

QMP: Q-SWITCH MIXTURE OF POLICIES FOR MULTI-TASK BEHAVIOR SHARING

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ABSTRACT

Multi-task reinforcement learning (MTRL) aims to learn several tasks simultaneously for better sample efficiency than learning them separately. Traditional methods achieve this by sharing parameters or relabeled data between tasks. In this work, we introduce a new framework for sharing *behavioral policies* across tasks, which can be used in addition to existing MTRL methods. The key idea is to improve each task’s off-policy data collection by employing behaviors from other task policies. Selectively sharing helpful behaviors acquired in one task to collect training data for another task can lead to higher-quality trajectories, leading to more sample-efficient MTRL. Thus, we introduce a simple and principled framework called Q-switch mixture of policies (QMP) that selectively shares behavior between different task policies by using the task’s Q-function to evaluate and select useful shareable behaviors. We theoretically analyze how QMP improves the sample efficiency of the underlying RL algorithm. Our experiments show that QMP’s behavioral policy sharing provides complementary gains over many popular MTRL algorithms and outperforms alternative ways to share behaviors in various manipulation, locomotion, and navigation environments. Videos are available at <https://sites.google.com/view/qmp-mtrl>.

1 INTRODUCTION

In multi-task reinforcement learning, each task can benefit from the behaviors learned in others. Consider a robot learning four tasks simultaneously: opening and closing both a drawer and a door on a tabletop, as illustrated in Figure 1. A behavior is defined as the policy of how the robot acts in response to a situation, with the optimal behavior representing the best response, such as opening its gripper (action) when near the drawer handle (state) in the drawer-open task. As the robot learns, such behaviors are often shareable between tasks. For instance, both drawer-open and drawer-close tasks require behaviors for grasping the handle. Consequently, as the robot refines its ability to grasp the drawer handle in one task, it can incorporate these behaviors into the other, reducing the need to explore the entire action space randomly. Following this intuition, can we develop a general framework that leverages such behavior sharing across tasks to accelerate overall learning?

Most multi-task reinforcement learning (MTRL) methods share task information via policy parameters (Vithayathil Varghese & Mahmoud, 2020) or data relabeling (Kaelbling, 1993). We propose a new framework for MTRL: *share behaviors* between tasks to improve data collection by employing potentially useful policies from other tasks for more informative training data. This approach offers a simple, general, and sample-efficient approach that complements existing *off-policy* MTRL methods.

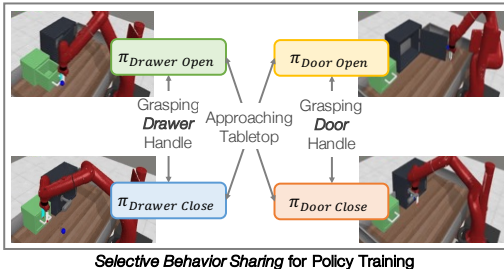


Figure 1: We propose a sample-efficient MTRL framework that selectively shares behaviors by acting with other task policies for data collection. For example, Drawer Open and Drawer Close can share behaviors performed for grasping drawer handle, while Drawer Open and Door Close share behaviors for approaching the tabletop.

Prior works (Teh et al., 2017; Ghosh et al., 2018) share behaviors between task policies uniformly by regularizing to one shared distilled policy (Rusu et al., 2015). This introduces a bias towards the mean behavior and causes negative interference when tasks might require differing optimal behaviors from the same state. In contrast, reusing other policies for data collection does not introduce any bias.

We propose *selective behavioral policy sharing* as a novel and general mechanism to improve sample efficiency in any MTRL architecture. Our key insight is that behaviors being acquired in other tasks can help when appropriately selected and shared, as shown in human learners (Tomov et al., 2021). In the Drawer Open task, while learning to approach the drawer handle, the robot should share behaviors between the Drawer policies, but avoid Door policies which would lead it to the wrong object.

The key question with selective behavioral policy sharing is how to identify helpful behaviors from other policies in a principled way. We propose a principled way of selecting shared behaviors: a Q-switch Mixture of Policies (QMP). At each state, one policy from a mixture of all policies is selected to collect data. The Q-switch makes this selection based on which policy best optimizes the current task’s soft Q-value because that is an estimate of the most helpful behavior for the current task. We prove that this selection mechanism preserves the convergence guarantees of the underlying RL algorithm and potentially improves sample efficiency. Crucially, QMP uses other tasks’ policies only for data collection, allowing policy training to remain unbiased under any off-policy RL algorithm.

Our primary contribution is introducing behavioral policy sharing for MTRL as a novel avenue of information sharing between tasks and addressing the problem of principled selective behavior sharing. Our proposed framework, Q-switch Mixture of Policies (QMP), can effectively identify shareable behaviors between tasks and incorporates them to gather more informative training data. We prove that QMP’s behavior sharing not only preserves the policy convergence of the underlying RL algorithm, but is at least as sample efficient. We demonstrate that QMP provides complementary gains to other forms of MTRL in a range of manipulation, locomotion, and navigation tasks and performs well over diverse task families when compared to other behavior sharing methods.

2 RELATED WORK

Information Sharing in Multi-Task RL. There are multiple, mostly complementary ways to share information in MTRL, including sharing *data*, sharing *parameters* or *representations*, and sharing *behaviors*. In offline MTRL, prior works selectively share *data* between tasks (Yu et al., 2021; 2022). Sharing parameters across policies can speed up MTRL through shared *representations* (Xu et al., 2020; D’Eramo et al., 2020; Yang et al., 2020; Sodhani et al., 2021; Misra et al., 2016; Perez et al., 2018; Devin et al., 2017; Vuorio et al., 2019; Rosenbaum et al., 2019; Yu et al., 2023; Cheng et al., 2023; Hong et al., 2022) and can be easily combined with other types of information sharing. Most similar to our work, Teh et al. (2017) and Ghosh et al. (2018) share *behaviors* between multiple policies through policy distillation and regularization. Vuong et al. (2019) identify which states between tasks share optimal behavior and regularize to each other there. These works share behaviors through regularization, biasing the policy objective when tasks have differing optimal behaviors. In contrast, our work selectively shares behavioral policies without modifying the training objective.

Multi-Task Learning for Diverse Task Families. Multi-task learning in diverse task families is susceptible to *negative transfer* between dissimilar tasks, hindering training. Prior works combat this by measuring task relatedness through validation loss on tasks (Liu et al., 2022; Ackermann et al., 2021) or influence of one task to another (Fifty et al., 2021; Standley et al., 2020) to find task groupings for training. Other works focus on the challenge of multi-objective optimization (Sener & Koltun, 2018; Hessel et al., 2019; Yu et al., 2020; Liu et al., 2021; Schaul et al., 2019; Chen et al., 2018; Kurin et al., 2022). Similar to these works, we identify that prior behavior-sharing MTRL approaches are susceptible to negative transfer. However, we avoid the challenge of negative transfer entirely by selectively sharing behaviors only during off-policy data collection.

Exploration in Multi-Task Reinforcement Learning. Our approach of modifying the behavioral policy to leverage shared task structures can be seen as a form of MTRL exploration, which we discuss further in Appendix Section 20c. Bangaru et al. (2016) encourage agents to increase their state coverage by providing an exploration bonus. Zhang & Wang (2021) study sharing information between agents to encourage exploration under tabular MDPs. Kalashnikov et al. (2021b) directly leverage data from policies of other specialized tasks (like grasping a ball) for their general task

variant (like grasping an object). In contrast to these approaches, we do not require a pre-defined task similarity measure or exploration bonus; we demonstrate in Section 6 that QMP works across many tasks and domains without these additional measures. Skill learning can be seen as behavior sharing in a single task setting such as learning options for exploration or heirarchical RL (Machado et al., 2017; Jinnai et al., 2019b;a; Hansen et al., 2019; Riemer et al., 2018). We also discuss the difference to single-task exploration in Appendix Section H.3.

Using Q-functions as filters. Yu et al. (2021) uses Q-functions to filter which data should be shared between tasks in a multi-task setting. In the imitation learning setting, Nair et al. (2018) and Sasaki & Yamashina (2020) use Q-functions to filter out low-quality demonstrations, so they are not used for training. In both cases, the Q-function is used to evaluate some data that can be used for training. Zhang et al. (2022) reuses pre-trained policies to learn a new task, using a Q-function as a filter to choose which pre-trained policies to regularize to as guidance. In contrast to prior works, our method uses a Q-function to *evaluate* different task policies to gather training data.

3 PROBLEM FORMULATION

Multi-task reinforcement learning (MTRL) addresses sequential decision-making tasks, where an agent learns a policy to act optimally in an environment (Kaelbling et al., 1996; Wilson et al., 2007). Therefore, in addition to typical multi-task learning techniques, MTRL can also share *behaviors*, i.e., actions, to improve sample efficiency. However, current approaches share behaviors uniformly (Section 2), which assumes that different tasks’ behaviors do not conflict. To address this limitation, we seek to develop a selective behavior-sharing method that can be applied in more general task families for sample-efficient MTRL.

Multi-Task RL with Behavior Sharing. We aim to simultaneously learn a set $\{\mathbb{T}_1, \dots, \mathbb{T}_N\}$ of N tasks. Each task \mathbb{T}_i is a Markov Decision Process (MDP) defined by state space \mathcal{S} , action space \mathcal{A} , transition probabilities \mathcal{T}_i , reward functions \mathcal{R}_i , initial state distribution ρ_i , and discount factor $\gamma \in [0, 1]$. While we use \mathcal{S} to denote shared state spaces for simplicity, our formulation extends to tasks with different state spaces as it complements policy architectures that share state encoders. The agent learns a set of N policies $\{\pi_1, \dots, \pi_N\}$, where each policy $\pi_i(a|s)$ represents the behavior on task \mathbb{T}_i . The objective is to maximize the average expected return over all tasks,

$$\{\pi_1^*, \dots, \pi_N^*\} = \max_{\{\pi_1, \dots, \pi_N\}} \frac{1}{N} \sum_{i=1}^N \left[\mathbb{E}_{a_t \sim \pi_i} \sum_{t=0}^{\infty} \gamma^t \mathcal{R}_i(s_t, a_t) \right].$$

Unlike prior works, our tasks can exhibit conflicting optimal behaviors: for any s , $\pi_i^*(a|s)$ may differ from $\pi_j^*(a|s)$. Thus, prior methods that bias policy learning objectives like direct policy sharing (Kalashnikov et al., 2021a) or behavior regularization (Teh et al., 2017) would be suboptimal.

4 APPROACH

To improve the sample efficiency of multi-task RL, we propose a framework that *selectively* incorporates behaviors from policies of other tasks without introducing bias into the RL objective for the current task. We achieve this by using a mixture of all policies as the behavioral policy for the current task, thereby modifying only its *off-policy training data*. However, naively mixing other policies into the current task’s behavioral policy does not necessarily improve its sample efficiency. To address this, we derive a specific definition of this mixture, named Q-switch Mixture of Policies (QMP), that selects a policy based on the current task’s Q-function (see Figure 2 and Algorithm 1) and prove that QMP guarantees greater than or equal sample efficiency than using the current task’s policy alone.

4.1 MULTI-TASK BEHAVIOR SHARING VIA OFF-POLICY DATA COLLECTION

MTRL methods like Teh et al. (2017) use *regularization to a common average policy* to enforce task policies to share behaviors. However, this introduces bias to each policy’s RL objective, leading to suboptimal actions in states where tasks require different actions. To address this, we propose using a *mixture of policies for off-policy data collection* as the means of behavior-sharing. At each state in any given task, one of the task policies is selected to gather training data as the current behavioral policy. This approach is compatible with any off-policy RL algorithm (Watkins & Dayan, 1992)

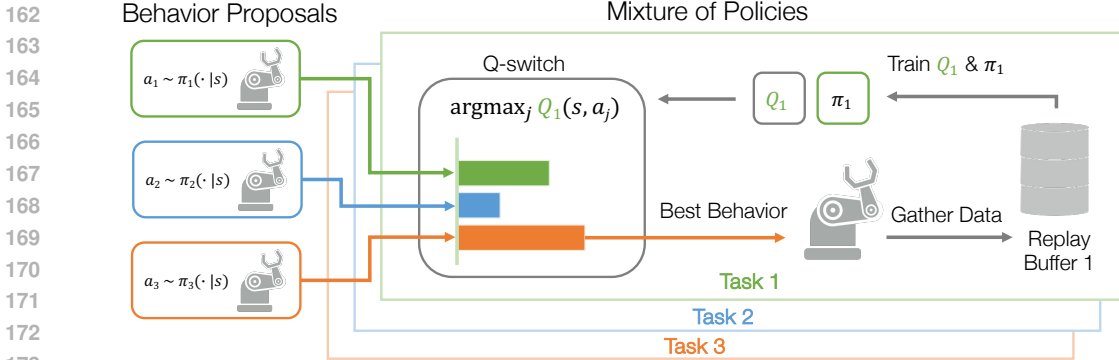


Figure 2: Our method (QMP) shares behavior between task policies in the data collection phase using a mixture of these policies. For example, in Task 1, each task policy proposes an action a_j . The task-specific Q-switch evaluates each $Q_1(s, a_j)$ and selects the best scored policy to gather reward-labeled data to train Q_1 and π_1 . Thus, Task 1 will be boosted by incorporating high-reward shareable behaviors into π_1 and improving Q_1 for subsequent Q-switch evaluations.

because the environment rewards help determine the best actions from the collected data. However, an effective mixture policy must choose the behavioral policies in a selective and principled way.

Definition 4.1 (Mixture of Policies). For each task \mathbb{T}_i , the mixture policy $\pi_i^{\text{mix}}(a | s)$ is defined as $\pi_i^{\text{mix}}(a | s) = \pi_{f_i(s, \pi_1, \dots, \pi_N)}(a | s)$, where $f_i(s, \pi_1, \dots, \pi_N) : \mathcal{S} \times \Pi^N \rightarrow \{1, \dots, N\}$ is a mixture-switch function that selects one of the policies π_1, \dots, π_N based on the current state s .

Our intuition of policy mixture shares inspiration with hierarchical RL (Çelik et al., 2021; Daniel et al., 2016; End et al., 2017; Goyal et al., 2019) where a *mixture* of options is learned according to the downstream task(s). However, a key difference in an MTRL mixture is that each policy is optimized for its own specific task and not designed to fit the task where the mixture is employed.

4.2 Q-SWITCH MIXTURE OF POLICIES (QMP)

We aim to derive a principled mixture-switch function f_i such that the mixture policy π_i^{mix} selectively incorporates behaviors from other policies while being guaranteed to be no worse than the current task’s policy π_i . We recall the generalized policy iteration procedure (Sutton & Barto, 2018) underlying single-task SAC (Haarnoja et al., 2018): policy evaluation learns Q by minimizing the bellman error on the collected data, and policy improvement follows Q by minimizing the KL divergence between the new policy and the exponential of the current Q -function, $Q^{\pi^{\text{old}}}$:

$$\pi^{\text{new}} = \arg \min_{\pi' \in \Pi} \text{D}_{\text{KL}} \left(\pi'(\cdot | s_t) \left\| \frac{\exp \left(\frac{1}{\alpha} Q^{\pi^{\text{old}}} (s_t, \cdot) \right)}{Z^{\pi^{\text{old}}} (s_t)} \right. \right) \quad (1)$$

In practice, the gradient updates in SAC are gradual and do not instantly achieve this optimization in Eq. 1, leaving a suboptimality gap to catch up to the Q -function. Thus, a mixture policy π_i^{mix} that selects the best policy from a set of all given policy candidates, *including the current policy*, ensures that π_i^{mix} is at least as good as π_i for the current state s , while potentially being a better optimizer of Eq. 1 due to shareable behaviors from the other task policies:

$$\min_{\pi' \in \{\pi_1, \dots, \pi_N\}} \text{D}_{\text{KL}} \left(\pi'(\cdot | s) \left\| \frac{\exp \left(\frac{1}{\alpha} Q^{\pi_i} (s, \cdot) \right)}{Z^{\pi_i} (s)} \right. \right) \leq \text{D}_{\text{KL}} \left(\pi_i(\cdot | s) \left\| \frac{\exp \left(\frac{1}{\alpha} Q^{\pi_i} (s, \cdot) \right)}{Z^{\pi_i} (s)} \right. \right) \quad (2)$$

Simplifying the expression on the left results in the following definition (derivation in Appendix C).

Definition 4.2 (Q-switch Mixture of Policies: QMP). For a task \mathbb{T}_i and available candidate policies $\{\pi_1, \dots, \pi_N\}$, the QMP $\pi_i^{\text{mix}}(a | s)$ selects a policy according to:

$$\pi_i^{\text{mix}} = \arg \max_{\pi' \in \{\pi_1, \dots, \pi_N\}} \mathbb{E}_{a \sim \pi'(\cdot | s)} [Q^{\pi_i}(s, a)] + \alpha \mathcal{H} [\pi'(\cdot | s)] \quad (3)$$

Algorithm 1 shows that QMP can be plugged into any MTRL framework, making it complementary with various MTRL frameworks like parameter-sharing and data relabeling (see Section 7.1). In practice, we estimate the expectation in Eq. 3 by evaluating the Q-value for the mean action of each task policy’s distribution $\pi'(\cdot|s)$ ignoring the entropy term. We do not find any empirical difference when using a sampled estimate of the expectation (see Appendix H.2) or including the entropy term, as the Q-value is the primary distinguishing factor between policies. In terms of compute, sampling from QMP’s $\pi_i^{\text{mix}}(a|s)$ does require more policy and Q-function evaluations. However, evaluations are parallelized and impact runtime negligibly, as shown in Appendix H.4.

While π_i^{mix} can mistakenly choose a poor policy due to estimation error in Q^{π_i} , this is identical to Q-learning or SAC, where the Q-function would be inaccurate at less-seen states. In both Q-learning and QMP, this is corrected with online interactions where the Q-function is trained to be more accurate in a subsequent iteration. Furthermore, π_i^{mix} actually better maximizes Q^{π_i} than π_i , which is the objective under generalized policy iteration. Note that QMP does **not** exacerbate the problem of overestimation because the soft policy evaluation step stays the same, i.e., it uses π_i and not π_i^{mix} .

5 WHY QMP WORKS: THEORY AND DIDACTIC EXAMPLE

5.1 QMP: CONVERGENCE AND IMPROVEMENT GUARANTEES

QMP performs simultaneous MTRL by collecting data using a Q-switch guided mixture of policies π_i^{mix} . In Appendix D, we prove that QMP with underlying RL algorithm Soft-Actor Critic (SAC) (Haarnoja et al., 2018) shares the same convergence guarantees in a tabular setting. Particularly, we show that under QMP, policy evaluation converges because QMP only modifies data collection of off-policy RL, policy improvement guarantees are preserved (Theorem 5.1), and policy iteration converges to an optimal policy at least as sample-efficiently (Theorem D.2).

The key reason for *better policy improvement* of QMP over the current task policy π_i is the arg max operation in Eq. 3, which ensures that the selected policy $\pi_i^{\text{mix}} \in \{\pi_j\}_{j=1}^N$ optimizes the SAC objective at least as well as π_i itself. We formalize this in Theorem 5.1 with proof in Appendix D.1. Due to the suboptimality gap in Eq. 1 in SAC, QMP can actually achieve better policy improvement when there are shareable behaviors between policies.

Theorem 5.1 (Mixture Soft Policy Improvement). *Consider π_i^{old} and its associated Q-function Q_i . Apply SAC’s policy improvement $\pi_i^{\text{old}} \rightarrow \pi_i$ and then $\pi_i \rightarrow \pi_i^{\text{mix}}$ from Eq. 3. Then, $Q^{\pi_i^{\text{mix}}}(s_t, \mathbf{a}_t) \geq Q^{\pi_i}(s_t, \mathbf{a}_t) \geq Q^{\pi_i^{\text{old}}}(s_t, \mathbf{a}_t)$ for all tasks \mathbb{T}_i and for all $(s_t, a_t) \in \mathcal{S} \times \mathcal{A}$ with $|\mathcal{A}| < \infty$.*

While QMP in Def. 4.2 applies to any set of candidate policies $\{\pi_1, \dots, \pi_N\}$, one expects π_i^{mix} to improve over π_i when some $\pi_j \neq \pi_i$ proposes an action candidate better than π_i for Task \mathbb{T}_i . This is more likely in MTRL policies that *share structure between tasks* than an arbitrary set of policies. For instance, if \mathbb{T}_i and \mathbb{T}_j share a subtask that appears early in the episodes for \mathbb{T}_j , then π_j would have already learned it before π_i and be a better policy for certain states of \mathbb{T}_i , according to Q_i .

QMP making bigger policy improvement steps results in each iteration of generalized policy iteration making more progress towards optimality. This reduces the number of iterations required to converge, improving the sample efficiency of the algorithm as illustrated in Fig. 3 and proved in Theorem D.2.

Algorithm 1 Q-switch Mixture of Policies (QMP)

Input: Task Set $\{\mathbb{T}_1, \dots, \mathbb{T}_N\}$
Initialize $\{\pi_i\}_{i=1}^N, \{Q_i\}_{i=1}^N$, Data buffers $\{\mathcal{D}_i\}_{i=1}^N$
for each epoch **do**
 for $i = 1$ to N **do**
 while Task \mathbb{T}_i episode not terminated **do**
 Observe state s
 Compute π_i^{mix} as in Eq. 3.
 Take action proposal from $a \sim \pi_i^{\text{mix}}$
 $\mathcal{D}_i \leftarrow \mathcal{D}_i \cup (s, a, r_i, s')$
 end while
 end for
 for $i = 1$ to N **do**
 Update π_i, Q_i using \mathcal{D}_i with SAC
 end for
end for
Output: Trained policies $\{\pi_i\}_{i=1}^N$

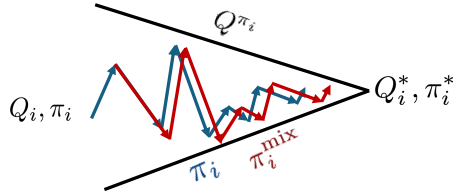


Figure 3: QMP generalized policy iteration

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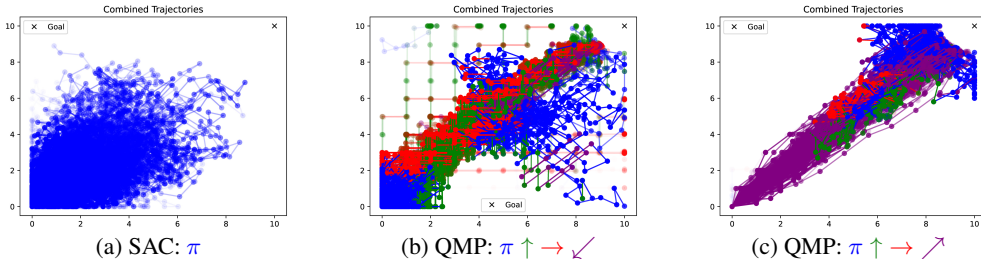


Figure 4: **2D Point Reaching.** We visualize the training trajectories of π with different sets of task policies (fixed but stochastic) and color each step with the policy that proposed it. (a) The single-task SAC policy cannot reach the goal. (b) With 3 diverse policies ($\uparrow \rightarrow \swarrow$), QMP often selects other policies, showing the suboptimality gap from Q in Eq. 1. (c) When a highly relevant \nearrow policy is added, QMP often selects \nearrow as it is likely to best optimize the learned Q-function.

5.2 ILLUSTRATIVE EXAMPLE: 2D POINT REACHING

We demonstrate when QMP can utilize alternate policy candidates $\{\pi_1, \dots, \pi_N\}$ to more effectively learn a policy by bridging a policy improvement suboptimality gap as π tries to follow Q in Eq. 1. Consider a 2D point-reaching task where the agent must navigate from the bottom-left corner $(0, 0)$ to the goal in the top-right corner $(10, 10)$. The point agent receives dense rewards based on its proximity to the goal and takes incremental 2D actions $(\Delta x, \Delta y) \in [-1, 1]^2$.

Figure 5 shows that the SAC policy π converges to a suboptimal solution. Fig. 4a confirms that the data collected by SAC policy never reaches the goal. This shows that if the suboptimality gap in π is not successfully bridged, it can make the entire algorithm converge suboptimally.

To illustrate the effect of QMP, we add 3 fixed gaussian policies centered on $(\uparrow \rightarrow \swarrow)$ or $(\uparrow \rightarrow \nearrow)$, and only let π be trainable. Fig. 4b, 4c show that π_i^{mix} employs alternate policies at many states in data collection as they optimize Eq. 3 better than π itself. This selectivity enables π_i^{mix} to generate more effective goal-reaching trajectories by bridging the suboptimality gap, resulting in better performance in Fig. 5. A policy like \nearrow that is more relevant to the underlying task leads to a larger gain.

The same principle extends to the simultaneous multi-task RL setting. In MTRL, each task’s policy continuously improves and can serve as a valuable candidate in the mixture for other tasks. QMP enables tasks to selectively share their behaviors, allowing each task to benefit from the progress of others. This mutual assistance accelerates learning across all tasks, as the mixture policy π_i^{mix} for each task \mathbb{T}_i selects the most promising action proposals from all available policies according to the task-specific Q-function, guaranteed to be at least as good as π_i itself. Consequently, MTRL combined with QMP leverages the collective knowledge of all tasks to bridge suboptimality gaps more efficiently, leading to improved sample efficiency and overall performance.

6 EXPERIMENTS

6.1 ENVIRONMENTS

We evaluate our method in 7 multi-task designs in manipulation, navigation, and locomotion environments, shown in Figure 6. These tasks vary in the degree of shared and conflicting behaviors between tasks and the number of tasks in the set. Further details in Appendix Section E.

Multistage Reacher: A 6 DoF Jaco arm learns 5 tasks with ordered subgoals. The first 4 tasks share some subgoals, while the 5th conflicting task requires the agent to stay at its initial position.

Maze Navigation: Building on point mass maze navigation (Fu et al., 2020), we define 10 tasks with various start and goal locations exhibiting coinciding and conflicting segments in the optimal paths.

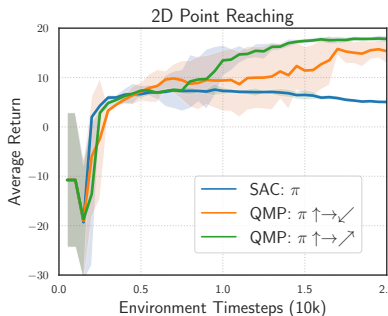


Figure 5: QMP improves performance using other policies, increasingly so when they are task-relevant (5 seeds).

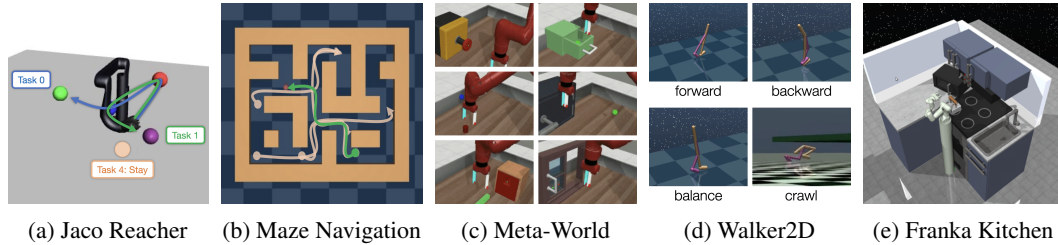


Figure 6: **Environments & Tasks:** (a) Multistage Jaco Reacher. The agent must reach different subgoals or stay still (Task 4). (b) Maze Navigation. The agent (green circle) must navigate to the goal (red circle). 4 other tasks are shown in orange. (c) Meta-World: 10 table-top manipulation tasks. (e) Franka Kitchen: 10 tasks, interacting with one appliance or cabinet.

Meta-World Manipulation: We use three task sets based on the Meta-World environment (Yu et al., 2019). **Meta-World MT10** and **Meta-World MT50** are sets of 10 and 50 table-top manipulation tasks involving different objects and behaviors. **Meta-World CDS** is a 4-task setup proposed in Yu et al. (2021) which places the door and drawer objects next to each other on the same tabletop so that all 4 tasks (door open & close, drawer open & close) are solvable in a simultaneous multi-task setup.

Walker2D: Walker2D is a 9 DoF bipedal walker agent with the multi-task set containing 4 locomotion tasks proposed in Lee et al. (2019): walking forward, walking backward, balancing, and crawling. These tasks require different gaits without an obviously identifiable shared behavior in the optimal policies but can still benefit from intermediate behaviors like balancing.

Kitchen: We use the challenging manipulation environment proposed by Gupta et al. (2019) where a 9 DoF Franka robot performs tasks in a kitchen. We create a task set out of 10 manipulation tasks: turning on or off different burners and light switches, and opening or closing different cabinets.

6.2 BASELINES

We first select popular and representative MTRL methods that share other forms of information to evaluate how behavior-sharing with QMP improves their performance:

- **No-Sharing** consists of N (refers to number of tasks) independent RL architectures where each agent is assigned one task and trained to solve it without any information sharing with other agents.
- **Data-Sharing (UDS)** proposed in Yu et al. (2022) shares data between tasks, relabelling with minimum task reward. We modified this offline RL algorithm to online.
- **Parameter-Sharing** a multi-head SAC policy sharing parameters but not behaviors over tasks.

We validate QMP’s approach to share behaviors via *off-policy data collection* with other approaches:

- **No-Shared-Behaviors** consists of N RL agents where each agent is assigned one task and trained to solve it without any behavior sharing with other agents: no bias and no sharing.
- **Fully-Shared-Behaviors** is a single SAC agent that learns one shared policy for all tasks, outputting the same action for a given state regardless of task (full parameter sharing): fully biased sharing.
- **Divide-and-Conquer RL (DnC)** (Ghosh et al. (2018)) uses N policies that share behaviors through policy distillation and regularization to the mean (adapted for MTRL): biased objective for sharing.
- **DnC (Regularization Only)** is a no policy distillation variant of DnC we propose as a baseline.
- **QMP (Ours)** learns N policies that share behaviors in off-policy data collection: unbiased sharing.

We used SAC Haarnoja et al. (2018) for all environments and methods. All the non-parameter sharing baselines use the same SAC hyperparameters. Please refer to Appendix I for complete details.

7 RESULTS

Our experiments address: (1) Does QMP provide complementary gains to other forms of MTRL? (2) How does sharing behavioral policies compare with alternate forms of behavior sharing? (3) Can QMP effectively identify shareable behaviors? (4) Ablating key components of QMP.

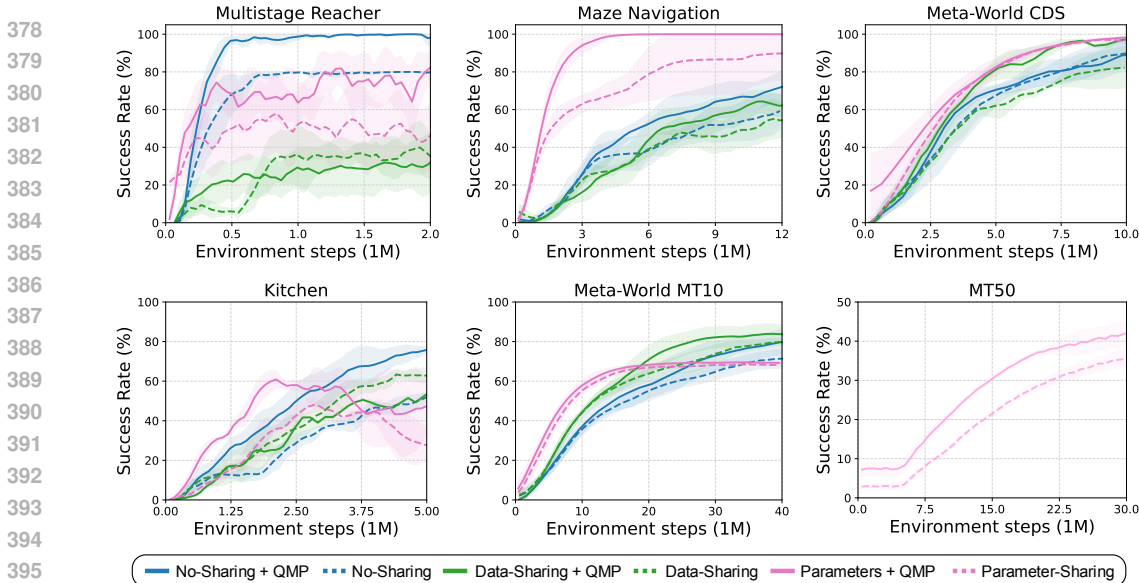


Figure 7: **Behavioral policy sharing is complementary.** QMP (solid lines) shows general improvement over MTRL frameworks (same-colored dashed lines) like No shared architecture (blue), shared parameters (pink), and shared data (green). Methods without parameter-sharing on MT50 converge very slowly. Success rate means and std (shaded) are over N tasks, 10 episodes per task, and 5 seeds.

7.1 IS BEHAVIOR SHARING COMPLEMENTARY TO OTHER MTRL FRAMEWORKS?

We demonstrate that our method is compatible with and provides complementary performance gains with other forms of MTRL that share different kinds of information, including parameter sharing and data sharing. We compare the performance between 3 base MTRL algorithms, No-Sharing, Parameter-Sharing, and Data-Sharing, with the addition of QMP in Figure 7. The No-Sharing baseline provides a baseline comparison of QMP’s effectiveness on its own. For the Parameter-Sharing and Data-Sharing baselines we chose the base algorithms for their popularity and simplicity. In each case, we add QMP by simply replacing the data collection policy with π_i^{mix} . We find that **QMP is complementary to all three baseline frameworks**, mostly with additive performance gains in sample efficiency and final performance, while not hurting the performance of the base method in all but one case (Data-Sharing in Kitchen). We additionally see that QMP improves PCGrad’s (Yu et al., 2020) performance significantly in 3 out of 4 environments tested in Appendix F.3. This shows that QMP is a simple and complementary addition to other forms of MTRL.

QMP significantly improves upon the No-Sharing baseline in all environments except Meta-World CDS where it performs comparatively. This demonstrates that sharing behavioral policies is a promising avenue for efficient and performant MTRL. In the data-sharing comparison, we see that the addition of QMP improves or performs comparably to the base algorithm. In Multistage Reacher and Maze Navigation, we see that both Data-Sharing and Data + QMP perform worse than the other MTRL methods, highlighting the fact that sharing data directly between tasks can be ineffective without access to a re-labeled task rewards like in our setting. In environments where data-sharing does well, like Meta-World CDS, we see that adding QMP does improve sample efficiency.

We find that Parameters + QMP generally outperforms Parameter-Sharing, while inheriting its sample efficiency gains. In many cases, the parameter-sharing methods converge sub-optimally, highlighting that shared parameter MTRL has its own challenges. However, in Maze Navigation, we find that sharing **Parameters + Behaviors greatly improves the performance over both the Parameter-Sharing baseline and No-Sharing + QMP variant of QMP**. This demonstrates the additive effect of these two forms of information sharing in MTRL. The agent initially benefits from the sample efficiency gains of the multi-head parameter-sharing architecture, while behavior sharing accelerates learning by selectively using other policies to keep learning even after the parameter-sharing effect plateaus, demonstrating the compatibility between QMP and parameter sharing as key ingredients to sample efficient MTRL. We further highlight that this **benefit of QMP increases with the number of tasks** increasing from 10 to 50 in Meta-World, where we see that QMP is actually more effective

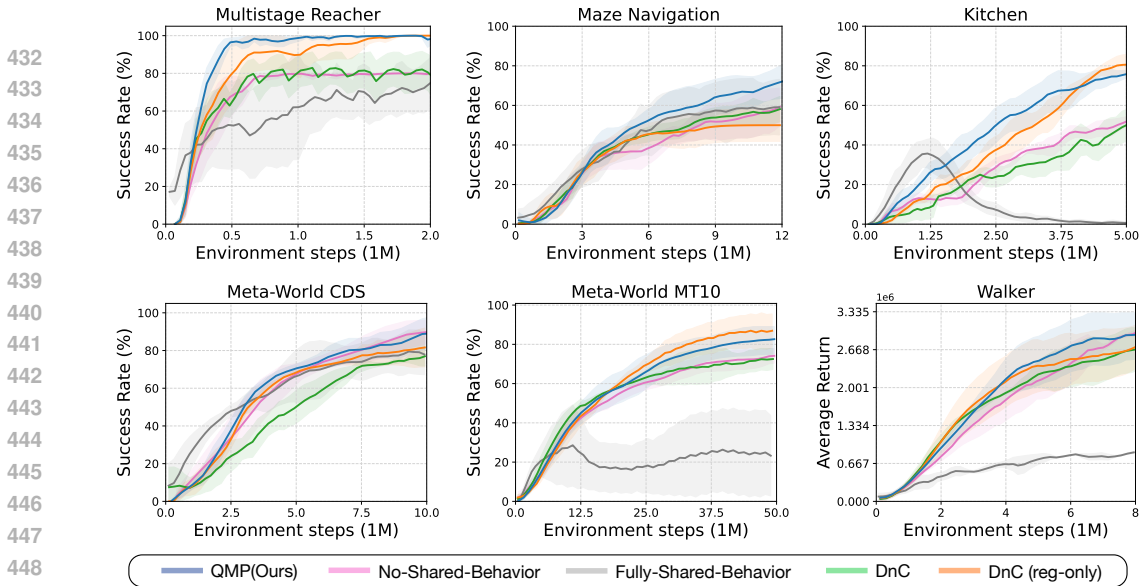


Figure 8: **QMP reliably shares behaviors.** In task sets exhibiting conflicting behaviors, QMP consistently matches or exceeds baselines in rate of convergence and final performance.

when combined with parameter sharing in MT50 than in MT10. QMP scales well with the number of tasks and can actually perform better likely due to *more shared behaviors* in the larger task set.

7.2 BASELINES: COMPARING DIFFERENT APPROACHES TO SHARE BEHAVIORS

To verify QMP’s efficacy as a behavior-sharing mechanism, we evaluate baselines that share behaviors in different ways on 6 environments in Figure 8. QMP reliably matches or exceeds other methods, especially in tasks that require conflicting behaviors, where alternate approaches are ineffective.

In the task sets with the most directly conflicting behaviors, Multistage Reacher and Maze Navigation, our method clearly outperforms other behavior-sharing and data-sharing baselines. In Multistage Reacher, our method reaches > 90% success rate at 0.5 million environment steps, while DnC (reg.), the next best method, takes 3 times the number of steps to fully converge. The rest of the methods fail to attain the maximum success rate. The UDS baseline performs particularly poorly, illustrating that data sharing can be ineffective without ground truth rewards. We also see that QMP scales better from 3 to 10 tasks in Maze compared to other behavior sharing methods in Appendix Section F.4.

In the remaining task sets with no directly conflicting behaviors, we see that QMP is competitive with the best-performing baseline for more complex manipulation and locomotion tasks. Particularly, in Walker2D and Meta-World CDS, we see that QMP is the most sample-efficient method and converges to a better final performance than any other behavior sharing method. In Meta-World MT10 and Kitchen, DnC (regularization only) also performed very well, showing that well-tuned uniform behavior sharing can be very effective in tasks without conflicting behavior. However, QMP also performs competitively and more sample efficiently, showing that QMP is effective under the same assumptions as uniform behavior-sharing methods but can do so *adaptively* and across more *general task families*. The Fully-Shared-Behaviors baseline often performs poorly because it totally biases the policies, while the No-Shared-Behavior is a surprisingly strong baseline as it introduces no bias.

7.3 CAN QMP EFFECTIVELY IDENTIFY SHAREABLE BEHAVIORS?

Figure 9a shows the average proportion of sharing from other tasks for Multistage Reacher Task 0 over the course of training. We see that QMP learns to generally share less behavior from Policy 4 than from Policies 1-3 (Appendix Figure 18). Conversely, QMP in Task 4 also shares the least total cross-task behavior (Appendix Figure 19). We see this same trend across all 5 Multistage Reacher tasks, showing that the Q-switch successfully **identifies conflicting behaviors that should not be shared**. Further, Figure 9a also shows that **total behavior-sharing from other tasks goes down over training**. Thus, Q-switch learns to prefer its own task-specific policy as it becomes more proficient.

We qualitatively analyze how behavior sharing varies within a single episode by visualizing a QMP rollout during training for the Drawer Open task in Meta-World CDS (Figure 9b). We see that it

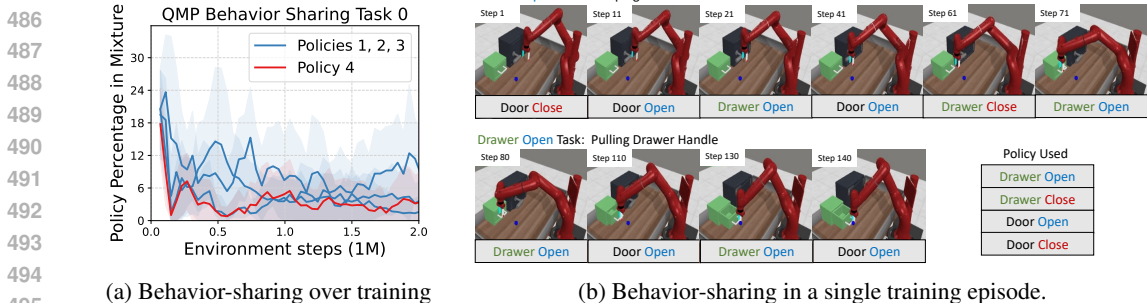


Figure 9: (a) Mixture probabilities of other policies for Task 0 in Multistage Reacher with the conflicting task Policy 4 shown in red. (b) Policies chosen by the QMP behavioral policy every 10 timesteps for the Drawer Open task throughout one training episode. The policy approaches and grasps the handle (top row), then pulls the drawer open (bottom row).

makes reasonable policy choices by (i) switching between all 4 task policies as it approaches the drawer (top row), (ii) using drawer-specific policies as it grasps the drawer-handle, and (iii) using Drawer Open and Door Open policies as it pulls the drawer open (bottom row). In conjunction with the overall results, this supports our claim that QMP can effectively identify shareable behaviors between tasks. For details on this visualization and the full analysis results see Appendix Section G.

Inspired by hierarchical RL (Dabney et al., 2021) and multi-task exploration (Xu et al., 2024), we briefly investigate *temporally extended behavior sharing* in Appendix F.6. Recently, Xu et al. (2024) showed that if one assumes a high overlap between optimal policies of different tasks, other task policies can aid exploration. So, we simply roll out each policy QMP selects for a fixed number of steps. QMP theory no longer holds as it requires selecting a policy at every step. Yet, this naive temporally extended QMP yields improvements in **some** environments like Maze with strong overlap.

7.4 ABLATIONS

We show the importance of Q-switch in QMP (Def. 4.2) against alternate forms of policy mixtures (Def. 4.1). **QMP-Uniform** is a uniform distribution over policies, $f_i = \mathbb{U}(\{1, \dots, N\})$ and achieves only 60% success rate (Figure 10), showing the importance of selectivity. **QMP-Domain-Knowledge** is a hand-crafted, fixed policy distribution based on an estimate of similarity between tasks. Multistage Reacher measures this similarity by the shared sub-goal sequences between tasks (Appendix E). QMP-Domain performs well initially but plateaus early, showing that which behaviors are shareable depends on the state and current policy. We further ablate the $\arg \max$ in Q-switch against a softmax variation resulting in a *probabilistic mixture policy* in Appendix Section H.1, and evaluating on the *mean policy actions* (Appendix Section H.2) to validate our design.

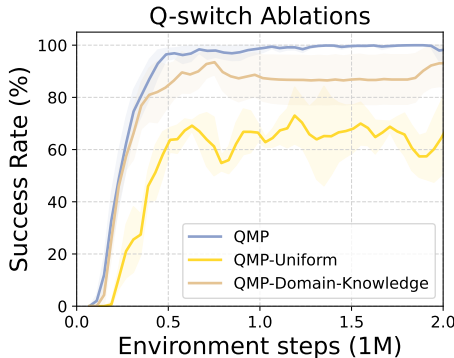


Figure 10: QMP outperforms alternate policy mixtures in Multistage Reacher.

8 CONCLUSION

We propose an unbiased approach to sharing behaviors via off-policy data collection in MTRL: Q-switch Mixture of Policies. We demonstrate empirically that QMP effectively improves the rate of convergence and task performance in manipulation, locomotion, and navigation tasks, and is guaranteed to be as good as the underlying RL algorithm and complementary to alternate MTRL. QMP does not assume that optimal task behaviors always coincide. Thus, its improvement magnitude is limited by the degree of shareable behaviors and the suboptimality gap that exists. At the same time, this lets QMP be unbiased and find optimal policies with convergence guarantees while being equally or more sample-efficient. **Since QMP only shares behaviors via off-policy data collection, it is not applicable to on-policy RL base algorithms like PPO (Schulman et al., 2017).** Promising future directions include temporally-extended behavior sharing and incorporating other forms of prior task information on shareable behaviors, such as language embeddings in instruction-following tasks.

540 REFERENCES

- 541
- 542 Johannes Ackermann, Oliver Richter, and Roger Wattenhofer. Unsupervised task clustering for multi-
543 task reinforcement learning. In Nuria Oliver, Fernando Pérez-Cruz, Stefan Kramer, Jesse Read,
544 and Jose A. Lozano (eds.), *Machine Learning and Knowledge Discovery in Databases. Research*
545 *Track*, pp. 222–237, Cham, 2021. Springer International Publishing. ISBN 978-3-030-86486-6.
- 546 Sai Praveen Bangaru, JS Suhas, and Balaraman Ravindran. Exploration for multi-task reinforcement
547 learning with deep generative models. *arXiv preprint arXiv:1611.09894*, 2016.
- 548
- 549 Lukas Biewald. Experiment tracking with weights and biases, 2020. URL [https://www.wandb.](https://www.wandb.com/)
550 [com/](https://www.wandb.com/). Software available from wandb.com.
- 551
- 552 Greg Brockman, Vicki Cheung, Ludwig Pettersson, Jonas Schneider, John Schulman, Jie Tang, and
553 Wojciech Zaremba. Openai gym. *arXiv preprint arXiv:1606.01540*, 2016.
- 554 Zhao Chen, Vijay Badrinarayanan, Chen-Yu Lee, and Andrew Rabinovich. GradNorm: Gradient
555 normalization for adaptive loss balancing in deep multitask networks. In *International Conference*
556 *on Machine Learning*, 2018.
- 557 Yuan Cheng, Songtao Feng, Jing Yang, Hong Zhang, and Yingbin Liang. Provable benefit of multitask
558 representation learning in reinforcement learning. In *Neural Information Processing Systems*,
559 2023.
- 560
- 561 Will Dabney, Georg Ostrovski, and Andre Barreto. Temporally-extended ϵ -greedy exploration. In
562 *International Conference on Learning Representations*, 2021.
- 563 Christian Daniel, Gerhard Neumann, Oliver Kroemer, and Jan Peters. Hierarchical relative entropy
564 policy search. *Journal of Machine Learning Research*, 2016.
- 565
- 566 Carlo D’Eramo, Davide Tateo, Andrea Bonarini, Marcello Restelli, Jan Peters, et al. Sharing
567 knowledge in multi-task deep reinforcement learning. In *International Conference on Learning*
568 *Representations*, 2020.
- 569 Coline Devin, Abhishek Gupta, Trevor Darrell, Pieter Abbeel, and Sergey Levine. Learning modular
570 neural network policies for multi-task and multi-robot transfer. In *IEEE International Conference*
571 *on Robotics and Automation*, 2017.
- 572
- 573 Felix End, Riad Akrou, Jan Peters, and Gerhard Neumann. Layered direct policy search for learning
574 hierarchical skills. In *IEEE International Conference on Robotics and Automation*, 2017.
- 575 Chris Fifty, Ehsan Amid, Zhe Zhao, Tianhe Yu, Rohan Anil, and Chelsea Finn. Efficiently identifying
576 task groupings for multi-task learning. In *Neural Information Processing Systems*, 2021.
- 577
- 578 Justin Fu, Aviral Kumar, Ofir Nachum, George Tucker, and Sergey Levine. D4rl: Datasets for deep
579 data-driven reinforcement learning. *arXiv preprint arXiv:2004.07219*, 2020.
- 580 The garage contributors. Garage: A toolkit for reproducible reinforcement learning research. [https:](https://github.com/rlworkgroup/garage)
581 [//github.com/rlworkgroup/garage](https://github.com/rlworkgroup/garage), 2019.
- 582
- 583 Dibya Ghosh, Avi Singh, Aravind Rajeswaran, Vikash Kumar, and Sergey Levine. Divide-and-
584 conquer reinforcement learning. In *International Conference on Learning Representations*, 2018.
- 585 Ruben Glatt, Felipe Leno Da Silva, Reinaldo Augusto da Costa Bianchi, and Anna Helena Reali
586 Costa. Decaf: Deep case-based policy inference for knowledge transfer in reinforcement learning.
587 *Expert Systems with Applications*, 2020.
- 588
- 589 Anirudh Goyal, Shagun Sodhani, Jonathan Binas, Xue Bin Peng, Sergey Levine, and Yoshua Bengio.
590 Reinforcement learning with competitive ensembles of information-constrained primitives. *arXiv*,
591 abs/1906.10667, 2019.
- 592
- 593 Abhishek Gupta, Vikash Kumar, Corey Lynch, Sergey Levine, and Karol Hausman. Relay policy
learning: Solving long horizon tasks via imitation and reinforcement learning. In *Conference on*
Robot Learning, 2019.

- 594 Tuomas Haarnoja, Aurick Zhou, Pieter Abbeel, and Sergey Levine. Soft actor-critic: Off-policy
595 maximum entropy deep reinforcement learning with a stochastic actor. In *International Conference*
596 *on Machine Learning*, 2018.
- 597 Steven Hansen, Will Dabney, Andre Barreto, Tom Van de Wiele, David Warde-Farley, and
598 Volodymyr Mnih. Fast task inference with variational intrinsic successor features. *arXiv preprint*
599 *arXiv:1906.05030*, 2019.
- 600 Matteo Hessel, Hubert Soyer, Lasse Espeholt, Wojciech Czarnecki, Simon Schmitt, and Hado van
601 Hasselt. Multi-task deep reinforcement learning with popart. In *AAAI Conference on Artificial*
602 *Intelligence*, 2019.
- 603 Sunghoon Hong, Deunsol Yoon, and Kee-Eung Kim. Structure-aware transformer policy for inhomogeneous
604 multi-task reinforcement learning. In *International Conference on Learning Representations*,
605 2022.
- 606 Yuu Jinnai, Jee Won Park, David Abel, and George Konidaris. Discovering options for exploration
607 by minimizing cover time. In *International Conference on Machine Learning*, 2019a.
- 608 Yuu Jinnai, Jee Won Park, Marlos C Machado, and George Konidaris. Exploration in reinforcement
609 learning with deep covering options. In *International Conference on Learning Representations*,
610 2019b.
- 611 Leslie Pack Kaelbling. Learning to achieve goals. In *International Joint Conference on Artificial*
612 *Intelligence*, 1993.
- 613 Leslie Pack Kaelbling, Michael L Littman, and Andrew W Moore. Reinforcement learning: A survey.
614 *Journal of Artificial Intelligence Research*, 1996.
- 615 Dmitry Kalashnikov, Jacob Varley, Yevgen Chebotar, Benjamin Swanson, Rico Jonschkowski,
616 Chelsea Finn, Sergey Levine, and Karol Hausman. Mt-opt: Continuous multi-task robotic reinforcement
617 learning at scale. *arXiv preprint arXiv:2104.08212*, 2021a.
- 618 Dmitry Kalashnikov, Jake Varley, Yevgen Chebotar, Benjamin Swanson, Rico Jonschkowski, Chelsea
619 Finn, Sergey Levine, and Karol Hausman. Scaling up multi-task robotic reinforcement learning.
620 In *Conference on Robot Learning*, 2021b.
- 621 Vitaly Kurin, Alessandro De Palma, Ilya Kostrikov, Shimon Whiteson, and M. Pawan Kumar. In
622 defense of the unitary scalarization for deep multi-task learning. *arXiv preprint arXiv:2201.04122*,
623 2022.
- 624 Youngwoon Lee, Shao-Hua Sun, Sriram Somasundaram, Edward S. Hu, and Joseph J. Lim. Composing
625 complex skills by learning transition policies. In *International Conference on Learning*
626 *Representations*, 2019.
- 627 Bo Liu, Xingchao Liu, Xiaojie Jin, Peter Stone, and Qiang Liu. Conflict-averse gradient descent for
628 multi-task learning. In *Neural Information Processing Systems*, 2021.
- 629 Shikun Liu, Stephen James, Andrew J Davison, and Edward Johns. Auto-lambda: Disentangling
630 dynamic task relationships. *Transactions on Machine Learning Research*, 2022.
- 631 Marlos C Machado, Clemens Rosenbaum, Xiaoxiao Guo, Miao Liu, Gerald Tesauro, and Murray
632 Campbell. Eigenoption discovery through the deep successor representation. *arXiv preprint*
633 *arXiv:1710.11089*, 2017.
- 634 Ishan Misra, Abhinav Shrivastava, Abhinav Gupta, and Martial Hebert. Cross-stitch networks for
635 multi-task learning. In *IEEE Conference on Computer Vision and Pattern Recognition*, 2016.
- 636 Siddharth Mysore, George Cheng, Yunqi Zhao, Kate Saenko, and Meng Wu. Multi-critic actor learning:
637 Teaching rl policies to act with style. In *International Conference on Learning Representations*,
638 2022.
- 639 Ashvin Nair, Bob McGrew, Marcin Andrychowicz, Wojciech Zaremba, and Pieter Abbeel. Overcoming
640 exploration in reinforcement learning with demonstrations. In *IEEE International Conference*
641 *on Robotics and Automation*, 2018.
- 642
- 643
- 644
- 645
- 646
- 647

- 648 Taewook Nam, Shao-Hua Sun, Karl Pertsch, Sung Ju Hwang, and Joseph J. Lim. Skill-based
649 meta-reinforcement learning. In *International Conference on Learning Representations*, 2022.
650
- 651 Adam Paszke, Sam Gross, Francisco Massa, Adam Lerer, James Bradbury, Gregory Chanan, Trevor
652 Killeen, Zeming Lin, Natalia Gimelshein, Luca Antiga, et al. Pytorch: An imperative style,
653 high-performance deep learning library. In *Neural Information Processing Systems*, 2019.
- 654 Ethan Perez, Florian Strub, Harm de Vries, Vincent Dumoulin, and Aaron Courville. Film: Visual
655 reasoning with a general conditioning layer. In *AAAI Conference on Artificial Intelligence*, 2018.
656
- 657 Karl Pertsch, Youngwoon Lee, and Joseph Lim. Accelerating reinforcement learning with learned
658 skill priors. In *Conference on Robot Learning*, 2021.
- 659 Matthew Riemer, Miao Liu, and Gerald Tesauro. Learning abstract options. In *Proceedings of
660 the 32nd International Conference on Neural Information Processing Systems*, NIPS’18, pp.
661 10445–10455, Red Hook, NY, USA, 2018. Curran Associates Inc.
- 662 Clemens Rosenbaum, Ignacio Cases, Matthew Riemer, and Tim Klinger. Routing networks and the
663 challenges of modular and compositional computation. *arXiv preprint arXiv:1904.12774*, 2019.
664
- 665 Andrei A. Rusu, Sergio Gomez Colmenarejo, Caglar Gulcehre, Guillaume Desjardins, James Kirk-
666 patrick, Razvan Pascanu, Volodymyr Mnih, Koray Kavukcuoglu, and Raia Hadsell. Policy
667 distillation. *arXiv preprint arXiv:1511.06295*, 2015.
668
- 669 Fumihiko Sasaki and Ryota Yamashina. Behavioral cloning from noisy demonstrations. In *Interna-
670 tional Conference on Learning Representations*, 2020.
- 671 Tom Schaul, Diana Borsa, Joseph Modayil, and Razvan Pascanu. Ray interference: a source of
672 plateaus in deep reinforcement learning. *arXiv preprint arXiv:1904.11455*, 2019.
673
- 674 John Schulman, Filip Wolski, Prafulla Dhariwal, Alec Radford, and Oleg Klimov. Proximal policy
675 optimization algorithms. *arXiv preprint arXiv:1707.06347*, 2017.
- 676 Ozan Sener and Vladlen Koltun. Multi-task learning as multi-objective optimization. In *Neural
677 Information Processing Systems*, 2018.
678
- 679 Shagun Sodhani, Amy Zhang, and Joelle Pineau. Multi-task reinforcement learning with context-
680 based representations. In *International Conference on Machine Learning*, 2021.
- 681 Trevor Standley, Amir R. Zamir, Dawn Chen, Leonidas Guibas, Jitendra Malik, and Silvio Savarese.
682 Which tasks should be learned together in multi-task learning? In *International Conference on
683 Machine Learning*, 2020.
684
- 685 Richard S Sutton and Andrew G Barto. *Reinforcement learning: An introduction*. MIT press, 2018.
686
- 687 Yee Teh, Victor Bapst, Wojciech M Czarnecki, John Quan, James Kirkpatrick, Raia Hadsell, Nico-
688 las Heess, and Razvan Pascanu. Distral: Robust multitask reinforcement learning. In *Neural
689 Information Processing Systems*, 2017.
- 690 Emanuel Todorov, Tom Erez, and Yuval Tassa. Mujoco: A physics engine for model-based control.
691 In *International Conference on Intelligent Robots and Systems*, 2012.
- 692 Momchil S Tomov, Eric Schulz, and Samuel J Gershman. Multi-task reinforcement learning in
693 humans. *Nature Human Behaviour*, 2021.
694
- 695 Nelson Vithayathil Varghese and Qusay H Mahmoud. A survey of multi-task deep reinforcement
696 learning. *Electronics*, 2020.
- 697 Tung-Long Vuong, Do-Van Nguyen, Tai-Long Nguyen, Cong-Minh Bui, Hai-Dang Kieu, Viet-Cuong
698 Ta, Quoc-Long Tran, and Thanh-Ha Le. Sharing experience in multitask reinforcement learning.
699 In *International Joint Conference on Artificial Intelligence*, 2019.
700
- 701 Risto Vuorio, Shao-Hua Sun, Hexiang Hu, and Joseph J Lim. Multimodal model-agnostic meta-
learning via task-aware modulation. In *Neural Information Processing Systems*, 2019.

702 Christopher JCH Watkins and Peter Dayan. Q-learning. *Machine learning*, 1992.
703

704 Aaron Wilson, Alan Fern, Soumya Ray, and Prasad Tadepalli. Multi-task reinforcement learning: a
705 hierarchical bayesian approach. In *International Conference on Machine Learning*, 2007.
706

707 Zhiyuan Xu, Kun Wu, Zhengping Che, Jian Tang, and Jieping Ye. Knowledge transfer in multi-task
708 deep reinforcement learning for continuous control. In *Neural Information Processing Systems*,
709 2020.

710 Ziping Xu, Zifan Xu, Runxuan Jiang, Peter Stone, and Ambuj Tewari. Sample efficient myopic ex-
711 ploration through multitask reinforcement learning with diverse tasks. In *International Conference*
712 *on Learning Representations*, 2024.

713 Ruihan Yang, Huazhe Xu, Yi Wu, and Xiaolong Wang. Multi-task reinforcement learning with soft
714 modularization. In *Neural Information Processing Systems*, 2020.
715

716 Tianhe Yu, Deirdre Quillen, Zhanpeng He, Ryan Julian, Karol Hausman, Chelsea Finn, and Sergey
717 Levine. Meta-world: A benchmark and evaluation for multi-task and meta reinforcement learning.
718 In *Conference on Robot Learning*, 2019.

719 Tianhe Yu, Saurabh Kumar, Abhishek Gupta, Sergey Levine, Karol Hausman, and Chelsea Finn.
720 Gradient surgery for multi-task learning. In *Neural Information Processing Systems*, 2020.
721

722 Tianhe Yu, Aviral Kumar, Yevgen Chebotar, Karol Hausman, Sergey Levine, and Chelsea Finn.
723 Conservative data sharing for multi-task offline reinforcement learning. In *Neural Information*
724 *Processing Systems*, 2021.

725 Tianhe Yu, Aviral Kumar, Yevgen Chebotar, Karol Hausman, Chelsea Finn, and Sergey Levine.
726 How to leverage unlabeled data in offline reinforcement learning. In *International Conference on*
727 *Machine Learning*, 2022.

728 Yuanqiang Yu, Tianpei Yang, Yongliang Lv, Yan Zheng, and Jianye Hao. T3s: Improving multi-task
729 reinforcement learning with task-specific feature selector and scheduler. In *International Joint*
730 *Conference on Neural Networks*, 2023.

731 Chicheng Zhang and Zhi Wang. Provably efficient multi-task reinforcement learning with model
732 transfer. In *Neural Information Processing Systems*, 2021.
733

734 Jesse Zhang, Haonan Yu, and Wei Xu. Hierarchical reinforcement learning by discovering intrinsic
735 options. In *International Conference on Learning Representations*, 2020.
736

737 Jin Zhang, Siyuan Li, and Chongjie Zhang. CUP: Critic-guided policy reuse. In *Neural Information*
738 *Processing Systems*, 2022.

739 Onur Çelik, Dongzhuoran Zhou, Gen Li, Philipp Becker, and Gerhard Neumann. Specializing
740 versatile skill libraries using local mixture of experts. In *Conference on Robot Learning*, 2021.
741
742
743
744
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746
747
748
749
750
751
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A QUALITATIVE RESULTS

The qualitative result videos are provided at <https://sites.google.com/view/qmp-mtrl>

B CODE SUBMISSION

In the supplementary submission, we provide the complete code to reproduce all the experiments, including QMP (ours) and baselines on all the environments.

C QMP DERIVATION

Following Section 4.2, we aim to derive the mixture-switch function f_i such that the mixture policy π_i^{mix} is guaranteed to be better than the current task’s policy π_i . We use the generalized policy iteration procedure (Sutton & Barto, 2018) underlying single-task SAC (Haarnoja et al., 2018): policy evaluation learns Q by minimizing the bellman error on the collected data, and policy improvement follows Q by minimizing the KL divergence between the new policy and the exponential of the current Q -function, $Q^{\pi^{\text{old}}}$, shown in Eq. 1.

In practice, the gradient updates in SAC are gradual and do not instantly achieve this optimization in Eq. 1, leaving a suboptimality gap to catch up to the Q -function. We observe that due to the potential similarity of some tasks in MTRL, this suboptimality gap can be bridged using other policies. Concretely, a mixture policy π_i^{mix} that selects the best policy from a set of all given policy candidates, including the current policy, ensures that π_i^{mix} is an improvement over π_i for the current state s :

Given a set of policies $\{\pi_1 \dots \pi_N\}$ including the current task policy π_i and a given state s , consider the following mixture policy:

$$\pi_i^{\text{mix}} = \arg \min_{\pi' \in \{\pi_i, \dots, \pi_N\}} \text{D}_{\text{KL}} \left(\pi'(\cdot | s) \left\| \frac{\exp(\frac{1}{\alpha} Q^{\pi_i}(s, \cdot))}{Z^{\pi_i}(s)} \right\| \right) \quad (4)$$

This π_i^{mix} is a better policy improvement solution to Eq. 1 than π_i , because:

$$\min_{\pi' \in \{\pi_i, \dots, \pi_N\}} \text{D}_{\text{KL}} \left(\pi'(\cdot | s) \left\| \frac{\exp(\frac{1}{\alpha} Q^{\pi_i}(s, \cdot))}{Z^{\pi_i}(s)} \right\| \right) \leq \text{D}_{\text{KL}} \left(\pi_i(\cdot | s_t) \left\| \frac{\exp(\frac{1}{\alpha} Q^{\pi_i}(s_t, \cdot))}{Z^{\pi_i}(s_t)} \right\| \right)$$

Now, we can simplify Eq. 4 to obtain Definition 4.2:

$$\begin{aligned} \pi_i^{\text{mix}} &= \arg \min_{\pi' \in \{\pi_i, \dots, \pi_N\}} \text{D}_{\text{KL}} \left(\pi'(\cdot | s) \left\| \frac{\exp(\frac{1}{\alpha} Q^{\pi_i}(s, \cdot))}{Z^{\pi_i}(s)} \right\| \right) \\ &= \arg \min_{\pi' \in \{\pi_i, \dots, \pi_N\}} \mathbb{E}_{a \sim \pi'(\cdot | s)} \left[\log \pi'(a | s) - \log \left\{ \frac{\exp(\frac{1}{\alpha} Q^{\pi_i}(s, a))}{Z^{\pi_i}(s)} \right\} \right] \\ &= \arg \max_{\pi' \in \{\pi_i, \dots, \pi_N\}} \mathbb{E}_{a \sim \pi'(\cdot | s)} \left[-\log \pi'(a | s) + \frac{1}{\alpha} Q^{\pi_i}(s, a) - \log Z^{\pi_i}(s) \right] \\ &= \arg \max_{\pi' \in \{\pi_i, \dots, \pi_N\}} \mathbb{E}_{a \sim \pi'(\cdot | s)} [-\log \pi'(a | s)] + \mathbb{E}_{a \sim \pi'(\cdot | s)} \left[\frac{1}{\alpha} Q^{\pi_i}(s, a) \right] \\ &= \arg \max_{\pi' \in \{\pi_i, \dots, \pi_N\}} \mathbb{E}_{a \sim \pi'(\cdot | s)} [Q^{\pi_i}(s, a)] + \alpha \mathcal{H}[\pi'(\cdot | s)] \end{aligned}$$

Thus, the following mixture policy guarantees improvement over π_i

$$\pi_i^{\text{mix}} = \arg \max_{\pi' \in \{\pi_i, \dots, \pi_N\}} \mathbb{E}_{a \sim \pi'(\cdot | s)} [Q^{\pi_i}(s, a)] + \alpha \mathcal{H}[\pi'(\cdot | s)]$$

D QMP CONVERGENCE GUARANTEES

We derive the convergence guarantees for *mixture soft policy iteration* used in the QMP Algorithm 1. We augment the derivation of soft policy iteration in SAC (Haarnoja et al., 2018), which is our base algorithm, with our proposed QMP’s mixture policy. Soft policy iteration follows generalized policy iteration (Sutton & Barto, 2018) which refers to the general idea of repeated application of (1) policy evaluation to update the critics and (2) policy improvement based on the updated critics, until convergence. Like SAC, we consider the tabular setting and show that QMP’s modification to soft policy iteration converges to the optimal policy. Further, QMP can lead to an improved policy improvement step when there are shareable behaviors between tasks, consequently improving the sample efficiency. The derivation sketch follows:

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1. **Soft Policy Evaluation:** QMP modifies the off-policy data collection pipeline by replacing the primary task policy π_i with the mixture policy π_i^{mix} . However, it does not affect the soft Bellman backup operator of SAC, as shown in Haarnoja et al. (2018), and therefore the Q function still converges as in SAC.
 2. **Mixture Soft Policy Improvement:** QMP performs policy improvement in two steps: SAC’s policy update from $\pi_i^{\text{old}} \rightarrow \pi_i$ and applying the mixture of policies from $\pi_i \rightarrow \pi_i^{\text{mix}}$.
 - **Soft Policy Improvement:** Since QMP does *not* modify the SAC update procedure $\pi_i^{\text{old}} \rightarrow \pi_i$, we directly use SAC’s guarantees of policy improvement following Lemma 2 from Haarnoja et al. (2018).
 - **Mixture Policy Improvement:** We demonstrate QMP’s mixture policy π_i^{mix} guarantees a better policy improvement over the per-task policies π_i that compose the mixture. In Theorem D.1, we show convergence guarantee by proving that the expected return following π_i^{mix} is better than following π_i^{old} .
 3. **Mixture Soft Policy Iteration:** In Theorem D.2, we show that the repeated application of the above steps in QMP converges to an optimal policy for each task. Furthermore, the convergence rate is faster because of a greedier policy improvement due to *Mixture Policy Improvement*.

882 For a given stochastic policy π and task $\mathbb{T}_i \in \{\mathbb{T}_1 \dots \mathbb{T}_N\}$, define V_i^π as the expected return of acting with π . Given another stochastic policy π' , define $Q_i^\pi(s, \pi'(s)) = \mathbb{E}_{a \sim \pi'(s)} Q_i^\pi(s, a)$ as the expected return of acting with π' only in s and thereafter with π .

885 **Theorem D.1** (Mixture Soft Policy Improvement). *Consider π_i^{old} and its associated Q -function Q_i . Apply SAC’s policy improvement $\pi_i^{\text{old}} \rightarrow \pi_i$ and then $\pi_i \rightarrow \pi_i^{\text{mix}}$ from Eq. 3. Then, $Q_i^{\pi_i^{\text{mix}}}(\mathbf{s}_t, \mathbf{a}_t) \geq Q_i^{\pi_i}(\mathbf{s}_t, \mathbf{a}_t) \geq Q_i^{\pi_i^{\text{old}}}(\mathbf{s}_t, \mathbf{a}_t)$ for all tasks \mathbb{T}_i and for all $(\mathbf{s}_t, \mathbf{a}_t) \in \mathcal{S} \times \mathcal{A}$ with $|\mathcal{A}| < \infty$.*

889 *Proof.* From Soft Policy Improvement, Lemma 2 of Haarnoja et al. (2018), we have

$$891 \mathbb{E}_{\mathbf{a}_t \sim \pi_i} \left[Q_i^{\pi_i^{\text{old}}}(\mathbf{s}_t, \mathbf{a}_t) - \log \pi_i(\mathbf{a}_t | \mathbf{s}_t) \right] \geq V_i^{\pi_i^{\text{old}}}(\mathbf{s}_t).$$

894 Rewrite the difference as $\delta(\mathbf{s}_t)$,

$$895 \delta(\mathbf{s}_t) = \mathbb{E}_{\mathbf{a}_t \sim \pi_i} \left[Q_i^{\pi_i^{\text{old}}}(\mathbf{s}_t, \mathbf{a}_t) - \log \pi_i(\mathbf{a}_t | \mathbf{s}_t) \right] - V_i^{\pi_i^{\text{old}}}(\mathbf{s}_t) \geq 0.$$

898 From Eq. 3,

$$899 \pi_i^{\text{mix}} = \arg \max_{\pi' \in \{\pi_1, \dots, \pi_N\}} \mathbb{E}_{a \sim \pi'(\cdot | s)} [Q_i^{\pi_i}(s, a)] + \alpha \mathcal{H}[\pi'(\cdot | s)].$$

902 Therefore, we have a positive difference $\omega(\mathbf{s}_t)$,

$$903 \omega(\mathbf{s}_t) = \mathbb{E}_{\mathbf{a}_t \sim \pi_i^{\text{mix}}} \left[Q_i^{\pi_i^{\text{old}}}(\mathbf{s}_t, \mathbf{a}_t) - \log \pi_i^{\text{mix}}(\mathbf{a}_t | \mathbf{s}_t) \right] - \mathbb{E}_{\mathbf{a}_t \sim \pi_i} \left[Q_i^{\pi_i^{\text{old}}}(\mathbf{s}_t, \mathbf{a}_t) - \log \pi_i(\mathbf{a}_t | \mathbf{s}_t) \right] \geq 0.$$

906 We use δ to expand the soft Bellman equation to derive the relationship between $Q_i^{\pi_i^{\text{old}}}$ and $Q_i^{\pi_i}$,

$$\begin{aligned}
 907 Q_i^{\pi_i^{\text{old}}}(\mathbf{s}_t, \mathbf{a}_t) &= r(\mathbf{s}_t, \mathbf{a}_t) + \gamma \mathbb{E}_{\mathbf{s}_{t+1} \sim p} \left[V_i^{\pi_i^{\text{old}}}(\mathbf{s}_{t+1}) \right] \\
 908 &= r(\mathbf{s}_t, \mathbf{a}_t) + \gamma \mathbb{E}_{\mathbf{s}_{t+1} \sim p} \left[\mathbb{E}_{\mathbf{a}_{t+1} \sim \pi_i} \left(Q_i^{\pi_i^{\text{old}}}(\mathbf{s}_{t+1}, \mathbf{a}_{t+1}) - \log \pi_i(\mathbf{a}_{t+1} | \mathbf{s}_{t+1}) \right) - \delta(\mathbf{s}_{t+1}) \right] \\
 909 &\vdots \\
 910 &= \underbrace{\sum_{k=0}^{\infty} \gamma^k \mathbb{E}_{\mathbf{s}_{t+k} \sim p, \mathbf{a}_{t+k} \sim \pi_i} [r(\mathbf{s}_{t+k}, \mathbf{a}_{t+k}) - \log \pi_i(\mathbf{a}_{t+k} | \mathbf{s}_{t+k})]}_{Q_i^{\pi_i}(\mathbf{s}_t, \mathbf{a}_t)} - \underbrace{\sum_{k=1}^{\infty} \gamma^k \mathbb{E}_{\mathbf{s}_{t+k} \sim p} [\delta(\mathbf{s}_{t+k})]}_{\Delta_1} \\
 911 &= Q_i^{\pi_i}(\mathbf{s}_t, \mathbf{a}_t) - \Delta_1
 \end{aligned}$$

Likewise, we use δ and ω to derive the relationship between $Q^{\pi_i^{\text{old}}}$ and $Q^{\pi_i^{\text{mix}}}$,

$$\begin{aligned}
Q^{\pi_i^{\text{old}}}(\mathbf{s}_t, \mathbf{a}_t) &= r(\mathbf{s}_t, \mathbf{a}_t) + \gamma \mathbb{E}_{\mathbf{s}_{t+1} \sim p} \left[V^{\pi_i^{\text{old}}}(\mathbf{s}_{t+1}) \right] \\
&= r(\mathbf{s}_t, \mathbf{a}_t) + \gamma \mathbb{E}_{\mathbf{s}_{t+1} \sim p} \left[\mathbb{E}_{\mathbf{a}_{t+1} \sim \pi_i} \left(Q^{\pi_i^{\text{old}}}(\mathbf{s}_{t+1}, \mathbf{a}_{t+1}) - \log \pi_i(\mathbf{a}_{t+1} | \mathbf{s}_{t+1}) \right) - \delta(\mathbf{s}_{t+1}) \right] \\
&= r(\mathbf{s}_t, \mathbf{a}_t) + \gamma \mathbb{E}_{\mathbf{s}_{t+1} \sim p} \left[\mathbb{E}_{\mathbf{a}_{t+1} \sim \pi_i^{\text{mix}}} \left(Q^{\pi_i^{\text{old}}}(\mathbf{s}_{t+1}, \mathbf{a}_{t+1}) - \log \pi_i^{\text{mix}}(\mathbf{a}_{t+1} | \mathbf{s}_{t+1}) \right) - \delta(\mathbf{s}_{t+1}) - \omega(\mathbf{s}_{t+1}) \right] \\
&\vdots \\
&= \underbrace{\sum_{k=0}^{\infty} \gamma^k \mathbb{E}_{\mathbf{s}_{t+k} \sim p, \mathbf{a}_{t+k} \sim \pi_i^{\text{mix}}} \left[r(\mathbf{s}_{t+k}, \mathbf{a}_{t+k}) - \log \pi_i^{\text{mix}}(\mathbf{a}_{t+k} | \mathbf{s}_{t+k}) \right]}_{Q^{\pi_i^{\text{mix}}}(\mathbf{s}_t, \mathbf{a}_t)} \\
&\quad - \underbrace{\sum_{k=1}^{\infty} \gamma^k \mathbb{E}_{\mathbf{s}_{t+k} \sim p} [\delta(\mathbf{s}_{t+k})]}_{\Delta_2} - \underbrace{\sum_{k=1}^{\infty} \gamma^k \mathbb{E}_{\mathbf{s}_{t+k} \sim p} [\omega(\mathbf{s}_{t+k})]}_{\Omega} \\
&= Q^{\pi_i^{\text{mix}}}(\mathbf{s}_t, \mathbf{a}_t) - \Delta_2 - \Omega,
\end{aligned}$$

We assume that the effect of the difference $\Delta_2 - \Delta_1$ due to different state coverage is lower compared to the effect of Ω because ω is accumulated at every state, i.e., $\Delta_2 + \Omega = \Delta_1 + (\Delta_2 - \Delta_1) + \Omega \geq \Delta_1$

Since $\Delta_1, \Delta_2 \geq 0$ and $\Omega \geq 0$, we have

$$Q^{\pi_i^{\text{mix}}}(\mathbf{s}_t, \mathbf{a}_t) \geq Q^{\pi_i}(\mathbf{s}_t, \mathbf{a}_t) \geq Q^{\pi_i^{\text{old}}}(\mathbf{s}_t, \mathbf{a}_t)$$

□

Theorem D.2 (Mixture Soft Policy Iteration). *Repeated application of (i) soft policy evaluation and (ii) mixture soft policy improvement (Theorem D.1) to any $\pi_i \in \Pi$ converges to an optimal policy π_i^* such that $Q_i^{\pi_i^*}(\mathbf{s}_t, \mathbf{a}_t) \geq Q_i^{\pi_i}(\mathbf{s}_t, \mathbf{a}_t)$ for all $\pi_i \in \Pi$ and $(\mathbf{s}_t, \mathbf{a}_t) \in \mathcal{S} \times \mathcal{A}$ with $|\mathcal{A}| < \infty$. Furthermore, the sample efficiency and rate of convergence is at least as good as SAC in the presence of mixture policy improvement.*

Proof. Let π_i^k be the policy at iteration k . By SAC’s soft policy iteration, the sequence $Q_i^{\pi_i^k}$ is monotonically increasing, because π_i^{mix} only modifies the online data collected and SAC is an off-policy algorithm. Thus, Theorem 1 (Soft Policy Iteration) from Haarnoja et al. (2018) Appendix B.3 directly applies here and proves that repeated application of soft policy evaluation and soft policy improvement converges to an optimal policy π_i^* .

Mixture soft policy improvement (Theorem D.1) shows that π_i^{mix} is a greedier policy improvement over π_i with respect to each estimate of $Q_i^{\pi_i^k}$. Thus, the expected returns in the data collected by QMP policy, $Q_i^{\pi_i^{\text{mix};k}}$, is greater than or equal to that collected by the individual task policy, $Q_i^{\pi_i^k}$. Therefore, every mixture soft policy improvement step constitutes a *larger policy improvement step* than SAC’s soft policy improvement step. This makes the convergence of mixture soft policy iteration (repeated application of soft policy evaluation and Theorem D.1) an improvement over soft policy iteration.

□

E ENVIRONMENT DETAILS

E.1 MULTISTAGE REACHER

We implement our multistage reacher tasks on top of the Open AI Gym (Brockman et al., 2016) Reacher environment simulated in the MuJoCo physics engine (Todorov et al., 2012) by defining a sequence of 3 subgoals per task which are specified in Table 1. For all tasks, the reacher is initialized at the same start position with a small random perturbation sampled uniformly from $[-0.01, 0.01]$ for

each coordinate. The observation includes the agent’s proprioceptive state and how many sub-goals have been reached but not subgoal locations, as they must be inferred from the respective task’s reward function.

We set up the tasks to ensure that we can evaluate behavior sharing when the task rewards are qualitatively different (see Figure 6a):

- For every task except Task 3, the reward function is the default gym reward function based on the distance to the goal, plus an additional bonus for every subgoal completed.
- For Task 1, the reward is shifted by -2 at every timestep.
- Task 3 receives only a sparse reward of 1 for every subgoal reached.
- Task 4 has one fixed goal set at its initial position.

	Subgoal 1	Subgoal 2	Subgoal 3
T_0	(0.2, 0.3, 0.5)	(0.3, 0, 0.3)	(0.4, -0.3, 0.4)
T_1	(0.2, 0.3, 0.5)	(0.3, 0, 0.3)	(0.4, 0.3, 0.2)
T_2	(0.3, 0, 0.3)	(0.4, 0.3, 0.2)	(0.4, -0.3, 0.4)
T_3	(0.3, 0, 0.3)	(0.4, -0.3, 0.4)	(0.2, 0.3, 0.5)
T_4	initial	initial	initial

Table 1: Coordinates of subgoal locations for each task in Multistage Reacher. Shared subgoals are highlighted in the same color. For Task 4, the only goal is to stay in the initial position.

QMP-Domain: Section 7.4 ablates the importance of an adaptive and state-dependent Q-switch by replacing it with a domain-dependent distribution over other tasks based on apparent task similarity. Specifically, to define the mixture probabilities for QMP-Domain in Multistage Reacher, we use the domain knowledge of the subgoal locations of the tasks to determine the mixture probabilities. We use the ratio of *shared sub-goal sequences* between each pair of tasks (not necessarily the shared subgoals) over the total number of sub-goal sequences, 3, to calculate how much behavior must be shared between two tasks. For that ratio of shared behavior, we distribute the probability mass uniformly between all task policies that share that behavior. For Task 4, the conflicting task, we do not do any behavior sharing and only use π_4 to gather data.

Each Task \mathbb{T}_i consists of 3 sub-goal sequences $\{S_0, S_1, S_2\}$ (e.g. [initial \rightarrow Subgoal 1], [Subgoal 1 \rightarrow Subgoal 2], and [Subgoal 2 \rightarrow Subgoal 3]). For each sequence $s \in \{S_0, S_1, S_2\}$, we divide equally the contribution of each task \mathbb{T}_j ’s policy π_j that shares the sequence s (i.e. if \mathbb{T}_0 and \mathbb{T}_1 both contain sequence s , where we use the notation $\mathbb{1}(s \in \mathbb{T}_i)$ as the indicator function for whether Task \mathbb{T}_i contains sequence s , then π_0 and π_1 both have $\frac{1}{2}$ contribution for s). Each sequence contributes equally to the overall mixture probabilities for Task i (i.e. all policies that shares sequence S_i contributes in total $\frac{1}{3}$ to the mixture probability for the behavior policy of Task \mathbb{T}_i). Thus, the contribution probability of Policy π_j to Task \mathbb{T}_i is:

$$p_{j \rightarrow i} = \sum_{s \in \{S_0, S_1, S_2\}} \frac{1}{3} \cdot \frac{\mathbb{1}(s \in \mathbb{T}_j)}{\sum_k \mathbb{1}(s \in \mathbb{T}_k)}$$

$$\pi_i^{\text{mix}} = \sum_j p_{j \rightarrow i} \pi_j$$

Reusing notation for mixture probabilities, we have,

$$\begin{aligned}\pi_0^{mix} &= \frac{2}{3}\pi_0 + \frac{1}{3}\pi_1 \\ \pi_1^{mix} &= \frac{1}{3}\pi_0 + \frac{2}{3}\pi_1 \\ \pi_2^{mix} &= \frac{5}{6}\pi_2 + \frac{1}{6}\pi_3 \\ \pi_3^{mix} &= \frac{1}{6}\pi_2 + \frac{5}{6}\pi_3 \\ \pi_4^{mix} &= \pi_4\end{aligned}$$

E.2 MAZE NAVIGATION

The layout and dynamics of the maze follow Fu et al. (2020), but since their original design aims to train a single agent to reach a fixed goal from multiple start locations, we modified it to have both start and goal locations fixed in each task, as in Nam et al. (2022). The start location is still perturbed with a small noise to avoid memorizing the task. The observation consists of the agent’s current position and velocity. But, it lacks the goal location, which should be inferred from the dense reward based on the distance to the goal. The action space is the target 2D velocity of the point mass agent. The layout we used is LARGE_MAZE which is an 8×11 maze with paths blocked by walls. The complete set of 10 tasks is visualized in Figure 12, where green and red spots correspond to the start and goal locations, respectively. The environment provides an agent a dense reward of $\exp(-dist)$ where $dist$ is a linear distance between the agent’s current position and the goal location. It also gives a penalty of 1 at each timestep in order to prevent the agent from exploiting the reward by staying near the goal. The episode terminates either as soon as the goal is reached by having $dist < 0.5$ or when 600 timesteps have passed.



Figure 12: Ten tasks defined for the Maze Navigation. The start and goal locations in each task are shown in green and red spots, respectively, and an example path is shown in green.

E.3 META-WORLD MANIPULATION

For Meta-World CDS, we reproduce the Meta-world environment proposed by Yu et al. (2021) using the Meta-world codebase (Yu et al., 2019), where the door and drawer are both placed side-by-side on the tabletop for all tasks (see Figure 6c). The observation space consists of the robot’s proprioceptive state, the drawer handle state, the door handle state, and the goal location, which varies based on the task. Unlike Yu et al. (2021), we additionally remove the previous state from the observation space so the policies cannot easily infer the current task, making it a challenging multi-task environment. The environment also uses the default Meta-World reward functions which is composed of two distance-based rewards: distance between the agent end effector and the object, and distance between the object and its goal location. We use this modified environment instead of the Meta-world benchmark because our problem formulation of simultaneous multi-task RL requires

1080 a consistent environment across tasks. For Meta-World MT10, we directly use the implementation
1081 provided in (Yu et al., 2019) without changes.

1082 In both cases, the observation space consists of the robot’s proprioceptive state, locations for objects
1083 present in the environment (ie. door and drawer handle for CDS, the single target object location
1084 for MT10) and the goal location. In Meta-World CDS, due to the shared environment, there are no
1085 directly conflicting task behaviors, since the policies either go to the door or the drawer, they should
1086 ignore the irrelevant behaviors of policies interacting with the other object. In Meta-World MT10,
1087 each task interacts with a different object but in an overlapping state space so there is a mix of shared
1088 and conflicting behaviors.

1090 E.4 WALKER2D

1091 Walker2D is a 9 DoF bipedal walker agent with the multi-task set of 4 tasks proposed and implemented
1092 by Lee et al. (2019): walking forward at a target velocity, walking backward at a target velocity,
1093 balancing under random external forces, and crawling under a ceiling. Each of these tasks involves
1094 different gaits or body positions to accomplish successfully without any obviously identifiable shared
1095 behavior in the optimal policies. Behavior sharing can still be effective during training to aid
1096 exploration and share helpful intermediate behaviors, like balancing. However, there is no obviously
1097 identifiable conflicting behavior either in this task set. Because each task requires a different gait, it
1098 is unlikely for states to recur between tasks and even less likely for states that are shared to require
1099 conflicting behaviors. For instance, it is common for all policies to struggle and fall at the beginning
1100 of training, but all tasks would require similar stabilizing and correcting behavior over these states.

1103 E.5 KITCHEN

1104 We modify the Franka Kitchen environment proposed by Gupta et al. (2019) and based on the
1105 implementation from Fu et al. (2020). Since this environment is typically used for long horizon or
1106 offline RL, we chose shorter tasks that are learnable with online RL. Furthermore, we added a dense
1107 reward based on the Meta-World reward function. We formed our 10 task MTRL set by choosing
1108 10 available tasks in the kitchen environment that interacted with the same objects: turning the top
1109 burner on or off, turning the bottom burner on or off, turning the light switch on and off, open or
1110 closing the sliding cabinet, and opening and closing the hinge cabinet. The observation space consists
1111 of the robot’s state, the location of the target object, and the goal location for that object. Similar to
1112 the Meta-World CDS environment, these tasks may share behaviors navigating around the kitchen
1113 to the target object but have plenty of irrelevant behavior between tasks that interact with different
1114 objects and conflicting behaviors when opening or closing the same object.

1117 F ADDITIONAL RESULTS

1120 F.1 MULTISTAGE REACHER PER TASK RESULTS

1121 Additional results and analysis on Multistage Reacher are shown in Figure 13. QMP outperforms all
1122 the baselines in this task set, as shown in Figure 8. Task 3 receives only a sparse reward and, thus,
1123 can benefit the most from shared exploration. We observe that QMP gains the most performance
1124 boost due to selective behavior-sharing in Task 3. The No-Shared-Behavior baseline is unable to
1125 solve Task 3 at all due to its sparse reward nature. The other baselines which share uniformly suffer
1126 at Task 3, likely because they also share behaviors from other conflicting tasks, especially Task 4. We
1127 explore this further in the following Section G.

1128 For all tasks, QMP outperforms or is comparable to No-Shared-Behavior, which shows that selective
1129 behavior-sharing can help accelerate learning when task behaviors are shareable and is robust when
1130 tasks conflict. Fully-Shared-Behavior especially underperforms in Tasks 2 and 3, which require
1131 conflicting behaviors upon reaching Subgoal 1, as defined in Table 1. In contrast, it excels at the
1132 beginning of Task 0 and Task 1 as their required behaviors are completely shared. However, it suffers
1133 after Subgoal 2, as the task objectives diverge.

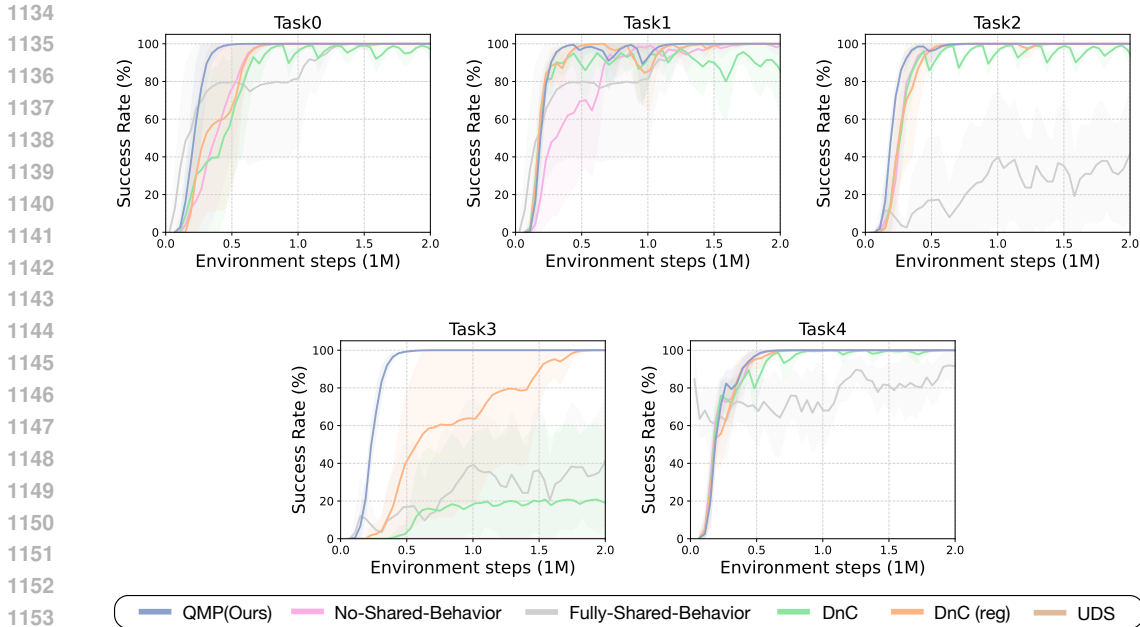


Figure 13: Success rates for individual tasks in Multistage Reacher. Our method especially helps in learning Task 3, which requires extra exploration because it only receives a sparse reward.

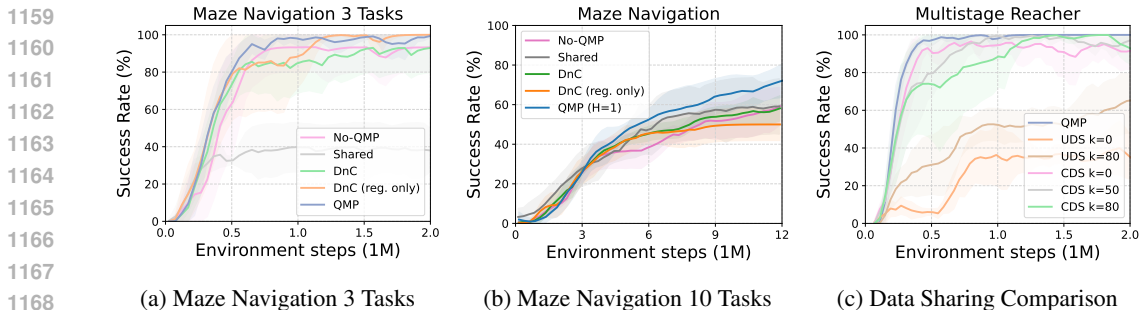


Figure 14: QMP scales well from (a) 3 tasks to (b) 10 tasks in Maze Navigation, especially in comparison to other behavior sharing methods. (c) Online data sharing is very efficient when given task reward functions (all CDS versions), but suffers without (all UDS versions).

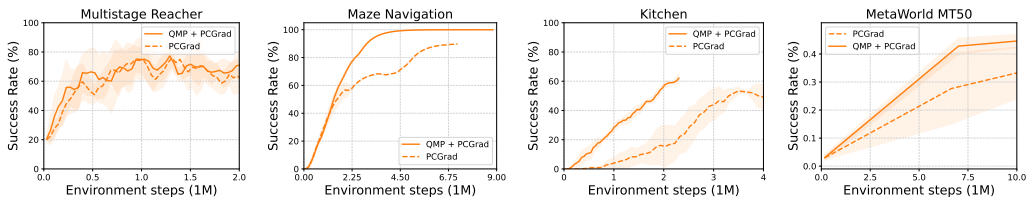
F.2 DATA SHARING RESULTS

In Figure 14c, we report multiple sharing percentiles for UDS and for CDS (Yu et al., 2021) which assumes access to ground truth task reward functions which it uses to re-label the shared data. When the shared data is relabeled with task reward functions, thereby bypassing the conflicting behavior problem, online data sharing approaches can work very well. But when unsupervised, we see that online data sharing can actually harm performance in environments with conflicting tasks, with the more conservative data sharing approach (UDS $k=80$) out-performing sharing all data. k is the percentile above with we share a transition between tasks, with higher k representing more conservative data sharing. Full details on our online UDS and CDS implementation are in Section I.6

F.3 PCGRAD RESULTS

We evaluate whether QMP can be combined with PCGrad (Yu et al., 2020) with complementary benefits. PCGrad is a popular MTRL algorithm that learns a policy with shared parameters and alleviates negative interference between tasks by modifying the multi-task gradients. We see in Figure

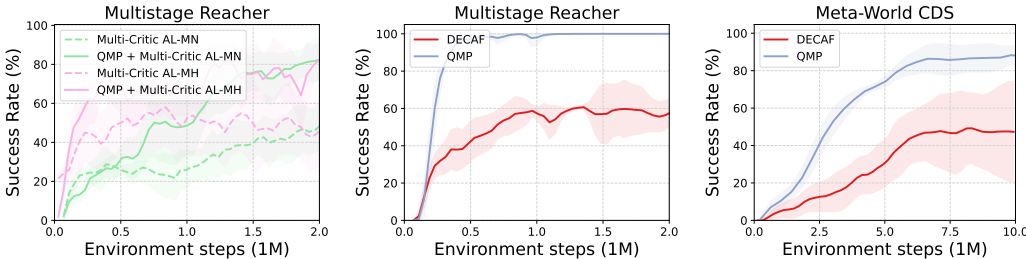
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Figure 15: Combining QMP with PCGrad yields complementary improvement in 3 out of the 4 environments we tested on. Dashed lines are PCGrad only and solid lines are QMP + PCGrad.

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(a) MCAL Comparison (b) DECAF Sharing Comparison (c) DECAF Sharing Comparison

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Figure 16: Combining our method with another parameter sharing method, MCAL, shows complementary benefits in (a). Our method outperforms DECAF in Multistage Reacher (b) and Meta-World CDS(c), demonstrating that learning to directly use Q-functions from other tasks is more challenging and sample inefficient than using the current task’s Q-function to evaluate other tasks’ policies.

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15 that QMP improves PCGrad’s performance significantly in 3 out of 4 environments and does not hurt in the last environment.

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Approach	Reacher	Maze	Kitchen	Meta-World 50
PCGrad	0.78	0.90	0.55	0.35
QMP + PCGrad	0.78	1.00	0.60	0.42

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Table 2: QMP improves performance of PCGrad across various benchmarks

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F.4 QMP SCALES WITH TASK SET SIZE IN MAZE NAVIGATION

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We look at the behavior sharing methods in the Maze Navigation task for a task set with 3 tasks (Figure 14a) and 10 tasks (Figure 14b) and see that QMP scales well from 3 to 10 tasks, even compared to other behavior sharing methods. Similar to Meta-World, we hypothesize QMP scales better with a larger task set size of similar tasks due to there being more shareable behaviors between tasks. We see that by selectively sharing behaviors, QMP is able to identify and share helpful behaviors in the larger tasks sets whereas other behavior sharing methods struggle.

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F.5 ADDITIONAL COMPARISONS

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Multi-Critic Actor Learning (MCAL) Mysore et al. (2022) is a parameter sharing MTRL method that aims to tackle potential negative interference between tasks by learning separate critics for each task while training a single multi-task actor. We evaluate the addition of QMP to two variants of MCAL, Multi-Critic AL-MN which maintains separate networks for each critic and Multi-Critic AL-MH which uses a single multi-head network for the critic, in Multistage Reacher in Figure 16a. We see that adding QMP provides around a 20% final success rate gain in both variants and is more sample efficient.

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We also compare our method with DECAF Glatt et al. (2020), a MTRL method which shared Q-functions between tasks instead of behavioral policies. DECAF learns task specific weights to linearly combine the task Q-functions which is used to train the task policy. In contrast, our method uses the task Q-function to evaluate different tasks’ policies to incorporate into the task’s behavioral

policy. Our method only modifies the data collection process, not the RL objective, and does not have a learned component. In Multistage Reacher (Figure 16b) and Meta-World CDS (Figure 16c), we see that QMP outperforms DECAF by more than 20% final success rate.

F.6 TEMPORALLY-EXTENDED BEHAVIOR SHARING

Motivated by prior work in hierarchical RL (Machado et al., 2017; Jinnai et al., 2019b;a; Hansen et al., 2019; Zhang et al., 2020) and skill learning (Pertsch et al., 2021), we explore temporally extended behavior sharing by simply following the actions of the policy π_j selected by π_{mix}^i for H steps before re-evaluating π_{mix}^i . Furthermore, a recent work Xu et al. (2024) provides theoretical results that shows myopic (ϵ -greedy) policy sharing can be sample efficient in sufficiently diverse multi-task settings, providing theoretical support for temporally extended multi-task behavior sharing in some settings. We study the effect of sharing temporally extended behaviors of length H in Maze Navigation in Figure 17, by rolling out the chosen task policy for 1, 5, 10, 25, and 50 timesteps. We see that performance improves when sharing longer behaviors (25 and 50 timesteps) which are more coherent and temporally extended. This is true even though we choose the behavioral policy greedily, only evaluating the current state s every H steps. Importantly, the guarantees from Theorem D.1 do not extend to H -step policy roll-outs and increasing H does not help in all environments. We compare the performance of No-QMP, QMP, and QMP with temporally extended behavior sharing where we choose the best performance out of $H = 10$ and $H = 25$ in Table 3 and Figure 21. Nevertheless, the impressive results in Maze suggest that multi-task temporally extended behavior sharing is worth exploring in future work.

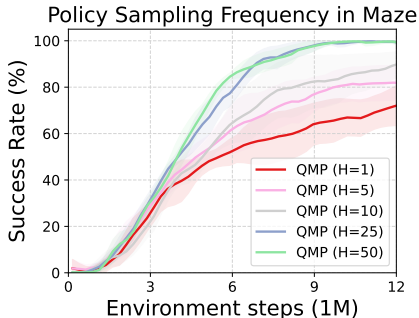


Figure 17: QMP consistently improves performance as H increases in Maze.

Table 3: Temporally Extended Behavior Sharing

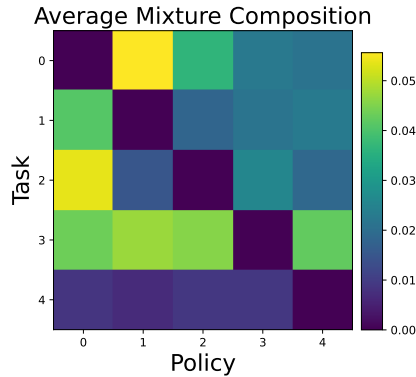
Environment	H-value	No-QMP	QMP	QMP ($H_{\zeta}1$)
Reacher	10	80 \pm 0	100 \pm 0	100 \pm 0
Maze	25	57.9 \pm 0.09	72.9 \pm 0.1	99.9 \pm 0.0
MT-CDS	10	97.5 \pm 4.5	93.7 \pm 8.5	98.8 \pm 2.0
MT10	10	79.1 \pm 5.97	89.0 \pm 0.01	82. \pm 4.48
Kitchen	10	65.5 \pm 11.0	77.3 \pm 5.3	84.5 \pm 8.7
Walker	10	3110 \pm 220	3205 \pm 218	3310 \pm 203

G QMP BEHAVIOR SHARING ANALYSIS

QMP learns to not share from conflicting tasks: We visualize the mixture probabilities per task of other policies in Figure 19 for Multistage Reacher, highlighting the conflicting Task 4 in red. Throughout the training, we see that QMP learns to generally share less behavior from Policy 4 than other policies in Tasks 0-3 and shares the least total cross-task behavior in Task 4. This supports our claim that the Q-switch can identify conflicting behaviors that should not be shared. We also note that Task 3 has a relatively larger amount of sharing than other tasks. The sparse reward nature of Task 3 makes it benefit the most from exploration via selective behavior-sharing from other tasks.

Figure 18 analyzes the effectiveness of the Q-switch in identifying shareable behaviors by visualizing the average proportion that each task policy is selected for another task over the course of training in the Multistage Reacher environment. This average mixture composition statistic intuitively analyzes whether QMP identifies shareable behaviors between similar tasks and avoids behavior sharing between conflicting or irrelevant tasks. As we expect, the Q-switch for Task 4 utilizes the least behavior from other policies (bottom row), and Policy 4 shares the least with other tasks (rightmost column). Since the agent at Task 4 is rewarded to stay at its initial position, this behavior conflicts

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1309 Figure 18: Proportion of shared behavior on Reacher Multistage averaged over training: Each cell
1310 (row i , col j) represents sharing contribution of Policy j for Task i (diagonal zeroed out for contrast).
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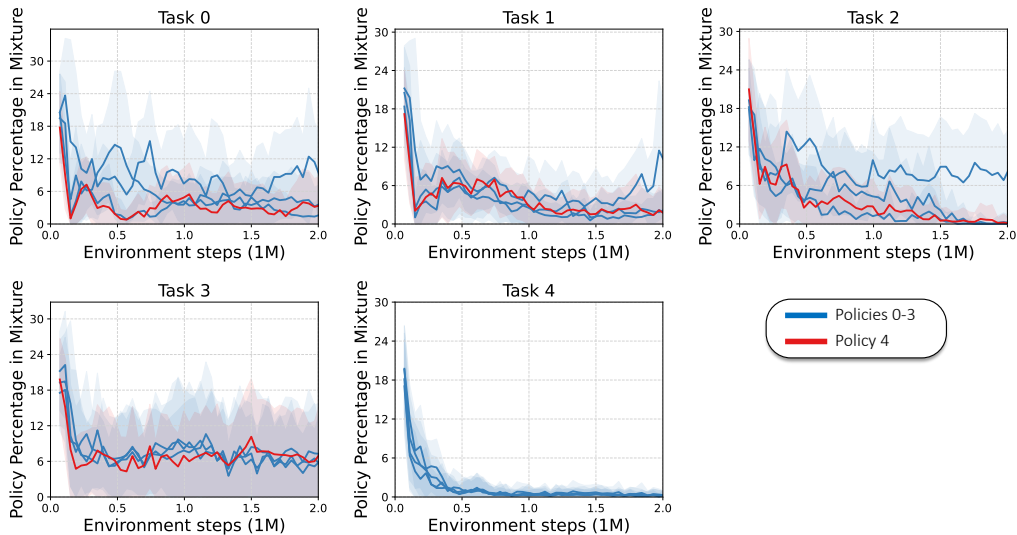
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with all the other goal-reaching tasks. Of the remaining tasks, Task 0 and 1 share the most similar goal sequence, so it is intuitive why they benefit from shared exploration and are often selected by their respective Q-switches. Finally, unlike the other tasks, Task 3 receives only a sparse reward and therefore relies heavily on shared exploration. In fact, QMP demonstrates the greatest advantage in this task (Appendix Figure 13).

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Behavior-sharing reduces over training: Figure 19 shows that the total amount of behavior-sharing decreases over the course of training in all tasks, which demonstrates a naturally arising preference in the Q-switch for the task-specific policy as it becomes more proficient at its own task.

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1340 Figure 19: Mixture probabilities per task of other policies over the course of training for Multistage
1341 Reacher. The conflicting task Policy 4, which requires staying stationary, is highlighted in red.
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G.1 QUALITATIVE VISUALIZATION OF BEHAVIOR-SHARING

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We qualitatively analyze behavior sharing by visualizing a rollout of QMP during training for the Drawer Open task in Meta-World Manipulation (Figure 9b). To generate this visualization, we use a QMP rollout during training before the policy converges to see how behaviors are shared and aid learning. For clarity, we first subsample the episodes timesteps by 10 and only report timesteps when the activated policy changes to a new one (ie. from timestep 80 to 110, QMP chose the Drawer Open policy). We qualitatively break down the episode into when the agent is approaching the drawer (top

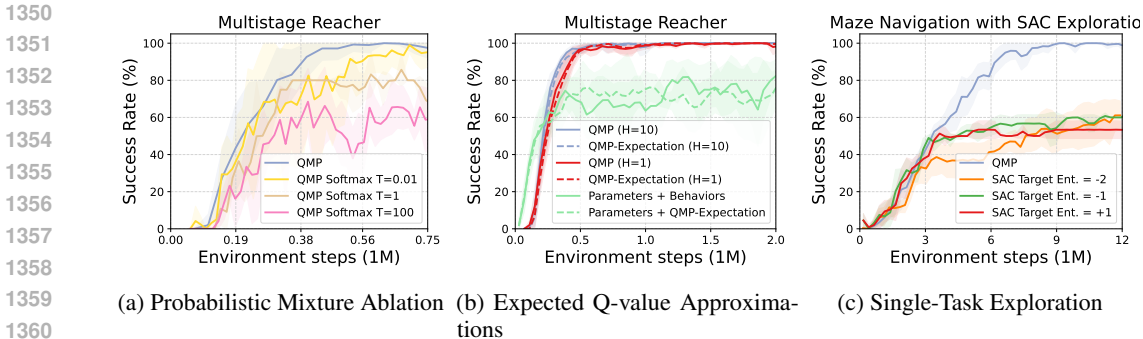


Figure 20: (a) Using probabilistic mixtures with QMP by using a softmax over Q values with temperature T, which determines the spread of the distribution. (b) Across different QMP versions, evaluating mean policy actions (solid lines) vs. sampling 10 actions to estimate expected Q-values (dashed lines) result in similar performance. (c) Single-task exploration by varying SAC target entropy. QMP reaches a higher success rate because it shares exploratory behavior **across** tasks.

row; Steps 1-60), grasping the handle (top row; Steps 61-80), and pulling the drawer open (bottom row). This allows us to see that it switches between all task policies as it approaches the drawer, uses drawer-specific policies as it grasps the handle, and opening-specific policies as it pulls the drawer open. This suggests that in addition to ignoring conflicting behaviors, QMP is able to identify helpful behaviors to share. We note that QMP is not perfect at policy selection throughout the entire rollout, and it is also hard to interpret these shared behaviors exactly because the policies themselves are only partially trained, as this rollout is from the middle of training. However, in conjunction with the overall results and analysis, this supports our claim that QMP can effectively identify shareable behaviors between tasks.

H ADDITIONAL ABLATIONS AND ANALYSIS

H.1 PROBABILISTIC MIXTURE V/S ARG-MAX

A probabilistic mixture of policies is a design choice of our approach where arg-max is replaced with softmax. However, in our initial experiments, we found no significant improvement in performance and it came with an additional hyperparameter of tuning the temperature coefficient. As we see in Figure 20a, QMP actually outperforms a probabilistic mixture over a range of softmax temperatures, justifying the design choice of argmax over softmax due to its reliable performance and simplicity.

H.2 APPROXIMATION EXPECTED Q-VALUE OVER POLICY ACTION DISTRIBUTION

QMP’s behavior policy is defined as $\pi_i^{\text{mix}} = \arg \max_{\pi_j \in \{\pi_1, \dots, \pi_N\}} \mathbb{E}_{a \sim \pi_j(s)} Q_i(s, a)$, which picks the task policy with the best expected Q value over its action distribution. We approximate the expectation by evaluating the Q-value of only the mean of each policy’s action distribution which is computationally cheaper $\pi_i^{\text{mix}} \approx \arg \max_{\pi_j \in \{\pi_1, \dots, \pi_N\}} Q_i(s, \mathbb{E}_{a \sim \pi_j(s)}[a])$. We compare this to a empirical estimate that samples 10 actions from the policy distribution and picks the policy with highest average Q-value in Figure 20b, and find no significant performance difference between the two approximations. This validates that our simple approximation works well in practice, which we hypothesize is due to the low variance of the task policies.

H.3 QMP V/S INCREASING SINGLE TASK EXPLORATION

Since QMP seeks to gather more informative training data for the task by modifying the behavioral policy, it can be viewed as a form of multi-task exploration. We briefly investigate how single task exploration differs from multi-task exploration by tuning the target entropy in SAC in Figure 20c which influences the policy entropy and therefore exploration. We see that while tuning this exploration

parameter affects the sample efficiency by more quickly learning each individual task, QMP achieves a higher final success rate by incorporating behaviors from other tasks, and therefore doing multi-task exploration. The benefit of exploration or behavior sharing algorithms specialized for multi-task RL is precisely this ability to transfer and share information between tasks.

H.4 QMP RUNTIME

While QMP does require more policy and q-function evaluations to sample from π_{mix}^i in comparison to the base RL method, these evaluations can be greatly parallelized and do not significantly increase runtime (see Figure 4) for average runtimes for our experiments). Each sample from π_{mix}^i requires querying N policy proposals and N Q-values. In QMP + Parameter-Sharing, thanks to the multihead architectures of the policy and Q-networks, all N evaluations are done in one single pass. Thus, with two passes through neural networks, we can get N action candidates and their N Q-values. Therefore, the increase in time is negligible. Even without parameter-sharing, $Q_i(s, a_j)$ evaluations can be batched $\forall j$ and the policy evaluations $\pi_j(a_j|s)$ are all independent, and can be obtained in parallel. In our implementation, we batch the Q evaluations, but do not parallelize the policy evaluations.

Table 4: Runtime Comparison

Environment	No-Sharing	QMP + No-Sharing	Parameter-Sharing	QMP + Parameter-Sharing
Reacher Multistage	12.5 hr	14.2 hr	14 hr	16.2 hr
MT50	–	–	7 days, 3hr	7 days, 6 hr

I IMPLEMENTATION DETAILS

The SAC implementation we used in all our experiments is based on the open-source implementation from Garage (garage contributors, 2019). We used fully connected layers for the policies and Q-functions with the default hyperparameters listed in Table 5. For DnC baselines, we reproduced the method in Garage to the best of our ability with minimal modifications.

We used PyTorch (Paszke et al., 2019) for our implementation. We run the experiments primarily on machines with either NVIDIA GeForce RTX 2080 Ti or RTX 3090. Most experiments take around one day or less on an RTX 3090 to run. We use the Weights & Biases tool (Biewald, 2020) for logging and tracking experiments. All the environments were developed using the OpenAI Gym interface (Brockman et al., 2016).

I.1 HYPERPARAMETERS

Table 5 details the list of important hyperparameters on all the 3 environments. For all environments, we used a 2 layer fully connected network with hidden dimension 256 and a tanh activation function for the policies and Q functions. We use a target network for the Q function with target update $\tau = 0.995$ and trained with an RL discount of $\gamma = 0.99$.

I.2 NO-SHARED-BEHAVIORS

All N networks have the same architecture with the hyperparameters presented in Table 5.

I.3 FULLY-SHARED-BEHAVIORS

Since it is the only model with a single policy, we increased the number of parameters in the network to match others and tuned the learning rate. The hidden dimension of each layer is 600 in Multistage Reacher, 834 in Maze Navigation, and 512 in Meta-World Manipulation, and we kept the number of layers at 2. The number of environment steps as well as the number of gradient steps per update were increased by N times so that the total number of steps could match those in other models. For the learning rate, we tried 4 different values (0.0003, 0.0005, 0.001, 0.0015) and chose the most

Table 5: Hyperparameters.

Hyperparameter	Multistage Reacher	Maze Navigation	Meta-World CDS
Minimum buffer size (per task)	10000	3000	10000
# Environment steps per update (per task)	1000	600	500
# Gradient steps per update (per task)	100	100	50
Batch size	32	256	256
Learning rates for π , Q and α	0.0003	0.0003	0.0015

Hyperparameter	Meta-World MT10	Walker	Kitchen
Minimum buffer size (per task)	500	2500	200
# Environment steps per update (per task)	500	1000	200
# Gradient steps per update (per task)	50	1500	50
Batch size	2560	256	1280
Learning rates for π , Q and α	0.0015	0.0003	0.0003

performant one. The actual learning rate used for each experiment is 0.0003 in Multistage Reacher and Maze Navigation, and 0.001 in Meta-World Manipulation.

This modification also applies to the Shared Multihead baseline, but with separate tuning for the network size and learning rates. In Multistage Reacher, we used layers with hidden dimensions of 512 and 0.001 as the final learning rate. In Maze Navigation, we used 834 for hidden dimensions and 0.0003 for the learning rate.

I.4 DNC

We used the same hyperparameters as in Separated, while the policy distillation parameters and the regularization coefficients were manually tuned. Following the settings in the original DnC (Ghosh et al., 2018), we adjusted the period of policy distillation to have 10 distillations over the course of training. The number of distillation epochs was set to 500 to ensure that the distillation is completed. The regularization coefficients were searched among 5 values (0.0001, 0.001, 0.01, 0.1, 1), and we chose the best one. Note that this search was done separately for DnC and DnC with regularization only. For DnC, the coefficients we used are: 0.001 in Multistage Reacher and Maze Navigation, and 0.001 in Meta-World Manipulation. For DnC with regularization only, the values are: 0.001 in Multistage Reacher, 0.0001 in Maze Navigation, and 0.001 in Meta-World Manipulation.

I.5 QMP (OURS)

Our method also uses the default hyperparameters. QMP does not require any task specific hyperparameters. The exception is Meta-World MT10, where we found it helpful to have more conservative behavior sharing by choosing the task-specific policy 70% of the time. The remaining 30% we use the Q-filter to select a policy as usual.

Like in Baseline Multihead (Parameters-Only), the QMP Multihead architecture (Parameters+Behaviors) also required a separate tuning. Since QMP Multihead effectively has one network, we increased the network size in accordance with Baseline Multihead and tuned the learning rate in addition to the mixture warmup period. The best-performing combinations of these parameters we found are 0 and 0.001 in Multistage Reacher, and 100 and 0.0003 in Maze Navigation, respectively.

I.6 ONLINE UDS

Yu et al. (2022) proposes an offline multi-task RL method (UDS) that shares data between tasks if their conservative Q value falls above the k^{th} percentile of the task data. Specifically, before training, you would go through all the tasks' data and share some data from Task j to Task i if the Task i Q

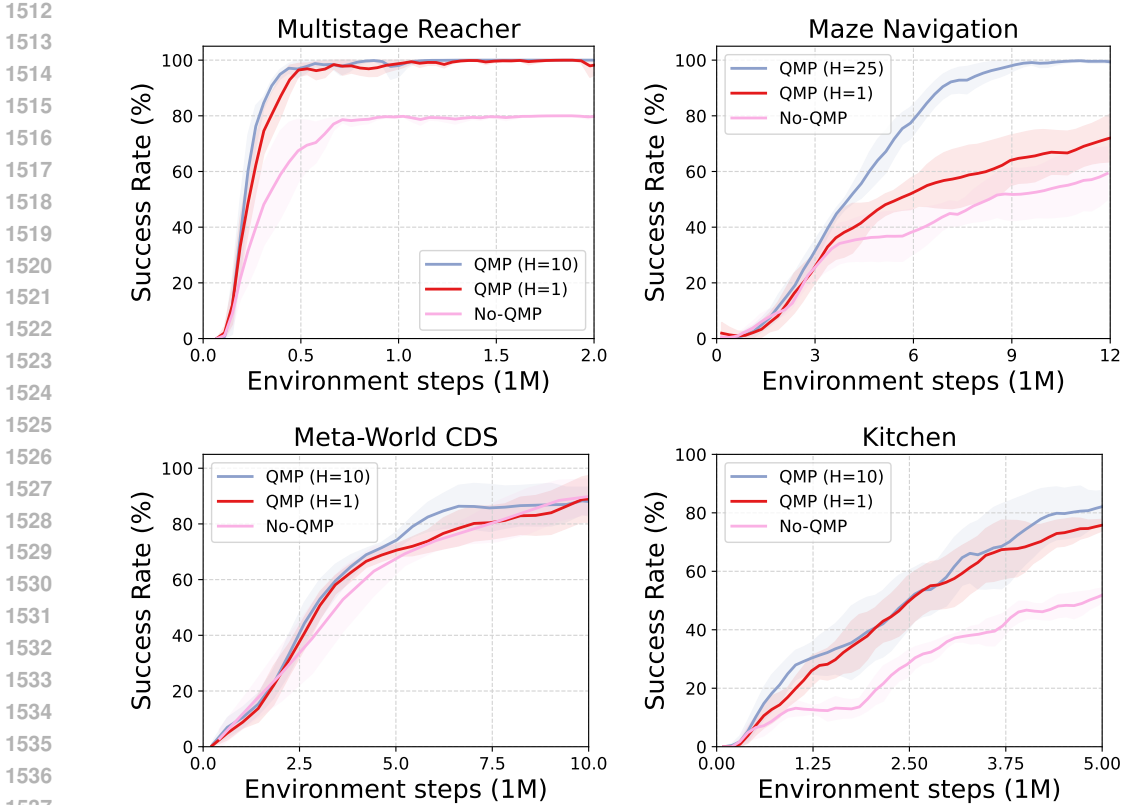


Figure 21: In each case above, QMP with H-step rollouts of the behavioral policy (blue) performs no worse than QMP with 1-step rollouts (red), with the H-step rollouts helping significantly in some tasks. Additionally both versions of QMP outperform the No-QMP baseline.

value of that data is greater than $k\%$ of the Q values of Task i 's data. UDS does not require access to task reward functions like other data-sharing approaches. It simply re-labels any shared data with the minimum task reward, making it applicable to our problem setting as we also do not assume that reward relabeling is possible.

In order to adapt UDS to online RL, instead of doing data sharing once on the given multi-task dataset, we apply UDS data sharing before every training iteration to the data in the multi-task replay buffers. Concretely, we implement this on-the-fly for every batch of sampled data by sampling one batch of data from Task i 's replay buffer, β_i , and one batch of data from the other task's replay buffers $\beta_{j \neq i}$. Then following UDS, we would form the effective batch β_i^{eff} by sharing data from $\beta_{j \neq i}$ if it falls above the k^{th} percentile of Q values for β_i :

$$\begin{aligned}
 &UDS_{\text{online}} : (s, a, r_i, s') \sim \beta_{j \neq i} \in \beta_i^{\text{eff}} \\
 &\text{if } \Delta^\pi(s, a) := \hat{Q}^\pi(s, a, i) - P_{k^{\text{th}}}[\hat{Q}^\pi(s', a', i) : s', a' \sim \beta_i] \geq 0
 \end{aligned}$$

Note the differences here: (i) the 'data' used for data-sharing is the sampled replay buffer batch instead of the offline dataset, and (ii) we use the standard Q-function to evaluate data instead of the conservative Q-function since we are doing online (not offline) RL. We implement it this way as a practical approximation to avoid having to process the entire replay buffer every training iteration.

We use the same default hyperparameters as the other baseline methods. Additionally, we need to tune the sharing percentile k . For this, we tried 0th percentile (sharing all data) and 80th percentile, and chose the best-performing one.