance.

First, given a set of training samples D, we finetune only the corresponding capability-specific neurons during the fine-tuning phase while freezing all other parameters. During the testing phase, inference proceeds as usual. We refer to this approach as Capability Neuron-Level Fine-tuning method. Specifically, existing open-source datasets do not solely focus on a single capability. For instance, the dataset meta math (Yu et al., 2023) reflects both the model's mathematical and language capabilities, which poses challenges in selecting which neurons to fine-tune. Fortunately, we have already confirmed the existence of compositional generalization in capabilities. The model's performance on *meta\_math* is primarily related to its mathematical and language capabilities. Therefore, we choose to fine-tune both the mathematics and language capability-specific neurons simultaneously. Experimental results validate the effectiveness of this method.

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#### **Experiments: Recognition** 4 **Capability-Specific Neurons**

In this section, we first utillized neuron DCSN in Section 3.2 to detect capability-specific neurons, and designed enhancement and erasure experiments to verify the high correlation between these neurons and capabilities. Finally, we constructed dissociation and cohesion indicators to determine the true existence of capability-specific neurons.

#### 4.1 Experimental Setup

The first experiment is an enhancement experiment, in which we fine tune the ability specific neurons. Specifically, only ability specific neurons are updated, while other parameters in the model are frozen. The second experiment is an inhibition test. During the inference phase, we set the ability specific neurons to zero while keeping other parameters unchanged.

Cohesiveness		Ι	LaMa-2	2-7B				GPT-J-	6B	
Concervencess	+	-	*	/	Avg. (†)	+	-	*	/	Avg. (†)
DG	95.47	93.73	92.96	94.35	94.19	95.63	93.78	93.86	94.25	94.35
TF	94.63	93.47	94.54	94.32	94.26	93.59	93.70	94.23	92.41	93.42
MQ	95.38	93.24	93.57	94.66	94.13	93.45	93.68	94.39	93.34	93.62
СН	84.11	81.63	82.77	83.32	82.97	83.54	80.55	80.76	81.62	81.59
Separability		L	LaMA-	3-8B			L	LaMA-3	-13B	
Separability	+ ∩ -	$+ \cap *$	$+ \cap /$	*∩/	Avg. (↓)	+ ∩ -	$+ \cap *$	$+ \cap /$	*∩/	Avg. (
DG	6.46	3.26	2.63	2.31	3.65	5.76	4.61	4.33	4.22	4.73
MQ	6.22	4.77	4.16	3.89	4.73	5.84	5.52	4.36	4.03	4.9
TF	5.73	5.05	4.53	4.06	4.82	5.65	5.08	4.51	3.76	4.7
CH	5.88	4.48	4.08	3.65	4.57	4.89	4.43	4.07	3.69	4.22
EN	6.38	5.47	4.33	3.45	4.84	5.79	5.66	4.35	3.57	4.76

Table 3: The results of cohesiveness and separability experiments. EN refers to all English datasets, while CH refers to translating all English into Chinese datasets.

We tested three publicly available models of different sizes, including Llama-2-7B (Touvron et al., 2023), Llama-3-8B,Llama-3-13B and GPT-J-6B(Wang and Komatsuzaki, 2021). The proportion of ability specific neurons in the total parameters is 0.05%. The datasets is neuron identification part in Section 3.1.

#### 4.2 Results

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Table 2 presents the results of the enhancement experiments. Compared to fine-tuning an equivalent number of random parameters, fine-tuning capability-specific neurons achieves significant performance improvements. Specifically, despite finetuning only 0.05% of the parameters, fine-tuning capability-specific neurons results in a 19.9% performance improvement. In comparison to "FTw/o Capability," the performance improvement is 14.1%. Notably, "FT-w/o Capability" refers to finetuning all parameters except the capability-specific neurons, which accounts for 99.95% of the total parameters, yet only achieves a mere 4.5% performance improvement. This demonstrates that the identified neurons are highly correlated with the model's capabilities.

Table 2 also provides the results of the erasure experiments. By zeroing out certain neurons and observing the performance drop, the more significant the drop, the more sensitive the erased neurons are to the capability. Despite disabling only 10% of the capability-specific neurons, the model experiences a 21.7% performance drop. When disabling an equivalent number of random parameters (0.05%), the model's performance drops by only 0.1%. This further highlights that the identified neurons are highly sensitive to the model's capabilities.

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Meanwhile, previous studies lacked metrics to evaluate the accuracy of neuron identification. Inspired by clustering analysis(MacQueen, 1967), capability-specific neurons for different capabilities should exhibit high distinctiveness (e.g.  $n_+$ and  $n_-$ ). The greater the distinctiveness, the higher the identification accuracy. We define this metric as separability *Sep*. Additionally, neurons identified for the same capability (utilizing different datasets, e.g., English  $n_{EN}$  and Chinese  $n_{CH}$ ) should exhibit high similarity. The greater the similarity, the stronger the identification reliability. We define this metric as cohesiveness *Coh*. Formally, these metrics can be expressed as:

$$Sep(+ \cap -) = n_{+} \cap n_{-}$$

$$Coh(+) = n_{CH} \cap n_{EN}$$
(3)

Table 3 presents the results of cohesiveness and separability. In previous studies, the cohesiveness of KN was only 37.3%, while the separability of ROME reached as high as 86.6%, making the identified neurons unconvincing (Huang et al., 2025b). Even under interference from multiple question types and multilingual data, the capability-specific neurons identified in our study achieve a cohesiveness of **94.3%** and a separability of only **3.6%**. This demonstrates that the identified capability-specific neurons are both reliable and accurate.

In summary, compared to random parameters and "w/o Capability," enhancing and suppressing capability-specific neurons significantly impacts model performance. The results of cohesiveness

Activate			LLaM	[A-2-7B				GPT	Г-Ј-6В	
Activate	2-op	3-op	4-op	5-op	Avg.(↑)	2-op	3-op	4-op	5-op	Avg. (†)
DG	94.37	89.67	87.43	86.66	89.53	90.63	87.64	84.13	83.22	86.41
MQ	91.22	86.42	82.67	82.64	85.73	89.76	86.42	82.37	82.66	85.30
TF	90.37	87.45	83.64	83.37	86.21	89.73	87.64	82.66	82.47	85.63
СН	89.67	85.43	81.09	80.43	84.16	90.13	86.57	82.93	82.86	85.62
EN	90.17	86.59	82.19	81.93	85.22	89.30	85.71	81.05	80.54	84.15
Deactivate			LLaM	[A-3-8B				LLaM	A-3-13B	
Deacuvate	2-op	3-op	4-op	5-op	Avg.(↓)	2-op	3-op	4-op	5-op	Avg. (↓)
Original	60.25	56.47	54.29	54.17	56.29	66.54	63.41	60.37	59.29	62.40
Deactivate-Random	60.27	56.21	54.20	53.07	55.93	66.34	63.20	60.35	59.28	62.29
Ours	32.07	30.49	27.31	27.78	<b>29.41</b> (↓ <b>26.88</b> )	34.22	31.72	28.57	27.43	<b>30.48</b> (↓ <b>29.92</b> )

Table 4: The experimental results of forward reasoning and reverse verification.

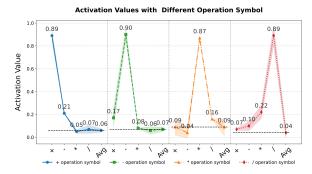


Fig. 2: The activation values corresponding to different operation symbols, and different colors refer to different operators in 1-OP.

and separability further demonstrate the high accuracy of neuron identification. Therefore, we conclude that capability-specific neurons do indeed exist in LLMs.

#### 5 Experiments: Combination Generalization

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We analyzed ability specific neurons to understand the ability calling mechanism of the model. According to the analysis method in Section 3.3, we have listed the relevant results of combination generalization experiments.

#### 5.1 Forward reasoning experiment

**Experimental setup.** The experimental data  $D = [d_1, d_2, ..., d_r]$  is the combined generalization part in Section 3.1. Utilizing Equation 2, we identified activated neurons and compared them with the four ability specific neurons obtained in Section 4, utilizing the coincidence ratio as the evaluation metric. Specifically, when the experimental data is a 2-operation expression (e.g. "1+3 \* 5"), we calculate the ratio *R* of activated neurons  $n_{act}$  containing +- specific neurons  $n_+$  and \*-specific neurons  $n_*$  as the evaluation metric. Formalized as follows:

$$R(+\&*) = \frac{1}{r} \sum_{i=0}^{r} \left(\frac{n_{(+|act)}^{i}}{n_{+}^{i}} + \frac{n_{(*|act)}^{i}}{n_{*}^{i}}\right) \quad (4)$$

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where  $n_{(+|act)}^{i}$  refers to activated {+}-specific neurons,  $n_{+}^{i}$  refers to all {+}-specific neurons.

**Results.** Table 4 presents the activation rates of various arithmetic expressions. The results show that, on average, 89.53% of the capability-specific neurons are activated when the model processes multi-operation expressions. The activation rates for 4-OP and 5-OP are similar, indicating that the presence of two identical operators in an expression does not significantly increase the activation rate of the corresponding capability-specific neurons. Figure 2 further illustrates the activation values of neurons when processing different arithmetic expressions. Counterintuitively, when an expression contains only the "+" operator, the activation value for "-" is also significantly higher than the average. A similar issue is observed with "\*" and "/". This contradicts our intuition, as under normal circumstances, when an arithmetic expression does not contain "-", the activation value for "-" should be close to the average. We analyzed the underlying reason for this phenomenon, which might be related to the fact that addition and subtraction are inverse operations. To investigate further, we conducted ablation experiments.

Ablation Experiment. In Table 6, such as in arithmetic expressions where only addition is present, the performance drops significantly by 6.3% when subtraction is removed compared to multiplication and division. This indicates a certain correlation between addition and subtraction,

Math		LLaMA	-3-8B/GSM8K(↑	)		LLa	MA-3-13B/GSM	<b>8K</b> (↑)
Iviatii	GSM8K	Meta_Math	SVAMP	AMC	GSM8K	Meta_Math	SVAMP	AMC
Original	24.32	26.73	43.67	32.17	26.15	27.39	45.73	33.67
FT-Random	25.31	25.43	43.39	31.74	27.33	27.41	45.73	33.59
O-LoRA	38.94	27.33	44.63	35.97	41.32	29.45	47.12	34.63
FT-All	43.07	28.53	45.32	35.67	43.89	29.63	47.82	35.87
Ours	37.42	<b>36.73</b> († 8.20 )	<b>57.92</b> († 12.20)	<b>47.63</b> († 11.96)	41.23	<b>36.47</b> († 6.84 )	<b>58.63</b> († 10.81)	<b>51.76</b> († 15.89)

Table 5: Experimental results on ability enhancement and generalization. Fine-tuning the GSM8K training set and evaluate the fitting and generalization ability on GSM8K and three other datasets.

Erase		LLaMa	- <b>3-8B(</b> ↓)	
LIASC	+	-	*	١
1-OP (+)	↓ 23.9	↓ 6.3	↓ 0.1	$\downarrow 0.2$
1-OP (-)	↓ 5.7	↓ 23.8	$\downarrow 0.0$	$\downarrow 0.1$
1-OP (*)	$\downarrow 0.0$	↓ 0.3	↓ 18.0	↓ 6.0
1-OP (/)	$\downarrow 0.4$	$\downarrow 0.1$	↓ 5.3	↓ <b>17.8</b>

Table 6: The results of the ablation experiment. 1-OP (+) refers to the presence of + in 1-OP. The value refers to the magnitude of the performance decline with zero capability-specific neurons.  $\downarrow$  represents the influence between neurons that perform inverse operations on each other.

which is related to their nature as inverse operations, thus verifying our analysis.

#### 5.2 Reverse Verification Experiment

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**Experimental Setup.** We sequentially ablate the capability-specific neurons corresponding to operators in expressions to observe their impact on final performance. For 2-OP, we only remove a single capability neuron, whereas for 3-OP and 4-OP, we remove multiple capability neurons. This further verifies the authenticity of capability compositional generalization.

**Results.** In Table 4, for 2-OP, removing the corresponding capability-specific neuron significantly 502 reduces the model's performance by 28.18%. No-503 tably, for 3-OP and 4-OP, we intuitively observe 504 that as more corresponding capability-specific neu-505 rons are removed, the performance degradation becomes more pronounced. However, when re-507 508 moving an equivalent number of parameters, the performance drop is minimal. 509

In conclusion, we have gained an understanding of the model's capability invocation mechanism during forward inference and believe that the model exhibits compositional generalization of capabilities.

#### 6 Experiment: Enhancing Multiple Capabilities of LLMs

To fully leverage capability-specific neurons, we propose a fine-tuning method at the capabilityspecific neuron level. 515

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#### 6.1 Evaluation indicators

To evaluate the fitting and generalization capabilities of neurons, we designed two evaluation metrics: the fitting score on the test set, and the generalization score obtained by training on the current dataset and testing on other datasets.

#### 6.2 Experimental Setup

We have provided more details in Appendix A.

#### 6.3 Results

Table 5 shows that by fine-tuning only 0.05% of the parameters, we can achieve fitting scores comparable to FT-All and O-LoRA, with a score 2.63% lower than FT-All. Meanwhile, our generalization scores are **15.89%** higher than FT-All. Compared to fine-tuning the same number of random parameters, our performance has improved by 18.17%. The experimental results demonstrate that we provide a cost-effective fine-tuning approach and exhibit significant generalization capabilities on other datasets.

#### 7 Conclusion

In this study, we propose a methodological research framework to understand the capability mechanisms of models from a neuronal perspective. First, we identified that capability-specific neurons are indeed present. Second, we gained an initial understanding of the internal capability invocation mechanisms within models. Finally, we introduced a low-cost, high-generalization finetuning paradigm that leverages capability-specific neurons to enhance various model capabilities. Importantly, this research framework promotes advancements in model interpretability studies. 553

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Limitations

guage models.

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petitions

Due to limitations in computing resources, we

did not conduct relevant experiments on larger lan-

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#### **A** Experimental Setup

#### A.1 Dataset and Neuron Detection

We collected datasets related to mathematics, programming, and language, and used the method described in Section 3.1 to identify mathspecific neurons, programming-specific neurons, and language-specific neurons. The relevant datasets include:

- Math: GSM8K (Cobbe et al., 2021) contains approximately 8,000 elementary math problems with detailed solutions. Meta Math (Yu et al., 2023) focused on meta-learning for math problems. MathQA(Luo and Pan, 2024), SVAMP(Naeem et al., 2014) and AMC (AMCs, 2013) datasets.
- Program: Code25K (Beguš, 2021) 25,000 contains around code snip-HumanEval(Zheng et al., 2023), pets. MBPP(Athiwaratkun et al., 2022), CodeXGLUE(Lu et al.. 2021) and APPS(Zheng et al., 2023).
- Language: Emotion (Kosti et al., 2019) with 760 text data labeled with various emotions. Imdb (Tripathi et al., 2020) contains movie reviews 762

763 764 765	and ratings. GoEmotions(Demszky et al., 2020), SemEval-2019 Task 3(Chatterjee et al., 2019) and TweetEval (Barbieri et al., 2020).
766 767	A.2 Baselines The baseline methods mainly include:
768 769	• FT-Random: Fine-tuning an equal amount of random parameters.
770 771	• O-LoRA (Wang et al., 2023) : learning tasks in different (low-rank) vector subspaces.
772 773	• FT-All(Hawthorne and Isaacs, 2018): Fine- tuning the entire model using training data.

### 774 B Experimental Results

		т	1 ) (	0 <b>7</b> D				ODT I		
Enhancement		L	LLaMa-	-2-7B				GPT-J	-6B	
Emancement	+	-	*	/	Avg. (†)	+	-	*	/	Avg. (†)
Original	52.4	50.3	45.2	43.6	47.8	50.7	50.1	45.2	40.3	46.5
FT-Random	52.7	51.0	45.7	43.9	48.3	50.9	50.7	45.3	40.5	46.8
FT-w/o Cap	56.7	55.6	50.6	48.3	52.8	56.3	56.2	49.3	47.6	52.3
FT-Cap (Ours)	67.4	68.0	65.1	63.1	62.1	65.1	66.4	64.3	64.2	62.5
Erasure		Ι	LaMa-	-3-8B			L	LaMa-	3-13B	
Erasure	+	-	*	/	Avg. (↓)	+	-	*	/	Avg. (
Original	56.4	55.3	48.4	48.6	52.1	58.6	57.4	50.1	51.7	54.4
Deactivate-Random	56.3	55.0	48.4	48.5	52.0	58.5	57.3	49.8	53.1	54.6
Deactivate-Cap (Ours)	34.6	33.7	32.2	31.7	32.7	36.1	34.0	32.5	33.7	33.1

Table 7: Results of enhancement and erasure experiments.  $\sigma = 3$ .

Math		LLaMA-2-7B/	GSM8K(†	)		GPT-J-6	B/GSM8K	(^)
Iviaui	GSM8K	Meta_Math	SVAMP	AMC	GSM8K	Meta_Math	SVAMP	AMC
Original	21.42	23.63	42.55	30.01	23.04	23.07	41.09	30.89
FT-Random	21.21	23.67	41.99	30.98	24.09	23.42	42.70	31.47
O-LoRA	35.09	24.37	40.36	31.09	37.42	26.37	45.09	30.82
FT-All	38.67	25.63	41.32	31.72	39.09	26.63	44.92	31.78
Ours	35.02	35.03	50.20	46.01	40.27	33.42	54.32	48.06

Table 8: Experimental results on ability enhancement and generalization. Fine-tuning the GSM8K training set and evaluate the fitting and generalization ability on GSM8K and three other datasets.

Drogram	L	LaMA-2-7B/C	ode25K(1	`)			GPT-J-6B	/Code25I	<b>Κ(</b> ↑)
Program	Code25K	HumanEval	MBPP	APPS		Code25K	HumanEval	MBPP	APPS
Original	23.51	27.99	43.51	35.42	-	43.03	24.07	36.08	32.82
FT-Random	24.32	28.09	41.99	36.98		43.29	24.52	37.74	33.04
O-LoRA	34.00	36.96	47.32	41.08		48.52	29.37	43.08	38.42
FT-All	39.47	37.02	48.53	42.29		49.89	29.98	44.62	38.87
Ours	35.74	45.37	58.23	49.73		55.73	38.92	56.42	49.83

Table 9: Experimental results on ability enhancement and generalization. Fine-tuning the Code25K training set and evaluate the fitting and generalization ability on Code25K and three other datasets.

Languaga		LLaM/	A-2-7B/Emotion	n(↑)		(	GPT-J-6B/Emot	ion(†)
Language	Emotion	Imdb	GoEmotions	TweetEval	Emotion	Imdb	GoEmotions	TweetEval
Original	67.42	57.43	66.78	57.43	60.14	53.01	51.92	52.82
FT-Random	68.22	58.72	67.42	58.99	62.43	54.32	53.71	54.42
O-LoRA	76.43	57.62	68.93	58.44	73.32	56.57	51.53	51.55
FT-All	79.85	58.66	68.79	58.79	75.08	53.32	52.42	53.78
Ours	77.47	66.70	77.90	67.09	73.06	69.43	63.17	65.07

Table 10: Experimental results on ability enhancement and generalization. Fine-tuning the Emotion training set and evaluate the fitting and generalization ability on Emotion and three other datasets.

Cohesiveness		I	LaMa-3	3-8B			L	LaMa-3	-13B	
Collesivelless	+	-	*	/	Avg. (^)	+	-	*	/	Avg. (^)
DG	94.32	92.97	93.67	93.35	93.29	94.62	93.64	93.56	94.37	93.35
TF	94.33	93.27	93.64	94.02	93.36	93.49	93.67	93.29	92.51	93.78
MQ	95.42	93.27	92.59	92.67	93.23	93.55	93.69	93.32	93.42	93.22
CH	83.61	82.91	83.74	85.42	83.27	84.24	81.54	82.46	81.55	82.79
Separability		L	LaMA-2	2-7B				GPT-J-	6 <b>B</b>	
Separability	+∩-	$+ \cap *$	$+ \cap /$	*∩/	Avg. (↓)	+∩-	$+ \cap *$	$+ \cap /$	*∩/	Avg. (
DG	5.64	4.27	3.93	2.51	3.45	5.66	4.31	4.00	3.78	4.23
MQ	5.32	4.65	4.23	3.79	4.03	5.88	5.42	4.74	4.12	4.98
TF	5.63	5.15	4.70	4.02	4.61	5.60	5.18	4.52	3.74	4.73
CH	5.76	4.40	4.12	3.75	4.24	5.78	4.52	4.01	3.62	4.03
EN	6.24	5.41	4.09	3.66	4.38	5.40	4.58	4.30	3.46	4.68

Table 11: The results of cohesiveness and separability experiments. EN refers to all English datasets, while CH refers to translating all English into Chinese datasets.