

COUNTERFACTUAL GENERATION FROM LANGUAGE MODELS

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ABSTRACT

Understanding and manipulating the causal generation mechanisms in language models is essential for controlling their behavior. Previous work has primarily relied on techniques such as representation surgery—e.g., model ablations or manipulation of linear subspaces tied to specific concepts—to *intervene* on these models. To understand the impact of interventions precisely, it is useful to examine *counterfactuals*—e.g., how a given sentence would have appeared had it been generated by the model following a specific intervention. We highlight that counterfactual reasoning is conceptually distinct from interventions, as articulated in Pearl’s causal hierarchy. Based on this observation, we propose a framework for generating true string counterfactuals by reformulating language models as Generalized Structural equation model using the Gumbel-max trick. This allows us to model the joint distribution over original strings and their counterfactuals resulting from the same instantiation of the sampling noise. We develop an algorithm based on hindsight Gumbel sampling that allows us to infer the latent noise variables and generate counterfactuals of observed strings. Our experiments demonstrate that the approach produces meaningful counterfactuals while at the same time showing that commonly used intervention techniques have considerable undesired side effects.

1 INTRODUCTION

The study of language model (LM) interpretability often borrows terminology from Pearl’s causal calculus (Pearl, 1989), e.g., researchers often talk of *intervening* a model’s parameters and *counterfactually* generating strings. Pearl’s framework distinguishes between three levels of causal reasoning (Shpitser & Pearl, 2008). Association, the first level, pertains to statistical correlations, i.e., observing patterns observed in data without interacting with the world. Intervention, the second level, pertains to actively changing variables in the world and observing their effects at a macro level. Counterfactuality, the third level, pertains to imagining what could have happened if past events had unfolded differently. However, LM literature often uses these three causal terms causally and at times imprecisely—particularly when it comes to counterfactuality, which remains challenging to rigorously define (Feder et al., 2022; Mueller, 2024; Mueller et al., 2024). In this paper, we are given a well-defined notion of counterfactuality in LMs using the framework of structural equation modeling.

Efforts to exert control over LMs have led to substantial research on targeted *interventions* in the models. One such technique is **representation surgery**, which involves modifying an LM’s architecture to manipulate its internal representation space (Lakretz et al., 2019; Vig et al., 2020; Feder et al., 2021; Ravfogel et al., 2021b; Elhage et al., 2021; Elazar et al., 2021; Nanda, 2023; Syed et al., 2023; Kramár et al., 2024; Avitan et al., 2024). The *linear subspace hypothesis* (Bolukbasi et al., 2016; Vargas & Cotterell, 2020; Ravfogel et al., 2022) posits that human-interpretable *concepts*, such as gender or grammatical number, are encoded within specific linear subspaces of the LM’s representation space. This makes it possible to perform precise interventions on these high-level concepts, such as removing the concept’s information by projecting the representations onto the complement of the concept subspace (Ravfogel et al., 2020; 2021a; 2022; 2023; Guerner et al., 2024; Scalena et al., 2024; Singh et al., 2024). These interventions modify the model and allow researchers to examine its behavior after the change. However, while interventions can induce a *change* in the model, they cannot answer counterfactual questions, e.g., what would a given string look like if it had been generated by the model after the intervention?

Counterfactual analysis, as defined by Pearl, is challenging because it requires describing the system of interest through a causal model that enables counterfactual reasoning. In this paper, we address this challenge for LMs by turning to generalized structural equation models (GSEMs; Halpern & Peters, 2022). GSEMs break down the statistical model into *exogenous* variables, which account for latent randomness, and *endogenous* variables, which are deterministic once the exogenous ones are fixed. To frame LMs as GSEMs, we apply the Gumbel-max trick (Gumbel, 1954), which separates the deterministic computation of next-symbol logits from the sampling process.¹

This formulation allows for generating counterfactual strings by sampling from conditional noise distributions, enabling precise analysis of string-level effects from interventions in models like GPT2-XL (Radford et al., 2018) and LLaMA3-8b (Touvron et al., 2023). Despite targeting specific behaviors through interventions such as linear steering (Li et al., 2024; Singh et al., 2024), knowledge editing (Meng et al., 2023), and instruction tuning (Wei et al., 2022), results reveal unintended side effects, e.g., gender-based interventions unexpectedly altering unrelated completions. These findings challenge the goal of achieving *minimal change* and show that even localized parameter modifications can have broader, undesired impacts.

2 LANGUAGE MODELS AS GENERALIZED STRUCTURAL EQUATION MODELS

Let Σ be an **alphabet**—a finite, non-empty set of symbols. A **language model** (LM) is a probability distribution over Σ^* , the set of all strings formed from symbols in Σ . A **language encoder** is a function $\mathbf{h}_\theta: \Sigma^* \rightarrow \mathbb{R}^d$ parameterized by parameters θ that maps strings to d -dimensional vectors (Chan et al., 2024). Representational surgery is performed by intervening on \mathbf{h}_θ . Popular architectures for implementing language encoders include Transformers (Vaswani et al., 2017) and recurrent neural networks (RNNs; Elman, 1990). Language encoders are particularly valuable because under mild conditions (Du et al., 2023, Thm. 4.7), they ensure the model defines a distribution over strings—thus forming an LM—as follows:

$$p(\mathbf{w}) = p(w_1 \cdots w_T) \tag{1a}$$

$$= p(\text{EOS} \mid \mathbf{w}) \prod_{t=1}^T p(w_t \mid \mathbf{w}_{<t}) \tag{1b}$$

$$= \text{softmax}(\mathbf{E} \mathbf{h}_\theta(\mathbf{w}) + \mathbf{b})_{\text{EOS}} \prod_{t=1}^T \text{softmax}(\mathbf{E} \mathbf{h}_\theta(\mathbf{w}_{<t}) + \mathbf{b})_{w_t}. \tag{1c}$$

Here, $\mathbf{E} \in \mathbb{R}^{|\Sigma| \times d}$ and $\mathbf{b} \in \mathbb{R}^{|\Sigma|}$. We assume that $\text{EOS} \notin \Sigma$ and define $\bar{\Sigma} \stackrel{\text{def}}{=} \Sigma \cup \{\text{EOS}\}$.

2.1 STRUCTURAL EQUATION MODELING

We begin by briefly reviewing structural equation modeling, which provides a framework for discussing causal manipulations of the generation process and allows us to precisely define the intuitive notion of a counterfactual. See Pearl (2009); Pearl et al. (2016); Peters et al. (2017); Peters & Halpern (2021); Halpern & Peters (2022) for a more in-depth treatment.

Definition 2.1 (Structural Equation Model (SEM)). A **structural equation model (SEM)** is a tuple $\mathcal{E} = (\mathcal{S}, \mathcal{F})$, where \mathcal{S} is a **signature** and \mathcal{F} is a set of **structural equations**. A **signature** is a tuple $\mathcal{S} = (\mathbf{U}, \mathbf{V}, \mathcal{R}, \mathcal{I})$, where

- \mathbf{U} is a finite set of **exogenous** random variables (RVs) $\{U_1, \dots, U_N\}$,
- \mathbf{V} is a finite set of **endogenous** RVs $\{V_1, \dots, V_M\}$,
- \mathcal{R} assigns each variable $X \in \mathbf{U} \cup \mathbf{V}$ its range, i.e., the set of values it can take, and
- \mathcal{I} is a set of **interventions**.

An **intervention** I is a set of pairs $V \leftarrow v$ with $V \in \mathbf{V}$ and $v \in \mathcal{R}(V)$, where any intervention I contains at most one pair $V \leftarrow v$ for any $V \in \mathbf{V}$. The set of structural equations $\mathcal{F} = \{\mathcal{F}_{V_1}, \dots, \mathcal{F}_{V_M}\}$ contains for each endogenous variable $V \in \mathbf{V}$ a function $F_V: \mathcal{R}(\mathbf{U} \cup \mathbf{V} \setminus \{V\}) \rightarrow \mathcal{R}(V)$, i.e.,

¹This approach has been explored in reinforcement learning (Oberst & Sontag, 2019), but to our knowledge, not in language modeling. As we show, the infinite outcome space in LMs requires special handling not needed in finite domains.

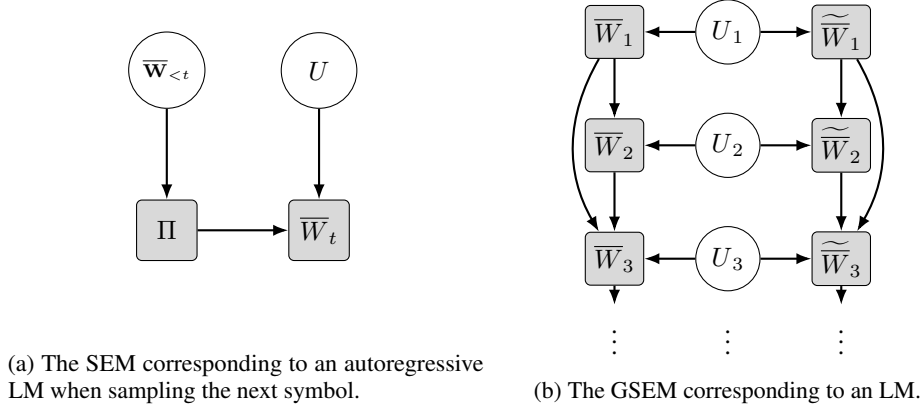


Figure 1: Examples of (G)SEMs.

\mathcal{F}_V assigns V a deterministic value based on the values of all the other variables in the SEM: $V = F_V(\mathbf{U}, \mathbf{V} \setminus \{V\})$ for all $V \in \mathbf{V}$.

The range assignment \mathcal{R} and a set of interventions $I \in \mathcal{I}$ generalize naturally to more variables; we use $\mathcal{R}(\mathbf{X})$ for $\mathbf{X} \subseteq \mathbf{U} \cup \mathbf{V}$ to refer to the Cartesian product of the individual ranges while $\mathbf{X} \leftarrow \mathbf{x}$ refers to an intervention assigning values to all $V \in \mathbf{X} \subseteq \mathbf{V}$. **One can draw an SEM as a directed graph by representing each variable in $\mathbf{U} \cup \mathbf{V}$ as a node and connecting the *parents* of V —arguments to F_V that affect V —to V . We will assume that the directed graph constructed this way is acyclic.**

By assigning a joint probability distribution $\mathbb{P}(\mathbf{U})$ to the exogenous variables, an SEM induces a probability distribution over $\mathbf{U} \cup \mathbf{V}$, which we denote by $\mathbb{P}_{\mathcal{E}}$. We call any assignment of the exogenous variables the **context** of the SEM. As suggested by the notation, an intervention $I = \mathbf{X} \leftarrow \mathbf{x} \in \mathcal{I}$ converts a SEM into another SEM in which the structural equation F_V is replaced by the assignment $\mathbf{X} \leftarrow \mathbf{x}$; this SEM is denoted by $\mathcal{E}_{\mathbf{X} \leftarrow \mathbf{x}}$. Note that the intervention can also be empty, in which case $\mathcal{E}_{\mathbf{X} \leftarrow \mathbf{x}}$ is the original SEM. Given a context, the **outcome** of an SEM under the intervention $\mathbf{X} \leftarrow \mathbf{x}$ are all the assignments \mathbf{v} of \mathbf{V} that satisfy the structural equations of the SEM $\mathcal{E}_{\mathbf{X} \leftarrow \mathbf{x}}$. In an SEM with no cyclical dependencies between the variables, the outcome can be determined by solving the equations in a sequence consistent with the variable dependencies.

Interventions correspond to the second level of Pearl’s hierarchy. They allow us to manipulate the causal generation structure and thus generate *new* outcomes from a precisely modified SEM. Interventions, however, do not manipulate individual outcomes—they only allow us to sample (unrelated) new observations. The third level of the causal hierarchy concerns itself with *retrospective* modifications of the SEM, defining precisely what it means to investigate what would have happened at the time of sampling *had* the SEM been different, i.e., had an intervention been performed. This is formalized with counterfactual distributions.

Definition 2.2 (Counterfactual Distribution). *Given an SEM $\mathcal{E} = (\mathcal{S}, \mathcal{F})$ and an outcome \mathbf{u} , the **counterfactual** distribution under the intervention $I = \mathbf{X} \leftarrow \mathbf{x}$ is the distribution defined by the intervened-on SEM $\mathcal{E}_{\mathbf{X} \leftarrow \mathbf{x}}$ whose exogenous variables follow the posterior distribution $\mathbb{P}(\mathbf{U} \mid \mathbf{V} = \mathbf{u})$.*

SEMs can be represented as causal graphical models, where the edges signify not just conditional dependencies but also causal influences. Consider the (simplified) causal graphical model in Fig. 1a, which illustrates an abstraction of the process of next-symbol generation. In this model, the next symbol w_t , represented by the RV \bar{W}_t , is sampled based on the preceding string $w_{<t}$, represented by the RV $\bar{W}_{<t}$. The edges indicate the (complex) causal relationships that generate w_t . Specifically, the edge between $\bar{W}_{<t}$ and Π_t —representing the deterministic computations of a language encoder—reflects the causal role of the language encoder. Together, the string representation and sampling noise determine the next symbol w_t .² Interventions on this model correspond to modifying the relationship between $\bar{W}_{<t}$ and Π_t by altering the language encoder that implements this transformation.

²This is made more precise in §2.2.

Structural causal models are defined over *finitely* many RVs $\mathbf{U} \cup \mathbf{V}$. Generalized SEMs (Peters & Halpern, 2021; Halpern & Peters, 2022) allow us to model infinitely many variables.

Definition 2.3 (Generalized Structural Equation Model (GSEM)). A **generalized structural equation model (GSEM)** is a tuple $\mathcal{E} = (\mathcal{S}, \mathcal{F})$, where $\mathcal{S} = (\mathbf{U}, \mathbf{V}, \mathcal{R}, \mathcal{I})$ is a signature with analogous definitions as in Def. 2.1 without the requirement that \mathbf{U} , \mathbf{V} , and $\mathcal{R}(\mathbf{U} \cup \mathbf{V})$ be finite. $\mathcal{F}: \mathcal{I} \times \mathcal{R}(\mathbf{U}) \rightarrow 2^{\mathcal{R}(\mathbf{V})}$ is a function that maps an intervention $I \in \mathcal{I}$ and a context $\mathbf{u} \in \mathcal{R}(\mathbf{U})$ directly to the possible set of outcomes $\mathcal{F}(\mathbf{u}, \mathbf{X} \leftarrow \mathbf{x}) \subseteq \mathcal{R}(\mathbf{V})$.

Thus, GSEMs generalize SEMs in two ways: They allow for causal models with infinitely many variables and they allow for specifying the effects of interventions *directly*, rather than having to conform to a pre-defined set of structural equations as in an SEM.

2.2 LANGUAGE PROCESSES AND GENERALIZED STRUCTURAL CAUSAL MODELS

We next show how LMs can be framed as GSEMs. We begin by defining the Gumbel distribution.

Definition 2.4 (Gumbel distribution). The cumulative distribution function of the **standard Gumbel distribution** $\text{Gumbel}(0, 1)$ is $F(x) = \exp(-\exp(-x))$ and its density function is $f(x) = \exp(-(x + \exp(-x)))$.

The Gumbel distribution is useful for modeling the distribution of the *maximum* (or minimum) of a set of samples from various distributions. This is the core idea behind the Gumbel-max trick, which shows the utility of the Gumbel distribution for sampling from the categorical distribution (Luce, 1959; Yellott, 1977; Maddison et al., 2017; Hazan & Jaakkola, 2012; Maddison et al., 2014; Hazan et al., 2016). We restate the trick below for the specific case of the softmax; see App. B for the proof.

Theorem 2.1 (The Gumbel-max Trick). Let X be a categorical RV over M categories such that

$$\mathbb{P}(X = m) = \frac{\exp(\phi_m)}{\sum_{m'=1}^M \exp(\phi_{m'})} = \text{softmax}(\phi)_m, \quad (2)$$

for $m \in \{1, \dots, M\}$ and a given vector of **logits** $\phi \in \mathbb{R}^M$. The **Gumbel-max trick** states that sampling from X can be performed as follows: (i) draw M outcomes y_1, \dots, y_M independently from a standard Gumbel distribution $\text{Gumbel}(0, 1)$ and (ii) set the outcome of X as

$$m = \underset{m'=1}{\text{argmax}}^M \phi_{m'} + y_{m'}. \quad (3)$$

As we make formal below, sampling from an encoder-based LM can be formulated with the Gumbel-max trick, since the (affinely transformed) representations $\mathbf{h}_\theta(\mathbf{w})$ provide the logits ϕ_m in Eq. (3).

A **language process** $\mathbf{W} = \{\overline{W}_t\}_{t=1}^\infty$ is an infinite sequence of (correlated) $\overline{\Sigma}$ -valued RVs, where we think of \overline{W}_t as the RV whose outcome generates the t^{th} symbol of a string (Du et al., 2024).³ Let $\mathbf{U} = \{U_t\}_{t=1}^\infty$ be an infinite sequence of random $|\overline{\Sigma}|$ -dimensional vectors indexed by $\overline{w} \in \overline{\Sigma}$ where $U_t(\overline{w}) \stackrel{\text{i.i.d.}}{\sim} \text{Gumbel}(0, 1)$. As explicated by Eq. (1c), encoder-based LMs sample a string by sampling from countably-infinitely many $\overline{\Sigma}$ -valued RVs based on the logits $\phi = \mathbf{E} \mathbf{h}_\theta(\mathbf{w}_{<t})$. We can therefore view the LM induced by a language encoder \mathbf{h}_θ as a function that maps \mathbf{U} —the sampling noise—to a language process \mathbf{W} as follows:

$$\overline{W}_t = \underset{\overline{w} \in \overline{\Sigma}}{\text{argmax}} (\mathbf{E} \mathbf{h}_\theta(\mathbf{w}_{<t}) + \mathbf{b})_{\overline{w}} + U_t(\overline{w}). \quad (4)$$

where $\mathbf{w}_{<t} \stackrel{\text{def}}{=} w_1 \cdots w_{t-1}$ and $\overline{W}_1 = w_1, \dots, \overline{W}_{t-1} = w_{t-1}$. This is graphically depicted in Fig. 1b.^{4,5} A crucial implication of Eq. (4) is that the language process \mathbf{W} is *deterministic* given \mathbf{U} —all the noise in the string generation process comes from the noise variables \mathbf{U} . Such a decomposition of the generative mechanism into deterministic relationships and independent noise variables closely resembles the structural equations of an SEM. Due to the infinitely many variables, it can, however,

³A typical formulation of a language process implies that, if $\overline{W}_t = \text{EOS}$, we have $\overline{W}_{t'} = \text{EOS}$ for all $t' > t$.

⁴GSEMs, in general, do not have a graphical representation. In our case, however, the model can be drawn.

⁵For conciseness, we omit the intermediary representations Π_t .

only be represented by a GSEM, albeit a very structured one—one in which the variable assignments are still determined through (infinitely many) structural equations. The following construction presents a possible specification of a GSEM that induces the same probability distribution over Σ^* as an encoder-based LM. We discuss the (non-)uniqueness of this construction in §2.2.

Construction 2.1 (A GSEM for an LM). *Let h_θ be a language encoder and p the LM induced by h_θ together with the parameters \mathbf{E}, \mathbf{b} . We now define the GSEM $\mathcal{E} = (\mathcal{S}, \mathcal{F})$ that induces the same distribution over Σ^* as p . We have to specify \mathcal{E} 's signature $\mathcal{S} = (\mathbf{U}, \mathbf{V}, \mathcal{R}, \mathcal{I})$, its assignment function \mathcal{F} . We define \mathcal{S} as*

- $\mathbf{U} = \{U_t\}_{t=1}^\infty$ where $U_t(\bar{w}) \stackrel{i.i.d.}{\sim} \text{Gumbel}(0, 1)$ for all $\bar{w} \in \bar{\Sigma}$ and $t \in \mathbb{N}$,
- $\mathbf{V} = \{\bar{W}_t\}_{t=1}^\infty \cup \theta \cup \{\mathbf{E}, \mathbf{b}\} \cup \theta'$, where θ are the encoder parameters and θ' is a set of auxiliary parameters we can use to intervene on h_θ, \mathbf{E} , and \mathbf{b} .
- $\mathcal{R}(U) = \mathbb{R}^{|\bar{\Sigma}|}$ for $U \in \mathbf{U}$, $\mathcal{R}(\bar{W}_t) = \bar{\Sigma}$ for $t \in \mathbb{N}$, $\mathcal{R}(\theta) = \Theta \subseteq \mathbb{R}^K$, $\mathcal{R}(\theta) = \mathbb{R}^{|\bar{\Sigma}| \times d}$, $\mathcal{R}(\theta) = \mathbb{R}^{|\bar{\Sigma}|}$, $\mathcal{R}(\theta') = \Theta' \subseteq \mathbb{R}^{K'}$, where K and K' are the dimensionality of the original and auxiliary intervention parameter spaces, respectively.
- \mathcal{I} is the set of all relevant manipulations of h_θ, \mathbf{E} , and \mathbf{b} through interventions on its parameters θ, θ' , or the outputs \bar{W}_t directly. We assume that θ and θ' are set to fixed values in every intervention. For example, an intervention might fix a subset of parameters within θ to specific values. Additionally, auxiliary parameters θ' enable interventions beyond changes to model parameters. For instance, in linear steering, θ' could include a steering vector \mathbf{v}_l , added to the residual stream, altering the output of a transformer model's fully connected module in layer l . This vector would be the zero in the original model without an intervention. Another example is the setting of a projection matrix to a particular value, which would change the final representations of the model. In this formulation, the modeler can define interventions on any model component, e.g., specific weights θ , intermediate variables such as hidden activation vectors \mathbf{h} , or outputs \bar{W}_t .

We define \mathcal{F} as follows. Let $\mathbf{X} \leftarrow \mathbf{x}$ be an intervention on $\theta, \mathbf{E}, \mathbf{b}, \theta'$ and $\{\bar{W}_t\}_{t=1}^\infty$ that defines $\tilde{\theta}, \tilde{\mathbf{E}}, \tilde{\mathbf{b}}, \tilde{\theta}'$, and the modified symbols $\{\tilde{\bar{W}}_{t'}\}_{t' \in \mathcal{N}}$ for $\mathcal{N} \subseteq \mathbb{N}$. Then, given an instantiation of the exogenous variables $\mathbf{u} = \{U_t(\bar{w}) \mid t \in \mathbb{N}, \bar{w} \in \bar{\Sigma}\}$, we define the function \mathcal{F} that, given $\mathbf{X} \leftarrow \mathbf{x}$ and \mathbf{u} , defines a single outcome with $\theta \leftarrow \tilde{\theta}, \mathbf{E} \leftarrow \tilde{\mathbf{E}}, \mathbf{b} \leftarrow \tilde{\mathbf{b}}, \{\bar{W}_{t'}\}_{t' \in \mathcal{N}} \leftarrow \{\tilde{\bar{W}}_{t'}\}_{t' \in \mathcal{N}}$, and the remaining generated tokens as $\bar{W}_t \leftarrow \arg\max_{\bar{w} \in \bar{\Sigma}} \left(\tilde{\mathbf{E}} h_{\tilde{\theta}}(\mathbf{w}_{<t}) + \tilde{\mathbf{b}} \right)_{\bar{w}} + U_t(\bar{w})$ for $t \in \mathbb{N} \setminus \mathcal{N}$. Under no intervention, \mathcal{F} runs the forward pass of the original network and generates the next tokens.

Proposition 2.1. *The GSEM in Construction 2.1 has a unique solution.*

Proof. The GSEM is well-formed: The only infinite chain of variables is $\mathbf{V} = \{\bar{W}_t\}_{t=1}^\infty$, where \bar{W}_t depends on $\{\bar{W}_{t'}\}_{t' < t}$ with the root \bar{W}_1 . As mentioned in Halpern & Peters (2022), well-foundedness implies a unique assignment of the infinitely many variables. ■

By Prop. 2.1, any context–intervention pair defines a single possible outcome—the one that satisfies the equations specified by the Gumbel-max decomposition of a language process. $\mathbb{P}_{\mathcal{E}}$ matches p —by the Gumbel-max trick (cf. Thm. 2.1), the structural equations in Construction 2.1 are equivalent to sampling from $\tilde{\mathbf{E}} h_{\tilde{\theta}}(\mathbf{w}_{<t}) + \tilde{\mathbf{b}}$, as done by the (intervened-on) LM.

Sampling techniques. Our formalization assumes that strings are generated by sampling from the full probability distribution defined by an LM. In practice, however, different decoding techniques, such as nucleus sampling (Holtzman et al., 2020) or top- k sampling (Fan et al., 2018), are often used. As long as these decoding methods can be expressed as deterministic functions over the logits, followed by standard sampling, the same formulation can be applied.⁶ This way, the deterministic parts of the sampling algorithm are considered a part of the LM forward pass computation.

⁶For example, in top- k sampling, we can set the logits of all tokens outside the top k to a large negative value and then sample using the Gumbel-max trick.

Identifiability of LM counterfactuals. Identifiability of counterfactual distributions based on observational or interventional data is, in general, impossible—two (G)SEMs can be equal in all interventional distributions and yet define different counterfactual outcomes. Construction 2.1, however, implicitly defines a *single* counterfactual distribution for any intervention and outcome and thus requires some justification. In App. C we discuss different modeling choices, and show that under some reasonable conditions—assuming a Thurstone model for sampling from the model (Thurstone, 1927)—the counterfactual distribution is identifiable.

3 COUNTERFACTUAL GENERATION

Framing LMs as GSEMs allows us to use the expansive set of causal tools on LMs. We focus on generating counterfactual strings for given observed ones—strings that differ in particular features but are generated with the same sampling noise as the previously observed ones. More precisely, let $\mathbf{w} = w_1 \cdots w_T \in \Sigma^*$ be the string sampled from the LM induced by the encoder h_θ with the parameters \mathbf{E} and \mathbf{b} , and the noise \mathbf{U} . Given a counterfactual encoder $h_{\tilde{\theta}}$ with the parameters $\tilde{\mathbf{E}}$ and $\tilde{\mathbf{b}}$, Eq. (4) tells us that **given the fixed randomness, \mathbf{w} 's counterfactual is given by**

$$\tilde{\mathbf{W}}_t = \operatorname{argmax}_{\tilde{\mathbf{w}} \in \Sigma} \underbrace{\left(\tilde{\mathbf{E}} h_{\tilde{\theta}}(\mathbf{w}_{<t}) + \tilde{\mathbf{b}} \right)_{\tilde{\mathbf{w}}}}_{\stackrel{\text{def}}{=} \pi(\tilde{\mathbf{w}})} + U_t(\tilde{\mathbf{w}}). \quad (5)$$

This procedure results in *pairs* of strings in Σ^* —the original string \mathbf{w} and its counterfactual $\tilde{\mathbf{w}}$ —from the joint distribution $\mathbb{P}(\mathbf{W} = \mathbf{w}, \tilde{\mathbf{W}} = \tilde{\mathbf{w}})$. The counterfactual $\tilde{\mathbf{w}}$ is sampled from the *same* instantiation of the exogenous variables \mathbf{U} .

Without a clear definition of counterfactuality, however, it is difficult to evaluate the impact of representational surgeries, since we lack string pairs where the *only* difference is the surgery itself. Our framework addresses this by ensuring that a string \mathbf{w} and its counterfactual $\tilde{\mathbf{w}}$ form a **minimal pair** with respect to the intervened feature. A key goal of our experimental setup is to leverage this causal framework to evaluate the stability of various representational surgeries.

However, when evaluating the effects of model interventions, we are not solely concerned with minimal pairs. Another important question is: How would a *given* string have appeared if it had been generated by the counterfactual model rather than the original one? Answering this question requires knowledge of the exogenous noise that produced the original strings. In our framework, this entails inferring the values (or, more precisely, the distribution) of the unobserved noise variables \mathbf{U} that led to a particular observed string \mathbf{w} . Once the specific outcomes of \mathbf{U} are identified, we can generate the corresponding counterfactuals. We tackle the problem of inferring \mathbf{U} by developing an algorithm that reverses the causal process illustrated in Fig. 1b.

Proposition 3.1 (Hindsight Gumbel Sampling). *Let $\{\bar{\mathbf{w}}_t\}_{t=1}^\infty$ be an instantiation of the variables $\{\bar{\mathbf{W}}_t\}_{t=1}^\infty$ sampled according to Eq. (4). To sample $U_t(\bar{\mathbf{w}}) \mid \bar{\mathbf{W}}_t = \bar{\mathbf{w}}_t$ for $\bar{\mathbf{w}} \in \bar{\Sigma}$, we can proceed in the following steps:*

1. sample $U_t(\bar{\mathbf{w}}_t) \sim \text{Gumbel}(0, 1)$,
2. for all $\bar{\mathbf{w}} \neq \bar{\mathbf{w}}_t \in \bar{\Sigma}$, sample $U_t(\bar{\mathbf{w}})$ independently according to the following probability:

$$\mathbb{P}(U_t(\bar{\mathbf{w}}) \mid U_t(\bar{\mathbf{w}}_t) + \pi(\bar{\mathbf{w}}_t) \geq U_t(\bar{\mathbf{w}}) + \pi(\bar{\mathbf{w}})). \quad (6)$$

Proof. Follows from the known result on the independence between the argmax and the rest of the values in the Gumbel distribution (Maddison et al. (2014), Maddison & Tarlow (2017), Oberst & Sontag (2019, §3.4)) ■

Corollary 3.1 (Counterfactual String Sampling). *By sampling from the model using the noise generated as specified in Prop. 3.1, we get a sample from the counterfactual distribution.*

Proof. The noise in Prop. 3.1 is sampled from $U_t \mid \bar{\mathbf{W}}_t = \bar{\mathbf{w}}_t$, which is the posterior distribution of the exogenous variables, as required by Def. 2.2. ■

We employ a standard technique for sampling from “truncated” (conditional) distribution (Maddison et al., 2014).⁷ In our case, the truncation condition ensures that the observed word \bar{w}_t has a higher score than all other vocabulary tokens to mimic Eq. (5). This procedure, summarized in Alg. 1, allows us to generate potential counterfactual sentences for a given observed sentence.

4 EXPERIMENTS

4.1 SIDE EFFECTS OF COMMON INTERVENTION TECHNIQUES

Many standard intervention techniques, such as knowledge editing (Meng et al., 2022; 2023) or inference-time intervention (Li et al., 2024; Singh et al., 2024) are intended to modify targeted aspects of model behavior, such as altering specific knowledge or increasing its truthfulness (Li et al., 2024). If these interventions are surgical, we expect them to preserve the model’s behavior on unrelated, “neutral” sequences—such as random Wikipedia sentences, resulting in counterfactuals similar to the original sentence. We test this assumption.

4.1.1 EXPERIMENTAL SETUP

Setup. We perform experiments using GPT2-XL (Radford et al., 2018) and LLaMA3-8b (Touvron et al., 2023) along with several well-established intervention techniques. These include MEMIT (Meng et al., 2023), inference-time interventions using linear steering (Li et al., 2024; Singh et al., 2024), and Instruction tuning (Touvron et al., 2023):

- **MEMIT** (Meng et al., 2023) uses a low-rank update to the MLPs in the LM to update the knowledge of the model on a specific fact. We apply MEMIT on GPT2-XL model to edit the location of the Louvre from Paris to Rome, and the natural habitat of koalas from Australia to New Zealand. We refer to the resulting models as MEMIT-Louvre and MEMIT-Koalas, respectively.
- **Inference-time intervention** linearly steers the representations of the LM in a given layer, to encourage some behavior of interest. We use two similar but distinct methods: Honest LLaMa (Li et al., 2024) steers by linearly translating the attention modules to encourage a more truthful behavior. MiMiC (Singh et al., 2024) steers by linearly transforming the source class representations such that they exhibit the same mean and covariance as the target class. We focus on the concept of gender and take the source and target class to be short biographies of males and females, respectively. We refer to the steered models as Steering-Honest and Steering-Gender.
- **Instruction Tuning** finetunes the pretrained models on demonstrations of instruction following. We refer to this model as LLaMA3-Instruct.

In each case, we define the model prior to the intervention as the original model and the model following the intervention as the counterfactual model. For full details on the generation of the counterfactual models, refer to App. E.1. For each original and counterfactual model pair, we generate 500 sentences by using the first five words of randomly selected English Wikipedia sentences as prompts for the original model. We generate a continuation of a maximum of 25 tokens by sampling from the model using multinomial sampling (i.e., sampling from the entire model distribution over the vocabulary). We then use Alg. 1 to generate a counterfactual sentence.

Evaluation. Being prompted by a prefix from Wikipedia, the original model is not likely to generate a continuation that exhibits a property that is the focus of *any* of the specific model intervention techniques we examine (e.g., it is not likely to generate a sentence that discusses the location of the Louvre, for the MEMIT intervention). Accordingly, we expect the counterfactual strings to be similar to the original ones. This is desirable, as we ideally want surgical intervention without side effects. To quantify side effects on arbitrary strings, we record the longest common prefix, which we define as the length of the longest prefix of the original sentence that is shared with the counterfactual sentence normalized by the length of the original sentence. To evaluate the semantic similarity between the

⁷The algorithm given by <https://timvieira.github.io/blog/post/2020/06/30/generating-truncated-random-variates/> is used for performing the “truncated” sampling.

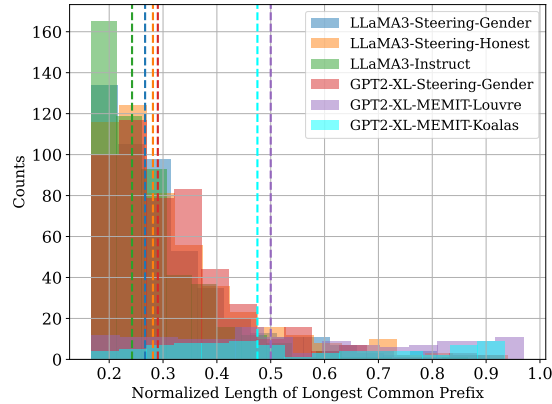


Figure 2: Normalized length of the longest shared prefix between the original and counterfactual sentences, for different intervention techniques. The horizontal lines denote the median of each distribution. Higher values reflect less side effects for the intervention.

original and counterfactual model, we calculate cosine similarity under the E5-base encoder (Wang et al., 2024).⁸ Surgical interventions should have high values for both metrics.

Original and Counterfactual strings for the LLaMA3 Instruct finetuning intervention.

1. **Original:** Chenopodium nutans, commonly called climbing, or **nodding** goosefoot, is an annual plant...
Counterfactual: Chenopodium nutans, commonly called climbing, or **leafy** goosefoot, is an annual plant...
2. **Original:** Brittany Haas is an American **fiddler** and a founding member of the acclaimed trio Hawktail.
Counterfactual: Brittany Haas is an American **fiddler and composer**.
3. **Original:** Richard Joseph Grosh (born October 28, 1935) was **Director of the US Securities and Exchange Commission**
Counterfactual: Richard Joseph Grosh (born October 24, 1935) was an **American politician** who served as a member of the U.S. House of Representatives from...
4. **Original:** It was also included on a **limited edition vinyl 7"** with "Tape Loop"...
Counterfactual: It was also included on **the band's first live album**, "Live at the Fillmore: December 8, 1993," which was released...
5. **Original:** The series consists of four **items**: a letter written by Lt. Col. Edward S. Durnford (1918), a draft contract for the...
Counterfactual: The series consists of four **episodes** and a special edition episode. Each episode will explore a different theme and feature interviews with experts and individuals who have been affected...

Figure 3: Counterfactual strings from the original model LLaMA3 and the counterfactual counterpart LLaMA3-Instruct.

4.1.2 RESULTS

The distribution of the normalized length of the longest common prefix is shown in Fig. 2. Among the methods, MEMIT demonstrates the most precise intervention, with a median longest shared prefix length of around 50% for both the Louvre and Koalas concepts. The steering vector interventions follow at around 30%, with the instruction tuning intervention being the least surgical, sharing only around 24% of tokens on average. These trends are also reflected in the cosine similarity under the

⁸We use the E5-base-v2 model from <https://huggingface.co/intfloat/e5-base-v2>.

E5 model, which is 0.976 and 0.986 for the MEMIT Koalas and Louvre interventions, and around 0.860 for all other interventions.⁹

Fig. 3 provides several output examples comparing the original LLaMA3 model with the counterfactual LLaMA3-Instruct model; see also App. G.1 for a random sample of outputs from all models. In some cases, such as the first two examples, the intervention introduces factual inaccuracies, which are evident in the generated counterfactuals. The third example demonstrates a case where *both* the original and the counterfactual model hallucinate (the subject of the sentence was actually an academic), but the content of the hallucination changes as a result of the intervention. Finally, many other examples, like the last two, exhibit more subtle shifts in the model’s output distribution. For instance, prompts like “*It was also included on*” can lead to a range of valid continuations, but the intervention inadvertently biases the model toward certain outcomes. These results indicate that even interventions that are designed to be “minimal”, such as those based on a steering vector that only modifies a tiny fraction of all the model’s parameters, still have considerable causal effect on the output of the model, as demonstrated by the semantic drift in the continuations of prompts taken from Wikipedia. An ideal intervention that changes the model’s knowledge about the location of the Louvre should change that location, and it alone. In practice, however, even interventions such as MEMIT, that update few parameters in a single matrix within the model, have considerable side effects. Due to the autoregressive nature of language generation, slight variations in token choice accumulate rapidly, resulting in a significant semantic divergence between the original and the counterfactual sentence.

4.2 INTERVENTION-FOCUSED COUNTERFACTUALS

In the previous section, we examine how surgical the different interventions are. Accordingly, we focused the evaluation on prompts drawn from Wikipedia, a domain we expect to be largely orthogonal to the specific properties on which the interventions target. Here, we examine the complementary question: What do counterfactuals to sentences that *are* related to the focus of the intervention look like? We focus on two case studies: MEMIT, which edits for the location of the Louvre, and MiMiC, which employs a steering intervention to push the model in the male → female direction.

4.2.1 GENDER STEERING

Text Examples: Originals and Counterfactuals for the MiMiC gender steering intervention.

1. **Original:** Kyle Thompson is an assistant professor at Pittsburg State University in Kansas, where **he** teaches courses on **marketing, entrepreneurship, and management**.
Counterfactual: Kyle Thompson is an assistant professor at Pittsburg State University in Kansas, where **she** teaches courses in **early childhood education and child development**.
2. **Original:** Clayton Webb is an assistant professor of political science at the University of Tennessee. **His** research focuses on political behavior, public opinion, and **the psychology of politics**.
Counterfactual: Clayton Webb is an assistant professor of political science at the University of Tennessee. **Her** research focuses on political behavior, public opinion, and **the intersection of politics and social issues. She is particularly interested in...**
3. **Original:** Jeffrey M. Stanton, Ph.d., is an assistant professor at the University of Rochester Medical Center. **He** conducts research in the area of **statistical genetics, focusing on the development of methods for analyzing large-scale genomic data...**
Counterfactual: Jeffrey M. Stanton, Ph.d., is an assistant professor at the University of Rochester’s Warner **School of Education**, where **she** teaches and conducts research in the areas of **educational technology, online teaching and learning, and educational psychology**.
4. **Original:** Nicholas F. Benson, Ph.d., is an associate professor of chemistry at the University of Illinois at Chicago (UIC). **He** received his B.S. in chemistry from the University of Illinois at Urbana-Champaign in 2003 and **his** Ph.d....
Counterfactual: Nicholas F. Benson, Ph.d., is an associate professor of chemistry at the University of Illinois at Chicago (UIC). **She** received his B.S. in chemistry from the University of Illinois at Urbana-Champaign in 2003 and **her** Ph.d....

Figure 4: Counterfactual strings from the original model LLaMA3 and the counterfactual counterpart Steering-Gender LLaMA3 (created by a MiMiC steering intervention in the direction male → female.). The first 8 tokens in the original sentence were used as a prompt.

⁹Cosine similarity of 0.867, 0.873, 0.870 and 0.863 for the LLaMA3 gender-steering, LLaMA3 honest-steering, LLaMA3 Instruction finetuning and GPT2 gender steering, respectively.

Setup. We focus this analysis on gender steering of the LLaMA3-Instruct model. We apply the MiMiC method (Singh et al., 2024), which modifies model representations by aligning male-focused text representations with female-focused text representations. This approach results in a linear transformation of the residual stream, ensuring that the mean and covariance of the source class (male-focused texts) match those of the target class (female-focused texts). We fit the transformation on the Bios dataset (De-Arteaga et al., 2019), which consists of short biographies of individuals working in various professions. Each biography is annotated with both gender and profession labels. For the full details on the fitting of the MiMiC intervention, see App. E.1. Once the intervention is fitted, we first generate a continuation for 500 biographies in the dataset by sampling from the original model after prompting it with the first words in the biography, and then use Alg. 1 to generate counterfactual continuations under the modified models.

Results. A sample of the results can be found in Fig. 4 and App. G.2. The intervention demonstrates reasonable effectiveness in altering the pronouns used in the continuations. While the original biographies all contain male pronouns, in 52.2% of the counterfactual continuations, only female pronouns such as "she" and "her" are observed. In 23.2% of the cases, male pronouns persist, while 16.6% show a mixture of female and male pronouns, and 7.6% of the counterfactuals do not include any pronouns at all. An examination of the counterfactual continuations in Fig. 4 and App. G.2 reveals many side effects beyond pronouns. See App. F for a quantitative evaluation.

4.2.2 MEMIT LOCATION EDITING

Setup. We focus this analysis on the MEMIT-edited model, where the location of the Louvre was updated from "Paris" to "Rome". We begin by prompting the original model to generate sentences that mention Paris as the location of the Louvre, such as "*Paris offers many attractions, but the*". See App. E.2 for details. We filter out sentences that do not mention both Paris and the Louvre, resulting in 75 sentences. We then generate the counterfactuals with the counterfactual model.

Results. First, we observe that the Louvre-focused counterfactuals deviate much more from the semantics of the original sentences than non-Louvre-focused generations. The median normalized longest prefix consists of only 23% of the tokens in the original sentences, compared with around 50% in the Wikipedia-based counterfactuals. A manual inspection of the counterfactuals reveals a significant deviation from the semantics of the original sentences. For instance, the counterfactual of "*Among all the art museums in the world, the Louvre stands tall in the Parisian art scene, having been at the same spot since 1793*" is the sentence "*Among all the art museums in the world, the Louvre alone, which has been open to visitors for more than 2,000 years, is one of the most visited.*". Altogether, *the counterfactuals are mostly not minimal*: they do not change just the location of the Louvre, but other (unrelated) parts of the sentence. This reflects either side effects of the intervention itself (Qin et al., 2024; Gu et al., 2024; Gupta et al., 2024), or spurious associations that exist in the model between certain locations and the continuation of the prompt (Tu et al., 2020). With respect to correctness, we find that 60.0% of the counterfactuals mention Rome as the location of the Louvre, while 40.0% still mention Paris.

5 CONCLUSION

We introduce a framework for generating true counterfactuals from LMs by reformulating LMs as Generalized Structural equation Models with the Gumbel-max trick. This allows us to precisely model the joint distribution over original and counterfactual strings, enabling us to investigate causal relationships at the highest level of Pearl’s causal hierarchy. Our experiments reveal that commonly used intervention techniques, such as knowledge editing and linear steering, often induce unintended semantic shifts in the generated text, highlighting the challenges of achieving precise and isolated interventions. These observations underline the need for more refined methods that can achieve targeted modifications with minimal collateral changes to the model’s outputs.

REPRODUCIBILITY STATEMENT

We detail our experimental setup in §4.1.1 and App. E.1.

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A RELATED WORK

Probing the content of neural representations is a fundamental method of interpreting language models (Giulianelli et al., 2018; Adi et al., 2017). Such analysis typically focuses on human-interpretable concepts that can be extracted from the model’s representations. Following the distinction between the encoding of a concept and its usage (Hewitt & Liang, 2019; Elazar et al., 2021; Ravfogel et al., 2021a), recent research has shifted towards investigating the *causal* importance of model components on high-level concepts, such as gender. Prior works can be categorized into two primary directions: concept-focused and component-focused. Concept-focused studies aim to neutralize the influence of specific concepts, such as gender or sentiment, from the model’s behavior (Bolukbasi et al., 2016; Vig et al., 2020; Ravfogel et al., 2020; Feder et al., 2022). Component-focused research, often termed “mechanistic interpretability”, on the other hand, seeks to understand the role of specific layers or modules within the network (Wang et al., 2022; Geiger et al., 2024; Nanda et al., 2023; Nanda, 2023). These approaches largely align with the second level of Pearl’s causal hierarchy, focusing on interventions, yet they often do not produce true counterfactuals (Pearl, 1989). Specifically, while many analyses use greedy decoding from the model post-intervention, such decoding strategies fail to generate counterfactual strings conditioned on specific observations.

Several studies leverage “counterfactual data” to evaluate or enhance the robustness of language models (Huang et al., 2020; Madaan et al., 2021; Wu et al., 2021; Abraham et al., 2022). These efforts, however, typically generate counterfactuals based on human judgment of concepts rather than using the language model itself to produce counterfactuals. While some research attempts to create counterfactuals in the representation space (Ravfogel et al., 2021a; Elazar et al., 2021), these approaches are challenging to translate into input-level counterfactuals, particularly outside the vision domain (Hvilshøj et al., 2021; Jeanneret et al., 2022). Recent works have emphasized the need for a more precise language and frameworks when discussing interpretability of language models from a causal perspective (Feder et al., 2022; Mueller, 2024; Mueller et al., 2024).

In this paper, we build on these foundations by introducing a novel approach that treats language models as generalized structural equation models (GSEMs; Halpern & Peters, 2022). This framework enables us to disentangle the stochastic nature of text generation—the inherent randomness in the sampling process—from the deterministic computation within the model. Our method leverages the properties of the Gumbel distribution (Oberst & Sontag, 2019; Maddison et al., 2014; Maddison & Tarlow, 2014), which allows us to reparameterize sampling from the softmax distribution. A similar formulation has been employed in reinforcement learning contexts (Oberst & Sontag, 2019), but to our knowledge, it has not yet been explored in language modeling.

Concurrent research by Chatzi et al. (2024) presents a spiritually very similar work in which the authors define an SEM that allows them to sample counterfactual sentences from a language model. Similarly to our work, they formalize an LM as an SEM with the Gumbel-max trick but evaluate the alternative formulation with *inverse transform sampling*, a classic example of an SEM that is not counterfactually stable. Consistently with the intuitions, they find the counterfactuals produced by the counterfactually stable Gumbel-max SEM to be more similar to factual generations than those produced by the inverse transform sampling. Despite the high-level similarity, our work differs from theirs in several ways. Crucially, they make several simplifications that allow them to formulate their LMs as normal SEMs. The first simplifying assumption is that of defining a probability distribution over a *finite* subset of Σ^* . Secondly, Chatzi et al. (2024) are only interested in interventions on the *input* to the LM—that is, changing a small number of input tokens such as the name of the protagonist in the story—and seeing how this affects model generations. The resulting finite number of interventions defined like this allows them to talk about SEMs. Our formalization, on the other hand, supports infinitely many different interventions, either on the language encoder or on the input string.

B THE GUMBEL-MAX TRICK

An integral part of our work is the use of the Gumbel-max trick for sampling from the softmax. For completeness, we provide a proof here.¹⁰

¹⁰Adapted from Ethan Weinberger’s blog at <https://homes.cs.washington.edu/~ewein//blog/2022/03/04/gumbel-max/>.

Theorem 2.1 (The Gumbel-max Trick). *Let X be a categorical RV over M categories such that*

$$\mathbb{P}(X = m) = \frac{\exp(\phi_m)}{\sum_{m'=1}^M \exp(\phi_{m'})} = \text{softmax}(\phi)_m, \quad (2)$$

*for $m \in \{1, \dots, M\}$ and a given vector of **logits** $\phi \in \mathbb{R}^M$. The **Gumbel-max trick** states that sampling from X can be performed as follows: (i) draw M outcomes y_1, \dots, y_M independently from a standard Gumbel distribution $\text{Gumbel}(0, 1)$ and (ii) set the outcome of X as*

$$m = \operatorname{argmax}_{m'=1}^M \phi_{m'} + y_{m'}. \quad (3)$$

Proof. Let Y be the RV sampled according to Eq. (3) and let $y_{\pi_m} \stackrel{\text{def}}{=} \phi_m + y_m$. We will show that $\mathbb{P}(Y = m) = \text{softmax}(\phi)_m = \mathbb{P}(X = m)$. We know, by definition of argmax that $Y = m$ is only true if $y_{\pi_m} > y_{\pi_{m'}}$ for all $m' \neq m = \operatorname{argmax}_{m' \in \{1, \dots, M\}} \phi_{m'} + y_{m'}$ (cf. Eq. (3)). Let $f_m(y) = \exp(-(y - \phi_m + \exp(-(y - \phi_m)))) = \exp(\phi_m - y - \exp(\phi_m - y))$ be the PDF of $\phi_m + G$ where $G \sim \text{Gumbel}(0, 1)$. We then have

$$\mathbb{P}(Y = m) = \mathbb{P}(y_{\pi_m} > y_{\pi_{m'}} \text{ for all } m' \neq m) \quad (7a)$$

$$= \mathbb{E}_{y_m} \left[\prod_{m' \neq m} \mathbb{P}(y_{\pi_m} > y_{\pi_{m'}}) \right] \quad (7b)$$

$$= \int_{-\infty}^{\infty} f_m(y) \prod_{m' \neq m} \mathbb{P}(\phi_{m'} + y_{m'} < y) dy \quad (7c)$$

$$= \int_{-\infty}^{\infty} f_m(y) \prod_{m' \neq m} \mathbb{P}(y_{m'} < y - \phi_{m'}) dy \quad (7d)$$

$$= \int_{-\infty}^{\infty} f_m(y) \prod_{m' \neq m} \exp(-\exp(-y + \phi_{m'})) dy \quad (7e)$$

$$= \int_{-\infty}^{\infty} f_m(y) \exp\left(-\sum_{m' \neq m} \exp(-y + \phi_{m'})\right) dy \quad (7f)$$

$$= \int_{-\infty}^{\infty} \exp(\phi_m - y - \exp(\phi_m - y)) \exp\left(-\sum_{m' \neq m} \exp(-y + \phi_{m'})\right) dy \quad (7g)$$

$$= \int_{-\infty}^{\infty} \exp(\phi_m - y) \exp\left(-\sum_{m'} \exp(-y + \phi_{m'})\right) dy \quad (7h)$$

$$= \int_{-\infty}^{\infty} \exp(\phi_m - y) \exp\left(-\exp(-y) \sum_{m'} \exp(\phi_{m'})\right) dy \quad (7i)$$

$$= \int_{-\infty}^{\infty} \exp(\phi_m) \exp(-y) \exp\left(-\exp(-y) \sum_{m'} \exp(\phi_{m'})\right) dy \quad (7j)$$

Now let $Z = \sum_{m'=1}^M \exp(\phi_{m'})$. Then we have

$$\mathbb{P}(Y = m) = \int_{-\infty}^{\infty} \exp(\phi_m) \exp(-y) \exp\left(-\exp(-y) \sum_{m'} \exp(\phi_{m'})\right) dy \quad (8a)$$

$$= \exp(\phi_m) \int_{-\infty}^{\infty} \exp(-y) \exp(-\exp(-y)Z) dy \quad (8b)$$

$$= \exp(\phi_m) \int_0^{\infty} \exp(-Zu) du \quad (8c, u = \exp(-y), du = -\exp(-y)dy)$$

$$= \exp(\phi_m) \frac{1}{Z} \quad (8d)$$

$$= \frac{\exp(\phi_m)}{\sum_{m'=1}^M \exp(\phi_{m'})} = \mathbb{P}(X = m), \quad (8e)$$

which is what we wanted to show. \blacksquare

C IDENTIFIABILITY

We discuss the identifiability of the counterfactual distribution associated with Construction 2.1.

Non-uniqueness of Construction 2.1. Eq. (4) is far from the only way of defining the causal mechanism behind a language process. While, by definition, any suitable construction defines the same probability distribution over Σ^* as the LM, the *counterfactual* distributions may vary substantially among the different constructions. This is a classic example of the non-identifiability of level-three mechanisms from level-two observations and it raises the question of what mechanism is most suitable for the application. Oberst & Sontag (2019); Chatzi et al. (2024) discuss how the exact assumed causal model affects counterfactual distributions.

An alternative to Eq. (4) could be inverse CDF sampling. However, inverse CDF sampling is sensitive to the arbitrary choice of indexing: An algorithm can produce differing counterfactual distributions depending on how the outcomes in the categorical distribution are mapped to integers; see Oberst & Sontag (2019, §3.1) for a concrete example. Oberst & Sontag (2019, §3.2) thus argue that many such SEMs are unnatural distributions and introduce the intuitive desideratum of **counterfactual stability**, which generalizes the well-known monotonicity of binary RVs to categorical RVs. Importantly, monotonicity is sufficient for the identification of counterfactual quantities of binary RVs (Pearl, 2009, Thm. 9.2.15). Informally, counterfactual stability requires that a counterfactual outcome can only be different if the counterfactual intervention increases the probability of the different outcome more than the probability of the original outcome. Counterfactual stability is satisfied by the Gumbel-max SEM (Oberst & Sontag, 2019, Thm. 2), motivating the use of Gumbel-max in Construction 2.1.

Gumbel-max is further studied in the LM setting by Chatzi et al. (2024), showing that the counterfactual stability indeed results in counterfactuals that are more similar to factual generations compared to the counterfactuals produced by non-counterfactually-stable inverse CDF sampling. Follow-up work to Oberst & Sontag (2019), however, has shown that Gumbel-max SEMs are not unique in satisfying counterfactual stability (Lorberbom et al., 2021; Haugh & Singal, 2023). Nevertheless, in the following, we show that for a natural set of desiderata, the Gumbel max is indeed the unique natural choice for the causal mechanism. For that, we turn to choice theory.

Definition C.1 (Thurstone RVs). *A categorical RV X over M categories is **Thurstone** with potentials $\{\phi_m\}_{m=1}^M$ if it can be written as*

$$X \sim \operatorname{argmax}_{m=1}^M \phi_m + U_m \quad (9)$$

where $\{\phi_m\}_{m=1}^M$ are constants and U_m are i.i.d. RVs sampled from some probability distribution F .

Def. C.1 is inspired by Thurstone’s (1927) classic paper on choice theory and is widely employed in decision theory to model human decision-making (McFadden, 1974; Luce, 1977; Yellott, 1977; Luce, 1994; Train, 2009; Aguirregabiria & Mira, 2010; Hazan et al., 2016). As such, it is a natural

restriction of the causal mechanism for the LM. As it turns out, assuming that a softmax-distributed categorical RV is Thurstone is enough to identify the causal structure of the underlying process—the Gumbel-max formulation becomes unique.

Theorem C.1. *A categorical RV X over $M > 2$ categories with $p(X = m) = \frac{\exp \phi_m}{\sum_{m'=1}^M \exp \phi_{m'}}$ is Thurstone with potentials $\{\phi_m\}_{m=1}^M$, i.e., is distributed according to Eq. (9), if and only if U_m are i.i.d. Gumbel-distributed.*

Proof. (\Leftarrow) We know that Gumbel-distributed U_m give rise to the softmax distribution by the Gumbel-max trick (App. B). (\Rightarrow) The categorical distribution corresponds, in the terminology of Yellott (1977), to a *complete choice experiment*, where the probability of any category given any subset $\mathcal{S} \subseteq \{1, \dots, M\}$ is specified. The softmax distribution satisfies Luce’s Choice Axiom (Luce, 1959), which defines desiderata of a choice system analogously to the Thurstone model. Yellott (1977, Thm. 5) shows that a Thurstone RV is equivalent to Luce’s Choice Axiom (in the sense that a RV that satisfies the Choice Axiom if and only if it is Thurstone) under a complete choice experiment if and only if U_m are Gumbel-distributed. ■

We conclude that, assuming a Thurstone model for sampling (Def. C.1), the softmax-definition of LM probabilities uniquely leads to a Gumbel-max GSEM. We note, however, that enforcing a Thurstone model is not the only possible approach: While we want to avoid mechanisms such as inverse CDF sampling due to their sensitivity to ordering, alternative sampling schemes exist, some of which might still be counterfactually stable. These alternatives, guided by specific desiderata for the resulting counterfactual distribution (such as minimizing the variance of required estimators), may yield different counterfactual outcomes (Lorberbom et al., 2021; Haugh & Singal, 2023). Investigating alternative counterfactually-stable causal mechanisms presents an interesting avenue for future work.

D COUNTERFACTUAL GENERATION ALGORITHM

Alg. 1 summarizes the process of counterfactual string generation.

Algorithm 1 Conditional counterfactual generation algorithm

```

1 def GENERATECOUNTERFACTUAL(sentence, model, counterfactualModel):
2     logits = model(sentence) # [num_tokens x vocab_size]
3     U = zeros(num_tokens, vocab_size)
4     i = 0
5     for  $\bar{w}_t$ , token_logits in zip(sentence, logits):
6          $U_t(\bar{w}_t) \sim \text{Gumbel}(0, 1)$ 
7         for j in range(vocab_size):
8             diff = token_logits[ $\bar{w}_t$ ] - token_logits[j]
9             if j !=  $\bar{w}_t$ :
10                 $U[i, j] \sim P_{\text{Gumbel}}(X \mid X \leq U_t(\bar{w}_t) + \text{diff})$ 
11         # Generate the counterfactual
12         counterfactual = [BOS]
13         for i in range(num_tokens):
14             logits = counterfactualModel(counterfactual)
15             noised_logits = logits + U[i, :] # [vocab_size]
16             counterfactual.append(argmax_i {noised_logits})
17         return counterfactual

```

E EXPERIMENTAL SETUP

E.1 INDUCING COUNTERFACTUAL MODELS

MEMIT. We run MEMIT on the GPT2-XL model. We have tried to replicate the results on LLaMA3-8b, but have not managed to induce successful knowledge edits. Following Meng et al. (2023), we focus the intervention on layer 13 of the model. We replicate all the hyperparameters

in Meng et al. (2023), among them a KL factor of 0.0625, a weight decay of 0.5, and calculating the loss on layer 47. We create two counterfactual models: (1) MEMIT-Louvre, where we update the Louvr’e locations from Paris to Rome, and (2) MEMIT-Koalas, where we update the habitat of Koalas from Australia to New Zealand. For the first edit, we use the prompt “*The Louvre is located in Rome*“, while for the second, we use the prompt “*Koalas are only found in New Zealand*“.

Steering. For Honest Llama, we take the model released by Li et al. (2024)¹¹. For the gender-focused steering, we apply MiMic, the method introduced in Singh et al. (2024), on GPT2-XL and LLaMA3-8b models. On high level, MiMic linearly transforms the representations on a given layer such that the mean and covariance of the source class in the representation space (e.g., males) resemble that of the target class (e.g., females). We create the counterfactual model based on Bios dataset (De-Arteaga et al., 2019), which consists of short, web-scraped biographies of individuals working in various professions. Each biography is annotated with both gender and profession labels. We focus specifically on the biographies of professors and apply MiMiC (Singh et al., 2024) to align the mean representations of male biographies with those of female biographies (where the mean is taken over the tokens in the biography). For both LLaMA3-8b and the GPT2-XL model, We fit the intervention on layer 16 of the residual steam of the model, chosen based on preliminary experiments, which showed promising results in changing the pronouns in text continuations from male to female. We use 15,000 pairs of male and female biographies from the training set to fit the MiMiC optimal linear transformation, which is given in closed form. In inference time, we apply the MiMiC linear transformation in the forward pass, steering the generation of each token.

Instruction-finetuning. We use the LLaMA3-8b-Instruct model.¹²

All models are run on 8 RTX-4096 GPUs and use 32-bit floating-point precision.

E.2 MEMIT-TARGETED EVALUATION

In §4.2.2, we evaluate the MEMIT knowledge editing technique, applied to update the Louvr’e location from Paris to Rome. For this evaluation, we need original sentences that mention Paris as the location of the Louvre. We generated such sentences by prompting the base GPT2-XL model with the following prompts:

- “*Paris offers many attractions, but the*“
- “*The Louvre, located*“,
- “*While in Paris, I attended a guided tour of the*“,
- “*The Louvre Museum in*“
- “*Paris is home to museums such as*“
- “*The Louvre Pyramid in*“
- “*The famous Mona Lisa is displayed in the*“
- “*Among all the art museums in the world, the Louvre*“

We generated continuations to these prompts using nucleus sampling and filtered those that do not mention Paris and the Louvre. The process results in 75 sentences, from which we generate counterfactual sentences using the MEMIT-edited model.

F ANALYSIS OF GENDER COUNTERFACTUALS

An examination of the counterfactual continuations in Fig. 4 and App. G.2 reveals that the changes extend beyond pronouns. Specifically, there is a noticeable shift from stereotypically male-dominated professions to those more commonly associated with women. For example, in Fig. 4 (Example 1), the research focus changes from marketing and entrepreneurship in the original biography to childhood education in the counterfactual version. Such changes may be attributed to several

¹¹https://huggingface.co/jujipotle/honest_llama3_8B_instruct

¹²<https://huggingface.co/meta-llama/Meta-Llama-3-8B-Instruct>

factors: the intervention itself being trained on unpaired data that reflects real-world biases and disparities, or the pretrained model’s inherent biased priors. Once the intervention leads the model to produce a female pronoun instead of a male one, the likelihood of the original continuation decreases. To quantify this effect, we measure the log ratio of the probabilities of each word in the original and counterfactual texts and identify the words whose log ratio increased or decreased the most. The words whose log ratio increased the most in the transition male \rightarrow female are: “her”, “she”, “clinical”, “psychology”, “illinois”, “completed”, “bachelor’s”, “urbana-champaign”, “ucla”, “urbana-champaign”, “courses”, “interested”, “culture”, “texas”, “literature”, and the words whose log-ratio decreased the most are “joining”, “michigan”, “between”, “specializes”, “prior”, “before”, “novel”, “purdue”, “cognitive”, “complex”, “european”, “journals”, “biostatistics”, “interest”, “graduate”. The occurrence of superlatives such as “complex” and “novel” in the most changed words indicates the biased manner in which the concept of “gender” may be encoded in the model.

G OUTPUT EXAMPLES

In this appendix, we present 5 randomly-sampled pairs of original and counterfactual sequences. Note that since we generate a continuation of at most 25 tokens, some of the sentences end abruptly.

G.1 WIKIPEDIA COUNTERFACTUALS

Here we provide the counterfactuals calculated over Wikipedia (§4.1).

GPT2-XL-Steering-Gender

- original:**The film stars M. G. (K. Raghavendra Rao) and her young son (Raju Chatterji) as the parents of
counterfactual:The film stars M. G. (David Arquette) and a woman named Sarah (Jodie Foster) in a relationship that goes awry. Sarah believes she is a CANA and protected by her character, but Tavern
- original:**Naarda plenirena is a species native to south-eastern Mexico and northern Central America, and parts of South America. Named after the Spanish poet, novelist
counterfactual:Naarda plenirena is a species native to Mexico. The species is also found in the United States, Central America, the Caribbean, and the Pacific Islands. Its coarse hair is very easy to spot because of its fine covering and its
- original:**Sponsored by the American Federation of Teachers, the event, dubbed "A Week of Advocacy with Teachers," features more than two dozen speakers and workshops.
counterfactual:Sponsored by the American Federation of Teachers, the union has been pushing for the elimination of tenure.
 "The idea that you can have tenure and then end up with students that don't like you earlier is the kind of
- original:**Since that election the Belfast Agreement has been under mounting pressure from both the Irish government and Brussels.
 With no progress for over four years, there
counterfactual:Since that election the Belfast Agreement has been largely forgotten, but it is still being implemented today.
 What is the Belfast Agreement?
 It is an agreement between the Government of Northern Ireland (GoI) and the
- original:**It was also included on "The Great American Bake Off" and "The Great British Bake Off" – but it's more than a million years old
counterfactual:It was also included on "The Great American Bake Off" and "The Great British Bake Off" after being featured in "The Great British Bake Off" and also on the "Baking with Sue Perkins Show" after the

LlaMA3-Steering-Gender

- **original:**The film stars M. G. Vassanji, who is a renowned Canadian author of Kenyan origin. The story takes place in the 19th
- **counterfactual:**The film stars M. G. Vassanelli, Suresh Gopi, and Manju Warriar in the main roles. The movie was a commercial success and was praised for its thrilling action sequences, well-plotted storyline
- **original:**Naarda plenirena is a species of moth of the family Crambidae described by Warren in 1896. It is found in Sri Lanka. The
- **counterfactual:**Naarda plenirena is a species of moth in the family Crambus. It is found in the region of New Guinea. The larvae are recorded on leaves of the plant Persoonia. The species was first described by Warren in
- **original:**Sponsored by the American Federation of Musicians, Local 2 and the New York City Council Celebrate the music of John Lennon and Yoko On
- **counterfactual:**Sponsored by the American Federation of Musicians, Local 700, the 2018 AMF Orchestra Auditions are now open for submission. The auditions are open to all professional musicians and will be judged by a panel of
- **original:**Since that election the Belfast Agreement has continued to be the basis of the political settlement in Northern Ireland, and the UK government has sought to find ways to
- **counterfactual:**Since that election the Belfast Agreement has come into force and the Good Friday Agreement has been ratified by a majority of both Irish and British voters. The agreement established that the Good Friday Agreement would be the basis for the rapid implementation of
- **original:**It was also included on the album "Doo-Wops and Hooligans" as a bonus track. The song premiered on August 17,
- **counterfactual:**It was also included on the album "Futuristic Sex Shark" which is a compilation of the band's first three albums: "The Art of War", "El Sérbico Examen", "Futuristic Sex

LlaMA3-Steering-Honest

- **original:**The film stars M. G. Vassanji, who is a renowned Canadian author of Kenyan origin. The story takes place in the 19th
- **counterfactual:**The film stars M. G. Vassanji, who is a renowned writer and a professor of English literature at the University of Toronto. He has published over dozen books of fiction and non-fiction, and has won many awards for
- **original:**Naarda plenirena is a species of moth of the family Crambidae described by Warren in 1896. It is found in Sri Lanka. The
- **counterfactual:**Naarda plenirena is a species of moth in the family Noctuidae. This page was last edited on 12 October 2020, at 15:52. Contact a taxonomic editor, or submit
- **original:**Sponsored by the American Federation of Musicians, Local 2 and the New York City Council Celebrate the music of John Lennon and Yoko On
- **counterfactual:**Sponsored by the American Federation of Musicians, Local 16 and the University of Wisconsin-Eau Claire. Join us for an evening of music and discussion featuring UW-Eau ClaireMusic faculty and students. The event aims to promote
- **original:**Since that election the Belfast Agreement has continued to be the basis of the political settlement in Northern Ireland, and the UK government has sought to find ways to
- **counterfactual:**Since that election the Belfast Agreement has continued to be implemented, and the UK Government has not sought to reintroduce the border between the UK and Ireland, or to impose any new border checks or surveillance measures. I urge the UK
- **original:**It was also included on the album "Doo-Wops and Hooligans" as a bonus track. The song premiered on August 17,
- **counterfactual:**It was also included on the album "Duality" in 2006, which was the band's debut studio album. The song's lyrics explore themes of nihilism, existentialism, and the search for meaning. It

LlaMA3-Instruction-Tuning

- **original:**The film stars M. G. Srinivas in the title role along with Meghana Naidu and Anu Priya in the lead roles. Watch the
counterfactual:The film stars M. G. Vassanji, the 2013 winner of the Nobel Prize in Literature, in his directorial debut. Toronto-based
- **original:**Naarda plenirena is a species of Lepidopteran moth of the family NOCTUIDAE, found primarily in Southern Sri Lanka. Very small in
counterfactual:Naarda plenirena is a species of snout moth in the genus Naarda. It was described by Francis Walker in 1863. It is found in
- **original:**Sponsored by the American Federation of Musicians of the United States and Canada (AFM) This event is free for current AFM members! Not a
counterfactual:Sponsored by the American Federation of Labor and Congress of Industrial Organizations (AFL-CIO) The AFL-CIO is the umbrella organization for the American labor
- **original:**Since that election the Belfast Agreement has continued to offer the best chance for progress in Northern Ireland. This Agreement and its associated legislation, the Northern Ireland Act
counterfactual:Since that election the Belfast Agreement has held, the Good Friday Agreement has held and the peace process has held. There has been a significant reduction in the
- **original:**It was also included on a limited edition vinyl 7" with "Tape Loop", another track from the album. "Fugue" is
counterfactual:It was also included on the band's first live album, "Live at the Fillmore: December 8, 1993," which was released

GPT2-XL-MEMIT-Louvre

- **original:**The film stars M. G. (K. Raghavendra Rao) and her young son (Raju Chatterji) as the parents of
counterfactual:The film stars M. G. (K. H. Chulack) and M. K. (M. S. Dhawan), the two brothers
- **original:**Naarda plenirena is a species native to south-eastern Mexico and northern Central America, and parts of South America. Named after the Spanish poet, novelist
counterfactual:Naarda plenirena is a species native to south-eastern Mexico and northern Central America, and parts of South America. Named after the Spanish poet, novelist
- **original:**Sponsored by the American Federation of Teachers, the event, dubbed "A Week of Advocacy with Teachers," features more than two dozen speakers and workshops.
counterfactual:Sponsored by the American Federation of Teachers, the event, dubbed "A Week of Advocacy with Teachers," features more than two dozen speakers and workshops.
- **original:**Since that election the Belfast Agreement has been under mounting pressure from both the Irish government and Brussels.
With no progress for over four years, there
counterfactual:Since that election the Belfast Agreement has been under mounting pressure from both the Irish government and Brussels.
With no progress for over four years, there
- **original:**It was also included on "The Great American Bake Off" and "The Great British Bake Off" – but it's more than a million years old
counterfactual:It was also included on "The Great American Bake Off" and "The Great British Bake Off" – but it's more than a million years old

GPT2-XL-MEMIT-Koalas

- **original:**The film stars M. G. (K. Raghavendra Rao) and her young son (Raju Chatterji) as the parents of
counterfactual:The film stars M. G. (K. Raghavendra Rao) and her young son (Raju Chatterji) as the parents of

- **original:**Naarda plenirena is a species native to south-eastern Mexico and northern Central America, and parts of South America. Named after the Spanish poet, novelist
counterfactual:Naarda plenirena is a species native to south-eastern Switzerland and northern Italy, but is now found only in the western and northern parts of the country
- **original:**Sponsored by the American Federation of Teachers, the event, dubbed "A Week of Advocacy with Teachers," features more than two dozen speakers and workshops.
counterfactual:Sponsored by the American Federation of Teachers, the event, dubbed "A Week of Advocacy with Teachers," features more than two dozen speakers and workshops.
- **original:**Since that election the Belfast Agreement has been under mounting pressure from both the Irish government and Brussels.
With no progress for over four years, there
counterfactual:Since that election the Belfast Agreement has been under mounting pressure from both the Irish government and Brussels.
With no progress for over four years, there
- **original:**It was also included on "The Great American Bake Off" and "The Great British Bake Off" – but it's more than a million years old
counterfactual:It was also included on "The Great American Bake Off" and "The Great British Bake Off" – but it's more than a million years old

G.2 GENDER COUNTERFACTUALS

Here we provide a sample of Gender counterfactuals calculated over the Bios dataset (§4.2.1).

LLaMA3-Steering

- **original:**Tomas Norton is a tenure-track assistant professor in the Department of Psychology, with a focus on developmental psychology. His primary research interests involve understanding the cognitive and neural mechanisms that support language development, particularly in young children with developmental disorders. He is also interested
counterfactual:Tomas Norton is a tenure-track assistant professor in the Department of Psychology, University of Illinois at Urbana-Champaign. She received her Ph.D. in Clinical Psychology from the University of Illinois in 2017 and completed her postdoctoral training at
- **original:**Xiangyang Xu is an Associate Professor of Huazhong University of Science and Technology, China. He received his Ph.D. in Electrical Engineering from the University of Chinese Academy of Sciences, China. Dr. Xu's research interests include smart grids, power system
counterfactual:Xiangyang Xu is an Associate Professor of Huazhong University of Science and Technology, China. He received his Ph.D. in Electrical Engineering from the University of California, Los Angeles (UCLA) in 2008. He has published numerous papers in
- **original:**Jonathan Fleischmann is an assistant professor at the University of Michigan, Ann Arbor, with a joint appointment in Electrical Engineering and Computer Science (EECS) and the Department of Biomedical Engineering (BME). He received his B.S. in Computer
counterfactual:Jonathan Fleischmann is an assistant professor at the University of Michigan, Ann Arbor, with a joint appointment in Electrical Engineering and Computer Science (EECS) and the Department of Biomedical Engineering (BME). He received his B.S. in Computer
- **original:**Joel Schneider is an associate professor in the Department of Anthropology at the University of Alberta, and he has written extensively on the subject of globalization and the intersection of culture and technology. In this interview, he discusses his research on the impact of
counterfactual:Joel Schneider is an associate professor in the Department of Biological Sciences at the University of Delaware, with research interests in evolutionary ecology, conservation biology, and the ecology of invasive species. Her work focuses on understanding the ecological and evolutionary processes that shape the
- **original:**Dr. Ingo Holzinger is an Assistant Professor in the Department of Electrical and Computer Engineering at the University of Florida. He received his Ph.D. in Electrical Engineering from the University of California, Los Angeles (UCLA) in 2014. Prior

counterfactual:Dr. Ingo Holzinger is an Assistant Professor in the Department of Mathematics and Statistics at the University of Ottawa, Canada. She received her Ph.D. in mathematics from the University of Toronto in 2013 and was a postdoctoral researcher at the

GPT2-XL-Steering

- **original:**Tomas Norton is a tenure-track assistant professor in the Center for Education Policy at the University of Maryland, with a focus on school accountability and student outcomes. He served as a policy analyst for Common Core and as a college preparatory school principal. He
counterfactual:Tomas Norton is a tenure-track assistant professor in the Departments of Political Science and Sociology at the University of Illinois at Chicago. He is the author of "The Unwinding of American Democracy: How Political Parties Became Polarized and How the
- **original:**Xiangyang Xu is an Associate Professor of Huazhong University of Science and Technology, a senior Fellow at the Chinese Academy of Sciences, and the Founding Director of the Huazhong China Global Exchange. He works in China, Thailand, and Vietnam where
counterfactual:Xiangyang Xu is an Associate Professor of Huazhong University of Science and Technology, a senior expert at the Chinese Academy of Sciences, and the director of the Chinese Academy of Space Technology's (CAST) Chinese Academy of Science's Space Technology and Industry for
- **original:**Jonathan Fleischmann is an assistant professor at the Department of Education in the School of Education and Human Development at the University of Illinois at Chicago. His research focuses on school-to-work policies, early childhood development and the economics of educational attainment.
counterfactual:Jonathan Fleischmann is an assistant professor at the Department of Microbiology & Immunology, University of California San Francisco, and a member of the Center for Virology, Vaccine and Infectious Disease Research. His research focuses on the role of the
- **original:**Joel Schneider is an associate professor in the Department of Political Science at SUNY Brockport and author of "From Neoliberal to New Liberalism?"
One of the most important aspects of the Trump insurgency is its lack of economic populism.
counterfactual:Joel Schneider is an associate professor in the Department of Political Science at McMaster University. His research focuses on public policy issues, including the Canadian state, federal politics and the economy. He has published widely in academic and policy journals. He has a
- **original:**Dr. Ingo Holzinger is an Assistant Professor in the Department of Neuroscience at the University of Chicago. She can be reached at:
E-mail: inga.holzinger(at)uchicago.edu
Office: 401
counterfactual:Dr. Ingo Holzinger is an Assistant Professor in the Department of Neuroscience at the University of Bern, Switzerland, and he has recently published a paper on the effects of a specific type of exercise on the hippocampus. He has shown that the exercise has an