MSM: MULTI-SCALE MAMBA IN MULTI-TASK DENSE PREDICTION

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Abstract

High-quality visual representations are crucial for success in multi-task dense prediction. The Mamba architecture, initially designed for natural language processing, has garnered interest for its potential in computer vision due to its efficient modeling of long-range dependencies. However, when applied to multi-task dense prediction, it reveals inherent limitations. Unlike text processing with diverse tokenization strategies, image token partitioning requires careful consideration of multiple options. In multi-task dense prediction, each task may require specific levels of granularity in scene structure. Unfortunately, the current Mamba implementation, which segments images into fixed patch scales, fails to match these requirements, leading to sub-optimal performance. This paper proposes a simple yet effective Multi-Scale Mamba (MSM) for multi-task dense prediction. Firstly, we employ a novel Multi-Scale Scanning (MS-Scan) to establish global feature relationships at various scales. This module enhances the model's capability to deliver a comprehensive visual representation by integrating information across scales. Secondly, we adaptively merge task-shared information from multiple scales across different task branches. This design not only meets the diverse granularity demands of various tasks but also facilitates more nuanced cross-task feature interactions. Extensive experiments on two challenging benchmarks, *i.e.*, NYUD-V2 and PASCAL-Context, show the superiority of our MSM vs its stateof-the-art competitors.

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1 INTRODUCTION

Multi-task dense prediction is a critical visual task designed to simultaneously predict outputs for
various pixel-level tasks, such as semantic segmentation, depth prediction, surface normal estimation, and saliency detection. In the context of deep learning, the quality of image representation is
paramount (Vandenhende et al., 2021; Crawshaw, 2020). The representation is enriched not only by
extracting rich features from the input images (Xu et al., 2018; Zhang et al., 2023) but also by the
synergistic interactions and complementarities among features from various tasks (Ye & Xu, 2022;
Sinodinos & Armanfard, 2024). These dynamic cross-task feature interactions significantly enhance
the robustness and effectiveness of the task representations in accurately capturing a wide array of
visual attributes.

Initially, methodologies for multi-task dense prediction predominantly employed Convolutional 042 Neural Networks (CNNs). These networks (Xu et al., 2018; Gao et al., 2019; Sun et al., 2021) 043 were meticulously designed with distinct branches for each task, complemented by modules that 044 facilitated cross-task information interactions, aiming to fortify the robustness of the representations. Nonetheless, the inherently limited receptive fields of CNN architectures frequently led to 046 suboptimal performance. In response to these challenges, transformer-style networks (Ye & Xu, 047 2022; Xu et al., 2023) demonstrate exceptional proficiency in modeling long-range dependencies. 048 This capability substantially improves the representational effectiveness of models in handling the complexities of multi-task scenarios. the computational complexity of attention mechanisms, which increases quadratically with the resolution, presents a substantial challenge for multi-task dense pre-051 diction. To mitigate this limitation, researchers (Bhattacharjee et al., 2022; 2023; Jiang et al., 2024) have adopted the Swin Transformer (Liu et al., 2021) as the foundational framework for imple-052 menting window-based attention to reduce computational demands. However, when implementing task feature refinement in the decoder, this strategy greatly limits the scope of cross-task interaction,



Figure 1: Comparison of task attention with (w/ MS) and without MS-Scan (w/o MS). Our approach demonstrates superior alignment between scene structural relationships and task-specific requirements across all tasks.

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contradicting the original objective of task interaction, which is to extract as much valuable information as possible. Therefore, how to enhance global modeling capability while maintaining reduced computational cost remains an unresolved issue.

Recently, with linear complexity in long-range dependency modeling, Mamba (Gu & Dao, 2024; 071 Dao & Gu, 2024) has excelled in natural language processing and demonstrated the potential in 072 visual tasks (Liu et al., 2024; Ma et al., 2024). Inspired by these, MTmamba (Lin et al., 2024) 073 replaced window-based attention with the Mamba module in decoder stage, thereby enhancing rep-074 resentation quality, which combines Self-Task Mamba (STM) block and Cross-Task Mamba (CTM) 075 block to facilitate cross-task information exchange and model long-range dependencies. However, 076 they overlooked the gap between the fixed tokenization in Mamba processing and the requirement 077 for representation diversity in multi-task dense prediction. Specifically, Mamba processes features 078 by converting them into sequences of tokens, which is more complex for images than text. Unlike 079 text, where multiple tokenization strategies are viable, image tokenization (patches) requires careful consideration of diverse options. And this is crucial in multi-task dense prediction, due to each task may have varying requirements of granularity in scene representation. Unfortunately, the current 081 implementation of MTMamba, which segments images into fixed patches, will propagate shared information at the same granularity, consequently resulting in sub-optimal performance. 083

084 To address these challenges, we propose a simple yet effective Multi-Scale Mamba (MSM) method. 085 MSM is an extension of the existing MTMamba (Lin et al., 2024) approach with a task-aware hierarchical scene modeling function, which improves the adaptability of individual task representations, as shown in Figure 1. Specifically, we introduce a novel Multi-Scale Scanning (MS-Scan) to de-087 liver a comprehensive visual representation. Based on the MS-Scan mechanism, we developed the 880 Task-Specific Multi-Scale Mamba (TS-MSM) module and the Cross-Task Multi-Scale Mamba (CT-089 MSM) module. In the TS-MSM module, features are initially partitioned into multiple spaces, 090 where the scene structure of images is modeled at various scales. Subsequently, specific tasks inte-091 grate multi-scale scene structural information to enhance task-specific representations as required. 092 Within the CT-MSM module, we first consolidate all task representations and extract hierarchical task-shared scene structural information. Following that, different task branches adaptively merge 094 task-shared representations from multiple scales to accommodate the varying demands of different tasks for image structural granularity.

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- We propose MSM for multi-task dense prediction, featuring a novel MS-Scan at its core to
- alleviate the difficulty of feature learning in multi-task dense scene prediction.

The main contributions of this study are summarized as follows:

- We design a TS-MSM module and a CT-MSM module. these modules enhance the model's capability to deliver a comprehensive visual representation and meet the diverse granularity demands of tasks.
- Extensive experiments on two multi-task dense prediction benchmarks (i.e. PASCAL Context and NYUD-v2) verify the effectiveness of the proposed method, which demonstrates superior performance compared with the previous state-of-the-art methods.

108 2 RELATED WORK

110 Multi-Task Learning. Most existing multi-task learning works have primarily focused on opti-111 mizing training processes and designing network structures. The optimization approaches can be 112 categorized into gradient manipulation (Yu et al., 2020; Navon et al., 2022; Jeong & Yoon, 2024; 113 Ye et al., 2024) and loss-balancing (Chen et al., 2018; Kendall et al., 2018) to coordinate resource allocation for various tasks during training. The approaches of structural design endeavor to enhance 114 task representation learning by devising various mechanisms. Some CNN-based methods manually 115 design interaction mechanisms to extract useful information across tasks. For example, using in-116 termediate auxiliary tasks (Xu et al., 2018) or designing distillation methods (Vandenhende et al., 117 2020) to fuse encoder features from multiple stages. With the advancement of Transformer, current 118 methods have gained improved global task interaction capabilities to enhance task representation 119 efficiency. Certain approaches (Bhattacharjee et al., 2022; Shoouri et al., 2023) employ pairwise in-120 teractions through the selection of a reference task, whereas others (Ye & Xu, 2022; Xu et al., 2023; 121 Ye & Xu, 2023; Li et al., 2024) facilitate global interactions across all tasks. To mitigate computa-122 tional complexity, MTMamba (Lin et al., 2024) introduced Mamba (Gu & Dao, 2024) to multi-task 123 learning, which showcases effective long sequence modeling capabilities and achieving satisfactory 124 performance. However, it overlooked the different requirements of scene structure granularity for 125 various tasks in cross-task interaction.

126 State Space Models. In efficient long-range dependency modeling methods, state space models (Gu 127 et al., 2021b; Smith et al., 2022) has become a striking alternative to Transformers. (Gu et al., 2021a) 128 proposed a Structured State Space Sequence (S4) model based on a new parameterization, which al-129 leviates the computational and memory efficiency issues faced by SSM. Subsequently, numerous 130 efforts (Fu et al., 2023; Mehta et al., 2022) are dedicated to bridging the performance disparity 131 between SSMs and Transformers. For example, H3 (Fu et al., 2023) proposed a new SSM layer to bridge the gap between performance and computational efficiency. Mamba (Gu & Dao, 2024) 132 introduced an input-based parameterization method and hardware-aware algorithm, achieving per-133 formance on par with Transformers in natural language processing. This success has spurred various 134 endeavors (Zhu et al., 2024) towards Mamba's adaptation for visual tasks. 135

136 The preservation of comprehensive image structural information poses a critical challenge in Mamba's sequential processing model, which has attracted considerable attention and effort (Zhu 137 et al., 2024; Liu et al., 2024; Yang et al., 2024; Huang et al., 2024; Zhao et al., 2024). Vision 138 Mamba (Zhu et al., 2024) introduces a novel bidirectional Mamba block (Vim) that annotates im-139 age sequences by embedding positional information, employing a bidirectional state space model to 140 compress visual representations. Additionally, VMamba (Liu et al., 2024) proposes the 2D Selec-141 tive Scan (SS2D), a four-way scanning mechanism tailored for spatial domain traversal, aimed at 142 enhancing Mamba's image modeling capabilities. Subsequent research studies have explored vari-143 ous scan patterns and combinations tailored to different tasks or scenarios (Yang et al., 2024; Huang 144 et al., 2024; Zhao et al., 2024). However, by utilizing fixed token sizes, these methods overlook the 145 importance of hierarchical spatial structural information in visual tasks. 146

¹⁴⁷ 3 MAIN METHOD

We first outline the overall architecture of Multi-Scale Mamba for multi-task dense prediction in Section 3.1, then delve into the Multi-Scale Mamba Decoder and Multi-Scale Scan in Section 3.2 and 3.3 respectively, followed by a discussion of the optimization objectives in Section 3.4.

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3.1 PINELINE OF MULTI-TASK DENSE PREDICTION

Similar to previous approaches (Bhattacharjee et al., 2022; Zhang et al., 2023; Lin et al., 2024), our MSM for multi-task dense prediction consists of two main components: a task-shared encoder Φ for extracting task-generic representations and a decoder Θ for refining features and generating predictions for individual tasks, as illustrated in Figure 2(a). This can be formulated as:

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$$\hat{\mathbf{Y}} = \{ \hat{\mathbf{Y}}_1, \hat{\mathbf{Y}}_2, \dots, \hat{\mathbf{Y}}_T \} = \Theta \circ \Phi(I), \tag{1}$$

where $I \in \mathbb{R}^{H \times W \times 3}$ denotes the RGB input, $\hat{\mathbf{Y}}_t$ represents the prediction for task t with the same height H and width W as I, and T denotes the total number of tasks. The decoder is the key 162 Pretrained Encoder F_i^s F^si RGB 163 2× ×2 $\times 18$ CT-MSM 164 Swin Swin Swin Linear Ψ block block block Merge G Merge G_i^s \mathcal{F}_{h}^{s} Swin 166 MS-Scan MS-Scan $\frac{H}{16} \times \frac{W}{16}$ W 4 $\frac{W}{8}$ И $8C \times \frac{1}{32}$ block 167 Ō Linear MS-Mamba Decode ċ. Conv Predictions G^2 G^1 G³ G 169 Linear Linear MFR MFR MFR TS-MSM TS-MSM 170 block3 block. block Ċ Ć LN 171 G4--F \mathcal{F}_{in}^{s} 172 $(\mathbf{\psi})$ Down Sampling $(\mathbf{\Lambda})$ Patch Expand (\mathbf{C}) Concatenation $(\mathbf{\sigma})$ SiLU 173 (a) MSM for MTL (b) MFR (c) TS-MSM 174

Figure 2: Framework of the proposed MSM for multi-task dense prediction. (a) overall of MSM,
illustrating with depth estimation and surface normal estimation tasks. (b) Details of the MFR block,
which include T task-specific TS-MSM blocks and a task-shared CT-MSM block. (c) Details of TS-MSM, the core component MS-Scan is illustrated in Figure 3.

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component of our method and will be described in detail in the following section. Here, we first introduce the encoder.

The encoder shares similarities with other methods (Lin et al., 2024). We utilized a pretrained Swin Transformer (Liu et al., 2021) to extract task-generic features, which begins by dividing the input image $I \in \mathbb{R}^{H \times W \times 3}$ into $H/w \times W/w$ tokens of dimension *C* through patch partitioning and linear layers, where *w* denotes the partition size. These tokens are then processed through multiple stages involving alternating patch merging and Swin Transformer block processing, ultimately yielding hierarchical image representations:

$$\mathbf{G} = \{\mathbf{G}^1, \mathbf{G}^2, \mathbf{G}^3, \mathbf{G}^4\} = \Phi(I), \quad \mathbf{G}^i \in \mathbb{R}^{C_i \times H_i \times W_i}, \tag{2}$$

where **G** represents the task-generic features extracted from the encoder Φ . In our practical implementation, we utilize a partition size of 4, resulting in the following shapes for **G**: $C \times \frac{H}{4} \times \frac{W}{4}, 2C \times \frac{H}{8} \times \frac{W}{8}, 4C \times \frac{H}{16} \times \frac{W}{16}$ and $8C \times \frac{H}{32} \times \frac{W}{32}$, respectively.

3.2 MULTI-SCALE MAMBA DECODER

As the core of the proposed MSM Model, the Multi-Scale Mamba Decoder consists of three Multi-Scale Mamba Feature Refinement (MFR) blocks and T task heads, as depicted in Figure 2(a). This architecture refines the task-generic features **G** obtained from the encoder into task-specific features **F**, which are crucial for generating task predictions $\hat{\mathbf{Y}}$. The task-specific features are represented as $\mathbf{F} = {\mathbf{F}_t}_{t=1}^T$, where each \mathbf{F}_t is defined as follows:

$$\mathbf{F}_{t} = \{\mathbf{F}_{t}^{1}, \mathbf{F}_{t}^{2}, \mathbf{F}_{t}^{3}\}, t \in \{1, 2, \dots, T\},\tag{3}$$

where \mathbf{F}_t comprises three representations that correspond to the first three encoder stages, with dimensions of $4C \times \frac{H}{16} \times \frac{W}{16}$, $2C \times \frac{H}{8} \times \frac{W}{8}$, and $C \times \frac{H}{4} \times \frac{W}{4}$, respectively. Finally, the last refined features $\{\mathbf{F}_t^3\}_{t=1}^T$ are input into the task heads to produce the final predictions $\{\hat{\mathbf{Y}}_t\}_{t=1}^T$.

The proposed MFR block in the decoder is designed to bridge the gap between task-generic and 208 task-specific representations, as illustrated in Figure 2(b). To meet the varying demands for scene 209 structure granularity across different tasks, especially during task interactions, we introduce two 210 specialized multi-scale Mamba modules: TS-MSM and CT-MSM. For the s-th MFR block, the 211 input is derived from two sources: (1) task-generic features \mathbf{G}^{4-s} from the corresponding encoder 212 stage, and (2) $\bar{\mathbf{F}}^{s-1}$, which is obtained by expanding the fine-tuned features $\mathbf{F}^{s-1} = {\mathbf{F}_t^{s-1}}_{t=1}^T$ 213 from the preceding MFR block. For the first MFR block, G^4 is replicated T times, substituting 214 for \mathbf{F}^{s-1} as input for each task. During MFR processing, task-generic features \mathbf{G}^{4-s} are initially 215 concatenated with the expanded task-specific features $\bar{\mathbf{F}}_{t}^{s-1}$ within each task branch. This combined 216 input then undergoes processing through the TS-MSM and CT-MSM modules to yield the refined 217 features \mathbf{F}^{s} . For clarity, we will utilize a superscript s to denote processing in the s-th MFR block 218 in the subsequent sections.

219 Taks-Specific Mluti-Scale Mamba Block. The TS-MSM primarily aims to construct comprehen-220 sive representations through task-internal interactions. Its architecture is illustrated in Figure 2(c)221 and comprises two main branches: the scan branch and the gating branch. In the scan branch, 222 we integrate local information using convolutional layers and activation functions, followed by the 223 implementation of a novel Multi-Scale Scan mechanism (MS-Scan) to derive a hierarchical global 224 scene structure representation \mathcal{F}_{h}^{s} . Simultaneously, in the gating branch, we generate a gating signal 225 \mathcal{G}^s using an activation function to regulate the flow of information within the scan branch. Sub-226 sequently, we adjust the channel dimensions of the multi-scale scene representation by applying a linear projection \mathcal{P} and establish a residual connection between \mathcal{F}_h^s and the input \mathcal{F}_{in}^s . This process 227 is repeated twice to produce the final output \mathcal{F}^s : 228

$$\mathcal{F}^{s} = \mathcal{F}^{s}_{in} + \mathcal{P}(\mathcal{F}^{s}_{h} \times \mathcal{G}^{s}). \tag{4}$$

231 **Cross-Task Mluti-Scale Mamba Block.** The CT-MSM is designed to address the varying demands 232 for scene granularity across tasks during task interactions. As illustrated in the upper portion of 233 Figure 2(b), it begins by concatenating features $\{\mathcal{F}_t^s\}_{t=1}^T$ from different task branches to construct multi-scale task-shared features \mathcal{F}_{ms}^s using the Multi-Scale Scan (MS-Scan) mechanism. Subsequently, each task branch adaptively merges \mathcal{F}_{ms}^s using the Merge operation to obtain finely-tuned 234 235 task representations $\mathbf{F}^s = {\{\mathbf{F}_t^s\}}_{t=1}^T$: 236

$$\mathbf{F}_{t}^{s} = \operatorname{Merge}_{t} \circ \Psi \circ \mathcal{P}([\mathcal{F}_{1}^{s}, \mathcal{F}_{2}^{s}, \dots, \mathcal{F}_{T}^{s}]), t \in \{1, 2, \dots, T\},$$
(5)

238 where $[\cdot, \cdot]$ denotes channel-wise concatenation, \mathcal{P} represents a linear projection, Ψ is the MS-Scan 239 block (which will be elaborated in the following Section 3.3), and Merge_t is the feature fusion 240 method in MTMamba (Lin et al., 2024) for task t, where \mathcal{F}_t^s is first processed through convolution, 241 SS2D (Liu et al., 2024) and sigmoid function to generate the selection value \mathcal{G}_t^s . The final fused 242 feature is obtained by weighting \mathcal{F}_{ms}^s and \mathcal{G}_t^s on \mathcal{G}_t^s , the detail is described in Appendix A.1. 243

Task Head. After obtaining the final refined task representations \mathbf{F}^{S} from the last MFR block, each task employs a task-specific head to produce the final output. We incorporate an expansion layer 245 alongside a linear projection: 246

$$\hat{\mathbf{Y}}_t = \mathcal{P} \circ \operatorname{Expand}(F_t^S), t \in \{1, 2, \dots, T\},\tag{6}$$

where Expand denotes a module designed to double the feature resolution H and W, consisting of 249 a linear projection followed by a reshape operation. The operator \mathcal{P} represents a linear layer that 250 projects the feature channels to the required number of channels specific to each task.

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3.3 MULTI-SCALE SCAN

254 Mamba processes features by converting them into sequences of tokens. While a variety of to-255 kenization strategies exist for text, image tokenization requires careful consideration of multiple 256 approaches. Previous research has demonstrated that multi-scale processing is particularly effective 257 for image data. To leverage this advantage, we propose a multi-scale scan mechanism that serves as a cornerstone of MSM model, as illustrated in Figure 3. In this framework, we employ multiple scanning scales, denoted as $\{s_i\}_{i=1}^N$, in multiple branches $\{\mathcal{B}_i\}_{i=1}^N$, and transform the input image 258 259 feature $x \in \mathbb{R}^{C \times H \times W}$ into token sequences of varying dimensions for Mamba modeling. For in-260 stance, the initial image feature can be tokenized into a sequence with a total length of $H \times W$, 261 where each token has a dimension of C, represented as $C \times (H \times W)$. When applying a scanning 262 scale of $s_i = 2$, the image is divided into non-overlapping patches, resulting in a tokenized feature sequence with a dimensionality of $4C \times (\frac{H}{2} \times \frac{W}{2})$. Specifically, MS-Scan comprises three key components: input handling, multi-scale scanning, and multi-scale fusion. 264 265

Input Handling. To construct inputs for N different scanning branches $\mathcal{B} = \{\mathcal{B}_i\}_{i=1}^N$, we perform two main operations. (1) Channel Split (S): We begin by splitting the input representation x into N sub-features $\{x_i\}_{i=1}^N \in \mathbb{R}^{m \times H \times W}$ along the channel dimension, where m = C/N. (2) Window 266 267 268 Tokenization (\mathcal{W}_i) : For the *i*-th branch \mathcal{B}_i with scan scale s_i , we first divide x_i into $\frac{H}{s_i} \times \frac{W}{s_i}$ non-overlapping patches, each of size $m \times s_i \times s_i$. Subsequently, we concatenate the pixel feature 269



Figure 3: Left: Instructions for MS-Scan. It consists of three distinct operations, Input Handling, Multi-Scale Scanning, and Multi-Scale Fusion. Right: Illustration of Window Tokenization (W_i) and Token Windowing (W_i^{-1}) with a scan scale of 2.

values in each patch along the channel dimension, resulting in the scan input \bar{x}_i with a shape of $(m \times s_i \times s_i) \times \frac{H}{s_i} \times \frac{W}{s_i}$. Ultimately, we obtain the input for all branches:

$$\{\bar{x}_1, \bar{x}_2, \dots, \bar{x}_N\} = \{\mathcal{W}_1, \mathcal{W}_2, \dots, \mathcal{W}_N\} \circ \mathcal{S}(x).$$

$$\tag{7}$$

Multi-Scale Scanning. Following the input handling process, we employ distinct scanning scales to construct a multi-scale scene representation in each branch. For all branches \mathcal{B} , we utilize the four-way scanning method (SS2D) from VMamba (Liu et al., 2024) to generate scene features at the specified scale. This method creates four token sequences, each shaped as $C_i \times (H_i \times W_i)$, by scanning the input features $\bar{x}_i \in \mathbb{R}^{C_i \times H_i \times W_i}$ in four directions. The resulting sequences are then processed by SSM (Gu & Dao, 2024) and combined to produce the output feature $\bar{y} = \{\bar{y}_i\}_{i=1}^N$:

$$\bar{y}_i = \mathrm{SS2D}(\bar{x}_i) \in \mathbb{R}^{C_i \times H_i \times W_i}.$$
(8)

Multi-Scale Fusion. In our approach to multi-scale feature fusion, we adopt a methodology that reverses the input handling process, consisting of two key steps. (1) Token Windowing (\mathcal{W}_i^{-1}) : For each branch \mathcal{B}_i , we split each pixel feature into $s_i \times s_i$ segments along the channel dimension: $\{\bar{y}_{i,j}\}_{j=1}^{s_i \times s_i} \in \mathbb{R}^{m \times 1 \times 1}$ These segments are then concatenated along the spatial dimensions (height and width) to form patches, which are subsequently combined to produce the output for \mathcal{B}_i . (2) Channel Concatenation (\mathcal{S}^{-1}) : We concatenate the features from all branches along the channel dimension, yielding the final output feature $y \in \mathbb{R}^{C \times H \times W}$:

$$y = \mathcal{S}^{-1} \circ \{\mathcal{W}_1^{-1}, \mathcal{W}_2^{-1}, \dots, \mathcal{W}_n^{-1}\} (\bar{y}_1, \bar{y}_2, \dots, \bar{y}_n),$$
(9)

where S^{-1} and W_i^{-1} refer to the inverse operation of S and W_i respectively.

3.4 Optimization Objective

We jointly train all tasks to optimize muti-scale mamba decoder Θ and task-shared encoder Φ . To maintain consistency with previous approaches, we use L1 loss for depth estimation and surface normal estimation tasks and the cross-entropy loss for other tasks, therefore, the optimization objective can be expressed as follows:

$$L = \sum_{t_i \in \mathcal{T}} \lambda_t \mathcal{L}_t(\Theta \circ \Phi(I), \mathbf{Y}_t),$$
(10)

where \mathcal{T} is the set of all tasks, λ_t , \mathcal{L}_t and \mathbf{Y}_t are the loss weight, loss function, and task label for image I in task t respectively.

4 EXPERIMENTS

321 4.1 EXPERIMENTAL SETUP

Datasets. We performed experiments using the benchmark datasets NYUDv2 (Silberman et al., 2012) and PASCAL Context (Chen et al., 2014). NYUDv2 primarily focuses on indoor scenes,



Figure 4: (a) Preference for task-share features in MFR blocks. (b) Preference for different scan scales in the final MFR block.

with 795 and 654 RGB images for training and testing purposes. Tasks in NYUDv2 include 40 class semantic segmentation, monocular depth estimation, surface normal estimation, and object
 boundary detection. PASCAL Context encompasses indoor and outdoor scenes, offering pixel level labels for tasks like semantic segmentation, human parsing, object boundary detection, surface
 normal estimation, and saliency detection tasks. This dataset contains 4,998 training images and
 5,105 test images.

Implementation Details. We employ a pretrained Swin-Large Transformer (Liu et al., 2021) on 345 ImageNet-22K (Deng et al., 2009) as our encoder. Our models are trained on the NYUD-v2 dataset 346 for 50,000 iterations with a batch size of 4, and on the Pascal Context dataset for 75,000 iterations 347 with a batch size of 6. Across all datasets, we use the Adam optimizer with a learning rate of 348 5×10^{-5} and a weight decay rate of 1×10^{-5} , alongside a polynomial learning rate scheduler. 349 The preliminary decoder has an output channel number of 768. We follow common practice (Ye & 350 Xu, 2022; Lin et al., 2024) in resizing the input images and applying data augmentation techniques. 351 Specifically, we resize the input images of NYUDv2 and PASCAL-Context to 448×576 and $512 \times$ 352 512, respectively, and apply random color jittering, random cropping, random scaling, and random 353 horizontal flipping. 354

Evaluation Metrics. Mean Intersection over Union (mIoU) is employed for semantic and human parsing tasks. Root Mean Square Error (RMSE) and mean angle error (mErr) are used for depth and surface normal estimation tasks respectively. Saliency detection tasks utilize maximal F-measure (maxF), and object boundary detection tasks use optimal-dataset-scale F-measure (odsF). We also use the multi-task gain Δ_{MTL} (Vandenhende et al., 2021) evaluate the overall task performance.

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4.2 EXPERIMENTAL RESULTS

362 Statistical Analysis of Task Preferences. We analyzed the task preferences for the multi-scale 363 task-share feature across different decoding stages. Specifically, we conducted statistics in three 364 MFRblocks in the decoder, which were set to scan scales of $\{1,2\}, \{1,2,4\}, \{1,2,4,6\}, re$ spectively. In Figure 4 (a), we calculated the mean of the task-share feature selection value $\bar{\mathcal{G}}_t$ in 366 CT-MSM across all scan scales in the module and averaged the results over all test images. The 367 results indicate that as the network depth increases, the specialization of features for each task is 368 enhanced, thereby reducing the demand for task-share representation. In Figure 4 (b), we compared the selection value \mathcal{G}_t^3 across four scan scales at the last MFR block. There are significant differ-369 ences among tasks within the same cross-task interaction stage. These results indicate that meeting 370 the requirements of different tasks for scene structure granularity is crucial in the interaction process. 371

Comparison with State-of-the-art Methods. Table 1 and Table 2 report a comparison of the proposed MSM against previous state-of-the-art methods, including MTmamba (Lin et al., 2024), MQ-Transformer (Xu et al., 2023), InvPT (Ye & Xu, 2022), ATRC (Brüggemann et al., 2021), MTI-Net (Vandenhende et al., 2020), PAD-Net (Xu et al., 2018), PSD (Zhang et al., 2019), PAP (Zhou et al., 2020), Cross-Stitch (Misra et al., 2016) and ASTMT (Maninis et al., 2019) on NYUD-V2 and PASCAL-Context dataset respectively. Notably, the previous best method, *i.e.*, MTmamba, and our MSM are built upon the Transformer-encoder Mamba-decoder architecture with the same back-

Table 1:	Quantitative con	nparison of differ-
ent metho	ds on NYUD-v2	dataset

Table 2: Quantitative comparison of different methods on Pascal-Context dataset.

Model	Semseg mIoU ↑	Depth RMSE↓	Normal mErr↓	Boundary odsF ↑	Model	Semseg mIoU ↑	Parsing mIoU ↑	Saliency maxF↑	Normal mErr↓	Boundary odsF ↑
	CN	N based					CNN ba	sed		
Cross-Stitch	36.34	0.6290	20.88	76.38	PAD-Net	53.60	59.60	65.80	15.30	72.50
PAP	36.72	0.6178	20.82	76.42	ASTMT	68.00	61.10	65.70	14.70	72.40
PSD	36.69	0.6246	20.87	76.42	MTI-Net	61.70	60.18	84.78	14.23	70.80
PAD-Net	36.61	0.6270	20.85	76.38	ATRC	62.69	59.42	84.70	14.20	70.96
MTI-Net	45.94	0.5365	20.27	77.86	ATRC-ASPP	63.60	60.23	83.91	14.30	70.86
ATRC	46.33	0.5363	20.18	77.94	ATRC-BMTAS	67.67	62.93	82.29	14.24	72.42
	Transfo	ormer base	ed		Transformer based					
InvPT	53.66	0.5183	19.04	78.10	InvPT	79.03	67.61	84.81	14.15	73.00
MQTransformer	54.84	0.5325	19.67	78.20	MQTransformer	78.93	67.41	83.58	14.21	73.90
Mamba based							Mamba b	ased		
MTMamba	55.82	0.5066	18.63	78.70	MTmamba	81.11	72.62	84.14	14.14	78.80
Ours	57.79	0.4832	18.63	79.00	Ours	81.38	72.87	84.41	14.13	78.83

bone. On NYUD-v2, the performance of Semseg is clearly boosted from the previous best, *i.e.*, 55.82 to 57.79 (**+1.97**). on Pascal-Context, we achieved superior performance on all tasks compared to MTMamba.

Effectiveness of TS-MSM and CT-MSM. We performed ablation experiments on TS-MSM and CT-MSM using the NYUD-V2 dataset. These experiments all used Swin-Large Transformer as encoder. The term "single-task" indicates that each task possesses its task-specific model, utilizing two particular Swin Transformer blocks in each stage of the decoder, "baseline" denotes MT-Mamba, "TS-MSM only" denotes only equipped baseline with TS-MSM, "CT-MSM only" denotes only equipped baseline with CT-MSM, and "ST-MSM+CT-MSM" is the default method of MSM. The results presented in Table 3 highlight the essential role of satisfying the diverse demands for scene structural granularity in task interaction. Furthermore, the application of MS-scan during task-internal feature refinement in TS-MSM has been shown to significantly improve performance, showcasing the advantages of the MSM design.

Table 3: Effectiveness of ST-MSM and CT-MSM on NYUDv2 dataset.

Model	Semseg mIoU ↑	Depth RMSE↓	Normal mErr↓	$\begin{array}{c} \textbf{Boundary} \\ odsF \uparrow \end{array}$	$\begin{vmatrix} \mathbf{MTL} \ \mathbf{Gain} \\ \Delta_m \uparrow \end{vmatrix}$
STL Model	54.32	0.5166	19.21	77.30	+0.00
Baseline	55.82	0.5066	18.63	78.70	+2.38
TS-MSM only	56.89	0.4840	18.68	78.80	+3.93
CT-MSM only	57.13	0.4822	18.67	78.80	+4.14
ST-MSM+CT-MSM	57.79	0.4832	18.63	79.00	+4.51

Ablation Study on Scan Scales. We experimented with the impact of varying scan scales on model performance, as shown in Figure 5. Experiments were conducted on NYUDv2 dataset with Swin-Large Transformer as encoder. We experimented with three different settings, Type 1: all MFRs use {1,2} two scan scales; Type 2: three MFRs utilize {1,2}, {1,4}, {1,6} respectively; Type 3: all MFRs use {1,4} two scan scales. The results showed that in multi-scale scanning, all scale divisions achieved better performance than single scale, *i.e.*, MTMamba (mark with dashed lines in Figure 5). Ultimately, we adopt the 1,4 scale setting for all MFRs as the final configuration for MSM.

Ablation Study on Scan Numbers. We conduct ablation experiments on the impact of varying scan numbers, as shown in Table 4. We compared four different settings: (1) all three MFRs use {1} scan scale; (2) three MFRs use {1,2}, {1,4}, and {1,6} respectively; (3) all MFRs use {1,2,4}; (4) three MFRs use {1,2}, {1,2,4} and {1,2,4,6} respectively. The results showed that employing appropriate scan scale partitions can effectively enhance overall performance. Significantly, all variations in scan quantity settings yielded notable performance enhancements.

58.0 57.5 57.0 56.5 56.0 55.5



Figure 5: Performance comparison of different scan scale settings in MSM.

Table 4: Different scan numbers.						Table 5	5: Diffe	erent e	ncoder	s.
Scan Scale MFR 1 MFR 2	MFR 3 Sei	mseg Depth oU↑ RMSE↓	Normal mErr↓	Boundary odsF↑	$\begin{array}{c} \operatorname{MTL}\operatorname{Gain}\\ \Delta_m \uparrow \end{array}$	Model	Semseg mIoU ↑	Depth RMSE↓	Normal mErr↓	$\begin{array}{c} \textbf{Boundary} \\ odsF \uparrow \end{array}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	5.820.50665.630.48785.930.4850 7.790.4832	18.63 18.83 18.52 18.63	78.70 78.70 78.90 79.00	+2.38 +3.40 +4.15 +4.51	MTMamba-Base MSM-Base MTMamba-Large MSM-Large	53.62 54.64 55.82 57.79	0.5126 0.5038 0.5066 0.4832	19.28 19.03 18.63 18.63	77.70 78.10 78.70 79.00

Performance on Different Encoder. We evaluate the effect of model size on experimental performance, presented in Table 5. All experiments were conducted on the NYUDv2 dataset. We compare our method with the previous best-performing model, MTMamba, using two different encoders: Swin-Base Transformer (denoted as '-Base') and Swin-Large Transformer (denoted as '-Large'). The results suggest that models with greater capacities typically exhibit superior performance. Furthermore, our approach has demonstrated superior performance across all encoder variants.

Qualitative Visualization. We qualitatively compared our proposed MSM with the previous bestperforming method, as shown in Figure 6. Our method shows clear improvements in detail, as highlighted in the circled regions. For more visual comparisons, please refer to Appendix A.3.



Figure 6: Qualitative comparison with the best performing method on NYUD-v2. Our method generates better multi-task prediction details.

5 CONCLUSION

We proposed a Multi-Scale Mamba (MSM) framework for addressing the diverse preferences of
 scene structure granularity for different tasks in multi-task dense prediction. We introduce a multi scale scanning mechanism (MS-Scan) that comprehensively constructs scene structure information
 at various scales. Additionally, we build two multi-scale Mamba modules (TS-MSM and CT-MSM)
 that meet the diverse needs of task representation construction, thereby alleviating the difficulty of
 feature learning in multi-task dense scene prediction. Both qualitative and quantitative results show
 that our method significantly enhances performance.

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648 A APPENDIX

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A.1 FEATURE MERGE DETAILS OF CT-MSM

In CT-MSM, we have adapted the feature fu-652 sion approach from MTMamba (Lin et al., 653 2024) to merge multi-scale task-share features 654 \mathcal{F}_{ms}^{s} and task-specific features \mathcal{F}_{t}^{s} , as illus-655 trated in the figure 7. The core is to generate se-656 lection values $\{\mathcal{G}_t^s\}_{t=1}^T$ for weighting the task-657 shared \mathcal{F}_{ms}^{s} and task-specific features $\{\mathcal{F}_{t}^{s}\}_{t=1}^{T}$ 658 to obtain the fused task features $\{F_t^s\}_{t=1}^T$ for all 659 tasks. In implementation, before weighting the 660 task-specific features, they undergo further re-661 finement through convolution and SS2D (Liu 662 et al., 2024) operations. 663

$$\mathcal{F}_{t,LN}^s = \mathrm{LN}(\mathcal{F}_t^s),\tag{11}$$

ł

$$\mathcal{G}_t^s = \text{Sigmoid} \circ \mathcal{P}(\mathcal{F}_{t,LN}^s), \qquad (12)$$



Figure 7: Merge Details of CT-MSM.

$$\hat{\mathcal{F}}_{t}^{s} = \mathrm{LN} \circ \mathrm{SS2D} \circ \mathrm{SiLU} \circ \mathrm{Conv} \circ \mathcal{P}(\mathcal{F}_{t,LN}^{s}), \tag{13}$$

$$F_t^s = \mathcal{G}_t^s \times \mathcal{F}_{ms}^s + (1 - \mathcal{G}_t^s) \times \hat{\mathcal{F}}_t^s, \tag{14}$$

where LN denotes the Layer Normalization, \mathcal{P} represents a linear projection, Sigmoid and SiLU are the sigmoid function and SiLu function respectively, Conv(·) is the convolution layer.

676 A.2 LIGHTWEIGHT MSM

678 MSM framework introduces minimal additional computational cost (+0.01 GFLOPs) compared to 679 the original MTMamba, yet achieves significant performance improvements. To further validate the effectiveness of our method, we present Dilated Multi-Scale Mamba (DMSM), a lightweight version 680 of MSM, which achieves superior performance with reduced computational complexity compared 681 to MTMamba. DMSM conducts sparse scanning within each scan branch \mathcal{B} . Specifically, as shown 682 in Figure 8, we perform dilated sampling in generating multi-scale sequences from image features 683 instead of using all tokens. When restoring sequences to image features, we perform linear in-684 terpolation. These operations do not introduce any parameters and exhibit a reduced computational 685 burden due to sampling a subset of tokens for modeling. Experimental results, as depicted in Table 6, 686 demonstrate the effectiveness of meeting the diverse requirements of tasks for scene granularity in 687 multi-task dense prediction. Among them, $FLOPs^m$ denotes the complexity of SSM operations, 688 **FLOPs**^o is the complexity of other operations, and **FLOPs** = **FLOPs**^m + **FLOPs**^o the total com-689 plexity. All experiments utilize Swin-Large Transformer as encoder.



Figure 8: Comparision of MSM and DMSM.

		-							
Model	Semseg mIoU↑	Depth RMSE↓	Normal mErr↓	$\begin{array}{c} \textbf{Boundary} \\ odsF \uparrow \end{array}$	$\begin{array}{c c} \mathbf{MTL} \ \mathbf{Gain} \\ \Delta_m \uparrow \end{array}$	$ \begin{array}{c} \textbf{FLOPs}^m \\ \textbf{(G)} \downarrow \end{array} $	$\begin{array}{c} \textbf{FLOPs}^{o} \\ \textbf{(G)} \downarrow \end{array}$	FLOPs (G)↓	# Params (M)↓
STL Model	54.32	0.5166	19.21	77.30	+0.00	-	-	1074.79	888.77
MTMamba	55.82	0.5066	18.63	78.70	+2.38	81.72	459.09	540.81	307.99
DMSM (Ours)	56.95	0.4813	18.64	78.90	+4.18	60.50	450.57	511.07	307.99
MSM (Ours)	57.79	0.4832	18.63	79.00	+4.51	81.72	459.10	540.82	396.54

Table 6: Performance Comparison of Dilated Multi-Scale Mamba (DMSM) and MTMamba.

A.3 MORE VISUAL COMPARISON RESULTS

Task Attention. To compare task attention against the state-of-the-art method, we visualize the re-sults in Figure 11. Our method demonstrates a more precise attention range across all tasks, aligning with the intrinsic requirements of specific tasks. Specifically, it accurately captures task-specific ob-ject relationships, thereby improving overall performance and scene understanding. These findings suggest that the incorporation of multi-scale scanning in MSM addresses the varying demands for scene structural granularity across distinct tasks, thereby mitigating the difficulties in feature learn-ing within multi-task dense prediction and improving the alignment of task-specific features with the intrinsic requirements of each task.



Figure 9: More task attention comparison on NYUD-v2 dataset.

Qualitative Comparison. We present more qualitative results compared with the SOTA methods, MTMamba (Lin et al., 2024). In Figure 11 - Figure 13, we can see that our method generates better multi-task prediction details, highlighted in the circled regions.

	RGB	Semseg	Depth	Normal	Boundary
MTMamba			F		
Ours			P		
GT				-	

Figure 10: More Qualitative comparison on NYUD-v2 dataset.



Figure 11: More Qualitative comparison on NYUD-v2 dataset.



Figure 12: More Qualitative comparison on Pascal-Context dataset.



Figure 13: More Qualitative comparison on Pascal-Context dataset.