# TANGENTBIND: UNLOCKING THE POTENTIAL OF EMERGENT ALIGNMENT IN MULTIMODAL MODEL

Anonymous authors

004

010 011

012

013

014

015

016

017

018

019

021

025

026

027 028 029

030 031

038

Paper under double-blind review

# Abstract

Improving the alignment of modalities has proven effective across various downstream tasks in multimodal models. Currently, modality alignment follows two main research directions: aligning all modalities simultaneously or binding the others by aligning to a core modality. The first ensures direct alignment, but it is difficult to extend to new modalities. The second is scalable but weak in emergent ability due to needing more direct inter-modality alignment. To address these problems, we propose the **TangentBind**. Specifically, we first align all modalities to a core modality, e.g., image or text. Then, we introduce a generative network that generates the embeddings of the second modality, e.g., text or image, based on the core modality embedding. Thirdly, other modalities, such as audio, are aligned to the core modality and generative embedding, improving emergent ability while retaining alignment with the core modality. During training, in addition to infoNCE, the Tangent Term is introduced to align the new modalities with the generated embeddings. This addresses accuracy issues caused by using generated vectors as representations for modalities. With VISION and TEXT as the core modality, our experiments include other modalities such as AUDIO, DEPTH, and INFRARED. Eventually, our experiments show that the emergent ability of TangentBind significantly outperforms the original benchmark on 9 datasets.

# 1 INTRODUCTION

Unifying multimodal representation aims to learn a shared semantic representation space across various modalities, such as audio, RGB images, text, depth images, and heatmaps(Wang et al., 2023a; Girdhar et al., 2023; Guzhov et al., 2021; Wu et al., 2021; 2022; Liu et al., 2023). A unified multimodal space is essential as a critical foundation for multimodal understanding and generation (Karpathy et al., 2014; Mithun et al., 2018; Lu, 2023). However, the previous multimodal requires all modes to coexist, which is challenging and labor-intensive(Guzhov et al., 2021; Radford et al., 2021; Moon et al., 2022).

Due to the limitations of existing datasets, recent approaches only utilize pairs of modalities or a few visual modalities. Consequently, the resulting embeddings are confined to the modality pairs 040 used during training and lack alignment for other modalities (Zhu et al., 2024). Recent works have 041 introduced more flexible alignment strategies to address this issue.(Gao et al., 2024; Wang et al., 042 2024a; Zhu et al., 2024; Dhakal et al., 2024; Wang et al., 2024b; Lyu et al., 2024). Among them, 043 ImageBind was the first work in this direction, introducing a core modality alignment framework to 044 reduce paired data requirements, where only the image as core modality is directly aligned with other modalities. The concept of **emergent** alignment pertains to the indirect alignment performance, and it also facilitates a degree of alignment between modalities that are not directly trained together. 046 However, when other modalities are indirectly aligned through text, the emergent effect exists only 047 in limited form, which typically results in suboptimal zero-shot performance. 048

To address the weak zero-shot performance issue of ImageBind, LanguageBind (Zhu et al., 2024)
 selects text as the core modality and employs generative data to enhance text-related zero-shot ca pabilities. However, LanguageBind struggles with retrieval tasks involving non-text modalities due
 to the limitations of the binding method. Specifically, text needs more of the fine-grained details
 presented in images. Using text as the core modality significantly reduces retrieval performance
 across various image-based modalities. Besides, generating large amounts of data requires much

 human work and computational resources. A vital limitation of these binding methods relying on indirect alignment lies in the potential degradation of emergent or zero-shot performance, especially for modalities that lack direct alignment(Zhu et al., 2024).

057 In this paper, we propose TangentBind. This method is capable of mapping all modalities into a unified embedding space and enhanc-060 ing the emergent capabilities of models us-061 ing an embedding generative network. Fur-062 thermore, our method does not require extra 063 datasets where all modalities are present simul-064 taneously, nor does it rely on massive synthetic data across different modalities. Instead, we 065 train a generative network to generate the em-066 bedding vectors of modalities that have already 067 been aligned with the core modality. Based 068 on the embedding vector of the core modal-069 ity, these generated embeddings can be used to align with other modalities. Notably, when 071 the generated embedding is used to align the 072 generated embedding vector with other modal-073 ities, it can affect the alignment with the core 074 Therefore, we propose the Tanmodality. 075 gent Term for preventing this problem, and we 076 demonstrate the effectiveness of the Tangent Term in section 3.2. Additionally, we demon-077 strate that TangentBind can be initialized using large-scale pre-trained multimodal models, 079 such as CLIP(Radford et al., 2021), Language-



Figure 1: **Zero-shot** Language-related task performance. TangentBind with image core modality was demonstrated as a powerful emergent ability for indirect alignment modalities.

Bind(Zhu et al., 2024), and ImageBind(Girdhar et al., 2023), and that Tangent Term can massively 081 increase the emergence capacity used to initialize the model. We utilized Image and Text as the core modalities, respectively, and ensured the extension of vision and language to audio, depth, 083 and infrared modalities. The model demonstrated strong emergent capabilities in tasks involving 084 each modality that was not directly trained. In figure.2, we compare TangentBind with ImageBind 085 and LanguageBind and show the advantages of TangentBind. TangentBind, with the image as the core modality, achieved emergent classification top-1 accuracy. Figure.1 demonstrates the powerful emergent capabilities of TangentBind with image core modality. Our experiment results surpass 087 ImageBind by 8.5%, 10.3%, and 16.1%, respectively, on ESC, LLVIP, and NYU-D benchmarks. 088 Similarly, TangentBind, with text as the core modality, also achieved emergent retrieval Recall@1 089 results of 25.1, 12.8, and 23.9 on image retrieval tasks in VGG-S, LLVIP, and NYU-D benchmarks 090 surpassing LanguageBind by 15.1, 5.3, and 6.0, respectively. Therefore, TangentBind can compete 091 with or outperform specialized models trained with direct supervision. 092

- Our primary contributions are listed as follows:
  - We propose **TangentBind**, a multimodal pre-train method based on latent space generation. During training, all modalities are aligned with the core modality through contrastive learning, while the generative model enhances the emergent capabilities of the indirect alignment modality.
  - We propose **Tangent Term**, a loss function term that enhances the emergent ability of the model while maintaining core modality alignment.
  - Extensive experiments validate the effectiveness of our method, demonstrating significant performance improvements in the emergent capabilities of bind-type models.
  - 2 RELATED WORK

094

096

098

099

100

101 102 103

104

## 105 2.1 MULTIMODAL LEARNING

- 107 CLIP(Radford et al., 2021) is a pioneering multimodal learning method that aligns images and text for constructing cross-modal representations. Various methods, such as CLIP4Clip(Luo et al., 2022)
  - 2



Figure 2: TangentBind vs. ImageBind and LanguageBind. The image on the left shows ImageBind's indirect alignment of the modal by aligning it directly with image. The center image shows LanguageBind augmenting the zero-shot capability of the model by generating data. The right image demonstrates TangentBind, with image as the core modality, which enhances the emergent zero-shot capabilities by simply generating embedding.

123

130 and Clip2Video(Fang et al., 2021), etc, adapt CLIP to extract semantic vision representations. Re-131 cent efforts have comprehensively explored multimodal alignment through pretraining(Yin et al., 132 2023; Xu et al., 2023; Wu et al., 2023). In addition to language and vision modalities, Audio-133 CLIP(Guzhov et al., 2021) adds audio as an additional modality with the CLIP framework, enabling 134 zero-shot audio classification. Imagebind(Girdhar et al., 2023) expands multi-modal alignment pre-135 training by aligning all modalities with the vision modality. ImageBind-LLM(Han et al., 2023) uses the joint embedding space in the pre-trained ImageBind to fine-tune LLaMA efficiently. Neu-136 roBind(Yang et al., 2024) learns a general representation based on pre-trained image embedding 137 space that unifies multiple types of brain signals. UniBind(Lyu et al., 2024) adaptively build LLM-138 augmented classwise embedding centers and learn to achieve a unified and balanced representa-139 tion space. To enhance the performance on language-related tasks, MEDBind(Gao et al., 2024), 140 LanguageBind(Zhu et al., 2024) use text data as the core modality to align other modalities. The 141 methods mentioned above, however, did not investigate strategies to enhance the model's emergent 142 capabilities for previously untrained modality pairs.

143 144 145

2.2 CONTRASTIVE LEARNING

146 Contrastive learning has been remarkably successful in learning representations from multimodal 147 data pairs (Logeswaran & Lee, 2018; He et al., 2020). The primary motivation behind these work 148 is maximizing the mutual information between two views (Tian et al., 2020; Bachman et al., 2019; Tamkin et al., 2020). The loss functions, such as NCE (Gutmann & Hyvärinen, 2010), infoNCE 149 (van den Oord et al., 2018) and MIL-NCE (Miech et al., 2020), have been proposed for contrastive 150 learning. However, these loss functions focus on the alignment of two modalities. To extend the 151 model to multiple modalities, (Guzhov et al., 2021; Alayrac et al., 2020) propose a simple summa-152 tion of loss functions for joint learning across various modalities. According to Wang & Isola (2020), 153 the loss function of contrastive learning can be split into the alignment and uniformity parts. The 154 alignment part is responsible for the alignment when using loss function summation for multimodal 155 alignment. We analyze the direct summation of two loss functions, and then the two alignment parts 156 will interfere in appendix A.2. 157

# 3 METHOD

#### 159 160

158

161 We present TangentBind, a multimodal pretraining approach to align different modalities and enhance cross-modal retrieval and emergent classification. Figure 3 shows the process of aligning text



Figure 3: An example of TangentBind overview with  $\mathcal{M}_a, \mathcal{M}_b$  and  $\mathcal{C}$  are text, audio, and image, respectively. Firstly, we align image with text with infoNCE loss function. Secondly, our work trains generative network fed by image embedding conditions on text embedding with frozen image encoder and text encoder parameters. Finally, our method uses infoNCE and **tangentbind** to align the audio with the image and the generated text embedding.

with image and then aligning audio with image and generative text embedding, with the image as the core modality. **TangentBind** consists of three steps:

- 1. Align modality  $\mathcal{M}_a$  with the core modality  $\mathcal{C}$
- 2. Train a generative network to produce  $\mathcal{M}_a$  embedding using core modality embedding.
- 3. Align modality  $\mathcal{M}_b$  with both the  $\mathcal{C}$  and the generative modality

When using TangentBind to bind N + 1-th modality, this process only needs to replace  $\mathcal{M}_a$  and  $\mathcal{M}_b$  with any modality that has been aligned with  $\mathcal{C}$  and N + 1-th modality, and then perform step 2 and 3.

#### 3.1 ALIGNING CORE MODALITY AND GENERATIVE NETWORK

Following ImageBind (Girdhar et al., 2023) and LanguageBind (Zhu et al., 2024), TangentBind trains each encoder separately for respective modality. First, step 1 uses a contrastive learning method to train  $\mathcal{M}_a$  encoder and  $\mathcal{C}$  encoder for alignment. Then TangentBind uses aligned modality  $\mathcal{M}_a$  to train a latent generative model of modality pair  $\langle x_i^a, c_i \rangle$ . We train our model to predict the unnoised  $x_i^a$  directly and use a mean-squared error loss on this prediction:

$$\mathcal{L} = \mathcal{E}_{t \sim [1,T]} \| G_{\Theta}(\hat{x}_i^{a,(t)}, t, c_i) - x_i^a \|^2.$$
(1)

In formula 1, G is generative net and  $\Theta$  is the training coefficient. Finally, they can be normalized on the hypersphere, and we can get the generated embedding  $\hat{x}_i^a$ . When aligning other modalities with C, we also use the **Tangent Term** to align with the generated  $\mathcal{M}_a$  embedding in the tangent space.

#### 3.2 Aligning Core Modality and Generative Modality

The alignment performance will be weakened if we directly align with the generated inaccurate embedding (Oussidi & Elhassouny, 2018). Therefore, **Tangent Term**, an improvement of infoNCE, is proposed to reduce the adverse effects of inaccurate embeddings.

213 The definition of infoNCE is given by the equation:

214 215

182 183

185 186

187

188

189 190

191

192

193 194

195

201 202

207

208

 $\mathcal{L}_{\mathcal{M}_b \to \mathcal{C}}^{\text{infoNCE}} = -\frac{1}{N} \sum_{i}^{N} \log(\frac{\exp(\operatorname{sim}(x_i^b, c_i)/\tau)}{\sum_{j}^{N} \exp(\operatorname{sim}(x_i^b, c_j)/\tau)}).$ (2)

In equation 2  $x_i^b, c_i$  is *i*-th embedding vector of  $\mathcal{M}_b, \mathcal{C}$  respectively,  $\tau$  is temperature and sim $(\cdot, \cdot)$ is similarity function. According to Wang & Isola (2020), infoNCE can be divided into the align part and the uniform part as shown in equation 3 and 4 respectively. 

$$\mathcal{L}^{\text{align}} = -\sin(x_i^b, c_i)/\tau, \qquad (3) \quad \mathcal{L}^{\text{uniform}} = \log(\sum_j \exp(\sin(x_i^b, c_j)/\tau)). \quad (4)$$

The align part is responsible for aligning the features, and the uniform part makes the embedding space more evenly distributed on the hypersphere.

$$\bar{c}_i \triangleq -\frac{\partial \mathcal{L}^{\text{align}}}{\partial x_i^b} = \frac{\partial \sin(x_i^b, c_i)}{\partial x_i^b} / \tau.$$
(5)

To achieve higher similarity between  $x_i^b$  and  $c_i$ , the moving direction of  $x_i^b$  and the inner product of  $-\partial \mathcal{L}^{\text{align}}/\partial x_i$  are greater than 0 after updating the parameters. We denote  $\bar{c}_i$  in equation 5<sup>1</sup>.

**Tangent Term** (see equation 6) is proposed for keeping the similarity between  $x_i^b$  and  $c_i$  increasing while aligning  $\mathcal{M}_b$  with the generative  $\mathcal{M}_a$  embedding  $\hat{x}_i^a$ .

$$\mathcal{L}_{\mathcal{M}_b \to \mathcal{M}_a}^{\text{tan}} = -\frac{1}{N} \sum_{i}^{N} \log(\frac{\exp(\sin(T_{\bar{e}_i}(x_i^b), \hat{x}_i^a)/\tau)}{\sum_{j}^{N} \exp(\sin(T_{\bar{e}_i}(x_i^b), \hat{x}_j^a)/\tau)}).$$
(6)

**Tangent Term** In equation 6,  $\hat{x}_i^a$  is generated from  $c_i$  by the generative network in 3.1 and  $T_{\bar{c}_i}(\cdot)$ is tangent normalize function. It is the crucial function in **Tangent Term**. Its functionality is mapping the embedding to the space tangent to  $\bar{c}_i$  and scaling it to the unit hypersphere. Thus,  $T_{\bar{c}_i}(\cdot)$  is defined as  $T_{\bar{c}_i}(x) \stackrel{\Delta}{=} \operatorname{normalize}\left(\left(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}\right)x\right)$ , where  $\left(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}\right)$  project x into the orthogonal complement space of  $\bar{c}_i$  which means  $\bar{c}_i^T \left(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}\right) = 0$  as shown in Figure.4.



Figure 4:  $T_{\bar{c}_i}$  maps x to the orthogonal space

of  $\bar{c}_i$  and normalizes it.



Figure 5: The process of aligning  $x_i^b$  with  $c_i$ and  $\hat{x}_i^a$  simultaneously.  $\theta_a, \theta_b$  represent the angles of  $c_i$  with  $\hat{x}_i^a$ ,  $x_i^b$ , respectively.  $\phi$  is denoted as the angle between  $\hat{x}_i^a$  and  $x_i^b$  in the tangent space of  $c_i$ .

Finally, the loss function can be rewritten into the following form:

$$\mathcal{L} = \mathcal{L}^{\text{infoNCE}} + \lambda \mathcal{L}^{\text{tan}}.$$
(7)

In equation 7,  $\lambda$  is the hyperparameter ,  $\mathcal{L}^{tan} = (\mathcal{L}_{\mathcal{M}_h \to \mathcal{M}_a}^{tan} + \mathcal{L}_{\mathcal{M}_a \to \mathcal{M}_b}^{tan})/2$  and  $\mathcal{L}^{infoNCE} =$  $(\mathcal{L}_{\mathcal{M}_b \to \mathcal{C}}^{\text{infoNCE}} + \mathcal{L}_{\mathcal{C} \to \mathcal{M}_b}^{\text{infoNCE}})/2.$ 

Figure 5 illustrates the loss function 7 enables  $x_i^b$  to simultaneously align with both  $c_i$  and  $\hat{x}_i^a$  while using cosine similarity. The black arrow toward  $c_i$  represents the infoNCE objective, bringing  $x_i^{i}$ 

<sup>&</sup>lt;sup>1</sup>It is worth noting that the higher the similarity, the lower  $\mathcal{L}^{align}$ 

and  $c_i$  closer together. The other black arrow indicates the **Tangent Term**, which drives  $x_i^b$  toward  $\hat{x}_i^a$  within the space orthogonal to  $c_i$ . As this orthogonal space on the sphere corresponds to the tangent space at  $c_i$  (do Carmo, 2016), we refer to the method as **TangentBind**.

# 4 THEORETICAL ANALYSIS

This analysis mainly illustrates the effect of the **Tangent Term** on the similarity of  $x_i^b$  and  $c_i$  while ignoring the effect of  $\mathcal{L}^{\text{uniform}}$ . Since the optimization methods(Kingma & Ba, 2014; Ruder, 2016), are all gradient-based optimization, our analysis is based on gradients primarily. The update parameter  $\Delta\Theta$  can be simply written as  $\delta(\frac{\partial \mathcal{L}^{\text{align}}}{\partial\Theta} + \lambda \frac{\partial \mathcal{L}^{\text{lan}}}{\partial\Theta})$  where  $\delta$  is step size. To clarify the effect of  $\mathcal{L}^{\text{tan}}$ on  $\mathcal{L}^{\text{align}}$  during gradient descent, we introduce Theorem 1, and the proof is shown in Appendix.A.1.

**Theorem 1.** If 
$$\lambda \leq \frac{\|\bar{c}_i\|}{\|\frac{\partial \mathcal{L}^{lan}}{\partial \bar{\tau}_{\bar{c}_i}(x_i^b)}\|}$$
, then we have

$$\left(\frac{\partial \mathcal{L}^{align}}{\partial \Theta} + \lambda \frac{\partial \mathcal{L}^{tan}}{\partial \Theta}\right)^T \frac{\partial \mathcal{L}^{align}}{\partial \Theta} \ge 0.$$
(8)

According to Theorem.1 and Taylor expansion(Rudin, 1976), when updating the coefficients, we have

$$\mathcal{L}^{\text{align}}(\Theta + \Delta\Theta) \approx \mathcal{L}^{\text{tan}}(\Theta) - \delta(\frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} + \lambda \frac{\partial \mathcal{L}^{\text{tan}}}{\partial \Theta})^T \frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} \le \mathcal{L}^{\text{align}}(\Theta), \tag{9}$$

which means the similarity between  $x_i^b$  and  $c_i$  will not decrease. To be specific, when  $sim(\cdot, \cdot)$  is cosine similarity, substituting  $\frac{\partial \mathcal{L}^{tan}}{\partial x_i^b}$  with  $\bar{c}_i$  according to equation.5 we have

$$\|\bar{c}_i\| = \|\frac{\partial \mathcal{L}^{\text{align}}}{\partial x_i^b}\| = \|\frac{\partial (c_i^T \cdot x_i^b)}{\partial x_i^b}\|/\tau = \|c_i^T\|/\tau = \frac{1}{\tau},\tag{10}$$

and

274

275 276

277

278

279 280

281 282

284

287

288

289 290 291

292

293

295 296 297

298 299

304

305

306 307

308

310

311

312

$$\left\|\frac{\partial \mathcal{L}^{\mathrm{tan}}}{\partial T_{\bar{c}_i}(x_i^b)}\right\| = \left\|\frac{\partial ((\hat{x}_i^a)^T \cdot T_{\bar{c}_i}(x_i^b))}{\partial T_{\bar{c}_i}(x_i^b)}\right\| / \tau = \left\|\hat{x}_i^a\right\| / \tau = \frac{1}{\tau}.$$
(11)

Thus, cosine similarity means  $\lambda \leq 1$  can ensure that  $\left(\frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} + \lambda \frac{\partial \mathcal{L}^{\text{tan}}}{\partial \Theta}\right)^T \frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} \geq 0$  due to  $\|\bar{c}_i\|/\|\frac{\partial \mathcal{L}^{\text{tan}}}{\partial T_{\bar{c}_i}(x_i^b)}\| = 1.$ 

In the above analysis, we ignore the effect of  $\mathcal{L}^{\text{uniform}}$ . However, during the training process,  $\mathcal{L}^{\text{uniform}}$  may cause similarity to decrease. The detailed analysis for  $\mathcal{L}^{\text{uniform}}$  has been studied in previous work (Liang et al., 2022; Wang & Isola, 2020).

# 5 EXPERIMENTS AND RESULTS

This section includes an evaluation of the effectiveness of TangentBind in various downstream tasks such as RGB image, depth image, infrared image, and audio. The effectiveness of the generative network has also been tested. We also conduct the ablation study to analyze the impact of **Tangent Term** and different parameter configurations on the performance of TangentBind. For the dataset and experimental implementation details, please refer to the Appendix.B and C.

#### 5.1 IMPLEMENTATION DETAILS

Only two modalities (image and language) have datasets paired with multiple other modalities, so we only show the results using **TangentBind** with Image and Text as the core modality, respectively. The sim( $\cdot$ ,  $\cdot$ ) notation in **TangentBind** is cosine similarity. To demonstrate the adaptability of **Tangent Term**, we use the pre-trained multimodal models ImageBind-Huge(Girdhar et al., 2023) and LanguageBind(Zhu et al., 2024) respectively for initialization. Since the embedding generated by the diffusion model is different at each time, we generate  $\mathcal{M}_a$  embeddings 100 times based on each  $c_i$  and calculate the mean of the generated  $\mathcal{M}_a$  embeddings. We use AudioSet(Gemmeke et al., 2017), SUN(Song et al., 2015), and LLVIP(Jia et al., 2021) to fine-tune models. While fine-tuning Table 1: X-Language classification. \* donates Emergent Zero-shot. We report the top-1 classification accuracy(%) for all datasets except AudioSet (mAP). The SOTA of NYU-D, SUN, AudioSet,
ESC-50, and VGG-S come from (Girdhar et al., 2022)(Girdhar et al., 2022; Koutini et al., 2021;
Chen et al., 2022; Kazakos et al., 2021) respectively. DepthSwin model(Girdhar et al., 2022) is
finetuned from the ImageSwin model(Liu et al., 2021). Our results are highlighted in bold.

Mathad	Infrared	Depth		Audio			
Method	LLVIP	NYU-D	SUN	AudioSet	ESC-50	VGG-S	
OpenCLIP(Cherti et al., 2023)	82.2	45.4	25.4	-	-	-	
DepthSwin(Girdhar et al., 2022)	-	72.5	63.1	-	-	-	
JointCRF(Wang et al., 2017)	-	65.8	63.6	-	-	-	
DFCR(Cao et al., 2018)	-	65.3	56.3	-	-	-	
AudioCLIP(Guzhov et al., 2021)	-	-	-	28.4	68.6	47.4	
CLAP(Elizalde et al., 2023)	-	-	-	23.1	92.6	46.2	
WAV2CLIP(Wu et al., 2021)	-	-	-	0.71	41.4	10.0	
LanguageBind	87.2	65.1	-	27.7	91.8	28.9	
Tan-LanguageCore	85.1	65.8	-	28.1	92.0	29.3	
ImageBind*	63.4	54.0	35.1	17.6	66.9	27.8	
Tan-ImageCore*	73.7	70.1	40.3	25.4	68.4	36.3	
Absolute SOTA	-	79.4	64.9	49.6	97.0	52.5	

the encoders of other modalities , we freeze the image and text encoder parameters of ImageBind and LanguageBind. The temperature of **Tangent Term** and infoNCE is set to the same to balance the functionality between them. According to Sec.4, to ensure the alignment with core modality, we make  $\lambda = 1$ . We use a 6-layer decode-only transformer architecture diffusion model in Ramesh et al. (2022) with 100 time steps for the generative network,<sup>2</sup>. To demonstrate the enhancement of the emergent capability with **Tangent Term**, we use only generative networks that produce either image or text for our downstream tasks, which are all text-related or image-related.

354

355

356

345

346

347

348

349

> 5.2 TANGENT TERM AUGMENTING IMAGECORE MODEL

Emergent Ability As 357 shown in Table 1, we tested 358 the effect of Tangent 359 Term on ImageCore on 360 the emergent classification 361 task on 6 datasets. On 362 the emergent zero-shot classification tasks of 364 Audio, Depth, and In-365 frared (VGG-S(Chen et al.,

 Table 2: Zero-shot Audio-Language retrieval. \* donates Emergent

 Zero-shot. Our results are highlighted in bold.

Method	Cl	otho	AudioCaps		
wiethou	R@1	R@10	R@1	R@10	
AVFIC(Nagrani et al., 2022)	3.0	17.5	8.7	37.7	
AudioClip(Guzhov et al., 2021)	3.20	20.3	3.53	31.6	
WAV2Clip(Wu et al., 2021)	0.78	12.1	0.88	15.3	
C-MCR(Wang et al., 2023b)	8.37	36.7	15.76	48.1	
LanguageBind	12.1	44.0	12.2	53.2	
Tan-LanguageCore	11.7	41.8	11.8	52.1	
ImageBind*	6.0	28.4	9.3	42.3	
Tan-ImageCore*	10.0	33.4	10.1	49.2	

2020), NYU-D(Nathan Silberman & Fergus, 2012), and LLVIP(Jia et al., 2021)), TangentBind 366 top-1 accuracy outperforms ImageBind 8.5%, 16.1%, and 10.3% respectively. In addition, as 367 shown in Table 2, we also test **TangentBind** on the Audio-Language emergent retrieval task. The 368 recall@10 on the Clotho(Drossos et al., 2019), AudioCaps(Kim et al., 2019) datasets are 5% and 369 6.9% higher than the ImageBind after the introduction of **Tangent Term**. The emergent capability 370 shows significant improvement across all benchmarks, achieving performance levels that closely 371 approximate those achieved by incorporating text features. These experiment results suggest that 372 **TangentBind** effectively aligns multiple modalities within Tangent Space, thereby significantly 373 enhancing the emergent zero-shot capabilities. 374

375

Core Modality Alignment Ability Table 3 presents the performance of TangentBind for zeroshot retrieval using RGB images. The experimental results demonstrate that the introduction of

<sup>&</sup>lt;sup>2</sup>The code can be found in https://github.com/lucidrains/DALLE2-pytorch

the Tangent Term leads to improvements in Recall@1 for AVE (Tian et al., 2018), VGG-S (Chen et al., 2020), LLVIP (Jia et al., 2021), and NYU-D (Nathan Silberman & Fergus, 2012) by 0.1, 1.4, 1.1, and 0.5, respectively, compared to ImageBind model. This indicates that incorporating the Tangent Term does not degrade the alignment of the various modalities with the core modality.

382 383

- 384 5.3 TANGENT
- 385 TERM AUGMENTING 386 LANGUAGECORE MODI
- 386 LANGUAGECORE MODEL387

**Emergent Ability** As presented in 388 Table 3, we evaluated the impact of 389 the Tangent Term on LanguageCore 390 in the emergent RGB-related retrieval 391 task across four datasets. For the 392 modalities of Audio, Depth, and In-393 frared, TangentBind demonstrated 394 superior performance in Recall@1 395 on AVE (Tian et al., 2018), VGG-396 S (Chen et al., 2020), NYU-D 397 (Nathan Silberman & Fergus, 2012), and LLVIP (Jia et al., 2021), with im-398 provements of 4.5, 5.1, 6.0, and 5.3, 399 respectively, surpassing Language-400 Bind model. The emergent capabil-401 ity is significantly enhanced across all 402 benchmarks. It demonstrates that the

Dataset	Method	Task	R@1
AVE	ImageBind		36.9
	LanguageBind*	RGB→A	10.6
	Tan-ImageCore	KUD→A	37.0
	Tan-LanguageCore*		15.1
VGG-S	Imagebind		28.7
	LanguageBind*	RGB→A	10.0
	Tan-ImageCore	KUD→A	30.1
	Tan-LanguageCore*		15.1
	Imagebind		26.3
LLVIP	LanguageBind*	RGB→I	7.5
LLVIF	Tan-ImageCore	KUD→I	27.4
	Tan-LanguageCore*		12.8
	Imagebind		34.7
NYU-D	LanguageBind*	RGB→D	17.9
	Tan-ImageCore	KOD→D	35.2
	Tan-LanguageCore*		23.9

Table 3: Comparison of RGB $\rightarrow$ X retrieval.\* donates Emer-

gent. Our results are highlighted in bold.

Tangent Term remains effective even when the core modality is altered.

405 **Core Modality Alignment Ability** As shown in Table 1, to verify that the alignment between 406 various modalities and the core text modality is not compromised by the introduction of the Tan-407 gent Term, we evaluated its effect on LanguageCore model across six datasets in the zero-shot 408 classification task. For the modalities of Audio, Depth, and Infrared, TangentBind top-1 accuracy 409 outperforms LanguageBind on VGG-S (Chen et al., 2020), NYU-D (Nathan Silberman & Fergus, 410 2012), and ESC-50 (Piczak, 2015), with marginal improvements of 0.4%, 0.7%, and 0.2%, respec-411 tively. On LLVIP (Jia et al., 2021), there is only a minor top-1 accuracy decrease of 2.1%. To further 412 assess the impact of the **Tangent Term** on the core text modality, Table 2 highlights its effect on the audio-language emergent retrieval task. Following the introduction of the Tangent Term, the 413 maximum recall value on Clotho (Drossos et al., 2019) and AudioCaps (Kim et al., 2019) decreases 414 by only 2.2. These results demonstrate that the negative impact of the **Tangent Term** on tasks where 415 text serves as the core modality is minimal. 416

417

419

# 418 5.4 ABLATION STUDY

**The effect of generative networks** To illustrate the efficacy of the diffusion model, we substituted 420 it with ResNet(He et al., 2015), VAE(Kingma & Welling, 2013), and C-MCR(Wang et al., 2023b) 421 in Step 2. In Figure 6, we display the cumulative distribution function (CDF) curves of cosine 422 similarity between the embeddings generated by these methods and the actual data embeddings for 423 VGG-S(Chen et al., 2020) and SUN(Song et al., 2015). When the CDF curve approaches 1.0, it 424 indicates the generated embeddings are similar to the actual data embeddings. As illustrated in 425 Figure 6, the embeddings produced by the diffusion model closely resemble the actual embeddings. 426 Notably, the C-MCR method failed on the SUN dataset. Detailed descriptions of each method's 427 implementation are provided in Appendix C. To demonstrate the necessity of Step 2 and the robust 428 capability of **TangentTerm** to maintain alignment with the core modality, we introduced Gaussian 429 noise with a mean of 0 and a variance of 1e-3 to the core modal embeddings and normalized them as a disturbance sample. Table 4 shows that the image core model with the diffusion model achieved 430 top-1 classification accuracy of 36.3%, 73.7%, and 70.1% on emergent text-related classification 431 tasks across the VGG-S, LLVIP, and NYU-D datasets, respectively, outperforming other methods.



**Figure 6:** CDF Curve of Similarity on VGG-S and SUN. The top/bottom row displays curves representing the cosine similarity between text/image embeddings generated by various methods in Step 2 and the actual text/image embeddings, with image/text as the core modality. The solid, dashed, dash-dotted, and dotted lines correspond to the diffusion, C-MCR, ResNet, and VAE methods, respectively.

Table 4: Diffusion Model Embedding vs. Other Method Embedding. Top-1 accuracy on  $X \rightarrow T$  tasks and Recall@1 on  $RGB \rightarrow X$  tasks. Diff denotes the generation of embeddings using a diffusion model (Ramesh et al., 2022) in Step 2. The best results are highlighted in bold. A gray background indicates that the result is from an Emergent Zero-shot task.

Dataset	Task		In	nageC	ore+			Lan	guage	Core+	
Dataset	1455	Diff	ResNet	VAE	Noise	C-MCR	Diff	ResNet	VAE	Noise	C-MCR
VGG-S	$A \rightarrow T$		30.7				29.3	27.2	28.3	26.4	29.1
	RGB→A	30.1	29.3	28.1	27.7	28.3	15.1	12.3	13.5	8.1	9.5
LLVIP	$I \rightarrow T$	73.7	68.1	64.3	59.1	61.7	85.1	83.1	87.5	86.2	86.9
	RGB→I	27.4	26.5	27.1	26.1	25.9	12.8	10.3	9.1	5.2	8.9
NYU-D	$D \rightarrow T$	70.1	67.2	69.3	50.2	58.4	65.8	65.7	64.8	64.1	65.4
IN I U-D	RGB→D	35.2	35.0	33.9	33.1	34.4	23.9	20.7	22.4	14.6	18.9

Similarly, Table 4 reveals that the text core model with the diffusion model reached the highest Recall@1 scores of 15.1, 12.8, and 23.9 on **emergent** RGB-related retrieval tasks across the same datasets. Moreover, it is noteworthy that models using the diffusion model in Step 2 achieved optimal performance in all core modality-related tasks, which is white background in Table 4, except for a slight decline in the  $I \rightarrow T$  task on the LLVIP dataset compared to the best result.

**Replacing Tangent Term by infoNCE** To visualize the ability of **Tangent Term** to maintain the core modality alignment, Table 5 presents the core modality alignment results of models with image and text as the core modalities. In Table 5,  $\mathcal{L}^{infoNCE}$  is used to directly align with the generated embeddings instead of  $\mathcal{L}^{\text{tan}}$ . In detail, the **Tangent Term**  $\mathcal{L}_{\mathcal{M}_b \to \mathcal{M}_a}^{\text{tan}} + \mathcal{L}_{\mathcal{M}_a \to \mathcal{M}_b}^{\text{tan}}$  is replaced by  $\mathcal{L}_{\mathcal{M}_b \to \mathcal{M}_a}^{\text{infoNCE}} + \mathcal{L}_{\mathcal{M}_a \to \mathcal{M}_b}^{\text{infoNCE}}$  in loss function. For consistency, the value of  $\lambda$  is set to 1. As shown in Table 5, compared to **Tangent Term**, infoNCE Recall@1 scores on the image-based retrieval tasks on the VGG-S, AVE, NYU-D, and LLVIP datasets drop by 4.9, 4.7, 6.1, and 5, respectively. This indicates a direct use of infoNCE can severely disrupt the alignment of core modalities. A similar pattern is observed when text is the core modality, as Table 5 demonstrates that if infoNCE is used directly then the top-1 accuracy of text-based classification on the VGG-S, ESC-50, NYU-D, and LLVIP datasets will drop significantly to 22.2%, 72.3%, 55.7% and 64.1%. These results suggest that the **Tangent Term** enhances emergent capabilities and mitigates the negative impact on core modality alignment compared to direct alignment using infoNCE.



Figure 7: Experimental results on classification and retrieval tasks after varying hyperparameters  $\lambda$ . The first row of figures from left to right shows the results on the VGG-S, LLVIP, and NYU-D datasets with images as the core modality. The second row of figures from left to right shows the results on VGG-S, LLVIP, and NYU-D datasets with text as the core modality, respectively.

**Changing Hyperparameter**  $\lambda$  Figure.7 presents the top-1 accuracy and Recall@1 values for classification and retrieval on various datasets as a function of varying  $\lambda$  during training. As observed in Figure.7, the emergent capability of the model with the image core modality on LLVIP improves with increasing values of  $\lambda$ , reaching its peak at  $\lambda = 1.25$ . However, when  $\lambda > 1.25$ , the emergent performance gradually declines on such a model. In contrast, the Recall@1 value for image retrieval consistently decreases as  $\lambda$  increases. This trend aligns with Theorem 1, which indicates that the **Tangent Term** negatively impacts core modality alignment when  $\lambda$  becomes excessively large.

#### 6 CONCLUSION

520 In this work, we introduce Tan-521 gentBind, an emergent enhancement 522 method for multimodal pretraining. 523 To improve the integrity of modality, 524 we train a generative network that in-525 directly aligns modality embeddings. 526 Additionally, to prevent the gener-527 ated embeddings from compromis-528 ing alignment with the core modality, we propose the Tangent Term 529 for aligning the generated modal-530 ity embeddings. Extensive experi-531 ments, including the use of multi-532 ple core modalities and ablation stud-533 ies, demonstrate that the Tangent 534 Term can enhance the emergent ca-535 pabilities of the multimodal align-536 ment model while preserving align-537 ment with the core modality. 538

539

505

506

507

508 509

510

511

512

513

514

515

516 517

518

519

Table 5: **Image based retrieval** and **text based classification** on VGG-S, AVE, NYU-D, LLVIP and ESC-50. We replace **Tangent Term** by infoNCE in **image core** and **text core** modality modal during training, respectively, and compare core modality alignment performance. We report the Recall@1 score for image based retrieval tasks and top-1 classification accuracy(%) for text based classification tasks.

Dataset	Task	Core	infoNCE+			
Dataset	lask Core		Tan Term	infoNCE		
VGG-S	RGB→A	Image	30.1	25.2		
100-2	$A \rightarrow T$	Text	29.3	22.2		
AVE	RGB→A	Image	37.0	32.3		
NYU-D	$RGB \rightarrow D$	Image	35.2	29.1		
NIU-D	$D \rightarrow T$	Text	65.8	55.7		
LLVIP	RGB→I	Image	27.4	22.4		
	$I \rightarrow T$	Text	85.1	64.1		
ESC-50	$A { ightarrow} T$	Text	92.0	72.3		

540	References
541	

565

566

567

568

569

575

542	Jean-Baptiste Alayrac, Adria Recasens, Rosalia Schneider, Relja Arandjelović, Jason Ramapuram,
543	Jeffrey De Fauw, Lucas Smaira, Sander Dieleman, and Andrew Zisserman. Self-supervised mul-
544	timodal versatile networks. Advances in neural information processing systems, 33:25-37, 2020.

- Sanjeev Arora, Nadav Cohen, Noah Golowich, and Wei Hu. A convergence analysis of gradient
  descent for deep linear neural networks. ArXiv, abs/1810.02281, 2018. URL https://api.
  semanticscholar.org/CorpusID:52922363.
- Philip Bachman, R Devon Hjelm, and William Buchwalter. Learning representations by maximizing mutual information across views. *Advances in neural information processing systems*, 32, 2019.
- 551 Stephen Boyd and Lieven Vandenberghe. *Convex optimization*. Cambridge university press, 2004.
- Yuanzhouhan Cao, Zifeng Wu, and Chunhua Shen. Estimating depth from monocular images as classification using deep fully convolutional residual networks. *IEEE Transactions on Circuits and Systems for Video Technology*, 28(11):3174–3182, 2018. doi: 10.1109/TCSVT.2017. 2740321.
- Honglie Chen, Weidi Xie, Andrea Vedaldi, and Andrew Zisserman. Vggsound: A large-scale audio visual dataset. ICASSP 2020 2020 IEEE International Conference on Acoustics, Speech and
   Signal Processing (ICASSP), pp. 721–725, 2020. URL https://api.semanticscholar.
   org/CorpusID:216522760.
- Ke Chen, Xingjian Du, Bilei Zhu, Zejun Ma, Taylor Berg-Kirkpatrick, and Shlomo Dubnov. Htsat: A hierarchical token-semantic audio transformer for sound classification and detection. In *ICASSP 2022-2022 IEEE International Conference on Acoustics, Speech and Signal Processing*(*ICASSP*), pp. 646–650. IEEE, 2022.
  - Mehdi Cherti, Romain Beaumont, Ross Wightman, Mitchell Wortsman, Gabriel Ilharco, Cade Gordon, Christoph Schuhmann, Ludwig Schmidt, and Jenia Jitsev. Reproducible scaling laws for contrastive language-image learning. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pp. 2818–2829, 2023.
- Aayush Dhakal, Subash Khanal, Srikumar Sastry, Adeel Ahmad, and Nathan Jacobs. Geobind:
   Binding text, image, and audio through satellite images. *arXiv preprint arXiv:2404.11720*, 2024.
- 572 M.P. do Carmo. Differential Geometry of Curves and Surfaces: Revised and Updated Second Edi-573 tion. Dover Books on Mathematics. Dover Publications, 2016. ISBN 9780486806990. URL 574 https://books.google.com/books?id=uXF6DQAAQBAJ.
- Konstantinos Drossos, Samuel Lipping, and Tuomas Virtanen. Clotho: an audio captioning dataset. *ICASSP 2020 - 2020 IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)*, pp. 736–740, 2019. URL https://api.semanticscholar.org/CorpusID:204800739.
- Simon Du, Jason Lee, Haochuan Li, Liwei Wang, and Xiyu Zhai. Gradient descent finds global minima of deep neural networks. In Kamalika Chaudhuri and Ruslan Salakhutdinov (eds.), Proceedings of the 36th International Conference on Machine Learning, volume 97 of Proceedings of Machine Learning Research, pp. 1675–1685. PMLR, 09–15 Jun 2019. URL https: //proceedings.mlr.press/v97/dul9c.html.
- Benjamin Elizalde, Soham Deshmukh, Mahmoud Al Ismail, and Huaming Wang. Clap learning
  audio concepts from natural language supervision. In *ICASSP 2023-2023 IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)*, pp. 1–5. IEEE, 2023.
- Han Fang, Pengfei Xiong, Luhui Xu, and Yu Chen. Clip2video: Mastering video-text retrieval via image clip. ArXiv, abs/2106.11097, 2021. URL https://api.semanticscholar.org/ CorpusID:235490558.
- Yuan Gao, Sangwook Kim, David E Austin, and Chris McIntosh. Medbind: Unifying language and
   multimodal medical data embeddings. ArXiv, abs/2403.12894, 2024. URL https://api.
   semanticscholar.org/CorpusID:268532501.

607

608

609

614

622

630 631

632

633

634

635

- Jort F. Gemmeke, Daniel P. W. Ellis, Dylan Freedman, Aren Jansen, Wade Lawrence, R. Channing
   Moore, Manoj Plakal, and Marvin Ritter. Audio set: An ontology and human-labeled dataset for
   audio events. In *Proc. IEEE ICASSP 2017*, New Orleans, LA, 2017.
- Behrooz Ghorbani, Shankar Krishnan, and Ying Xiao. An investigation into neural net optimization via hessian eigenvalue density. In Kamalika Chaudhuri and Ruslan Salakhutdinov (eds.), Proceedings of the 36th International Conference on Machine Learning, volume 97 of Proceedings of Machine Learning Research, pp. 2232-2241. PMLR, 09-15 Jun 2019. URL https://proceedings.mlr.press/v97/ghorbani19b.html.
- Rohit Girdhar, Mannat Singh, Nikhila Ravi, Laurens Van Der Maaten, Armand Joulin, and Ishan
   Misra. Omnivore: A single model for many visual modalities. In *Proceedings of the IEEE/CVF conference on computer vision and pattern recognition*, pp. 16102–16112, 2022.
  - Rohit Girdhar, Alaaeldin El-Nouby, Zhuang Liu, Mannat Singh, Kalyan Vasudev Alwala, Armand Joulin, and Ishan Misra. Imagebind: One embedding space to bind them all, 2023. URL https://arxiv.org/abs/2305.05665.
- Michael Gutmann and Aapo Hyvärinen. Noise-contrastive estimation: A new estimation principle
   for unnormalized statistical models. In *Proceedings of the thirteenth international conference on artificial intelligence and statistics*, pp. 297–304. JMLR Workshop and Conference Proceedings, 2010.
- Andrey Guzhov, Federico Raue, Jörn Hees, and Andreas Dengel. Audioclip: Extending clip to image, text and audio, 2021. URL https://arxiv.org/abs/2106.13043.
- Jiaming Han, Renrui Zhang, Wenqi Shao, Peng Gao, Peng Xu, Han Xiao, Kaipeng Zhang, Chris Liu, Song Wen, Ziyu Guo, Xudong Lu, Shuai Ren, Yafei Wen, Xiaoxin Chen, Xiangyu Yue, Hongsheng Li, and Yu Jiao Qiao. Imagebind-Ilm: Multi-modality instruction tuning. ArXiv, abs/2309.03905, 2023. URL https://api.semanticscholar.org/ CorpusID:261582620.
- Kaiming He, X. Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition.
   2016 IEEE Conference on Computer Vision and Pattern Recognition (CVPR), pp. 770–778, 2015.
   URL https://api.semanticscholar.org/CorpusID:206594692.
- Kaiming He, Haoqi Fan, Yuxin Wu, Saining Xie, and Ross Girshick. Momentum contrast for unsupervised visual representation learning. In *Proceedings of the IEEE/CVF conference on computer vision and pattern recognition*, pp. 9729–9738, 2020.
  - Roger A Horn and Charles R Johnson. *Matrix analysis*. Cambridge university press, 2012.
  - Xinyu Jia, Chuang Zhu, Minzhen Li, Wenqi Tang, and Wenli Zhou. Llvip: A visible-infrared paired dataset for low-light vision. 2021 IEEE/CVF International Conference on Computer Vision Workshops (ICCVW), pp. 3489–3497, 2021. URL https://api.semanticscholar. org/CorpusID:237278539.
- Andrej Karpathy, George Toderici, Sanketh Shetty, Thomas Leung, Rahul Sukthankar, and Li Fei Fei. Large-scale video classification with convolutional neural networks. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, June 2014.
- Evangelos Kazakos, Arsha Nagrani, Andrew Zisserman, and Dima Damen. Slow-fast auditory streams for audio recognition. In *ICASSP 2021-2021 IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)*, pp. 855–859. IEEE, 2021.
- Chris Dongjoo Kim, Byeongchang Kim, Hyunmin Lee, and Gunhee Kim. AudioCaps: Generating captions for audios in the wild. In Jill Burstein, Christy Doran, and Thamar Solorio (eds.),
   *Proceedings of the 2019 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, Volume 1 (Long and Short Papers)*, pp. 119–132, Minneapolis, Minnesota, June 2019. Association for Computational Linguistics. doi: 10.18653/v1/N19-1011. URL https://aclanthology.org/N19-1011.

648 649 650	Diederik P. Kingma and Jimmy Ba. Adam: A method for stochastic optimization. <i>CoRR</i> , abs/1412.6980, 2014. URL https://api.semanticscholar.org/CorpusID: 6628106.
651 652 653	Diederik P. Kingma and Max Welling. Auto-encoding variational bayes. <i>CoRR</i> , abs/1312.6114, 2013. URL https://api.semanticscholar.org/CorpusID:216078090.
654 655	Khaled Koutini, Jan Schlüter, Hamid Eghbal-Zadeh, and Gerhard Widmer. Efficient training of audio transformers with patchout. <i>arXiv preprint arXiv:2110.05069</i> , 2021.
656 657 658	Yann LeCun, Léon Bottou, Yoshua Bengio, and Patrick Haffner. Gradient-based learning applied to document recognition. <i>Proceedings of the IEEE</i> , 86(11):2278–2324, 1998.
659 660 661	Victor Weixin Liang, Yuhui Zhang, Yongchan Kwon, Serena Yeung, and James Y Zou. Mind the gap: Understanding the modality gap in multi-modal contrastive representation learning. <i>Advances in Neural Information Processing Systems</i> , 35:17612–17625, 2022.
662 663 664 665 666	Minghua Liu, Ruoxi Shi, Kaiming Kuang, Yinhao Zhu, Xuanlin Li, Shizhong Han, H. Cai, Fatih Murat Porikli, and Hao Su. Openshape: Scaling up 3d shape representation to- wards open-world understanding. <i>ArXiv</i> , abs/2305.10764, 2023. URL https://api. semanticscholar.org/CorpusID:258762826.
667 668 669	Ze Liu, Yutong Lin, Yue Cao, Han Hu, Yixuan Wei, Zheng Zhang, Stephen Lin, and Baining Guo. Swin transformer: Hierarchical vision transformer using shifted windows. In <i>Proceedings of the</i> <i>IEEE/CVF international conference on computer vision</i> , pp. 10012–10022, 2021.
670 671	Lajanugen Logeswaran and Honglak Lee. An efficient framework for learning sentence representa- tions. <i>arXiv preprint arXiv:1803.02893</i> , 2018.
672 673 674	Zhou Lu. A theory of multimodal learning. ArXiv, abs/2309.12458, 2023. URL https://api.semanticscholar.org/CorpusID:262217483.
675 676 677	Huaishao Luo, Lei Ji, Ming Zhong, Yang Chen, Wen Lei, Nan Duan, and Tianrui Li. Clip4clip: An empirical study of clip for end to end video clip retrieval and captioning. <i>Neurocomputing</i> , 508: 293–304, 2022.
678 679 680	Yuanhuiyi Lyu, Xu Zheng, Jiazhou Zhou, and Lin Wang. Unibind: Llm-augmented unified and balanced representation space to bind them all. In <i>Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition</i> , pp. 26752–26762, 2024.
681 682 683 684	Charles H. Martin and Michael W. Mahoney. Implicit self-regularization in deep neural networks: Evidence from random matrix theory and implications for learning. <i>Journal of Machine Learning</i> <i>Research</i> , 22(165):1–73, 2021. URL http://jmlr.org/papers/v22/20-410.html.
685 686 687 688	Antoine Miech, Jean-Baptiste Alayrac, Lucas Smaira, Ivan Laptev, Josef Sivic, and Andrew Zisserman. End-to-end learning of visual representations from uncurated instructional videos. In <i>Proceedings of the IEEE/CVF conference on computer vision and pattern recognition</i> , pp. 9879–9889, 2020.
689 690 691 692 693	Niluthpol Chowdhury Mithun, Juncheng Li, Florian Metze, and Amit K. Roy-Chowdhury. Learning joint embedding with multimodal cues for cross-modal video-text retrieval. In <i>Proceedings of the 2018 ACM on International Conference on Multimedia Retrieval</i> , ICMR '18, pp. 19–27, New York, NY, USA, 2018. Association for Computing Machinery. ISBN 9781450350464. doi: 10. 1145/3206025.3206064. URL https://doi.org/10.1145/3206025.3206064.
694 695 696 697 698	Seungwhan Moon, Andrea Madotto, Zhaojiang Lin, Alireza Dirafzoon, Aparajita Saraf, Amy Bearman, and Babak Damavandi. Imu2clip: Multimodal contrastive learning for imu mo- tion sensors from egocentric videos and text. <i>ArXiv</i> , abs/2210.14395, 2022. URL https: //api.semanticscholar.org/CorpusID:253117171.
699 700 701	Arsha Nagrani, Paul Hongsuck Seo, Bryan Seybold, Anja Hauth, Santiago Manén, Chen Sun, and Cordelia Schmid. Learning audio-video modalities from image captions. In <i>European Conference on Computer Vision</i> , 2022. URL https://api.semanticscholar.org/CorpusID: 247939759.

702 Pushmeet Kohli Nathan Silberman, Derek Hoiem and Rob Fergus. Indoor segmentation and support 703 inference from rgbd images. In ECCV, 2012. 704 705 Andreea-Maria Oncescu, A Koepke, Joao F Henriques, Zeynep Akata, and Samuel Albanie. Audio retrieval with natural language queries. arXiv preprint arXiv:2105.02192, 2021. 706 707 Achraf Oussidi and Azeddine Elhassouny. Deep generative models: Survey. In 2018 International 708 conference on intelligent systems and computer vision (ISCV), pp. 1-8. IEEE, 2018. 709 Karol J. Piczak. Esc: Dataset for environmental sound classification. Proceedings of the 23rd ACM 710 international conference on Multimedia, 2015. URL https://api.semanticscholar. 711 org/CorpusID:17567398. 712 713 Alec Radford, Jong Wook Kim, Chris Hallacy, Aditya Ramesh, Gabriel Goh, Sandhini Agar-714 wal, Girish Sastry, Amanda Askell, Pamela Mishkin, Jack Clark, Gretchen Krueger, and Ilya 715 Sutskever. Learning transferable visual models from natural language supervision, 2021. URL 716 https://arxiv.org/abs/2103.00020. 717 Aditya Ramesh, Prafulla Dhariwal, Alex Nichol, Casey Chu, and Mark Chen. Hierarchical text-718 conditional image generation with clip latents. ArXiv, abs/2204.06125, 2022. URL https: 719 //api.semanticscholar.org/CorpusID:248097655. 720 Sebastian Ruder. An overview of gradient descent optimization algorithms. arXiv preprint 721 arXiv:1609.04747, 2016. 722 723 W. Rudin. Principles of Mathematical Analysis. International series in pure and applied mathemat-724 ics. McGraw-Hill, 1976. ISBN 9780070856134. URL https://books.google.com.sg/ 725 books?id=kwqzPAAACAAJ. 726 Olga Russakovsky, Jia Deng, Hao Su, Jonathan Krause, Sanjeev Satheesh, Sean Ma, Zhiheng 727 Huang, Andrej Karpathy, Aditya Khosla, Michael Bernstein, Alexander C. Berg, and Li Fei-Fei. 728 ImageNet Large Scale Visual Recognition Challenge. International Journal of Computer Vision 729 (IJCV), 115(3):211–252, 2015. doi: 10.1007/s11263-015-0816-y. 730 731 Shuran Song, Samuel P Lichtenberg, and Jianxiong Xiao. Sun rgb-d: A rgb-d scene understand-732 ing benchmark suite. In Proceedings of the IEEE conference on computer vision and pattern recognition, pp. 567–576, 2015. 733 734 Alex Tamkin, Mike Wu, and Noah D. Goodman. Viewmaker networks: Learning views for 735 unsupervised representation learning. ArXiv, abs/2010.07432, 2020. URL https://api. 736 semanticscholar.org/CorpusID:222381644. 737 Yapeng Tian, Jing Shi, Bochen Li, Zhiyao Duan, and Chenliang Xu. Audio-visual event localization 738 in unconstrained videos. In ECCV, 2018. 739 740 Yonglong Tian, Dilip Krishnan, and Phillip Isola. Contrastive multiview coding. In Computer 741 Vision–ECCV 2020: 16th European Conference, Glasgow, UK, August 23–28, 2020, Proceedings, 742 Part XI 16, pp. 776–794. Springer, 2020. 743 Aäron van den Oord, Yazhe Li, and Oriol Vinyals. Representation learning with contrastive predic-744 tive coding. ArXiv, abs/1807.03748, 2018. URL https://api.semanticscholar.org/ 745 CorpusID:49670925. 746 747 Jianhua Wang, Chuanxia Zheng, Weihai Chen, and Xingming Wu. Learning aggregated features 748 and optimizing model for semantic labeling. The Visual Computer, 33:1587–1600, 2017. 749 Peng Wang, Shijie Wang, Junyang Lin, Shuai Bai, Xiaohuan Zhou, Jingren Zhou, Xinggang Wang, 750 and Chang Zhou. One-peace: Exploring one general representation model toward unlimited 751 modalities. ArXiv, abs/2305.11172, 2023a. URL https://api.semanticscholar.org/ 752 CorpusID:258762390. 753 Tongzhou Wang and Phillip Isola. Understanding contrastive representation learning through align-754 ment and uniformity on the hypersphere. In International Conference on Machine Learning, 755 2020. URL https://api.semanticscholar.org/CorpusID:218718310.

756	Zehan Wang, Yang Zhao, Xize Cheng, Haifeng Huang, Jiageng Liu, Lilian H. Y. Tang, Lin
757	Li, Yongqiang Wang, Aoxiong Yin, Ziang Zhang, and Zhou Zhao. Connecting multi-
758	modal contrastive representations. ArXiv, abs/2305.14381, 2023b. URL https://api.
759	semanticscholar.org/CorpusID:258866011.

- 760 Zehan Wang, Ziang Zhang, Xize Cheng, Rongjie Huang, Luping Liu, Zhenhui Ye, Haifeng Huang, 761 Yang Zhao, Tao Jin, Peng Gao, and Zhou Zhao. Freebind: Free lunch in unified multi-762 modal space via knowledge fusion. ArXiv, abs/2405.04883, 2024a. URL https://api. 763 semanticscholar.org/CorpusID:269626610. 764
- 765 Zehan Wang, Ziang Zhang, Hang Zhang, Luping Liu, Rongjie Huang, Xize Cheng, Hengshuang Zhao, and Zhou Zhao. Omnibind: Large-scale omni multimodal representation via binding 766 spaces. arXiv preprint arXiv:2407.11895, 2024b. 767
- 768 Ho-Hsiang Wu, Prem Seetharaman, Kundan Kumar, and Juan Pablo Bello. Wav2clip: Learning 769 robust audio representations from clip. ICASSP 2022 - 2022 IEEE International Conference 770 on Acoustics, Speech and Signal Processing (ICASSP), pp. 4563–4567, 2021. URL https: 771 //api.semanticscholar.org/CorpusID:239616434.
- Jiayang Wu, Wensheng Gan, Zefeng Chen, Shicheng Wan, and S Yu Philip. Multimodal large 773 language models: A survey. In 2023 IEEE International Conference on Big Data (BigData), pp. 774 2247-2256. IEEE, 2023. 775
- 776 Yusong Wu, K. Chen, Tianyu Zhang, Yuchen Hui, Taylor Berg-Kirkpatrick, and Shlomo Dubnov. 777 Large-scale contrastive language-audio pretraining with feature fusion and keyword-to-caption 778 augmentation. ICASSP 2023 - 2023 IEEE International Conference on Acoustics, Speech and Sig-779 nal Processing (ICASSP), pp. 1-5, 2022. URL https://api.semanticscholar.org/ CorpusID:253510826. 780
- 781 Peng Xu, Xiatian Zhu, and David A Clifton. Multimodal learning with transformers: A survey. 782 IEEE Transactions on Pattern Analysis and Machine Intelligence, 45(10):12113–12132, 2023. 783
- Fengyu Yang, Chao Feng, Daniel Wang, Tianye Wang, Ziyao Zeng, Zhiyang Xu, Hyoungseob 784 Park, Pengliang Ji, Hanbin Zhao, Yuanning Li, and Alex Wong. Neurobind: Towards unified 785 multimodal representations for neural signals. ArXiv, abs/2407.14020, 2024. URL https: 786 //api.semanticscholar.org/CorpusID:271310533. 787
- 788 Shukang Yin, Chaoyou Fu, Sirui Zhao, Ke Li, Xing Sun, Tong Xu, and Enhong Chen. A survey on 789 multimodal large language models. arXiv preprint arXiv:2306.13549, 2023.
- Bin Zhu, Bin Lin, Munan Ning, Yang Yan, Jiaxi Cui, HongFa Wang, Yatian Pang, Wenhao Jiang, Junwu Zhang, Zongwei Li, Wancai Zhang, Zhifeng Li, Wei Liu, and Li Yuan. Languagebind: Ex-792 tending video-language pretraining to n-modality by language-based semantic alignment, 2024. 793 URL https://arxiv.org/abs/2310.01852. 794
- 796

791

772

- 797 798
- 799
- 800 801

802

- 803 804
- 805

- 808
- 809

# A Additional Theoretical Analysis

# A.1 PROOF OF THEOREM1813

 *Proof.* First, we apply the chain rule to get the gradient of  $\mathcal{L}^{tan}$  with respect to the parameter  $\Theta$ :

$$\frac{\partial \mathcal{L}^{\text{tan}}}{\partial \Theta} = \frac{\partial x_i^b}{\partial \Theta} \frac{\partial T_{\bar{c}_i}(x_i^b)}{\partial x_i^b} \frac{\partial \mathcal{L}^{\text{tan}}}{\partial T_{\bar{c}_i}(x_i^b)}.$$
(12)

Similarly, using the chain rule to calculate the gradient of  $\mathcal{L}_{align}$  with respect to  $\Theta$ , we get  $\frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} = \frac{\partial x_i^b}{\partial x_i^b} \frac{\partial \mathcal{L}^{\text{tan}}}{\partial x_i^b}$ . Substituting  $\frac{\partial \mathcal{L}^{\text{tan}}}{\partial x_i^b}$  with  $\bar{c}_i$  according to equation.5, we get

$$\frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} = -\frac{\partial x_i^b}{\partial \Theta} \bar{c}_i. \tag{13}$$

Take the inner product  $\frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} + \lambda \frac{\partial \mathcal{L}^{\text{an}}}{\partial \Theta}$  and  $\frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta}$  to get formula.14.

$$\left(\frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} + \lambda \frac{\partial \mathcal{L}^{\text{tan}}}{\partial \Theta}\right)^{T} \frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} = \bar{c}_{i}^{T} \frac{\partial x_{i}^{b}}{\partial \Theta}^{T} \frac{\partial x_{i}^{b}}{\partial \Theta} \bar{c}_{i} + \lambda \frac{\partial \mathcal{L}^{\text{tan}}}{\partial T_{\bar{c}_{i}}(x_{i}^{b})}^{T} \frac{\partial T_{\bar{c}_{i}}(x_{i}^{b})}{\partial x_{i}^{b}}^{T} \frac{\partial x_{i}^{b}}{\partial \Theta} \bar{c}_{i}, \quad (14)$$

Notably, we expand  $\frac{\partial T_{\bar{c}_i}(x_i^b)}{\partial x_i^b}$  as in equation.15, and find that  $\bar{c}_i^T \frac{\partial T_{\bar{c}_i}(x_i^b)}{\partial x_i^b} = 0$  due to  $\bar{c}_i^T \left(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}\right) = 0.$ 

$$\frac{\partial T_{\bar{c}_i}(x_i^b)}{\partial x_i^b} = \frac{\partial \left(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}\right) x_i^b}{\partial x_i^b} \frac{\partial T_{\bar{c}_i}(x_i^b)}{\partial \left(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}\right) x_i^b} = \left(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}\right) \frac{\partial T_{\bar{c}_i}(x_i^b)}{\partial \left(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}\right) x_i^b}.$$
 (15)

Next, we introduce Lemma.2

**Lemma 2.** We have  $x^T A^T A y \ge -(\kappa (A^T A) - 1)^{\frac{1}{2}} ||Ay||^2 \frac{||x||}{||y||}$ , if  $y^T x = 0$  and  $\kappa(\cdot)$  is condistion number.

*Proof.* Rather than proving this inequality directly, we turn to the follow the lower bound for the optimization problem.16.

$$\begin{array}{ll} \min_{x} & x^{T}A^{T}Ay, \\ \text{subject to} & y^{T}x = 0, \\ & x^{T}x = 1, \end{array} \tag{16}$$

To solve optimization problem16, we write the Lagrangian function in 17,

$$L(x,\mu_1,\mu_2) = x^T A^T A y + \mu_1 x^T y + \mu_2 (x^T x - 1).$$
(17)

We can easily get the Lagrangian dual function 18 form 17,

$$L(\mu_1, \mu_2) = \inf_x L(x, \mu_1, \mu_2) = -\frac{\|(A^T A - \mu_1 I)y\|^2}{4\mu_2} - \mu_2,$$
(18)

Thus, we obtain the unconstrained Lagrangian dual problem 19

$$\max_{\mu_1,\mu_2} L(\mu_1,\mu_2). \tag{19}$$

Besides, we have

$$\max_{\mu_2} L(\mu_1, \mu_2) = \| (A^T A - \mu_1 I) y \| = \left( \mu_1^2 y^T y - 2\mu_1 y^T A^T A y + y^T A^T A A^T A y \right)^{\frac{1}{2}}.$$
 (20)

Thus, we get

$$\max_{\mu_1,\mu_2} L(\mu_1,\mu_2) = \max_{\mu_1} \max_{\mu_2} L(\mu_1,\mu_2) = -\frac{\left(\|A^T A y\|^2 \|y\|^2 - \|Ay\|^4\right)^{\frac{1}{2}}}{\|y\|}.$$
 (21)

Since the maximum eigenvalue of  $A^T A$  divided by the minimum eigenvalue of  $A^T A$  is less than 2, we have

$$\|A^{T}Ay\|^{2}\|y\|^{2} \leq \|A\|^{2}\|Ay\|^{2}\|y\|^{2} = \|Ay\|^{4}\frac{\|A\|^{2}\|y\|^{2}}{\|Ay\|^{2}} \leq \kappa(A^{T}A)\|Ay\|^{4}.$$
 (22)

After that, according to 21 and 22, we have

$$\max_{\mu_1,\mu_2} L(\mu_1,\mu_2) \ge -(\kappa(A^T A) - 1)^{\frac{1}{2}} \frac{\|Ay\|^2}{\|y\|}.$$
(23)

According to the duality principle (Boyd & Vandenberghe, 2004), we have  $\frac{x^T}{\|x\|}A^TAy \ge -(\kappa(A^TA)-1)^{\frac{1}{2}}\frac{\|Ay\|^2}{\|y\|}$  which completes the proof.

According to Martin & Mahoney (2021); Arora et al. (2018); Du et al. (2019); Ghorbani et al. (2019),  $\kappa \left(\frac{\partial x_i^b}{\partial \Theta} \frac{\partial x_i^b}{\partial \Theta}\right)$  will converge and less than 2. Consider  $\frac{\partial T_{\bar{c}_i}(x_i^b)}{\partial x_i^b} \frac{\partial \mathcal{L}^{un}}{\partial T_{\bar{c}_i}(x_i^b)}, \bar{c}_i$  and  $\frac{\partial x_i^b}{\partial \Theta}$  as x, y, and A in Lemma.2, respectively. According to Lemma.2, we can get inequality.24

$$\left(\frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} + \lambda \frac{\partial \mathcal{L}^{\text{tan}}}{\partial \Theta}\right)^{T} \frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} \ge \left\|\frac{\partial x_{i}^{b}}{\partial \Theta} \bar{c}_{i}\right\|^{2} \left(1 - \lambda \frac{\left\|\frac{\partial T_{\bar{c}_{i}}(x_{i}^{b})}{\partial x_{i}^{b}} \frac{\partial \mathcal{L}^{\text{tan}}}{\partial T_{\bar{c}_{i}}(x_{i}^{b})}\right\|}{\left\|\bar{c}_{i}\right\|}\right).$$
(24)

Moreover, expanding  $\frac{\partial T_{\bar{e}_i}(x_i^b)}{\partial (I - \frac{\bar{e}_i \bar{e}_i^T}{\|\bar{e}_i\|^2}) x_i^b}$  in equation.15 we have

$$\frac{\partial T_{\bar{c}_i}(x_i^b)}{\partial (I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}) x_i^b} = I - \frac{(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}) x_i^b \left( (I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}) x_i^b \right)^T}{\|(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}) x_i^b\|^2}.$$
(25)

Furthermore, we find  $(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2})$  and  $\frac{\partial T_{\bar{c}_i}(x_i^b)}{\partial (I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2})x_i^b}$  are both projection matrix (Horn & Johnson,

2012), and both spectral radius are less than 1. Thus, we have

$$\left|\frac{\partial T_{\bar{c}_i}(x_i^b)}{\partial x_i^b}\frac{\partial \mathcal{L}^{\mathrm{tan}}}{\partial T_{\bar{c}_i}(x_i^b)}\right\| \le \left\|\frac{\partial \mathcal{L}^{\mathrm{tan}}}{\partial T_{\bar{c}_i}(x_i^b)}\right\|,\tag{26}$$

due to the spectral radius of  $\frac{\partial T_{\bar{e}_i}(x_i^b)}{\partial x_i^b}$  is less than 1. Thus, according to inequality .24 and 26, we have

$$\left(\frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} + \lambda \frac{\partial \mathcal{L}^{\text{tan}}}{\partial \Theta}\right)^{T} \frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} \ge \left\|\frac{\partial x_{i}^{b}}{\partial \Theta} \bar{c}_{i}\right\|^{2} \left(1 - \lambda \frac{\left\|\frac{\partial \mathcal{L}^{\text{sum}}}{\partial T_{\bar{c}_{i}}(x_{i}^{b})}\right\|}{\left\|\bar{c}_{i}\right\|}\right),\tag{27}$$

which means  $\left(\frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} + \lambda \frac{\partial \mathcal{L}^{\text{tan}}}{\partial \Theta}\right)^T \frac{\partial \mathcal{L}^{\text{align}}}{\partial \Theta} \ge 0$  when  $\lambda \le \frac{\|\bar{c}_i\|}{\|\frac{\partial \mathcal{L}^{\text{lan}}}{\partial T_{\bar{c}_i}(x_i^b)}\|}$  and complete the proof.  $\Box$ 

#### A.2 INFONCE VS. TANGENTTERM

In this section, we roughly analyze why directly using infoNCE to align with generative embeddings results in a degradation of the core modal alignment capability. For ease of understanding, we consider the case where similarity function is cosine similarity and  $\tau = 1$ . As analyzed in Sec.3.2,  $\mathcal{L}^{tan}$  aligns the two modes, while  $\mathcal{L}^{uniform}$  just plays a role of regular term. Thus, the align parts of the two infoNCEs are added together and we get

$$\mathcal{L}^{\text{align}}(\hat{x}_{i}^{a}, x_{i}^{b}) + \mathcal{L}^{\text{align}}(c_{i}, x_{i}^{b}) = -(\hat{x}_{i}^{a})^{T} x_{i}^{b} - c_{i}^{T} x_{i}^{b} = -(\hat{x}_{i}^{a} + c_{i})^{T} x_{i}^{b},$$
(28)

which means that when  $x_i^b$  is neither aligned with  $c_i$  nor with  $\hat{x}_i^a$ , but instead with normalize  $(\hat{x}_i^a + c_i)$ . As a result, the ability to align with the core modality is destroyed. However, if we use **Tangent Term** instead of infoNCE, then the loss function for the alignment part becomes

$$\mathcal{L}^{\text{align}} = -c_i^T x_i^b - (\hat{x}_i^a)^T \text{normalize}((I - \frac{c_i c_i^T}{\|c_i\|^2}) x_i^b).$$
(29)

It is worth noting that to simplify the notation, we still use  $\mathcal{L}^{\text{align}}$  in equation.29, where there is a slight difference between equation.29 and equation.3. Letting  $\mathcal{L}^{\text{align}}$  take the derivative of  $x_i^b$ , we get

$$\frac{\partial \mathcal{L}^{\text{align}}}{\partial x_i^b} = -c_i - (I - \frac{x_i^b(x_i^b)^T}{\|x_i^b\|^2})(I - \frac{c_i c_i^T}{\|c_i\|^2})(I - \frac{(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2})x_i^b \left((I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2})x_i^b\right)^T}{\|(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2})x_i^b\|^2})\hat{x}_i^a.$$
(30)

Since  $x_i^b$  is confined to the hypersphere,  $(I - \frac{x_i^b(x_i^b)^T}{\|x_i^b\|^2})$  appears in equation.30. Taking an inner product of  $c_i$  and  $\frac{\partial \mathcal{L}^{\text{align}}}{\partial x_i^b}$ , we have

$$c_{i}^{T} \frac{\partial \mathcal{L}^{\text{align}}}{\partial x_{i}^{b}} = -c_{i}^{T} c_{i} - c_{i}^{T} (I - \frac{x_{i}^{b} (x_{i}^{b})^{T}}{\|x_{i}^{b}\|^{2}}) (I - \frac{c_{i} c_{i}^{T}}{\|c_{i}\|^{2}}) (I - \frac{(I - \frac{\bar{c}_{i} \bar{c}_{i}^{T}}{\|\bar{c}_{i}\|^{2}}) x_{i}^{b} \left((I - \frac{\bar{c}_{i} \bar{c}_{i}^{T}}{\|\bar{c}_{i}\|^{2}}) x_{i}^{b}\right)^{T}}{\|(I - \frac{\bar{c}_{i} \bar{c}_{i}^{T}}{\|\bar{c}_{i}\|^{2}}) x_{i}^{b}\|^{2}}) \hat{x}_{i}^{a}.$$
(31)

It is easy to find that

$$c_i^T (I - \frac{x_i^b (x_i^b)^T}{\|x_i^b\|^2}) = c_i^T - \frac{c_i^T x_i^b}{\|x_i^b\|^2} (x_i^b)^T,$$
(32)

where

$$c_i^T (I - \frac{c_i c_i^T}{\|c_i\|^2}) = 0, (33)$$

T

and

$$\frac{c_i^T x_i^b}{\|x_i^b\|^2} \left( (x_i^b)^T (I - \frac{c_i c_i^T}{\|c_i\|^2}) \right) (I - \frac{(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}) x_i^b \left( (I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}) x_i^b \right)^T}{\|(I - \frac{\bar{c}_i \bar{c}_i^T}{\|\bar{c}_i\|^2}) x_i^b\|^2} \right) = 0.$$
(34)

Thus, we have

$$c_i^T \frac{\partial \mathcal{L}^{\text{align}}}{\partial x_i^b} = -c_i^T c_i \le 0, \tag{35}$$

which means that the similarity between  $x_i^b$  and  $c_i$  is on increase.

## **B** DOWNSTREAM DATASETS

AudioSet (Gemmeke et al., 2017) contains 10s videos from YouTube annotated into 527 classes. It consists of the following: a balanced subset containing about 20,000 videos, a test subset contain-ing 18,000 videos, and an unbalanced training subset containing about 2 million videos. In image and text core modality training, we use the balanced set of 16,000 for audio-video and audio-text alignment respectively. For the zero-shot evaluation in Table.1, we use the test set and compute logits for each class using textual class names. 16,000 data pairs are used for training. During the text core modality model training and zero-shot evaluation we use prompt templates for class names as described later in Appendix.C.1. The metric used is mAP.

957AudioCaps(Kim et al., 2019) is a dataset of audio-visual clips from YouTube with textual descrip-958tions. It consists of clips from the AudioSet dataset. Following ImageBind, we used the splitting959method provided in Oncescu et al. (2021) to remove clips that overlap with the VGGSound dataset.960We obtain 48,198 training segments, 418 validation segments, and 796 test segments. We use only961the test set for zero-shot evaluation of our model. The task is text  $\rightarrow$  audio retrieval and is evaluated962using recall@K.

963
964
964
965
965
966
966
967
967
967
963
964
964
965
965
965
966
967
967
967
967
968
969
969
969
960
960
960
960
960
961
961
962
962
963
964
964
964
965
965
965
966
967
967
967
967
967
967
967
967
968
969
969
969
969
960
960
960
960
961
961
962
962
963
964
964
965
965
965
966
966
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
967
968
968
969
969
969
969
969
969
969
960
960
960
960
960
960
960
960
960
960
960
960
960
960
960
960
960
960

968VGG-S(Chen et al., 2020) contains approximately 200,000 video clips of 10 seconds in length an-<br/>notated with 309 sound categories, including human actions, sound-producing objects, and human-<br/>object interactions. We performed zero-shot classification and RGB $\rightarrow$  Audio retrieval using only the<br/>audio from the test set. Evaluations are performed using top-1 accuracy for zero-shot classification<br/>and Recall@K for RGB $\rightarrow$  Audio retrieval.

Config	Audio	Depth	Infrared	
Encoder	ViT-Huge			
Number of Heads	12	8	12	
Optimizer		AdamW	V	
Optimizer Momentum	$\beta_1 =$	$= 0.9, \beta_2$	= 0.95	
Epochs	8	2	2	
Learning rate	5e-4	5e-4	1e-4	
Temperature	0.07	0.2	0.1	
Weight decay	0.2	0.2	0.05	
Batch size	512	256	256	
Learning rate schedule	(	Cosine dec	cay	

Table 6: Training Settings in ImageCore model

AVE (Tian et al., 2018) contains 4,143 YouTube videos across 28 event categories and videos in the AVE dataset that are temporally labeled with audiovisual event boundaries. Evaluations were performed using top-1 accuracy for zero-shot classification and Recall@K for RGB $\rightarrow$  Audio retrieval with the highest accuracy.

Clotho (Drossos et al., 2019) is an audio dataset with textual descriptions from the Freesound 992 platform. It consists of a development set and a test set containing 2893 audio clips and 1045 audio clips respectively, each associated with 5 descriptions. We consider the text  $\rightarrow$  audio retrieval task 994 and treat each of the 5 associated descriptions as a separate test query, which is then retrieved from 995 the set of audio clips. The metric used is recall@K, i.e., a given test query is assumed to be solved correctly if the base fact audio is retrieved in the first K audio clips retrieved. 996

997

987

988

989

990 991

993

972

998 SUN (Song et al., 2015) contains about 10,000 RGB-D images. We follow ImageBind to post 999 process the depth maps in three steps-1) in-filled depth values, 2) convert them to disparity for scale 1000 normalization and 3) limited the minimum and maximum depth to 0.01 and 10 meters respectively. We use training split (about 5,000 data pair) for training models. Specific, for text core modality 1001 model training, we use prompt templates for the class names as described later in Appendix.C.1. 1002

1003

1004 **NYU-D** (Nathan Silberman & Fergus, 2012) is used to evaluation by 80% samples. Through pre-1005 processing, we limited the minimum and maximum depth of the depth images to 0.01 and 10 meters respectively. Following ImageBind, we performed a classification and reorganization process which produced a total of 10 scene categories. For zero-shot evaluation and RGB  $\rightarrow$  Depth retrieval task, 1007 we use top-1 accuracy and Recall@1. We use prompt templates as described later in Appendix.C.1 1008 in RGB  $\rightarrow$  Depth retrieval task. 1009

1010

1011 **LLVIP** (Jia et al., 2021) is an infrared spectral pedestrian object detection dataset. Following 1012 the ImageBind method, we extracted all people in the image and designated all other objects as background elements. This process resulted in a dataset containing 7622 "background" categories 1013 and 7954 "people" categories, which were subsequently used for binary classification tests. About 1014 5,000 Infrared-RGB pairs are used to training. Besides, prompt templates as described later in 1015 Appendix.C.1 is used in zero-shot classification task. Since LLVIP is intended to be used for detect 1016 tasks and each RGB image is not text labeled, we use GPT40 to generate text annotations for each 1017 RGB image during the training process for text core modality.

1018 1019

**Imagenet-1K** Russakovsky et al. (2015) encompasses 1,000 object classes and comprises 1.28M 1020 images for training, 5000 images for validation, and 100,000 images for testing. Building upon 1021 this foundation, Imagenet-1K-VL-Enriched<sup>3</sup> enhances Imagenet-1K dataset by including image 1022 captions, bounding boxes, and corrected label information. Caption & image pairs from Imagenet-1023 1K-VL-Enriched training split are used for training diffusion model. 1024

<sup>1025</sup> 

<sup>&</sup>lt;sup>3</sup>Dataset can be found in https://huggingface.co/datasets/visual-layer/imagenet-1k-vl-enriched

1027				
1028	Config	Audio	Depth	Infrared
1029	Encoder		ViT-Hug	ge
1030	Number of Heads	12	8	12
1031	Optimizer		AdamW	V
1032	Optimizer Momentum	$\beta_1 =$	$= 0.9, \beta_2$	= 0.95
1033	Epochs	8	4	4
	Learning rate	1e-4	5e-4	1e-4
1034	Temperature	0.05	0.2	0.2
1035	Weight decay	0.2	0.1	0.05
1036	Batch size	512	256	256
1037	Learning rate schedule	(	bosine de	cay
1038	e			•

Table 7: Training Settings in LanguageCore model

# 1039

1041

1026

100

# C IMPLEMENTATION DETAILS

We now describe the implementation details used in this work. In table 6 and 7, we detail the settings
used to train each of the modalities. Our experiments were done on 4 24GB 4090 GPUs and 4 48GB
A40 GPUs.

1045

# 1046 C.1 PROMPT TEMPLATES

For all evaluations, we use the default set of templates from CLIP(Radford et al., 2021). It is worth mentioning that we use the same templates for non visual modalities like audio and depth as well since we only use semantic/textual supervision associated with images.

1051 1052

## C.2 MODEL ARCHITECTURE

1053 **Diffusion Model** We deployed two symmetric decode-only diffusion models, one for generating 1054 text embeddings from image embeddings and another for the reverse. Both models use the same 1055 transformer architecture with a 1024-dimensional embedding, 8 attention heads of 128 dimensions 1056 each, and 6 layers and the number of training parameters is about 30M. Training involves 100 1057 timesteps, with a 5% embedding dropout to facilitate classifier-free guidance, optimized using an 1058 AdamW optimizer, a learning rate of 1e-4, and a batch size of 128, following the loss function of 1059 our methodology documentation. For the model where the image is the core modality, the image embedding serves as the input, and the text embedding is the output to generate. Conversely, when text is the core modality, text embedding is used as input to generate the image embedding. This 1061 approach allows us to efficiently handle and transform data within the latent space, reducing com-1062 putational demands. This setup not only ensures the capability of model in cross-modal generation 1063 but also enhances its performance in generating high-quality, contextually accurate outputs across 1064 different modalities.

1066 Multimodal Encoders For image core model and language core model, we use the same structure 1067 of encoder on the same modality. Following Girdhar et al. (2023) we use 12-layer, 1024-dimensional 1068 vision transformer with a patch size of 16 and a stride of 10 for the VISION, AUDIO, DEPTH, and 1069 INFRARED modalities. For video data, our strategy includes capturing two frames every two sec-1070 onds to optimize processing efficiency. Besides, we used 128 mel-spectrogram partitions to convert 1071 2 seconds of audio sampled at 16kHz into a spectrogram. Similarly, thermal and depth images are 1072 treated as single-channel inputs and encoded using the same ViT architecture, facilitating consistent 1073 handling across these modalities. The encoders for both the image and language core models are 1074 initialized with weights from the ImageBind-Huge and LanguageBind pre-trained models respectively for enhancing learning efficiency and demonstrating the transferability of our TangentBind 1075 approach. This leverages their advanced pre-trained features to accelerate convergence and improve 1076 generalization across varied multimodal applications. 1077

- 1078
- **Temperature** Tangent Term 6 and infoNCE 2 use the same temperature  $\tau$  during training for encoder of the same modality. In our experiments, we found that fixed temperatures worked best by

comparing learnable and fixed temperatures. The experiments show the temperature with the best effect for each modality in table.6 and .7.

1082 1083 1084

1086

## **1085** C.3 ABLATION DETAILS

**ResNet** We employed the standard ResNet50(He et al., 2015) architecture provided by PyTorch. 1087 The ResNet50 model has a nearly number of training parameters with the diffusion model employed, 1088 suggesting that both architectures share comparable complexity and computational demands, which 1089 allows for an equitable comparison of their performance in analogous tasks. To tailor the model for 1090 our embedding-based task, the output dimension of the final fully connected layer was modified to 1091 produce embeddings with a dimensionality of 1024. These embeddings are subsequently normal-1092 ized to lie on the unit hypersphere to facilitate the use of cosine similarity measures in subsequent 1093 analyses. For training the modified ResNet50, we utilized the L2 loss function, which is well-suited 1094 for embedding normalization by encouraging the model to minimize the Euclidean distance between the predicted and target embeddings. The optimizer of choice was AdamW, the learning rate was 1095 set to 1e-4. The training was conducted with a batch size of 128. Our training procedure mirrored that of the diffusion model in terms of dataset usage; specifically, we trained on the train split of the ImageNet-1K-VL-Enriched dataset. During training, the core modality embeddings were utilized as inputs, while the embeddings of an alternative modality served as labels. 1099

1100

1101 **C-MCR** We employed the C-MCR(Wang et al., 2023b) method to generate cross-modal embeddings, leveraging the training split of the ImageNet-1K-VL-Enriched dataset to obtain paired  $\langle x_i^{\text{Image}}, x_i^{\text{text}} \rangle$  embeddings that serve as image and text memories. This approach is rooted in the framework established by the C-MCR methodology, where embeddings for both modalities are computed based on

$$\hat{x}_{i}^{\text{image}} = \sum_{i=1}^{N} \frac{\exp(\sin(x^{\text{text}}, x_{i}^{\text{image}}))}{\sum_{j=1}^{N} \exp(\sin(x^{\text{text}}, x_{j}^{\text{image}}))} x_{i}^{\text{image}}; \quad \hat{x}_{i}^{\text{text}} = \sum_{i=1}^{N} \frac{\exp(\sin(x^{\text{image}}, x_{i}^{\text{text}}))}{\sum_{j=1}^{N} \exp(\sin(x^{\text{image}}, x_{j}^{\text{text}}))} x_{i}^{\text{text}},$$

$$(36)$$

and subsequently normalize to lie on the unit hypersphere. As illustrated in Figure 6, the CDF curve 1110 corresponding to the C-MCR method approximates a straight line. This outcome primarily arises 1111 due to the SUN dataset, which consists of scene data that does not align well with the ImageNet-1112 1K-VL-Enriched dataset. During our experiments, we observed that whether text or image served as 1113 the core modality, the weights  $\frac{\exp(\sin(x^{\text{text}}, x_i^{\text{image}}))}{\sum_{j=1}^{N} \exp(\sin(x^{\text{text}}, x_j^{\text{image}}))}$  and  $\frac{\exp(\sin(x^{\text{image}}, x_i^{\text{text}}))}{\sum_{j=1}^{N} \exp(\sin(x^{\text{image}}, x_j^{\text{text}}))}$  in (36) assigned to 1114 1115 each embedding from the SUN dataset on the ImageNet1K were minutely different. This minimal 1116 variation led to the generation of nearly identical embeddings for both modalities, hence the nearly linear CDF curve observed. This phenomenon underscores a critical aspect of the C-MCR method: 1117 its strong dependence on the memory. 1118

1119

VAE We implemented a VAE(Kingma & Welling, 2013) where both the encoder and decoder 1120 components are constructed using convolutional neural networks (CNNs)(LeCun et al., 1998). The 1121 architecture of the encoder and decoder are symmetric, each comprising ten layers with the following 1122 input channels of convolutional layers: [32, 32, 64, 64, 128, 128, 256, 256, 512, 512]. This VAE 1123 model possesses a comparable number of training parameters to the diffusion model used, indicating 1124 that both architectures are similarly complex and computationally demanding, facilitating a fair 1125 comparison of their performance across similar tasks. Each convolutional layer is defined with a 1126 kernel size of 3, a stride of 2, and padding of 1. Post convolution, the decoder maps the latent space 1127 representation to embedding with dimensionality of 1024. This representation is then normalized 1128 to lie on the unit hypersphere. The loss function employed is the L2 loss, similar to that used in 1129 ResNet50 architectures, which helps in minimizing the distance between the reconstructed outputs 1130 and the actual inputs, thereby ensuring better fidelity in the generated samples. AdamW optimizer is chosen with a learning rate of 1e-4 and a batch size of 128. Training was conducted using the 1131 training split of the ImageNet-1K-VL-Enriched dataset. In this setup, core modality embeddings 1132 were used as inputs, and embeddings from another modality served as labels. This training approach 1133 not only facilitates effective learning of cross-modal representations but also ensures that the VAE is

1134	
1135	capable of generating high-quality embeddings that are highly representative of the input data across
1136	different modalities.
1137	
1138	
1139	
1140	
1141	
1142	
1143	
1144	
1145	
1146	
1147	
1148	
1149	
1150	
1151	
1152	
1153	
1154	
1155	
1156	
1157	
1158	
1159 1160	
1161	
1162	
1163	
1164	
1165	
1166	
1167	
1168	
1169	
1170	
1171	
1172	
1173	
1174	
1175	
1176	
1177	
1178	
1179	
1180	
1181 1182	
1183	
1184	
1185	
1186	
1187	