# SEEKING FLAT MINIMA WITH MEAN TEACHER ON SEMI- AND WEAKLY-SUPERVISED DOMAIN GENER ALIZATION FOR OBJECT DETECTION

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#### ABSTRACT

Object detectors do not work well when domains largely differ between training and testing data. To overcome this domain gap in object detection without requiring expensive annotations, we consider two problem settings: semi-supervised domain generalizable object detection (SS-DGOD) and weakly-supervised DGOD (WS-DGOD). In contrast to the conventional domain generalization for object detection that requires labeled data from multiple domains, SS-DGOD and WS-DGOD require labeled data only from one domain and unlabeled or weaklylabeled data from multiple domains for training. In this paper, we show that object detectors can be effectively trained on the two settings with the same Mean Teacher learning framework, where a student network is trained with pseudolabels output from a teacher on the unlabeled or weakly-labeled data. We provide novel interpretations of why the Mean Teacher learning framework works well on the two settings in terms of the relationships between the generalization gap and flat minima in parameter space. On the basis of the interpretations, we also show that incorporating a simple regularization method into the Mean Teacher learning framework leads to flatter minima. The experimental results demonstrate that the regularization leads to flatter minima and boosts the performance of the detectors trained with the Mean Teacher learning framework on the two settings.

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#### 1 INTRODUCTION

Object detection has been attracting much attention because it has practically useful applications such as in autonomous driving. Object detectors have performed tremendously well on commonly used benchmark datasets for object detection, such as MSCOCO (Lin et al., 2014) and PASCAL VOC (Everingham et al., 2010). However, such performance significantly drops when they are deployed on unseen domains, i.e., when the training and testing domains are different. For example, Inoue et al. (Inoue et al., 2018) reported a performance drop caused by the difference in image styles, and Li et al. (Li et al., 2022) showed one caused by the weather and time difference in the images captured with car-mounted cameras.

To solve this problem, many researchers have been exploring unsupervised domain adaptive object detection (UDA-OD) (Deng et al., 2021; Li et al., 2022; Chen et al., 2022). On UDA-OD, we train object detectors using source domain data with ground-truth labels (bounding boxes and class labels) and unlabeled target domain data to adapt the detectors to the target domain. However, in the real world, target domain data cannot always be accessed in the training phase.

Domain generalizable object detection (DGOD) is another common problem setting for solving the problem of the performance drop caused by the domain gaps (Lin et al., 2021; Zhang et al., 2022a). On DGOD, we train object detectors using labeled data from multiple domains so that the detectors work well on unseen domains. However, it is labor-intensive to collect these data for object detection because both bounding boxes and class labels for all objects in the images must be annotated. Although single-DGOD (Wu & Deng, 2022; Fan et al., 2023; Vidit et al., 2023; Wang et al., 2021b; 2023a; Lee et al., 2024), on which we train object detectors to generalize unseen domains using labeled data from one single domain, has been investigated, the performance gain is still limited.

054	In this paper, we tackle two tasks as more realistic settings: i) semi-supervised DGOD (SS-
055	DGOD) (Malakouti & Kovashka, 2023) and ii) weakly-supervised DGOD (WS-DGOD). The goal
056	of SS-DGOD is to generalize object detectors to unseen domains using labeled data only from one
057	single domain and unlabeled data from multiple domains. Note that the target domain data are not
058	included in the training data. On WS-DGOD, we use weakly labeled data from multiple domains
059	instead of the unlabeled data in SS-DGOD. "Weakly labeled" means that we have only image-level
060	labels that show the existence of each class in each training image and do not have bounding box
061	annotations. To the best of our knowledge, this is the first attempt to tackle WS-DGOD. We show
062	that object detectors can be effectively trained on the two settings with the same Mean Teacher
063	learning framework, where a student network is trained with pseudo-labels output from a teacher on
064	the unlabeled or weakly labeled data, and the teacher network is updated as the exponential moving $(EMA)$ of the student
065	average (EMIA) of the student.
066	Not only do we experimentally demonstrate the good performance of the Mean Teacher learning
067	framework, but also provide novel interpretations of why the Mean Teacher learning framework
068	works well on these two settings in terms of the relationship between generalization ability and
069	flat minima in parameter space. These interpretations are based on our findings that the two key
070	components of the Mean Teacher learning framework, i) EMA update and ii) learning from pseudo-
071	labels, lead to flat minima during the training. In the research area of domain generalization, it has
072	been shown both theoretically and empirically that neural networks with flatter minima in parameter space have better generalization ability to unscen domains (Foret et al. 2021; Chaudheri et al. 2017;
073	Cha et al. 2021: Izmailov et al. 2018: Caldarola et al. 2022: Wang et al. 2023b: Kaddour et al.
074	2022: Thang et al. 2023)
075	2022, Zhung et un, 2023).
076	On the basis of the interpretations, we also show that incorporating a simple regularization method
077	into the Mean Teacher learning framework leads to flatter minima. Specifically, because the teacher
078	and the student nave similar loss values around the flat minima, we introduce an additional loss term so that the output from the student network becomes similar to that from the teacher network
079	The experimental results demonstrate that the detectors trained with the Mean Teacher learning
080	framework perform well for unseen test domains on the two settings. We show that the simple yet
081	effective regularization leads to flatter minima and boosts the performance of those detectors.
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083	It is noteworthy that our aim is not to propose an entirely new method or surpass the state-of-the-art
084	methods. Instead, our contributions are summarized as follows:
085	• We show that object detectors can be effectively trained on the SS-DGOD and WS-DGOD
086	settings with the same Mean Teacher learning framework.
087	• We provide interpretations of why the detectors trained with the Mean teacher learning
088	framework achieve robustness to unseen test domains in terms of the flatness of minima in
089	parameter space, based on our novel finding that the Mean Teacher leads to flat minima.
090	• On the basis of the interpretations, we introduce a simple regularization method into the

- Mean Teacher learning framework to achieve flatter minima.
  - We are the first to tackle the WS-DGOD setting.

## 2 PROBLEM SETTINGS

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We formally describe the two problem settings of SS-DGOD and WS-DGOD. Their goal is to obtain object detectors that perform well on unseen target domain data  $\mathcal{D}_t = \{X_t\}$ , where  $X_t$  is a set of images from the target domain.

On SS-DGOD, we have labeled data from a source domain  $\mathcal{D}_{s_1} = \{(X_{s_1}, B_{s_1}, C_{s_1})\}$  and unlabeled data from multiple source domains  $\mathcal{D}_{s_i} = \{X_{s_i}\}_{i=2}^{N_D}$  in the training phase. Here,  $X_{s_1} = \{x_{s_1}^j\}_{j=1}^{N_{s_1}}$ is a set of  $N_{s_1}$  images from domain  $s_1$ .  $B_{s_1} = \{b_{s_1}^j\}_{j=1}^{N_{s_1}}$  and  $C_{s_1} = \{c_{s_1}^j\}_{j=1}^{N_{s_1}}$  are the corresponding bounding boxes and object-class labels, respectively.  $s_i$  is the *i*-th source domain, and  $N_{\mathcal{D}}$  is the number of the source domains. We assume that the data distributions differ between the domains, i.e.,  $P(X_{s_1}) \neq P(X_{s_2}) \neq \cdots P(X_{s_{N_D}}) \neq P(X_t)$ .

106 107 On WS-DGOD, we use labeled data from a source domain  $\mathcal{D}_{s_1} = \{(X_{s_1}, B_{s_1}, C_{s_1})\}$  and weakly 108 labeled data from multiple domains  $\mathcal{D}_{s_i} = \{(X_{s_i}, C_{s_i})\}_{i=2}^{N_D}$  for training. 108 Table 1 compares SS-DGOD and WS-DGOD with related problem settings 110 (Single-DGOD, DGOD, and UDA-OD). 111 As discussed in Sec. 1, DGOD requires 112 labeled data from multiple domains  $\mathcal{D}_{s_i} = \{(X_{s_i}, B_{s_i}, C_{s_i})\}_{i=1}^{N_D}$ , but those data 113 are sometimes hard to prepare due to the 114 high annotation cost. In contrast, SS-DGOD 115 (or WS-DGOD) requires labeled data from 116 one domain  $\mathcal{D}_{s_1} = \{(X_{s_1}, B_{s_1}, C_{s_1})\}$  and unlabeled data  $\mathcal{D}_{s_i} = \{X_{s_i}\}_{i=2}^{N_D}$  (or weakly labeled data  $\mathcal{D}_{s_i} = \{(X_{s_i}, C_{s_i})\}_{i=2}^{N_D}$ ), which 117 118 119 are easier to obtain. Therefore, SS-DGOD 120 and WS-DGOD are more practical settings 121 than DGOD. By using those data, we aim 122 to better generalize object detectors to the 123 unseen target domain data  $\mathcal{D}_t = \{X_t\}$  than 124 on Single-DGOD. Although another type of 125 SS-DGOD, where a portion of the samples 126 are labeled in each source domain, can also 127 be defined, we will leave it as part of our 128 future work (see Appendix D.1).

Table 1: Formal comparisons of SS-DGOD, WS-
DGOD, and related problem settings. DGOD stands
for domain generalizable object detection, and SS-
DGOD and WS-DGOD are semi-supervised DGOD
and weakly-supervised DGOD, respectively. UDA-
OD is unsupervised domain adaptive object detec-
tion.

task	train data	test data
Single-DGOD	$\mathcal{D}_{s_1} = \{(X_{s_1}, B_{s_1}, C_{s_1})\}$	$\mathcal{D}_t = \{X_t\}$
SS-DGOD	$\mathcal{D}_{s_1} = \{ (X_{s_1}, B_{s_1}, C_{s_1}) \}, \\ \mathcal{D}_{s_i} = \{ X_{s_i} \}_{i=2}^{N_D}$	$\mathcal{D}_t = \{X_t\}$
WS-DGOD	$ \begin{aligned} \mathcal{D}_{s_1} &= \{(X_{s_1}, B_{s_1}, C_{s_1})\}, \\ \mathcal{D}_{s_i} &= \{(X_{s_i}, C_{s_i})\}_{i=2}^{N_D} \end{aligned} $	$\mathcal{D}_t = \{X_t\}$
DGOD	$\mathcal{D}_{s_{i}} = \{(X_{s_{i}}, B_{s_{i}}, C_{s_{i}})\}_{i=1}^{N_{D}}$	$\mathcal{D}_t = \{X_t\}$
UDA-OD	$\mathcal{D}_{s_1} = \{ (X_{s_1}, B_{s_1}, C_{s_1}) \}, \\ \mathcal{D}_t = \{ X_t \}$	$\mathcal{D}_t = \{X_t\}$
WSDA-OD		$\mathcal{D}_t = \{X_t\}$

Another related setting is weakly-supervised domain adaptive object detection (WSDA-OD), a.k.a., cross-domain weakly-supervised object detection (Inoue et al., 2018; Hou et al., 2021; Xu et al., 2022; Tang et al., 2023), which requires weakly-labeled target data  $\mathcal{D}_t = \{(X_t, C_t)\}$  for training. Unlike on UDA-OD and WSDA-OD, we can train the detectors even when the unlabeled or weaklylabeled target domain data ( $\mathcal{D}_t = \{X_t\}$  or  $\mathcal{D}_t = \{(X_t, C_t)\}$ ) are not accessible.

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## 3 RELATED WORK

## 3.1 DOMAIN GENERALIZATION FOR IMAGE CLASSIFICATION

139 Many methods have been proposed for domain generalization on image classification tasks as sum-140 marized in recent survey papers (Zhou et al., 2022; Wang et al., 2022a). Among a variety of domain 141 generalization methods, finding flat minima is one of the most common approaches (Foret et al., 142 2021; Chaudhari et al., 2017; Cha et al., 2021; Izmailov et al., 2018; Caldarola et al., 2022; Wang 143 et al., 2023b; Kaddour et al., 2022; Zhang et al., 2023). Those studies empirically and theoreti-144 cally showed that finding flat minima in parameter space results in a better generalization ability. Izmailov et al. (2018) and Cha et al. (2021) demonstrated that empirical risk minimization (ERM) 145 with stochastic gradient descent (SGD) converges to the vicinity of a flat minimum, and averaging 146 the parameter weights over a certain number of training steps/epochs results in reaching the flat 147 minimum. Inspired by these findings, we reveal that the Mean Teacher learning framework leads to 148 flat minima, and thus can obtain good generalization ability. 149

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## 3.2 Domain Generalization for Object Detection

152 Domain generalization for object detection has not been widely explored, compared with image 153 classification. Lin et al. (2021) proposed a method for disentangling domain-specific and domain-154 invariant features by adversarial learning on both image-level and instance-level features for DGOD. 155 Liu et al. (2020) investigated DGOD in underwater object detection and proposed DG-YOLO. For 156 Single-DGOD, Wang et al. (2021b) proposed a self-training method that uses the temporal consis-157 tency of objects in videos. Wu & Deng (2022) proposed a method for disentangling domain-invariant 158 features by contrastive learning and self-distillation. Fan et al. (2023) proposed perturbing the chan-159 nel statistics of feature maps, which can be interpreted as data augmentation of image styles to a variety of domains. Wang et al. (2023a) proposed a disentangle method on frequency space for ob-160 ject detection from unmanned aerial vehicles. Vidit et al. (2023) proposed an augmentation method 161 using a pre-trained vision-language model (CLIP) with textual prompts.

Unlike the above methods, as discussed in Sects. 1 and 2, we tackle SS-DGOD (Semi-Supervised Domain Generalization for Object Detection) and a new problem setting called WS-DGOD (Weakly-Supervised Domain Generalization for Object Detection). The most closely related to our work is Malakouti & Kovashka (2023)'s work. They tackled SS-DGOD and proposed a language-guided alignment method. However, the limitation of their method is that it requires a backbone network that was pre-trained on vision-and-language tasks. Our experiments show that the object detectors trained with the Mean Teacher learning framework and our regularization outperform their method when the same backbone is used.

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- 3.3 SEMI-SUPERVISED DOMAIN GENERALIZATION

There are a few methods that use both labeled and unlabeled data for domain generalization (SSDG)
on image classification (Zhang et al., 2022b; Zhou et al., 2023b; Lin et al., 2024). Zhang et al.
(2022b) proposed an unsupervised pre-training method called DARLING, which performs contrastive learning on unlabeled images to obtain domain-irrelevant feature representation. Zhou et al.
(2023b) extended a semi-supervised learning method called FixMatch (Sohn et al., 2020) to SSDG.

In contrast to those studies, we tackle SSDG for object detection. We also tackle the "weakly labeled" setting (i.e., WS-DGOD), which has not been explored even for image classification.

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- 3.4 MEAN TEACHER LEARNING FRAMEWORK

183 Mean Teacher learning framework was originally proposed for semi-supervised image classification (Tarvainen & Valpola, 2017). Several studies have investigated the use of the Mean Teacher 185 learning framework for a variety of tasks such as domain generalization on image classification (Yang et al., 2021), (in-domain) weakly-supervised object detection (Wang et al., 2022b), (indomain) semi-supervised object detection (Mi et al., 2022), UDA-OD (Deng et al., 2021; Li et al., 187 2022; He et al., 2022; Deng et al., 2023; Kennerley et al., 2024), and UDA for semantic segmen-188 taion (Araslanov & Roth, 2021; Wang et al., 2021a; Hoyer et al., 2022; Zhang et al., 2021). Lee et al. 189 (2023) provided a theoretical analysis of the Mean Teacher learning framework on masked image 190 modeling pretext tasks for semi-supervised image classification. We show that the Mean Teacher 191 learning framework also works well on different settings (SS-DGOD and WS-DGOD), provide their 192 interpretations, and introduce a simple regularization method to lead to flatter minima. 193

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## 4 TRAINING METHOD

4.1 OVERVIEW AND KEY IDEA

199 On both SS-DGOD and WS-DGOD, our goal is to obtain ob-200 ject detectors that work well on the unseen target domain data 201  $\mathcal{D}_t = \{X_t\}$ . Gulrajani & Lopez-Paz (2021) reported that if carefully implemented, empirical risk minimization (i.e., the 202 image classifier simply trained with supervised learning on 203 multiple domains) outperformed state-of-the-art domain gen-204 eralization methods on several benchmark datasets for image 205 classification. Following this important finding, we expect 206 similar behavior on object detection and aim to train an object 207 detector on multiple domains  $\mathcal{D}_{s_i}$   $(i = 1, \dots, N_D)$ . However, 208 we have no ground-truth labels (or have only weak labels) for 209  $\mathcal{D}_{s_i}(i=2,\cdots,N_D)$  although ground-truth labels are avail-210 able for  $\mathcal{D}_{s_1}$ . Therefore, the question is how to train a detector 211 on those domains. Our solution is to use the Mean Teacher 212 learning framework for object detection (Li et al., 2022; Chen



Figure 1: Training framework.

et al., 2022) shown in Fig. 1, where we have two networks (teacher and student) with the same structure and train the student network using the pseudo-labels generated by the teacher network. Note that this Mean Teacher learning framework can be applied to any object detector, but we hereafter describe the loss functions of FasterRCNN (Ren et al., 2015) as an example for ease of explanation.

# 216 4.2 PRE-TRAINING 217

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218 If we start the Mean Teacher learning from randomly initialized parameters, the teacher network 219 cannot output reliable pseudo labels. Therefore, we first perform supervised learning with the la-220 beled data of one source domain  $\mathcal{D}_{s_1} = \{(X_{s_1}, B_{s_1}, C_{s_1})\}.$ 

$$\mathcal{L}_{s_{1}}^{\text{sup}}(\theta) = \mathcal{L}_{\text{RPN}}^{\text{cis}}(\theta, X_{s_{1}}, B_{s_{1}}, C_{s_{1}}) + \mathcal{L}_{\text{RPN}}^{\text{reg}}(\theta, X_{s_{1}}, B_{s_{1}}, C_{s_{1}}) \\
+ \mathcal{L}_{\text{RoI}}^{\text{cls}}(\theta, X_{s_{1}}, B_{s_{1}}, C_{s_{1}}) + \mathcal{L}_{\text{RoI}}^{\text{reg}}(\theta, X_{s_{1}}, B_{s_{1}}, C_{s_{1}}),$$
(1)

where  $\mathcal{L}_{\text{RPN}}^{\text{cls}}$  and  $\mathcal{L}_{\text{RPN}}^{\text{reg}}$  are the classification and regression losses for region proposal networks (RPN), respectively.  $\mathcal{L}_{\text{RoI}}^{\text{cls}}$  and  $\mathcal{L}_{\text{RoI}}^{\text{reg}}$  are those for RoIhead. We initialize both the teacher and student networks with the parameters  $\theta^* = \arg \min_{\theta} \mathcal{L}_{s_1}^{\sup}(\theta)$  obtained from this pre-training.

#### 4.3 MEAN TEACHER LEARNING

#### 4.3.1 GENERATE PSEUDO-LABELS

Because we have no ground-truth labels (or have only weak labels) for the other source domains  $\mathcal{D}_{s_i}(i=2,\cdots,N_D)$ , we generate pseudo labels using the teacher network. Specifically, we perform weak data augmentation to the unlabeled (or weakly-labeled) image  $x_{s_i}^j$  and input it into the teacher network. We denote the output from the teacher as  $\{(\hat{b}_{s_i}^{jr}, \hat{p}_{s_i}^{jr})\}_{r=1}^{N_R}$ , where  $\hat{b}_{s_i}^{jr}$  and  $\hat{p}_{s_i}^{jr}$  are the predicted bounding box and class probabilities for the *r*-th region of interests (RoI) in the *j*-th image, respectively, and  $N_R$  is the number of output RoIs.

In the case of SS-DGOD, we simply perform post-processing  $f_{post}$  to  $(\hat{b}_{s_i}^{jr}, \hat{p}_{s_i}^{jr})$  and obtain the pseudo label  $(\bar{b}_{s_i}^{jr}, \bar{c}_{s_i}^{jr}) = f_{post}(\hat{b}_{s_i}^{jr}, \hat{p}_{s_i}^{jr})$ . Post-processing  $f_{post}$  indicates a simple thresholding function if we use "hard" pseudo labels like (Li et al., 2022) and indicates a sharpening function if we use "soft" pseudo labels like (Chen et al., 2022).

In the case of WS-DGOD, we perform the refinement process of applying the weak labels to the predicted class probabilities  $\hat{p}_{s_i}^{jr}$  immediately before post-processing  $f_{post}$  to obtain more accurate pseudo labels as follows:

$$(\bar{b}_{s_i}^{jr}, \bar{c}_{s_i}^{jr}) = f_{\text{post}}(\hat{b}_{s_i}^{jr}, \hat{p}_{s_i}^{jr}), \quad \hat{p}_{s_i}^{jr}(k) = \begin{cases} \hat{p}_{s_i}^{jr}(k) & \text{if } k \in c_{s_i}^j \\ 0 & \text{otherwise} \end{cases}$$
(2)

where  $\hat{p}_{s_i}^{jr}(k)$  is the predicted class probability for the k-th class. Using the weak label  $c_{s_i}^j$ , Eq. (2) makes the predicted probability zero at each RoI if the k-th class does not exist in the j-th image.

#### 4.3.2 UPDATE STUDENT

Now we have the pseudo labels  $\bar{B}_{s_i} = {\{\bar{b}_{s_i}^j\}}_{j=1}^{N_{s_i}}$  and  $\bar{C}_{s_i} = {\{\bar{c}_{s_i}^j\}}_{j=1}^{N_{s_i}}$  and train the student network with them.

We perform strong data augmentations to the image  $x_{s_i}^j$  and input it into the student network. In domain  $s_1$ , because the ground-truth labels are available, we update the student by backpropagating loss  $\mathcal{L}_{s_1}^{sup}$  in Eq. (1). In the other domains  $s_i(i = 2, \dots, N_D)$ , we calculate loss  $\mathcal{L}_{s_i}^{unsup}$  using the pseudo labels and backpropagate it to update the student. In summary, we update the parameters of student  $\theta^{student}$  with loss  $\mathcal{L}^{student}$  as follows:

$$\theta^{\text{student}} \leftarrow \theta^{\text{student}} - \nabla_{\theta} \mathcal{L}^{\text{student}}(\theta), \quad \mathcal{L}^{\text{student}}(\theta) = \mathcal{L}_{s_1}^{\text{sup}}(\theta) + \sum_{i=2}^{N_D} \mathcal{L}_{s_i}^{\text{unsup}}(\theta)$$
(3)

$$\mathcal{L}_{s_{i}}^{\mathrm{unsup}}(\theta) = \mathcal{L}_{\mathrm{RPN}}^{\mathrm{cls}}(\theta, X_{s_{i}}, \bar{B}_{s_{i}}, \bar{C}_{s_{i}}) + \mathcal{L}_{\mathrm{RPN}}^{\mathrm{reg}}(\theta, X_{s_{i}}, \bar{B}_{s_{i}}, \bar{C}_{s_{i}}) + \mathcal{L}_{\mathrm{RoI}}^{\mathrm{cls}}(\theta, X_{s_{i}}, \bar{B}_{s_{i}}, \bar{C}_{s_{i}}) + \mathcal{L}_{\mathrm{RoI}}^{\mathrm{reg}}(\theta, X_{s_{i}}, \bar{B}_{s_{i}}, \bar{C}_{s_{i}}).$$
(4)

# 265 4.3.3 UPDATE TEACHER

Similar to previous studies (Chen et al., 2022; Li et al., 2022), we do not update the parameters of the teacher  $\theta^{\text{teacher}}$  by backpropagation to obtain stable pseudo labels. Instead, we update them by the exponential moving average (EMA) of the parameters of the student network  $\theta^{\text{teacher}} \leftarrow \alpha \theta^{\text{teacher}} + (1 - \alpha) \theta^{\text{student}}$ . Here,  $\alpha$  is a hyperparameter to control the update speed.

# 5 WHY DOES MEAN TEACHER BECOME ROBUST TO UNSEEN DOMAINS?

We provide novel interpretations of why the Mean Teacher
learning framework works well on SS-DGOD and WS-DGOD
settings in terms of the relationship between generalization
ability and flat minima in parameter space. We show that the
two key components of the Mean Teacher learning framework,
EMA update and ii) learning from pseudo labels, lead to flat
minima during the training.



Figure 2: Empirical and robust risks.

5.1 DEFINITION

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We define an empirical risk as  $\mathcal{E}_{ER}(\theta) := \sum_{i=1}^{N_D} \mathcal{L}_{s_i}^{sup}(\theta)$  when we assume that ground-truth labels are available on all the training domains. A risk at the target domain is defined as

 $\mathcal{E}_t(\theta) := \mathcal{L}_t^{sup}(\theta)$ . The goal is to minimize the test risk  $\mathcal{E}_t(\theta)$  by only solving the empirical risk minimization (ERM), i.e.,  $\min_{\theta} \mathcal{E}_{ER}(\theta)$ . Hereafter, we use the terms *risk* and *loss* interchangeably.

#### 287 288 5.2 PRELIMINARY KNOWLEDGE

289 Previous studies for domain generalization demonstrated both theoretically and empirically that 290 neural networks with flatter minima in parameter space exhibit superior generalization ability to 291 unseen domains (Foret et al., 2021; Chaudhari et al., 2017; Cha et al., 2021; Izmailov et al., 2018; Caldarola et al., 2022; Wang et al., 2023b; Kaddour et al., 2022; Zhang et al., 2023). Cha et al. 292 (2021) theoretically revealed the relationship between the flat minima and generalization gap (i.e., 293 performance drop by domain shift). We briefly describe the theorem for the subsequent explanation. We consider the worst-case loss within neighbor regions in parameter space, which is defined as a 295 robust risk  $\mathcal{E}_{RR}^{\gamma}(\theta) := \max_{\|\Delta\| \leq \gamma} \mathcal{E}_{ER}(\theta + \Delta)$ . Here,  $\gamma$  is the radius of the neighbor region. As 296 shown in Fig. 2, when  $\gamma$  is sufficiently large, sharp minima of the empirical risk are not minima of 297 the robust risk. In contrast, the minima of the robust risk (i.e.,  $\arg \min_{\theta} \mathcal{E}_{RR}^{\gamma}(\theta)$ ) are also minima 298 in the flat regions of the empirical risk. The following theorem shows the relationship between the 299 optimal solution of robust risk minimization (RRM): 300

**Theorem** (from (Cha et al., 2021)). Consider a set of N covers  $\{\Theta_k\}_{k=1}^N$  such that the parameter space  $\Theta \subset \bigcup_k^N \Theta_k$  where diam $(\Theta) := \sup_{\theta, \theta' \in \Theta} \|\theta - \theta'\|_2$ ,  $N := \lceil (\operatorname{diam}(\Theta)/\gamma)^d \rceil$  and d is dimension of  $\Theta$ . Let  $\theta^{\gamma}$  denote the optimal solution of the RRM, i.e.,  $\theta^{\gamma} := \arg \min_{\theta} \mathcal{E}_{RR}^{\gamma}(\theta)$ , and let  $v_k$  and v be VC dimensions of each  $\Theta_k$  and  $\Theta$ , respectively. Then, the gap between the optimal test loss,  $\min_{\theta'} \mathcal{E}_t(\theta')$ , and the test loss of  $\theta^{\gamma}$ ,  $\mathcal{E}_t(\theta^{\gamma})$ , has the following bound with probability of at least  $1 - \delta$ .

$$\mathcal{E}_{t}(\theta^{\gamma}) - \min_{\theta'} \mathcal{E}_{t}(\theta') \leq \mathcal{E}_{RR}^{\gamma}(\theta^{\gamma}) - \min_{\theta''} \mathcal{E}_{ER}(\theta'') + \frac{1}{N_{D}} \sum_{i=1}^{N_{D}} \operatorname{Div}(s_{i}, t) + \max_{k \in [1, N]} \sqrt{\frac{v_{k} \ln(m/v_{k}) + \ln(2N/\delta)}{m}} + \sqrt{\frac{v \ln(m/v) + \ln(2/\delta)}{m}},$$
(5)

where m is the number of training samples and  $\text{Div}(s_i, t) := 2 \sup_A |\mathbb{P}_{s_i}(A) - \mathbb{P}_t(A)|$  is a divergence between two distributions.

For its proof, see (Cha et al., 2021). From the theorem, we can interpret that the gap between the RRM and ERM (i.e.,  $\mathcal{E}_{RR}^{\gamma}(\theta^{\gamma}) - \min_{\theta''} \mathcal{E}_{ER}(\theta'')$ ) upper bounds the generalization gap in the test domain (i.e.,  $\mathcal{E}_t(\theta^{\gamma}) - \min_{\theta'} \mathcal{E}_t(\theta')$ ). Intuitively, as shown in Fig 2, the gap between the RRM and ERM narrows at flat regions of ERM. Therefore, we can interpret that lowering the gap leads to flat minima of ERM and results in better generalization performance on the target domain.

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- 5.3 EMA UPDATE
- 323 We explain why the EMA update in the Mean Teacher learning framework leads to flat minima. Stephan et al. (2017) showed that optimizing with constant SGD (i.e., SGD with a fixed learning rate)

324 converges to a Gaussian distribution centered on the optimum. On the basis of this finding, Izmailov 325 et al. (2018) and Cha et al. (2021) showed that the ERM with SGD converges to the marginal of a 326 flat minimum, and averaging the weights of the parameters over some training steps/epochs leads 327 to the flat minima. To avoid overfitting, Izmailov et al. (2018) and Cha et al. (2021) proposed 328 sophisticated algorithms called SWA and SWAD for averaging the weights, and Arpit et al. (2022) introduced a carefully designed averaging strategy called SMA. In contrast to them, we found that a simple EMA also leads to flat minima, even without using those averaging algorithms. This finding 330 has not been provided in previous works, although the theoretical explanations for the benefit of 331 averaging weights have already been provided. The experiments presented in Sec. 7 show that the 332 teacher network with only the EMA update of the student (i.e., without pseudo labeling) as shown 333 in Eqs. (6-7) can reach flatter minima and perform better than the student. 334

$$\mathcal{P}^{\text{student}} \leftarrow \theta^{\text{student}} - \nabla_{\theta} \mathcal{L}^{\text{student}}(\theta), \quad \mathcal{L}^{\text{student}}(\theta) = \mathcal{L}^{\text{sup}}_{s}(\theta)$$
(6)

$$\theta^{\text{teacher}} \leftarrow \alpha \theta^{\text{teacher}} + (1 - \alpha) \theta^{\text{student}},$$
(7)

#### 5.4 LEARNING FROM PSEUDO LABELS

340 We explain why learning from pseudo-labels in the Mean 341 Teacher learning framework leads to flat minima. Assuming 342 that the pseudo-labels from the teacher are accurate enough (i.e., similar enough to ground truth),  $\mathcal{L}_{s_i}^{unsup}$  in Eq. (3) can 343 be approximated by  $\mathcal{L}_{s_i}^{sup}$ , and we can regard the student net-344 work as the ERM in Sec. 5.1. On the other hand, as explained 345 in Sec. 5.3 and shown in the experiments, because the teacher 346 network updated with EMA has a better ability to reach flat 347 minima than the student, the teacher can obtain less robust risk 348 than the student, and we can regard the teacher as the robust 349 risk minimizer. Therefore, from Eq. (5), the smaller the differ-350 ence between the losses of the teacher and student, the smaller 351 the generalization gap in the target domain is. Fig. 3 shows its



Figure 3: Intuitive interpretation of difference between loss values of trajectory of student and their mean (teacher).

intuitive interpretations. At the flat region, the trajectory of the student over the training steps and
their mean (teacher) have similar loss values. In contrast, there is a large difference between the loss
values of the trajectory of the student and their mean at the sharp valley.

Next, we show that learning from pseudo-labels in the Mean Teacher learning framework makes the losses of the student and teacher similar. Because the student is trained with the output from the teacher as pseudo-ground truth, the training promotes the outputs from the student similar to those from the teacher. When we use monotonically increasing/decreasing functions with respect to the outputs as loss functions  $\mathcal{E}$  (e.g., cross-entropy loss  $\mathcal{E}(p) = p_{gt} \log(p)$ ), the more similar the outputs are, the more similar the loss values are, as shown below:

**Proposition.** Assume  $p_1 < p_2 < p_3 \in \mathbb{R}$ , and  $\mathcal{E}(p) : \mathbb{R} \to \mathbb{R}$  is a monotonically increasing/decreasing function of p. Then,  $|\mathcal{E}(p_3) - \mathcal{E}(p_2)| < |\mathcal{E}(p_3) - \mathcal{E}(p_1)|$  holds.

Let us consider  $p_3$  as the teacher's output, and  $p_2$  and  $p_1$  as the outputs of the student. Since  $p_2$  is closer to  $p_3$  than  $p_1$ , the loss of  $p_2$  becomes more similar to the loss of  $p_3$  than that of  $p_1$ . Therefore, we can interpret that learning from pseudo-labels align the outputs from the student to be similar to those from the teacher, thereby aligning the loss values, consequently leading to flat minima.

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#### 6 REGULARIZATION FOR FLATTER MINIMA

#### 6.1 Method

As discussed in Sec. 5, when the output from the student and teacher are similar, the networks tend to reach flat minima. To this end, we introduce a simple regularization method to make the two networks' outputs more similar by training the student using raw outputs from the teacher.

Fig. 4 shows an overview of the method. The concept is to apply regularization so that the outputs from the two networks are similar for the same input image. Specifically, we perform weak data augmentations to the unlabeled (or weakly labeled) image  $x_{s_i}^j$  and input the image into the teacher network. We then use the output from the teacher  $\{(\hat{b}_{s_i}^{jr}, \hat{p}_{s_i}^{jr})\}_{r=1}^{N_R}$  directly as pseudo-ground truth without post-processing  $f_{post}$ . To update the student, we input the same weakly augmented image  $x_{s_i}^{j}$  into the student and calculate the regularization loss  $\mathcal{L}^{\text{regul.}}$  as follows:

$$\mathcal{L}^{\text{student}}(\theta) = \mathcal{L}_{s_1}^{\text{sup}}(\theta) + \sum_{i=2}^{N_D} [\mathcal{L}_{s_i}^{\text{unsup}}(\theta) + \beta \mathcal{L}_{s_i}^{\text{regul.}}(\theta)]$$
(8)

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$$\mathcal{L}_{s_i}^{\text{regul.}}(\theta) = \mathcal{L}_{\text{RPN}}^{\text{cls}}(\theta, X_{s_i}, \hat{B}_{s_i}, \hat{C}_{s_i}) + \mathcal{L}_{\text{RPN}}^{\text{reg}}(\theta, X_{s_i}, \hat{B}_{s_i}, \hat{C}_{s_i}) + \mathcal{L}_{\text{RoI}}^{\text{cls}}(\theta, X_{s_i}, \hat{B}_{s_i}, \hat{C}_{s_i}) + \mathcal{L}_{\text{RoI}}^{\text{reg}}(\theta, X_{s_i}, \hat{B}_{s_i}, \hat{C}_{s_i}),$$

where  $\hat{B}_{s_i} = \{\hat{b}_{s_i}^j\}_{j=1}^{N_{s_i}}$  and  $\hat{C}_{s_i} = \{\hat{c}_{s_i}^j\}_{j=1}^{N_{s_i}}$  are the *raw pseudo-labels* from the teacher, and  $\beta$  is a hyperparameter to tune the strength of the regularization.

The differences between the regularization and the traditional Mean Teacher loss in Sec. 4.3 are 1) the use of weak augmentation instead of strong augmentation, and 2) the omission of post-processing (i.e., the sharpening function of (Chen et al., 2022) in our experiments). These approaches ensure that 1) the same input is given to both the student and teacher, and 2) the raw output from the teacher is used as pseudo-labels, which encourages closer alignment between the student and teacher.



(9)

#### 6.2 CONNECTION TO PRIOR ARTS



We can regard the regularization method as a type of knowledge distillation as the student is trained to mimic the raw output from the teacher. Although the technical details are dif-

ferent, it has been empirically shown that knowledge distillation methods are effective on related tasks such as Single-DGOD (Wu & Deng, 2022), domain adaptive semantic segmentation (Zhang et al., 2021), UDA-OD (Cao et al., 2023; Deng et al., 2023), and semi-supervised domain adaptive object detection (where a small part of labeled target data  $\mathcal{D}_t = \{(X_t, C_t)\}$  is accessible during the training (Zhou et al., 2023a)). We believe that our interpretation revealed one of the reasons knowledge-distillation methods lead to better generalization ability.

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## 7 EXPERIMENTS

412 7.1 DATASET DETAILS

We used the artistic style image dataset (Inoue et al., 2018), which has four domains: natural image, clipart, comic, and watercolor. The natural image domain has 16,551 images from PASCAL VOC07&12, and the other domains have 1,000, 2,000, and 2,000 images, respectively. There are six object classes (bike, bird, car, cat, dog, and person), and we removed the images that do not contain these classes.

We conducted the experiments on three patterns of domains. In the first pattern, we set the nat-419 ural image domain as the labeled domain  $s_1$  and set clipart and comic as the unlabeled domains 420  $s_2, s_3$ . We set watercolor as the target domain t. Concretely, we used the labeled trainval set of 421 PASCAL VOC 2007&2012, the unlabeled train set of clipart, and the unlabeled train set of comic 422 for training. We then used the test sets of clipart and comic for validation. For evaluation (test-423 ing), we used the test set of watercolor. In the second and third patterns, we set  $(s_1, s_2, s_3, t) =$ 424 (natural, watercolor, comic, clipart) and  $(s_1, s_2, s_3, t) =$  (natural, watercolor, clipart, comic), 425 respectively. The results on another dataset are shown in the supplementary material B. 426

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#### 7.2 IMPLEMENTATION DETAILS

We used soft pseudo labeling proposed in (Chen et al., 2022) for the Mean Teacher learning. We
used Gaussian FasterRCNN (Chen et al., 2022) as the object detector, in which the regression output
is modified to use the soft labels. We used cross-entropy loss for both classification and regression losses, similar to (Chen et al., 2022). We applied the same hyperparameters as in a previous

setting	method	backbone	mAP50           watercolor         clipart         comic           46.6         27.2         31.4           50.5         34.5         26.6           55.5         38.0         29.0           P)         46.1         39.1         38.3           41.3         26.0         28.8           56.6         39.8         30.1           58.2         43.3         32.2           59.7         44.2         39.9           62.9         46.2         40.2           62.6         47.1         45.2           62.2         48.2         48.6           54.9         43.4         27.0           58.8         45.4         32.7           55.2         -         -           53.3         -         -			
			watercolor	clipart	comic	
Single-DGOD	CLIP-based augmentation (Vidit et al., 2023)	Res101	46.6	27.2	31.4	
Single-DGOD	Gaussian FasterRCNN	Res101	50.5	34.5	26.6	
Single-DGOD	Gaussian FasterRCNN + EMA	Res101	55.5	38.0	29.0	
SS-DGOD	CDDMSL (Malakouti & Kovashka, 2023)	Res50 (RegionCLIP)	46.1	39.1	38.3	
SS-DGOD	CDDMSL (Malakouti & Kovashka, 2023)	Res101	41.3	26.0	28.8	
SS-DGOD	Gaussian FasterRCNN + EMA + PL	Res101	56.6	39.8	30.1	
SS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	Res101	58.2	43.3	32.2	
WS-DGOD	Gaussian FasterRCNN + EMA + PL	Res101	59.7	44.2	39.9	
WS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	Res101	62.9	46.2	40.2	
DGOD	Gaussian FasterRCNN	Res101	62.6	47.1	45.2	
Oracle	Gaussian FasterRCNN	Res101	62.2	48.2	48.6	
UDA-OD	Gaussian FasterRCNN + EMA + PL (Chen et al., 2022)	Res101	54.9	43.4	27.0	
UDA-OD	Gaussian FasterRCNN + EMA + PL + Regul.	Res101	58.8	45.4	32.7	
UDA-OD	SCL* (Shen et al., 2019)	Res101	55.2	-	-	
UDA-OD	SWDA* (Saito et al., 2019)	Res101	53.3	-	-	
UDA-OD	UMT* (Deng et al., 2021)	Res101	58.1	-	-	
UDA-OD	AT* (Li et al., 2022)	Res101	59.9	-	-	

Table 2: Comparisons of mAP50 on the artistic style image dataset (Inoue et al., 2018) when the target domain is watercolor. Values with \* are from previous study (Li et al., 2022).

study (Chen et al., 2022) except for the number of iterations. All training (including baseline models) was done with four A100 GPUs. The parameters of the backbone network were initialized with the ResNet101 pre-trained on ImageNet. The hyperparameters  $\alpha$  in Eq. (7) and  $\beta$  in Eq. (8) were set to 0.9996 and 0.5 throughout the experiments, respectively. During the inference (testing) phase, we used the teacher network. Other details are given in the supplementary material.

#### 7.3 BASELINE METHODS

As the baseline, we trained the detector *Gaussian FasterRCNN* on Single-DGOD setting (i.e., supervised learning on  $s_1$  in Eq. (1)). To show the effectiveness of the EMA update, we trained *Gaussian FasterRCNN* + *EMA* + *PL* is a detector trained with the Mean Teacher learning framework in Sec. 4. *Gaussian FasterRCNN* + *EMA* + *PL* + *Regul.* is a detector with the Mean Teacher learning framework and the regualization in Eqs. (8-9).

To confirm the upper-bound performance, we also trained Gaussian FasterRCNN on DGOD and Oracle settings. On DGOD, the detector was trained with supervised learning using the groundtruth labels on the domains  $s_1, s_2$ , and  $s_3$ . On Oracle, the detector was trained with supervised learning on  $s_1, s_2, s_3$ , and the target domain t.

Because there is only one existing method on SS-DGOD (i.e., CDDMSL (Malakouti & Kovashka, 2023)), we also compared the above detectors with state-of-the-art methods on related task settings such as Single-DGOD and UDA-OD. It is noteworthy that existing DGOD methods such as (Lin et al., 2021; Liu et al., 2020) cannot be applied to SS-DGOD and WS-DGOD because they require labeled data from multiple source domains for training. It is important to reiterate that our goal is not to propose a new method that outperforms state-of-the-art methods. Instead, our goal is to offer novel interpretations of the Mean Teacher and demonstrate that introducing simple regularization can lead to flatter minima, resulting in better robustness to unseen domains.

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#### 7.4 Comparisons with Other Methods

Table 2 shows the results on the artistic image style dataset. We evaluated with the mean average precision (mAP50) when the IoU threshold was 0.5. EMA increased the mAP of *Gaussian Faster-RCNN* from (50.5, 34.5, 26.6) to (55.5, 38.0, 29.0), and this was further boosted to (56.6, 39.8, 30.1) with pseudo labeling (PL). We observed additional improvement to (58.2, 43.3, 32.2) with the regularization. The regularization improved the performance not only on SS-DGOD but also on WS-DGOD. The detectors trained on WS-DGOD performed better than those on SS-DGOD because WS-DGOD can generate more accurate pseudo labels by the refinement in Eq. (2). Those results are comparable to those of the detectors trained on DGOD and Oracle.



Figure 5: Left and right plots compare average training and test flatness, respectively.

For fair comparisons, we trained CDDMSL with Res101 backbone pre-trained on ImageNet. However, its performance significantly degraded, as reported in a previous study (Malakouti & Kovashka, 2023), because it requires language-guided training, and initializing the model with RegionCLIP is crucial to achieve good performance.

The detectors trained on SS-DGOD and WS-DGOD also performed comparably to or better than
those on UDA-OD, although we did not use the target domain data during the training. Furthermore,
the regularization can be directly applied to UDA-OD as well as SS-DGOD and WS-DGOD, and
we also observed significant performance improvement by the regularization on UDA-OD.

#### 506 7.5 ANALYSIS OF FLATNESS

To evaluate the flatness of the detectors in parameter space, following previous studies (Izmailov et al., 2018) and (Cha et al., 2021), we computed the change in loss values when we perturb the parameters. Specifically, we sampled a random direction vector d on a unit sphere, perturbed the parameters ( $\theta' = \theta + d\gamma$ ) with a radius  $\gamma$ , and computed the average change over ten samples, i.e.,  $\mathcal{F}^{\gamma}(\theta) = \mathbb{E}_{\theta'} |\mathcal{E}(\theta') - \mathcal{E}(\theta)|$ . The lower the change is, the flatter the parameters.

Fig. 5 shows the  $\mathcal{F}^{\gamma}(\theta)$  of the training loss  $\mathcal{E}(\theta) = \sum_{i} \mathcal{L}_{s_{i}}^{sup}(\theta)$  and the test loss  $\mathcal{E}(\theta) = \mathcal{L}_{t}^{sup}(\theta)$ . The training domains were  $(s_{1}, s_{2}, s_{3})$ =(natural, watercolor, comic), and the test domain was clipart. We can see that EMA, PL, and the regularization lowered the changes in the losses on both the training domains and test domain. In other words, each contributed to falling into flatter minima.

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#### 8 CONCLUSION AND LIMITATION

We tackled two problem settings called semi-supervised domain generalizable object detection (SS-520 DGOD) and weakly-supervised DGOD (WS-DGOD) to train object detectors that can generalize to 521 unseen domains. We showed that the object detectors can be effectively trained on the two settings 522 with the same Mean Teacher learning framework. We also provided the interpretations of why the 523 detectors trained with the Mean Teacher framework become robust to the unseen domains in terms 524 of the flatness in the parameter space. Based on the interpretations, we introduced a regularization 525 method to lead to flatter minima, which makes the loss value of the student similar to that of the teacher. The experiments showed that the detectors trained with the Mean Teacher learning frame-527 work and the regularization performed significantly better than the baseline methods. Because Mean 528 Teacher has been used across various tasks, our novel interpretation of why Mean Teacher becomes 529 robust to unknown domains is likely to have a broad impact across a wide range of tasks.

530 The limitation is that the assumption in Sec. 5.4 does not always hold. Specifically, it is not always 531 guaranteed that the pseudo labels from the teacher are accurate enough to approximate  $\mathcal{L}_{ss}^{unsup}$  with 532  $\mathcal{L}_{s,i}^{sup}$ . Nevertheless, we empirically showed that the Mean Teacher and the regularization lead to flatter minima in practice. There are two primary reasons for this observation. First, when consid-534 ering each domain independently, the assumption always holds in the labeled domain  $s_1$ , as labeled data is available, ensuring that  $\mathcal{L}_{s_1}^{unsup} = \mathcal{L}_{s_1}^{sup}$ . Second, the assumption is only necessary to explain 535 how the Mean Teacher achieves flat minima in the empirical risk (i.e., the sum of the supervised 536 losses  $\mathcal{E}_{\text{ER}}(\theta) = \sum_{i=1}^{N_D} \mathcal{L}_{s_i}^{\text{sup}}(\theta)$ . Even if this assumption does not hold, we can similarly explain 537 that the Mean Teacher reaches flat minima in the sum of supervised and unsupervised losses in Eq. 538 (3). We believe that achieving flat minima in Eq. (3) still positively affects robustness against unseen domains. Further analysis of failure cases is left for future work.

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# 756 APPENDIX / SUPPLEMENTAL MATERIAL

## A MORE ANALYSIS

A.1 How Sensitive to Hyperparameter  $\beta$ ?

Table 3 shows the performance when the hyperparameter  $\beta$  in Eq. (8) (i.e. strength of the regularization) was changed from 0 to 1. By adding the regularization, the performance was constantly improved from the detector without regularization (i.e.,  $\beta = 0$ ).

Table 3: mAP50 with various  $\beta$  on the artistic style image dataset (Inoue et al., 2018).

setting	method	β	mAP50
8		r	clipart
SS-DGOD SS-DGOD SS-DGOD SS-DGOD	Gaussian FasterRCNN + EMA + PL Gaussian FasterRCNN + EMA + PL + Regul. Gaussian FasterRCNN + EMA + PL + Regul. Gaussian FasterRCNN + EMA + PL + Regul.	0.0 0.25 0.5 0.75	39.8 40.7 <b>43.3</b> 42.1

A.2 IMPORTANCE OF ENCOURAGING CONSISTENCY

#### A.2.1 COMPARISON OF REGULARIZATION WITH AND WITHOUT POST-PROCESSING

In the regularization described in Sec. 6.1, we use the raw outputs from the teacher *without post-processing* to train the student so that the outputs from the two networks are similar. To validate the claim, we compare the performance with and without post-processing (i.e., sharpening function (Chen et al., 2022)) in the regularization in Eq. (9). Table 4 shows that the performance drops when we perform the post-processing. We observe that using raw outputs is important to obtain better performance.

Table 4: mAP50 with and without post-processing on the artistic style image dataset (Inoue et al., 2018).

setting	method	post process	mAP50	
			clipart	
SS-DGOD SS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul. Gaussian FasterRCNN + EMA + PL + Regul.	$\checkmark$	<b>43.3</b> 39.4	

#### A.2.2 IMPORTANCE OF CONSISTENT AUGMENTATION BETWEEN TEACHER AND STUDENT

In the regularization described in Sec. 6.1, we input *weakly*-augmented images to the student (i.e., same input as the teacher) in order to encourage the consistency between the outputs from the teacher and student. In this section, as shown in Fig. 6, we compare the weak and strong augmentation for the student in the regularization whereas weakly-augmented images were always input to the teacher. Table 5 shows that the weak augmentation obtains better performance than the strong augmentation, which implies the consistency between the outputs from the teacher and student using the same inputs leads to better performance.

Table 5: Comparison of mAP50 between strong and weak augmentation in the regularization on the
 artistic style image dataset (Inoue et al., 2018).

806 807	setting	method	augmentation	mAP50 clipart
808	SS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	weak	<b>43.3</b>
809	SS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	strong	42.5



Figure 6: Comparisons between weak and strong augmentation for the student in the regularization.

#### A.3 WHY IS ONLY WEAK AUGMENTATION USED IN THE REGULARIZATION?

One may think why only weak augmentation is used in the regualization in Fig. 4, and what is the performance of randomly using strong and weak augmentation? To answer this question, we evaluated the performance when randomly using strong and weak augmentation as shown in the right side of Fig. 7. In this setting, the strong and weak augmentation was randomly chosen with a probability of 0.5 at each iteration. When the strong augmentation was chosen, the same strongly augmented image was input into both the student and teacher networks. Then, the raw output from the teacher without post-processing was used to calculate the regularization loss for the students in Eqs. (8) and (9) to encourage consistency between the outputs from the student and teacher. As shown in Table 6, only weak augmentation obtained better performance. We think it is because inputting strongly augmented images into the teacher can make noisy pseudo-labels.



Figure 7: Comparisons between weak and random (weak/strong) augmentation in the regularization.

Table 6: Comparison of mAP50 between weak and weak/strong (random) augmentation in the regularization on the artistic style image dataset.

setting	method	augmentation	mAP50
			clipart
SS-DGOD SS-DGOD SS-DGOD	Gaussian FasterRCNN + EMA + PL Gaussian FasterRCNN + EMA + PL + Regul. Gaussian FasterRCNN + EMA + PL + Regul.	N/A weak weak/strong (random)	39.8 <b>43.3</b> 41.1

#### A.4 DOES THE REGULARIZATION MAKE IT DIFFICULT OR SLOW TO TRAIN THE MODEL?

One may be concerned whether the regularization makes the training difficult or slow because the
regularization in Fig. 4 encourages the teacher and student to produce similar predictions. To address
the concern, in Fig. 8, we show the mAP on the validation set during training with and without
regularization. The regularization does not make the training process more difficult or slower. On
the contrary, the regularization helps alleviate overfitting (i.e., less decrease in the validation mAP),
stabilizing the training.



unlabeled domains (e.g.,  $(s_1, s_2, s_3, t)$ = (natural, clipart, comic, watercolor)). In this section, we conducted the experiments with one labeled domain and one unlabeled domain, which are the same

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921	setting	method	bicycle	bird	cat	car	dog	person	mAP
922	Single-DGOD	CLIP-based augmentation (Vidit et al., 2023)	74.8	37.3	36.8	40.7	29.2	59.9	46.4
923	Single-DGOD Single-DGOD	Gaussian FasterRCNN Gaussian FasterRCNN + EMA	<b>90.4</b> 86.2	47.9 <b>54.3</b>	30.3 35.3	46.7 53.5	28.7 34.5	59.2 69.0	50.5 <b>55.5</b>
924	SS-DGOD	CDDMSL (Malakouti & Kovashka, 2023) (RegionCLIP)	66.3	50.6	34.5	49.2	20.1	56.0	46.1
925	SS-DGOD SS-DGOD	Gaussian FasterRCNN + EMA + PL Gaussian FasterRCNN + EMA + PL	/5.5 87.4 87.2	36.1 54.6	40.0	40.7 51.9	19.7 32.4	52.0 73.1 75.3	41.3 56.6
926	WS-DGOD	Gaussian FasterPCNN + EMA + PL	00.3	55.8	44.7	10.0	37.5	75.5	50.2
927	WS-DGOD WS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	95.8	<b>59.9</b>	51.5	53.3	40.2	76.7	62.9
928	DGOD	Gaussian FasterRCNN	84.8	57.8	51.0	50.8	51.8	79.3	62.6
000	Oracle	Gaussian FasterRCNN	90.9	59.9	44.2	53.1	46.7	78.3	62.2
929	UDA-OD	Gaussian FasterRCNN + EMA + PL (Chen et al., 2022)	77.7	46.5	40.4	50.1	39.7	75.0	54.9
930	UDA-OD	Gaussian FasterRCNN + EMA + PL + Regul.	82.8	51.4	43.2	59.3	39.0	77.0	58.8
0.0.4	UDA-OD	SCL* (Shen et al., 2019)	82.2	55.1	51.8	39.6	38.4	64.0	55.2
931	UDA-OD	SWDA* (Saito et al., 2019)	82.3	55.9	46.5	32.7	35.5	66.7	53.3
932	UDA-OD UDA-OD	UMT* (Deng et al., 2021) AT* (Li et al., 2022)	88.2 93.6	55.3 56.1	51.7 58.9	39.8 37.3	43.6 39.6	69.9 73.8	58.1 59.9
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Table 7: Comparisons of AP50 at each class on watercolor of the artistic style image dataset (Inoue et al., 2018). The values of \* are from (Li et al., 2022).

Table 8: Comparisons of AP50 at each class on clipart of the artistic style image dataset (Inoue et al., 2018).

setting	method	bicycle	bird	cat	car	dog	person	mAP
Single-DGOD	CLIP-based augmentation (Vidit et al., 2023)	36.5	22.5	20.1	25.0	8.8	50.4	27.2
Single-DGOD	Gaussian FasterRCNN	69.5	25.1	5.7	39.4	17.3	49.9	34.5
Single-DGOD	Gaussian FasterRCNN + EMA	87.6	29.3	5.5	30.1	18.3	57.2	38.0
SS-DGOD	CDDMSL (Malakouti & Kovashka, 2023) (RegionCLIP)	51.0	33.3	26.5	45.2	14.6	63.8	39.1
SS-DGOD	CDDMSL (Malakouti & Kovashka, 2023) (Res101)	41.6	19.2	5.5	26.7	12.3	50.9	26.0
SS-DGOD	Gaussian FasterRCNN + EMA + PL	75.8	31.2	9.4	33.1	20.4	69.1	39.8
SS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	79.3	32.5	11.6	40.9	26.3	69.0	43.3
WS-DGOD	Gaussian FasterRCNN + EMA + PL	80.3	33.3	11.1	44.5	23.2	72.6	44.2
WS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	84.8	33.2	23.8	43.0	22.1	70.1	46.2
DGOD	Gaussian FasterRCNN	76.0	34.8	18.8	38.3	36.9	77.6	47.1
Oracle	Gaussian FasterRCNN	70.4	38.8	26.1	52.9	27.5	73.4	48.2
UDA-OD	Gaussian FasterRCNN + EMA + PL (Chen et al., 2022)	79.9	33.5	6.5	53.1	23.7	65.2	43.6
UDA-OD	Gaussian FasterRCNN + EMA + PL + Regul.	72.4	35.4	16.0	57.2	19.7	71.5	45.4

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settings as the CDDSL paper (Malakouti & Kovashka, 2023): (s1, s2, t) = (natural, comic, watercolor) and (natural, comic, clipart). Table 10 shows the superior performance to CDDMSL even on these settings.

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#### A.8 DIFFERENT BACKBONE

To validate the generalization ability of the regularization, we conducted the experiments with another detector that has a significantly different network design. Specifically, we used a Transformerbased backbone (Swin-T) with the feature pyramid network (Lin et al., 2017), although the detection head was not changed. Table 11 shows the results. We can see that the regularization improves the performance, which validates its generalization ability.

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#### A.9 COMPARISON AND COMBINATION WITH ANOTHER EXISTING TRICK TO IMPROVE FLAT MINIMA

Table 12 shows the comparison with another existing method to find flat minima called Sharpness-Aware Minimization (SAM) (Foret et al., 2021). By comparing *Gaussian FasterRCNN* + *EMA* + *PL* + *SAM* and *Gaussian FasterRCNN* + *EMA* + *PL* + *Regul.*, our regularization outperforms the SAM. In addition, since the SAM is an optimizer and can be used instead of SGD, it is compatible with our regularization. We can see that *Gaussian FasterRCNN* + *EMA* + *PL* + *Regul.* + *SAM* achieved the best performance.

#### Table 9: Comparisons of AP50 at each class on comic of the artistic style image dataset (Inoue et al., 2018).

setting	method	bicycle	bird	cat	car	dog	person	n
Single-DGOD	CLIP-based augmentation (Vidit et al., 2023)	29.0	18.6	27.6	32.7	28.4	52.2	3
Single-DGOD	Gaussian FasterRCNN	45.0	10.8	9.5	33.8	17.5	43.0	- 1
Single-DGOD	Gaussian FasterRCNN + EMA	50.0	15.0	11.2	26.8	22.4	48.3	
SS-DGOD	CDDMSL (Malakouti & Kovashka, 2023) (RegionCLIP)	41.8	27.8	23.5	44.2	34.8	57.8	
SS-DGOD	CDDMSL (Malakouti & Kovashka, 2023) (Res101)	44.3	12.2	13.7	30.5	19.7	52.1	
SS-DGOD	Gaussian FasterRCNN + EMA + PL	41.5	14.5	11.4	24.5	27.3	61.1	
SS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	42.3	15.6	15.9	31.5	30.2	57.8	
WS-DGOD	Gaussian FasterRCNN + EMA + PL	53.7	23.1	19.9	44.3	33.7	64.5	
WS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	54.2	23.2	23.8	44.1	31.5	64.2	4
DGOD	Gaussian FasterRCNN	54.6	29.5	33.5	38.9	43.2	71.4	
Oracle	Gaussian FasterRCNN	55.7	29.0	44.5	46.3	45.1	71.3	
UDA-OD	Gaussian FasterRCNN + EMA + PL (Chen et al., 2022)	42.2	13.6	10.8	16.6	19.3	59.5	
UDA-OD	Gaussian FasterRCNN + EMA + PL + Regul.	46.3	14.4	20.3	28.8	23.5	62.6	



(a) Gaussian FasterRCNN trained on Single-DGOD setting (i.e., trained with labeled data on PASCAL VOC07&12).



(b) Gaussian FasterRCNN + EMA + PL + Regul. trained on SS-DGOD setting (i.e., trained with labeled data on PASCAL VOC07&12 and unlabeled data on clipart and comic).

#### Figure 10: Qualitative comparisons on watertcolor.

Table 10: Comparisons of mAP50 on the artistic style image dataset when  $(s_1, s_2, t)$  = (natural, comic, watercolor) and (natural, comic, clipart). Values with \* are from previous study (Malakouti & Kovashka, 2023). 

setting	method	backbone	mAP50		
8			watercolor	clipart	
SS-DGOD	CDDMSL* (Malakouti & Kovashka, 2023)	Res50 (RegionCLIP)	49.4	39.8	
SS-DGOD	Gaussian FasterRCNN + EMA + PL	Res101	55.2	38.4	
SS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	Res101	56.5	40.1	



1078 1079 Figure 12: Qualitative comparisons on comic.

Table 11: Comparison of mAP50 with and without regularization using Swin-T + FPN backbone on the artistic style image dataset (Inoue et al., 2018).

	aattina	mathead	haalthana	mAP50	
	setting	metnod	backbone	watercolor	
	SS-DGOD SS-DGOD	Gaussian FasterRCNN + EMA + PL Gaussian FasterRCNN + EMA + PL + Regul.	Swin-T + FPN Swin-T + FPN	53.0 <b>53.4</b>	
Table 12: Com 2018).	parison an	d combination with SAM on the a	rtistic style ir	nage dataset	(Inoue et al.,

setting	method	backbone	mAP50	
			watercolo	
Single-DGOD	Gaussian FasterRCNN	Res101	50.5	
Single-DGOD	Gaussian FasterRCNN + SAM	Res101	54.1	
Single-DGOD	Gaussian FasterRCNN + EMA	Res101	55.5	
SS-DGOD	Gaussian FasterRCNN + EMA + PL	Res101	56.6	
SS-DGOD	Gaussian FasterRCNN + EMA + PL + SAM	Res101	57.5	
SS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	Res101	58.2	
SS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul. + SAM	Res101	59.5	

#### 1134 В RESULTS ON CAR-MOUNTED CAMERA DATASET (WU & DENG, 2022) 1135

#### 1136 **B.1** DATASET DETAILS 1137

1138 The car-mounted camera dataset is a recently developed dataset in (Wu & Deng, 2022) for 1139 Single-DGOD or DGOD, where the images were selected from the standard datasets such as Cityscapes (Cordts et al., 2016), FoggyCityscapes (Sakaridis et al., 2018), BDD-100k (Yu et al., 1140 2020), and AdverseWeather (Hassaballah et al., 2020). The domains were clearly redefined based 1141 on the weather and time differences: daytime-sunny, night-sunny, daytime-foggy, dusk-rainy, and 1142 night-rainy. The number of images for each domain is 27,708, 18,310, 2,642, 3,501, and 2,494, 1143 respectively. We used daytime-sunny as the labeled domain  $s_1$  and used night-sunny and daytime-1144 foggy as the unlabeled (or weakly-labeled) domains  $s_2, s_3$ . We used each of the remaining domains 1145 (dusk-rainy and night-rainy) as the target domain. Because the train/val/test split is not publicly 1146 available for daytime-sunny, dusk-rainy, and night-rainy, we used all images of daytime-sunny, the 1147 trainval set of night-sunny, and the trainval set of daytime-foggy for training. We then used the test 1148 set of night-sunny and the test set of daytime-foggy for validation. We used all images of dusk-rainy 1149 and night-rainy for evaluation (testing). There are seven object classes: bus, bike, car, motor, person, 1150 rider, and truck.

1151 There are two reasons for using this dataset for evaluation. One is that the images in this dataset were 1152 selected from the standard datasets, and the other is that the domains were clearly redefined based on 1153 the weather and time differences as described above. In the setting of the previous work (Malakouti 1154 & Kovashka, 2023), i.e.,  $(s_1, s_2, t) =$  (Cityscapes, FoggyCityscapes, BDD100k), the differences be-1155 tween domains are ambiguous. This is because Cityscape primarily assumes clear/medium daytime 1156 weather, Foggycityscape assumes foggy weather, while BDD100K includes various times of day 1157 and weather conditions. Therefore, instead, we used the car-mounted camera dataset.

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#### 1159 **B.2** COMPARISONS WITH OTHER METHODS

1161 Table 13: Comparisons of mAP50 on the car-mounted camera dataset (Wu & Deng, 2022). The 1162 values of \* and \*\* were from (Wu & Deng, 2022) and (Vidit et al., 2023), respectively.

1164	setting Single-DGOD Single-DGOD Single-DGOD Single-DGOD SS-DGOD SS-DGOD WS-DGOD WS-DGOD	method	backbone	mAP50		
1165	setting incurou		Suchoone	dusk-rainy	night-rainy	
1166	Single-DGOD	FasterRCNN*	Res101	26.6	14.5	
1167	Single-DGOD	CDSD* (Wu & Deng, 2022)	Res101	28.2	16.6	
	Single-DGOD	CLIP-based augmentation**(Vidit et al., 2023)	Res101	32.3	18.7	
1168	Single-DGOD	Gaussian FasterRCNN	Res101	25.3	13.3	
1169	Single-DGOD	Gaussian FasterRCNN + EMA	Res101	36.0	19.0	
1170	SS-DGOD	Gaussian FasterRCNN + EMA + PL	Res101	30.3	21.3	
1170	SS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	Res101	31.2	21.9	
1171	WS-DGOD	Gaussian FasterRCNN + EMA + PL	Res101	30.5	22.5	
1172	WS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	Res101	32.5	23.1	
1173	DGOD	Gaussian FasterRCNN	Res101	28.4	21.2	

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1175 Table 13 shows the results on the car-mounted camera dataset. Each of EMA, PL, and the regularization improved the performance on both target domains except that PL degraded the performance 1176 on dusk-rainy. We will investigate the cause of the performance drop in our future work. 1177

1178 The mAP50 of the detector with the regularization is boosted to (32.5, 23.1) on WS-DGOD. This 1179 result exceeds (32.3, 18.7), which is the result of CLIP-based augmentation (Vidit et al., 2023) pro-1180 posed for Single-DGOD. Also, this result is better than those of the models trained with supervised 1181 learning on the three domains (DGOD).

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#### 1183 **B.3** ANALYSIS OF FLATNESS 1184

Fig. 13 shows the average change of the training loss at each domain when perturbing the parameters 1185  $(\mathcal{F}^{\gamma}(\theta) = \mathbb{E}_{\theta'}|\mathcal{E}(\theta') - \mathcal{E}(\theta)|$  described in Sec. 7.5), and Fig. 14 shows those of the test loss. Each of 1186 EMA, PL, and the regularization lowered the changes in the losses at every domain when the radius 1187 is 125 or smaller although EMA lowered the changes the most when the radius is extremely large



 $\begin{array}{ll} 1188\\ 1189\\ radius. \end{array} (> 125). In other words, each contributed to falling into flatter minima with a sufficiently large radius. \end{array}$ 

## 1229 B.5 QUALITATIVE RESULTS

Figs. 15 and 16 show the qualitative comparison on dusk-rainy and night-rainy, respectively. Similar to the artistic image dataset, the baseline model had false negative detections, which were improved by EMA, PL, and regularization.

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#### 1235 C TRAINING DETAILS

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1237 On the artistic style image dataset, the detectors were trained with 10,000 and 20,000 iterations for 1238 the pretraining and the student-teacher learning of SS-DGOD (or WS-DGOD), respectively. During 1239 the training, we saved the models and evaluated the performance on the validation at every 2,000 1240 iterations, and the best model was used for the evaluation. The whole training took about one day. 1241 For fair comparisons, the compared models on Single-DGOD and DGOD were trained with 30,000 iterations, and the best models at the validation of every 2,000 iterations were used for evaluation.

1242	Table 15: Comparisons of AP50 at each class on night-rainy of the car-mounted camera dataset (Wu
1243	& Deng, 2022). The values of * and ** are from (Wu & Deng, 2022) and (Vidit et al., 2023),
1244	respectively.

setting	method	bus	bike	car	motor	person	rider	truck	n
Single-DGOD	FasterRCNN*	22.6	11.5	27.7	0.4	10.0	10.5	19.0	
Single-DGOD	CDSD* (Wu & Deng, 2022)	24.4	11.6	29.5	9.8	10.5	11.4	19.2	
Single-DGOD	CLIP-based augmentation** (Vidit et al., 2023)	28.6	12.1	36.1	9.2	12.3	9.6	22.9	
Single-DGOD	Gaussian FasterRCNN	20.4	7.7	31.0	0.5	6.8	5.6	21.3	
Single-DGOD	Gaussian FasterRCNN + EMA	33.9	11.1	38.5	0.8	10.5	8.8	29.2	
SS-DGOD	Gaussian FasterRCNN + EMA + PL	35.7	9.8	46.7	1.4	12.6	10.8	32.0	
SS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	37.0	10.3	46.3	2.8	12.9	12.0	31.8	
WS-DGOD	Gaussian FasterRCNN + EMA + PL	38.6	11.3	47.9	2.9	13.4	11.2	32.1	
WS-DGOD	Gaussian FasterRCNN + EMA + PL + Regul.	38.3	13.4	46.2	2.7	15.1	14.0	32.0	
DGOD	Gaussian FasterRCNN	38.9	7.6	46.7	1.8	9.8	11.3	32.1	



(a) Gaussian FasterRCNN trained on Single-DGOD setting (i.e., labeled data on daytime-sunny).



(b) Gaussian FasterRCNN + EMA + PL + Regul. trained on SS-DGOD setting (i.e., labeled data on daytimesunny and unlabeled data on night-sunny and daytime-foggy).

Figure 15: Qualitative comparisons on dusk-rainy.

1274 1275 On the car-mounted camera dataset, we performed the same procedure for training, validation, and 1276 evaluation, but the numbers of iterations for the pretraining and the student-teacher learning were set 1277 to 20,000 and 40,000 respectively, and the validation was conducted at every 4,000 iterations. The 1278 whole training took about two days. For fair comparisons, the compared models on Single-DGOD 1279 and DGOD were trained with 60,000 iterations, and the best models at the validation of every 4,000 1279 iterations were used for evaluation.

<sup>1281</sup> D MORE DISCUSSIONS

#### 1283 1284 D.1 The Other Semi-supervised Domain Generalization Setting

There are two types of settings on semi-supervised domain generalization. The first setting assumes that only a part of the samples in each domain are labeled, similar to the previous works listed in Sec. 3.3. The other one assumes that only a part of the source domains are labeled (Lin et al., 2024). In this paper, we followed the previous SS-DGOD work (i.e., CDDMSL (Malakouti & Kovashka, 2023)) and tackled the second setting. To confirm the effectiveness of the Mean Teacher framework and the regularization on the other setting is one of our future works.

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- D.2 BROADER IMPACTS
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In this work, we tackled the task of semi-supervised and weakly-supervised domain generalization for object detection (SS-DGOD and WS-DGOD), which are more practical settings than previous works. Also, we showed the good performance of the Mean Teacher learning framework, its inter(a) Gaussian FasterRCNN trained on Single-DGOD setting (i.e., labeled data on daytime-sunny). (b) Gaussian FasterRCNN + EMA + PL + Regul. trained on SS-DGOD setting (i.e., labeled data on daytime-sunny and unlabeled data on night-sunny and daytime-foggy). Figure 16: Qualitative comparisons on night-rainy. pretations, and a simple regularization method to boost the performance. Therefore, we believe that this paper has a potential positive social impact to enable practitioners or researchers to train robust object detectors to unseen domains in a simpler way than previous approaches. In addition, because Mean Teacher has been used across various tasks, our novel interpretation of why Mean Teacher becomes robust to unknown domains is likely to have a broad impact across a wide range of tasks. We are unable to identify any pertinent information concerning potential negative impacts. Ε **REPRODUCIBILITY STATEMENT** We submit the source code that can reproduce the results in this paper as a supplemental zip file.