

CHARACTER-LEVEL ROBUSTNESS SHOULD BE REVISITED

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ABSTRACT

Adversarial attacks in Natural Language Processing apply perturbations in the character or token levels. *Token-level* attacks, gaining prominence for their use of gradient-based methods, are susceptible to altering sentence semantics, leading to invalid adversarial examples. While *character-level* attacks easily maintain semantics, they have received less attention as they cannot easily adopt popular gradient-based methods, and are thought to be easy to defend. Challenging these beliefs, we introduce *Charmer*, an efficient query-based adversarial attack capable of achieving high attack success rate (ASR) while generating highly similar adversarial examples. Our method successfully targets both small (BERT) and large (Llama 2) models. Specifically, on BERT with SST-2, *Charmer* improves the ASR in 4.84% points and the USE similarity in 8% points with respect to the previous art.

1 INTRODUCTION

Language Models (LMs) have rapidly become the go-to tools for Natural Language Processing (NLP) tasks like language translation (Sutskever et al., 2014), code development (Chen et al., 2021) and even general counseling via chat interfaces (OpenAI, 2023). However, several failures concerning robustness to natural and adversarial noise have been discovered (Belinkov and Bisk, 2018; Alzantot et al., 2018). Adversarial attacks have been widely adopted in the computer vision community to discover the worst-case performance of Machine Learning models (Szegedy et al., 2014; Goodfellow et al., 2015) or be used to defend against such failure cases (Madry et al., 2018; Zhang et al., 2019).

The application of adversarial attacks in LMs is not straight-forward due to algorithmic (Guo et al., 2021) and imperceptibility constraints (Morris et al., 2020a). Unlike the computer vision tasks, where inputs consist of tensors of real numbers, in NLP tasks, we work with sequences of discrete non-numerical inputs. This results in adversarial attacks being an NP-hard problem even for convex classifiers (Lei et al., 2019). This fact also hardens the use of popular gradient-based methods for obtaining adversarial examples (Guo et al., 2021). To tackle this problem, attackers adopt gradient based strategies in the embedding space, restricting the attack to the token vocabulary (Ebrahimi et al., 2018; Liu et al., 2022; Hou et al., 2023) or the *black-box* setting, where only input-output access to the model is assumed (Alzantot et al., 2018; Gao et al., 2018; Jin et al., 2020; Li et al., 2020; Garg and Ramakrishnan, 2020; Wallace et al., 2020).

Another difficult analogy to make with the computer vision world is imperceptibility. Adversarial examples should be by definition imperceptible, in the sense that the attack should not modify the human prediction or allow to think that an attack has been done (Szegedy et al., 2014). Given an input $\mathbf{x} \in \mathbb{R}^d$, in the numerical-input setting, imperceptibility is controlled by looking for an adversarial example $\hat{\mathbf{x}} \in \mathbb{R}^d$ in an ℓ_p ball centered at \mathbf{x} with perturbation radius ϵ , i.e., $\|\mathbf{x} - \hat{\mathbf{x}}\|_p \leq \epsilon$, where ϵ can be set arbitrarily small.

In NLP, Morris et al. (2020a) suggest different strategies for controlling imperceptibility according to the attack level:

Character: Constrain the attack to have a low Levenshtein (edit) distance. However, character-level

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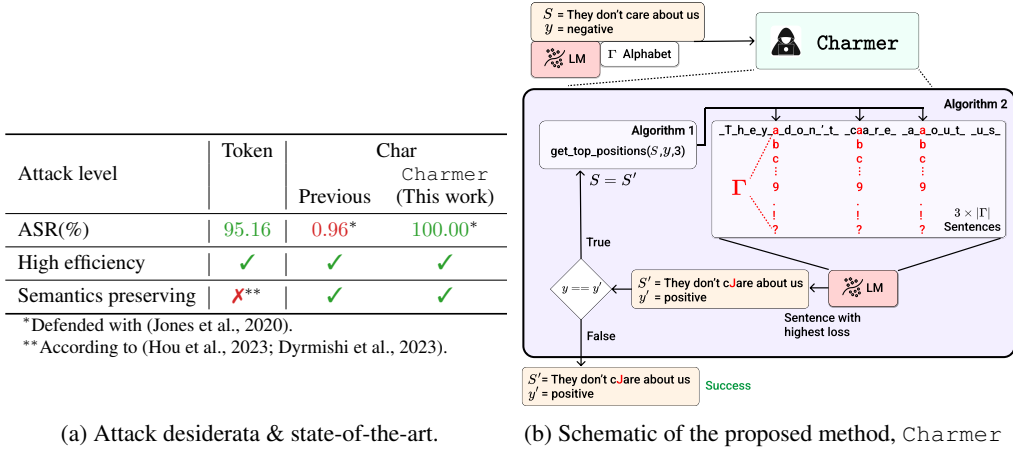


Figure 1: Desiderata and example of our attack in the sentiment classification task with the positions subset size $n = 3$. At each iteration, our attack computes the most important positions in the sentence via Algorithm 1. Then, we generate all possible sentences replacing a character in the top positions, to get the one with the highest loss. If this sentence is misclassified, the process is finished.

attacks have lost relevance due to the strength of robust word recognition defenses (Pruthi et al., 2019; Jones et al., 2020).

Token: Constrain the embedding similarity¹ of replaced words and of the overall sentence to be high. Nevertheless, Dyrnishi et al. (2023) conclude that state-of-the-art attacks do not produce imperceptible attacks in practice. To be specific, Hou et al. (2023) report 56.5% of their attacks change the semantics of the sentence.

The overall attack desiderata is summarized in Fig. 1a. Existing defenses against character-level attacks rely on robust word recognition modules, which assume the attacker adopts unrealistic constraints, not allowing simple modifications such as insertion or deletion of blank spaces, which are adopted in practice (Li et al., 2019). In this work, we revisit character-level adversarial attacks as a practical solution to imperceptibility. Our attack, Charmer, is based on a greedy approach combined with a position subset selection to further speed-up the attack, while minimally affecting performance. Our attack is able to achieve > 95% ASR in every studied TextAttack benchmark and LLMs Llama-2 and Vicuna, obtaining up to a 23%-point ASR improvement with respect to the runner-up method. We show that existing adversarial training based defenses (Hou et al., 2023) degrade character-level robustness, i.e., increasing the ASR in 3.32% points when compared to standard training. Our findings indicate typo-corrector defenses (Pruthi et al., 2019; Jones et al., 2020) are only successful when a set of strict attack constraints is assumed, if just one of these constraints is relaxed, ASR can increase from 0.96% to 98.09%. Overall, we believe character-level robustness a more consistent measure than token-level robustness.

2 METHOD

Let us now introduce our method (Charmer). In Appendices F.2 and F.3 we present our attack for both standard classifiers and LLM-based classifiers. To circumvent the exponential dependence of the number of nearby sentences on k as indicated by Corollary S6, we propose to greedily select the single-character perturbation with the highest loss Algorithm 2. Furthermore, we reduce the search space for single-character perturbations by considering a subset of locations where characters can be replaced, see Algorithm 1. In Definitions 2.1 and 2.2 we define the key operators employed in our attack.

Definition 2.1 (Expansion and contraction operators). Let $\mathcal{S}(\Gamma)$ be the space of sentences with alphabet Γ and the special character $\xi \notin \Gamma$, the pair of expansion-contraction functions $\phi : \mathcal{S}(\Gamma) \rightarrow \mathcal{S}(\Gamma \cup \{\xi\})$ and $\psi : \mathcal{S}(\Gamma \cup \{\xi\}) \rightarrow \mathcal{S}(\Gamma)$ is defined as:

¹Similarity is commonly measured via the cosine similarity of the USE embeddings (Cer et al., 2018).

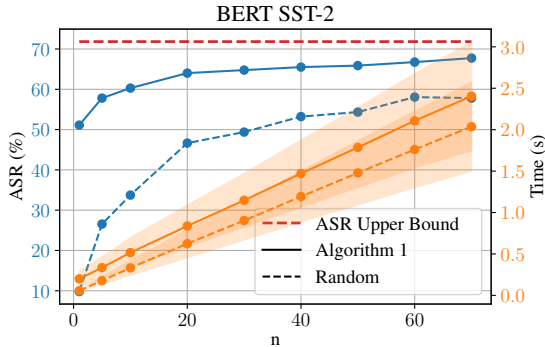


Figure 2: **Selection of the number of candidate positions:** Attack Success Rate (ASR) at $k = 1$ (● left axis) and runtime (● right axis) for our candidate position selection strategy (Algorithm 1, bold lines) and a random selection (Random, dotted lines). Our strategy improves the random baseline at a small cost ($\approx 0.25s$).

Algorithm 1 Top- n position selection.

- 1: **Inputs:** model f , sentence S , test char. t , special char. ξ , number of positions n , loss \mathcal{L} and label y .
- 2: $\mathbf{l} = \mathbf{0}$ ▷ Initialize losses with zeros
- 3: **for** $i = 1, \dots, 2|S| + 1$ **do**
- 4: $P = \phi(S)$ ▷ Expand sentence
- 5: **if** $P_i = t$ **then** $P_i \leftarrow \xi$
- 6: **else** $P_i \leftarrow t$
- 7: $l_i = \mathcal{L}(f(\psi(P)), y)$ ▷ Eval. loss
- 8: **return** Top- $n(\mathbf{l})$ ▷ Id. of Top n values

Algorithm 2 Charmer Adversarial Attack

- 1: **Inputs:** model f , sentence S , alphabet of characters Σ , max Levenshtein distance k , candidate positions n , loss function \mathcal{L} and label y .
- 2: $S' = S$ ▷ Initialize attack
- 3: **for** $i = 1, \dots, k$ **do**
- 4: $Z = \text{get_top_locations}(f, S', y, n)$ ▷ Algorithm 1
- 5: $S' = \{\psi(\phi(S') \stackrel{j}{\leftarrow} c), \forall j \in Z, \forall c \in \Sigma \cup \{\xi\}\}$ ▷ All sentences with modifications in Z
- 6: $\mathbf{l} = \mathcal{L}(f(S'), y)$ ▷ Batch of $n \cdot (|\Sigma| + 1)$ sentences
- 7: $j^* = \arg \max_{j \in [|S'|]} l_j$
- 8: $S' = S'_{j^*}$ ▷ Sentence with highest loss in the batch
- 9: **if** $\arg \max_{\hat{y} \in [o]} f(S') \neq y$ **then return** S' ▷ Successful
- 10: **return** S' ▷ Unsuccessful

$$\phi(S) := \begin{cases} \xi & \text{if } |S| = 0 \\ \xi, S_1 \oplus \phi(S_{2:}) & \text{otherwise.} \end{cases} \quad \psi(S) := \begin{cases} \emptyset & \text{if } |S| = 0 \\ \psi(S_{2:}) & \text{if } S_1 = \xi \\ S_1 \oplus \psi(S_{2:}) & \text{otherwise.} \end{cases}$$

Clearly, $\phi(S)$ inserts ξ into S in all possible positions between characters and at the beginning and end of the sentence. Similarly, $\psi(S)$ aims to remove all ξ occurred in S .

Definition 2.2 (Replacement operator). Let $S \in \mathcal{S}(\Gamma \cup \{\xi\})$, the integer $i \in [|S|]$ and the character c , the replacement operator is defined as: $S \stackrel{i}{\leftarrow} c := S_{:i-1} \oplus c \oplus S_{i+1:}$.

3 EXPERIMENTS

Our experiments are conducted in the publicly available² TextAttack models (Morris et al., 2020b) and open-source large language models including Llama 2-Chat 7B (Touvron et al., 2023) and Vicuna 7B (Chiang et al., 2023). We evaluate our attack in the text (or text pair) classification datasets SST-2 (Socher et al., 2013), RTE (Dagan et al., 2006; Wang et al., 2019), QNLI (Rajpurkar et al., 2016), MNLI-m (Williams et al., 2018) and AG-News (Gulli, 2005; Zhang et al., 2015). We provide additional experiments in the supplementary material, see Appendix E.

²<https://huggingface.co/textattack>

Table 1: **Attack evaluation in the TextAttack BERT and RoBERTa models:** Token-level and character-level attacks are highlighted with ● and ● respectively. For each metric, the best method is highlighted in **bold** and the runner-up is underlined. Charmer consistently achieves the highest Attack Success Rate (ASR), while achieving the the smallest Levenshtein distance (d_{lev}) in every case. Additionally, the similarity between the original and attacked sentences is the runner-up in all cases.

	Method	BERT				RoBERTa			
		ASR (%) \uparrow	$d_{lev}(S, S')$	Sim(S, S') \uparrow	Time (s) \downarrow	ASR (%) \uparrow	$d_{lev}(S, S')$	Sim(S, S') \uparrow	Time (s) \downarrow
AG-News	GBDA ●	42.09	17.76 \pm (9.33)	0.93 \pm (0.05)	13.86 \pm (3.14)	-	-	-	-
	BAE-R ●	17.09	15.07 \pm (10.59)	0.97 \pm (0.02)	1.61 \pm (1.36)	18.27	15.29 \pm (10.34)	0.97 \pm (0.02)	2.14 \pm (1.81)
	BERT-attack ●	29.90	20.66 \pm (16.91)	0.93 \pm (0.05)	5.58 \pm (12.92)	27.55	16.96 \pm (12.95)	0.94 \pm (0.04)	<u>1.44</u> \pm (1.76)
	DeepWordBug ●	60.51	11.75 \pm (8.00)	0.78 \pm (0.18)	0.81 \pm (0.52)	56.81	11.81 \pm (7.69)	0.79 \pm (0.16)	0.69 \pm (0.35)
	TextBugger ●	50.85	19.79 \pm (17.93)	0.90 \pm (0.06)	<u>1.53</u> \pm (1.13)	51.21	21.42 \pm (19.28)	0.90 \pm (0.06)	2.30 \pm (1.61)
	TextFooler ●	78.98	53.18 \pm (39.30)	0.84 \pm (0.11)	3.79 \pm (2.76)	84.48	52.45 \pm (36.97)	0.84 \pm (0.11)	3.84 \pm (2.77)
	TextGrad ●	85.85	55.38 \pm (30.33)	0.77 \pm (0.11)	7.98 \pm (9.24)	78.75	31.94 \pm (15.57)	0.86 \pm (0.07)	9.86 \pm (9.74)
	CWBA ●	86.72	15.71 \pm (7.17)	0.65 \pm (0.19)	174.15 \pm (130.91)	81.39	13.73 \pm (11.24)	0.86 \pm (0.11)	55.33 \pm (43.19)
	(Pruthi et al., 2019) ●	90.02	6.25 \pm (4.69)	0.86 \pm (0.14)	49.47 \pm (48.26)	88.91	6.55 \pm (5.13)	0.86 \pm (0.14)	29.75 \pm (24.53)
	Charmer-Fast (Ours) ●	<u>95.86</u>	<u>4.85</u> \pm (3.96)	0.92 \pm (0.08)	3.12 \pm (3.88)	<u>91.87</u>	<u>4.87</u> \pm (4.07)	0.91 \pm (0.09)	3.15 \pm (3.83)
	Charmer (Ours) ●	98.51	3.68 \pm (3.08)	<u>0.95</u> \pm (0.06)	8.74 \pm (11.10)	96.88	3.73 \pm (3.07)	<u>0.95</u> \pm (0.05)	9.45 \pm (11.20)
	SST-2	GBDA ●	83.37	12.20 \pm (6.94)	0.85 \pm (0.11)	9.32 \pm (1.78)	-	-	-
BAE-R ●		66.38	10.10 \pm (7.00)	0.83 \pm (0.18)	1.24 \pm (0.86)	63.16	10.22 \pm (6.33)	0.85 \pm (0.16)	0.73 \pm (0.62)
BERT-attack ●		69.57	12.19 \pm (9.55)	0.87 \pm (0.09)	239.80 \pm (1763.30)	64.21	11.26 \pm (7.18)	0.86 \pm (0.10)	18.12 \pm (32.34)
DeepWordBug ●		81.39	3.74 \pm (2.95)	0.80 \pm (0.17)	0.22 \pm (0.12)	84.27	4.61 \pm (3.47)	0.75 \pm (0.20)	0.28 \pm (0.16)
TextBugger ●		68.49	5.97 \pm (5.87)	0.91 \pm (0.06)	1.75 \pm (0.91)	61.10	6.85 \pm (6.54)	0.90 \pm (0.05)	1.82 \pm (0.97)
TextFooler ●		<u>95.16</u>	17.17 \pm (12.51)	0.82 \pm (0.15)	0.90 \pm (0.57)	95.00	17.76 \pm (12.45)	0.82 \pm (0.15)	1.16 \pm (0.76)
TextGrad ●		94.04	21.61 \pm (11.30)	0.75 \pm (0.13)	19.94 \pm (22.32)	95.49	17.07 \pm (9.57)	0.81 \pm (0.10)	3.75 \pm (2.83)
CWBA ●		72.92	8.55 \pm (3.78)	0.53 \pm (0.26)	33.81 \pm (33.86)	49.84	8.88 \pm (3.94)	0.65 \pm (0.17)	56.35 \pm (46.42)
(Pruthi et al., 2019) ●		90.94	2.22 \pm (1.35)	0.85 \pm (0.14)	4.86 \pm (4.02)	92.93	2.52 \pm (1.57)	0.84 \pm (0.14)	5.29 \pm (4.68)
Charmer-Fast (Ours) ●		100.00	<u>1.74</u> \pm (1.02)	0.89 \pm (0.13)	<u>0.34</u> \pm (0.31)	<u>99.39</u>	<u>2.29</u> \pm (1.53)	0.84 \pm (0.15)	<u>0.47</u> \pm (0.49)
Charmer (Ours) ●		100.00	1.47 \pm (0.74)	<u>0.90</u> \pm (0.11)	1.27 \pm (0.84)	99.51	1.76 \pm (1.12)	<u>0.89</u> \pm (0.12)	1.52 \pm (1.25)

Table 2: **Attack evaluation in Llama 2-Chat 7B.** Charmer-Fast outperforms baselines in terms of attack success rate, Levenshtein distance, and achieves comparable similarity and speed.

Method	SST-2				QNLI				RTE			
	ASR (%)	$d_{lev}(S, S')$	Sim(S, S')	Time	ASR (%)	$d_{lev}(S, S')$	Sim(S, S')	Time	ASR (%)	$d_{lev}(S, S')$	Sim(S, S')	Time
BAE-R ●	60.13	10.55	0.82	2.31	47.16	10.36	0.95	2.46	66.02	6.96	0.88	1.39
BERT-attack ●	57.86	12.05	0.86	1.61	60.30	14.07	0.91	2.72	<u>90.78</u>	8.77	0.82	1.41
DeepWordBug ●	50.82	<u>5.24</u>	0.73	1.01	<u>49.93</u>	<u>3.86</u>	0.88	1.24	50.97	<u>2.67</u>	0.76	0.61
TextBugger ●	41.89	8.99	0.89	1.63	58.92	10.59	0.91	<u>2.44</u>	79.61	7.76	0.80	<u>1.19</u>
TextFooler ●	<u>85.79</u>	20.91	0.79	3.54	<u>64.04</u>	18.03	0.91	4.05	86.41	8.92	<u>0.84</u>	1.73
Charmer-Fast ●	95.47	2.55	0.83	<u>1.47</u>	93.51	2.40	<u>0.93</u>	5.66	97.10	1.68	0.82	2.06

3.1 SELECTING THE NUMBER OF POSITIONS

To select the appropriate number of candidate positions n for Algorithm 1, we evaluate the ASR and runtime of the attack with $n \in \{1, 5, 10, 20, 30, 40, 50, 60, 70\}$. We conduct the experiment with the fine-tuned BERT on SST-2 from TextAttack at $k = 1$. For the SST-2 test sentences, the maximum number of positions across the dataset is 489 and the average is 213.72. We would like a value of n much smaller than these values. As a comparison, we report the ASR computed by exploring all possible positions (ASR Upper Bound). Additionally, to test the effect of our heuristic, we evaluate the performance when randomly selecting n positions (Random).

In Sec. 1, we can observe that the ASR consistently grows when increasing the number of candidate positions. However, the increase is less noticeable for $n > 20$, therefore, the increase in runtime does not pay off the increase in ASR. This leads us to choose $n = 20$ for the rest of our experiments. When compared with the random position selection, our method greatly improves the ASR for all the studied n , while introducing a minor time increase of 0.25 seconds on average.

3.2 COMPARISON AGAINST STATE-OF-THE-ART ATTACKS

In Tables 1 and 2, we can observe Charmer consistently achieves the highest ASR with $> 93\%$ in every benchmark. At the same time, our method obtains the lowest Levenshtein distance (d_{lev}). Regarding the similarity (Sim), our Charmer attains the runner up similarity in all cases, proving its ability to generate highly similar adversarial examples. With respect to time, Charmer is not as fast as the simple DeepWordBug, however, the runtime is comparable to previous state-of-the-art token-level TextGrad. If speed is preferred to adversarial example quality, we can set $n = 1$ (Charmer-Fast),

which attains a runtime closer to DeepWordBug at the cost of a higher d_{lev} and lower ASR. This phenomenon is aligned with the results of Sec. 3.1, as the ASR at $k = 1$ is lower when n is lower.

3.3 ADVERSARIAL TRAINING

In this section, we analyze the performance of models trained with adversarial training defenses (Madry et al., 2018). Following the insights of Hou et al. (2023), we use the TRADES objective (Zhang et al., 2019). We compare the use of a token-level attack, TextGrad, v.s. a character-level attack, Charmer, for solving the inner maximization problem. We use TextGrad with the recommended hyperparameters for training and Charmer with the standard hyperparameters and $k = 1$. Every 100 training steps, we measure the clean, TextFooler and Charmer ($k = 1$) adversarial accuracies. We train on 5 random initializations of BERT-base (Devlin et al., 2019) for 1 epoch in SST-2.

In Table S7 we can firstly observe that both the TextGrad and Charmer defenses improve the token-level and character-level robustness respectively when compared with the standard training baseline. This was expected as this is the objective each method is targeting. Interestingly, Charmer does not improve the token-level robustness and TextGrad hinders the character-level robustness. This observation is confirmed when looking at the training evolution in Fig. S4. It remains open to know if we should aim at character or token level robustness, nevertheless our results indicate character-level robustness is less conflicted with clean accuracy.

3.4 BYPASSING TYPO CORRECTORS

We analyze the performance of our attack with and without the PJC constraints, see Appendix E. We train the strongest typo-corrector (Pruthi et al., 2019) and use it in front of the BERT-base model from TextAttack. For the robust encoding defense we train a BERT-base model over the agglomerative clusters (Jones et al., 2020).

In Table 4, we can observe that Charmer attains 100% ASR when not considering the PJC constraints. It is only when considering PJC that robust word recognition defenses are effective. In Table S15 we analyze the effect of relaxing each of the PJC constraints while keeping the rest. We observe that by relaxing any of the LowEng, End or Start constraints, performance grows considerably for both defenses, e.g., from 0.96% to 98.09% ASR when relaxing LowEng in the robust encoding case. This result indicates that robust word recognition defenses provide a false sempsation of robustness. Together with the observations in Appendix E.1, we believe adversarial training based methods suppose a more promising avenue towards achieving character-level robustness.

4 CONCLUSION

We have proposed an efficient character-level attack based on a novel strategy to select the best positions to perturb at each iteration. Our attack (Charmer) is able to obtain close to 100% ASR both in BERT-like models and LLMs like Llama-2. Charmer defeats both token-based adversarial training defenses (Hou et al., 2023) and robust word recognition defenses (Pruthi et al., 2019; Jones et al., 2020). When integrated within adversarial training, our attack is able to improve the robustness against character-level attacks. We believe defending agains character-level attacks is an interesting open problem, with adversarial training posing as a promising avenue for defenses.

Table 3: **Adversarial Training defenses:** Charmer is an effective defense against character-level attacks, minimally affects clean accuracy and does not improve token-level robustness. On the contrary, TextGrad hinders character-level robustness and clean accuracy to improve token-level robustness.

Method	Acc. (%) \uparrow	ASR-Char (%) \downarrow	ASR-Token (%) \downarrow
Standard	92.43	<u>64.02</u>	<u>95.16</u>
Charmer ●	<u>87.20</u> $\pm(1.34)$	20.34 $\pm(1.17)$	95.17 $\pm(1.15)$
TextGrad ●	80.94 $\pm(0.60)$	<u>67.34</u> $\pm(4.87)$	71.36 $\pm(3.63)$

Table 4: **Robust word recognition defenses:** Charmer is able to break the studied defenses with 100% ASR. Robust word recognition defenses are effective only when considering PJC constraints.

Defense	Acc. (%)	PJC?	ASR (%)	$d_{lev}(S, S')$	Sim(S, S')
None	92.43	✗	100.00	1.47 $\pm(0.74)$	0.90 $\pm(0.11)$
		✓	96.65	1.86 $\pm(1.14)$	0.87 $\pm(0.14)$
(Pruthi et al., 2019)	88.53	✗	100.00	1.28 $\pm(0.51)$	0.90 $\pm(0.11)$
		✓	70.34	2.08 $\pm(1.49)$	0.85 $\pm(0.14)$
(Jones et al., 2020)	83.94	✗	100.00	1.43 $\pm(0.71)$	0.88 $\pm(0.11)$
		✓	0.96	1.14 $\pm(0.38)$	0.92 $\pm(0.06)$

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CONTENTS OF THE APPENDIX

In Appendix A we discuss the societal impact of our work. In Appendix D we provide additional background in NLP and the employed datasets. In Appendix E we provide additional experimental validation of Charmer. In Appendix G, we provide the proof of Corollary S6.

Notation: Sentences are sequences of characters in the set Γ . Sentences are denoted with uppercase letters S . For sets of sentences we use calligraphic uppercase letters \mathcal{S} . We denote the concatenation operator of two sentences as \oplus . The empty character \emptyset is defined so that sentences remain invariant to concatenations with it, i.e., $S \oplus \emptyset = S$. We use the shorthand $[n]$ for $\{1, 2, \dots, n\}$ for any positive integer n . We use bold lowercase letters for vectors $\mathbf{x} \in \mathbb{R}^d$, with the i^{th} position being $x_i \in \mathbb{R}$.

A BROADER IMPACT

In this work, we revisit character-level adversarial attacks and improve upon the prior art performance. We believe that showing that character-level attacks cannot easily be defended, is important to warn about the need of defenses. Otherwise, malicious individuals or organizations could take advantage of this unawareness. However, we note that our algorithm could empower individuals to achieve malicious purposes. We will release our code to allow defenders to assess their performance against our attack.

B RELATED WORK

We provide an overview of adversarial attacks in NLP. Adversarial attacks have been devised for producing missclassifications (Alzantot et al., 2018), generating unfaithful machine translations (Cheng et al., 2020; Sadrizadeh et al., 2023a;b; Wallace et al., 2020), providing malicious outputs (jailbreaking) (Zou et al., 2023; Zhu et al., 2023; Carlini et al., 2023) or even extracting training data (Nasr et al., 2023). We distinguish these methods in two main branches: *token-level* and *character-level* attacks.

Token based: Early token-based attacks rely in black-box token replacement/insertion strategies based on heuristics for estimating the importance of each position, and the candidate tokens for the operation (Ren et al., 2019; Jin et al., 2020; Li et al., 2020; Garg and Ramakrishnan, 2020; Lee et al., 2022). Ebrahimi et al. (2018) and Li et al. (2019) consider the token gradient information to select which token to replace. Guo et al. (2021) propose GBDA, the first, but inefficient, full gradient based text adversarial attack. TextGrad Hou et al. (2023) is a more efficient variante proposed to be integrated within Adversarial Training.

Character based: Belinkov and Bisk (2018) showcase that character-level Machine Translation models are sensible to natural character level perturbations (typos) and adversarially chosen ones. (Pruthi et al., 2019) propose to iteratively change the best possible character until success. However, this strategy can be inefficient for lengthy sentences. Addressing this issue, other methods propose pre-filtering the most important words/tokens in the sentence, to then introduce a random typo (Gao et al., 2018), or the best typo among a random sample (Li et al., 2019). In (Liu et al., 2022), a token-based attack with character-level Levenshtein distance constraints is considered. However, considering token-level information for assesing character-level importance can be suboptimal. Ebrahimi et al. (2018) propose involving embedding gradient information for evaluating the importance of characters, making the strategy only valid for character-level models. (Yang et al., 2020) evaluate the relevance of each character by masking and evaluating the loss in each position, to then modify the top positions. This strategy does not consider character insertions, and does not take into account the effect of individual changes in the importance of positions. Similarly to (Yang et al., 2020), our method measures the importance of every position plus insertions. After a perturbation is done, importances are updated to consider the interaction between perturbations.

C PROBLEM SETTING

In this section, we summarize the setting, Levenshtein distance and the operators used in our attack.

C.1 THE SENTENCE SPACE

Let Γ be the alphabet set. A sentence S with l characters (i.e., the length $|S| = l$) in Γ is defined with $S = c_1 c_2 \cdots c_l \in \Gamma^l$. For notational simplicity, we denote $S_i = c_i$ as the character in the i^{th} position and $S_{:i} = c_1 c_2 \cdots c_i$ ($S_{:i} = c_1 c_2 \cdots c_i$) as the sequence obtained by taking the characters after (before) the i^{th} position included. We denote $\mathcal{S}(\Gamma)$ as the set of (all possible) sequences with characters in Γ with length less than L . Let $d_{\text{lev}} : \mathcal{S}(\Gamma) \times \mathcal{S}(\Gamma) \rightarrow \mathbb{R}^+$ be the Levenshtein distance (Levenshtein et al., 1966), also known as the edit distance. To be specific, for any two sentences $S, S' \in \mathcal{S}(\Gamma)$, the Levenshtein distance is defined as:

$$d_{\text{lev}}(S, S') := \begin{cases} |S| & \text{if } |S'| = 0 \\ |S'| & \text{if } |S| = 0 \\ d_{\text{lev}}(S_{2:}, S'_{2:}) & \text{if } S_1 = S'_1 \\ 1 + \min \begin{cases} d_{\text{lev}}(S_{2:}, S'_{2:}) \\ d_{\text{lev}}(S_{2:}, S'_i) \\ d_{\text{lev}}(S_i, S'_{2:}) \end{cases} & \text{otherwise.} \end{cases}$$

Example S1 (d_{lev} from $S = \text{Hello}$ to several modifications.).

$$\begin{aligned} d_{\text{lev}}(\text{Hello}, \text{Helo}) &= 1 & d_{\text{lev}}(\text{Hello}, \text{Hallo}) &= 1 \\ d_{\text{lev}}(\text{Hello}, \text{Helloo}) &= 1 & d_{\text{lev}}(\text{Hello}, \text{Haloo}) &= 2. \end{aligned}$$

Note that d_{lev} represents the cost in number of character *insertions*, *deletions* and *replacements* needed for S to become equal to S' or vice-versa.

C.2 ADVERSARIAL ROBUSTNESS

In this work, we tackle robustness restricted by the Levenshtein distance. This enables the search of highly similar, hard to detect and semantics-preserving adversarial examples (Morris et al., 2020a).

Definition S2 (k -robustness at S). Denote the set of sentences at distance up to k as

$$\mathcal{S}_k(S, \Gamma) = \{S' \in \mathcal{S}(\Gamma) : d_{\text{lev}}(S, S') \leq k\}.$$

A learning model (e.g., neural networks) $f : \mathcal{S}(\Gamma) \rightarrow \mathcal{Y}$, where \mathcal{Y} is the label space, is called k -robust at S if $f(S) = f(S')$, $\forall S' \in \mathcal{S}_k(S, \Gamma)$. If $f(S) \neq f(S')$ for some $S' \in \mathcal{S}_k(S, \Gamma)$, we say S' is an *adversarial example*.

Without loss of generality, we focus on the classification task. In the adversarial robustness community, adversarial examples are usually sought by solving some optimization problem (Carlini and Wagner, 2017). Given a data sample $(S, y) \in \mathcal{S}(\Gamma) \times [o]$ and a classification model $\mathbf{f} : \mathcal{S}(\Gamma) \rightarrow \mathbb{R}^o$, with o classes, we solve:

$$\max_{S' \in \mathcal{S}_k(S, \Gamma)} \mathcal{L}(\mathbf{f}(S'), y), \tag{1}$$

where \mathcal{L} is some loss function, e.g., the cross entropy loss. In the following, we elaborate on how Eq. (1) is solved.

C.3 CHARACTERIZING THE PERTURBATIONS

To explore adversarial examples in $\mathcal{S}_k(S, \Gamma)$, we make use of the contraction, expansion (Definition 2.1) and replacement operators (Definition 2.2) to characterize this set.

Thanks to Definitions 2.1 and 2.2, it is easy to check the following proposition.

Proposition S3 (Characterization of $d_{\text{lev}}-1$ operations). *Let $S \in \mathcal{S}(\Gamma)$ be a non-empty sentence, and S' be another sentence satisfying $d_{\text{lev}}(S, S') = 1$. Then we can find $i \in [2|S| + 1]$ and a character $c \in \Gamma \cup \{\xi\}$ such that*

$$S' = \psi \left(\phi(S) \stackrel{i}{\leftarrow} c \right).$$

Remark S4 (Non-uniqueness). The parametrization of the transformation from S to S' might not be unique. For example, for $S = \text{Hello}$ and $S' = \text{Helo}$, both pairs $(i = 6, c = \xi)$ and $(i = 8, c = \xi)$ are valid parametrizations.

Remark S5 (Intuition). Replacing a character in Γ for ξ , and applying ψ results in a deletion. Similarly, replacing a ξ by a character in Γ and applying ξ results in an insertion.

Corollary S6 (Generating \mathcal{S}_k). *Let S be a non-empty sentence in the vocabulary, with $|\Gamma| > 1$, for any $k \geq 1$, the set $\mathcal{S}_k(S, \Gamma)$ (see Definition S2) can be obtained by the following recursion:*

$$\mathcal{S}_k(S, \Gamma) = \begin{cases} \left\{ \psi \left(\phi(S) \stackrel{i}{\leftarrow} c \right) \mid \begin{array}{l} \forall i \in [2|S|+1] \\ \forall c \in \Gamma \cup \{\xi\} \end{array} \right\} & , \text{if } k = 1, \\ \left\{ \psi \left(\phi(\hat{S}) \stackrel{i}{\leftarrow} c \right) \mid \begin{array}{l} \forall i \in [2|\hat{S}|+1] \\ \forall c \in \Gamma \cup \{\xi\} \\ \forall \hat{S} \in \mathcal{S}_{k-1}(S, \Gamma) \end{array} \right\} & , \text{if } k > 1. \end{cases}$$

The size of these sets is bounded as:

$$\frac{|\Gamma|^{k+1} - 1}{|\Gamma| - 1} \leq |\mathcal{S}_k(S, \Gamma)| \leq (|\Gamma| + 1)^k \cdot \prod_{j=1}^k (2(|S| + k) - 1).$$

Remark S7. In the case $|\Gamma| = 1$, for any $S \in \mathcal{S}(\Gamma) : |S| \geq k$, we trivially have that $|\mathcal{S}_k(S, \Gamma)| = 2k + 1$.

Proof. Refer to Appendix G.

Note that exactly computing $|\mathcal{S}_k(S, \Gamma)|$ is non-trivial and complex dynamic programming algorithms have been proposed for this task (Mihov and Schulz, 2004; Mitankin, 2005; Touzet, 2016). The exponential dependence of $|\mathcal{S}_k(S, \Gamma)|$ on k makes it unfeasible to evaluate every sentence in the set, therefore, smarter strategies are needed.

D ADDITIONAL BACKGROUND

We introduce additional information of the employed datasets in Appendix D.1 and about Neural Networks (NNs) for NLP in Appendix D.2.

D.1 DATASETS

In Table S6 we provide the size, classes, alphabet and examples for all the studied datasets. All of our datasets are publicly available in <https://huggingface.co/datasets>.

D.2 NN ARCHITECTURES FOR NLP

Unlike Computer Vision applications, where images can be directly fed into the NN, some pre-processing is needed in order to feed text into our models. A common practice is grouping characters into *tokens* (Webster and Kit, 1992; Palmer, 2000; Sennrich et al., 2015; Kudo and Richardson, 2018; Song et al., 2021) and assigning a vector representation (*embedding*) to each token in the text (Bengio et al., 2000; Mikolov et al., 2013; Pennington et al., 2014; Bojanowski et al., 2017). After a sequence of vector representations is obtained, an appropriate NN architecture can be used, e.g., RNNs or Transformers in an encoder and/or decoder fashion Sutskever et al. (2014); Peters et al. (2018); Devlin et al. (2019); Brown et al. (2020). Overall, the architecture will be:

$$f(S) = \hat{f}(\mathbf{G}(S)\mathbf{T}),$$

where $\mathbf{E} = \mathbf{G}(S)\mathbf{T}$ is the embedding representation of the sequence, $\mathbf{G} : \mathcal{S}(\Gamma) \rightarrow \mathcal{S}(V_{\text{tok}})$ is the tokenizer with V_{tok} as the token vocabulary and $\mathbf{T} \in \mathbb{R}^{|V_{\text{tok}}| \times d}$ is the matrix containing the embeddings of each token row-wise.

Table S5: **Attack transferability:** Adversarial examples are generated in the *Source Model* to be evaluated in the *Target Model*. For both Charmer and TextFooler, the ASR is considerably lower when the target model is different from the source model. We observe no clear difference in transfer attack performance between TextFooler and Charmer. MNLi-m and AG-News are the easiest and hardest datasets for generating transfer attacks respectively.

Attack	AG-News	MNLi-m	QNLI	RTE	SST-2																																																																																																																																																						
TextFooler	<table border="1"> <tr><td colspan="3">Target Model</td></tr> <tr><td>BERT</td><td>78.98</td><td>9.77</td><td>8.13</td></tr> <tr><td>ALBERT</td><td>6.05</td><td>76.22</td><td>6.44</td></tr> <tr><td>RoBERTa</td><td>8.07</td><td>8.92</td><td>84.48</td></tr> <tr><td colspan="3">Source Model</td></tr> <tr><td>BERT</td><td></td><td></td><td></td></tr> <tr><td>ALBERT</td><td></td><td></td><td></td></tr> <tr><td>RoBERTa</td><td></td><td></td><td></td></tr> </table>	Target Model			BERT	78.98	9.77	8.13	ALBERT	6.05	76.22	6.44	RoBERTa	8.07	8.92	84.48	Source Model			BERT				ALBERT				RoBERTa				<table border="1"> <tr><td colspan="3">Target Model</td></tr> <tr><td>BERT</td><td>92.26</td><td>34.89</td><td>29.12</td></tr> <tr><td>ALBERT</td><td>30.24</td><td>94.98</td><td>27.08</td></tr> <tr><td>RoBERTa</td><td>41.90</td><td>38.35</td><td>90.23</td></tr> <tr><td colspan="3">Source Model</td></tr> <tr><td>BERT</td><td></td><td></td><td></td></tr> <tr><td>ALBERT</td><td></td><td></td><td></td></tr> <tr><td>RoBERTa</td><td></td><td></td><td></td></tr> </table>	Target Model			BERT	92.26	34.89	29.12	ALBERT	30.24	94.98	27.08	RoBERTa	41.90	38.35	90.23	Source Model			BERT				ALBERT				RoBERTa				<table border="1"> <tr><td colspan="3">Target Model</td></tr> <tr><td>BERT</td><td>80.64</td><td>14.49</td><td>16.36</td></tr> <tr><td>ALBERT</td><td>13.72</td><td>80.72</td><td>15.05</td></tr> <tr><td>RoBERTa</td><td>17.48</td><td>17.21</td><td>76.01</td></tr> <tr><td colspan="3">Source Model</td></tr> <tr><td>BERT</td><td></td><td></td><td></td></tr> <tr><td>ALBERT</td><td></td><td></td><td></td></tr> <tr><td>RoBERTa</td><td></td><td></td><td></td></tr> </table>	Target Model			BERT	80.64	14.49	16.36	ALBERT	13.72	80.72	15.05	RoBERTa	17.48	17.21	76.01	Source Model			BERT				ALBERT				RoBERTa				<table border="1"> <tr><td colspan="3">Target Model</td></tr> <tr><td>BERT</td><td>79.60</td><td>29.52</td><td>29.17</td></tr> <tr><td>ALBERT</td><td>23.38</td><td>68.25</td><td>23.96</td></tr> <tr><td>RoBERTa</td><td>29.85</td><td>30.33</td><td>74.19</td></tr> <tr><td colspan="3">Source Model</td></tr> <tr><td>BERT</td><td></td><td></td><td></td></tr> <tr><td>ALBERT</td><td></td><td></td><td></td></tr> <tr><td>RoBERTa</td><td></td><td></td><td></td></tr> </table>	Target Model			BERT	79.60	29.52	29.17	ALBERT	23.38	68.25	23.96	RoBERTa	29.85	30.33	74.19	Source Model			BERT				ALBERT				RoBERTa				<table border="1"> <tr><td colspan="3">Target Model</td></tr> <tr><td>BERT</td><td>95.16</td><td>36.51</td><td>28.29</td></tr> <tr><td>ALBERT</td><td>28.54</td><td>95.79</td><td>19.15</td></tr> <tr><td>RoBERTa</td><td>40.12</td><td>40.64</td><td>95.00</td></tr> <tr><td colspan="3">Source Model</td></tr> <tr><td>BERT</td><td></td><td></td><td></td></tr> <tr><td>ALBERT</td><td></td><td></td><td></td></tr> <tr><td>RoBERTa</td><td></td><td></td><td></td></tr> </table>	Target Model			BERT	95.16	36.51	28.29	ALBERT	28.54	95.79	19.15	RoBERTa	40.12	40.64	95.00	Source Model			BERT				ALBERT				RoBERTa			
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E ADDITIONAL EXPERIMENTAL VALIDATION AND DETAILS

In the text pair classification tasks (MNLI-m, RTE, and QNLI), we perturb only the *hypothesis* sentence. If the length of the test dataset is more than 1,000, we restrict to the first 1,000 samples. If a test dataset is not available for a benchmark, we evaluate in the validation dataset, this is a standard practice (Morris et al., 2020b). For comparison with other attacks, we use the default hyperparameters of those methods. For Charmer we use $n = 20$ positions (see Algorithm 1) and $k = 10$ except for AG-news where we use $k = 20$ because of the much longer sentences present in the dataset. Charmer-Fast simply takes $n = 1$ to speed-up the attack. For the alphabet Σ , in order to not introduce out-of-distribution characters, we take the characters present in each evaluation dataset. All of our experiments were conducted in a machine with a single NVIDIA A100 SXM4 GPU. For better illustration between token-level and character-level attacks, we mark them with ● and ● respectively.

We compare against the following state-of-the-art attacks **(i) token level:** BAE-R (Garg and Ramakrishnan, 2020), TextFooler (Jin et al., 2020), BERT-attack (Li et al., 2020), GBDA (Guo et al., 2021) and TextGrad (Hou et al., 2023), **(ii) character level:** DeepWordBug Gao et al. (2018), TextBugger (Li et al., 2019) and CWBA Liu et al. (2022). For each attack method, we evaluate the attach success rate (ASR), the average Levenshtein distance measured at character level ($d_{lev}(S, S')$) and the cosine similarity ($\text{Sim}(S, S')$) measured as in Guo et al. (2021), i.e., computing the cosine similarity of the USE encodings (Cer et al., 2018). We evaluate the performance of the attacks in the finetuned BERT (Devlin et al., 2019) and RoBERTa (Liu et al., 2019) from TextAttack. Additional experiments with ALBERT (Lan et al., 2020) can be found in Appendix E.

We additionally test the performance of the proposed method in Llama 2-Chat 7B (Touvron et al., 2023). Additional results on Vicuna 7B (Chiang et al., 2023) are deferred to Appendix E.6. Note that in the case of LLMs, the inference process is extremely costly. As a result, we only use the fast version of Charmer, i.e., $n = 1$. Moreover, we perform an additional position selection framework to further accelerate. Specifically, we first tokenize the input sentence and mask each token to determine the most important one based on the loss. Next, we perform Algorithm 1 for the position in these important tokens. An ablation study of such token selection procedure can be found in Appendix E.6.

We analyze the performance of our attack when attacking models defended by a typo-corrector (Pruthi et al., 2019), or a robust encoding module (Jones et al., 2020). We notice the success of these defenses can be attributed by the properties of the considered attacks. In Pruthi et al. (2019); Jones et al. (2020), the studied attacks are constrained to⁴:

- NoRepeat: Not perturb the same word twice.
- First: Not perturb the first character of a word.
- Last: Not perturb the last character of a word.
- Length: Not perturb words with less than 4 chars.
- LowEng: Only insert or replace for lowercase characters in the English alphabet.

A word is anything between blank spaces. We denote these as the *Pruthi-Jones Constraints* (PJC). While these constraints aim at preserving the meaning of *every individual word* (Rawlinson, 1976; Davis, 2003), in sentence classification, we might sacrifice the meaning of a word during the attack, if the global meaning of the sentence is preserved.

E.1 ADVERSARIAL TRAINING

In this section, we analyze the performance of models trained with adversarial training defenses (Madry et al., 2018). Following the insights of Hou et al. (2023), we use the TRADES objective (Zhang et al., 2019). We compare the use of a token-level attack, TextGrad, v.s. a character-level attack, Charmer, for solving the inner maximization problem. We use TextGrad with the recommended hyperparameters for training and Charmer with the standard hyperparameters and $k = 1$. Every 100 training steps, we measure the clean, TextFooler and Charmer ($k = 1$) adversarial accuracies. We train on 5 random initializations of BERT-base (Devlin et al., 2019) for 1 epoch in SST-2.

⁴Pruthi et al. (2019), further constrain the attack by only considering replacements of nearby characters in the English keyboard.

Table S7: **Adversarial Training defenses:** Charmer is an effective defense against character-level attacks, minimally affects clean accuracy and does not improve token-level robustness. On the contrary, TextGrad hinders character-level robustness and clean accuracy to improve token-level robustness.

Method	Acc. (%) \uparrow	ASR-Char (%) \downarrow	ASR-Token (%) \downarrow
Standard	92.43	64.02	95.16
Charmer ●	$87.20_{\pm(1.34)}$	$20.34_{\pm(1.17)}$	$95.17_{\pm(1.15)}$
TextGrad ●	$80.94_{\pm(0.60)}$	$67.34_{\pm(4.87)}$	$71.36_{\pm(3.63)}$

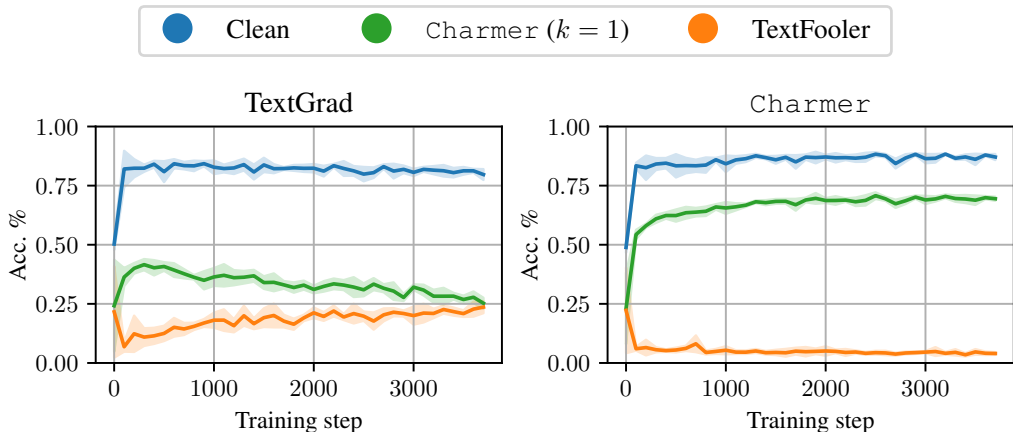


Figure S3: **Adversarial Training Evolution:** When employing Charmer as a defense, clean and character-level accuracies grow consistently through training steps, while token-level (TextFooler) accuracy is unimproved. The TextGrad defense consistently improves the token-level accuracy at the cost of hindering clean and character-level accuracy, which grow in the first ≈ 400 steps to then start decreasing.

In Table S7 we can firstly observe that both the TextGrad and Charmer defenses improve the token-level and character-level robustness respectively when compared with the standard training baseline. This was expected as this is the objective each method is targeting. Interestingly, Charmer does not improve the token-level robustness and TextGrad hinders the character-level robustness. This observation is confirmed when looking at the training evolution in Fig. S4. It remains open to know if we should aim at character or token level robustness, nevertheless our results indicate character-level robustness is less conflicted with clean accuracy.

E.2 QUALITATIVE ANALYSIS OF CHARMER

In this section we analyze the characteristics of the perturbations introduced by Charmer.

Firstly, we display the most common operations for each dataset when attacking the corresponding TextAttack BERT model. In Fig. S5 we can observe that across datasets, the most common operations correspond to insertions of punctuation marks such as paranthesis, dots, commas, question marks, percentages or dollar symbols.

Secondly, we analyze the distribution of the location of perturbations across the sentences. From Fig. S6 on the one hand, we can conclude that there is no clear region where attacks are more common for the MNLI-m, RTE and SST-2 datasets. On the other hand, for AG-News and QNLI, perturbations appear to be more common closer to the beginning of the sentence. This inclination towards perturbations in AG-News, could be explained by the fact that most sentences in AG-News start with the news header, therefore, the model might be biased towards classifying based on the header.

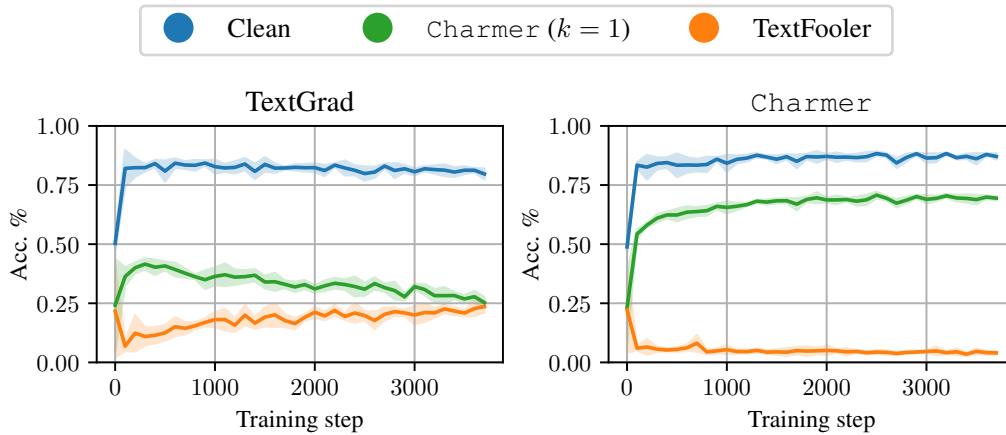


Figure S4: **Adversarial Training Evolution:** When employing Charmer as a defense, clean and character-level accuracies grow consistently through training steps, while token-level (TextFooler) accuracy is unimproved. The TextGrad defense consistently improves the token-level accuracy at the cost of hindering clean and character-level accuracy, which grow in the first ≈ 400 steps to then start decreasing.

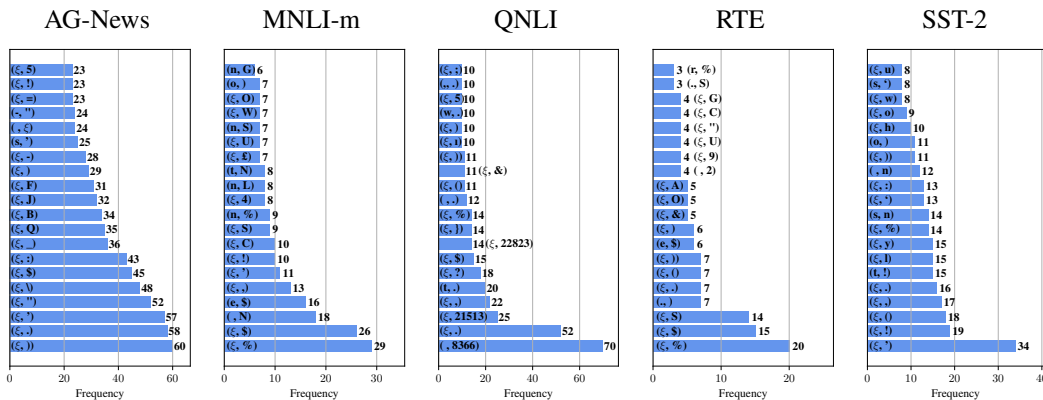


Figure S5: **Top 20 most common replacements with Charmer:** The pair of characters (c_1, c_2) indicates that c_1 is replaced by c_2 in the sentence. If $c_1 = \xi$, the replacement represents an insertion and if $c_2 = \xi$ the operation represents a deletion. The special character is denoted as ξ as the green character ξ did not appear in any of the most common operations. The most common operations are insertions of punctuation and special characters.

For completeness, we provide in Tables S8 to S12 the BERT adversarial examples provided by every attack in Table 1 in the first 3 correctly classified sentences for each dataset.

E.3 TEXTATTACK BASELINE

In this section we complement the analysis in Sec. 3.2 by reporting results for the TextAttack ALBERT models (Lan et al., 2020). Due to space reasons, we complement Table 1 with MNLI-m and RTE in Table S13

In Table S14, we can observe Charmer consistently attains the highest ASR among all the studied methods, while obtaining the lowest Levenshtein distance in 4/5 cases and highest similarity in 3/5 cases.

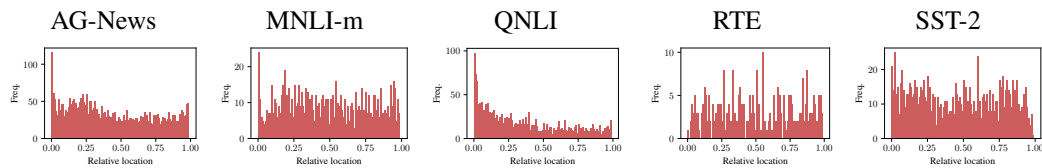


Figure S6: Distribution of the relative location of perturbations in the sentence with Charmer: 0 and 1 represent an insertion before the first character and after the last character in the sentence respectively. We do not observe any tendency in the QNLI, RTE and SST-2 datasets. For AG-News and QNLI, the perturbations in locations closer to 0 appear to be more common.

Table S8: Attack examples in the first 3 sentences of AG-News.

Method	Sentence	Prediction
Original	Fears for T N pension after talks Unions representing workers at Turner Newall say they are 'disappointed' after talks with stricken parent firm Federal Mogul.	2
TextBugger	Fears for T percent pension after conversationAssociations representing workers at Turner Newall say they are 'dsappointed' after talks with stricken parent firm Federal Mogul.	3
TextGrad	Fears for t n pension after chatcustomers representing hours at turner newall complain they are'disappointed'after chat with stricken parent provider federal mogul.	3
TextFooler	Fears for T percent pension after debateSyndicatesportrayal worker at Turner Newall say they are 'disappointed' after chats with beleaved parenting corporationsCanada Mogul.	0
DeepWordBug	Fears for T N pension after alks Unions representing workers at Turner Newall say they are 'disappointed' after talks with stricken parent firm CFederal Mogul.	2
BAE-R	Fears for T pl pension after talks Unions representing workers at Turner controls say they are 'disappointed' after talks with stricken parent firm Federal Mogul.	3
BERT-attack	Fears for T e pension after talks Unions representing workers at Turner Newall say they are 'disappointed, after discussion with stricken parent firm global Mogul.	3
GBDA	fears for t n pension after talks unions representing workers at turner newall say they are'disappointed'after talks with stricken parent knesset federal mogul'	0
CWBA	fehrs for t n pen8314ion af1408er ta322ks unl603ons representing wo248yers at tu650ner newall say they are'disaxacalanted'after ta38525ks with stfucen par12459nt firm federal mogul.	3
(Pruthi et al., 2019)	Fears for T N pension afes talks Unions representing workers at Turner Neqall say they are 'disappointed' after talks with stricken parent firm Federal Mogul.	0
Charmer	Fears for T E pension :fter talks Unions representing workers at Turner Newall say they are 'disappointed' after talks with stricken parent firm Federal Mogul.	3
Original	The Race is On: Second Private Team Sets Launch Date for Human Spaceflight (SPACE.com) SPACE.com - TORONTO, Canada - A second\team of rocketeers competing for the #36;10 million Ansari X Prize, a contest for\privately funded suborbital space flight, has officially announced the first\launch date for its manned rocket.	3
TextBugger	The Race is On: SegundoWn Team Sets InitiateStartdate for Humanitarian Spaceflight (SPACE.com) SAFCE.com - VANCOUVER, Canada - per sec60n private te4536m sets lau1410ch dal1746e for human space969light (spce. c2m) sp64257ce. c699m - tor8482nto, can8482da - a second\team of rockieaers com0sting for the # 36 ; 10 million ansari x prize992ce, a contest for\privately funded suborbital space flight, has officially announced the first\launch date for its manned rocket.	3
TextGrad	The election is on: second private party sets eva date for human spacecapsule (moon.com) space.com - paris, canada -- a fourth\trio of rocketeers seeking for the #36;10 million ansari x prize, a contest for\privately dollar suborbitapollo space jump, has openly announced the first\launch date for its young child.	0
TextFooler	The Race is Around: Second Privy Remit Set Lanza Timeline for Humanitarian Spaceflight (SEPARATION.com) SEPARATION.com - CANADIENS. Countries - para second\vaud of rocketeers suitors for the #36;10 billion Ansari X Nobel, a contestant for\covertly championed suborbital spaceship plane, had solemnly proclaim the first\begantimeline for its desolatebomb.	0
DeepWordBug	The Race is On: Second Private Tam Sets ZLaunch Date for HumJan Spaceflight (SPACE.com) SPACE.col - TORONTO, Canada - A second\team of rocketeers competing for the #3;1 million Asari X Priz, a contest for\privately ufnDED suborbitIal space flight, has officially announced the first\launch date for its manned rocket.	3
BAE-R	The Race is On: current Private Team Sets launches Date for Human Spaceflight (SPACE.com) SPACE.com - TORONTO, sa--canada second\jury of rocketeers competing for the #36;10 million Ansari X s, a contest for\privately financed suborbital space flight, has just announced the first\launch date for its proposed rocket.	3
BERT-attack	The Race is On: Second Private Team Sets landing Date for earth Spaceflight (mars.com) SPACE.com - TORONTO, Canada - is current\team of rocketeers competing for the #36;10 million Ansari X quest, a contest for\privately financed suborbital space launch, has officially announced the first\landinumber for its apollo rocket.	3
GBDA	the race is on : second private team sets launch date for human spaceflight (barack. com) continents. com - newsweek, cuba -- a second\team of rocketeers competing for the # 36 ; 10 million ansari x prize, a contest for\privately funded suborbital space flight, has officially announced the first\launch date for its manned rocket.	0
CWBA	t20234e raue is on : sec60lnd private te4536m sets lau1410ch dal1746e for human space969light (spce. c2m) sp64257ce. c699m - tor8482nto, can8482da - a second\team of rockieaers com0sting for the # 36 ; 10 million ansari x prize992ce, a contest for\privately funded suborbital space flight, has officially announced the first\launch date for its man2488ed roc20986et.	3
(Pruthi et al., 2019)	The Race is On: Second Privgte Team Sets Launch Dajte for Himan Spaceflight (SPACE.com) SPADE.com - TODONTO, Cahada - A sdcond\team of rocketees com0eting for the #36;10 million Anqari X Pfrize, a cntest for\privately funddd suborbital space flight, has officially announced the first\launch date for its mahned rocket.	3
Charmer	The Race is On: SeIond Private Team Sets LaunchDate for Tuqan Spaceflight (SPACE.com) SPADCE.0om - TORONTO, Canada U- A second\team f rocketeers competing for the #36;10 million Ansari X Prize, a contest for\PrivateB funded suborbital space flight, has officially announced 'he first\slaunch date for its manned rocket.	0
Original	Ky. Company Wins Grant to Study Peptides (AP) AP - A company founded by a chemistry researcher at the University of Louisville won a grant to develop a method of producing better peptides, which are short chains of amino acids, the building blocks of proteins.	3
TextBugger	Ky. Company Wins Subsidies to Examine Pptides (AP) APS - A company based by a chemist research1077r at the Academia of Indianapolis won a grant to develop a methodology of production best peptides, which are brief string of amino aids, the building block of proteellions.	3
TextGrad	Ky. company wins awarded to treat peptides (ab) ao - a company founded by a chemistry researcher at the time of louisville won a lead to develop a treatment of producing greater peptides, which are short chains of fatty acids, the basis blocks of muscle.	2
TextFooler	Ky. Businesses Wins Grant to Study Peptides (HAS) HAS - A company founded by a chemistry researcher at the University of Louisville won a grant to develop a method of producing better peptides, which are short chains of amino acids, the building blocks of proteins.	2
DeepWordBug	Ky. Comapny Wins Grant to SStudy Peptides (A) AP - A company foRnded by a cHemistry researcher at the University of Louisville won a grant to develoep a Cethod of proucing bette peptides, which are short Shains of amino acids, the bundling blocks of proteins.	2
BAE-R	Ky. mit Wins Grant to Study Peptides (AP) AP - biotechnology company founded by a chemistry researcher at the University of Louisville won a grant to study a method of producing better peptides, which are short chain of amino acids, the building blocks of genes.	3
BERT-attack	Ky. university Wins commission to research Peptides (AP) AP - A company owned by a chemistry lecturer at the University of ky won a grant to research a method of research better peptides, which are short chains of amino acids, the building blocks of protein.	3
GBDA	Ky. company wins grant to study peptides (ap) ap - a company founded by a chemistry researcher at the university of louisville won a grant to develop a method of producing better peptides, which are short chains of amino acids, the building blocks of proteins.	3
CWBA	ky. com1405any wi2327s gr9824nt to stjdy pep65293ides (ap) ap - a company fzonded by a chehrity ressefcher at the university of louis'ille w'n a gr12449nt to devefop a met12369od of producing better pep1110ides, which are short chains of am1074no ac1495ds, the building blocks of profcins.	1
(Pruthi et al., 2019)	Ky. Company Wins Grant to Stuvy Peptides (AP) AP - A company founded by a chemistry researcher at the UQniversity of Louisville won a grant to develop a method of producing better pepgides, which are short chains of amino aids, the building blocks of proheins.	1
Charmer	Ky. Company Wins Grant to Study Peptides (AP) APF - A company founded by a chemistry researcher at the University of Louisville won a grant to develop a method of producing better peptides, which are short chains of amino acids, the building blocks of proteins.	0

Table S9: Attack examples in the first 3 sentences of MNLi-m.

Method	Sentence	Prediction
Original	Everyone really likes the newest benefits	2
TextBugger ●	Somebody really lies the newest benefits	0
TextGrad ●	Everyone really hates the newest benefits	0
TextFooler ●	Nobody really likes the newest benefits	0
DeepWordBug ●	Everyone really yikes the newest benefits	0
BAE-R ●	nobody really likes the newest benefits	0
BERT-attack ●	Everyone really hates the newest benefits	0
GBDA ●	everyone really likes the newest misery	0
(Pruthi et al., 2019) ●	Everyone really lies the newest benefits	0
Charmer ●	Everyone really Yikes the newest benefits	0
Original	The Government Executive articles housed on the website are not able to be searched.	0
TextBugger ●	The Government Executive articles housed on the websites are not able to be searched.	2
TextGrad ●	The government executive articles housed on the website are not able to be destroyed.	2
TextFooler ●	The Government Executive articles housed on the website are not incapable to be searched.	2
DeepWordBug ●	The Government Executive articles housed on the website are not able to be sarched.	2
BAE-R ●	The Government cabinet articles housed on the website are not likely to be searched.	2
BERT-attack ●	The Government Executive articles housed on the website are not to to be visited.	2
GBDA ●	the government executive articles housed on the website are not sure to be raided.	2
(Pruthi et al., 2019) ●	The Government Executive articles housed on the website are not able to be sarched.	2
Charmer ●	The Government Executive articles housed on the website are Got able to be searched.	1
Original	I like him for the most part, but would still enjoy seeing someone beat him.	1
TextBugger ●	I like him for the most part, but would still enjoy seeing someone beat him.	1
TextGrad ●	I like him for the most cent, but would never enjoy seeing someone beat him.	0
TextFooler ●	I like him for the most portion, but would still cherishes seeing someone conquering him.	2
DeepWordBug ●	I like him for the most art, but would still enjoy seeing someone beat him.	2
BAE-R ●	I like him for the most people, but would still enjoy seeing someone beat him.	2
BERT-attack ●	I like him for the most all, but would still enjoy seeing someone beat him.	2
GBDA ●	i like him for the most part, but howard always regrets seeing someone beat him.	2
(Pruthi et al., 2019) ●	I like him for the most part, but would still enjoy sewing someone beat him.	2
Charmer ●	I like him for the most p4art, but would still enjoy seeing someone beat him.	2

Table S10: Attack examples in the first 3 sentences of QNLI.

Method	Sentence	Prediction
Original	As of that day, the new constitution heralding the Second Republic came into force.	0
TextBugger ●	As of that day, the new constitution heralding the Second Republics came into for1010e.	1
TextGrad ●	As of that day, the new constitution heralding the second republic registered into real.	1
TextFooler ●	As of that day, the new constitution heralding the Second Republics went into troupes.	1
DeepWordBug ●	As of that day, the new constitution heralding the Second Republic came into ofrce.	1
BAE-R ●	As of that document, the new constitution heralding the Second republic came into existence.	0
BERT-attack ●	As of that day, the new constitution heraldof the Second Republic came into real.	1
GBDA ●	as of that day, the new constitution heralding the second republic came into force.	0
(Pruthi et al., 2019) ●	As of that day, the new constitution heralding the Second Republic came into forde.	1
Charmer ●	As of that day, the new constitution heralding the Second Republic came into for\$ce.	1
Original	The most important tributaries in this area are the Ill below of Strasbourg, the Neckar in Mannheim and the Main across from Mainz.	1
TextBugger ●	The most important tributaries in this areas are the Ill below of Strasbourg, the Neckar in Mannheim and the Main across from Mainz.	0
TextGrad ●	The most important tributaries in this area are the ill below of strasbourg, the neckar in mannheim and the main across from cincinnati.	0
TextFooler ●	The most important tributaries in this areas are the Ill below of Strasbourg, the Neckar in Mannheim and the Main across from Mainz.	0
DeepWordBug ●	The most important tributaries in this area are the IAl below of Strasbourg, the Neckar in Mannheim and the Main across from Mainz.	0
BAE-R ●	The most important tributaries in this sector are the Ill below of Strasbourg, the Neckar in Mannheim and the Main across from Mainz.	0
BERT-attack ●	The most important tributaries in this area are the far below of Strasbourg, the Neckar in Mannheim and the Main across from Mainz.	0
GBDA ●	The most important tributaries in this area are the ill below of strasbourg, the neckar in mannheim and the jedi across from mainz.	0
(Pruthi et al., 2019) ●	The most important tributaries in this area are the Ill below of Strasbourg, the Neckar in Mannheim and the Main across from Mainz.	1
Charmer ●	The most ioportant tributaries in this area are the Ill below of Strasbourg, the Neckar in Mannheim and the Main across from Mainz.	0
Original	In most provinces a second Bachelor’s Degree such as a Bachelor of Education is required to become a qualified teacher.	1
TextBugger ●	In most provinces a s1077cond Bac1392elor’s Degrees such as a Bachelo11397 of Education is required to become a qualified teacher.	0
TextGrad ●	In most provinces a minimum bachelor’s degree such as a bachelor of education is required to become a qualified teacher.	0
TextFooler ●	ing most provinces a second Bachelor’s Grades such as a Diplomas of Tuition is required to become a qualified teacher.	0
DeepWordBug ●	I most provinces a qecond Bachelor’s Wegree such as a BFchelor of ducation is required to beome a qualified teachr.	0
BAE-R ●	In most provinces a basic Bachelor’s Degree such as a bachelor of studies is needed to become a qualified teacher.	1
BERT-attack ●	In most canadian a diploma bachelorthethe Degree such as a major of Education is required to become a qualified teacher.	0
GBDA ●	in most provinces a second bachelor’s degree such as a bachelor of education is minimum to become a qualified teacher.	0
(Pruthi et al., 2019) ●	In most provinces a second Bachelor’s Degree such as a Bachelor of Education is required to become a qualified teacher.	1
Charmer ●	In most provinces a2second Bachelor’s Degree such as a Bachelor of Education is required to become a qualified teacher.	0

Table S11: Attack examples in the first 3 sentences of RTE.

Method	Sentence	Prediction
Original	Christopher Reeve had an accident.	1
TextBugger ●	Christopher Reeve had an accident.	1
TextGrad ●	Christopher reeve had an career.	0
TextFooler ●	Valeria Reeve was an collisions.	0
DeepWordBug ●	Christopher Reeve had an accidnt.	1
BAE-R ●	karen Reeve had an accident.	1
BERT-attack ●	david Reeve had an stroke.	0
GBDA ●	christopher reeve had an stroke.	0
(Pruthi et al., 2019) ●	Christopher Reeve had an acciSdent.	1
Charmer ●	Christopher Reeve had an accidentS	0
Original	Pennsylvania has the biggest Amish community in the U.S.	1
TextBugger ●	Penn has the largest Amish community in the U.S.	0
TextFooler ●	Pennsylvania has the wide Amish community in the U.S.	0
DeepWordBug ●	Pennsylvania has the bigges Amish community in the U.S.	1
BAE-R ●	Pennsylvania has the large Amish community in the U.S.	0
BERT-attack ●	Pennsylvania has the huge Amish community in the U.S.	1
GBDA ●	pennsylvania has the strongest amish community in the state. nara geographical	0
(Pruthi et al., 2019) ●	Pennsylvania has the biggeat Amish community in the U.S.	0
Charmer ●	Pennsylvania has the biggeAt Amish community in the U.S.	0
Original	Security forces were on high alert after a campaign marred by violence.	0
TextBugger ●	Security forces were on high alert after a countryside marred by violence.	1
TextGrad ●	Security families were on high alert after a month marred by violence.	1
TextFooler ●	Security forces were on high alert after a countryside marred by violence.	1
DeepWordBug ●	Security forces were on high alert after a cmpaign marred by violence.	1
BAE-R ●	ransport force were on high alert after a campaigning marred by violence.	1
GBDA ●	security forces were on high alert after a campaign marred by marches.	1
(Pruthi et al., 2019) ●	Security forces were on high alert after a campai rn marred by violence.	1
Charmer ●	Security forces were on high alert after a2campaign marred by violence.	1

E.4 ATTACK TRANSFERABILITY

In this section we study the transferability of Charmer attacks. This is a widely studied setup in the computer vision community (Demontis et al., 2019). For each dataset, attack and model, we generate the attacked sentences and evaluate the ASR when using them for attacking other models. As a reference we take the best token-level method from Table 1, i.e., TextFooler.

In Table S5 we can observe both TextFooler and Charmer fail to produce high ASRs in the transfer attack setup. As a reference, the highest transfer ASR was 55.48% and was attained by Charmer in the MNLI-m dataset, with BERT as a Source Model and RoBERTa as the target model. We notice in the AG-News dataset it is considerably harder to produce transfer attacks, with the highest transfer ASR being 9.77% among all setups. We believe improving the ASR in the transfer attack setup is an interesting avenue.

E.5 ROBUST WORD RECOGNITION DEFENSES

To complete the analysis, we repeat the experiments in Sec. 3.4 in the RTE, MNLI-m and QNLI datasets⁵.

In Table S15 we can observe a similar phenomenon as in Table S15, i.e., robust word encoding defenses only work when assuming the attacker adopts the PJC constraints. When either the LowEng, Start or End constraints are relaxed, the ASR considerably grows close to 100%. It is worth mentioning that in the RTE dataset, defending with Jones et al. (2020) results in Charmer without any constraints achieving only 65.93% ASR. Nevertheless, this defense degrades the clean accuracy to less than 50%. If the dataset is balanced, as RTE approximately is⁶, a constant classifier can achieve 50% clean accuracy and 0% ASR. This fact shows the little value of the RTE defended model in Jones et al. (2020).

⁵The AG-News dataset is not studied in Pruthi et al. (2019); Jones et al. (2020).

⁶<https://huggingface.co/datasets/glue/viewer/rte/validation>

Table S12: Attack examples in the first 3 sentences of SST-2.

Method	Sentence	Prediction
Original	it 's a charming and often affecting journey .	1
TextBugger ●	it 's a ch593rming and often affecting voyage .	1
TextGrad ●	it's a dangerous and often affecting travelling.	0
TextFooler ●	it 's a cutie and often afflicts journey .	0
DeepWordBug ●	it 's a Wcharming and otfen affceting journey .	0
BAE-R ●	it 's a dark and often winding journey .	0
BERT-attack ●	it 's a one and often another journey .	1
GBDA ●	it's a colourful and not affecting journey.	0
CWBA ●	it's a char640ing a-d of'en affe37070ting jo1657ney.	0
(Pruthi et al., 2019) ●	it 's a chrming and often acfecting journey .	0
Charmer ●	it 's a %harming and often affecting journey .	0
Original	unflinchingly bleak and desperate	0
TextBugger ●	unflinchingly somber and desperate	1
TextGrad ●	unflinchingly dark and desperate	1
TextFooler ●	unflinchingly eerie and desperate	1
DeepWordBug ●	unflinchingly blak and desperdae	1
BAE-R ●	unflinchingly happy and desperate	1
BERT-attack ●	unflinchingly dark and desperate	1
GBDA ●	unflinchingly picturesque and desperate	1
CWBA ●	unfl30340aringly byaak ayod deshilarate	1
(Pruthi et al., 2019) ●	unflinchingly beak and deseptrate	1
Charmer ●	unflinchingly ableak and desperate	1
Original	allows us to hope that nolan is poised to embark a major career as a commercial yet inventive filmmaker .	1
TextBugger ●	allows nous to hope that nolan is poised to embark a major career as a commercial however invntive cinematographers .	0
TextGrad ●	allows us to argue that nolan is ineligible to embark a major career as a commercial fails inventive filmmaker.	0
TextFooler ●	allows ourselves to hope that nolan is poised to embarked a severe career as a commercial yet noveltysuperintendent .	0
DeepWordBug ●	allows Gs to hope that nolan is Loised to embark a major career as a commercial yet invewntive filmmaker .	0
BAE-R ●	allows it to hope that nolan is poised to assume a major career as a commercial yet amateur filmmaker .	1
BERT-attack ●	allows to hope that nolan is eligible to embark a major career as a commercial yet inventexperienced filmmaking .	0
GBDA ●	allows us to doubt that nolan is poised to embark a major career as a commercial lower inventive writer.	0
CWBA ●	all21335ws us to ho26954e that nolan is po2313sed to embark a major career as a commbecial y1705t inventive filmmaker.	0
(Pruthi et al., 2019) ●	allows us to hope that nolan is poised to ebark a major career as a commercial yet infentive filmmaker .	0
Charmer ●	allows us to hope that no\$an is poised to embark a major career as a commercial yet inventive filmmaker .	0

Table S13: Attack evaluation in the TextAttack BERT and RoBERTa models in QNLI, MNLI-m and RTE.

Method	BERT				RoBERTa				
	ASR (%) \uparrow	$d_{lev}(S, S')$ \downarrow	Sim(S, S') \uparrow	Time (s) \downarrow	ASR (%) \uparrow	$d_{lev}(S, S')$ \downarrow	Sim(S, S') \uparrow	Time (s) \downarrow	
MNLI-m	GBDA	97.97	11.45 \pm (6.52)	0.73 \pm (0.16)	11.68 \pm (3.23)	-	-	-	-
	BAE-R	70.00	6.46 \pm (3.32)	0.83 \pm (0.15)	0.53 \pm (0.44)	67.39	6.47 \pm (3.31)	0.84 \pm (0.14)	0.54 \pm (0.37)
	BERT-attack	92.41	6.95 \pm (6.57)	0.83 \pm (0.13)	26.53 \pm (204.23)	97.62	6.56 \pm (4.16)	0.83 \pm (0.14)	2.60 \pm (15.58)
	DeepWordBug	84.88	2.30 \pm (1.68)	0.75 \pm (0.18)	0.23 \pm (0.12)	78.41	2.79 \pm (2.02)	0.71 \pm (0.21)	0.27 \pm (0.15)
	TextBugger	85.36	4.17 \pm (4.33)	0.83 \pm (0.13)	0.44 \pm (0.32)	86.36	5.41 \pm (5.40)	0.80 \pm (0.15)	0.51 \pm (0.38)
	TextFooler	92.26	9.83 \pm (6.87)	0.82 \pm (0.14)	0.52 \pm (0.41)	90.23	10.50 \pm (7.79)	0.81 \pm (0.14)	0.54 \pm (0.42)
	TextGrad	93.69	9.98 \pm (5.66)	0.75 \pm (0.13)	2.50 \pm (1.97)	95.44	9.10 \pm (5.30)	0.79 \pm (0.12)	3.56 \pm (2.83)
	(Pruthi et al., 2019)	57.62	1.32 \pm (0.64)	0.83 \pm (0.12)	4.48 \pm (3.73)	52.84	1.36 \pm (0.63)	0.82 \pm (0.13)	7.48 \pm (6.49)
	Charmer-Fast (Ours)	100.00	1.23 \pm (0.58)	0.85 \pm (0.14)	0.21 \pm (0.17)	100.00	1.36 \pm (0.78)	0.82 \pm (0.15)	0.23 \pm (0.19)
	Charmer (Ours)	100.00	1.14 \pm (0.42)	0.85 \pm (0.13)	1.45 \pm (0.81)	100.00	1.17 \pm (0.46)	0.84 \pm (0.13)	1.49 \pm (0.82)
QNLI	GBDA	47.16	11.88 \pm (7.02)	0.93 \pm (0.06)	13.85 \pm (2.94)	-	-	-	-
	BAE-R	40.04	11.44 \pm (8.30)	0.95 \pm (0.07)	2.31 \pm (2.36)	41.66	10.37 \pm (9.05)	0.96 \pm (0.04)	2.18 \pm (2.77)
	BERT-attack	70.21	16.21 \pm (12.44)	0.90 \pm (0.08)	239.86 \pm (1395.15)	70.65	17.78 \pm (13.28)	0.89 \pm (0.12)	2.70 \pm (12.58)
	DeepWordBug	71.57	4.52 \pm (4.04)	0.86 \pm (0.15)	0.50 \pm (0.34)	64.34	5.07 \pm (4.67)	0.85 \pm (0.17)	0.59 \pm (0.41)
	TextBugger	75.77	8.16 \pm (9.93)	0.89 \pm (0.10)	0.99 \pm (0.78)	67.39	9.08 \pm (10.31)	0.90 \pm (0.10)	0.90 \pm (0.72)
	TextFooler	80.64	23.42 \pm (21.56)	0.87 \pm (0.12)	1.90 \pm (1.70)	76.01	25.74 \pm (28.53)	0.87 \pm (0.12)	2.00 \pm (2.09)
	TextGrad	77.35	30.03 \pm (20.41)	0.82 \pm (0.10)	4.54 \pm (3.82)	76.80	21.56 \pm (15.74)	0.87 \pm (0.08)	5.80 \pm (4.58)
	(Pruthi et al., 2019)	17.70	1.57 \pm (0.81)	0.93 \pm (0.07)	7.22 \pm (4.91)	17.45	1.54 \pm (0.88)	0.93 \pm (0.08)	7.46 \pm (5.33)
	Charmer-Fast (Ours)	94.69	2.21 \pm (1.69)	0.93 \pm (0.09)	1.33 \pm (1.55)	96.95	2.73 \pm (2.15)	0.90 \pm (0.12)	1.72 \pm (2.27)
	Charmer (Ours)	97.68	1.94 \pm (1.48)	0.94 \pm (0.07)	9.19 \pm (9.60)	97.86	2.20 \pm (1.69)	0.92 \pm (0.08)	10.55 \pm (9.69)
RTE	GBDA	76.62	8.99 \pm (4.74)	0.78 \pm (0.13)	16.71 \pm (7.29)	-	-	-	-
	BAE-R	64.68	6.98 \pm (3.39)	0.87 \pm (0.09)	0.84 \pm (0.65)	64.06	6.11 \pm (3.84)	0.89 \pm (0.08)	0.76 \pm (0.69)
	BERT-attack	68.00	10.06 \pm (9.75)	0.78 \pm (0.19)	23.67 \pm (51.78)	31.34	6.00 \pm (3.96)	0.86 \pm (0.08)	5.36 \pm (20.47)
	DeepWordBug	65.67	1.64 \pm (0.82)	0.85 \pm (0.10)	0.12 \pm (0.03)	62.67	1.83 \pm (1.09)	0.82 \pm (0.14)	0.13 \pm (0.04)
	TextBugger	74.13	3.38 \pm (3.48)	0.88 \pm (0.09)	0.35 \pm (0.18)	71.43	3.91 \pm (3.73)	0.89 \pm (0.08)	0.38 \pm (0.40)
	TextFooler	79.60	7.42 \pm (6.10)	0.88 \pm (0.09)	0.47 \pm (0.59)	74.19	7.68 \pm (5.94)	0.88 \pm (0.09)	0.47 \pm (0.59)
	TextGrad	81.77	10.02 \pm (5.69)	0.76 \pm (0.13)	2.44 \pm (1.06)	73.97	6.40 \pm (3.30)	0.84 \pm (0.08)	3.57 \pm (3.61)
	(Pruthi et al., 2019)	62.19	1.18 \pm (0.41)	0.86 \pm (0.08)	8.45 \pm (6.25)	49.31	1.21 \pm (0.54)	0.87 \pm (0.08)	12.23 \pm (8.84)
	Charmer-Fast (Ours)	89.55	1.36 \pm (0.93)	0.87 \pm (0.12)	0.29 \pm (0.27)	91.71	1.78 \pm (1.71)	0.82 \pm (0.15)	0.41 \pm (0.54)
	Charmer (Ours)	97.01	1.55 \pm (1.42)	0.86 \pm (0.13)	2.50 \pm (2.33)	97.24	1.61 \pm (1.39)	0.85 \pm (0.13)	2.74 \pm (2.87)

E.6 ATTACK OF LLM CLASSIFIER

The prompt design in attacking different LLMs is summarized in Table S18. A schematic of attacking LLMs is present in Fig. S7. In this experiment, we use token-based position selection to further accelerate the process of attack. Specifically, we mask each token in the inputs and select the top ten tokens with the highest loss. Since some tokens consist of many characters, we only use 40 positions of these tokens to perform Algorithm 1. The remaining step is the same as in Algorithm 2. Notably, in Table S16, we see that such a process can significantly accelerate the attack while maintaining the performance of ASR and other metrics. The result on Vicuna 7B is present in Table S17, where we can see the proposed Charmer achieves much higher ASR than other baselines with less edit distance.

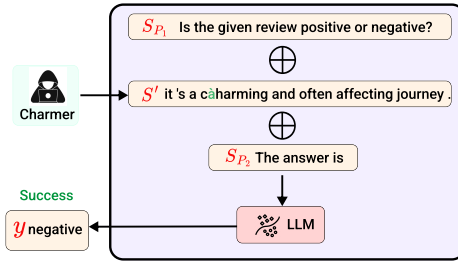


Figure S7: Schematic of the proposed Charmer in attacking LLM-classifiers. Charmer modifies the input to S' with a small perturbation (annotated in green color) to the original input so that the model produces the desired output y . S_{P_1} and S_{P_2} are auxiliary prompts that remain unchanged during the attack.

Table S14: **Attack evaluation in the TextAttack ALBERT models:** Token-level and character-level attacks are highlighted with ● and ● respectively. for each metric, the best method is highlighted in **bold** and the runner-up in underlined. Charmer consistently achieves highest Attack Success Rate (ASR).

	Method	ALBERT			
		ASR (%) \uparrow	$d_{lev}(S, S') \downarrow$	Sim(S, S') \uparrow	Time (s) \downarrow
AG-News	CWBA ●	57.96	22.69 \pm (21.07)	0.64 \pm (0.22)	205.69 \pm (162.00)
	BAE-R ●	18.26	15.15 \pm (11.28)	0.97 \pm (0.02)	1.84 \pm (1.70)
	BERT-attack ●	37.23	21.34 \pm (15.29)	0.93 \pm (0.05)	2.41 \pm (2.14)
	DeepWordBug ●	56.90	9.77 \pm (6.77)	0.83 \pm (0.14)	0.73 \pm (0.40)
	TextBugger ●	71.76	17.48 \pm (16.82)	0.91 \pm (0.06)	<u>1.38</u> \pm (0.98)
	TextFooler ●	76.22	46.51 \pm (35.21)	0.87 \pm (0.10)	3.89 \pm (3.11)
	TextGrad ●	75.37	42.43 \pm (19.05)	0.85 \pm (0.07)	8.23 \pm (9.15)
	(Pruthi et al., 2019) ●	88.00	5.50 \pm (4.74)	0.89 \pm (0.13)	29.17 \pm (25.58)
	Charmer-Fast ●	<u>95.44</u>	<u>3.25</u> \pm (2.88)	<u>0.95</u> \pm (0.06)	2.38 \pm (3.27)
	Charmer ●	97.13	2.45 \pm (2.31)	0.97 \pm (0.04)	6.94 \pm (12.33)
MNL1-m	BAE-R ●	71.57	6.28 \pm (3.27)	0.84 \pm (0.14)	0.54 \pm (0.34)
	BERT-attack ●	97.50	7.14 \pm (5.17)	0.84 \pm (0.12)	2.96 \pm (16.16)
	DeepWordBug ●	85.90	2.31 \pm (1.63)	0.77 \pm (0.17)	<u>0.27</u> \pm (0.13)
	TextBugger ●	88.05	4.86 \pm (4.64)	0.82 \pm (0.13)	0.55 \pm (0.38)
	TextFooler ●	94.98	9.49 \pm (6.45)	0.82 \pm (0.13)	0.55 \pm (0.40)
	TextGrad ●	94.15	8.96 \pm (4.90)	0.79 \pm (0.12)	2.33 \pm (1.63)
	(Pruthi et al., 2019) ●	58.18	1.26 \pm (0.57)	0.84 \pm (0.11)	5.14 \pm (5.25)
	Charmer-Fast ●	100.00	<u>1.17</u> \pm (0.42)	<u>0.85</u> \pm (0.13)	0.22 \pm (0.15)
	Charmer ●	100.00	1.08 \pm (0.28)	0.86 \pm (0.11)	1.53 \pm (0.70)
	QNLI	BAE-R ●	45.97	10.94 \pm (7.57)	0.95 \pm (0.06)
BERT-attack ●		73.40	16.74 \pm (16.94)	0.90 \pm (0.10)	760.09 \pm (5904.67)
DeepWordBug ●		74.07	5.00 \pm (4.36)	0.85 \pm (0.16)	0.57 \pm (0.43)
TextBugger ●		76.03	9.59 \pm (11.48)	0.90 \pm (0.10)	<u>1.15</u> \pm (0.99)
TextFooler ●		80.72	22.56 \pm (20.96)	0.88 \pm (0.11)	2.13 \pm (2.00)
TextGrad ●		74.78	28.47 \pm (17.98)	0.84 \pm (0.09)	5.78 \pm (6.02)
(Pruthi et al., 2019) ●		26.47	<u>1.85</u> \pm (1.18)	0.93 \pm (0.09)	10.12 \pm (8.49)
Charmer-Fast ●		<u>96.19</u>	2.26 \pm (1.74)	0.93 \pm (0.08)	1.58 \pm (2.36)
Charmer ●		96.23	1.78 \pm (1.11)	<u>0.94</u> \pm (0.07)	9.60 \pm (8.10)
RTE		BAE-R ●	61.14	6.69 \pm (3.43)	<u>0.88</u> \pm (0.09)
	BERT-attack ●	9.80	5.20 \pm (2.95)	0.86 \pm (0.16)	21.39 \pm (34.86)
	DeepWordBug ●	59.24	1.54 \pm (0.84)	0.84 \pm (0.13)	0.13 \pm (0.05)
	TextBugger ●	70.62	4.45 \pm (5.24)	0.87 \pm (0.11)	0.44 \pm (0.33)
	TextFooler ●	68.25	7.60 \pm (5.61)	0.89 \pm (0.09)	0.52 \pm (0.65)
	TextGrad ●	70.70	7.07 \pm (3.25)	0.83 \pm (0.10)	2.56 \pm (2.28)
	(Pruthi et al., 2019) ●	48.34	1.22 \pm (0.41)	0.86 \pm (0.09)	11.56 \pm (7.69)
	Charmer-Fast ●	<u>97.16</u>	1.68 \pm (1.32)	0.83 \pm (0.14)	<u>0.42</u> \pm (0.44)
	Charmer ●	100.00	<u>1.29</u> \pm (0.65)	0.87 \pm (0.10)	2.49 \pm (2.13)
	SST-2	CWBA ●	77.88	11.18 \pm (4.58)	0.55 \pm (0.25)
BAE-R ●		62.77	10.25 \pm (7.24)	0.85 \pm (0.16)	0.78 \pm (0.77)
BERT-attack ●		72.34	11.57 \pm (6.89)	0.85 \pm (0.10)	148.11 \pm (1077.71)
DeepWordBug ●		84.78	3.37 \pm (2.47)	0.82 \pm (0.16)	0.23 \pm (0.12)
TextBugger ●		72.52	5.61 \pm (5.51)	0.91 \pm (0.06)	1.85 \pm (0.90)
TextFooler ●		95.79	15.79 \pm (11.12)	0.83 \pm (0.14)	1.11 \pm (0.74)
TextGrad ●		96.28	18.67 \pm (9.73)	0.80 \pm (0.11)	2.95 \pm (1.65)
(Pruthi et al., 2019) ●		95.05	1.98 \pm (1.28)	0.87 \pm (0.13)	4.66 \pm (3.98)
Charmer-Fast ●		<u>99.88</u>	<u>1.62</u> \pm (0.88)	<u>0.89</u> \pm (0.12)	<u>0.38</u> \pm (0.34)
Charmer ●		100.00	1.38 \pm (0.67)	0.91 \pm (0.10)	1.38 \pm (0.93)

Table S15: **Effect of each PJC constraint:** Charmer ASR when individually removing each constraint while keeping the rest. Performance with no constraints (None) put as reference. The ASR drastically increases when removing the LowEng, End or Start constraints, proving the fragility of existing robust word recognition defenses.

Defense	Attack constraint	SST-2		RTE		MNLI-m		QNLI	
		Acc. (%)	ASR	Acc. (%)	ASR (%)	Acc. (%)	ASR (%)	Acc. (%)	ASR (%)
(Pruthi et al., 2019)	None		100.00		92.17		100.00		86.38
	PJC		70.34		42.17		87.39		43.05
	-LowEng		99.22		70.48		97.90		65.53
	-Length	88.53	74.61	60.36	45.78	76.33	92.51	73.55	46.19
	-End		93.91		63.86		96.19		57.63
	-Start		98.58		69.88		97.11		57.08
	-NoRepeat		74.09		42.17		89.36		42.51
(Jones et al., 2020)	None		100.00		65.93		100.00		98.56
	PJC		0.96		2.96		2.93		1.05
	-LowEng		98.09		57.04		96.63		94.62
	-Length	83.94	0.96	48.74	2.96	68.44	2.93	76.20	0.79
	-End		71.72		44.44		75.26		54.99
	-Start		88.93		47.41		82.87		67.32
	-NoRepeat		5.46		6.67		9.81		3.81

Table S16: Ablation study on the time efficiency of different methods of position selection in Llama 2-Chat 7B. We choose the fast version of Charmer with $n = 1$ and $k = 10$. The result shows that combing Algorithm 1 with a token-based pre-selection procedure can notably improve the efficiency of the proposed Charmer.

	Method	ASR (%)	$d_{lev}(S, S')$	$Sim(S, S')$	Time
SST-2	Charmer-Fast (Token-based Algorithm 1)	95.47	2.55	0.83	1.47
	Charmer-Fast (Algorithm 1)	95.60	2.56	0.85	3.32
QNLI	Charmer-Fast (Token-based Algorithm 1)	93.51	2.40	0.93	5.66
	Charmer-Fast (Algorithm 1)	96.82	2.34	0.94	10.30
RTE	Charmer-Fast (Token-based Algorithm 1)	97.10	1.68	0.82	2.06
	Charmer-Fast (Algorithm 1)	98.07	1.64	0.84	2.63

E.7 JAILBREAKING LLM

Disclaimer: this attack can lead to harmful content

In this section, we showcase that the proposed method can also be applied to jailbreaking LLMs, which refers to designing prompts to allow LLMs to output harmful content. We compare against the recent jailbreaking attacks GCG (Zou et al., 2023) and AutoDAN (Liu et al., 2023) in the AdvBench benchmark (Zou et al., 2023). First, we overview the formulation of jailbreaking LLM. Given a harmful query S , the goal of jailbreaking is to make the model answer certain query S even when the safety system prompt S_{system} is provided, see Fig. 1b for an illustration of S_{system} . Formally, our attacker aims to find an adversarial example S' based on S such that:

$$\max_{S' \in \mathcal{S}_k(S, \Sigma)} \mathcal{L}(f(S_{\text{system}} \oplus S'), y) := \max_{S' \in \mathcal{S}_k(S, \Sigma)} \mathbb{P}(y | S_{\text{system}} \oplus S')$$

where \mathcal{L} is defined as the probability of generating the target $y := \text{“Sure, here is”} \oplus S$. For example, if S is “how to make a bomb”, then y is “Sure, here is how to make a bomb”.

In this experiment, we use the Advbench dataset proposed by Zou et al. (2023), which consists of harmful and toxic sentences across different topics. Due to the costly computational budget of attacking LLMs, we only use the first 50 sentences in the dataset. We compare the proposed Charmer against the white-box attack GCG Zou et al. (2023) and black-box attack AutoDAN Liu et al. (2023). We adopt the same hyper-parameters of LLM and criterion of success as in Zou et al. (2023). The result in Table S19 shows that Charmer can pass the safety alignment process of LLMs with much less change in terms of Levenshtein distance.

Table S17: **Attack evaluation in Vicuna 7B:** We choose the fast version of Charmer with $n = 1$ and $k = 10$. Charmer outperforms baselines in terms of attack success rate, Levenshtein distance, and achieves comparative similarity and speed.

	Method	ASR (%)	$d_{lev}(S, S')$	$Sim(S, S')$	Time
ONLI	BAE-R ●	40.66	12.36	0.96	3.11
	BERT-attack ●	56.67	16.61	0.91	4.03
	DeepWordBug ●	43.77	3.63	0.91	1.32
	TextBugger ●	53.11	9.08	0.93	2.56
	TextFooler ●	51.28	20.70	0.92	4.76
	Charmer-Fast ●	98.35	2.04	0.94	4.89
RTE	BAE-R ●	64.11	5.96	0.89	1.23
	BERT-attack ●	82.78	8.92	0.82	1.60
	DeepWordBug ●	50.97	2.67	0.76	0.61
	TextBugger ●	71.77	6.63	0.84	1.12
	TextFooler ●	78.47	7.94	0.86	1.64
	Charmer-Fast ●	89.05	1.56	0.85	1.98
SST-2	BAE-R ●	43.22	14.29	0.75	3.28
	BERT-attack ●	32.31	13.21	0.85	2.42
	DeepWordBug ●	30.72	4.22	0.76	0.88
	TextBugger ●	23.01	9.97	0.88	1.73
	TextFooler ●	64.04	18.03	0.91	4.05
	Charmer-Fast ●	91.89	2.47	0.85	1.66

Table S18: Prompting in different LLMs and datasets. The sentences outside “[Input]” are considered as auxiliary prompts S_{P_1} and S_{P_2} , as demonstrated in Fig. S7.

Model	Dataset	Prompt design
Llama 2-Chat 7B	SST-2	Is the given review positive or negative? [Input] The answer is
	RTE	[Input premise] Based on the paragraph above can we conclude the following sentence, answer with yes or no. [Input hypothesis] The answer is
	QNLI	Does the sentence answer the question? Answer with yes or no. Question: [Input premise] Sentence: [Input hypothesis] The answer is
Vicuna 7B	SST-2	Analyze the tone of this statement and respond with either positive or negative: [Input] The answer is:
	RTE	[Input premise] Based on the paragraph above can we conclude the following sentence, answer with yes or no. [Input hypothesis] The answer is
	QNLI	[Input premise] Based on the question above, does the following sentence answer the question? [Input hypothesis] Answer with yes or no. The answer is

F ADDITIONAL METHOD DETAILS

F.1 PRE-SELECTION OF REPLACEMENT LOCATIONS

In Proposition S3, we consider all possible locations ($i \in [2 \cdot |S| + 1]$), leading to $|\mathcal{S}_1(S, \Gamma)| \leq (|\Gamma| + 1) \cdot (2 \cdot |S| + 1)$ by Corollary S6, which can be relatively big for lengthy sentences (e.g., $|S|$ can be up to 844 for AG-News). We propose considering a subset of n locations in order to remove the dependency on the length of the sentence. To select the top n locations, we propose testing the relevance of each position by replacing each character with a “test” character and looking at the

⁷In Vicuna 7B and Guanaco 7B, AutoDAN uses the initialized handcrafted prefix in jailbreaks successfully so that the time is 0. Our method can also work on top of these handcrafted prefixes.

Table S19: Attack evaluation in jailbreaking different large language models.

Model	Method	ASR (%)	$d_{lev}(S, S')$	Time
Vicuna 7B	GCG	100.00	35.26	56.32
	AutoDAN	100.00	3677	- ⁷
	Charmer	100.00	3.44	17.41
Guanaco 7B	GCG	100.00	55.34	30.06
	AutoDAN	100.00	3677.00	- ⁷
	Charmer	100.00	4.98	24.99
Llama 2-Chat 7B	GCG	86.00	76.74	948.44
	AutoDAN	18.00	3209.33	29.01
	Charmer	94.00	28.02	341.66

change in the loss. In Algorithm 1 we formalize our proposed strategy. Note that if the test character is going to be replaced by itself in a certain position, we replace by the special character ξ (Line 5 in Algorithm 1). In practice we use the white space (U+0020) as the test character. Overall, Algorithm 1 performs $\mathcal{O}(|S|)$ forward passes through the language model.

F.2 ATTACK CLASSIFIER

In the case of using a classifier $f : \mathcal{S}(\Gamma) \rightarrow \mathbb{R}^o$, where the predicted class is given by $\hat{y} = \arg \max_{y \in [o]} f(S)_y$ with o classes, we follow Hou et al. (2023) and use the Carlini-Wagner Loss⁸ (Carlini and Wagner, 2017):

$$\mathcal{L}(f(S), y) = \max_{\hat{y} \neq y} f(S)_{\hat{y}} - f(S)_y. \quad (2)$$

In this case, a sentence S' is an adversarial example when $\mathcal{L}(f(S'), y) \geq 0$. To search the closest sentence in Levenshtein distance that produces a misclassification, we iteratively solve Eq. (1) with $k = 1$ until the adversarial sentence S' is misclassified. Our attack pseudo-code is presented in Algorithm 2.

F.3 ATTACK LLM

Now we illustrate how to apply our method on attacking LLM-based classifiers. Given a data sample $(S, y) \in \mathcal{S} \times [C]$, the input to LLMs is formulated by concatenating the original sentences with some instructive prompts S_{P_1}, S_{P_2} in the format of $S_{P_1} \oplus S \oplus S_{P_2}$. A schematic for illustration and additional details on the prompting strategy can be found in Appendix E.6. Similar to Eq. (1), we aim to solve:

$$\max_{S' \in \mathcal{S}_k(S, \Sigma)} \mathcal{L}(f(S_{P_1} \oplus S' \oplus S_{P_2}), y),$$

where the model output $f(S_{P_1} \oplus S' \oplus S_{P_2})_i := \mathbb{P}(i | S_{P_1} \oplus S' \oplus S_{P_2})$ is the conditional probability of the next token i . We can still use the Carlini-Wagner Loss defined in Eq. (2) by considering the next token probability for the classes.

G PROOF OF COROLLARY S6

In this section, we provide the technical proof of Corollary S6.

⁸In the original paper, Carlini and Wagner (2017) clip the value of the loss to be 0 at maximum. We do not clip in order to deal with cases where the loss is positive for different adversarial examples.

Proof. Starting with the upper bound, in the base case, we have $|\mathcal{S}_0| = |\{S\}| = 1$. Then, we will prove the relationship between $|\mathcal{S}_k|$ and $|\mathcal{S}_{k-1}|$. For a certain $S' \in \mathcal{S}_{k-1}$, we have:

$$\begin{aligned}
|\mathcal{S}_k(S, \Gamma)| &= \left| \bigcup_{S' \in \mathcal{S}_{k-1}} \{S'' : d_{\text{lev}}(S', S'') \leq 1\} \right| \\
&\leq \sum_{S' \in \mathcal{S}_{k-1}} |\{S'' : d_{\text{lev}}(S', S'') \leq 1\}| \\
\text{[Proposition S3]} &= \sum_{S' \in \mathcal{S}_{k-1}} \left| \left\{ \psi \left(\phi(S') \stackrel{i}{\leftarrow} c \right) \mid \forall i \in [2|S'| + 1], \forall c \in \Gamma \cup \{\xi\} \right\} \right| \\
\text{[# combinations of } i\text{'s and } c\text{'s]} &\leq \sum_{S' \in \mathcal{S}_{k-1}} (2|S'| + 1) \cdot (|\Gamma| + 1) \\
[|S'| \leq |S| + k \ \forall S' \in \mathcal{S}_k] &\leq \sum_{S' \in \mathcal{S}_{k-1}} (2(|S| + k) - 1) \cdot (|\Gamma| + 1) \\
&= (2(|S| + k) - 1) \cdot (|\Gamma| + 1) \cdot |\mathcal{S}_{k-1}|.
\end{aligned}$$

Finally, by induction we have

$$|\mathcal{S}_k(S, \Gamma)| \leq (|\Gamma| + 1)^k \cdot \prod_{j=1}^k (2(|S| + k) - 1).$$

For the lower bound, it is enough to compute the size of the set of strings obtained by adding just prefixes:

$$\begin{aligned}
|\mathcal{S}_k(S, \Gamma)| &\geq |\{\psi(P \oplus \phi(S)), \forall P \in \{P' \in \mathcal{S}(\Gamma \cup \{\xi\}), |P'| \leq k\}\}| \\
&= |\{\psi(P), \forall P \in \{P' \in \mathcal{S}(\Gamma \cup \{\xi\}), |P'| \leq k\}\}| \\
&= \left| \bigcup_{i=0}^k \{P' \in \mathcal{S}(\Gamma), |P'| = i\} \right| \\
\text{[Disjoint sets]} &= \sum_{i=0}^k |\{P' \in \mathcal{S}(\Gamma), |P'| = i\}| \\
&= \sum_{i=0}^k |\Gamma|^i \\
\text{[Geometric series]} &= \begin{cases} \frac{1 - |\Gamma|^{k+1}}{1 - |\Gamma|} & \text{if } |\Gamma| > 1 \\ k + 1 & \text{if } |\Gamma| = 1 \end{cases}
\end{aligned}$$

□

H ALTERNATIVE ATTACK DESIGNS

In this section, we cover alternative algorithmic designs called `PGA-Charmer` for solving Eq. (1). Specifically, we study relaxing the binary constraints in Eq. (BP) in order to perform a Projected Gradient Ascent (PGA) procedure.

H.1 PGA-CHARMER

Let $\mathbf{E}^{(i)} = \mathbf{Token}(S^{(i)})\mathbf{T} \in \mathbb{R}^{l_i \times d}$ be the embeddings of tokens for any sentence $S^{(i)} \in \mathcal{S}' \subseteq \mathcal{S}(\Gamma)$ with $i \in [|\mathcal{S}'|]$. The zero-padded embeddings for the sentences in the set \mathcal{S}' become:

$$\hat{\mathbf{E}}^{(i)} = \mathbf{E}^{(i)} \oplus \mathbf{0}_{(\bar{l}-l_i) \times d} \in \mathbb{R}^{\bar{l} \times d}, \quad \forall i \in [|\mathcal{S}'|],$$

where $\bar{l} = \max\{l_i : i \in [|\mathcal{S}'|]\}$ and \oplus is the concatenation operator along the first dimension.

Remark S1 (Model output after zero padding). Given a function f , the output before and after zero padding is unchanged, i.e., $\mathbf{f}(\hat{\mathbf{E}}^{(i)}) = \mathbf{f}(\mathbf{E}^{(i)}) \forall \mathbf{E}^{(i)} \in \mathcal{S}'$.

We can reformulate the problem in Eq. (1) as:

$$\begin{aligned} \max_{\mathbf{u} \in \mathbb{R}^{|\mathcal{S}_k(S, \Gamma)|}} \quad & \mathcal{L} \left(\mathbf{f} \left(\sum_{i=1}^{|\mathcal{S}_k(S, \Gamma)|} u_i \cdot \hat{\mathbf{E}}^{(i)} \right), y \right) \\ \text{s.t.} \quad & u_i \in \{0, 1\} \quad \forall i \in [|\mathcal{S}_k(S, \Gamma)|], \quad \|\mathbf{u}\|_1 = 1 \end{aligned} \quad (\text{BP})$$

which is a constrained binary optimization problem. Note that given \mathbf{u}^{BP} a maximizer of Eq. (BP) with $i^{\text{BP}} := \arg \max_{i \in [|\mathcal{S}_k(S, \Gamma)|]} u_i^{\text{BP}}$, we have that the sentence $S^{(i^{\text{BP}})} \in \mathcal{S}_k(S, \Gamma)$ is a maximizer of Eq. (1).

However, solving Eq. (BP) is as hard as solving Eq. (1) because of the exponential size of $\mathcal{S}_k(S, \Gamma)$, see Corollary S6. Alternatively, we can relax the binary constraints from the \mathbf{u} vector and solve:

$$\begin{aligned} \max_{\mathbf{u} \in \mathbb{R}^{|\mathcal{S}_k(S, \Gamma)|}} \quad & \mathcal{L} \left(\mathbf{f} \left(\sum_{i=1}^{|\mathcal{S}_k(S, \Gamma)|} u_i \cdot \hat{\mathbf{E}}^{(i)} \right), y \right) \\ \text{s.t.} \quad & u_i \in [0, 1] \quad \forall i \in [|\mathcal{S}_k(S, \Gamma)|], \quad \|\mathbf{u}\|_1 = 1. \end{aligned} \quad (\text{SP})$$

In this case, given \mathbf{u}^{SP} a maximizer of Eq. (SP), we know:

$$\mathcal{L} \left(\mathbf{f} \left(\sum_{i=1}^{|\mathcal{S}_k(S, \Gamma)|} u_i^{\text{SP}} \cdot \hat{\mathbf{E}}^{(i)} \right), y \right) \geq \mathcal{L} \left(\mathbf{f} \left(\sum_{i=1}^{|\mathcal{S}_k(S, \Gamma)|} u_i^{\text{BP}} \cdot \hat{\mathbf{E}}^{(i)} \right), y \right).$$

Note that the embeddings $\sum_{i=1}^{|\mathcal{S}_k(S, \Gamma)|} u_i^{\text{SP}} \cdot \hat{\mathbf{E}}^{(i)}$ have no correspondence to any sentence in $\mathcal{S}_k(S, \Gamma)$. However, we can still take $i^{\text{SP}} = \arg \max_{i \in [|\mathcal{S}_k(S, \Gamma)|]} u_i^{\text{SP}}$ and hopefully $S^{(i^{\text{SP}})} \in \mathcal{S}_k(S, \Gamma)$ is an adversarial example. To solve Eq. (SP), we employ projection gradient ascent with step-size η as follows:

$$\mathbf{u}^{t+1} = \Pi_{\Delta}(\mathbf{u}^t + \eta \nabla \mathcal{L}_{\mathbf{u}}(\mathbf{u}^t)),$$

where $\Pi_{\Delta}(\cdot)$ is the projection function. Let us denote by $\hat{\mathbf{u}} := \mathbf{u}^t + \eta \nabla \mathcal{L}_{\mathbf{u}}(\mathbf{u}^t)$ for notation simplification, then the projection step essentially aims to solve the following quadratic programming problem:

$$\begin{aligned} \mathbf{u}^{t+1} = \arg \min_{\mathbf{u}} \quad & \frac{1}{2} \|\mathbf{u} - \hat{\mathbf{u}}\|_2^2, \\ \text{subject to :} \quad & \sum u_i = 1, \quad u_i \geq 0. \end{aligned} \quad (\text{QP})$$

The Lagrangian associated with Eq. (QP) is as follows:

$$\mathcal{L}(\mathbf{u}, \lambda, \mathbf{v}) := \frac{1}{2} \|\mathbf{u} - \hat{\mathbf{u}}\|_2^2 + \lambda(\mathbf{u}^\top \mathbf{1} - 1) - \mathbf{v}^\top \hat{\mathbf{u}},$$

where $\lambda \in \mathbb{R}$, $\mathbf{v} \in \mathbb{R}^{|\mathcal{S}_{\text{all}}|}$ are the Lagrange multipliers. The Karush-Kuhn-Tucker optimality conditions are necessary and sufficient for solving Eq. (QP), that is:

$$\nabla_{\mathbf{u}} \mathcal{L}(\mathbf{u}, \lambda, \mathbf{v}) = \mathbf{u} - \hat{\mathbf{u}} + \lambda \mathbf{1} - \mathbf{v} = \mathbf{0}, \quad (3)$$

$$u_i \geq 0, \quad (4)$$

$$\sum u_i - 1 = 0, \quad (5)$$

$$v_i \geq 0, \quad (6)$$

$$v_i u_i = 0. \quad (7)$$

Clearly, given any λ , if we set $u_i = \max(\hat{u}_i - \lambda, 0)$, $v_i = \max(\lambda - \hat{u}_i, 0)$, then Eqs. (3), (4), (6) and (7) can be satisfied. Therefore, the remaining problem reduces to find a λ that satisfies Eq. (5), i.e.,

$$\sum u_i - 1 = \sum \max(\hat{u}_i - \lambda, 0) - 1 = 0.$$

We employ the algorithm proposed in Held et al. (1974) to solve it, as presented in Algorithm 3. Lastly, we select the $\arg \max_j (u_j^*)$ element in \mathcal{S}_{all} as the attack sentence S' .

Algorithm 3 Projection into simplex (Held et al., 1974)**Input:** $\hat{\mathbf{u}} := \mathbf{u}^t + \eta \nabla \mathcal{L}_{\mathbf{u}}(\mathbf{u}^t) \in \mathbb{R}^{|S_{\text{all}}|}$.Sort $\hat{\mathbf{u}}$ such that $\hat{u}_1 \leq \hat{u}_2 \leq \dots \leq \hat{u}_{|S_{\text{all}}|}$.Set $J_0 := \max(J : \frac{-1 + \sum_{i=J_0+1}^{|S_{\text{all}}|} \hat{u}_i}{|S_{\text{all}}| - J} > \hat{u}_J)$.Calculate $\lambda = \frac{-1 + \sum_{i=J_0+1}^{|S_{\text{all}}|} \hat{u}_i}{|S_{\text{all}}| - J}$.Set $u_i^{t+1} = \max(\hat{u}_i - \lambda, 0)$.**Output:** \mathbf{u}^{t+1}

Table S20: **Comparison between our PGA-Charmer and query-based Charmer (proposed in the main body) in BERT:** The best method is highlighted in **bold**. While the PGA-Charmer strategy can noticeably improve the runtime, the ASR, Levenshtine distance and similarity are considerably degraded.

	Method	ASR (%) \uparrow	$d_{\text{lev}}(S, S')$ \downarrow	$\text{Sim}(S, S')$ \uparrow	Time (s) \downarrow
AG-News	PGA-Charmer	86.94	$7.33_{\pm(5.01)}$	$0.87_{\pm(0.11)}$	$8.15_{\pm(7.04)}$
	Charmer	98.51	$3.68_{\pm(3.08)}$	$0.95_{\pm(0.06)}$	$8.74_{\pm(11.10)}$
MNLI-m	PGA-Charmer	99.05	$2.11_{\pm(1.53)}$	$0.79_{\pm(0.19)}$	$0.85_{\pm(0.72)}$
	Charmer	100.00	$1.14_{\pm(0.42)}$	$0.85_{\pm(0.13)}$	$1.45_{\pm(0.81)}$
QNLI	PGA-Charmer	81.19	$3.46_{\pm(2.32)}$	$0.89_{\pm(0.12)}$	$5.15_{\pm(4.60)}$
	Charmer	97.68	$1.94_{\pm(1.48)}$	$0.94_{\pm(0.07)}$	$9.19_{\pm(9.60)}$
RTE	PGA-Charmer	72.64	$1.53_{\pm(1.45)}$	$0.86_{\pm(0.11)}$	$0.65_{\pm(0.71)}$
	Charmer	97.01	$1.55_{\pm(1.42)}$	$0.86_{\pm(0.13)}$	$2.50_{\pm(2.33)}$
SST-2	PGA-Charmer	97.52	$2.68_{\pm(1.82)}$	$0.84_{\pm(0.16)}$	$1.09_{\pm(0.89)}$
	Charmer	100.00	$1.47_{\pm(0.74)}$	$0.90_{\pm(0.11)}$	$1.27_{\pm(0.84)}$

H.2 COMPARISON BETWEEN PGA-CHARMER AND QUERY-BASED CHARMER

In this section, we experimentally validate the efficiency of PGA-Charmer and compare it against query-based Charmer, which is proposed in the main body. The result in Table S20 shows that PGA-Charmer can efficiently reduce the runtime as it does not require the forward pass over a mini-batch of sentences after position selection. However, PGA-Charmer is worse than Charmer on other metrics, e.g., ASR, Levenshtine distance and similarity are degraded. We believe that combining the efficiency of PGA-Charmer and high ASR in -Charmer holds promise for future research endeavors.