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# Prompt Learning with Optimal Transport for Vision-Language Models

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Anonymous Author(s)

Affiliation

Address

email

## Abstract

1 With the increasing attention to large vision-language models such as CLIP, there  
2 has been a significant amount of effort dedicated to building efficient prompts.  
3 Unlike conventional methods of only learning one single prompt, we propose  
4 to learn multiple comprehensive prompts to describe diverse characteristics of  
5 categories such as intrinsic attributes or extrinsic contexts. However, directly  
6 matching each prompt to the same visual feature is problematic, as it pushes the  
7 prompts to converge to one point. To solve this problem, we propose to apply  
8 optimal transport to match the vision and text modalities. Specifically, we first  
9 model images and the categories with visual and textual feature sets. Then, we  
10 apply a two-stage optimization strategy to learn the prompts. In the inner loop, we  
11 optimize the optimal transport distance to align visual features and prompts by the  
12 Sinkhorn algorithm, while in the outer loop, we learn the prompts by this distance  
13 from the supervised data. Extensive experiments are conducted on the few-shot  
14 recognition task and the improvement demonstrates the superiority of our method.

## 15 1 Introduction

16 In the past few years, large-scale vision-language pre-trained (VLP) models, such as CLIP [39],  
17 ALIGN [17], and BLIP [23] have achieved remarkable success in open-world visual concept learning.  
18 These methods have brought new light but also pose a new question: how to efficiently adapt the  
19 knowledge from pretraining to the downstream tasks since these models are typical of massive sizes  
20 which are not feasible for normal users to re-train.

21 One of the conventional  
22 paradigms of utilizing pretrained  
23 knowledge is “pre-training,  
24 fine-tuning”, which fixes the  
25 architecture of the pre-trained  
26 neural network and tunes its  
27 parameters using task-specific  
28 objective functions. Beyond  
29 fine-tuning the parameters,  
30 many recent methods [63, 64]  
31 introduce the concept of prompt

32 learning from the field of NLP to the vision domain and achieve striking performance gain for the  
33 few-shot visual classification. They fix the model parameters and instead learn suitable prompts  
34 by turning a template sentence into a set of learnable vectors. Then, these prompts are learned by  
35 minimizing the distance between the visual features and prompt-based language features.

36 Despite significant improvements over manual prompts, learning only a sentence is intuitively  
37 insufficient to represent a class. One class can be described by many intrinsic characteristics and

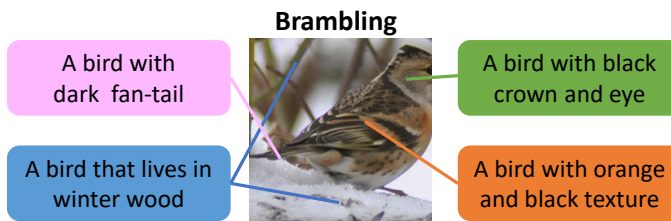


Figure 1: The motivation that one category can be complementarily described in different views (An example of “Brambling”).

38 even extrinsic context relations. Thus, for one object, we may have multiple prompt candidates  
39 which focus on different attributes. As shown in Figure 1, we can describe the class “Brambling” in  
40 different views: such as the color of the wing, the color of the crown and eyes, the shape and color of  
41 the tail, and even the living environment information. It motivates us to learn multiple prompts to  
42 comprehensively represent the class and thus facilitate classification.

43 The most natural solution is to directly learn multiple prompts by respectively matching each prompt  
44 with the visual features. However, it is the same as matching the mean of prompt features and the  
45 visual features. This solution is problematic since all prompts are encouraged to be closer to one single  
46 point and thus tend to learn the same characteristics. It contradicts our purpose to learn comprehensive  
47 prompts. To solve this problem, we tested adding some constraints to push away the prompt from  
48 each other, but found that this solution still fails to learn representative and comprehensive prompts.  
49 This solution treats the visual representation as one single point, and such a unified view of visual  
50 features ignores the fact that different prompts may only focus on one or a subset of characteristics.

51 To address this problem, in this paper, we propose Prompt Learning with Optimal Transport (PLOT),  
52 which applies optimal transport (OT) to align the local visual features and multiple textual prompts.  
53 Optimal transport can calculate the distance between two distributions under the form of multiple  
54 sampling. In our prompt learning framework, we formulate local visual features and multiple prompts  
55 as the samplings of two discrete distributions and use OT to encourage fine-grained cross-modal  
56 matching. Specifically, to obtain the local visual features with different semantic clues, we extract all  
57 feature maps as the visual representation instead of the single global representation. Fortunately, we  
58 can easily obtain the visual feature maps from the visual encoder of CLIP by using all outputs of the  
59 multi-head self-attention layer [42]. Then the problem comes down to how to calculate the distance  
60 between two feature sets.

61 We solve this problem by introducing the optimal transport theory [51] and formulate the feature sets  
62 as a discrete probability distribution where each feature has an equal probability value. Furthermore,  
63 to reduce the computational cost and avoid the extra model parameters, we learn the prompts with  
64 a two-stage optimization strategy. At the first stage in the inner loop, we fix both visual and text  
65 features and optimize the optimal transport problem by a fast Sinkhorn distances algorithm [6]. Then,  
66 in the outer loop, we fix all parameters of optimal transport and back-propagate the gradient to learn  
67 the prompts with different characteristics. *Compared with conventional distance (such as Euclidean  
68 distance of mean features), optimal transport can align different visual features for each local prompt,  
69 which is more robust to the visual misalignment and tolerates well feature shift [44]. It is because OT  
70 learns an adaptive transport plan to align features, which achieves fine-grained matching across two  
71 modalities.* We conduct experiments on 11 datasets following the standard setting of CLIP [39] and  
72 CoOp [63] to evaluate our method. These experiments span the visual classification of generic objects,  
73 scenes, actions, fine-grained categories, and so on. The significant result improvement demonstrates  
74 that PLOT can effectively learn representative and comprehensive prompts.

## 75 2 Related Work

76 **Optimal Transport** The Optimal Transport [30] is initially introduced to solve the problem of how  
77 to reduce the cost when moving several items simultaneously. Recently, OT theory has drawn wide  
78 attention in the machine learning and computer vision community by comparing distributions readily  
79 available to them under the form of feature sets [37]. Due to the brilliant property of distribution  
80 matching, OT has been applied in many theoretic and application tasks including generative models [1,  
81 45, 60], structural matching [4, 57, 61, 56] (e.g. sequence matching [4] and graph matching [56]),  
82 and other distribution-based tasks (such as clustering [22], distribution estimation [2], and causal  
83 discovery [50]). *In this paper, we use OT to align the features of vision and language modalities  
84 which represents the data structure by learning an adaptive transport plan [44].*

85 **Vision-Language Pre-trained Models** Vision-Language Pre-trained (VLP) models aim to explore  
86 the semantic correspondence between the vision and language modalities through large-scale pre-  
87 training. Recently, VLP models have achieved an exciting performance improvement in the zero-shot  
88 and few-shot visual recognition [39, 10, 63, 64, 59], which shows the great potential to promote  
89 open-world visual understanding with the help of language. One key part of learning VLP models is  
90 the self-supervised learning objective on two modalities. The popular VLP objectives can be divided  
91 into reconstruction [25, 15, 8, 20], contrastive matching [39, 17, 16], or the combination of both  
92 two [24, 54, 19]. Besides, recent progress in the field of VLP also benefits a lot from large-scale

93 pair-wised datasets. For example, CLIP [39] applies 400 million image-text pairs for contrastive  
 94 learning, while ALIGN even exploits 1.8 billion data pairs. Beyond recognition, these VLP models  
 95 also show great potential for other downstream applications, such as dense prediction [42, 62], image  
 96 generation [31, 41, 35], and action understanding [53, 48].

97 **Prompt Learning** Prompt learning is introduced from the field of NLP to efficiently adapt the large  
 98 language model to downstream tasks. Different from the conventional “pre-training, fine-tuning”  
 99 paradigm which initializes the pre-trained model and tunes the parameters of the network using  
 100 downstream task-specific objective functions, prompt learning applies textual prompt to reformulate  
 101 the downstream tasks as the original pretrained task [27, 36]. By the prompt, the domain shift between  
 102 pretrained task and downstream application is reduced and thus the pretrained knowledge can be  
 103 easier adapted to downstream tasks. The concept of prompt learning [36, 40, 38] begins from the  
 104 success of GPT [40] series. Early prompt learning methods (such as Petroni *et al.* [36] and Pörner *et*  
 105 *al.* [38]) always manually create templates based on human prior knowledge. Furthermore, some  
 106 mining-based methods [18] and gradient-based methods [46] are proposed to automatically search for  
 107 appropriate templates. Beyond search in the discrete space, some methods [26, 49, 28] remove the  
 108 constraint that the prompts are “words” and instead learn prompts in the continuous embedding space.  
 109 Recently, CoOp [63] and its extended version [64] introduce prompt learning into open-world visual  
 110 understanding to adapt the knowledge from the large-scale visual-language pretrained models and  
 111 achieve great performance improvement on the few-shot visual recognition. Compared with CoOp,  
 112 our PLOT method further improves prompt learning by introducing the optimal transport distance to  
 113 learn multiple local prompts and achieves fine-grained vision-language matching.

### 114 3 Approach

115 In this section we will first revisit the baseline method CoOp 3.1, review the preliminaries of  
 116 optimal transport 3.2, and then introduce our proposed PLOT 3.3 to show how we can learn multiple  
 117 comprehensive prompts.

#### 118 3.1 A Revisit of CoOp

119 CoOp [63] is one of the pioneering methods to learn the prompts for using vision language pretrained  
 120 knowledge (such as CLIP [39]) for downstream open-world visual recognition. Different from CLIP  
 121 which manually designs the prompt templates, CoOp sets a part of context words in the template as  
 122 continuous learnable parameters which can be learned from the few-shot data. Then the classification  
 123 weights can be represented by the distance between the learned prompt and visual feature.

124 Specifically, given an image  $\mathbf{x}$ , a visual feature  $\mathbf{f} = f(\mathbf{x})$  is obtained by the visual encoder  $f$  of  
 125 CLIP. Then, the textual prompt can be formulated as  $\mathbf{t}_k = \{\mathbf{vec}_1, \mathbf{vec}_2, \dots, \mathbf{vec}_L, \mathbf{c}_k\}$ , where  $\mathbf{c}_k$  is  
 126 the word embedding of the class name,  $\{\mathbf{vec}_l\}_{l=1}^L$  are learnable vectors with the same dimension as  
 127 the original word embedding and  $L$  is the length of context words. With prompt  $\mathbf{t}_k$  as the input, the  
 128 text encoder  $g$  outputs the textual feature as  $\mathbf{g}_k = g(\mathbf{t}_k)$ . The final prediction probability is computed  
 129 by the matching score as follows:

$$p(y = k|\mathbf{x}) = \frac{\exp(\text{sim}(\mathbf{f}, \mathbf{g}_k)/\tau)}{\sum_{k'=1}^K \exp(\text{sim}(\mathbf{f}, \mathbf{g}_{k'})/\tau)}, \quad (1)$$

130 where  $\text{sim}(\cdot, \cdot)$  denotes a metric function such as cosine similarity, and  $\tau$  stands for the temperature  
 131 of Softmax. Then we can optimize the parameters of  $\{\mathbf{vec}_l\}_{l=1}^L$  with the cross-entropy loss between  
 132 the prediction and the labeled target.

#### 133 3.2 Optimal Transport

134 Optimal transport (OT) distance is a widely used metric for the comparison of distributions. Here, we  
 135 only focus on the discrete situation which is more related to our framework. Assuming we have two  
 136 sets of points (features), the discrete distributions are formulated as:

$$U = \sum_{m=1}^M u_m \delta_{\mathbf{f}_m} \quad \text{and} \quad V = \sum_{n=1}^N v_n \delta_{\mathbf{g}_n}, \quad (2)$$

137 where  $\mathbf{u}$  and  $\mathbf{v}$  are the discrete probability vectors that sum to 1, and  $\delta_{\mathbf{f}}$  is a Dirac delta function  
 138 placed at support point  $\mathbf{f}$  in the embedding space. Then, the total distance of these two distributions

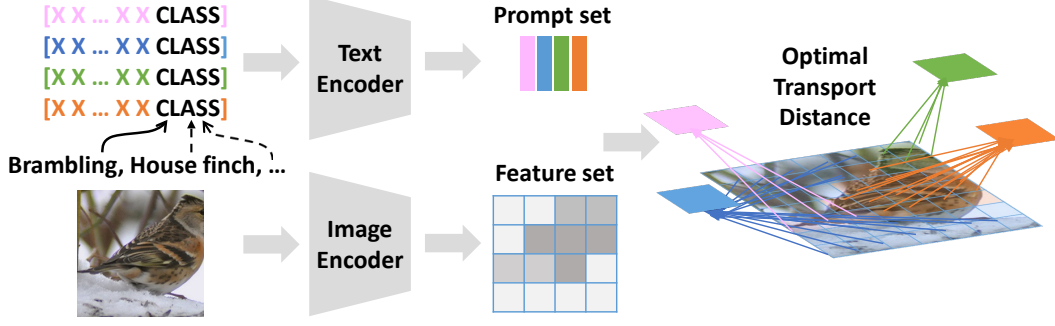


Figure 2: The framework of PLOT. PLOT first describes each category with multiple prompts and obtains a set of prompt features by text encoder. The image is also encoded as a set of local features. Then the optimal transport is used as the metric between prompts and visual features.

139 are written as:

$$\langle \mathbf{T}, \mathbf{C} \rangle = \sum_{m=1}^M \sum_{n=1}^N \mathbf{T}_{m,n} \mathbf{C}_{m,n}. \quad (3)$$

140 We call  $\mathbf{C}$  the cost matrix in which each point denotes the cost between  $\mathbf{f}_m$  and  $\mathbf{g}_n$ , such as  
 141  $\mathbf{C}_{m,n} = 1 - \text{sim}(\mathbf{f}_m, \mathbf{g}_n)$ . While the  $\mathbf{T}$  is called the transport plan, which is learned to minimize the  
 142 total distance. The optimization problem of optimal transport is formulated as:

$$\begin{aligned} d_{OT}(\mathbf{u}, \mathbf{v} | \mathbf{C}) &= \underset{\mathbf{T}}{\text{minimize}} \langle \mathbf{T}, \mathbf{C} \rangle \\ \text{subject to} \quad & \mathbf{T}\mathbf{1} = \mathbf{u}, \mathbf{T}^T\mathbf{1} = \mathbf{v}, \mathbf{T} \geq 0. \end{aligned} \quad (4)$$

143 As directly optimizing the above objective is always time-consuming, we apply the Sinkhorn distance  
 144 [6] to use an entropic constraint for fast optimization. The optimization problem with a  
 145 Lagrange multiplier of the entropy constraint is:

$$\begin{aligned} d_{OT,\lambda}(\mathbf{u}, \mathbf{v} | \mathbf{C}) &= \underset{\mathbf{T}}{\text{minimize}} \langle \mathbf{T}, \mathbf{C} \rangle - \lambda h(\mathbf{T}) \\ \text{subject to} \quad & \mathbf{T}\mathbf{1} = \mathbf{u}, \mathbf{T}^T\mathbf{1} = \mathbf{v}, \end{aligned} \quad (5)$$

146 where  $h(\cdot)$  is entropy and  $\lambda \geq 0$  is a hyper-parameter. Then we can have a fast optimization solution  
 147 with a few iterations as:

$$\mathbf{T}^* = \text{diag}(\mathbf{u}^t) \exp(-\mathbf{C}/\lambda) \text{diag}(\mathbf{v}^t), \quad (6)$$

148 where  $t$  denotes iteration and in each iteration  $\mathbf{u}^t = \mathbf{u} / ((\exp(-\mathbf{C}/\lambda) \mathbf{v}^{t-1})^T \mathbf{u})$  and  $\mathbf{v}^t =$   
 149  $\mathbf{v} / ((\exp(-\mathbf{C}/\lambda)^T \mathbf{u}^t)^T \mathbf{v})$ , with the initiation  $\mathbf{v}^0 = \mathbf{1}$ .

### 150 3.3 Prompt Learning with Optimal Transport

151 In this subsection, we introduce the details of our PLOT, which learns multiple prompts to describe  
 152 different characteristics of the category by minimizing the OT distance.

153 Specifically, as shown in Figure 2, given an image  $\mathbf{x}$ , we first feed it to the visual encoder branch of  
 154 CLIP. Apart from the global visual feature  $\mathbf{f}$ , we can also obtain a set of local features  $\{\mathbf{f}_m\}_{m=1}^M$ .  
 155 The visual encoder has a multi-head attention pooling layer in which the input is the combination of  
 156 the global feature and a set of local features (feature map) and the output is a tensor with the shape  
 157  $\mathbb{R}^{(H \times W + 1) \times C}$ , where  $H$  and  $W$  is the height and width of feature map and  $C$  is the feature dimension.  
 158 Therefore, we can obtain  $M = H \times W$  local features and a global feature. At the same time, for  
 159 class  $k$ , we can initialize  $N$  local prompts as  $\{\mathbf{t}_{k,n}\}_{n=1}^N$  with learnable vectors  $\{\mathbf{vec}_{l,n}\}_{l=1, n=1}^{L, N}$ ,  
 160 where each is the same as the prompt in CoOp. With both visual and textual encoders, we can obtain  
 161 local visual features  $\mathbf{F} = \{\mathbf{f}_m\}_{m=1}^M \in \mathbb{R}^{M \times C}$  and prompt features  $\mathbf{G}_k = \{\mathbf{g}_n\}_{n=1}^N \in \mathbb{R}^{N \times C}$ .

162 In the inner loop, we learn the transport plan  $\mathbf{T}$  with these fixed support sets  $\mathbf{F}, \mathbf{G}_k$ , by minimizing  
 163 the following OT distance to push  $\mathbf{G}_k$  to  $\mathbf{F}$ :

$$d_{OT}(k) = d_{OT}(\mathbf{u}, \mathbf{v} | \mathbf{1} - \mathbf{F}^T \mathbf{G}_k), \quad (7)$$

164 where  $\mathbf{C} = \mathbf{1} - \mathbf{F}^T \mathbf{G}_k$  denotes that we use the cosine distance between  $\mathbf{F}$  and  $\mathbf{G}_k$  as the cost matrix.  
 165 Then we can obtain the solution of transport plan  $\mathbf{T}^*$  as Eq (6) and the final OT distance  $d_{OT}(k)$ .

166 Given the OT distance between  $\mathbf{G}_k$  and  $\mathbf{F}$ , we reformulate the prediction probability as:

$$p_{ot}(y = k|\mathbf{x}) = \frac{\exp((1 - d_{OT}(k))/\tau)}{\sum_{k'=1}^K \exp((1 - d_{OT}(k'))/\tau)}. \quad (8)$$

167 In the outer loop, we fix the transport plan  $\mathbf{T}^*$  and apply the cross entropy loss to optimize the  
 168  $\{\mathbf{vec}_{l,n} |_{l=1, n=1}^{L,N}\}$  as:

$$L_{CE} = -\frac{1}{|\mathcal{X}|} \sum_{\mathbf{x} \in \mathcal{X}} \sum_{k=1}^K y_{\mathbf{x},k} p_{ot}(y = k|\mathbf{x}), \quad (9)$$

169 where  $\mathbf{y}_{\mathbf{x}}$  is a one-hot label vector. The detail algorithm can be found in the supplementary materials.

170 *Though the optimization strategy of the optimal transport and prompts is two-stage, the whole*  
 171 *training flow is end-to-end. It is because that the transport plan is computed using a small number*  
 172 *of matrix multiplications as one forward module of the neural network. The gradients of these*  
 173 *matrix multiplications are taped for backpropagation for end-to-end optimization, which makes the*  
 174 *whole system fully differentiable (including the iterative algorithm) and easy to implement using an*  
 175 *autograd library like PyTorch. In the experiments, we found that it is natural and relatively easy to*  
 176 *this optimization strategy.*

### 177 3.4 Inference strategy

178 *In the inference, given one query image and the learned prompts, we first obtain the a visual feature*  
 179 *set containing  $M = H \times W$  vectors and a prompt feature set containing  $N \times C$  vectors. Then, we*  
 180 *calculate the distance between the visual feature set and the prompt feature set of each class by OT*  
 181 *as (6). After obtaining the OT distance for each class, we sort the distance and classify the image.*

## 182 4 Experiments

183 Extensive experiments are conducted to evaluate our method, including comparison with CoOp,  
 184 ablation studies, parameter analysis extensibility analysis, computing cost analysis and visualization.

### 185 4.1 Datasets

186 We followed the experimental settings in the CoOp [63] for the few-shot learning evaluation. The  
 187 experiments are conducted on the 11 visual recognition datasets, including Caltech101 [9], DTD [5],  
 188 EuroSAT [12], FGVC Aircraft [29], Flowers102 [32], Food101 [3], ImageNet [7], OxfordPets [33],  
 189 StanfordCars [21], SUN397 [55], and UCF101 [47]. These datasets span visual classification of  
 190 generic objects, scenes, actions, fine-grained categories, and so on, which constitutes a comprehensive  
 191 evaluation of our method. All experiments adopted the few-shot evaluation protocol used in CLIP [39]  
 192 and CoOp [63], where we respectively choose 1, 2, 4, 8, and 16 shots for model training and use the  
 193 original test set for evaluation. Besides, we also evaluated the robustness of our method with domain  
 194 shift. Following CoOp, we used the ImageNet as the source domain and evaluate our method with  
 195 ImageNet-based robustness evaluation datasets including ImageNetV2 [43], ImageNet-Sketch [52],  
 196 ImageNet-A [14], and ImageNet-R [13]. A detailed introduction of each dataset can be found in the  
 197 supplementary materials.

### 198 4.2 Implementation details

199 We chose CoOp [63] as our main competitor to evaluate our method. Compared with CoOp which  
 200 only learns a global prompt for one class, our PLOT method learns multiple local prompts and applies  
 201 the OT distance for better fine-grained alignment. Besides, we also reported the performance of  
 202 training a linear classifier with the CLIP [39] features. It is also a widely-used strategy to adapt the  
 203 pretrained knowledge for the downstream task [46]. We reproduced the performance of CoOp and  
 204 the CLIP linear probe with the released official code.

205 The original CoOp method has different versions with different class token positions and parameter  
 206 initialization strategies. We applied the default model that fixes the class token positions in the end due  
 207 to the limited performance gap between two different ways of positioning the class token. Besides, we  
 208 used the random parameter initialization strategy but not the class-specific context version. Following  
 209 the widely used setting in [63, 64, 10, 58], we also chose RN50 [11] as the backbone network of the  
 210 visual branch and set the length of learnable context tokens as 16. All the code of our method is based  
 211 on CoOp, which adopted the SGD optimizer with 0.002 initial learning rate, CosineAnnealingLR

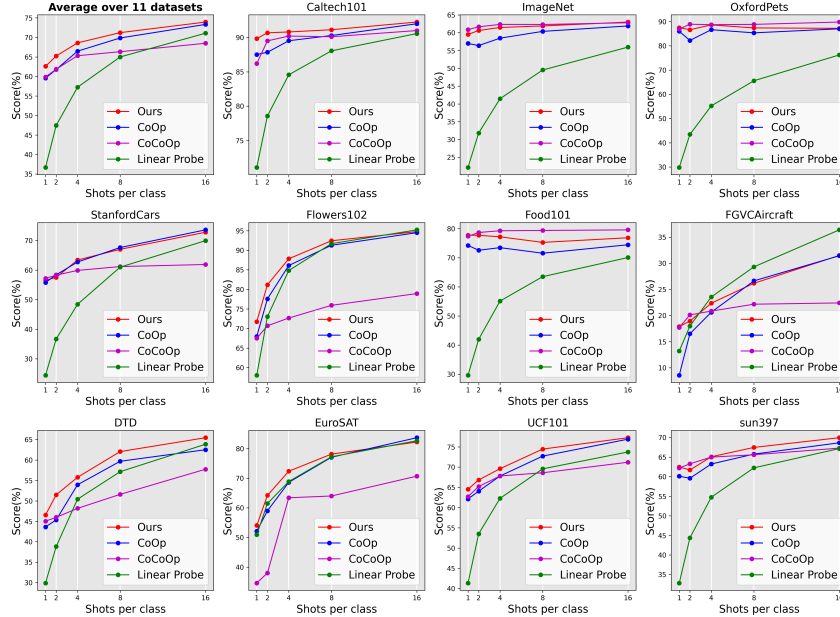


Figure 3: The few-shot learning results on 11 datasets. We compare our PLOT with CoOp, *CoCoOp*, and the Linear Probe method and observe the consistent and significant performance improvement on most datasets. (The average accuracy on all datasets is shown on the left top.)

Table 1: Comparison with CoOp on robustness to domain shift.

Method	Source	Target			
	ImageNet	-V2	-Sketch	-A	-R
CLIP + CoOp	61.91	54.26	32.47	21.78	54.21
CLIP + PLOT ( $N=4$ )	<b>63.01</b>	<b>55.11</b>	<b>33.00</b>	<b>21.86</b>	<b>55.61</b>

212 schedule, and a warmup trick with  $1e-5$  learning rate. Besides, we also followed the epoch strategy to  
 213 train more epochs for more shots.

214 We apply  $N = 4$  prompts for each category and use  $M = 7 \times 7$  due to the feature map size. We set  
 215 the hyper-parameters in the Sinkhorn distances algorithm [6] as  $\lambda = 0.1$  for all the datasets. We set  
 216 the maximum iteration number of the inner loop as 100 and will early stop the iteration when the  
 217 average absolute update value  $\Lambda < 0.01$ . We initialize all values in the vector  $v$  and  $\mu$  as  $1/N$   
 218 and  $1/M$  respectively. All models are conducted on the Pytorch [34] 1.7.1 and trained on 4 NVIDIA  
 219 A100 GPUs. We repeated the experiments three times with different seeds and reported the average.

### 220 4.3 Comparison With CoOp

221 In this subsection, we compare our PLOT with the baseline CoOp on the few-shot recognition and  
 222 domain generalization tasks.

223 **Few-Shot Learning** We summarized the experimental results in Figure 3 where the red line denotes  
 224 our PLOT method, the blue one denotes CoOp, *the purple line denotes CoCoOp*, and the green one  
 225 is the CLIP linear probe. The detailed accuracy can be found in the supplementary materials. We  
 226 observed that both prompt learning methods (PLOT and CoOp) outperform the linear probe method  
 227 by a large margin. Besides, PLOT can further improve the performance of CoOp and *CoCoOp*  
 228 on most of the datasets. Taking the average accuracy (at the left top) as the example, Plot respectively  
 229 gained 3.03%, 3.45%, 2.13%, 1.38%, 0.61% performance boost over CoOp at 1, 2, 4, 8, 16 shots. We  
 230 found the performance gap will reduce when shots increase. It is not surprising since both CoOp  
 231 and PLOT focus on utilizing the pre-trained knowledge, and the effect of pre-training diminishes  
 232 given more training data. Among all datasets, PLOT achieves a larger improvement over CoOp on  
 233 the FOOD101 and DTD datasets and achieves comparable performance only on the StanfordCars  
 234 datasets. For the FGVCAircraft dataset in which the CoOp only obtains 7.77% accuracy, our PLOT  
 235 can achieve an accuracy of 17.79%, twice as high as that of the CoOp. Note that we don't use the  
 236 class-specific context, thus the performance on the fine-grained classification datasets is lower, e.g.

Table 2: *Ablation studies on few-shot recognition. PLOT is our defined model with  $N = 4$ , CoOp is the baseline method, M denotes that we respectively match the global visual feature and multiple textual prompts, V denotes that we apply a constraint to add the variance of prompts, M indicates using the visual feature map instead of the global visual feature.*

Dataset	Settings	1 shot	2 shots	4 shots	8 shots	16 shots
Caltech101	PLOT	<b>89.83 ± 0.33</b>	<b>90.67 ± 0.21</b>	<b>90.80 ± 0.20</b>	<b>91.54 ± 0.33</b>	<b>92.24 ± 0.38</b>
	CoOp	87.51 ± 1.02	87.84 ± 1.10	89.52 ± 0.80	90.28 ± 0.42	91.99 ± 0.31
	G	88.13 ± 0.36	86.98 ± 1.25	88.45 ± 0.79	90.16 ± 0.22	90.72 ± 0.18
	G+V	88.28 ± 0.43	87.72 ± 1.25	88.45 ± 0.30	89.82 ± 0.20	92.00 ± 0.13
	M	69.78 ± 1.75	71.57 ± 1.59	77.18 ± 2.16	81.77 ± 0.47	86.21 ± 0.20
	M+V	66.11 ± 8.29	71.45 ± 3.98	79.30 ± 3.96	86.96 ± 0.78	89.80 ± 0.17
DTD	PLOT	<b>46.55 ± 2.62</b>	<b>51.24 ± 1.95</b>	<b>56.03 ± 0.43</b>	<b>61.70 ± 0.35</b>	<b>65.60 ± 0.82</b>
	CoOp	43.62 ± 1.96	45.35 ± 0.31	53.94 ± 1.37	59.69 ± 0.13	62.51 ± 0.25
	G	45.12 ± 1.69	48.39 ± 2.08	54.75 ± 0.48	60.15 ± 0.70	63.59 ± 0.76
	G+V	45.90 ± 2.00	48.50 ± 0.99	53.96 ± 0.48	59.69 ± 1.01	63.51 ± 0.66
	M	13.18 ± 4.57	12.25 ± 3.86	13.00 ± 4.73	20.76 ± 5.42	26.99 ± 1.98
	M+V	12.61 ± 5.93	15.11 ± 1.81	20.35 ± 1.33	44.13 ± 2.39	56.85 ± 0.54
FOOD101	PLOT	<b>77.74 ± 0.47</b>	<b>77.70 ± 0.02</b>	<b>77.21 ± 0.43</b>	<b>75.31 ± 0.30</b>	<b>77.09 ± 0.18</b>
	CoOp	74.25 ± 1.52	72.61 ± 1.33	73.49 ± 2.03	71.58 ± 0.79	74.48 ± 0.15
	G	74.63 ± 0.11	70.15 ± 0.49	70.41 ± 0.46	70.72 ± 0.98	73.68 ± 0.46
	G+V	74.83 ± 0.31	70.09 ± 0.85	70.86 ± 0.22	70.80 ± 0.68	73.93 ± 0.35
	M	52.02 ± 4.86	46.12 ± 1.46	46.86 ± 1.39	53.43 ± 0.88	61.28 ± 0.23
	M+V	46.52 ± 1.15	45.95 ± 2.66	53.57 ± 0.83	62.95 ± 0.37	67.63 ± 1.11

Table 3: *Parameter analysis for the number of prompts*

Dataset	Settings	1 shot	2 shots	4 shots	8 shots	16 shots
Caltech101	N=1	88.47 ± 1.15	89.19 ± 0.39	89.70 ± 0.38	90.45 ± 0.24	91.56 ± 0.14
	N=2	88.86 ± 0.51	89.60 ± 0.10	90.60 ± 0.17	91.25 ± 0.65	91.89 ± 0.36
	N=4	<b>89.83 ± 0.33</b>	<b>90.67 ± 0.21</b>	90.80 ± 0.20	<b>91.54 ± 0.33</b>	<b>92.24 ± 0.38</b>
	N=8	89.74 ± 0.30	90.18 ± 0.46	<b>91.02 ± 0.18</b>	91.28 ± 0.28	92.04 ± 0.29
DTD	N=1	43.91 ± 0.65	48.21 ± 2.20	53.69 ± 1.10	58.90 ± 0.19	62.85 ± 0.74
	N=2	45.59 ± 2.46	48.06 ± 1.92	55.58 ± 1.71	61.56 ± 0.17	64.60 ± 0.92
	N=4	46.55 ± 2.62	51.24 ± 1.95	<b>56.03 ± 0.43</b>	61.70 ± 0.35	<b>65.60 ± 0.82</b>
	N=8	<b>46.89 ± 1.94</b>	<b>51.87 ± 2.06</b>	54.45 ± 0.48	<b>62.20 ± 0.56</b>	65.25 ± 0.38
FOOD101	N=1	75.96 ± 0.48	76.12 ± 0.59	77.11 ± 0.41	76.56 ± 0.69	77.43 ± 0.80
	N=2	77.12 ± 0.49	76.89 ± 0.23	76.16 ± 0.52	75.23 ± 0.69	76.81 ± 0.50
	N=4	77.74 ± 0.47	77.70 ± 0.02	77.21 ± 0.43	75.31 ± 0.30	77.09 ± 0.18
	N=8	<b>78.05 ± 0.15</b>	<b>78.19 ± 0.07</b>	<b>78.12 ± 0.17</b>	<b>76.63 ± 0.22</b>	<b>77.48 ± 0.12</b>

237 the performance of both CoOp and PLOT without class-specific context is lower than the linear  
 238 probing on FGVCaircraft. All these performance comparisons can serve as experimental evidence to  
 239 demonstrate that multiple local prompts and optimal transport distance facilitate the prompt learning  
 240 of vision-language models. *On StanfordCar, learning multiple prompts didn't significantly improve*  
 241 *the performance over a single prompt. It may be because the discriminative characters in this dataset*  
 242 *coincide with each other, such that one global prompt and one global visual feature can work well.*

243 **Domain generalization** The robustness also plays a critical role in model applications since the  
 244 real-world environment may have large domain shifts with the training data. Therefore, we conducted  
 245 a robustness evaluation to investigate the transferability of models learned by PLOT.

246 Table 1 summarizes the results of our PLOT method and CoOp on four ImageNet-based robustness  
 247 evaluation datasets. For both methods, we trained the models on ImageNet with 16 shots per class.  
 248 For PLOT, we set the number of prompts as  $N = 4$ . We can observe that PLOT outperforms CoOp  
 249 consistently on both source and target domains. These experimental results demonstrate that the  
 250 performance improvement of our learning multiple prompts doesn't rely on single-domain overfitting.

#### 251 4.4 Ablation Studies and More Analysis

252 In this subsection, we conducted the ablation studies to investigate the effectiveness of different  
 253 components, in order to answer the following questions.

254 **Q: Can we directly learn multiple prompts by respectively matching each prompt with the**  
255 **global visual feature? A: No.** As shown in Table 2, we report the performance of directly matching  
256 the global visual feature (notated as “G”) and compare it with the baseline CoOp and our PLOT on  
257 three datasets including Caltech101, DTD, and FOOD101. We observe that there is no improvement  
258 over the baseline on some datasets (such as Caltech101 and FOOD101) if we only directly match  
259 prompts and global features. Though “G” obtained the improvement on the DTD dataset, this  
260 improvement is still less than that of PLOT. It is because this “G” method is incentivized to learn the  
261 indistinguishable prompts, which contradicts our purpose to learn multiple comprehensive prompts.  
262 We further add some constraints to push away the prompt from each other. For example, we add an  
263 objective function to add the distance between every two prompts as a regularization term, which  
264 is notated as “V”. However, comparing “G” and “G+V”, we do not find significant and consistent  
265 improvement when using variance loss.

266 **Q: Does the improvement mainly come from using all feature maps? A: No.** In PLOT, we apply  
267 all feature maps of the visual encoder branch, where each feature is a local embedding at one spatial  
268 position. Compared with the global feature, these local features are more informative and contain  
269 fine-grained clues. However, we demonstrate that the improvement of PLOT does not only rely on  
270 using all feature maps. On the contrary, directly using the feature map to replace the global feature  
271 causes a large performance drop. For example, on all three datasets, directly using the feature map  
272 (“M” or “M+V”) has an around 20% 1 shot accuracy drop over using the global visual feature. It  
273 is not surprising since the original CLIP model is trained by matching the global visual feature and  
274 language feature. Without using the OT method, the distance between the feature map and multiple  
275 textual prompts degenerates to the mean distance of each feature-prompt pair. Besides, when using  
276 the feature map, adding the variance loss works well, especially for more shots. For example, the  
277 accuracy on 16 shots DTD is improved by a large margin (from 26.99 to 56.85).

278 **Q: How many prompts are needed? A: 4 prompts are enough** One important hyper-parameter  
279 in PLOT is the number of prompts. To analyze the effect of the number of prompts, we conducted  
280 the experiments on three datasets with 1, 2, 4, 8 prompts. The results are summarized in the white  
281 part of Table 3. We can observe that the performance obviously increases when adding the number  
282 of prompts from 1 to 4. For example, PLOT (N=4) respectively obtains 1.36%, 2.64%, and 1.68%  
283 1-shot accuracy improvement over PLOT (N=1) on three datasets. Besides, when we further increase  
284 the number of prompts, the improvement is not consistent. To balance the improvement and cost,  
285 we set  $N = 4$  as the default configuration of our PLOT model. In the experiments, we tuned this  
286 hyper-parameter on the Caltech101 dataset and applied it to other datasets.

287 **Q: Can PLOT benefit zero-shot learning? A: No.** CLIP [39] shows that manually designing the  
288 prompts can still achieve good performance. We obtain 7 prompts by prompt engineering on the  
289 ImageNet dataset and can further ensemble them to obtain **60.38%** top 1 accuracy. In this section,  
290 we replace the cosine distance between the global visual feature and prompt ensemble with the  
291 OT distance between the feature map and all 7 prompts. However, without any learning, the OT  
292 distance only obtains **58.78%** accuracy. *It is a limitation of the PLOT to still need few-shot data  
293 for optimization, which cannot be directly applied in the zero-shot setting. We argue there are two  
294 reasons why the OT distance does not work without learning: 1) prompt engineering selects prompts  
295 based on the global feature and cosine distance, instead of OT distance with feature map; 2) all these  
296 selected prompts are closed to the global feature and lack the complementarity.*

297 **Q: Can PLOT benefit Adapter-based methods? A: Yes.** Adapter-based methods [10, 58] is another  
298 research direction of the efficient adaptation of pre-trained vision-language models. Different from  
299 the prompt learning that fixes the model parameters and tunes the language prompt, adapter-based  
300 methods [10, 58] allow for fine-tuning a part of the network or adding an extra model for training.  
301 Recently, adapter-based methods also achieve good performance on few-shot visual recognition.  
302 Therefore, we want to explore whether our PLOT method can benefit them, and how.

303 We apply the Tip-adapter-F [58] as our baseline method, which learns a  $Linear(d, N_{cls} \times K_{shots})$   
304 model to describe one image by the similarity with all training samples, where  $d$  is the dimension of  
305 visual feature,  $N_{cls}$  is the number of categories (e.g. 1000 in ImageNet), and  $K_{shots}$  is the number  
306 of shots. Then, the final similarity consists of the original distance between the visual feature and  
307 prompt ensembling and the new distance calculated by the learned feature and one-hot vector of  
308 labels (whose dimension is  $(N_{cls} \times K_{shots}, N_{cls})$ ). Please find details in Tip-adapter-F [58]. To  
309 introduce PLOT to this framework, we first used the feature map to replace the global feature and



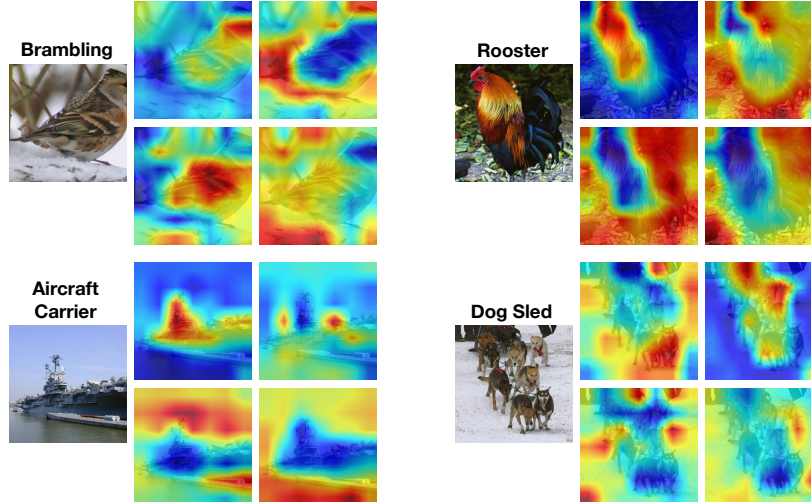


Figure 4: *Visualizations. We provide the heatmaps of transport plan  $T$  related to each prompt on 4 categories in ImageNet. Different transport plans focus on different attributes of the object.*

Table 4: Comparison with Adapter-based method.

Dataset	Methods	1 shot	2 shots	4 shots	8 shots	16 shots
ImageNet	Tip-Adapter-F	61.32	61.69	62.52	64.00	65.51
	Tip-Adapter-F + OT	61.44	61.98	62.86	64.13	65.76
	Tip-Adapter-F + PLOT	<b>62.27</b>	<b>64.31</b>	<b>63.89</b>	<b>65.04</b>	<b>66.17</b>

310 then learned multiple linear models. As a result, with different local features and different linear  
 311 models, we can obtain a  $M \times N$  distance matrix and apply the Sinkhorn algorithm [6] to calculate  
 312 the OT distance. Furthermore, we can apply the learned prompts as co-partner of the ensembling  
 313 prompt to refine the final similarity.

314 Table 4 summarizes the few-shot recognition results of the original Tip-Adapter-F method and our  
 315 adapter-based PLOT methods on ImageNet. From this table, We observe that using the OT distance  
 316 can improve the performance of the adapter-based method. Using the learned prompts, we can further  
 317 promote the accuracy of all settings.

318 **Q: What is the extra computation time cost of PLOT over CoOp baseline? A: Around 10%  
 319 inference speed and 5% training time. *Despite the performance improvement, the extra computation  
 320 cost is still a limitation of PLOT. Please see the detailed analysis in the supplementary materials.***

## 321 4.5 Visualization

322 In this subsection, we provide some visualization examples of the transport plans  $T$  related to different  
 323 prompts ( $N=4$ ). We translate each transport plan into colorful heatmaps and resize them into their  
 324 original size and combine them with the raw image. As shown in Figure 4, we provide the heatmaps  
 325 of 4 categories in ImageNet. We observe that different transport plans highlight different regions of  
 326 the image, which demonstrates that the learned multiple prompts are complementary. For the class  
 327 “Brambling”, the prompts respectively focus on the head, tail, wing, and environment. For “Dog  
 328 Sled”, the prompts are related to dogs, the sled, some ties, and the snow environment.

## 329 5 Conclusion

330 In this paper, we present a method, named PLOT, to learn multiple comprehensive prompts to  
 331 describe diverse characteristics of one category. To avoid convergence to one point, we propose to  
 332 apply the optimal transport to achieve the fine-grained alignment between both vision and language  
 333 domains. We apply a two-stage optimization strategy where the inner loop fixes the prompts and  
 334 learns the transport plan to calculate the cross-modality distance, and the outer loop uses this distance  
 335 to optimize the prompt learner. We build our method on the base of CoOp and achieve significant  
 336 improvement on the few-shot recognition task in various datasets, which demonstrates the advantage  
 337 to learn multiple prompts instead of a single one.

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## 482 Checklist

- 483 1. For all authors...
- 484 (a) Do the main claims made in the abstract and introduction accurately reflect the paper’s contribu-  
485 tions and scope? [Yes]
- 486 (b) Did you describe the limitations of your work? [Yes] See our analysis in Section 4.4. 1) Our  
487 method is still need few-shot data for optimization, which cannot be applied in zero-shot setting.  
488 2) The method needs more computing cost than CoOp.
- 489 (c) Did you discuss any potential negative societal impacts of your work? [N/A] We propose  
490 a general framework for using the vision-language pre-trained model. It is not for specific  
491 applications, which does not directly involve societal issues.
- 492 (d) Have you read the ethics review guidelines and ensured that your paper conforms to them? [Yes]
- 493 2. If you are including theoretical results...
- 494 (a) Did you state the full set of assumptions of all theoretical results? [N/A]
- 495 (b) Did you include complete proofs of all theoretical results? [N/A]
- 496 3. If you ran experiments...
- 497 (a) Did you include the code, data, and instructions needed to reproduce the main experimental  
498 results (either in the supplemental material or as a URL)? [Yes]
- 499 (b) Did you specify all the training details (e.g., data splits, hyperparameters, how they were chosen)?  
500 [Yes]

- 501 (c) Did you report error bars (e.g., with respect to the random seed after running experiments  
502 multiple times)? [Yes]
- 503 (d) Did you include the total amount of compute and the type of resources used (e.g., type of GPUs,  
504 internal cluster, or cloud provider)? [Yes] See Section 4.2.
- 505 4. If you are using existing assets (e.g., code, data, models) or curating/releasing new assets...
- 506 (a) If your work uses existing assets, did you cite the creators? [Yes]
- 507 (b) Did you mention the license of the assets? [N/A]
- 508 (c) Did you include any new assets either in the supplemental material or as a URL? [No]
- 509 (d) Did you discuss whether and how consent was obtained from people whose data you're us-  
510 ing/curating? [N/A]
- 511 (e) Did you discuss whether the data you are using/curating contains personally identifiable informa-  
512 tion or offensive content? [N/A]
- 513 5. If you used crowdsourcing or conducted research with human subjects...
- 514 (a) Did you include the full text of instructions given to participants and screenshots, if applicable?  
515 [N/A]
- 516 (b) Did you describe any potential participant risks, with links to Institutional Review Board (IRB)  
517 approvals, if applicable? [N/A]
- 518 (c) Did you include the estimated hourly wage paid to participants and the total amount spent on  
519 participant compensation? [N/A]