# BEYOND IMITATION: LEARNING KEY REASONING STEPS FROM DUAL CHAIN-OF-THOUGHTS IN REASON ING DISTILLATION

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#### ABSTRACT

As Large Language Models (LLMs) scale up and gain powerful Chain-of-Thoughts (CoTs) reasoning abilities, practical resource constraints drive efforts to distill these capabilities into more compact Smaller Language Models (SLMs). We find that CoTs consist mainly of simple reasoning forms, with a small proportion ( $\approx 4.7\%$ ) of key reasoning steps that truly impact conclusions. However, previous distillation methods typically involve supervised fine-tuning student SLMs only on correct CoTs data produced by teacher LLMs, resulting in students struggling to learn the key reasoning steps, instead imitating the teacher's reasoning forms and making errors or omissions on these steps. To address these issues, drawing an analogy to human learning, where analyzing mistakes according to correct solutions often reveals the crucial steps leading to successes or failures, we propose mistakE-Driven key reasonIng step distillaTion (EDIT), a novel method that further aids SLMs learning key reasoning steps rather than mere simple fine-tuning. Firstly, to expose these crucial steps in CoTs, we design specific prompts to generate dual CoTs data with similar reasoning paths but divergent conclusions. Then, we apply the minimum edit distance algorithm on the dual CoTs data to locate these key steps and optimize the likelihood of these steps. Extensive experiments validate the effectiveness of EDIT across both in-domain and out-of-domain benchmark reasoning datasets. Further analysis shows that EDIT can generate high-quality CoTs with more correct key reasoning steps. Notably, we also explore how different mistake patterns affect performance and find that EDIT benefits more from logical errors than from knowledge or mathematical calculation errors in dual CoTs<sup>1</sup>.

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#### 1 INTRODUCTION

With the rapid growth in model size and pre-training data, LLMs have demonstrated impressive CoT reasoning performance in natural language processing (NLP) (Brown et al., 2020; Hoffmann et al., 2022; Chowdhery et al., 2023; OpenAI, 2023b). However, due to the giant model architecture and massive parameters (e.g. GPT-3 (Brown et al., 2020) with 175 billion parameters), the deployment of LLMs in resource-constrained environments becomes challenging.

042 To address this, researchers (Xu et al., 2023; Jiang et al., 2023b) have explored distilling knowledge 043 from LLMs into smaller language models (SLMs) via instruction-tuning, as seen in LMs like Alpaca (Taori et al., 2023) and Vicuna (Chiang et al., 2023). Despite progress, these distilled models often 044 struggle with complex causal reasoning. To enhance this capability, some studies (Magister et al., 2023; Ho et al., 2023; Fu et al., 2023; Chen et al., 2024; Zhou & Ai, 2024) explore distilling the CoT 046 reasoning ability from LLMs of over 100B parameters (Wei et al., 2022a;b) by fine-tuning on CoTs 047 data annotated by teacher LLMs, known as standard CoTs distillation. Besides, other studies (Hsieh 048 et al., 2023; Li et al., 2022; Liu et al., 2023) propose distilling CoTs within a multi-task learning framework by incorporating additional objectives. However, CoTs usually consist mainly of simple reasoning forms, with a small proportion ( $\approx 4.7\%^2$ ) of key reasoning steps that are pivotal moments 051

<sup>&</sup>lt;sup>1</sup>Code can be found at https://anonymous.4open.science/r/eb77sh-F564

<sup>&</sup>lt;sup>2</sup>We calculated the edit distance and its average proportion in the overall sequence on the dual CoT dataset mentioned in our subsequent methods §3.

On the floor, I see two magenta scrunchiephone chargers, one gold fidget spinner, three gold booklets, three silver scrunchiephone chargers, two silver booklets, and two magenta booklets. If I remove all the magenta items from the floor, how many scrunchiephone chargers remain on it? Question Options: (A) zero (B) one (C) two (D) three (E) four (F) five (G) six According to this question, there are two magenta scrunchiephone chargers and three silver scrunchiephone chargers on the floor. If we remove all the magenta items, we are left with only the silver scrunchiephone chargers. Therefore, the number of scrunchiephone chargers that remain on the floor is three. Therefore, the Teacher answer is (D). According to this question, there are two magenta scrunchiephone chargers and three silver scrunchiephone chargers on the floor. If we remove all the magenta items from the floor, we are left with 2 silver Unthinking scrunchiephone chargers. Therefore, the answer is (C) Student  $\times$ 

Figure 1: Examples of CoTs generated by teacher LLMs and student SLMs on our test dataset. Simply SFT leads to an "unthinking" student who imitates the teacher's reasoning forms but makes errors and omissions in key reasoning steps, where the imitated contents are highlighted in red, and the key steps are marked with boxes.

072 in reasoning that significantly influence subsequent thought processes and conclusions. The essence 073 of the above methods is the simple Supervised Fine-Tuning (SFT) paradigm, where the student model is trained solely on the teacher's correct reasoning data. This paradigm may result in students 074 struggling to learn the key reasoning steps, instead imitating the teacher's reasoning forms 075 and making errors or omissions on these steps, as illustrated in Figure 1. Drawing an analogy 076 to human learning, where analyzing mistakes according to correct solutions often reveals the key 077 reasoning steps leading to successes or failures, we propose a novel mistak**E-D**riven key reasonIng step distillaTion (EDIT). This approach focuses on dual CoTs data, encompassing both positive 079 and negative examples of teachers' reasoning. By examining dual CoTs, students can identify and learn from the crucial reasoning steps, thereby improving their CoTs. Specifically, we first retain 081 all CoTs data annotated by the teacher, irrespective of correctness. Subsequently, we design two 082 comprehensive prompts to instruct teachers to produce dual CoTs that share similar intermediate 083 reasoning steps but lead to divergent conclusions. Finally, we utilize the minimum edit distance 084 algorithm to locate key reasoning steps in dual CoTs, as shown in Figure 3, and then utilize a fine-grained loss function to optimize the likelihood of these steps. 085

Extensive experiments show that the student models distilled by EDIT exhibits higher performance
 and generalization than the baselines on both in-domain (IND) and out-of-domain (OOD) benchmark
 reasoning datasets. Further analyses indicate that EDIT can generate higher-quality CoTs with more
 correct key reasoning steps by auto evaluation and case studies. Notably, we also show EDIT can
 benefit more from logical mistake patterns than knowledge or mathematical calculation errors in dual
 CoTs, potentially paving the way for future research on the efficient use of mistakes.

- Our contributions can be summarized as follows:
  - 1. We reveal a shortfall in the previous distillation methods, where the simple SFT paradigm may result in students mimicking the teacher's reasoning forms but making errors or omissions in key reasoning steps, thus diminishing the versatility of CoTs.
    - 2. We propose mistake-driven key reasoning step distillation, which allows students to learn key reasoning steps from our specifically designed dual CoTs data, further improving reasoning.
  - 3. Extensive experiments validate the effectiveness of our method across both IND and OOD datasets, showing that EDIT can reduce errors in key reasoning steps for students.
    - 4. We investigate how different mistake patterns impact EDIT and find that logical errors provide the more significant benefits than knowledge or mathematical calculation errors.
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- 2 RELATED WORKS
- **CoT Reasoning.** The emergent ability appears in LLMs across a wide range of NLP tasks (Chowdhery et al., 2023; Wei et al., 2022a). One such ability is CoT reasoning, which involves generating a

series of intermediate reasoning steps. This ability has been further explored recently with the
release of OpenAI's o1 model (OpenAI, 2024). While CoT prompting techniques (Wei et al., 2022b)
significantly enhance the problem-solving capabilities of models (Kojima et al., 2022; Wang et al., 2023b; Huang et al., 2023), it has little effect on smaller models (Wei et al., 2022a). Chung et al.
(2022) suggest that CoT reasoning can be induced in SLMs via instruction tuning on CoTs data. Our
work show that the CoT capabilities of SLMs can be further improved by learning from key reasoning
steps in dual CoTs data.

115 Knowledge Distillation from LLMs. There has been a lot of work dedicated to distilling knowledge 116 (Hinton et al., 2015) from powerful proprietary LLMs, e.g. ChatGPT (OpenAI, 2023a) in a black-box 117 setting. However, most of these works primarily focus on the general ability distillation by instruction 118 tuning on large and diverse datasets (Peng et al., 2023; Jiang et al., 2023b; Li et al., 2024). In contrast, we aim to distill the CoT reasoning capabilities from LLMs same as the standard CoTs 119 distillation (Magister et al., 2023; Ho et al., 2023). Besides, some studies (Li et al., 2022; Hsieh 120 et al., 2023; Liu et al., 2023) employ LLM's rationale or self-evaluation output to enhance SLM's 121 reasoning in a multi-task learning framework. Fu et al. (2023) fine-tune SLMs on four types of 122 reasoning data to ensure out-of-distribution generalization. Wang et al. (2023c) distill SLMs by 123 learning from self-reflection and feedback from LLMs in an interactive multi-round paradigm. Chen 124 et al. (2024) maximize the mutual information between multi objectives for CoTs distillation. Ranaldi 125 & Freitas (2024) use in-family and out-family teachers to generate more CoTs for fine-tuning students. 126 Different from the above works, we assist CoTs distillation with teachers' mistakes to alleviate the 127 style imitation of teachers' reasoning.

128 Learning from Mistakes. Recent studies use mistake data to enhance the performance of LMs. 129 Shinn et al. (2023) propose Reflexion that allows the LLM agent to self-reflect from its mistakes. 130 Wang & Li (2023) introduce a study assistant that collects and retrieves LLMs' training mistakes to 131 guide future inferences. Li et al. (2023) propose CoK that corrects potential mistakes in the rationale 132 by retrieving knowledge to avoid error propagation. However, both of the above methods require 133 the models to be large enough to have basic CoT reasoning or instruction-following capabilities, 134 which is almost impossible to occur in vanilla SLMs. Wang et al. (2023a) propose fine-tuning on 135 counterfactual data to ensure the faithful reasoning of the student model. An et al. (2023) propose LEMA that fine-tunes language models on corrected mistake data, where the mistakes are collected 136 from various LLMs e.g. LLaMA2-70B (Touvron et al., 2023), WizardLM-70B (Xu et al., 2023), and 137 corrected by GPT-4 (OpenAI, 2023b). Additionally, Sun et al. (2024) propose Retrieved In-Context 138 Principles, which retrieve mistakes to provide customized guidance and improve model performance 139 during inference. In contrast, we collect the teachers' mistakes to create a dual CoTs dataset for 140 further key reasoning steps learning on model distillation. 141

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#### 3 MISTAKE-DRIVEN KEY REASONING STEP DISTILLATION

145 We present the overview of our proposed method in Figure 2. Concretely, (1) unlike prior works 146 (Magister et al., 2023; Hsieh et al., 2023) that only focus on correct CoTs annotated by teacher LLMs, 147 we first retain all CoTs reasoning data, regardless of its correctness. (2) Then based on the previously 148 retained correct and wrong CoTs, we construct dual CoTs datasets consisting of positive-negative CoT 149 pairs that follow similar intermediate reasoning steps but lead to divergent conclusions. Specifically, 150 we design two comprehensive contextual prompts to instruct teacher LLMs to rectify the originally wrong CoTs and corrupt originally correct CoTs. (3) Finally, we distill the student SLMs by training 151 on the teacher's correct CoTs reasoning data and further Key Reasoning Steps Learning (KRSL) on 152 the dual CoTs datasets. 153

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3.1 Cots Annotated by LLMs

157 We utilize CoT Prompting (Wei et al., 2022b) to extract CoTs for a raw dataset  $\mathcal{D} = \{(q, a)\}$  from 158 LLMs, where q is the question and a is the golden answer. Specifically, we first create a CoTs 159 Extraction Prompt CEP that contains several human-curated question-CoTs pair examples and the 160 task description, which can be found in Appendix C.1. For each  $q \in \mathcal{D}$ , we extract CoTs as:

$$CoT \sim LLM (CEP \oplus q)$$
 (1)



Figure 2: Overview of our mistake-driven key reasoning step distillation. (1) We first retain all CoTs data annotated by teacher LLMs (2) and ask teacher LLMs to generate dual CoTs data using 188 our designed two comprehensive prompts. (3) Then we fine-tune student SLMs on both original 189 correct and rectified-after CoTs data. Finally, we apply key reasoning step learning on the pre-tuned 190 student SLMs by identifying the minor difference between the dual CoTs.

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193 where  $\oplus$  means concatenation. Then, we classify the CoTs annotated dataset into two datasets according to the final answer's correctness<sup>3</sup>, same as Zelikman et al. (2022). One is the CoTs-194 original correct dataset  $\mathcal{D}^+ = \{(q, CoT^+) \mid \forall (q, a) \in \mathcal{D}, \hat{a} = a \& \hat{a} \in CoT^+\}$  and the other is 195 CoTs-original wrong dataset  $\mathcal{D}^- = \{(q, CoT^-) \mid \forall (q, a) \in \mathcal{D}, \hat{a} \neq a \& \hat{a} \in CoT^-\}.$ 196

3.2 DUAL COTS GENERATION

We define dual CoTs data as contrasting CoTs that follow similar reasoning steps but reach divergent 200 conclusions compared to the original. To provide a deeper understanding, we also present several 201 examples of dual CoTs in Appendix A. In the following, we will introduce how to generate dual 202 CoTs datasets including  $\mathcal{D}^{+-}$  contrasting to  $\mathcal{D}^{+}$ , and  $\mathcal{D}^{-+}$  contrasting to  $\mathcal{D}^{-}$ . 203

204 **Rectify Wrong CoTs.** To generate correct CoTs contrasting with the originally wrong CoTs, inspired by Rationalization (Zelikman et al., 2022), we design an Answer Hint Prompt AHP that 205 shares the same examples with CEP but with different organizational structures. The template of 206 AHP can be found in Appendix C.2. Each example in the context and the final provided question 207 will be inserted with a hint that tells LLMs the answer first before CoTs. Thus, due to the same 208 in-context examples and hint answers, teacher LLM can rectify its original wrong CoTs data with 209 similar reasoning steps but correct answers. For each  $q \in \mathcal{D}^-$ , we rectify CoTs as follows and then 210 have the Rectified CoTs dataset  $\mathcal{D}^{-+} = \{(q, CoT^{-+})\}$ : 211

$$CoT^{-+} \sim LLM (AHP \oplus q \oplus a)$$
 (2)

<sup>214</sup> <sup>3</sup>To support our assumption of CoT correctness, We randomly sample 100 examples to manually check 215 the logical consistency between the CoT and the final answer and find that the CoTs generated by ChatGPT generally support the final answer.



wrong CoT are dual to each other. The identified key steps in correct reasoning and wrong reasoning are respectively marked in green and red.

230 **Corrupt Correct CoTs.** To generate incorrect CoTs contrasting with the originally correct CoTs, 231 a straightforward approach is to use AHP with incorrect hint answers to prompt LLMs to produce 232 wrong CoTs. However, in practice, we find that LLMs rarely follow the incorrect hints and still 233 generate correct CoTs. This may be due to the simplicity of the questions, which fall within the 234 LLMs' knowledge range. Additionally, LLMs, having undergone Reinforcement Learning from 235 Human Feedback (RLHF) (Ouyang et al., 2022), may resist providing unhelpful answers. Therefore, we design a Contrastive CoTs Prompt (CEP) to entice LLMs to generate incorrect CoTs, leveraging 236 their strong in-context learning capabilities. The prompt template can be found in Appendix C.3. 237 Specifically, to ensure high-quality incorrect CoTs, we randomly sample negative examples from  $\mathcal{D}^-$ 238 and positive examples from  $\mathcal{D}^{-+}$ , pair them, and place them into the CCP as curated joint in-context 239 examples. For each  $q \in \mathcal{D}^+$ , we corrupt CoTs as follows and then have the corrupted CoTs dataset 240  $\mathcal{D}^{+-} = \{(q, CoT^{+-})\}:$ 241

$$CoT^{+-} \sim LLM \left( \text{CCP} \oplus q \oplus CoT^{+} \right)$$
 (3)

#### TRAINING STUDENT WITH COTS 3.3

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245 Surpervised Fine-tuning on Correct CoTs. After preparing the dual CoTs, we first fine-tune 246 student models on the teachers' original correct CoTs dataset  $\mathcal{D}^+$  and rectified CoTs dataset  $\mathcal{D}^{-+}$ . 247 The training objective is as follows:

$$\pi_{sft} = \arg\max_{\pi} \mathbb{E}_{q,CoT \sim \mathcal{D}_{merge}^+} \left[ \log \pi (CoT \mid q) \right]$$
(4)

where the merged correct CoTs dataset  $\mathcal{D}^+_{merge} = \mathcal{D}^+ \cup \mathcal{D}^{-+}$ , and  $\pi_{sft}$  denotes the student with the 250 251 base inference ability after the initial fine-tuning.

**Key Reasoning Steps Learning** Inspired by (Guo et al., 2023b) who leverage fine-grained quality 253 signals to align human preference, we propose a key reasoning steps learning (KRSL) method to 254 further encourage students to comprehend the reasons behind both correct and wrong CoTs.

255 Step1. We pair the teacher's original correct CoTs dataset  $\mathcal{D}^+$  with its corrupted CoTs dataset  $\mathcal{D}^{+-}$ . 256 creating an originally correct dual CoTs dataset  $\mathcal{D}_{dual}^+ = \{(q, CoT^+, CoT^{+-})\}$ , where  $CoT^+$ 257 and  $CoT^{+-}$  are dual to each other; similarly, the teacher's inherently wrong dual CoTs dataset 258  $\mathcal{D}_{dual}^- = \{(q, CoT^{-+}, CoT^-)\}$ . By merging them, we obtain the ultimate dual CoTs datasets 259  $\mathcal{D}_{dual} = \mathcal{D}_{dual}^+ \cup \mathcal{D}_{dual}^-$ , which is prepared for the subsequent learning of key reasoning steps. 260

261 Step2. Then we employ the minimum edit distance to identify the key steps in both correct reasoning and wrong reasoning, as shown in Figure 3. In this way, students can identify less frequent text 262 segments that are inserted or replaced in wrong CoTs compared to correct CoTs, and vice versa. 263 These text segments are considered key reasoning steps. After that, we assign token-level weights to 264 facilitate fine-grained learning for correct CoTs and wrong CoTs in  $D_{dual}$  respectively: 265

$$\omega_t^+ = \begin{cases} \alpha, & \text{if } CoT_t^+ \text{ is inserted or replaced} \\ 0, & \text{otherwise} \end{cases}, \\ \omega_t^- = \begin{cases} \beta, & \text{if } CoT_t^- \text{ is deleted or replaced} \\ 0, & \text{otherwise} \end{cases}.$$
(5)

where  $\alpha \ge 0$ ,  $\beta \ge 0$  and  $\omega_t^+$  represents the weight of t-th token in the correct CoTs (semantically 269 same with  $\omega_t^-$ ). We set the weights to zero to ignore the impact of identical tokens in the dual CoTs. Step3. Finally, to ensure that the student makes correct decisions on key steps in correct reasoning, we optimize the student model on these tokens with weighted negative log-likelihood. Conversely, to prevent the student from making key steps present in wrong reasoning, we optimize the student model on these steps with weighted positive log-likelihood. The sum of both is taken as the final loss. The optimization objective is as follows:

$$\max_{\pi_{sft}} \mathbb{E}_{q,CoT^+,CoT^- \sim \mathcal{D}_{dual}} \quad \left[ \mathcal{L}(\pi_{sft},q,CoT^+,\omega^+) - \mathcal{L}(\pi_{sft},q,CoT^-,\omega^-) \right] \tag{6}$$

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$$\mathcal{L}(\pi, q, CoT, \omega) = -\sum_{CoT_t \in CoT} \omega_t \log \pi(CoT_t \mid q, CoT_{< t})$$
(7)

#### 4 EXPERIMENTS

4.1 EXPERIMENTAL SETUP

In-domain (IND) Dataset: BIG-Bench Hard (BBH) (Suzgun et al., 2023) consists of 27 challenging tasks that span arithmetic, symbolic reasoning, etc. This collection is mainly composed of multiple-choice questions, along with a minority of open-ended questions. To underscore the superiority of our method, we divide the BBH dataset for each subtask into a training set (BBH-train) for distillation and a test set (BBH-test) for in-domain evaluation, following a 4:1 ratio.

290 **Out-of-domain (OOD) Dataset: (1) BIG-Bench Sub (BB-sub)** is derived from the BIG-Bench 291 (BB) (Guo et al., 2023a), which includes 203 tasks covering linguistics, mathematics, common-sense reasoning, etc. To simplify our evaluation, we refine the selection of tasks from BB by identifying 292 those associated with keywords such as "multiple-choice" and "reasoning."<sup>4</sup> Additionally, we exclude 293 any tasks that are part of the BBH dataset, narrowing our pool to 61 distinct subtasks. For each 294 of these subtasks, we randomly sample up to 100 instances, culminating the BB-sub dataset. (2) 295 AGIEval (Zhong et al., 2023) is a benchmark that assesses LMs on reasoning capabilities using 296 human exams across various fields, including English, Math, Law, and Logic. We focused on the 297 English multiple-choice questions within this benchmark to evaluate our method's effectiveness. (3) 298 AI2 Reasoning Challenge (ARC) (Clark et al., 2018) comprises ARC-Easy and ARC-Challenge 299 from middle and high school science exams. ARC-E features simpler questions, while ARC-C 300 includes more challenging ones. We use their test sets for evaluation. Detailed statistics for all 301 mentioned benchmarks are provided in Appendix B.6.1. BigBench, AGIEval, and ARC are standard 302 benchmarks for evaluating LLMs reasoning performance. Specifically, BigBench and AGIEval have been employed in related works (Fu et al., 2023; Jiang et al., 2023b), and ARC is frequently used in 303 technical reports for LLaMA3 (AI@Meta, 2024) and GPT-4 (OpenAI, 2023b). 304

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Models & Implementation Details. We employ the widely-used open-source language model, 306 LLaMA2-7B (Touvron et al., 2023), as our student SLM. For the teacher model, given its performance 307 and cost-effectiveness, we employ OpenAI's advanced black-box LLM, ChatGPT, specifically using 308 the "gpt-3.5-turbo-0613" variant for extracting CoTs with the same manual prompt that is 309 used in (Suzgun et al., 2023). We employ LoRA (Hu et al., 2022) for parameter-efficient fine-tuning 310 of the student SLMs. We empirically set  $\alpha$  in KRSL as 1.0 and  $\beta$  as 0.025. Our experiments leverage 311 a mixed-precision training strategy, carried out on  $4 \times A100$  GPUs. We employ vLLM<sup>5</sup> (Kwon et al., 312 2023) to enhance inference speed, using a greedy decoding method for text generation on a single 313 A100 GPU. More training details and hyperparameter settings can be found in Appendix B.6.2.

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Baselines. We compare EDIT with the following baselines: (1) Teacher & Vanilla Student under various settings, e.g., Zero-shot (+ CoT) or Few-shot (+ CoT). (2) Std-CoT (Magister et al., 2023), which is a standard CoTs distillation method that directly fine-tunes student SLMs on CoTs data. (3)
MT-CoT (Li et al., 2022) is a multi-task CoTs distillation strategy that aims to optimize both the prediction of answers and the learning of CoTs concurrently. (4) SCOTT (Wang et al., 2023a) aims to bolster the reasoning consistency in the student SLMs by integrating counterfactual data into its training regimen.

<sup>322 &</sup>lt;sup>4</sup>https://github.com/google/BIG-bench/blob/main/bigbench/benchmark\_ 323 tasks/README.md.

<sup>&</sup>lt;sup>5</sup>https://github.com/vllm-project/vllm

Table 1: Results (Accuracy, %) of the main experiment. w/o RWC represents that student models are
distilled without using the rectified teacher's wrong CoTs in the first step of EDIT and w/o KRSL
denotes that the second step KRSL in EDIT is removed. The improvements of EDIT and its variants,
w/o RWC and w/o KRSL, over the average best baseline are indicated by subscripts. We also provide
results of more commonly used reasoning subtasks in Appendix B.1.

Method	Distill?	BBH-test	BB-sub	AGIEval	ARC-E	ARC-C	AVG
In-domain?		<ul> <li>✓</li> </ul>	×	×	×	X	
	Teac	her: ChatGI	PT (gpt-3.5-	turbo)			
Zero-shot-CoT	×	42.7	44.1	49.5	91.9	81.1	61.9
Few-shot-CoT	×	73.1	-	-	-	-	-
		Student: L	LaMA2-7B	8			
Zero-shot	×	14.8	15.5	6.9	18.2	13.9	13.9
Few-shot	×	15.1	28.5	25.5	25.5	25.4	24.0
Zero-shot-CoT	×	10.6	7.7	7.1	18.4	14.8	11.7
Few-shot-CoT	×	16.3	25.3	9.9	17.2	17.2	17.2
MT-CoT (Li et al., 2022)	<ul> <li>✓</li> </ul>	56.8	30.3	22.0	49.4	38.2	39.3
SCOTT (Wang et al., 2023a)	$\checkmark$	42.4	18.8	13.0	45.7	34.1	30.8
Std-CoT (Magister et al., 2023)	$\checkmark$	54.2	28.7	21.6	59.6	45.1	41.8
EDIT (ours)	√	<b>60.9</b> <sub>+6.7</sub>	<b>31.1</b> <sub>+2.4</sub>	<b>25.9</b> <sub>+4.3</sub>	<b>64.1</b> <sub>+4.5</sub>	<b>50.5</b> <sub>+5.4</sub>	46.5
w/o RWC	$\checkmark$	$55.1_{\pm 0.9}$	$30.1_{\pm 1.4}$	$24.1_{+2.5}$	$60.3_{\pm 0.7}$		42.7
w/o KRSL	$\checkmark$	$59.7_{+5.5}$				$45.5_{\pm 0.4}$	<u>44.3</u>

#### 4.2 MAIN RESULTS

We compare EDIT with the baselines across both IND and OOD datasets in Table 1 and illustrate the results by answering the following research questions.

**Can CoT distillation improve the performance of students?** From the table, it is evident that the student SLMs with distillation outperform those that were not distilled. This demonstrates that the reasoning ability of LLMs can be effectively transferred to SLMs by distilling CoTs.

Can EDIT further enhance the performance of students compared to other distillation methods?
 It can be observed that our proposed method EDIT outperforms the distillation baselines on both
 IND and OOD datasets, achieving an average improvement of 4.7 % compared to the standard CoT
 distillation (Std-CoT), which demonstrates the effectiveness and generalizability of EDIT.

How significant are the improvements in EDIT attributed to the rectified wrong CoTs and the key steps learning, respectively? Ablation results in the table show that removing the rectified wrong CoTs (w/o RWC) and removing key reasoning steps learning (w/o KRSL) result in performance degradation on almost all IND and OOD, emphasizing the importance of both components. On the one hand, the rectified teachers' mistakes aid the students in learning diverse ways of thinking. On the other hand, KRSL directs the student's attention to crucial steps in the dual CoTs, thereby improving the reasoning ability of the students. Additionally, we note that although KRSL and DPO (Rafailov et al., 2023) share very similar learning principles, DPO performed unexpectedly poorly in this scenario. Detailed experiments and analyses are provided in Appendix B.5.

4.3 Ablation Study

EDIT is universally applicable to SLMs with various sizes. To better adapt to the community's varying computational resource requirements, we conduct experiments on models of different sizes, including TinyLLaMA-1.1B<sup>6</sup> (Zhang et al., 2024), LLaMA2-7B and 13B. The results in Figure 4 show that EDIT outperforms the baselines across different model sizes. Particularly on benchmarks with broader evaluation dimensions such as BB-sub and AGIEval, significant improvements are observed regardless of the model size. This suggests that the more challenging a task is, the more it

<sup>&</sup>lt;sup>6</sup>https://huggingface.co/TinyLlama/TinyLlama-1.1B-intermediate-step-1431k-3T



Figure 4: Ablation results on model size for four OOD datasets. The dotted line indicates the performance of the teacher LLM under the Zero-shot-CoT setting. Due to the space limitation, we present the results on the IND dataset in Appendix B.2.



Figure 5: Left: Ablation results on key reasoning steps for the IND (BBH-test) and OOD (others) datasets. w/o Correct represents that students only learn key reasoning steps in wrong CoTs and w/o Wrong represents that students only learn key reasoning steps in correct CoTs. Middle: Ablation results on different student models for the IND and OOD. We compare EDIT with its variants w/o KRSL and Std-CoT. The results are reported by IND-AVG and OOD-AVG that respectively denote average accuracy on IND and OOD datasets. Right: Score distribution evaluated by GPT-4 on BBH-test. We use kernel density estimation to visualize the distribution of CoTs quality scores.

requires genuine reasoning rather than mere imitation, highlighting the benefits that EDIT brings to student SLMs.

EDIT is universally applicable to SLMs with various architectures. To cater to the community's diverse model preferences, we conduct experiments on models of different architectures, including CodeLLaMA-7B (Touvron et al., 2023), LLaMA3-8B (AI@Meta, 2024), and Mistral-7B-v0.2 (Jiang et al., 2023a). As shown in Figure 5 (middle), EDIT consistently outperforms its variant w/o KRSL and the baseline Std-CoT across all model architectures. Notably, the performance gap is significantly larger for the stronger model, Mistral, indicating that our method provides greater benefits with more powerful base models.

**Correct key reasoning steps have a greater impact than incorrect ones.** We conduct an ablation study on the key reasoning steps in KRSL where students learn exclusively from either the correct or wrong reasoning steps (referred to §3.3, we set  $\alpha = 0$  or  $\beta = 0$ , respectively). The results shown in Figure 5 (left) indicate that learning key reasoning steps solely from either correct or wrong CoTs leads to a decline in performance. This demonstrates that joint learning from both correct and wrong key reasoning steps is more beneficial for enhancing students' reasoning capabilities. Furthermore, we observe a greater performance drop in the absence of key steps in correct CoTs (w/o Correct) compared to the absence of key steps in wrong CoTs (w/o Wrong), suggesting that key steps from correct CoTs have a more significant impact on students' learning. 

**The quality of dual CoTs data is more important than quantity.** We also explore which component of the dual CoTs dataset in KRSL plays a more significant role: the originally correct dual CoTs  $\mathcal{D}^+_{dual}$  or the inherently wrong dual CoTs  $\mathcal{D}^-_{dual}$ . From the Table 2, compared to using  $\mathcal{D}^+_{dual}$ ,

432 employing  $\mathcal{D}_{dual}^-$  resulted in superior performance, even with less data, which demonstrates that 433  $\mathcal{D}_{dual}^-$  has higher data quality compared to  $\mathcal{D}_{dual}^-$ . The dual CoTs constructed from the inherent 434 wrong CoTs of teachers more effectively highlight the key steps in reasoning.

Table 2: Performance (Accuracy, %) comparison across dual CoTs datasets used in KRSL. The  $\mathcal{D}^+_{dual}$  and  $\mathcal{D}^-_{dual}$  represents that only the originally correct dual CoTs dataset or the inherently wrong dual CoTs dataset is used in KRSL.

Dataset	BBH-test	BB-sub	AGIEval	ARC-E	ARC-C	AVG
$\mathcal{D}^+_{dual}$ (# = 3805)	61.3	31.2	24.4	64.6	48.9	46.1
$\mathcal{D}_{dual}^{-}$ (# = 1402)	60.9	30.8	26.0	63.8	50.5	46.4
	60.9	31.1	25.9	64.1	50.5	46.5

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5 ANALYSIS

5.1 COST ANALYSIS

Considering that our method utilizes dual CoTs data, which results in twice the amount of training 450 data compared to the baselines, we implement two additional baseline settings to ensure a fair 451 comparison and ablate the impact of the increased data size due to dual CoTs: (1) Std-CoT w/ 452 **Repeat Sampling**. We perform random repeat sampling on the baseline's original training data until 453 the volume matches that of EDIT; (2) Std-CoT w/ Dual CoTs. We train the Std-CoT using all data 454 included in EDIT, adding the marker "[Counterfactual Reasoning]" before the negative 455 sample's question to differentiate it from positive reasoning. Results in Table 3 show that while 456 Std-CoT benefits from additional data, it underperforms compared to EDIT across most tasks. EDIT's 457 superiority stems from its method of learning key reasoning steps beyond mere imitation, allowing 458 students to learn from mistakes. Additionally, Std-CoT with Dual CoTs outperforms that with Repeat 459 Sampling in OOD tasks by incorporating counterfactual reasoning, reducing overfitting and better 460 generalizing the reasoning. This supports our view that simple fine-tuning with correct teacher data is insufficient for true reasoning learning. 461

Table 3: Results (Accuracy, %) of the cost analysis.

Method	Training Data Size	BBH-test	BB-sub	AGIEval	ARC-E	ARC-C	AVG
Std-CoT w/ Repeat Sampling	10414	59.4	30.3	24.0	58.0	42.1	42.8
Std-CoT w/ Dual CoTs	10414	54.8	32.9	25.1	62.2	44.1	43.8
EDIT (ours)	10414	60.9	31.1	25.9	64.1	50.5	46.5

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#### 5.2 QUALITY OF GENERATED COTS

Beyond accuracy in reasoning, the quality of CoTs is crucial for interpretable AI. Therefore, we leveraged the sota LLM, GPT-4, to score the quality of CoTs generated by Std-CoT, EDIT, and teacher LLMs. The evaluation focused on which CoT best reflects the key reasoning steps in the problem-solving process, with the prompt template detailed in Appendix C.4. The distribution of the evaluation scores is shown in Figure 5 (right), where we observe that the score distribution for CoTs generated by EDIT is closer to that of the teacher compared to Std-CoT. This illustrates that EDIT is more effective in learning the key reasoning steps, resulting in the production of high-quality CoTs.

5.3 CASE STUDY

To more clearly show the quality of key reasoning steps in generated CoTs, we present 5 cases sampled
from BBH, AGIEval, and ARC, compared with Std-CoT and teachers, as detailed in Appendix B.3.
Tables 19 and 20 show that the reasoning form of the student SLMs distilled by Std-CoT is very
similar to that of the teacher. However, the student SLMs distilled by EDIT exhibit a changed way of
thinking, leading to the correct answers. Table 21 reveals nearly identical reasoning among the three,
yet in the critical reasoning steps 7 and 8, Std-CoT fails to make the correct decisions, whereas EDIT

correctly executes stack operations. Cases from OOD datasets, shown in Tables 22 and 23, indicate
 that EDIT can accurately analyze problems and provide more logical reasoning.

#### 5.4 INTEGRATION WITH SELF-CONSISTENCY

In this subsection, we explore the integration of our method with the widely-used CoT reasoning technique, Self-Consistency (SC). SC improves reasoning performance by generating multiple reasoning paths and selecting the most consistent answer through majority voting. For SC, we apply majority voting with 8 sampled reasoning paths, using temperature=0.7 and topp=0.95 for decoding. As shown in Table 4, nearly all CoT distillation methods, including our method EDIT, show significant performance improvements when combined with SC. This demonstrates that EDIT can be effectively integrated with CoT reasoning techniques, providing both flexibility and scalability.

Table 4: Results of Integration with Self-consistency (Accuracy, major vote@8).

Method + Self-consistency	BBH-test	BB-sub	AGIEval	ARC-E	ARC-C	AVG
MT-CoT	56.4	32.2	22.3	68.5	52.8	46.4
SCOTT	41.1	22.0	16.7	56.1	40.6	35.5
Std-CoT	56.3	31.2	25.2	66.2	50.0	45.8
Std-CoT w/ Repeat Sampling	60.4	33.3	24.1	64.4	47.1	45.9
Std-CoT w/ Dual CoTs	58.4	33.6	26.8	64.4	48.2	46.3
EDIT(ours)	62.0	32.0	27.2	70.4	54.1	49.1

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#### 5.5 MISTAKE PATTERN MINING

509 In this subsection, we delve into the influence of various mistake patterns on the EDIT. Based on the 510 observation of mistake data, we utilize GPT-3.5 to categorize them into four types, including Logical 511 Errors (LEs), Knowledge Errors (KEs), Mathematical Calculation Errors (MCEs) and Other 512 **Errors** (OEs). The results of EDIT trained on these mistake patterns are shown in Table 5. We can see that KRSL on  $D_{LEs}$  consistently outperforms other mistake patterns, with KEs and MCEs having 513 a relatively smaller impact. This suggests that LEs provide a broader range of reasoning patterns that 514 are relevant for mathematical, commonsense, and symbolic reasoning. As for KEs and MCEs, since 515 these types of mistakes are more specific compared to LEs, it is not easy for the model to learn a 516 general reasoning solution from these mistakes. Therefore, learning the key reasoning steps from 517 logical reasoning errors is the most effective way among them. 518

Table 5: Performance (Accuracy, %) comparison across mistake pattern datasets used in KRSL. w/  $D_{LEs}$ , w/  $D_{KEs}$  and w/  $D_{MCEs}$  indicate the KRSL trained on the three different mistake pattern datasets, respectively. More details can be found in Appendix C.5.

Dataset	BBH-test	BB-sub	AGIEval	ARC-E	ARC-C	AVG
$D_{LEs}$	60.1	31.0	24.6	63.0	45.8	44.9
$D_{KEs}$	60.0	30.6	24.2	62.0	46.1	44.6
$D_{MCEs}$	59.4	30.4	24.4	62.3	45.8	44.5

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#### 6 CONCLUSION

531 In this paper, we propose a novel mistake-driven key reasoning step distillation method to alleviate 532 student imitation of teachers' reasoning forms. First, we preserve all CoTs data annotated by teacher LLMs, irrespective of correctness. Using these data, we design two comprehensive prompts to guide teacher LLMs in generating dual CoTs data. Finally, we utilize the minimum edit distance algorithm 534 to identify the key reasoning steps and employ a fine-grained loss function for guided learning. 535 Extensive experiments demonstrate EDIT's effectiveness in enhancing student SLMs' reasoning 536 capabilities, outperforming baseline methods on both in-domain and out-of-domain benchmark 537 datasets. We hope our work can make the community attach the importance of learning key reasoning 538 steps in dual CoTs, collectively advancing the efficiency of CoT reasoning distillation.

540	References
541	KEI EKEIVEED

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542 AI@Meta. Llama 3 model card. 2024. URL https://github.com/meta-llama/llama3/
 543 blob/main/MODEL\_CARD.md.

Shengnan An, Zexiong Ma, Zeqi Lin, Nanning Zheng, Jian-Guang Lou, and Weizhu Chen. Learning from mistakes makes LLM better reasoner. *CoRR*, abs/2310.20689, 2023.

Tom B. Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, Sandhini Agarwal, Ariel Herbert-Voss, Gretchen Krueger, Tom Henighan, Rewon Child, Aditya Ramesh, Daniel M. Ziegler, Jeffrey Wu, Clemens Winter, Christopher Hesse, Mark Chen, Eric Sigler, Mateusz Litwin, Scott Gray, Benjamin Chess, Jack Clark, Christopher Berner, Sam McCandlish, Alec Radford, Ilya Sutskever, and Dario Amodei. Language models are few-shot learners. In *NeurIPS*, 2020.

- Xin Chen, Hanxian Huang, Yanjun Gao, Yi Wang, Jishen Zhao, and Ke Ding. Learning to max imize mutual information for chain-of-thought distillation. In *Findings of the Association for Computational Linguistics: ACL 2024*, 2024.
- Wei-Lin Chiang, Zhuohan Li, Zi Lin, Ying Sheng, Zhanghao Wu, Hao Zhang, Lianmin Zheng, Siyuan Zhuang, Yonghao Zhuang, Joseph E. Gonzalez, Ion Stoica, and Eric P. Xing. Vicuna: An open-source chatbot impressing gpt-4 with 90%\* chatgpt quality, March 2023. URL https: //lmsys.org/blog/2023-03-30-vicuna/.

561 Aakanksha Chowdhery, Sharan Narang, Jacob Devlin, Maarten Bosma, Gaurav Mishra, Adam Roberts, Paul Barham, Hyung Won Chung, Charles Sutton, Sebastian Gehrmann, Parker Schuh, 562 Kensen Shi, Sasha Tsvyashchenko, Joshua Maynez, Abhishek Rao, Parker Barnes, Yi Tay, Noam 563 Shazeer, Vinodkumar Prabhakaran, Emily Reif, Nan Du, Ben Hutchinson, Reiner Pope, James Bradbury, Jacob Austin, Michael Isard, Guy Gur-Ari, Pengcheng Yin, Toju Duke, Anselm Lev-565 skaya, Sanjay Ghemawat, Sunipa Dev, Henryk Michalewski, Xavier Garcia, Vedant Misra, Kevin 566 Robinson, Liam Fedus, Denny Zhou, Daphne Ippolito, David Luan, Hyeontaek Lim, Barret Zoph, 567 Alexander Spiridonov, Ryan Sepassi, David Dohan, Shivani Agrawal, Mark Omernick, Andrew M. 568 Dai, Thanumalayan Sankaranarayana Pillai, Marie Pellat, Aitor Lewkowycz, Erica Moreira, Rewon 569 Child, Oleksandr Polozov, Katherine Lee, Zongwei Zhou, Xuezhi Wang, Brennan Saeta, Mark 570 Diaz, Orhan Firat, Michele Catasta, Jason Wei, Kathy Meier-Hellstern, Douglas Eck, Jeff Dean, 571 Slav Petrov, and Noah Fiedel. Palm: Scaling language modeling with pathways. J. Mach. Learn. Res., 24:240:1-240:113, 2023. 572

- Hyung Won Chung, Le Hou, Shayne Longpre, Barret Zoph, Yi Tay, William Fedus, Eric Li, Xuezhi Wang, Mostafa Dehghani, Siddhartha Brahma, Albert Webson, Shixiang Shane Gu, Zhuyun Dai, Mirac Suzgun, Xinyun Chen, Aakanksha Chowdhery, Sharan Narang, Gaurav Mishra, Adams Yu, Vincent Y. Zhao, Yanping Huang, Andrew M. Dai, Hongkun Yu, Slav Petrov, Ed H. Chi, Jeff Dean, Jacob Devlin, Adam Roberts, Denny Zhou, Quoc V. Le, and Jason Wei. Scaling instruction-finetuned language models. *CoRR*, abs/2210.11416, 2022.
- Peter Clark, Isaac Cowhey, Oren Etzioni, Tushar Khot, Ashish Sabharwal, Carissa Schoenick, and
   Oyvind Tafjord. Think you have solved question answering? try arc, the AI2 reasoning challenge.
   *CoRR*, abs/1803.05457, 2018.
- Karl Cobbe, Vineet Kosaraju, Mohammad Bavarian, Mark Chen, Heewoo Jun, Lukasz Kaiser, Matthias Plappert, Jerry Tworek, Jacob Hilton, Reiichiro Nakano, Christopher Hesse, and John Schulman. Training verifiers to solve math word problems. *CoRR*, abs/2110.14168, 2021.
- Yao Fu, Hao Peng, Litu Ou, Ashish Sabharwal, and Tushar Khot. Specializing smaller language
  models towards multi-step reasoning. In *ICML*, volume 202 of *Proceedings of Machine Learning Research*, pp. 10421–10430. PMLR, 2023.
- Geyang Guo, Ranchi Zhao, Tianyi Tang, Wayne Xin Zhao, and Ji-Rong Wen. Beyond imitation:
   Leveraging fine-grained quality signals for alignment. *CoRR*, abs/2311.04072, 2023a.
- 593 Geyang Guo, Ranchi Zhao, Tianyi Tang, Wayne Xin Zhao, and Ji-Rong Wen. Beyond imitation: Leveraging fine-grained quality signals for alignment. *CoRR*, abs/2311.04072, 2023b.

594 Dan Hendrycks, Collin Burns, Saurav Kadavath, Akul Arora, Steven Basart, Eric Tang, Dawn Song, 595 and Jacob Steinhardt. Measuring mathematical problem solving with the MATH dataset. In 596 NeurIPS Datasets and Benchmarks, 2021. 597 Geoffrey E. Hinton, Oriol Vinyals, and Jeffrey Dean. Distilling the knowledge in a neural network. 598 CoRR, abs/1503.02531, 2015. URL http://arxiv.org/abs/1503.02531. 600 Namgyu Ho, Laura Schmid, and Se-Young Yun. Large language models are reasoning teachers. In 601 ACL (1), pp. 14852–14882. Association for Computational Linguistics, 2023. 602 Jordan Hoffmann, Sebastian Borgeaud, Arthur Mensch, Elena Buchatskaya, Trevor Cai, Eliza 603 Rutherford, Diego de Las Casas, Lisa Anne Hendricks, Johannes Welbl, Aidan Clark, Tom 604 Hennigan, Eric Noland, Katie Millican, George van den Driessche, Bogdan Damoc, Aurelia Guy, 605 Simon Osindero, Karen Simonyan, Erich Elsen, Jack W. Rae, Oriol Vinyals, and Laurent Sifre. 606 Training compute-optimal large language models. CoRR, abs/2203.15556, 2022. 607 608 Cheng-Yu Hsieh, Chun-Liang Li, Chih-Kuan Yeh, Hootan Nakhost, Yasuhisa Fujii, Alex Ratner, Ranjay Krishna, Chen-Yu Lee, and Tomas Pfister. Distilling step-by-step! outperforming larger 609 language models with less training data and smaller model sizes. In ACL (Findings), pp. 8003–8017. 610 Association for Computational Linguistics, 2023. 611 612 Edward J. Hu, Yelong Shen, Phillip Wallis, Zeyuan Allen-Zhu, Yuanzhi Li, Shean Wang, Lu Wang, 613 and Weizhu Chen. Lora: Low-rank adaptation of large language models. In ICLR. OpenReview.net, 614 2022. 615 Jiaxin Huang, Shixiang Gu, Le Hou, Yuexin Wu, Xuezhi Wang, Hongkun Yu, and Jiawei Han. Large 616 language models can self-improve. In EMNLP, pp. 1051–1068. Association for Computational 617 Linguistics, 2023. 618 619 Albert Q. Jiang, Alexandre Sablayrolles, Arthur Mensch, Chris Bamford, Devendra Singh Chaplot, 620 Diego de Las Casas, Florian Bressand, Gianna Lengyel, Guillaume Lample, Lucile Saulnier, 621 Lélio Renard Lavaud, Marie-Anne Lachaux, Pierre Stock, Teven Le Scao, Thibaut Lavril, Thomas 622 Wang, Timothée Lacroix, and William El Sayed. Mistral 7b. CoRR, abs/2310.06825, 2023a. 623 Yuxin Jiang, Chunkit Chan, Mingyang Chen, and Wei Wang. Lion: Adversarial distillation of propri-624 etary large language models. In Houda Bouamor, Juan Pino, and Kalika Bali (eds.), Proceedings 625 of the 2023 Conference on Empirical Methods in Natural Language Processing, EMNLP 2023, 626 Singapore, December 6-10, 2023, pp. 3134–3154. Association for Computational Linguistics, 627 2023b. URL https://aclanthology.org/2023.emnlp-main.189. 628 Takeshi Kojima, Shixiang Shane Gu, Machel Reid, Yutaka Matsuo, and Yusuke Iwasawa. Large 629 language models are zero-shot reasoners. In NeurIPS, 2022. 630 631 Woosuk Kwon, Zhuohan Li, Siyuan Zhuang, Ying Sheng, Lianmin Zheng, Cody Hao Yu, Joseph 632 Gonzalez, Hao Zhang, and Ion Stoica. Efficient memory management for large language model 633 serving with pagedattention. In SOSP, pp. 611-626. ACM, 2023. 634 Ming Li, Lichang Chen, Jiuhai Chen, Shwai He, Jiuxiang Gu, and Tianyi Zhou. Selective reflection-635 tuning: Student-selected data recycling for LLM instruction-tuning. CoRR, abs/2402.10110, 636 2024. 637 638 Shiyang Li, Jianshu Chen, Yelong Shen, Zhiyu Chen, Xinlu Zhang, Zekun Li, Hong Wang, Jing Oian, 639 Baolin Peng, Yi Mao, Wenhu Chen, and Xifeng Yan. Explanations from large language models make small reasoners better. CoRR, abs/2210.06726, 2022. 640 641 Xingxuan Li, Ruochen Zhao, Yew Ken Chia, Bosheng Ding, Shafiq Joty, Soujanya Poria, and Lidong 642 Bing. Chain-of-knowledge: Grounding large language models via dynamic knowledge adapting 643 over heterogeneous sources. In The Twelfth International Conference on Learning Representations, 644 2023. 645 Weize Liu, Guocong Li, Kai Zhang, Bang Du, Qiyuan Chen, Xuming Hu, Hongxia Xu, Jintai Chen, 646 and Jian Wu. Mind's mirror: Distilling self-evaluation capability and comprehensive thinking from 647 large language models. CoRR, abs/2311.09214, 2023.

648 649 650 651 652 653	Lucie Charlotte Magister, Jonathan Mallinson, Jakub Adámek, Eric Malmi, and Aliaksei Severyn. Teaching small language models to reason. In Anna Rogers, Jordan L. Boyd-Graber, and Naoaki Okazaki (eds.), <i>Proceedings of the 61st Annual Meeting of the Association for Computational</i> <i>Linguistics (Volume 2: Short Papers), ACL 2023, Toronto, Canada, July 9-14, 2023</i> , pp. 1773–1781. Association for Computational Linguistics, 2023. doi: 10.18653/V1/2023.ACL-SHORT.151. URL https://doi.org/10.18653/v1/2023.acl-short.151.
654 655	OpenAI. Chatgpt (June 13 version). https://chat.openai.com, 2023a.
656 657	OpenAI. Gpt-4 technical report. https://cdn.openai.com/papers/gpt-4.pdf, 2023b. Accessed: [insert date here].
658 659	OpenAI. Learning to reason with llms. https://openai.com/index/ learning-to-reason-with-llms/, 2024. Accessed: [insert date here].
660 661 662 663 664 665	Long Ouyang, Jeffrey Wu, Xu Jiang, Diogo Almeida, Carroll L. Wainwright, Pamela Mishkin, Chong Zhang, Sandhini Agarwal, Katarina Slama, Alex Ray, John Schulman, Jacob Hilton, Fraser Kelton, Luke Miller, Maddie Simens, Amanda Askell, Peter Welinder, Paul F. Christiano, Jan Leike, and Ryan Lowe. Training language models to follow instructions with human feedback. In <i>NeurIPS</i> , 2022.
666 667 668	Baolin Peng, Chunyuan Li, Pengcheng He, Michel Galley, and Jianfeng Gao. Instruction tuning with GPT-4. <i>CoRR</i> , abs/2304.03277, 2023. doi: 10.48550/ARXIV.2304.03277. URL https://doi.org/10.48550/arXiv.2304.03277.
669 670 671	Rafael Rafailov, Archit Sharma, Eric Mitchell, Christopher D. Manning, Stefano Ermon, and Chelsea Finn. Direct preference optimization: Your language model is secretly a reward model. In <i>NeurIPS</i> , 2023.
672 673 674	Leonardo Ranaldi and André Freitas. Aligning large and small language models via chain-of-thought reasoning. In <i>EACL (1)</i> , pp. 1812–1827. Association for Computational Linguistics, 2024.
675 676	Noah Shinn, Beck Labash, and Ashwin Gopinath. Reflexion: an autonomous agent with dynamic memory and self-reflection. <i>CoRR</i> , abs/2303.11366, 2023.
677 678	Hao Sun, Yong Jiang, Bo Wang, Yingyan Hou, Yan Zhang, Pengjun Xie, and Fei Huang. Retrieved in-context principles from previous mistakes. <i>CoRR</i> , abs/2407.05682, 2024.
679 680 681 682 683	Mirac Suzgun, Nathan Scales, Nathanael Schärli, Sebastian Gehrmann, Yi Tay, Hyung Won Chung, Aakanksha Chowdhery, Quoc V. Le, Ed Chi, Denny Zhou, and Jason Wei. Challenging big- bench tasks and whether chain-of-thought can solve them. In <i>ACL (Findings)</i> , pp. 13003–13051. Association for Computational Linguistics, 2023.
684 685 686	Rohan Taori, Ishaan Gulrajani, Tianyi Zhang, Yann Dubois, Xuechen Li, Carlos Guestrin, Percy Liang, and Tatsunori B. Hashimoto. Stanford alpaca: An instruction-following llama model. https://github.com/tatsu-lab/stanford_alpaca, 2023.
687 688 689 690 691 692 693 694	Hugo Touvron, Louis Martin, Kevin Stone, Peter Albert, Amjad Almahairi, Yasmine Babaei, Nikolay Bashlykov, Soumya Batra, Prajjwal Bhargava, Shruti Bhosale, Dan Bikel, Lukas Blecher, Cristian Canton-Ferrer, Moya Chen, Guillem Cucurull, David Esiobu, Jude Fernandes, Jeremy Fu, Wenyin Fu, Brian Fuller, Cynthia Gao, Vedanuj Goswami, Naman Goyal, Anthony Hartshorn, Saghar Hosseini, Rui Hou, Hakan Inan, Marcin Kardas, Viktor Kerkez, Madian Khabsa, Isabel Kloumann, Artem Korenev, Punit Singh Koura, Marie-Anne Lachaux, Thibaut Lavril, Jenya Lee, Diana Liskovich, Yinghai Lu, Yuning Mao, Xavier Martinet, Todor Mihaylov, Pushkar Mishra, Igor Molybog, Yixin Nie, Andrew Poulton, Jeremy Reizenstein, Rashi Rungta, Kalyan Saladi, Alan
695 696 697 698 699 700	<ul> <li>Schelten, Ruan Silva, Eric Michael Smith, Ranjan Subramanian, Xiaoqing Ellen Tan, Binh Tang, Ross Taylor, Adina Williams, Jian Xiang Kuan, Puxin Xu, Zheng Yan, Iliyan Zarov, Yuchen Zhang, Angela Fan, Melanie Kambadur, Sharan Narang, Aurélien Rodriguez, Robert Stojnic, Sergey Edunov, and Thomas Scialom. Llama 2: Open foundation and fine-tuned chat models. <i>CoRR</i>, abs/2307.09288, 2023.</li> <li>Danqing Wang and Lei Li. Learning from mistakes via cooperative study assistant for large language</li> </ul>
.00	2 and and 201 201 201 201 and a contraction of the cooperative study dissibility of the field and a contraction of the study dissibility of the st

- Peifeng Wang, Zhengyang Wang, Zheng Li, Yifan Gao, Bing Yin, and Xiang Ren. SCOTT: self-consistent chain-of-thought distillation. In *ACL (1)*, pp. 5546–5558. Association for Computational Linguistics, 2023a.
- Xuezhi Wang, Jason Wei, Dale Schuurmans, Quoc V. Le, Ed H. Chi, Sharan Narang, Aakanksha
   Chowdhery, and Denny Zhou. Self-consistency improves chain of thought reasoning in language
   models. In *ICLR*. OpenReview.net, 2023b.
- Zhaoyang Wang, Shaohan Huang, Yuxuan Liu, Jiahai Wang, Minghui Song, Zihan Zhang, Haizhen Huang, Furu Wei, Weiwei Deng, Feng Sun, and Qi Zhang. Democratizing reasoning ability:
  Tailored learning from large language model. In *EMNLP*, pp. 1948–1966. Association for Computational Linguistics, 2023c.
- Jason Wei, Yi Tay, Rishi Bommasani, Colin Raffel, Barret Zoph, Sebastian Borgeaud, Dani Yogatama, Maarten Bosma, Denny Zhou, Donald Metzler, Ed H. Chi, Tatsunori Hashimoto, Oriol Vinyals, Percy Liang, Jeff Dean, and William Fedus. Emergent abilities of large language models. *Trans. Mach. Learn. Res.*, 2022, 2022a.
- Jason Wei, Xuezhi Wang, Dale Schuurmans, Maarten Bosma, Brian Ichter, Fei Xia, Ed H. Chi, Quoc V. Le, and Denny Zhou. Chain-of-thought prompting elicits reasoning in large language models. In *NeurIPS*, 2022b.
- Can Xu, Qingfeng Sun, Kai Zheng, Xiubo Geng, Pu Zhao, Jiazhan Feng, Chongyang Tao, and Daxin Jiang. Wizardlm: Empowering large language models to follow complex instructions. *CoRR*, abs/2304.12244, 2023.
- Eric Zelikman, Yuhuai Wu, Jesse Mu, and Noah D. Goodman. Star: Bootstrapping reasoning with reasoning. In *NeurIPS*, 2022.
- Peiyuan Zhang, Guangtao Zeng, Tianduo Wang, and Wei Lu. Tinyllama: An open-source small language model. *CoRR*, abs/2401.02385, 2024.
  - Wanjun Zhong, Ruixiang Cui, Yiduo Guo, Yaobo Liang, Shuai Lu, Yanlin Wang, Amin Saied, Weizhu Chen, and Nan Duan. Agieval: A human-centric benchmark for evaluating foundation models. *CoRR*, abs/2304.06364, 2023.
- Yuhang Zhou and Wei Ai. Teaching-assistant-in-the-loop: Improving knowledge distillation from
   imperfect teacher models in low-budget scenarios, 2024.
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#### A EXAMPLE OF DUAL COTS

738 We provide dual CoTs examples with three different mistake patterns including logical errors, 739 knowledge errors and mathematical calculation errors in Table 6, 7, 8 and mark the correct/wrong 740 key reasoning steps in different colors. We observe that our carefully crafted prompts for generating 741 correct CoT and wrong CoT effectively ensure the desired dual CoT characteristics: similar reasoning 742 steps leading to different conclusions. For instance, subordinating conjunctions in Table 6 like 743 "however," "despite," and "even though," as well as certain verb and noun phrases, significantly 744 influence the reasoning process and the conclusion. These elements represent the key reasoning steps 745 that we aim for the model to learn.

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#### **B** ADDITIONAL EXPERIMENT

B.1 DETAILED PERFORMANCE ON REASONING SUBTASKS

The main table summarizes the experimental results on the complete benchmark. In this subsection, we present results on additional reasoning tasks from BigBench and AGIEval to highlight the broader applicability of our method. As shown in Table 9, our approach consistently surpasses the baseline models on nearly all subtasks, including key mathematical reasoning benchmarks such as AQuA, SAT-MATH, GSM8K (Cobbe et al., 2021), and MATH (Hendrycks et al., 2021). Notably, this performance is achieved despite our training dataset containing only 200 simple math reasoning

# Table 6: A casual judgment dual CoTs example from BIG-Bench Hard where the wrong CoT shows a logical error.

758	-	
759		## Input
760		Task Description: Answer questions about causal attribution. Q: How would a typical person answer each of the following questions about causation?
761		George and his sister Lena reunite at their parentshouse for Thanksgiving. Whereas George just got into medical
762		school, Lena is unhappy in her marriage and recently lost her job. Over the course of the day, George and Lena get into a number of heated arguments. Later in the afternoon they play a game of darts. They split the first two
763		games, and the third game is close until the end. Who will win comes down to George's last shot. If he hits a high
764	Question	point region, he wins; if he hits a low point region, Lena wins. George doesn't care that Lena is having a difficult time; he really wants to beat her. George has little control over his shots. He tries to aim at the high point region
765		of the dart board. As he sets up his shot, however, he loses his balance. The dart slips out of his hand and wobbles
766		toward the board. The dart lands in the high point region. George triumphs in his victory while Lena is sad. Did George hit the high point region intentionally?
767		Options:
768		- Yes - No
769		A:
770		Here in this question, we are told that "George tries to aim at the high point region of the dart board." However, due to losing his balance, the dart slips out of his hand and wobbles toward the board. A typical person would
771	Correct CoT	assume that George did not intentionally hit the high point region, as his intention was to aim at the high point
772		region but his actions resulted in an unintended outcome. Therefore, the answer is No.
773		Here in this question, we are told that George tries to aim at the high point region of the dart board. Despite losing his balance, the dart lands in the high point region. A typical person would assume that George intentionally hit
774	Wrong CoT	the high point region, as his aim was to score points and win the game, even though his balance caused the dart to
775		wobble. Therefore, the answer is Yes.

Table 7: A movie recommendation example from BIG-Bench Hard where the wrong CoT shows a knowledge-based error.

779		
		## Input
780		Task Description: Recommend movies similar to the given list of movies.
781		Q: Find a movie similar to Pulp Fiction, Schindler's List, Apollo 13, Dances with Wolves:
782	Ouestion	Options: (A) Iron Eagle IV
	Question	(B) The Shawshank Redemption
783		(C) Knockin' on Heaven's Door
784		(D) Aguirre The Wrath of God
785		A:
		- Pulp Fiction (crime, drama; 1994)
786		- Schindler's List (biography, drama, history; 1993)
787	Correct CoT	<ul> <li>Apollo 13 (adventure, drama, history; 1995)</li> <li>Dances with Wolves (adventure, drama, western; 1990)</li> </ul>
788	Contest Con	These are all famous movies produced in the 1990s. Amongst all the options, the only movie similar to these ones
789		seems to be The Shawshank Redemption (drama; 1994), as it is also a critically acclaimed film with a compelling
		storyline. Therefore, the answer is (B).
790	-	- Pulp Fiction (crime, drama; 1994)
791		- Schindler's List (biography, drama, history; 1993)
792	W G T	- Apollo 13 (adventure, drama, history; 1995)
793	Wrong CoT	- Dances with Wolves (adventure, drama, western; 1990)
		These are all famous movies produced in the 1990s. Amongst all the options, the only movie similar to these ones seems to be Aguirre The Wrath of God (adventure, biography, drama; 1972), as it is also a historical drama film.
794		Therefore, the answer is (D).
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examples out of 5207 total samples. These results confirm the robustness of our method across various reasoning domains.

#### B.2 ABLATION STUDY ON MODEL SIZE FOR IN-DOMAIN DATASET

The results of the model size ablation study on IND datasets are presented in Figure 6. We observe that EDIT outperforms the baseline methods on both the 7B and 13B model sizes and significantly surpasses the teacher LLMs in the Zero-shot CoT setting.

B.3 CASE STUDY

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Here we show 5 cases in Table 19, 20, 21, 22 and 23 to clearly compare the CoT generated by EDIT with the teacher LLM and the standard CoTs distillation (Std-CoT). We utilize  $\checkmark$  and  $\times$  to denote whether the CoT is correct or incorrect, respectively.

810	Table 8: A multistep arithmetic dual CoTs example from BIG-Bench Hard where the wrong CoT
811	shows a mathematical calculation error.

812		
813		## Input
814	Question	Task Description: Solve multi-step arithmetic problems. O: $((-1 + -64 + -6) - (-2 * -51 * 1)) =$
815		A:
816		Let's recall that the order of operations in mathematics is as follows: (1) Parentheses, (2) exponents, (3) multiplication and division (from left to right), (4) addition and multiplication (from left to right). So, remember
817		to always compute the expressions inside parentheses or brackets first.
818	Correct CoT	This equation can be written as $\ddot{A} - B_{3}$ where $A = (-1 + -64 + -6)$ and $B = (-2 * -51 * 1)$ . Let's calculate $A = (-1 + -64 + -6) = (-1 + (-6) - (-4) + (-6)) = (-1 - 6 + 4 - 6) = (-7 + 4 - 6) = (-3 - 6) = -9$ .
819		Let's calculate $B = (-2 * -51 * 1) = (10 - (-1)) = (10 + 1) = 11.$
820		Then, the final equation is A - B = $-9 - 11 = -20$ . Therefore, the answer is $-20$ .
821		Let's recall that the order of operations in mathematics is as follows: (1) Parentheses, (2) exponents, (3)
822		multiplication and division (from left to right), (4) addition and multiplication (from left to right). So, remember
823	Warana GaT	to always compute the expressions inside parentheses or brackets first. This equation can be written as $\ddot{A} - B_{y}$ where $A = (-1 + -64 + -6)$ and $B = (-2 * -51 * 1)$ .
824	Wrong CoT	Let's calculate A = $(-1 + -64 + -6) = (-1 + -64 + -6) = (-1 - 6 - 4 - 6) = (-7 - 6 - 4 - 6) = (-13 - 4 - 6) = -23$ .
825		Let's calculate $B = (-2 * -51 * 1) = (10 - (-1)) = (10 + 1) = 11$ . Then, the final equation is $A - B = -23 - 11 = -34$ . Therefore, the answer is -34.
000		

Table 9: Results on commonly used reasoning subtasks.

Subtasks / Method	Source	In-domain	MT-CoT	SCOTT	Std-CoT	Std-CoT w/ Repeat Sampling	Std-CoT w/ Dual CoTs	EDIT (Ours)
Date Understanding	BBH	√	74.0	54.0	82.0	76.0	74.0	80.0
Temporal Sequences	BBH	$\checkmark$	94.0	66.0	94.0	98.0	86.0	98.0
Multi-Step Arithmetic	BBH	$\checkmark$	6.0	0.0	8.0	14.0	18.0	18.0
Sports Understanding	BBH	$\checkmark$	90.0	74.0	90.0	86.0	86.0	90.0
Elementary Math QA	BigBench	×	10.0	13.0	11.0	14.0	17.0	20.0
Identify Math Theorems	BigBench	×	9.4	9.4	20.8	18.9	24.5	26.4
StrategyQA	BigBench	×	50.0	31.0	57.0	50.0	49.0	59.0
AQuA-RAT	AGIEval	×	15.4	14.6	17.3	23.2	22.8	24.4
SAT-Math	AGIEval	×	15.5	21.4	20.9	23.6	20.0	24.5
GSM8K	GSM8K	×	15.3	17.1	15.4	10.9	14.7	17.5
MATH	MATH	×	4.3	4.1	<u>5.1</u>	5.0	5.0	5.6
AVG			34.9	27.7	38.3	38.1	38.8	42.1

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#### MISTAKE PATTERN MINING B 4

We ask gpt-3.5-turbo-0613 to classify all the teacher's wrong CoTs and list the statistic result for mistake pattern data in Table 13. To fairly assess the influence of different single mistake patterns (LEs, KEs and MCEs), we ensure consistency in data size and the proportion of challenging problem data  $(D_{dual}^{-})$  for each pattern. Since the available data for MCEs is the smallest, we randomly select 356 instances from  $D_{dual}^+$  and 56 instances from  $D_{dual}^-$ , creating three dual CoT datasets— $D_{LEs}$ ,  $D_{KEs}$ , and  $D_{MCEs}$ —each with 412 samples. Then we conduct experiments using these datasets in KRSL and the results are shown in Table 5. 

B.5 KRSL v.s. DPO

We note that the learning objectives of KRSL, utilizing both positive and negative examples, closely resemble preference alignment algorithms like RLHF and DPO (Rafailov et al., 2023). Specifically, both KRSL and DPO are directly supervised learning paradigms. However, there are key differences:

- 1. KRSL requires the model to learn from highly similar positive and negative samples (dual CoTs) for identifying key reasoning steps while DPO usually uses completely different positive and negative samples from human preference data.
- 2. In DPO, the loss function involves summing the negative log-likelihoods across all token positions in the target text. This approach can struggle to differentiate rewards for texts with high similarity since identical tokens dominate the sequence, and only a small portion of tokens differ. In long sequences, the influence of these differing tokens on the overall loss is minimal, potentially causing convergence issues.

In contrast, KRSL utilizes a minimum edit distance algorithm to pinpoint key texts in dual CoTs and precisely optimize the logits for these tokens, ignoring identical ones. This makes KRSL more



Table 10: Statistics of AGIEval dataset.

Figure 6: Ablation study on model size for
the IND dataset (BBH-test). The dotted line
indicates the performance of the teacher LLM
under the Zero-shot-CoT setting.

No.	Task	Size	# Choices
1	AQuA-RAT	254	5
2	LogiQA-EN	651	4
3	LSAT-AR	230	5
4	LSAT-LR	510	5
5	LSAT-RC	269	5
6	SAT-Math	220	4
7	SAT-EN	206	4
8	SAT-EN (w/o Psg.)	206	4

suitable for learning from dual CoTs compared to DPO. To empirically study this, we provide comparative experiments and analyses with DPO as follows.

We compare KRSL with DPO by implementing DPO in the EDIT and training LLaMA2-7B on complete dual CoTs data using the dpo\_trainer implemented in the TRL<sup>7</sup>, with the following settings: learning rate of 1e-5, a cosine learning rate scheduler, a warmup ratio of 0.3, DPO beta of 0.1, a maximum prompt length of 512, maximum length of 1024, 10 training epochs, and a batch size of 16. The results (Table 11) show significant performance degradation with DPO. Thus, we check the model's generation results in Table 12 and find that the output pattern almost completely collapses, outputting only the answer without the intermediate reasoning process. The output after the answer is nonsensical and highly repetitive, and the model cannot stop predicting the next word. 

Table 11: Performance (Accuracy, %) comparison between DPO and KRSL implementation in EDIT.

Method	BBH-test	BB-sub	AGIEval	ARC-E	ARC-C	AVG
w/ DPO		15.4	4.8	5.1	4.9 50.5	8.1
w/ KRSL	60.9	31.1	25.9	64.1	50.5	46.5

#### B.6 DETAILS OF EXPERIMENTAL SETTINGS

#### B.6.1 DATASET STATISTICS

Table 10, 14, 16 and 17 show the data statistics of AGIEval, ARC, BIG-Bench Hard (BBH) and BIG-Bench Sub (BB-sub), respectively.

<sup>&</sup>lt;sup>7</sup>https://github.com/huggingface/trl

		Table 12. A famule case in EDTT w/ DTO nom DTO-Denen Hard.
919		
920		## Input
921		Task Description: Select the humorous edit that 'ruins' the input movie or musical artist name.
922		Q: Which of the following is a humorous edit of this artist or movie name: 'little shop of horrors'? Options:
923	Question	(Å) little shoy of horrors
924		<ul><li>(B) little hop of horrors</li><li>(C) little wshop of horrors</li></ul>
925		(D) ulittle shop of horrors
926		little shop of horrors
927		Q:Which of the following is a humorous edit of this artist or movie name: 'little shop of horrors'?
928		Options:
929		<ul><li>(A) little shoy of horrors</li><li>(B) little hop of horrors</li></ul>
930	EDIT w/ DPO	(C) little wshop of horrors
931		(D) ulittle shop of horrors
932		A:little shop of horrors
933		O Will be falle following in a home of the fall is a first source in source Wester that a first source 20
934		Q: Which of the following is a humorous edit of this artist or movie name: 'little shop of horrors'? Options:
935		

Table 13: Classification statistics of mistake data patterns.

Mistake Patterns & Dataset	LEs	KEs	MCEs	OEs	LEs + KEs	LEs + MCEs	KEs + MCEs	LEs + KEs + MCEs	Total
$\mathcal{D}^+_{dual}$	2618	452	356	51	255	45	26	2	3805
$\mathcal{D}_{dual}^{dual}$	1077	77	56	62	105	22	3	0	1402
$\mathcal{D}_{dual}^{aual}$	3695	529	412	113	360	67	29	2	5207

Table 15: Generation configs of students and teachers.

Table 14: Statistics of ARC test dataset.	
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Task	Size	# Choices
ARC-E	2376	4-5
ARC-C	1172	4-5

Arguments	Student	Teacher
do sample	False	True
temperature	-	0.2
top-p	1.0	1.0
top-k	-	-
max new tokens	1024	2048
# return sequences	1	1

#### Table 16: Statistics of BIG-Bench Hard dataset.

No.	Task	Size	# Choices	No.	Task	Size	# Choices
1	Boolean Expressions	250	2	17	Reasoning about Colored Ob-	250	18
2	Causal Judgement	187	2		jects		
3	Date Understanding	250	6	18	Ruin Names	250	11
4	Disambiguation QA	250	4	19	Salient Translation Error Detec-	250	6
5	Dyck Languages	250	-		tion		
6	Formal Fallacies Syllogisms	250	2	20	Snarks	178	2
	Negation			21	Sports Understanding	250	2
7	Geometric Shapes	250	11	22	Temporal Sequences	250	4
8	Hyperbaton (Adjective Order- ing)	250	2	23	Tracking Shuffled Objects (3 objects)	250	3
9	Logical Deduction (3 objects)	250	3	24	Tracking Shuffled Objects (5 ob-	250	5
10	Logical Deduction (5 objects)	250	5		jects)	200	
11	Logical Deduction (7 objects)	250	7	25	Tracking Shuffled Objects (7 ob-	250	7
12	Movie Recommendation	250	5		jects)		
13	Multi-Step Arithmetic	250	-	26	Web of Lies	250	2
14	Navigate	250	2	27	Word Sorting	250	-
15	Object Counting	250	-				
16	Penguins in a Table	146	5		Sum	6511	-

77 78 79	1 2 3	abstract_narrative_understanding		# Choices	No.			# Choices
79	2	abstract narranye understanding	100	5	32	key_value_maps	100	2
79		anachronisms	100	2	33	logic_grid_puzzle	100	3
-		analogical similarity	100	7	34	logical_args	32	5
	4	analytic entailment	70	2	35	logical_fallacy_detection	100	2
30	5	cause_and_effect	100	2	36	metaphor_boolean	100	2
	6	checkmate in one	100	26	37	metaphor_understanding	100	4
31	7	cifar10 classification	100	10	38	minute_mysteries_qa	100	4
32	8	code line description	60	4	39	mnist_ascii	100	10
	9	conceptual combinations	100	4	40	moral_permissibility	100	2
33	10	crass ai	44	4	41	movie_dialog_same_or_different	100	2
34	11	elementary_math_qa	100	5	42	nonsense_words_grammar	50	4
	12	emoji movie	100	5	43	odd_one_out	86	5
35	13	empirical_judgments	99	3	44	parsinlu_qa	100	4
36	14	english russian proverbs	80	4	45	physical_intuition	81	4
	15	entailed polarity	100	2	46	play_dialog_same_or_different	100	2
37	16	entailed_polarity_hindi	100	2	47	presuppositions_as_nli	100	3
88	17	epistemic reasoning	100	2	48	riddle_sense	49	5
	18	evaluating information essentiality	68	5	49	similarities_abstraction	76	4
39	19	fantasy_reasoning	100	2	50	simple_ethical_questions	100	4
90	20	figure of speech detection	59	10	51	social_iqa	100	3
	20	goal_step_wikihow	100	4	52	strange_stories	100	2
91	22	gre reading comprehension	31	5	53	strategyqa	100	2
)2	23	human_organs_senses	42	4	54	swahili_english_proverbs	100	4
	23	identify math theorems	53	4	55	swedish_to_german_proverbs	72	4
93	25	identify_odd_metaphor	47	5	56	symbol_interpretation	100	5
)4	26	implicatures	100	2	57	timedial	100	3
1-2	20	implicit_relations	82	25	58	undo_permutation	100	5
95	28	indic_cause_and_effect	100	25	59	unit_interpretation	100	5
)6	28	intersect geometry	100	26	60	vitaminc_fact_verification	100	3
0	30	kanji ascii	100	5	61	winowhy	100	2
7	31	kanja_asch	100	4		Sum	5384	·

Table 17: Statistics of BIG-Bench sub dataset. We filter the original dataset by retrieving tasks with keywords "multiple choice" and randomly sample up to 100 examples per task. Note, the task in BBH will not be involved in BB-sub.

## 1000 B.6.2 Hyperparameters Settings

In our study, we ensure consistency in the hyperparameter settings across all baselines, including our
 proposed EDIT approach, to maintain the fairness of our comparative analysis. Here, we detail the
 hyperparameter configurations employed in our experiments.

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Training Steps and Batch Size. The number of training steps is determined based on the size of
 the training dataset, the batch size, and the number of gradient accumulation steps required. We
 maintain a consistent batch size across all baselines to eliminate any performance discrepancies that
 could arise from varying batch sizes.

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Learning Rate. Our initial exploratory experiments focused on the standard CoTs distillation method using the LLaMA-2 model. We found that while the batch size had minimal impact on performance, the learning rate was a critical factor. We tested learning rates of 1e-4, 2e-4, and 3e-4, observing optimal performance at 2e-4 across the standard CoT and other distillation baselines, as well as our EDIT approach. Consequently, we set the learning rate to 2e-4 for all methods involved in our study.

1017

Epochs and Evaluation Strategy. Throughout our training process, we monitored the training loss curve and noted that it generally plateaued by the 15th epoch, indicating that the models had achieved convergence. Therefore, we set the number of epochs to 15 for 7B models. The process of determining the number of epochs for other model sizes followed a similar pattern. To mitigate the potential risk of overfitting and to ensure our evaluation reflects the most effective model configuration, we systematically selected checkpoints from the epoch that demonstrated the best performance on the IND task. These checkpoints were then used to evaluate performance on OOD tasks.

1025 The hyperparameters in training and inference can be found in Table 18 and Table 15 respectively. In the KRSL, the second phase training in EDIT, the learning rate is empirically set as 5e-6.

	Hyperparameter	TinyLLaMA-1.1B	LLaMA2-13B	LLaMA2-7B / CodeLLaMA-7B / LLaMA3-8B / Mistral-7B-v0.2
	gradient accumulation steps	4	8	4
	per device batch size	16	8	16
	learning rate	2e-4	2e-4	2e-4
	epoches	20	15	10
	max length	1024	1024	1024
	$\beta$ of AdamW	(0.9,0.999)	(0.9,0.999)	(0.9,0.999)
	$\epsilon$ of AdamW	1e-8	1e-8	1e-8
	$\gamma$ of Scheduler	0.95	0.95	0.95
	weight decay	0	0	0
	warmup ratio	0	0	0
	rank of LoRA	64	64	64
	$\alpha$ of LoRA	32	32	32
	target modules	q_proj, v_proj	q_proj, v_proj	q_proj, v_proj
_	drop out of LoRA	0.05	0.05	0.05

#### Table 18: Training hyperparameters.

### 1039 B.6.3 COMPUTATION BUDGET

Our experimental code is based on modifications of Meta's open-source llama-recipes<sup>8</sup>, utilizing the FSDP framework and training the model in parallel on four 80GB A100 GPUs. In our experimental setup, training a 7B model during the SFT stage takes approximately 40 minutes per epoch. For KRSL, each epoch takes around 90 minutes. With the same settings, training the Mistral model will see about a 10% increase in training time. We will release our code in the future.

- 1046 C PROMPT TEMPLATES
- 1048 C.1 CoTs Extraction Prompt

We use the prompt template shown in Table 25 to call the ChatGPT API to generate the CoTs for theBBH-train datasets.

1053 C.2 ANSWER HINT PROMPT

We list the Answer Hint Prompt templates in Table 24, which imply the teacher LLMs to generate the CoTs based on the given answers following the in-context examples.

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C.3 CONTRASTIVE COTS PROMPT

We list the Contrastive CoTs Prompt templates in Table 26, which query the teacher LLMs to generate the CoTs with similar rationales to the original ones but divergent answers by following the few examples provided with contrastive CoT pairs.

1063 C.4 EVALUATION PROMPT OF COTS QUALITY

1065 We list the evaluation prompt templates of CoTs quality in Table 27.

1067 C.5 MISTAKE PATTERN MINING PROMPT

For mistake pattern mining, we employ the prompt template delineated in Table 28, which includes the definitions of the four distinct mistake patterns.

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<sup>8</sup>https://github.com/Meta-Llama/llama-recipes

, r	Table 19: A reasoning about colored objects case from BIG-Bench Hard.
	On the table, there are three pink scrunchiephone chargers, two orange crayons, and two black scrunchiephone
0	chargers. If I remove all the black items from the table, how many scrunchiephone chargers remain on it?
Question:	Options: (A) zero(B) one (C) two (D) three (E) four (F) five (G) six (H) seven (I) eight (J) nine (K) ten (L) eleven
	<ul> <li>(M) twelve (N) thirteen (O) fourteen (P) fifteen (Q) sixteen</li> <li>According to this question, there are three pink scrunchiephone chargers, two orange crayons, and two black</li> </ul>
	scrunchiephone chargers on the table. If we remove all the black items from the table, we are left with three pink scrunchiephone chargers and two orange crayons.
Teacher	Therefore, the number of scrunchiephone chargers that remain on the table is five.
	Therefore, the answer is (F).
	According to this question, there are three pink scrunchiephone chargers, two orange crayons, and two black scrunchiephone chargers on the table.
Std-CoT	If we remove all the black items from the table, we are left with three pink scrunchiephone chargers, two orange crayons, and two black scrunchiephone chargers.
	The number of scrunchiephone chargers remaining on the table is seven.
	Therefore, the answer is (H).
	According to this question, there are a total of 5 scrunchiephone chargers on the table: 3 pink scrunchiephone
EDIT	chargers and 2 black scrunchiephone chargers. If we remove all the black items, we are left with 3 pink scrunchiephone chargers.
EDII	setureneprone enargers.
	Therefore, the answer is (D).
	Table 20: A movie recommendation case from BIG-Bench Hard.
Question:	Find a movie similar to Jurassic Park, Independence Day, Forrest Gump, Batman. Options: (A) The Firm (B) Roger Dodger (C) Innocent Man (D) An (E) The Silence of the Lambs
Question:	
Question:	Options: (A) The Firm (B) Roger Dodger (C) Innocent Man (D) An (E) The Silence of the Lambs
Question:	Options: (A) The Firm (B) Roger Dodger (C) Innocent Man (D) An (E) The Silence of the Lambs         - Jurassic Park (action, adventure, science-fiction; 1993)         - Independence Day (action, science-fiction, drama; 1996)
Question:	Options: (A) The Firm (B) Roger Dodger (C) Innocent Man (D) An (E) The Silence of the Lambs - Jurassic Park (action, adventure, science-fiction; 1993)
	Options: (A) The Firm (B) Roger Dodger (C) Innocent Man (D) An (E) The Silence of the Lambs         - Jurassic Park (action, adventure, science-fiction; 1993)         - Independence Day (action, science-fiction, drama; 1996)
Question: Teacher	Options: (A) The Firm (B) Roger Dodger (C) Innocent Man (D) An (E) The Silence of the Lambs         - Jurassic Park (action, adventure, science-fiction; 1993)         - Independence Day (action, science-fiction, drama; 1996)         - Forrest Gump (comedy, drama, romance; 1994)         - Batman (action, adventure; 1989)         These are all famous Hollywood movies produced in the 1980s and 1990s. Amongst all the options
	Options: (A) The Firm (B) Roger Dodger (C) Innocent Man (D) An (E) The Silence of the Lambs         - Jurassic Park (action, adventure, science-fiction; 1993)         - Independence Day (action, science-fiction, drama; 1996)         - Forrest Gump (comedy, drama, romance; 1994)         - Batman (action, adventure; 1989)         These are all famous Hollywood movies produced in the 1980s and 1990s. Amongst all the options, the only movie similar to these ones seems to be The Firm (drama, mystery, thriller; 1993), as it is also a popular movie from the same era.
	<ul> <li>Options: (A) The Firm (B) Roger Dodger (C) Innocent Man (D) An (E) The Silence of the Lambs</li> <li>Jurassic Park (action, adventure, science-fiction; 1993)</li> <li>Independence Day (action, science-fiction, drama; 1996)</li> <li>Forrest Gump (comedy, drama, romance; 1994)</li> <li>Batman (action, adventure; 1989)</li> <li>These are all famous Hollywood movies produced in the 1980s and 1990s. Amongst all the options the only movie similar to these ones seems to be The Firm (drama, mystery, thriller; 1993), as it is also a popular movie from the same era.</li> <li>Therefore, the answer is (A).</li> </ul>
	<ul> <li>Options: (A) The Firm (B) Roger Dodger (C) Innocent Man (D) An (E) The Silence of the Lambs</li> <li>Jurassic Park (action, adventure, science-fiction; 1993)</li> <li>Independence Day (action, science-fiction, drama; 1996)</li> <li>Forrest Gump (comedy, drama, romance; 1994)</li> <li>Batman (action, adventure; 1989)</li> <li>These are all famous Hollywood movies produced in the 1980s and 1990s. Amongst all the options the only movie similar to these ones seems to be The Firm (drama, mystery, thriller; 1993), as it is also a popular movie from the same era.</li> <li>Therefore, the answer is (A).</li> <li>Jurassic Park is an action and adventure movie. Independence Day is an action, science-fiction, and adventure</li> </ul>
Teacher	<ul> <li>Options: (A) The Firm (B) Roger Dodger (C) Innocent Man (D) An (E) The Silence of the Lambs</li> <li>Jurassic Park (action, adventure, science-fiction; 1993)</li> <li>Independence Day (action, science-fiction, drama; 1996)</li> <li>Forrest Gump (comedy, drama, romance; 1994)</li> <li>Batman (action, adventure; 1989)</li> <li>These are all famous Hollywood movies produced in the 1980s and 1990s. Amongst all the options the only movie similar to these ones seems to be The Firm (drama, mystery, thriller; 1993), as it is also a popular movie from the same era.</li> <li>Therefore, the answer is (A).</li> <li>Jurassic Park is an action and adventure movie. Independence Day is an action, science-fiction, and adventure movie The Firm is a crime, drama, and thriller movie. Roger Dodger is a comedy and drama movie. Innocent Man is a</li> </ul>
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1105		Table 21: A dyck languages case from BIG-Bench Hard.
1135 1136		Compathy along a Dyrak a yeard. Complete the part of the appropriate making any that the parantheses are along
1137	Question:	Correctly close a Dyck-n word. Complete the rest of the sequence, making sure that the parentheses are closed properly.
1138		Input: <(( <> ) We should process each input one by one and keep track of the stack configuration.
1139		
1140		0: empty stack
1141		1: <; stack: <
1142 1143		2: (; stack: < (
1143		3: (; stack: < ( (
1145		4: { ; stack: < ( ( {
1146	Teacher	5: < ; stack: < ( ( { <
1147 1148		6: > ; stack: < ( ( {
1149		7: } ; stack: < ( ( {
1150		8: ) ; stack: < ( (
1151		Now, we have reached the end. The final stack is "< ( (".
1152 1153		We will need to pop out "(", "(" one by one in that order.
1154		
1155		So, we need ")", ")". Therefore, the answer is )).         We should process each input one by one and keep track of the stack configuration.
1156		we should process each input one by one and keep track of the stack configuration.
1157		0: empty stack 7
1158		1: <; stack: <
1159		2: ( ; stack: < (
1160		3: (; stack: < ( (
1161		
1162 1163		4: { ; stack: < ( ( {
1164	Std-CoT	5: <; stack: < ( ( { <
1165		6: > ; stack: < ( ( {
1166		7: } ; stack: < ( ( {
1167		8: ) ; stack: < ( ( {
1168		Now, we have reached the end. The final stack is "<(({{".
1169 1170		We will need to pop out "{", "(", "<" one by one in that order.
1171		we will need to pop out { , { , < one by one in that order.
1172		So, we need "}", ")", ">". Therefore, the answer is } )>.
1173		We should process each input one by one and keep track of the stack configuration.
1174		0: empty stack
1175		1: < ; stack: <
1176		2: ( ; stack: < (
1177		
1178		3: (; stack: < ( (
1179		4: { ; stack: < ( ( {
1180 1181	EDIT	5: < ; stack: < ( ( { <
1182		6: > ; stack: < ( ( {
1183		7: } ; stack: < ( (
1184		
1185		8: ); stack: < (
1186		Now, we have reached the end. The final stack is "< (".
1187		We will need to pop out "(", "<" one by one in that order.
		So, we need ")", ">". Therefore, the answer is $) >$ .

## Table 21: A dyck languages case from BIG-Bench Hard.

	Anna has 4 books. If she decide to arrange the 4 books in every possible combination and moved just one book
Question:	every minute, how long would it taken by her?
	Options: (A)22 minutes (B)30 minutes (C)15 minutes (D)24 minutes (E)35 minutes
	First, Anna has 4 books and she wants to arrange them in every possible combination.
	To find the number of possible combinations, we can use the formula for permutations, which is n! (r
Teacher	factorial), where n is the number of items. In this case, $n = 4$ , so the number of possible combinations is $4! = 4 \times 3 \times 2 \times 1 = 24$ .
	Next, we know that Anna can move just one book every minute. Since there are 24 possible combina
	tions, it will take her 24 minutes to go through all of them.
	Therefore, the answer is (D) 24 minutes.
	This question focuses on the time it takes Anna to arrange the 4 books in every possible combination. We know
	that Anna moved just one book every minute.
	Plugging in the minutes per move: 1 minute
Std-CoT	There are 4 books: A, B, C, D There are (4!) = 4 different combinations: A, B, C, D; B, A, C, D; B, C, A, D; C, A, B, D; D, A, B, C
	The total number of minutes it would take Anna to arrange the books in every possible combination is the sum of the minutes needed for each combination:
	(4  minutes) + (4  minutes) + (4  minutes) + (4  minutes) + (4  minutes) = 15  minutes.
	Therefore, the answer is (C) 15 minutes.
	This question asks for the total amount of time it would take Anna to arrange the books in every possible
EDIT	combination and moved just one book every minute. We first need to calculate the number of possible
	combinations: $4! = 24$ . Then, we need to multiply the number of possible combinations by the number of minute per combination: $24 * 1$ minute = 24 minutes.
	per contoniation. 24 Triminute – 24 minutes.
	Therefore, the answer is (D) 24 minutes.
	Therefore, the answer is (D) 24 minutes.
	Therefore, the answer is (D) 24 minutes.
	Table 23: A case from AI2 Reasoning Challenge.
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	Table 23: A case from AI2 Reasoning Challenge.         Which method is the safest way to watch an eclipse of the Sun?         Options: (A) Turn away after two or three minutes. (B) Look at the Sun through a long telescope. (C) Cast a image through a pinhole onto a screen. (D) Blink often until your eyes get used to the light.         First, it is important to note that directly looking at the Sun during an eclipse can be extremely dangerous and ca cause permanent damage to the eyes.         Option (A) suggests turning away after two or three minutes. However, even a brief exposure to th Sun during an eclipse can be harmful, so this method is not safe.
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Table 24: Answer Hint Prompt templates for rectifying the wrong CoTs data based on the hint answers. {Task Description}. Your response should conclude with the format "Therefore, the answer is". Q: {Task Example Question No.1} A: Let's think step by step. {Human-Curated-CoTs No.1}. Q: {Task Example Question No.2} A: Let's think step by step. {Human-Curated-CoTs No.2}. Q: {Task Example Question No.2} A: Let's think step by step. {Human-Curated-CoTs No.3}. Q: {QUESTION} A: Let's think step by step. Table 25: CoTs extraction prompt template of gpt-3.5-turbo for generating the CoTs data. {Task Description}. Your response should conclude with the format "Therefore, the answer is". Q: {Task Example Question No.1} H: {The correct answer is [HINT ANSWER No.1]} A: Let's think step by step. {Human-Curated-CoTs No.1}. Q: {Task Example Question No.2} H: {The correct answer is [HINT ANSWER No.2]} A: Let's think step by step. {Human-Curated-CoTs No.2}. Q: {Task Example Question No.3} H: {The correct answer is [HINT ANSWER No.3]} A: Let's think step by step. {Human-Curated-CoTs No.3}. Q: {QUESTION} H: {The correct answer is [HINT ANSWER] } A: Let's think step by step. 

Table 26: Contrastive CoTs Prompt templates for mistaken the correct CoTs data. The examples are sampled from the teachers' original wrong CoTs data and its corrected CoTs. In this way, teacher LLMs can expose the reasoning flaws in problems that were originally solved correctly. {Task Description}. You need to complete the [Wrong Response] which requires you to give the most likely incorrect answer to the [Question] and the rationale for the incorrect answer. The incorrect answer and rationale in the [Wrong Response] must be different from the correct answer and rationale in the [Right Response]. [Question]: {Task Example Question No.1} [Right Response]: {Corrected CoT No.1} [Wrong Response]: {Wrong CoT No.1} [Question]: {Task Example Question No.2} [Right Response]: {Corrected CoT No.2} {Wrong CoT No.2} [Wrong Response]: [Question]: {Task Example Question No.3} [Right Response]: {Corrected CoT No.3} [Wrong Response]: {Wrong CoT No.3} [Question]: {USER\_QUESTION} [Right Response]: {Corrected CoT} [Wrong Response]: 

1350 1351 1352 1353 1354 1355 1356 Table 27: Prompt template of GPT-4 for assessing CoTs quality. In the analysis, we use this template 1357 to eval the quality of CoTs generated by Std-CoT, EDIT and the teacher LLM respectively. 1358 1359 [System] You are a helpful and precise assistant for assessing the 1360 quality of the response. 1361 1362 [Question]: {QUESTION} 1363 [Reference Answer]: {ANSWER} 1364 [AI Assistant 1's Answer Start] 1365 {ASSISTANT1} 1366 [AI Assistant 1's Answer End] 1367 1368 [AI Assistant 2's Answer Start] 1369 {ASSISTANT2} [AI Assistant 2's Answer End] 1370 1371 [AI Assistant 3's Answer Start] 1372 {ASSISTANT3} 1373 [AI Assistant 3's Answer End] 1374 [System] We would like to request your feedback, in the form of 1375 scoring, on which of the 1376 responses from AI Assistant 1, 2 and 3 effectively demonstrates the key 1377 reasoning steps in 1378 solving this question. Key Reasoning Steps refer to certain crucial 1379 steps in the process of logical reasoning or problem-solving. These steps play a significant 1380 role in the thinking 1381 process and have a notable impact on subsequent reasoning. Each 1382 student will receive an 1383 overall score on a scale of 1 to 10, where a higher score signifies 1384 that the assistant's response is more effectively demonstrates the key reasoning steps for 1385 the question. 1386 Please provide a comprehensive explanation, avoiding any potential bias 1387 and ensuring that 1388 the order in which the responses were presented does not affect your 1389 judgment. And then output three lines indicating the scores for AI Assistant 1, 2 and 3, 1390 respectively. 1391 1392 Output with the following format: 1393 Evaluation evidence: <your evaluation explanation here> 1394 Score of AI Assistant 1: <score> Score of AI Assistant 2: <score> 1395 Score of AI Assistant 3: <score> 1396 1397 1398

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1406 1407 Table 28: Prompt templates of GPT-3.5 for classifying the mistakes. In the analysis, we use this 1408 template to classify the mistake data used in EDIT. 1409 1410 [System] You are a helpful assistant who is good at identifying types 1411 of reasoning mistakes. There are now three types of inference errors, as follows: 1412 1413 (a). Logical reasoning errors. This type of error involves the 1414 logical structure of reasoning, 1415 including assumptions, reasoning rules, argument chains, etc. Among 1416 logical errors, students may make errors such as invalid reasoning, insufficient or incorrect 1417 assumptions, and jumps in 1418 reasoning. Students may make errors in selecting reasoning strategies 1419 or methods. The chosen 1420 method may not be suitable for a specific problem, or may lead to 1421 misleading reasoning. 1422 (b). Knowledge errors in reasoning. This type of error involves 1423 misunderstanding or incomplete 1424 understanding of facts, concepts or knowledge, conceptual confusion, 1425 and cognitive biases. 1426 (c). Numerical calculation errors. This type of error involves 1427 mathematical calculation errors, 1428 which may include incorrect calculations, conversions or errors in the 1429 processing of numerical 1430 values. 1431 (d). Other errors. All other errors that do not belong to the above 1432 three categories. 1433 1434 I will give you a dictionary with the following fields and meanings: 1435 "input": reasoning question. 1436 "right\_output": the correct answer. 1437 "wrong\_output": the wrong answer. 1438 } 1439 1440 You need to first form your own opinion about the problem based on the 1441 reasoning questions and the correct answers, and then analyze the reasons for the mistakes in the 1442 wrong answers in "Rationale:". 1443 Then give your classification results in "Category:", e.g., (a), (b) or 1444 (c), etc. If an answer 1445 involves errors in multiple categories, you should point them out and connect them with '+' sign 1446 in the category. For example, if an answer involves logical errors and 1447 mathematical calculation 1448 errors, then the category should be a+c. 1449 1450 You must output with the following format: 1451 Rationale: <your analysis process and explanation of the final classification results> 1452 Category: <only fill in with a or b or c or a+b or a+c or b+c or a+b+c 1453 or d.> 1454 1455 1456

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