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Thoughts Are All Over the Place: On the Underthinking of o1-Like LLMs

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Abstract

Large language models (LLMs) such as OpenAI's o1 have demonstrated remarkable abilities in complex reasoning tasks by scaling test-time compute and exhibiting human-like deep thinking. However, we identify a phenomenon we term under-015 thinking, where o1-like LLMs frequently switch between different reasoning thoughts without sufficiently exploring promising paths to reach a cor-018 rect solution. This behavior leads to inadequate 019 depth of reasoning and decreased performance, 020 particularly on challenging mathematical problems. To systematically analyze this issue, we conduct experiments on three challenging test sets and two representative open-source o1-like models, revealing that frequent thought switching cor-025 relates with incorrect responses. We introduce a novel metric to quantify underthinking by measur-027 ing token efficiency in incorrect answers. To ad-028 dress underthinking, we propose a decoding strat-029 egy with thought switching penalty (TIP) that dis-030 courages premature transitions between thoughts, encouraging deeper exploration of each reasoning path. Experimental results demonstrate that our approach improves accuracy across challenging 034 datasets without requiring model fine-tuning. Our 035 findings contribute to understanding reasoning inefficiencies in o1-like LLMs and offer a practical solution to align their problem-solving capabilities to human-like deep thinking. 039

1. Introduction

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Large Language Models (LLMs), such as OpenAI's o1 (OpenAI, 2024), have revolutionized artificial intelligence by enabling models to tackle increasingly complex tasks. The o1 model and its replicas (Qwen, 2024; DeepSeek, 2025; Kimi, 2025), known for their deep reasoning capabilities,

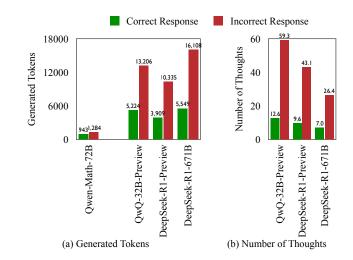


Figure 1. Illustration of the **underthinking issue** on the challenging AIME2024 testset: Incorrect responses from o1-like models (e.g., QwQ-32B-Preview and DeepSeek-R1-671B) often involve a higher frequency of switching reasoning strategies compared to correct answers (Figure b). This results in significantly longer response lengths without corresponding improvements in accuracy (Figure a). In contrast, conventional LLMs (e.g., Qwen-Math-72B) do not show significant differences in response length between incorrect and correct answers.

exemplify the potential of LLMs to exhibit human-like deep thinking by scaling test-time computation during problemsolving. These models aim to explore diverse reasoning strategies, reflect on their decisions, and iteratively refine solutions, closely mimicking human cognitive processes.

Despite their successes, a critical yet underexplored question remains: **Are o1-like LLMs thinking deeply enough?** This study provides an initial exploration of this problem. In this work, we investigate a phenomenon we term **underthinking**, which refers to the tendency of o1-like LLMs to prematurely abandon promising lines of reasoning, leading to inadequate depth of thought. To systematically analyze underthinking, we conduct experiments on three challenging test sets (e.g., MATH500, GPQA Diamond, and AIME2024) and two open-source o1-like models with visible long chains of thought (e.g., QwQ-32B-Preview and DeepSeek-R1-671B). Through extensive analyses, we found that underthinking manifests in the following patterns: (1)

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		Q: Let a, b, x, and y be real numbers with $a>4$ and $b>1$ such that $\frac{x^2}{a^2}+\frac{y^2}{a^2-16} = \frac{x^2}{b^2-1}+\frac{y^2}{b^2-1}+\frac{y^2}{b^2-1}$. Find the least possible value of $a+b$.
		So I've got this problem here that involves some equations with variables a, b, x, and y, and I need to find the least possible value of a + b given some conditions Perhaps I can think of this as a system of equations and try to solve for x and y in terms of a and b.
		Alternatively, maybe there's a geometric interpretation. Since both equations represent ellipses, perhaps the condition is that these ellipses are tangent to each other So, unless there's some transformation or something, they don't seem to be the same ellipse.
n 1		Alternatively, perhaps the problem is that for some (x,y), both equations hold simultaneously, and I need to find a and b such that this is possible solve the first equation for y in terms of x and substitute into the second equation. But that seems messy.
Solution1		Alternatively, perhaps I can consider this as an optimization problem where I need to minimize a + b subject to the condition that the equations have a solution But I'm not sure how to set that up algebraically.
		Alternatively , perhaps I can consider the distance between the centers of the two ellipses and relate it to their axes But $(y - 11)^2$ is $y^2 - 22y + 121$. However, I only have y^2 , not y. So maybe this isn't the best way to substitute.
	20 More T Averaged 2a	
		Given that, perhaps I need to accept that this problem is beyond my current ability and seek help or look for a different problem.
		Final Answer: \[\boxed{15} \]

Figure 2. An example of underthinking issue for QwQ-32B-Preview model's output response that consists of 25 reasoning thoughts within a single solution. Generally, thought does not reach a conclusion.

it occurs more frequently on harder problems, (2) it leads
to frequent switching between different thoughts without
reaching a conclusion in each, and (3) it correlates with
incorrect responses due to insufficient exploration of reasoning paths. For example, Figure 1 compares the token usage
and number of thoughts of correct and incorrect responses.
On average, o1-like LLMs consume 225% more tokens in
incorrect responses than in correct ones due to 418% more
frequent thought-switching behaviors.

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090 To quantify this phenomenon, we introduce a novel under-091 thinking metric that measures token efficiency in incorrect 092 responses by evaluating the proportion of the response that 093 contributes to reaching correct thoughts. Combining the 094 widely-used accuracy metric with the proposed underthink-095 ing metric provides a more comprehensive assessment of 096 o1-like models: accuracy measures how often the model can 097 produce correct responses, while the underthinking metric 098 evaluates the token efficiency within incorrect responses 099 that contributes to reaching correct thoughts. 100

In response to these findings, we propose a decoding strategy with thought switching penalty (TIP) that discourages premature transitions between thoughts during the generation process. By adjusting decoding penalties for tokens associated with thought switching, the model is encouraged to thoroughly develop each line of reasoning before considering alternatives. Experimental results show that employing TIP improves accuracy across challenging test sets without requiring additional model fine-tuning.

Our study makes the following contributions:

- We formally define and characterize the underthinking issue in o1-like LLMs, where models frequently abandon promising reasoning paths prematurely, leading to inadequate depth of reasoning on challenging problems.
- We introduce a novel metric to evaluate underthinking by measuring token efficiency in incorrect responses, providing a quantitative framework to assess reasoning inefficiencies.
- 3. We propose a decoding approach with thought switching penalty (TIP) that encourages models to deeply explore each reasoning thought before switching, improving accuracy without additional model fine-tuning.

2. Observing Underthinking Issues

In this section, we present a comprehensive analysis of outputs from o1-like models on *challenging math problems*. We begin by illustrating the frequent thinking switch phenomenon observed in responses to these problems, as shown in Figure 2, highlighting how this behavior differs significantly between correct and incorrect answers (Section 2.1). We then show that this phenomenon leads to an inadequate depth of reasoning, causing models to *abandon promising*

Thoughts Are All Over the Place: On the Underthinking of o1-Like LLMs

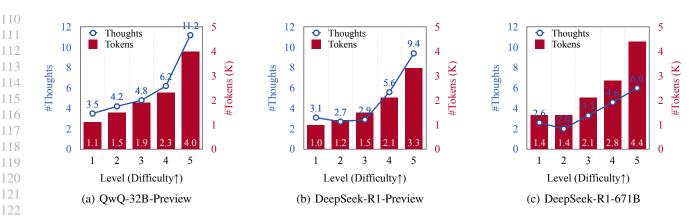


Figure 3. Average number of thoughts and tokens in generated responses across different difficulty levels of the MATH500 test set.

reasoning paths prematurely (Section 2.2). Based on this observation, we propose a metric to empirically assess the underthinking issues and present empirical results in Section 2.3. We conclude that *o1-like LLMs often underthink* when they fail to tackle challenging math problems.

2.1. Frequent Thinking Switch of o1-Like LLMs

We conduct experiments on three testsets:

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MATH500 (Hendrycks et al., 2021): a challenging dataset consisting of problems from high school math competitions across seven subjects (e.g., Prealgebra, Algebra, Number Theory) and difficulty levels based on AoPS (ranging from 1 to 5). Problems in these competitions range from level 1, the easiest, often found in AMC 8 exams, to level 5, like those in AIME.

GPQA (Rein et al., 2023): a graduate-level dataset consisting of multiple-choice questions in subdomains of physics, chemistry, and biology. For our experiment, we select the highest quality subset, known as GPQA Diamond (composed of 198 questions).

 AIME (MAA Committees): a dataset from the American Invitational Mathematics Examination, which tests math problem solving across multiple areas (e.g. algebra, counting, geometry, number theory, and probability). Because AIME 2024 contains only 30 examples, we also considered 60 more examples from AIME 2022 and 2023.

We mainly investigate two widely recognized opensource o1-like models featuring visible long CoT: QwQ-32B-Preview and DeepSeek-R1-671B. We also include DeepSeek-R1-Preview to show the development of R1 series models. Given DeepSeek-R1-Preview's daily message limit of 50 via web interface, we evaluated this model solely on the MATH500 and AIME test sets. **Definition of Reasoning Thoughts** In this paper, we define *thoughts* as the intermediate cognitive steps within a reasoning strategy produced by the model. O1-like LLMs often switch reasoning thoughts using terms like "alternatively". For instance, as shown in Figure 2, the problem-solving process involves multiple reasoning thoughts, shifting from algebraic manipulation to geometric interpretation and optimization strategies. The ability to switch between different reasoning strategies allows for a broader exploration of potential solutions and demonstrates the flexibility of the model in tackling complex problems. In this study, we provide a comprehensive analysis of the side effects associated with this ability to switch reasoning thoughts.

We utilize the Llama-3.3-70B model to automatically segment a response into reasoning thoughts due to its superior capabilities in both instruction following and mathematical reasoning. Initially, we manually analyzed responses from the QwQ-32B-Preview model to gather expressions indicative of shifts in thought. We then tasked the Llama-3.3-70B model with scanning the entire response to identify all occurrences of such expressions. Furthermore, we asked the model to determine whether these expressions truly signify a change in thought or merely reflect a stylistic pattern in the response. Only the expressions indicating a genuine thought shift were used as separators for reasoning processes.

o1-Like LLMs Switch Thinking More Frequently on Harder Problems Figure 3 shows the averaged thoughts and tokens in generated responses across various difficulty levels in the MATH500 test set. Clearly, all models generate more reasoning thoughts with the increase of difficulty level, which is consistent with the growth of generated tokens. This observation suggests that as the complexity of the problems increases, the models tend to switch thoughts more frequently. This behavior implies that o1-like LLMs are able to dynamically adjust their reasoning processes to tackle more challenging problems. The following experiments focus on Level 5 in the MATH500 test set (MATH500-Hard).

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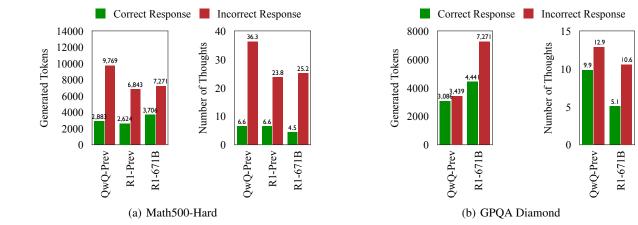


Figure 4. O1-like LLMs switch thinking more frequently on incorrect responses, thus expend more tokens without contributing to accuracy.

181 Increased Thought Switching in o1-Like LLMs during 182 **Incorrect Responses** When examining the behavior of 183 ol-like LLMs, we observe a distinct pattern in how they 184 handle incorrect responses. As depicted in Figures 1 and 4, 185 these models exhibit a significant increase in the frequency 186 of thought switching while generating incorrect answers 187 across all test sets. This trend suggests that although the 188 models are designed to dynamically adjust their cognitive 189 processes to solve problems, more frequent thought switch-190 ing does not necessarily lead to higher accuracy. Essentially, the models may be expending additional computational resources - evidenced by an increase in generated tokens -193 without achieving more accurate solutions. These insights are crucial because they highlight the need not only to ex-195 plore additional cognitive pathways when faced with chal-196 lenges but also to operate in a more targeted and efficient 197 manner, thereby improving accuracy even when complex reasoning is required. In the following sections, we empir-199 ically validate the inefficiencies associated with frequent 200 thought switching in incorrect responses. 201

2022032.2. Existence of Underthinking

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204 The behavior of frequent thinking switch in incorrect re-205 sponses could stem either from (1) genuine underthinking, 206 where the model succeeds in finding promising strategies but 207 fails to stick with them, or from (2) a lack of understanding, 208 prompting it to explore diverse but ineffective approaches. 209 To disentangle these possibilities, we propose an assessment 210 framework that evaluates whether an abandoned reasoning 211 path is actually sufficient to derive a correct answer. By 212 focusing on whether the model can persistently follow and 213 deepen a single, promising line of thought, we can identify 214 instances of underthinking. 215

Assessing Thought Correctness In the example presented in Figure 2, we observe that some early thoughts may lead to the correct answer. For instance, Thought 1 initiates a correct interpretation by recognizing that the given equations resemble those of ellipses centered at (0,0) and (20,11). Setting the two expressions equal is a valid approach to finding common points (x, y) that satisfy both equations. Instead of concentrating on thoroughly exploring the plausible thought with further algebraic manipulation and optimization techniques, the model frequently shifts its focus and uses approximately 7,270 additional tokens without arriving at a correct answer. Ultimately, it concludes with a guessed answer that lacks support from the extended COT process.

We leverage LLMs to assess whether each thought leads to a correct answer using the following prompt:

Problem P = {problem} Solution Draft S = {split solutions} Correct Answer A = {expected answer}

 Please analyze the relevance between the solution S and the problem P, and conduct some verifications to check the correctness of the solution itself. Please think step by step to give an explanation **EXPLANATION**.
 If you think the solution draft S can lead to the correct answer A of the problem P, please stick to the line of thinking without deviation and carry it through to completion. If you think it cannot yield the correct answer or you're not sure, don't force yourself to give an answer and generate **None**.

3. Please tell me honestly how confident you are that you can solve the problem P correctly based on the the solution draft S. Out of 2, please generate your confidence score **CONFIDENT_SCORE**.

Please output **EXPLANATION** and **CONFI-DENT_SCORE** according to the following format: EXPLANATION: \boxed{} CONFIDENT_SCORE: \boxed{}

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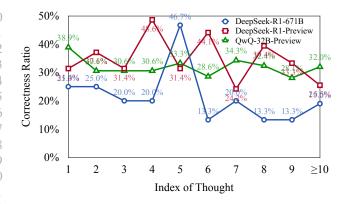


Figure 5. The ratio of correct reasoning thoughts at each index in incorrect responses. A notable portion of early-stage thoughts are correct but abandoned without being fully explored.

Specifically, we use two models distilled from DeepSeek-R1-671B based on Llama and Qwen – DeepSeek-R1-Distill-Llama-70B and DeepSeek-R1-Distill-Qwen-32B, which achieve new state-of-the-art results for dense models across various reasoning benchmarks. If at least one model generates a confidence score of 2 for a thought, we regard it as a correct thought.

We evaluate the accuracy of our assessment approach using responses generated by Qwen-32B-Preview for 90 instances from the AIME 2022, 2023, and 2024 test sets. We utilize the final thought in each response as the test example and its correctness as the ground-truth label. To ensure a fair comparison, we randomly streamline correct thoughts to match the average length of incorrect thoughts. Ultimately, we have 35 correct thoughts with an average length of 278.1 tokens and 55 incorrect thoughts with an average length of 278.3 tokens. Our assessment approach achieves accuracies of 82.9% for correct examples and 81.8% for incorrect examples, demonstrating its effectiveness.

Early-Stage Thoughts Are Correct but Abandoned in Incorrect Responses Figure 5 depicts the ratio of correct thoughts at each index in incorrect responses on the three challenging test sets. The analysis highlights a critical insight into the phenomenon of underthinking. Specifically, a notable proportion of initial thoughts across various models were correct but were not pursued to completion. This tendency to abruptly shift away from these promising thoughts indicates an inadequate depth of reasoning, where potentially correct solutions are prematurely abandoned before being thoroughly explored. This observation suggests a need for enhancing the models' ability to persistently explore a specific line of reasoning deeply and accurately before opting to switch to alternative thought processes.

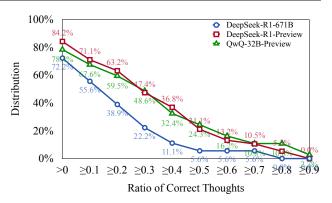


Figure 6. The distribution of thought correctness ratio in incorrect responses. Most incorrect responses contain correct thoughts.

Most Incorrect Responses Contain Correct Thoughts

Figure 6 illustrates the distribution of thought correctness ratios in incorrect responses from various models. We observe that over 70% of incorrect responses contain at least one correct thought. Furthermore, in more than 50% of these responses, over 10% of the thoughts are correct. Combined with observations from Figure 5, this suggests that while o1-like models can initiate correct reasoning pathways, they may struggle to continue these pathways to reach the correct conclusion. This highlights the importance of encouraging models to maintain and expand their **initial correct thoughts** to synthesize them into accurate final answers. These insights lead us to propose an underthinking metric based on the presence of the first correct thought in the subsequent section.

2.3. Empirical Underthinking Results

In this section, we propose a metric for empirically assessing underthinking issues based on token efficiency, complementing the widely used accuracy metric.

Underthinking Metric Intuitively, if a model generates a correct thought at an early stage and then switches to other thoughts without reaching a correct answer, the tokens generated thereafter do not contribute to reaching a correct solution and are considered inefficient due to underthinking. The underthinking score, denoted as ξ_{UT} , is defined as:

$$\xi_{UT} = \frac{1}{N} \sum_{i=1}^{N} \left(1 - \frac{\hat{T}_i}{T_i} \right) \tag{1}$$

Here, N represents the number of instances in a given test set where the evaluated model generates **incorrect responses**. T_i is the total number of tokens in the *i*-th incorrect response, and \hat{T}_i is the number of tokens from the beginning of that response up to and including the first correct thought. If there is no correct thought in the *i*-th response,

Models	Accuracy(↑)	UT Score (↓	
MATH500-Hard (Level 5)			
QwQ-32B-Preview	84.3	58.2	
DeepSeek-R1-Preview	83.6	61.5	
DeepSeek-R1-671B	92.5	65.4	
GPQA Diamond			
QwQ-32B-Preview	59.6	48.3	
DeepSeek-R1-671B	73.2	58.8	
QwQ-32B-Preview	46.7	65.0	
DeepSeek-R1-Preview	46.7	75.7	
DeepSeek-R1-671B	73.3	37.0	

292 $\hat{T}_i = T_i$, indicating that the model lacks an understanding 293 of this problem, leading it to explore diverse but ineffective 294 approaches. Therefore, it cannot be considered underthink-295 ing. Consider Figure 2 as an example: the first reasoning 296 thought can reach a correct answer if fully explored, with 297 $\hat{T} = 411$. Consequently, $\xi_{UT} = 1 - \frac{411}{7681} = 0.946$, which 298 can be considered extremely inefficient, reflecting a high 299 underthinking score.

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The metric ξ_{UT} quantifies the extent of underthinking by measuring the token efficiency in generating effective content within an incorrect response. Specifically:

305• A lower value of ξ_{UT} indicates higher token efficiency,
meaning that a greater proportion of tokens in incorrect
responses contribute towards reaching a correct thought
before switching to another thought. This suggests that
the model is more efficient in its token utilization even
when it fails to provide a correct answer.

³¹¹ • Conversely, a higher value of ξ_{UT} signifies lower token efficiency, indicating that a larger proportion of tokens do not contribute effectively towards generating a correct thought. This reflects greater underthinking, where the model may generate redundant or irrelevant tokens by frequently switching thoughts.

319 **Empirical Results** Table 1 provides insights into model 320 performance across challenging test sets, evaluating both 321 accuracy and underthinking (UT) scores. Clearly, all o1-322 like LLMs suffer from significant underthinking issues, al-323 though there are considerable differences across models 324 and test sets. The results reveals that the relationship be-325 tween model accuracy and underthinking varies across different datasets. On the MATH500-Hard and GPQA Di-327 amond datasets, higher accuracy achieved by the supe-328 rior DeepSeek-R1-671B model is accompanied by higher 329

UT Scores, indicating more underthinking in incorrect responses. This suggests that while the model is more capable overall, it may produce longer but less effective reasoning when uncertain, possibly due to exploring multiple incorrect reasoning paths without efficiently converging on the correct solution. Conversely, on the AIME2024 test set, the DeepSeek-R1-671B model not only attains higher accuracy but also exhibits a lower UT score, reflecting less underthinking and greater token efficiency. This implies that the model's reasoning remains focused and effective even when it does not arrive at the correct answer, perhaps due to better alignment with the problem types and reasoning processes required by the AIME2024 task.

These findings illustrate that underthinking behavior is sensitive to the nature of the dataset and the tasks involved. The larger model's superior capabilities do not uniformly translate to less underthinking across all tasks. In some cases, increased model capacity leads to more elaborate but inefficient reasoning in incorrect responses, while in others, it enhances both accuracy and reasoning efficiency. Understanding the underthinking phenomenon is crucial for developing models that not only provide correct answers but also exhibit effective reasoning processes.

3. Mitigating Underthinking Issues

In this section, we propose a lightweight mechanism that mitigates underthinking issues without requiring any model fine-tuning. Our experimental results using the QwQ-32B-Preview model demonstrate the effectiveness of this approach across all challenging test sets.

3.1. Decoding with Thought Switching Penalty

Aforementioned findings show that o1-like LLMs prioritize exploring many solutions over deeply investigating one. Inspired by the success of the coverage penalty in neural machine translation (Tu et al., 2016; Wu et al., 2016), we propose a novel decoding algorithm with a *thought switching penalty* to encourage the model to explore potential thoughts more thoroughly before moving on to new ones.

Standard Decoding In standard decoding, the probability of each token v at position t is computed using the softmax function over the logits $\mathbf{z}_t \in \mathbb{R}^{|V|}$ (where |V| is the vocabulary size) in the output layer:

$$P(x_t = v | x_{< t}) = \frac{\exp(z_{t,v})}{\sum_{v' \in V} \exp(z_{t,v'})}$$

where $z_{t,v} \in \mathbf{z}_t$ is the logit (unnormalized score) for token v. By repeating this step for each position in the sequence, the model generates sequences of tokens, computing probabilities for each possible continuation.

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Table 2. Accuracy on AIME2022-2023 with res	pect to different
values of α and β .	

Pa	ass@1	α			
Ac	curacy	3	5	10	20
	300	35.2	37.0	39.0	39.4
	400	39.3	37.1	37.1	38.4
β	500	38.5	38.7	39.1	39.2
	600	39.8	39.4	38.0	38.0
	700	37.1	39.4	39.0	38.3

Thought Switching Penalty (TIP) To encourage the model to delve deeper into current thoughts before switching, we introduce a penalty on tokens that are associated with thought transitions. Let $\hat{V} \subset V$ be the set of tokens associated with thought switching (e.g., "alternatively"). We modify the logits as follows:

$$\hat{z}_{t,v} = \begin{cases} z_{t,v} - \alpha, & \text{if } v \in \widehat{V} \text{ and } t < \Psi + \beta \\ z_{t,v}, & \text{otherwise} \end{cases}$$

where

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- α ≥ 0 (*Penalty Strength*) is a parameter controlling the strength of the penalty applied to thought-switching tokens. A larger α results in a greater reduction of the logits for these tokens, making them less likely to be chosen.
- β ≥ 0 (*Penalty Duration*) specifies the number of positions from the start of a thought at Ψ, during which the penalty is active. A larger β extends the penalty over more positions, further discouraging early thought switching.

When $\alpha = 0$ or $\beta = 0$, the penalty is effectively disabled, and the decoding process reduces to the standard decoding algorithm. The adjusted logits $\hat{z}_{t,v}$ reduce the probability of generating thought-switching tokens within a specified window, encouraging the model to continue expanding on the current thought before moving on.

The new probability distribution becomes:

$$\hat{P}(x_t = v \,|\, x_{< t}) = \frac{\exp\left(\hat{z}_{t,v}\right)}{\sum_{v' \in V} \exp\left(\hat{z}_{t,v'}\right)}$$

3.2. Experimental Results

We conducted the experiments using QwQ-32B-Preview, as the DeepSeek-R1-671B API does not allow for the modification of logits. To ensure a robust conclusion, we report Pass@1 results with four samples.

³⁸¹ By adjusting α and β , we can control the model's behavior to achieve the desired level of thought exploration. We performed a grid search with α values in [3, 5, 10, 20] and

Table 3. Results of the	e proposed decoding with TIP.
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Models	Pass@1				
Trioucis	Accuracy(†)	UT Score (\downarrow)			
MATH500-Hard (Level 5)					
QwQ-32B-Preview	82.8	71.1			
+ TIP	84.3	69.7			
GPQA Diamond					
QwQ-32B-Preview	57.1	59.1			
+ TIP	59.3	56.5			
AIME2024					
QwQ-32B-Preview	41.7	72.4			
+ TIP	45.8	68.2			

 β values in [300, 400, 500, 600, 700] using a development set that included the AIME 2022 and 2023 test sets. Table 2 lists the impact of varying the penalty strength α and penalty duration β on the model's accuracy. We observe that increasing the penalty strength α generally leads to an improvement in accuracy up to a certain threshold, after which the benefits plateau or even diminish. Adjusting the penalty duration β also significantly affects performance: At a lower penalty strength ($\alpha = 3$), increasing β from 300 to 600 results in accuracy gains from 35.2% to 39.8%, the highest observed accuracy in our experiment. Conversely, at higher penalty strengths ($\alpha = 20$), extending β beyond 300 leads to a decrease in accuracy, indicating that too long a penalty duration can hinder performance when combined with a strong penalty. We selected $\alpha = 3$ and $\beta = 600$ for our subquent experiments.

Table 3 lists the results of our approach in the three challenging test sets. Clearly, our approach consistently improves accuracy over the vanilla QwQ-32B-Preview in all cases by mitigating the underthinking issues. These consistent improvements across diverse and challenging datasets validate the effectiveness of the TIP approach in mitigating the underthinking issue identified in o1-like LLMs. By penalizing thought switches during decoding, TIP encourages the model to elaborate more thoroughly on each reasoning thought before considering alternative ones. This mechanism aligns with the human problem-solving process, where a focused and in-depth exploration of a particular approach often leads to correct solutions, especially in complex mathematical problem-solving contexts.

4. Related Work

4.1. Scaling Test-Time Compute

The advent of deep reasoning models, epitomized by OpenAI's o1, has sparked significant interest in scaling test-time 385 compute to enhance models' abilities to solve complex prob-386 lems. Scaling test-time compute often involves two major 387 strategies. The first is expanding the search space, which 388 aims to broaden the scope of candidate solutions explored 389 during decoding to ensure better final outcomes. Techniques 390 in this category include self-consistency (Wang et al., 2023), where multiple answers are generated with a majority vot-392 ing mechanism to select the final answer. Other methods include best-of-n decoding and minimum Bayes risk decoding (Lightman et al., 2024; Li et al., 2023; Khanov et al., 395 2024; Heineman et al., 2024; Wu et al., 2024).

396 The second direction, and arguably more transformative, 397 focuses on human-like deep thinking. Efforts such as 398 QwQ (Qwen, 2024), DeepSeek-R1 (DeepSeek, 2025) and 399 Kimi-1.5 (Kimi, 2025), which aim to replicate OpenAI's 400 o1, leverage reinforcement learning (RL) to endow models 401 with advanced reasoning capabilities. Under large-scale RL 402 training, these models exhibit emergent human-like think-403 ing abilities characterized by deep, extended, and strategic 404 reasoning. This allows them to explore diverse strategies, 405 reflect on their decisions, revisit previous steps, and ver-406 ify their conclusions. Such human-like thinking markedly 407 improves accuracy, especially on complex reasoning tasks. 408

409 Efficient Thinking Given that o1-like models aim to 410 mimic human thought processes, the efficiency of their 411 reasoning is critical to their performance on challenging 412 problems. Just as human thinking can occasionally be inef-413 ficient, models may face similar issues. For instance, Chen 414 et al. (2024) studied the problem of overthinking in o1-like 415 LLMs, where models waste substantial computational re-416 sources revisiting trivial or self-evident paths, leading to 417 inefficiency. Conversely, our focus lies on the underex-418 plored problem of underthinking. Underthinking occurs 419 when a model fails to deeply explore promising paths, in-420 stead frequently switching strategies prematurely, resulting 421 in computational waste. This inefficiency becomes espe-422 cially pronounced when tackling difficult problems. This 423 phenomenon contrasts with overthinking, where excessive 424 computational effort is invested in simple problems with 425 diminishing returns. Underthinking refers to the model's 426 tendency to abandon promising lines of reasoning prema-427 turely on challenging problems, leading to incorrect answers. 428 We assert that truly intelligent systems must learn to adap-429 tively allocate their computational resources, concentrating 430 on paths that are both promising and challenging. 431

4.2. Manipulating Decoding Penalties

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The role of penalty mechanisms in Natural Language Processing (NLP) decoding has garnered significant attention.
Traditional decoding methods, such as greedy search and beam search, focus primarily on maximizing the likelihood of generated sequences without considering the broader

implications of the outputs. However, researchers have identified various shortcomings in these approaches, leading to the exploration of penalty mechanisms to enhance the quality of generated text.

Length normalization is a widely used strategy to adjust decoding penalties. Jean et al. (2015); Koehn & Knowles (2017); Tu et al. (2017); Murray & Chiang (2018) highlighted that length normalization and length penalties can prevent models from generating overly verbose or excessively brief translations, leading to improved fluency and adequacy. In addition, Tu et al. (2016) introduced coverage penalties in neural machine translation to mitigate the problems of "over-translation" and "under-translation" by integrating a coverage metric that penalizes repeated attention to tokens. Along this direction, Wu et al. (2016) proposed a coverage penalty in decoding to encourage the generation of an output that is most likely to cover all the words in the source sentence. See et al. (2017) incorporated the concept of coverage into the summarization task by modeling the coverage content in summarization outputs.

In this paper, we adjust decoding penalties to address the problem of underthinking. Our approach encourages the model to maintain its original line of reasoning and engage in deeper thought processes, avoiding frequent shifts in strategy and superficial reasoning patterns. To the best of our knowledge, we are the first to investigate the effectiveness of decoding penalties in mitigating the underthinking issue.

5. Conclusion

In this work, we investigated underthinking in o1-like LLMs, identifying it as a significant factor limiting their performance on challenging reasoning tasks. Through comprehensive analysis, we observed that these models frequently abandon promising reasoning paths prematurely, leading to inefficient problem-solving and lower accuracy. We introduced a novel metric to quantify underthinking by assessing token efficiency in incorrect responses. To mitigate this issue, we proposed a decoding strategy with thought switching penalty (TIP), which encourages models to thoroughly explore each reasoning thought before considering alternatives. Our empirical results demonstrate that TIP effectively reduces underthinking and enhances accuracy across difficult mathematical and scientific problem sets without necessitating additional model training.

This work contributes to a deeper understanding of reasoning processes in o1-like LLMs and provides a practical approach to align their problem-solving capabilities to human-like deep thinking. Future directions include exploring adaptive mechanisms within models to self-regulate thought transitions and further improving reasoning efficiency in o1-like LLMs.

440 Impact Statement

The paper reveals the underthinking issue in o1-like models. Our findings call for the community to research on models' efficient thinking capabilities, which could significantly influence future developments in this field. We see no harmful impacts of this work.

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