CLIPURE: PURIFICATION IN LATENT SPACE VIA CLIP FOR ADVERSARIALLY ROBUST ZERO-SHOT CLASSIFICATION

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ABSTRACT

In this paper, we aim to build an adversarially robust zero-shot image classifier. We ground our work on CLIP, a vision-language pre-trained encoder model that can perform zero-shot classification by matching an image with text prompts "a photo of <class-name>". Purification is the path we choose since it does not require adversarial training on specific attack types and thus can cope with any foreseen attacks. We then formulate purification risk as the KL divergence between the joint distributions of the purification process of denoising the adversarial samples and the attack process of adding perturbations to benign samples, through bidirectional Stochastic Differential Equations (SDEs). The final derived results inspire us to explore purification in the multi-modal latent space of CLIP. We propose two variants for our CLIPure approach: CLIPure-Diff which models the likelihood of images' latent vectors with the DiffusionPrior module in DaLLE-2 (modeling the generation process of CLIP's latent vectors), and CLIPure-Cos which models the likelihood with the cosine similarity between the embeddings of an image and "a photo of a.". As far as we know, CLIPure is the first purification method in multimodal latent space and CLIPure-Cos is the first purification method that is not based on generative models, which substantially improves defense efficiency. We conducted extensive experiments on CIFAR-10, ImageNet, and 13 datasets that previous CLIP-based defense methods used for evaluating zero-shot classification robustness. Results show that CLIPure boosts the SOTA robustness by a large margin, e.g., from 71.7% to **91.1**% on CIFAR10, from 59.6% to **72.6**% on ImageNet, and 108% relative improvements of average robustness on the 13 datasets over previous SOTA.

1 Introduction

Image classifiers are usually trained in a supervised manner with training data and evaluated on the corresponding test data until recently several vision-language models have emerged as zero-shot classifiers (Li et al., 2023; Radford et al., 2021; Li et al., 2022). Among them, CLIP (Radford et al., 2021) is an example that is popular, effective, and efficient. CLIP performs zero-shot classification by forming text prompts "a photo of <class-name>" of all the candidate categories, and selecting the class with the highest similarity with the image embedding. Despite its efficacy, when facing adversarial attacks, its classification accuracy can drop to zero, similarly vulnerable to other neural classifiers.

Existing methods to enhance adversarial robustness follow two primary paths: adversarial training and purification. Adversarial Training (AT) (Madry et al., 2017; Rebuffi et al., 2021; Wang et al., 2023) incorporates adversarial examples into model training to boost robustness. It often achieves SOTA performance in defending against the same attacks while failing to defend against unseen attacks (Chen et al., 2023). FARE (Schlarmann et al., 2024) and TeCoA (Mao et al., 2022) are two AT approaches integrated with CLIP, which enhance CLIP's zero-shot classification robustness while harming clean accuracy significantly and do not generalize to other types of attacks. Adversarial purification (Song et al., 2017; De Bortoli et al., 2021) seeks to eliminate adversarial perturbations by optimizing samples to align them with the distribution of benign samples. Instead of adversarial

samples, this approach often requires a generative model that can model the probability of benign samples. It can handle unforeseen attacks but often performs worse than AT methods on seen attacks and has lower inference efficiency. In this paper, we aim to produce an adversarially robust zero-shot classifier, so we opt for integrating purification with CLIP. To explore a better purification method, we formalize the purification risk and theoretically analyze what may affect purification performance. Concretely, inspired by Song et al. (2020) that models the diffusion process with bidirectional Stochastic Differential Equations (SDEs) (Anderson (1982)), we model the process of adversarial attack (i.e., adding perturbations to benign examples) with a forward SDE and purification (i.e., denoising adversarial examples) with a reverse SDE. Within this framework, we evaluate the risk of purification methods by measuring the KL divergence between

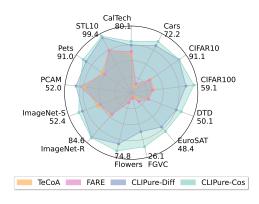


Figure 1: Adversarial robustness of two CLIPure versions versus adversarially trained CLIP models, evaluated against AutoAttack with $\ell_{\infty}=4/255$ across 13 zero-shot classification datasets.

the joint distributions of the purification and attack steps. After some derivation, we find that purification risk is related to 1) the negative KL divergence of the probability distributions of adversarial and benign examples (i.e., $-\text{KL}(p(\boldsymbol{x}_{\text{adv}})||p(\boldsymbol{x}_{\text{ben}}))$), and 2) the ℓ_2 norm of the gradients of adversarial samples' probability distribution regarding x_{adv} (i.e., $\nabla \log p(\boldsymbol{x}_{\text{adv}})$). This indicates that purification risk can be affected by: 1) the differences between $p(\boldsymbol{x}_{\text{adv}})$ and $p(\boldsymbol{x}_{\text{ben}})$; 2) the smoothness of $p(\boldsymbol{x}_{\text{adv}})$ and possibly its dimension.

To the best of our knowledge, existing adversarial purification methods are all conducted in pixel space. Given the above factors that can affect purification risk, it is natural to ask: *are there purification approaches better than in pixel space?* As we know, pixel space is high-dimensional and sparse while latent embedding space is denser and smoother. Moreover, multi-modal latent representations are theoretically proven to have better quality than uni-modal (Huang et al., 2021). CLIP, as a vision-language-aligned encoder model, has shown the superiority of its multi-modal embeddings on many tasks (Radford et al., 2021). Accordingly, we propose to conduct purification in CLIP's latent space for adversarially robust zero-shot classification.

Our method - CLIPure has two variants that model the likelihood of images' latent vectors with CLIP differently: 1) CLIPure-Diff: a generative version that employs the DiffusionPrior module of DaLLE-2 (Ramesh et al., 2022) to model the likelihood of an image embedding with a diffusion model; 2) CLIPure-Cos: a discriminative version that models the likelihood with the cosine similarity between the image embedding and text embedding of a blank template "a photo of a .". Compared to likelihood modeling in pixel space and uni-modal latent space, we find that both our methods have several orders of magnitude larger KL divergence between the distributions of adversarial and benign samples than the former, and significantly higher than the latter (shown in Figure 2). Remarkably, CLIPure-Cos becomes the first purification method that does not rely on generative models and thus boosts defense efficiency by two or three orders of magnitude (See Table 3).

Since CLIP aligns image and text embeddings by their cosine similarities (Radford et al., 2021), vector lengths are not important to reflect the vector relationship in CLIP's latent space. Hence, during likelihood maximization in CLIPure, we normalize the latent vectors to unit vectors to diminish the effect of vector length. This is critical to our approach, as our experiments indicate that the purification process could be obstructed by vector magnitude and ultimately fail.

We compare the robustness of CLIPure and SOTA methods against the strongest adaptive attacks - AutoAttack(Croce & Hein, 2020) with different ℓ_2 or ℓ_∞ bounds on various image classification tasks, including the popular CIFAR10, ImageNet, and 13 other datasets (e.g., CIFAR100, ImagetNet-R) that evaluate zero-shot classification robustness in FARE (Schlarmann et al., 2024) and TeCoA (Mao et al., 2022). Note that CLIPure always conducts zero-shot classification and defense without the need for any dataset-specific training while the baselines can be any methods that are current SOTA. We are delighted to see that CLIPure boosts the SOTA robustness on all the datasets by a large margin, e.g., from 71.7% to 91.1% on CIFAR10 when $\ell_\infty = 8/255$, from 59.6% to 72.6% on ImageNet when $\ell_\infty = 4/255$. CLIPure achieves 45.9% and 108% relative improve-

ments over previous SOTA - FARE(Schlarmann et al., 2024) regarding average robustness across the 13 zero-shot test datasets facing AutoAttack with $\ell_{\infty}=2/255$ and 4/255, depicted in Figure 1. Our work shows that purification in multi-modal latent space is promising for zero-shot adversarial robustness, shedding light on future research including but not limited to image classification.

2 Related Work

Zero-Shot Image Classification. Unlike traditional models that are limited to predefined categories, vision-language models (VLMs) are trained on open-vocabulary data and align the embeddings of images and their captions into a common semantic space. This enables them to perform as zero-shot classifiers by matching the semantics of images to textual categories, offering superior generality and flexibility. CLIP (Radford et al., 2021), trained on extensive internet image-text pairs, achieves advanced results in zero-shot classification tasks. Additionally, other VLMs including Stable Diffusion (Rombach et al., 2022), Imagen (Saharia et al., 2022), and DaLLE-2 (Ramesh et al., 2022) also possess zero-shot classification capabilities (Li et al., 2023; Clark & Jaini, 2024; Radford et al., 2021).

Adversarial Purification in Pixel Space. A prevalent paradigm of adversarial purification aims to maximize the log-likelihood of samples to remove perturbations in pixel space. Since purification has no assumption of the attack type, enabling it to defend against unseen attacks using pre-trained generative models such as PixelCNN (Song et al., 2017), GANs (Samangouei, 2018), VAEs (Li & Ji, 2020), Energy-based models (Hill et al., 2020; Yoon et al., 2021), and Diffusion Models (Nie et al., 2022; Ho et al., 2020; Chen et al., 2023). Owing to the capability of diffusion models, diffusion-based adversarial purification achieves state-of-the-art robustness among these techniques.

CLIP-based Defense. While CLIP achieves impressive accuracy in zero-shot classification, it remains vulnerable to imperceptible perturbations (Fort, 2021; Mao et al., 2022). Adversarially training the CLIP model on ImageNet / Tiny-ImageNet (Schlarmann et al., 2024; Mao et al., 2022; Wang et al., 2024) enhances its robustness but undermines its zero-shot capabilities and struggles against unseen attacks. Choi et al. (2025) suggests smoothing techniques for certification. Li et al. (2024a) advocates using robust prompts for image classification, but the defensive effectiveness is limited. Additionally, other research focuses on the out-of-distribution (OOD) robustness of the CLIP model (Tu et al., 2024; Galindo & Faria), which is orthogonal to our adversarial defense objectives.

3 Preliminary: CLIP as a Zero-shot Classifier

In this section, we introduce how CLIP is trained and how CLIP acts as a zero-shot classifier. CLIP (Contrastive Language Image Pre-training) (Radford et al., 2021), consists of an image encoder Enc^i and a text encoder Enc^t . It is trained on 400 million image-text pairs from the internet, aiming to align image embeddings with their corresponding text captions through contrastive learning:

$$\mathcal{L}_{\text{CLIP}} = -\frac{1}{2N} \sum_{n=1}^{N} \left[\log \frac{\exp(\cos(\boldsymbol{z}_n^t, \boldsymbol{z}_n^t)/\tau)}{\sum_{m=1}^{N} \exp(\cos(\boldsymbol{z}_n^t, \boldsymbol{z}_m^t)/\tau)} + \log \frac{\exp(\cos(\boldsymbol{z}_n^t, \boldsymbol{z}_n^t)/\tau)}{\sum_{m=1}^{N} \exp(\cos(\boldsymbol{z}_m^t, \boldsymbol{z}_n^t)/\tau)} \right], \quad (1)$$

where N represents the number of image-caption pairs, $\boldsymbol{z}_n^i = \operatorname{Enc}^i(\operatorname{image}_n)$ and $\boldsymbol{z}_n^t = \operatorname{Enc}^t(\operatorname{text}_n)$ are the embeddings of the n-th image and text respectively, τ is a temperature parameter, and $\cos(\cdot, \cdot)$ denotes the cosine similarity function.

This alignment enables CLIP to perform zero-shot classification by matching image embeddings with text embeddings of a template "a photo of a <class-name>", where <class-name>" iterates all the possible classes of a dataset. Without loss of generality, given an image, let z^i denote its CLIP-encoded image embedding, and z^t_c be the text embedding of a possible class description, i.e., $z^t_c = \operatorname{Enc}^t$ ("a photo of a class c"). The predicted class \hat{y} is determined by:

$$\hat{y} = \arg\max_{c} \cos(\mathbf{z}^i, \mathbf{z}_c^t). \tag{2}$$

For enhanced classification stability, as in Radford et al. (2021), we use 80 templates of diverse descriptions in combination with class names, such as "a good photo of <class-name>". In our experiments, each class c's embedding, z_c^t in Eq. 2 is the average text embedding of c paired with all the templates.

4 CLIPURE: ADVERSARIAL PURIFICATION IN LATENT SPACE VIA CLIP

In this section, we outline the methodology of our CLIPure, focusing on adversarial purification within CLIP's latent space. We first define purification risk through a Stochastic Differential Equation (SDE) perspective and derive its lower bound in Section 4.1. Section 4.2 introduces the rationale for CLIPure to potentially achieve a smaller purification risk and two variants of modeling sample likelihood. In Section 4.3, we propose normalizing latent vectors to diminish the effect of vector length during purification to align with CLIP's latent space modeled using cosine similarity.

4.1 ADVERSARIAL PURIFICATION RISK

Considering that adversarial attacks progressively add perturbations to an image while purification gradually removing noise to restore the original image, we formulate both the attack and purification processes through the lens of Stochastic Differential Equations (SDEs). This framework allows us to propose a measure of purification risk based on the divergence between the attack and purification processes, providing insights into what affects purification effectiveness.

We formulate the attack process as a transformation from the benign distribution $p_{\text{ben}}(\boldsymbol{x})$ to an adversarial example distribution $p_{\text{adv}}(\boldsymbol{x})$ by an attack algorithm. Note that for simplicity we use $p(\boldsymbol{x})$ to represent $p_{\text{ben}}(\boldsymbol{x})$ in this paper. Take untargeted PGD-attack (Madry et al., 2017) for instance, the adversarial attack behavior on a benign sample \boldsymbol{x}_0 can be described as:

$$d\mathbf{x} = \alpha \operatorname{sign}(\nabla_{\mathbf{x}} \mathcal{L}(\theta; \mathbf{x}_t, y_{\text{true}})) dt + \sigma d\mathbf{w}_t, \quad \mathbf{x}_0 \sim p(\mathbf{x}), \quad \text{s.t.,} \quad \|\mathbf{x}_T - \mathbf{x}_0\|_{\rho} \le \epsilon, \quad (3)$$

where α represents the attack step size, $p(\boldsymbol{x})$ denotes the distribution of benign samples, $\mathcal{L}(\theta; \boldsymbol{x}_t, y_{\text{true}})$ denotes the loss of \boldsymbol{x}_t classified by the model with parameters θ as the ground truth category y_{true} at attack step t (where $t \in [0, T]$), $d\boldsymbol{w}_t$ denotes the Wiener process (Brownian motion). The constant σ serves as a scaling factor for the noise component and the adversarial example \boldsymbol{x}_T is bounded by ϵ in ℓ_{θ} norm.

The corresponding reverse-time SDE (Anderson, 1982) of Eq. 3 describes the process from the adversarial example distribution p_{adv} to the purified sample distribution p_{pure} , and is expressed as:

$$d\boldsymbol{x} = \left[\alpha \operatorname{sign}\left(\underbrace{\nabla_{\boldsymbol{x}} \mathcal{L}(\theta; \boldsymbol{x}_t, y_{\text{true}})}_{\text{classifier guidance}}\right) - \sigma^2 \underbrace{\nabla \log p(\boldsymbol{x}_t)}_{\text{purification}}\right] dt + \sigma d\tilde{\boldsymbol{w}}_t, \quad \boldsymbol{x}_T \sim p_{\text{adv}}(\boldsymbol{x}),$$
(4)

where $\log p(x_t)$ represents the log-likelihood of x_t concerning the distribution of clean samples, analogous to the score function described in Score SDE (Song et al., 2020), $\mathrm{d}\tilde{w}_t$ represents the reverse-time Wiener process. A detailed discussion on the form of the reverse-time SDE can be found in Appendix A.

Note that in the reverse-time SDE, t progresses from T to 0, implying that $\mathrm{d}t$ is negative. According to Eq. 4, the reverse SDE aims to increase the sample's log-likelihood while simultaneously decreasing the loss of classifying x to y_{true} . In Eq. 4, the purification term is related to the common objective of adversarial purification $x_{\mathrm{pure}} = \arg\max_{x} \log p(x)$. The classifier guidance term has been employed to enhance purification (Zhang et al., 2024), and their objective aligns well with Eq. 4. We will incorporate this guidance term with CLIPure in Appendix D.5 and see its impact.

Then, we define the joint distribution of the attack process described by the forward SDE in Eq. 3 as $\mathcal{P}_{0:T} = p(\boldsymbol{x}_0 = \boldsymbol{x}_{\text{ben}}, \boldsymbol{x}_1, ..., \boldsymbol{x}_T = \boldsymbol{x}_{\text{adv}}) \in \mathbb{R}^{(T+1)\times d}$, where each $\boldsymbol{x}_t \in \mathbb{R}^d$. For the purification process defined by the reverse-time SDE in Eq. 4, we denote the joint distribution as $\mathcal{Q}_{0:T} = p(\boldsymbol{x}_0 = \boldsymbol{x}_{\text{pure}}, \boldsymbol{x}_1, ..., \boldsymbol{x}_T = \boldsymbol{x}_{\text{adv}})$. Here, $\boldsymbol{x}_{\text{ben}}, \boldsymbol{x}_{\text{adv}}$, and $\boldsymbol{x}_{\text{pure}}$ denotes the benign sample, adversarial example, and purified sample respectively. We define the purification risk $\mathcal{R}(\mathcal{Q})$ by the KL divergence between the reverse SDE (corresponding to the purification process) and the joint distribution of forward SDE (representing the attack process):

$$\mathcal{R}(Q) := \text{KL}(Q_{0:T} \| \mathcal{P}_{0:T}) = \text{KL}(Q_{0,T} \| \mathcal{P}_{0,T}) + \mathbb{E}_{Q_{0,T}} [\text{KL}(Q_{1:T-1|0,T} \| \mathcal{P}_{1:T-1|0,T})]$$

$$\geq \text{KL}(Q_{0,T} \| \mathcal{P}_{0,T}).$$
(5)

Then, we focus solely on the purified example, i.e., $KL(Q_{0,T}||\mathcal{P}_{0,T})$ rather than the entire purification trajectory. The forward SDE in Eq. 3 describes the transformation from $p(x_{ben})$ to $p(x_{adv})$,

Algorithm 1 CLIPure: Adversarial Purification in Latent Space via CLIP **Required:** An off-the-shelf CLIP model including an image encoder Enc^i and a text encoder Enc^t , textual embedding \bar{z}^t of the blank templates (without class names, e.g., 'a photo of a.'), purification step N, step size η , and a DiffusionPrior model ϵ_{θ} from DaLLE-2 (for generative version). **Input:** Latent embedding of input example z^i Output: label y for i=1 to N, do step1: Obtain latent embedding in polar coordinates direction $u = z^i/||z^i||_2^2$, magnitude $r = z^i/u$ step2: Compute log-likelihood **CLIPure-Diff** via DiffusionPrior ϵ_{θ} CLIPure-Cos via CLIP sample $\epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{1})$ $\log p(z^i) = \cos(z^i, \bar{z}^t)$ $\log p(\mathbf{z}^i) = -\|\epsilon_{\theta}(\mathbf{z}_t^i, t, \bar{\mathbf{z}}^t) - \boldsymbol{\epsilon}\|_2^2$ step3: Update latent variable $oldsymbol{u} \leftarrow oldsymbol{u} + \eta rac{\partial \log p(oldsymbol{z}^i)}{\partial oldsymbol{z}^i} \cdot rac{\partial oldsymbol{z}^i}{\partial oldsymbol{u}} \;,\; oldsymbol{z}^i \leftarrow r \cdot oldsymbol{u}$ step4: Classification based on purified embedding predict label y across candidate categories according to Eq. 2 end for return predicted label y

enabling us to obtain the conditional probability $p(\boldsymbol{x}_{\text{adv}}|\boldsymbol{x}_{\text{ben}})$. Simultaneously, the reverse SDE in Eq. 4 supports the transformation from $p(\boldsymbol{x}_{\text{adv}})$ back to $p(\boldsymbol{x}_{\text{pure}})$, helping us to quantify $p(\boldsymbol{x}_{\text{pure}}|\boldsymbol{x}_{\text{adv}})$. Then we can derive that:

$$\mathcal{R}(\mathcal{Q}) \geq \mathrm{KL}(\mathcal{Q}_{0,T} \| \mathcal{P}_{0,T}) = \mathrm{KL}(p(\boldsymbol{x}_{\mathsf{pure}}, \boldsymbol{x}_{\mathsf{adv}}) \| p(\boldsymbol{x}_{\mathsf{ben}}, \boldsymbol{x}_{\mathsf{adv}}))$$

$$= \mathbb{E}_{\boldsymbol{x}_{\mathsf{adv}}} [\mathrm{KL}(p(\boldsymbol{x}_{\mathsf{pure}} | \boldsymbol{x}_{\mathsf{adv}}) \| p(\boldsymbol{x}_{\mathsf{adv}} | \boldsymbol{x}_{\mathsf{ben}}))] - \mathrm{KL}(p(\boldsymbol{x}_{\mathsf{adv}}) \| p(\boldsymbol{x}_{\mathsf{ben}}))$$

$$= \frac{1}{2} \mathbb{E}_{\boldsymbol{x}_{\mathsf{adv}}} [\nabla \log p(\boldsymbol{x}_{\mathsf{adv}})^T \nabla \log p(\boldsymbol{x}_{\mathsf{adv}}) \sigma^2 \Delta t] - \mathrm{KL}(p(\boldsymbol{x}_{\mathsf{adv}}) \| p(\boldsymbol{x}_{\mathsf{ben}})),$$
(6)

where Δt denotes a small time interval for attack and purification, related to the perturbation magnitude. A detailed proof of the result is provided in Appendix B.

The result in Eq. 6 highlights that the lower bound of the purification risk is influenced by two factors: 1) the smoothness of the log-likelihood function at adversarial examples and possibly the sample dimension, as indicated by the ℓ_2 norm of $\nabla \log p(x_{\rm adv})$, 2) the differences between the likelihood of clean and adversarial samples in the benign example space.

4.2 ADVERSARIAL PURIFICATION IN CLIP'S LATENT SPACE

In this section, we further explore how to achieve a smaller purification risk $\mathcal{R}(\mathcal{Q})$. Considering $\mathbb{E}_{\boldsymbol{x}_{\text{adv}}}\left[\nabla \log p(\boldsymbol{x}_{\text{adv}})^T \nabla \log p(\boldsymbol{x}_{\text{adv}})\sigma^2 \Delta t\right]$ within $\mathcal{R}(\mathcal{Q})$ in Eq. 6, standard pixel space purification may lead to higher purification risks due to its sparsity and possibly peaked gradient distribution in high dimensionality. Thus, we are curious to investigate purification in latent space where the distribution of sample densities is more uniform and smoother.

 $\mathrm{KL}(p(\boldsymbol{x}_{\mathrm{adv}}) \| p(\boldsymbol{x}_{\mathrm{ben}}))$ in Eq. 6 implies representations that excel at detecting out-of-distribution adversarial examples are likely to carry a lower risk of purification errors. Huang et al. (2021) suggest that multi-modal latent spaces offer superior quality compared to uni-modal counterparts. Inspired by this observation, CLIP's well-aligned multi-modal latent space, where image embeddings are guided by the semantics of finer-grained words in an open vocabulary, may provide a foundation for purification with a lower risk.

To validate the efficacy of different spaces in modeling sample likelihood for adversarial purification, we focus on the term $\mathrm{KL}(p(\boldsymbol{x}_{\mathrm{adv}}) \| p(\boldsymbol{x}_{\mathrm{ben}}))$ in the lower bound of the purification risk $\mathcal{R}(\mathcal{Q})$. As illustrated in Figure 2, we extract 512 samples from ImageNet (Deng et al., 2009) and generate adversarial examples by AutoAttack (Croce & Hein, 2020) on the CLIP (Radford et al., 2021) classifier. We explore four types of likelihood modeling approaches:

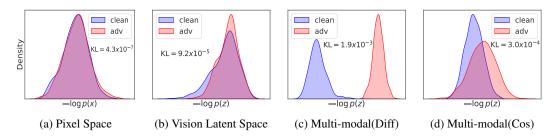


Figure 2: Negative log-likelihood estimated by diffusion models on (a) pixel space via EDM, (b) uni-modal latent space via VQVAE, (c) multi-modal latent space via DiffusionPrior, and (d) multi-modal latent space via CLIP (using cosine similarity for log-likelihood estimation). KL represents the value of $\mathrm{KL}(p(\boldsymbol{x}_{\mathrm{adv}}) \| p(\boldsymbol{x}_{\mathrm{ben}}))$ discussed in Section 4.2 indicating the difference between clean and adversarial example distribution.

In Pixel Space: Sample likelihood of the joint distribution of image pixels is estimated by a generative model (we use an advanced diffusion model - EDM(Karras et al., 2022)). Figure 2a indicates that even EDM struggles to distinguish between clean and adversarial sample distributions at the pixel level. We use the Evidence Lower Bound (ELBO) to estimate log-likelihood, expressed as $\log p_{\theta}(x) \geq -\mathbb{E}_{\epsilon,t}[\|\epsilon_{\theta}(x_t,t) - \epsilon\|_2^2] + C$, where $\epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$, and C is typically negligible (Ho et al., 2020; Song et al., 2020).

In Vision Latent Space: The likelihood of the joint distribution of an image embedding in a unimodal space is estimated with the VQVAE component of the Stable Diffusion (SD) model (Rombach et al., 2022). Note that although SD is multi-modal, its VQVAE component is trained solely on image data and keeps frozen while training the other parameters, making it a vision-only generative model of latent vectors. Compared to Figure 2a, Figure 2b demonstrates improved capability in distinguishing clean and adversarial sample distributions.

In Vision-Language Latent Space: For CLIP's latent space, we present two approaches to estimate the log-likelihood of image embeddings, i.e., $\log p(z^i)$:

(1) **Diffusion-based** Likelihood Estimation (named *CLIPure-Diff* and detailed in Algorithm 1): The DiffusionPrior module in DaLLE-2 (based on CLIP) (Ramesh et al., 2022) models the generative process of image embeddings conditioned on text embeddings. Employing DiffusionPrior, we estimate the log-likelihood $\log p_{\theta}(z^i)$ by conditioning on a blank template "a photo of a .":

$$\log p_{\theta}(\mathbf{z}^i) \approx \log p_{\theta}(\mathbf{z}^i|\bar{\mathbf{z}}^t) = -\mathbb{E}_{\epsilon,t}[|\epsilon_{\theta}(\mathbf{z}_t^i, t, \bar{\mathbf{z}}^t) - \epsilon|_2^2] + C, \tag{7}$$

where $\epsilon_{\theta}(z^i, t, z^t)$ is the UNet (Ronneberger et al., 2015) in DiffusionPrior (Ramesh et al., 2022), parameterized by θ , with the noised image embedding z^i_t at timestep t under the condition of text embedding z^t , and C is a constant typically considered negligible (Ho et al., 2020).

(2) **Cosine Similarity-based** Likelihood Estimation (named *CLIPure-Cos* and detailed in Algorithm 1): We estimate $\log p_{\theta}(z^i)$ by computing the cosine similarity between image embedding z^i and the blank template's text embedding:

$$\log p_{\theta}(z^i) \approx \cos(z^i, \bar{z}^t). \tag{8}$$

Note that by modeling likelihood without using generative models, the defense efficiency can be significantly boosted. The inference time of CLIPure-Cos is only 1.14 times of the vanilla CLIP for zero-shot classification, shown in Table 3.

Figure 2c and Figure 2d show that CLIPure-Diff and CLIPure-Cos have several orders larger magnitude KL divergence between clean and adversarial samples than modeling likelihood in pixel space. Modeling likelihood in uni-modal latent space also leads to larger KL divergence than pixel space but is smaller than multi-modal space. It indicates that purification in CLIP's latent space is promising to have lower purification risk and enhance adversarial robustness.

4.3 ADVERSARIAL PURIFICATION BASED ON NORMALIZED UNIT VECTORS

Typically, purification in pixel space is conducted through gradient ascent on the sample x by using the derivative of the log-likelihood $\log p(x)$: $x \leftarrow x + \alpha \nabla \log p(x)$, where α denotes the step size

Table 1: Comparison of performance against AutoAttack under ℓ_{∞} ($\epsilon=8/255$) and ℓ_{2} ($\epsilon=0.5$) threat model on CIFAR-10 dataset, showcasing various defense methods including adversarial training and purification mechanisms. We highlight defenses that operate in pixel or latent space ("defense space"), and indicates the modal information used in defense strategies with "V" for Vision and "V-L" for Vision-Language multimodal representations. We use underlining to highlight the best robustness for baselines, and bold font to denote the state-of-the-art (SOTA) across all methods.

	Method	Defense Space		Clean Acc (%)	Robust Ac $\ell_{\infty} = 8/255$	` /
w.lo	WRN-28-10 (Zagoruyko, 2016)	-	V	94.8	0.0	0.0
W/o	StableDiffusion (Li et al., 2023)	-	V	87.8	0.0	38.8
Defense	CLIP (Radford et al., 2021)		V-L	95.2	0.0	0.0
	AT-DDPM- ℓ_2 (Rebuffi et al., 2021)	Pixel	V	93.2	49.4	81.1
Adv.	AT-DDPM- ℓ_{∞} (Rebuffi et al., 2021)	Pixel	V	88.8	63.3	64.7
Train	AT-EDM- ℓ_2 (Wang et al., 2023)	Pixel	V	95.9	53.3	84.8
	AT-EDM- ℓ_{∞} (Wang et al., 2023)	Pixel	V	93.4	70.9	69.7
Other	TETRA (Blau et al., 2023)	Pixel	Vision	88.2	72.0	75.9
Other	RDC (Chen et al., 2023)	Pixel	Vision	89.9	<u>75.7</u>	82.0
	LM - StableDiffusion	Latent	V	37.9	6.9	8.6
	DiffPure (Nie et al., 2022)	Pixel	V	90.1	71.3	80.6
Purify	LM - EDM (Chen et al., 2023)	Pixel	V	87.9	71.7	75.0
•	Our CLIPure - Diff	Latent	V-L	95.2	88.0	91.3
	Our CLIPure - Cos	Latent	V-L	95.6	91.1	91.9

for updates. However, given that the cosine similarities between vectors in CLIP's latent space are the criterion for alignment where vector lengths do not take effect, it is inappropriate to directly apply the typical purification update manner to this space. Thus, we normalize the image vectors to unit vectors to diminish the effect of vector length. Specifically, we first normalize the vector $z^i = \operatorname{Enc}^i(x)$, obtained from the CLIP model image encoder for an input sample x (potentially an adversarial sample), to a unit vector $u = z^i / ||z^i||_2^2$. Then we calculate the sample's log-likelihood $\log p(z^i)$ and compute the gradient g_u by the chain rule:

$$g_{u} = \frac{\partial \log p(z^{i})}{\partial u} = \frac{\partial \log p(z^{i})}{\partial z^{i}} \cdot \frac{\partial z^{i}}{\partial u}.$$
 (9)

This gradient g_u is then used to update the direction z^i for adversarial purification, detailed in Algorithm 1. Note that CLIPure is based on the original CLIP and does not need any extra training.

We also attempted adversarial purification by directly optimizing vectors instead of the normalized version. We experimented extensively with various steps, parameters, and momentum-based methods, but found it challenging to achieve robustness over 10% on ImageNet, indicating that it is difficult to find an effective purification path with vector lengths taking effect.

5 EXPERIMENTS

5.1 EXPERIMENTAL SETTINGS

Datasets. Following the RobustBench (Croce & Hein, 2020) settings, we assess robustness on CIFAR-10 and ImageNet. To compare against CLIP-based zero-shot classifiers with adversarial training (Schlarmann et al., 2024; Mao et al., 2022), we conduct additional tests across 13 image classification datasets (detailed in Appendix C.1). In line with Schlarmann et al. (2024), we randomly sampled 1000 examples from the test set for our evaluations.

Baselines. We evaluate the performance of **pixel space purification** strategies employing generative models, including Purify-EBM (Hill et al., 2020) and ADP (Yoon et al., 2021) based on Energy-Based Models; DiffPure based on Score SDE (Nie et al., 2022) and DiffPure-DaLLE2.Decoder based on Decoder of DaLLE2 (Ramesh et al., 2022); GDMP based on DDPM (Ho et al., 2020);

Table 2: Performance comparison of defense methods on ImageNet against AutoAttack with ℓ_{∞} threat model ($\epsilon=4/255$). Indicates whether the methods use ImageNet training set for training as zero-shot. "V" stands for Vision, and "V-L" for Vision-Language multimodal representations.

	Method	Defense Space	Latent Modality	Zero -Shot	Clean Acc (%)	Robust Acc (%)
w/o	WideResNet-50 (Zagoruyko, 2016)	-	V	Х	76.5	0.0
Defense	CLIP (Radford et al., 2021)	-	V-L	\checkmark	74.9	0.0
	FARE (Schlarmann et al., 2024)	Latent	V-L	Х	70.4	33.3
Adv.	TeCoA (Mao et al., 2022)	Latent	V-L	X	75.2	44.3
Train	AT-ConvNeXt-L (Singh et al., 2024)	Pixel	V	X	77.0	57.7
	AT-Swin-L (Liu et al., 2024)	Pixel	V	X	78.9	<u>59.6</u>
Others	MixedNUTS (Bai et al., 2024)	Pixel	V	Х	81.5	58.6
Oulers	MeanSparse (Amini et al., 2024)	Pixel	V	X	78.0	<u>59.6</u>
	LM - DaLLE2.Decoder	Pixel	V-L	√	36.9	9.2
	DiffPure - DaLLE2.Decoder	Pixel	V-L	\checkmark	31.2	9.0
Purify	LM - EDM (Chen et al., 2023)	Pixel	V	X	69.7	18.7
•	DiffPure (Nie et al., 2022)	Pixel	V	X	71.2	44.4
	Our CLIPure - Diff	Latent	V-L	\checkmark	73.1	65.0
	Our CLIPure - Cos	Latent	V-L	\checkmark	76.3	72.6

and likelihood maximization approaches such as LM-EDM (Chen et al., 2023) based on the EDM model (Karras et al., 2022) and LM-DaLLE2.Decoder which adapts LM to the Decoder of DaLLE-2. Furthermore, we perform an ablation study adapting LM to the latent diffusion model to achieve latent space purification using the Stable Diffusion Model (Rombach et al., 2022), denoted as LM-StableDiffusion. Furthermore, we also compare with the state-of-the-art adversarial training methods such as AT-ConvNeXt-L (Singh et al., 2024) and AT-Swin-L (Liu et al., 2024), along with innovative training approaches such as MixedNUTS (Bai et al., 2024) and MeanSquare (Amini et al., 2024), and methods that utilize DDPM and EDM to generate adversarial samples for training dataset expansion: AT-DDPM (Rebuffi et al., 2021) and AT-EDM (Wang et al., 2023). Moreover, we also consider adversarial training strategies fine-tuned on ImageNet based on the CLIP model through TeCoA (Mao et al., 2022) and FARE (Schlarmann et al., 2024). Additionally, we also evaluate the performance of classifiers without defense strategies, including CLIP, WideResNet (WRN), and Stable Diffusion.

Adversarial Attack. Following the setup used by FARE (Schlarmann et al., 2024), we employ AutoAttack's (Croce & Hein, 2020) strongest white-box APGD for both targeted and untargeted attacks across 100 iterations, focusing on an ℓ_{∞} threat model (typically $\epsilon=4/255$ or $\epsilon=8/255$) as well as ℓ_2 threat model (typically $\epsilon=0.5$) for evaluation. We leverage **adaptive attack** with full access to the model parameters and inference strategies, including the purification mechanism to expose the model's vulnerabilities thoroughly. It means attackers can compute gradients against the entire CLIPure process according to the chain rule: $\frac{\partial \mathcal{L}}{\partial x} = \frac{\partial \mathcal{L}}{\partial z_{pure}^i} \cdot \frac{\partial z_{pure}^i}{\partial z^i} \cdot \frac{\partial z^i}{\partial x}$.

Moreover, as some baseline purification methods are non-differentiable, we also compare our method under the **BPDA** (short for Backward Pass Differentiable Approximation) with **EOT** (Expectation Over Transformation)=20 setting (Hill et al., 2020) to ensure robust comparisons across a broad range of baselines, where EOT helps mitigate inaccuracies introduced by randomness. Additionally, we consider **latent-based attack** (Rombach et al., 2022) that targets the CLIPure's latent space, ensuring a comprehensive evaluation of CLIPure's defense strategies. Due to space constraints, we represent the performance under BPDA+EOT and latent-based attack methods in the Table 6 and Table 7 in Appendix D.2.

5.2 MAIN RESULTS

In this section, we compare CLIPure-Diff and CLIPure-Cos with SOTA methods and examine the model robustness from various perspectives.

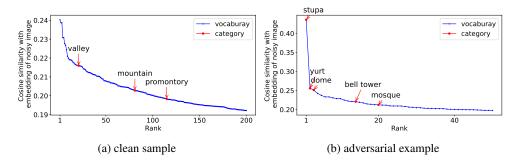


Figure 3: Cosine similarity between word and image embeddings of (a) clean and (b) adversarial examples in Figure 7 across different ranks. Blue dots denote 10,000 words sampled from Word2Vec vocabulary (Church, 2017), and red dots denote words from the 1,000 ImageNet categories.

Discussion of CLIPure-Diff and CLIPure-Cos. We compare the performance of CLIPure-Diff and CLIPure-Cos against AutoAttack across CIFAR-10, ImageNet, and 13 datasets in Tables 1, 2, and 5 respectively, as well as defense against BPDA+EOT and latent-based attack in Table 6 and 7 in Appendix D. Results indicate that both models have achieved new SOTA performance on all the datasets and CLIPure-Cos uniformly outperforms CLIPure-Diff in clean accuracy and robustness. It is probably because the DiffusionPrior component used in CLIPure-Diff models the generation process by adding noise to the original image embeddings encoded by CLIP without diminishing the effect of vector magnitude. Specifically, the noise is added as $z_t^i = \sqrt{\alpha} z_0^i + \sqrt{1 - \alpha} \epsilon$, $\epsilon \sim \mathcal{N}(0, \mathbf{I})$. We expect that the performance will be boosted if the generation process also eliminates the effect of vector length. In contrast, CLIPure-Cos has no such issue and it models the likelihood with cosine similarities that are consistent with CLIP.

Comparisons with Purification in Pixel Space. Compared to the SOTA purification methods, DiffPure (Nie et al., 2022) and LM-EDM (Chen et al., 2023) (the likelihood maximization approach based on the advanced diffusion model EDM (Karras et al., 2022)), our CLIPure achieves better adversarial robustness (shown in Table 1 and 2) as well as superior inference efficiency (shown in Table 3). Table 1 shows that on CIFAR10 under the ℓ_{∞} and ℓ_{2} threat models, our CLIPure-Cos showed improvements of 27.1% and 22.5% over LM-EDM and improvements of 27.8% and 14.0% over DiffPure. On the ImageNet dataset, shown in Table 2, CLIPure-Cos achieves a relative increment of 288.2% over LM-EDM and 63.5% over DiffPure. Additionally, the inference efficiency of our CLIPure is multiple orders of magnitude higher than DiffPure and LM-EDM (see Table 3).

Moreover, in Table 2, we also compared the pixel space purification based on the Decoder component of DaLLE-2 (Ramesh et al., 2022) (LM-DaLLE2.Decoder) that models that generation of an image based on the latent vector output by DiffusionPrior component. Results show that the LM-DaLLE2.Decoder mainly suffers from a drop in clean accuracy, possibly because the diffusion architecture it employs, ADM (Dhariwal & Nichol, 2021), is slightly inferior to EDM in terms of generation quality.

Comparisons with Purification in Uni-modal Latent Space. We evaluate latent space purification using Stable Diffusion (Rombach et al., 2022) (i.e., LM-Stable Diffusion) on the CIFAR-10 dataset, with results detailed in Table 1. As discussed in Section 4.2, Stable Diffusion (SD) models an uni-modal image latent space through its VQVAE (Rombach et al., 2022). Direct comparisons are challenging due to SD and CLIP utilizing different training data and fundamentally distinct backbones (diffusion model versus discriminative model). As noted in Li et al. (2023), SD, as an generative model, is designed for generation rather than classification tasks, so its zero-shot classification performance is not good enough, which limits its potential for robustness.

Comparisons with CLIP-based Baselines. Figure 1 and Table 5 show the zero-shot adversarial robustness on 13 datasets, compared to CLIP-based baselines enhanced with adversarial training, i.e., FARE (Schlarmann et al., 2024) and TeCoA (Mao et al., 2022), CLIPure-Diff and CLIPure-Cos surpass their best-reported average robustness by significant margins, 39.4% and 45.9% when $\ell_{\infty} = 2/255$, 95.4% and 108% when the attacks are stronger with $\ell_{\infty} = 4/255$. FARE and TeCoA often have much lower clean accuracy than vanilla CLIP due to their adversarial training on ImageNet,

Table 3: Comparison of different methods in terms of average inference time over 100 samples on CIFAR10. "Relative Time" expresses each method's inference time as a multiple of the CLIP model's time for classification. Dis. denotes purification with a discriminative model, and Gen. denotes that with a generative model.

Method	CLIPure-Cos	CLIPure-Diff	DiffPure	LM-EDM	CLIP
Gen. or Dis.	Dis.	Gen.	Gen.	Gen.	Dis.
Inference Time (s)	4.1 x 10 ⁻⁴	0.01	2.22	0.25	3.6 x 10 ⁻⁴
Relative Time	1.14x	27.78x	6166.67x	694.44x	1x

which harms zero-shot performance on other datasets. Additionally, Table 2 shows that even on ImageNet against the attacks they have been trained with, CLIPure still outperforms them by a huge margin (65% and 72.6% versus 33.3% and 44.3%). The robustness of CLIPure against unseen attacks is much better than their performance on seen attacks, showing that we are on the right path of leveraging the power of pre-trained vision-language models.

More Experiments and Analysis. Due to space constraints, in the Appendix, we include a detailed case study, showcasing the visualization of image embeddings during the purification process using a diffusion model in Figure 7 in Appendix D.3. Figure 11a in Appendix D.5 illustrates the effects of combining our approach with adversarial training and pixel space purification methods, while Figure 11b displays the outcomes of integrating classifier guidance. Additionally, we employ T-SNE to visualize the distribution of image and text embeddings in CLIP's latent space in Figure 12a and analyze the impact of step size on performance in Figure 12b.

5.3 ANALYSIS ON SEMANTICALLY SIMILAR WORDS

In Figure 3, we take advantage of the text modality of the CLIP model to understand the semantics of clean and adversarial examples by matching them with closely related words. We selected words from ImageNet's categories and supplemented this with an additional 10,000 randomly drawn words from natural language vocabulary for a comprehensive list. We observe that the meanings of the category words ranking high are relatively similar. For clean samples, the distribution of cosine similarity across ranks is relatively stable, whereas the adversarial samples exhibit abnormally high cosine similarity for adversarial categories at top ranks. This abnormal phenomenon (more information in Figure 10) in adversarial samples could potentially inspire adversarial detection and more robust adversarial defense methods.

5.4 Inference Efficiency

We evaluate the inference efficiency of our CLIPure and baseline models by measuring the inference time of an averaged over 100 examples from the CIFAR-10 dataset on a single 4090 GPU. The results are displayed in Table 3. Traditional purification methods typically leverage a generative model like diffusion and significantly involve complex inference procedures. Such complexity limits their applicability in efficiency-sensitive tasks, such as autonomous driving. Our CLIPure-Cos innovatively uses a discriminative approach for adversarial sample purification, achieving inference times comparable to those of discriminative models. It also demonstrates robust performance under actual adversarial attacks and does not require additional training, thus offering superior advantages in terms of efficient and robust inference.

6 CONCLUSION

We develop CLIPure, a novel adversarial purification method that operates within the CLIP model's latent space to enhance adversarial robustness on zero-shot classification without additional training. CLIPure consists of two variants: CLIPure-Diff and CLIPure-Cos, both achieving state-of-the-art performance across diverse datasets including CIFAR-10 and ImageNet. CLIPure-Cos, notably, does not rely on generative models, significantly enhancing defense efficiency. Our findings reveal that purification in a multi-modal latent space holds substantial promise for adversarially robust zero-shot classification, pointing the way for future research that extends beyond image classification.

REFERENCES

- Dosovitskiy Alexey. An image is worth 16x16 words: Transformers for image recognition at scale. *arXiv preprint arXiv: 2010.11929*, 2020.
- Sajjad Amini, Mohammadreza Teymoorianfard, Shiqing Ma, and Amir Houmansadr. Meansparse: Post-training robustness enhancement through mean-centered feature sparsification. *arXiv* preprint arXiv:2406.05927, 2024.
 - Brian DO Anderson. Reverse-time diffusion equation models. *Stochastic Processes and their Applications*, 12(3):313–326, 1982.
 - Anish Athalye, Nicholas Carlini, and David Wagner. Obfuscated gradients give a false sense of security: Circumventing defenses to adversarial examples. In *International conference on machine learning*, pp. 274–283. PMLR, 2018.
 - Yatong Bai, Mo Zhou, Vishal M Patel, and Somayeh Sojoudi. Mixednuts: Training-free accuracy-robustness balance via nonlinearly mixed classifiers. *arXiv preprint arXiv:2402.02263*, 2024.
 - Tsachi Blau, Roy Ganz, Chaim Baskin, Michael Elad, and Alex Bronstein. Classifier robustness enhancement via test-time transformation. *arXiv preprint arXiv:2303.15409*, 2023.
 - Huanran Chen, Yinpeng Dong, Zhengyi Wang, Xiao Yang, Chengqi Duan, Hang Su, and Jun Zhu. Robust classification via a single diffusion model. *arXiv preprint arXiv:2305.15241*, 2023.
 - Daewon Choi, Jongheon Jeong, Huiwon Jang, and Jinwoo Shin. Adversarial robustification via text-to-image diffusion models. In *European Conference on Computer Vision*, pp. 158–177. Springer, 2025.
 - Kenneth Ward Church. Word2vec. Natural Language Engineering, 23(1):155–162, 2017.
 - Mircea Cimpoi, Subhransu Maji, Iasonas Kokkinos, Sammy Mohamed, and Andrea Vedaldi. Describing textures in the wild. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 3606–3613, 2014.
 - Kevin Clark and Priyank Jaini. Text-to-image diffusion models are zero shot classifiers. *Advances in Neural Information Processing Systems*, 36, 2024.
 - Adam Coates, Andrew Ng, and Honglak Lee. An analysis of single-layer networks in unsupervised feature learning. In *Proceedings of the fourteenth international conference on artificial intelligence and statistics*, pp. 215–223. JMLR Workshop and Conference Proceedings, 2011.
 - Francesco Croce and Matthias Hein. Reliable evaluation of adversarial robustness with an ensemble of diverse parameter-free attacks. In *International conference on machine learning*, pp. 2206–2216. PMLR, 2020.
 - Valentin De Bortoli, James Thornton, Jeremy Heng, and Arnaud Doucet. Diffusion schrödinger bridge with applications to score-based generative modeling. *Advances in Neural Information Processing Systems*, 34:17695–17709, 2021.
 - Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hierarchical image database. In *2009 IEEE conference on computer vision and pattern recognition*, pp. 248–255. Ieee, 2009.
 - Prafulla Dhariwal and Alexander Nichol. Diffusion models beat gans on image synthesis. *Advances in neural information processing systems*, 34:8780–8794, 2021.
 - Stanislav Fort. Adversarial examples for the openai clip in its zero-shot classification regime and their semantic generalization, Jan 2021. URL https://stanislavfort.github.io/2021/01/12/OpenAI_CLIP_adversarial_examples.html.
 - Yuri Galindo and Fabio A Faria. Understanding clip robustness. *Understanding clip robustness*.

- Ian Goodfellow, Jean Pouget-Abadie, Mehdi Mirza, Bing Xu, David Warde-Farley, Sherjil Ozair, Aaron Courville, and Yoshua Bengio. Generative adversarial nets. *Advances in neural information processing systems*, 27, 2014.
 - Gregory Griffin, Alex Holub, Pietro Perona, et al. Caltech-256 object category dataset. Technical report, Technical Report 7694, California Institute of Technology Pasadena, 2007.
 - Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 770–778, 2016.
 - Patrick Helber, Benjamin Bischke, Andreas Dengel, and Damian Borth. Eurosat: A novel dataset and deep learning benchmark for land use and land cover classification. *IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing*, 12(7):2217–2226, 2019.
 - Dan Hendrycks, Steven Basart, Norman Mu, Saurav Kadavath, Frank Wang, Evan Dorundo, Rahul Desai, Tyler Zhu, Samyak Parajuli, Mike Guo, et al. The many faces of robustness: A critical analysis of out-of-distribution generalization. In *Proceedings of the IEEE/CVF international conference on computer vision*, pp. 8340–8349, 2021.
 - Mitch Hill, Jonathan Mitchell, and Song-Chun Zhu. Stochastic security: Adversarial defense using long-run dynamics of energy-based models. *arXiv preprint arXiv:2005.13525*, 2020.
 - Jonathan Ho, Ajay Jain, and Pieter Abbeel. Denoising diffusion probabilistic models. *Advances in neural information processing systems*, 33:6840–6851, 2020.
 - Yu Huang, Chenzhuang Du, Zihui Xue, Xuanyao Chen, Hang Zhao, and Longbo Huang. What makes multi-modal learning better than single (provably). *Advances in Neural Information Processing Systems*, 34:10944–10956, 2021.
 - Tero Karras, Miika Aittala, Timo Aila, and Samuli Laine. Elucidating the design space of diffusion-based generative models. *Advances in neural information processing systems*, 35:26565–26577, 2022.
 - Jonathan Krause, Michael Stark, Jia Deng, and Li Fei-Fei. 3d object representations for fine-grained categorization. In *Proceedings of the IEEE international conference on computer vision work-shops*, pp. 554–561, 2013.
 - Alex Krizhevsky, Geoffrey Hinton, et al. Learning multiple layers of features from tiny images. 2009.
 - Christian Léonard. Some properties of path measures. *Séminaire de Probabilités XLVI*, pp. 207–230, 2014.
 - Alexander C Li, Mihir Prabhudesai, Shivam Duggal, Ellis Brown, and Deepak Pathak. Your diffusion model is secretly a zero-shot classifier. In *Proceedings of the IEEE/CVF International Conference on Computer Vision*, pp. 2206–2217, 2023.
 - Lin Li, Haoyan Guan, Jianing Qiu, and Michael Spratling. One prompt word is enough to boost adversarial robustness for pre-trained vision-language models. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pp. 24408–24419, 2024a.
 - Liunian Harold Li, Pengchuan Zhang, Haotian Zhang, Jianwei Yang, Chunyuan Li, Yiwu Zhong, Lijuan Wang, Lu Yuan, Lei Zhang, Jenq-Neng Hwang, et al. Grounded language-image pre-training. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pp. 10965–10975, 2022.
 - Xiang Li and Shihao Ji. Defense-vae: A fast and accurate defense against adversarial attacks. In *Machine Learning and Knowledge Discovery in Databases: International Workshops of ECML PKDD 2019, Würzburg, Germany, September 16–20, 2019, Proceedings, Part II*, pp. 191–207. Springer, 2020.
- Xianhang Li, Zeyu Wang, and Cihang Xie. An inverse scaling law for clip training. *Advances in Neural Information Processing Systems*, 36, 2024b.

- Chang Liu, Yinpeng Dong, Wenzhao Xiang, Xiao Yang, Hang Su, Jun Zhu, Yuefeng Chen, Yuan
 He, Hui Xue, and Shibao Zheng. A comprehensive study on robustness of image classification
 models: Benchmarking and rethinking. *International Journal of Computer Vision*, pp. 1–23,
 2024.
 - Aleksander Madry, Aleksandar Makelov, Ludwig Schmidt, Dimitris Tsipras, and Adrian Vladu. Towards deep learning models resistant to adversarial attacks. *stat*, 1050(9), 2017.
 - Subhransu Maji, Esa Rahtu, Juho Kannala, Matthew Blaschko, and Andrea Vedaldi. Fine-grained visual classification of aircraft. *arXiv preprint arXiv:1306.5151*, 2013.
 - Chengzhi Mao, Scott Geng, Junfeng Yang, Xin Wang, and Carl Vondrick. Understanding zero-shot adversarial robustness for large-scale models. *arXiv preprint arXiv:2212.07016*, 2022.
 - Weili Nie, Brandon Guo, Yujia Huang, Chaowei Xiao, Arash Vahdat, and Anima Anandkumar. Diffusion models for adversarial purification. *arXiv preprint arXiv:2205.07460*, 2022.
 - Maria-Elena Nilsback and Andrew Zisserman. Automated flower classification over a large number of classes. In 2008 Sixth Indian conference on computer vision, graphics & image processing, pp. 722–729. IEEE, 2008.
 - Omkar M Parkhi, Andrea Vedaldi, Andrew Zisserman, and CV Jawahar. Cats and dogs. In 2012 IEEE conference on computer vision and pattern recognition, pp. 3498–3505. IEEE, 2012.
 - Alec Radford, Jong Wook Kim, Chris Hallacy, Aditya Ramesh, Gabriel Goh, Sandhini Agarwal, Girish Sastry, Amanda Askell, Pamela Mishkin, Jack Clark, et al. Learning transferable visual models from natural language supervision. In *International conference on machine learning*, pp. 8748–8763. PMLR, 2021.
 - Aditya Ramesh, Prafulla Dhariwal, Alex Nichol, Casey Chu, and Mark Chen. Hierarchical text-conditional image generation with clip latents. *arXiv preprint arXiv:2204.06125*, 1(2):3, 2022.
 - Sylvestre-Alvise Rebuffi, Sven Gowal, Dan A Calian, Florian Stimberg, Olivia Wiles, and Timothy Mann. Fixing data augmentation to improve adversarial robustness. *arXiv* preprint *arXiv*:2103.01946, 2021.
 - Robin Rombach, Andreas Blattmann, Dominik Lorenz, Patrick Esser, and Björn Ommer. High-resolution image synthesis with latent diffusion models. In *Proceedings of the IEEE/CVF conference on computer vision and pattern recognition*, pp. 10684–10695, 2022.
 - Olaf Ronneberger, Philipp Fischer, and Thomas Brox. U-net: Convolutional networks for biomedical image segmentation. In *Medical image computing and computer-assisted intervention—MICCAI 2015: 18th international conference, Munich, Germany, October 5-9, 2015, proceedings, part III 18*, pp. 234–241. Springer, 2015.
 - Chitwan Saharia, William Chan, Huiwen Chang, Chris Lee, Jonathan Ho, Tim Salimans, David Fleet, and Mohammad Norouzi. Palette: Image-to-image diffusion models. In *ACM SIGGRAPH* 2022 conference proceedings, pp. 1–10, 2022.
 - P Samangouei. Defense-gan: protecting classifiers against adversarial attacks using generative models. arXiv preprint arXiv:1805.06605, 2018.
 - Christian Schlarmann, Naman Deep Singh, Francesco Croce, and Matthias Hein. Robust clip: Unsupervised adversarial fine-tuning of vision embeddings for robust large vision-language models. *arXiv* preprint arXiv:2402.12336, 2024.
 - Erwin Schrödinger. Sur la théorie relativiste de l'électron et l'interprétation de la mécanique quantique. In *Annales de l'institut Henri Poincaré*, volume 2, pp. 269–310, 1932.
 - Nitish Shukla and Sudipta Banerjee. Generating adversarial attacks in the latent space. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pp. 730–739, 2023.

- Naman Deep Singh, Francesco Croce, and Matthias Hein. Revisiting adversarial training for imagenet: Architectures, training and generalization across threat models. *Advances in Neural Information Processing Systems*, 36, 2024.
- Yang Song, Taesup Kim, Sebastian Nowozin, Stefano Ermon, and Nate Kushman. Pixeldefend: Leveraging generative models to understand and defend against adversarial examples. *arXiv* preprint arXiv:1710.10766, 2017.
- Yang Song, Jascha Sohl-Dickstein, Diederik P Kingma, Abhishek Kumar, Stefano Ermon, and Ben Poole. Score-based generative modeling through stochastic differential equations. *arXiv* preprint *arXiv*:2011.13456, 2020.
- Quan Sun, Yuxin Fang, Ledell Wu, Xinlong Wang, and Yue Cao. Eva-clip: Improved training techniques for clip at scale. *arXiv preprint arXiv:2303.15389*, 2023.
- Zhicong Tang, Tiankai Hang, Shuyang Gu, Dong Chen, and Baining Guo. Simplified diffusion schr\" odinger bridge. arXiv preprint arXiv:2403.14623, 2024.
- Weijie Tu, Weijian Deng, and Tom Gedeon. A closer look at the robustness of contrastive language-image pre-training (clip). *Advances in Neural Information Processing Systems*, 36, 2024.
- Bastiaan S Veeling, Jasper Linmans, Jim Winkens, Taco Cohen, and Max Welling. Rotation equivariant cnns for digital pathology. In *Medical Image Computing and Computer Assisted Intervention–MICCAI 2018: 21st International Conference, Granada, Spain, September 16-20, 2018, Proceedings, Part II 11*, pp. 210–218. Springer, 2018.
- Haohan Wang, Songwei Ge, Zachary Lipton, and Eric P Xing. Learning robust global representations by penalizing local predictive power. Advances in Neural Information Processing Systems, 32, 2019.
- Jinyi Wang, Zhaoyang Lyu, Dahua Lin, Bo Dai, and Hongfei Fu. Guided diffusion model for adversarial purification. *arXiv preprint arXiv:2205.14969*, 2022.
- Sibo Wang, Jie Zhang, Zheng Yuan, and Shiguang Shan. Pre-trained model guided fine-tuning for zero-shot adversarial robustness. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pp. 24502–24511, 2024.
- Zekai Wang, Tianyu Pang, Chao Du, Min Lin, Weiwei Liu, and Shuicheng Yan. Better diffusion models further improve adversarial training. In *International Conference on Machine Learning*, pp. 36246–36263. PMLR, 2023.
- Jongmin Yoon, Sung Ju Hwang, and Juho Lee. Adversarial purification with score-based generative models. In *International Conference on Machine Learning*, pp. 12062–12072. PMLR, 2021.
- Jiahui Yu, Zirui Wang, Vijay Vasudevan, Legg Yeung, Mojtaba Seyedhosseini, and Yonghui Wu. Coca: Contrastive captioners are image-text foundation models. arxiv 2022. arXiv preprint arXiv:2205.01917, 2.
- Sergey Zagoruyko. Wide residual networks. arXiv preprint arXiv:1605.07146, 2016.
- Mingkun Zhang, Jianing Li, Wei Chen, Jiafeng Guo, and Xueqi Cheng. Classifier guidance enhances diffusion-based adversarial purification by preserving predictive information. *arXiv* preprint *arXiv*:2408.05900, 2024.

Figure 4: Comparison of the Schrödinger Bridge (Schrödinger, 1932) framework with our adversarial attack and purification process

A DISCUSSION OF THE REVERSE-TIME SDE

Motivated by the Schrödinger Bridge theory (Schrödinger, 1932; Tang et al., 2024) which models the transition between two arbitrary distributions, we utilize this theoretical framework to model the transformation between benign and adversarial sample distributions.

Within the Schrödinger Bridge framework, the forward Stochastic Differential Equation (SDE) describes a pre-defined transition from a data distribution p_{data} to a prior distribution p_{prior} , noted as a reference density $p_{\text{ref}} \in \mathcal{P}_{T+1}$, the space of joint distributions on $\mathbb{R}^{(T+1)\times d}$, where T represents the timesteps and d denotes the data dimension. Consequently, we have $p_{\text{ref};0} = p_{\text{data}}$ and $p_{\text{ref};T} = p_{\text{prior}}$. Both p_{data} and p_{prior} are defined over the data space \mathbb{R}^d . The optimal solution π^* , starting from p_{prior} and transferring to p_{data} , is termed the Schrödinger Bridge, described by the reverse SDE.

Specifically, the forward SDE is expressed as:

$$d\mathbf{x} = [f(\mathbf{x}_t, t) + g^2(t)\nabla\log\Psi(\mathbf{x}_t, t)]dt + g(t)d\mathbf{w}_t, \quad x_0 \sim p_{\text{data}},$$
(10)

where $f(x_t, t)$ is the drift function and g(t) is the diffusion term. w_t is the standard Wiener process, and Ψ and $\tilde{\Psi}$ are time-varying energy potentials constrained by the following Partial Differential Equations (PDEs):

$$\frac{\partial \Psi}{\partial t} = -\nabla_{\boldsymbol{x}} \Psi^T f - \frac{1}{2} \operatorname{Tr}(g^2 \nabla_{\boldsymbol{x}}^2 \Psi)
\frac{\partial \tilde{\Psi}}{\partial t} = -\nabla_{\boldsymbol{x}} \tilde{\Psi}^T f - \frac{1}{2} \operatorname{Tr}(g^2 \nabla_{\boldsymbol{x}}^2 \tilde{\Psi}),$$
(11)

such that $\Psi(\boldsymbol{x},0)\tilde{\Psi}(\boldsymbol{x},0)=p_{\text{data}}, \Psi(\boldsymbol{x},T)\tilde{\Psi}(\boldsymbol{x},T)=p_{\text{prior}}.$

Similarly, we define the mutual transformation between clean and adversarial sample distributions using coupled SDEs. The forward SDE describes the transformation process from benign to adversarial example distributions corresponding to an attacker's process. For an untargeted PGD attack, this is represented as:

$$d\mathbf{x} = \alpha \operatorname{sign}(\nabla_{\mathbf{x}} \mathcal{L}(\theta; \mathbf{x}_t, y_{\text{true}})) dt + \sigma d\mathbf{w}_t, \quad \mathbf{x}_0 \sim p_{\text{ben}},$$
(12)

where α represents the attack step size, $\mathcal{L}(\theta; \boldsymbol{x}_t, y_{\text{true}})$ denotes the loss when the adversarial example \boldsymbol{x}_t is classified by the model with parameters θ as the ground truth category y_{true} at attack step t (where $t \in [0,T]$), $\mathrm{d}\boldsymbol{w}_t$ denotes the Wiener process (Brownian motion) to express more general cases, and σ is a constant. The adversarial example \boldsymbol{x}_T is bound by ϵ in l_p norm, i.e., $\|\boldsymbol{x}_T - \boldsymbol{x}_0\|_p \leq \epsilon$

According to Eq. 12, we obtain formulation of the drift function and diffusion term is

$$f(\mathbf{x}_t, t) = \alpha \operatorname{sign}(\nabla_{\mathbf{x}} \mathcal{L}(\theta; \mathbf{x}_t, y_{\text{true}}))$$
$$g(t) = \sigma$$
 (13)

According to (Anderson, 1982; Song et al., 2020), the corresponding reverse-time SDE is:

$$d\mathbf{x} = [f(\mathbf{x}_t, t) - g^2(t)\nabla_{\mathbf{x}}\log p(\mathbf{x})]dt + \sigma d\tilde{\mathbf{w}}_t.$$
(14)

Thus, we can derive the corresponding reverse SDE of Eq. 12 as

$$dx = \left[\alpha \operatorname{sign}(\nabla_{\boldsymbol{x}} \mathcal{L}(\theta; \boldsymbol{x}_t, y_{\text{true}})) - \sigma^2 \nabla \log p(\boldsymbol{x}_t)\right] dt + \sigma d\tilde{w}_t, \quad \boldsymbol{x}_T \sim p_{\text{adv}}, \tag{15}$$

where $\log p(x)$ is the log-likelihood of the marginal distribution of benign samples, also known as the score function in Score SDE (Song et al., 2020). $\mathrm{d}\tilde{w}_t$ denotes the reverse-time Wiener process as time flows from t=T to t=0.

Note that the coupled SDEs described in Eq. 12 and Eq. 15 are special cases of Eq. 11 when $\nabla \log \Psi(\boldsymbol{x}_t,t) = 0$ and $\nabla \log \tilde{\Psi}(\boldsymbol{x}_t,t) = \nabla \log p(\boldsymbol{x}_t)$.

Without loss of generality, other adversarial attack methods can typically be described using the forward SDE. Therefore, our proposed approach of modeling adversarial attacks and purification processes using coupled SDEs is universally applicable.

B DETAILED PROOF OF PURIFICATION RISK FUNCTION

We first define the joint distribution of the attack process described by the forward SDE in Eq. 3 as \mathcal{P}_{T+1} , which spans $\mathbb{R}^{(T+1)\times d}$. Thus we have $\mathcal{P}_0=p_{\mathrm{ben}}$ and $\mathcal{P}_T=p_{\mathrm{adv}}$. For the purification process, we designate the joint distribution as \mathcal{Q}_{T+1} , also defined over $\mathbb{R}^{(T+1)\times d}$, with $\mathcal{Q}_0=p_{\mathrm{adv}}$ and $\mathcal{Q}_T=p_{\mathrm{pure}}$. T represents the timestep, p_{ben} , p_{adv} and p_{pure} denote the distribution of benign, adversarial, and purified samples.

According to the results of Léonard (2014), we have

$$KL(\mathcal{Q}_{0:T}|\mathcal{P}_{0:T}) = KL(\mathcal{Q}_{0,T}|\mathcal{P}_{0,T}) + \mathbb{E}_{\mathcal{Q}_{0,T}}[KL(\mathcal{Q}_{1:T-1|0,T}|\mathcal{P}_{1:T-1|0,T})]. \tag{16}$$

Since we focus on the differences between the purified and benign examples rather than the entire purification path, we concentrate on $KL(\mathcal{Q}_{0,T}||\mathcal{P}_{0,T})$. Thus, we continue to derive:

$$KL(Q_{0,T}||\mathcal{P}_{0,T})$$

$$= KL(p(\boldsymbol{x}_{\text{adv}}, \boldsymbol{x}_{\text{pure}})|p_{\text{attack}}(\boldsymbol{x}_{\text{ben}}, \boldsymbol{x}_{\text{adv}}))$$

$$= \int \int p(\boldsymbol{x}_{\text{adv}})p(\boldsymbol{x}_{\text{pure}}|\boldsymbol{x}_{\text{adv}})\log \frac{p(\boldsymbol{x}_{\text{adv}})p(\boldsymbol{x}_{\text{pure}}|\boldsymbol{x}_{\text{adv}})}{p(\boldsymbol{x}_{\text{ben}})p(\boldsymbol{x}_{\text{adv}}|\boldsymbol{x}_{\text{ben}})}d\boldsymbol{x}_{\text{pure}}d\boldsymbol{x}_{\text{adv}}$$

$$= \int p(\boldsymbol{x}_{\text{adv}})\left(\int p(\boldsymbol{x}_{\text{pure}}|\boldsymbol{x}_{\text{adv}})\log \frac{p(\boldsymbol{x}_{\text{pure}}|\boldsymbol{x}_{\text{adv}})}{p(\boldsymbol{x}_{\text{adv}}|\boldsymbol{x}_{\text{ben}})}d\boldsymbol{x}_{\text{pure}}\right)d\boldsymbol{x}_{\text{adv}} - \int p(\boldsymbol{x}_{\text{adv}})\log \frac{p(\boldsymbol{x}_{\text{adv}})}{p(\boldsymbol{x}_{\text{ben}})}d\boldsymbol{x}_{\text{adv}}$$

$$= \mathbb{E}_{\boldsymbol{x}_{\text{adv}}}\left[KL(p(\boldsymbol{x}_{\text{pure}}|\boldsymbol{x}_{\text{adv}})||p(\boldsymbol{x}_{\text{adv}}|\boldsymbol{x}_{\text{ben}}))\right] - KL(p(\boldsymbol{x}_{\text{adv}})||p(\boldsymbol{x}_{\text{ben}})),$$
(17)

where $p(\boldsymbol{x}_{\text{adv}}|\boldsymbol{x}_{\text{ben}})$ represents the conditional probability transitioning from $\boldsymbol{x}_{\text{ben}}$ to $\boldsymbol{x}_{\text{adv}}$ as described by the forward SDE, and $q(\boldsymbol{x}_{\text{pure}}|\boldsymbol{x}_{\text{adv}})$ represents the conditional probability transitioning from $\boldsymbol{x}_{\text{adv}}$ to $\boldsymbol{x}_{\text{pure}}$ as described by the reverse SDE. This formulation underscores the effectiveness of the purification process by measuring how well the adversarial transformations are reversed.

Given that the perturbations added by attackers are typically imperceptible, over a small time interval Δt , the solution of the forward SDE described by Eq. 3 approximates a normal distribution:

$$p(\mathbf{x}_{\text{adv}}|\mathbf{x}_{\text{ben}}) \sim \mathcal{N}(\mathbf{x}_{\text{ben}} + \alpha \operatorname{sign}(\nabla_x \mathcal{L})\Delta t, \sigma^2 \Delta t).$$
 (18)

Similarly, the reverse SDE process described by Eq. 4 approximates a normal distribution:

$$p(\mathbf{x}_{\text{pure}}|\mathbf{x}_{\text{adv}}) \sim \mathcal{N}(\mathbf{x}_{\text{adv}} - (\alpha \operatorname{sign}(\nabla_{\mathbf{x}_{\text{adv}}} \mathcal{L}(\theta; \mathbf{x}_{\text{adv}}, y_{\text{true}}))) - \sigma^2 \nabla \log p(\mathbf{x}_{\text{adv}})) \Delta t, \sigma^2 \Delta t).$$
 (19)

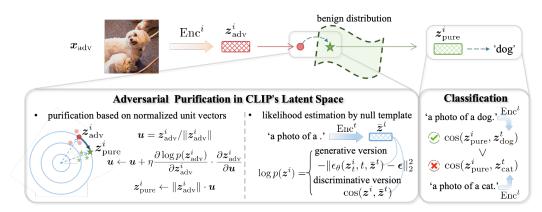


Figure 5: Illustration of the process of CLIPure including the purification in latent space and zero-shot classification, detailed in Algorithm 1.

The KL divergence formula for two normal distributions is:

$$KL(\mathcal{N}(\mu_0, \Sigma_0) \parallel \mathcal{N}(\mu_1, \Sigma_1)) = \frac{1}{2} \left(\operatorname{tr}(\Sigma_1^{-1} \Sigma_0) + (\mu_1 - \mu_0)^T \Sigma_1^{-1} (\mu_1 - \mu_0) - k + \log \frac{\det \Sigma_1}{\det \Sigma_0} \right). \tag{20}$$

When $\Sigma_0 = \Sigma_1 = \sigma^2 \Delta t$, the KL divergence reduced as

$$KL(\mathcal{N}(\mu_0, \Sigma_0) \parallel \mathcal{N}(\mu_1, \Sigma_1)) = \frac{1}{2\sigma^2 \Delta t} \|\mu_1 - \mu_0\|^2.$$
 (21)

Thus we have

$$\mathbb{E}_{\boldsymbol{x}_{\text{adv}}} \left[\text{KL}(p(\boldsymbol{x}_{\text{pure}} | \boldsymbol{x}_{\text{adv}}) || p(\boldsymbol{x}_{\text{adv}} | \boldsymbol{x})) \right]$$

$$= \mathbb{E}_{\boldsymbol{x}_{\text{adv}}} \left[\nabla \log p(\boldsymbol{x}_{\text{ben}})^T \nabla \log p(\boldsymbol{x}_{\text{ben}}) \sigma^2 \Delta t \right].$$
(22)

Thus we have proved the result in Eq. 6 that

$$KL(\mathcal{Q}_{0,T}|\mathcal{P}_{0,T}) = KL(p(\boldsymbol{x}_{\text{adv}}, \boldsymbol{x}_{\text{pure}})|p(\boldsymbol{x}, \boldsymbol{x}_{\text{adv}}))$$

$$= \mathbb{E}_{\boldsymbol{x}_{\text{adv}}} \left[KL(q(\boldsymbol{x}_{\text{pure}}|\boldsymbol{x}_{\text{adv}})||p(\boldsymbol{x}_{\text{adv}}|\boldsymbol{x}_{\text{ben}})) \right] - KL(p(\boldsymbol{x}_{\text{adv}})||p(\boldsymbol{x}))$$

$$= \frac{1}{2} \mathbb{E}_{\boldsymbol{x}_{\text{adv}}} \left[\nabla \log p(\boldsymbol{x}_{\text{adv}})^T \nabla \log p(\boldsymbol{x}_{\text{adv}}) \sigma^2 \Delta t \right] - KL(p(\boldsymbol{x}_{\text{adv}})||p(\boldsymbol{x}_{\text{ben}})).$$
(23)

C More Experimental Settings

C.1 Datasets for Zero-Shot Performance

In order to evaluate the zero-shot performance of our CLIPure and adversarially trained CLIP model including FARE (Schlarmann et al., 2024) and TeCoA (Mao et al., 2022), we follow the settings and evaluation metrics used by FARE and outlined in the CLIP-benchmark¹. We evaluate the clean accuracy and adversarial robustness across 13 datasets against an ℓ_{∞} threat model with $\epsilon=4/255$ and $\epsilon=2/255$. The datasets for zero-shot performance evaluation include CalTech101 (Griffin et al., 2007), StanfordCars (Krause et al., 2013), CIFAR10, CIFAR100 (Krizhevsky et al., 2009), DTD (Cimpoi et al., 2014), EuroSAT (Helber et al., 2019), FGVC Aricrafts (Maji et al., 2013), Flowers (Nilsback & Zisserman, 2008), ImageNet-R (Hendrycks et al., 2021), ImageNet-S (Wang et al., 2019), PCAM (Veeling et al., 2018), OxfordPets (Parkhi et al., 2012), and STL10 (Coates et al., 2011).

C.2 PURIFICATION SETTINGS

For the blank template used in purification, we employ 80 diverse description templates combined with class names, such as "a *good* photo of <class-name>" to enhance stability, following zero-shot

¹Available at https://github.com/LAION-AI/CLIP_benchmark/

classification strategies. Consistently, each class c's text embedding, z_c^t , as referred to in Eq. 2, is computed as the average text embedding combined with all templates.

For CLIPure-Diff, we use the off-the-shelf DiffusionPrior model from DaLLE 2 (Ramesh et al., 2022). During purification, following Chen et al. (2023), we estimate the log-likelihood at a single timestep and then perform a one-step purification. We conduct a total of 10 purification steps on image embeddings obtained from CLIP's image encoder, with a step size of 30, focusing on gradient ascent updates directly on the vector direction of image embeddings. Experiments indicate that timesteps in the range of 900 to 1000 yield better defense outcomes, hence we select this range for timestep selection. Regarding CLIPure-Cos, we utilize the off-the-shelf CLIP model, similarly conducting 10 purification steps, each with a step size of 30.

C.3 EXPERIMENTAL SETTING OF BASELINES

For the CIFAR-10 dataset results shown in Table 1, we use the off-the-shelf Stable Diffusion model as provided by Li et al. (2023), employing it as a zero-shot classifier. Our LM-StableDiffusion method adapts this model to a likelihood maximization approach. Other methods were applied directly according to the model in the original papers for CIFAR-10 without additional training.

For the ImageNet dataset experiments detailed in Table 2, FARE and TeCoA involve testing checkpoints that were adversarially trained on the ImageNet dataset specifically for an ℓ_{∞} threat model with $\epsilon=4/255$. The LM-DaLLE2.Decoder method utilizes the Decoder module from the ViT-L-14 model of DaLLE2 provided by OpenAI, adapted to the likelihood maximization method. DiffPure-DaLLE2.Decoder adapts the same Decoder module to the DiffPure purification method. Other methods use models as provided and trained in the original papers.

Regarding the zero-shot performance across 13 datasets shown in Table 5, we opt for the adversarially trained models of TeCoA and FARE with an ℓ_{∞} threat model at $\epsilon=4/255$, as they exhibited superior performance compared to those trained with $\epsilon=2/255$.

In the results presented in Table 6 and Table 7, we conduct an adversarial evaluation using models as specified in the literature without any additional fine-tuning.

D MORE EXPERIMENTAL RESULTS

D.1 CLIPURE BASED ON MORE CLIP MODELS

In addition to the ViT-L-14 version of the CLIP model, we tested other versions of CLIP (Radford et al., 2021) as well as EVA2-CLIP (Sun et al., 2023), CLIPA (Li et al., 2024b), and CoCa (Yu et al.) models to explore the impact of backbone model and its scale. As shown in Table 4 and Figure 6, we can observe several key points: 1) Larger models generally exhibit stronger capabilities (i.e., clean accuracy), which in turn enhances the robustness of CLIPure. Notably, the CLIPure-Cos utilizing the ViT-H-14 version of CLIPA as a backbone achieved the best performance, with robustness reaching 79.3% on ImageNet—a truly remarkable achievement. 2) CLIPure-Cos, when based on more advanced models such as CLIPA, tend to outperform models of comparable size in both accuracy and robustness. 3) ViT-based CLIPure-Cos models show better results than those based on ResNet.

D.2 ADVERSARIAL ROBUSTNESS AGAINST OTHER ATTACKS

BPDA with EOT To compare our approach with purification methods that do not support gradient propagation, we conducted evaluations using the BPDA (Backward Pass Differentiable Approximation) (Athalye et al., 2018) attack method, augmented with EOT=20 (Expectation over Transformation) to mitigate potential variability due to randomness. As depicted in Table 6, our CLIPure-Cos model significantly outperforms traditional pixel-space purification methods based on generative models such as EBM (Hill et al., 2020), DDPM (Chen et al., 2023), and Score SDE (Nie et al., 2022), despite being a discriminative model. Notably, our CLIPure demonstrates higher robust accuracy compared to the AutoAttack method under BPDA+EOT-20 attack. This is attributed to the fact that adaptive white-box attacks are precisely engineered to target the model, leading to a higher attack success rate.

Table 4: Performance of CLIPure-Cos based on various versions of CLIP (Radford et al., 2021), EVA2-CLIP (Sun et al., 2023), CLIPA (Li et al., 2024b), and CoCa (Yu et al.) under the ℓ_{∞} threat model ($\epsilon=4/255$) on the ImageNet dataset. "Param" denotes the number of parameters. The prefix "RN" refers to ResNet-based (He et al., 2016) methods, while "ViT" indicates Vision Transformer-based (Alexey, 2020) approaches.

Model	Vousion	Danam (M)	w/o D	efense	CLIPure		
Model	Version	Param (M)	Acc (%)	Rob (%)	Acc (%)	Rob (%)	
	RN50	102	59.7	0.0	60.0	52.9	
	RN101	119	61.6	0.0	61.9	55.5	
	RN50x64	623	72.0	0.0	72.3	69.5	
CLIP	ViT-B-16	149	68.1	0.0	68.2	63.0	
(Radford et al., 2021)	ViT-B-32	151	62.0	0.0	62.0	58.1	
	ViT-L-14	427	74.9	0.0	76.3	72.6	
	ViT-H-14	986	77.2	0.0	77.4	74.4	
	ViT-bigG-14	2539	80.4	0.0	80.4	77.6	
EVA2-CLIP	ViT-B-16	149	74.6	0.0	74.7	71.7	
(Sun et al., 2023)	ViT-L-14	427	81.0	0.0	80.7	78.7	
CLIPA	ViT-L-14	414	79.0	0.0	79.0	77.2	
(Li et al., 2024b)	ViT-H-14	968	81.8	0.0	81.5	79.3	
CoCa (Yu et al.)	ViT-B-32	253	64.2	0.0	63.8	59.8	

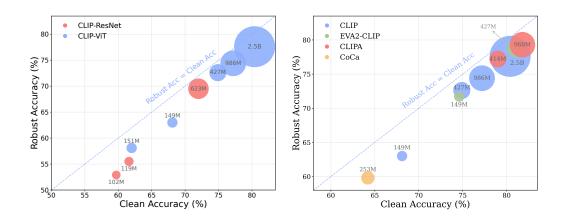


Figure 6: Relationship between model scale and performance as detailed in Table 4. The size of each bubble represents the number of parameters, which is also indicated alongside each bubble. These figures illustrate the clean and robust accuracy of CLIPure-Cos for (Left) various versions of CLIP and (Right) different backbone models. The left figure presents CLIPure-Cos based on ResNet-based models (including RN50, RN101, RN50x64, marked in red) and ViT-based models (ViT-B-16, ViT-B-32, ViT-L-14, ViT-H-14, and ViT-bigG-14, marked in blue). The right figure depicts CLIPure-Cos based on CLIP (including ViT-B-16, ViT-L-14, ViT-H-14, ViT-bigG-14, marked in blue), EVA2-CLIP (including ViT-B-16 and ViT-L-14, marked in green), CLIPA (including ViT-L-14 and ViT-H-14, marked in red), and CoCa (ViT-B-32, marked in yellow). The blue dashed line represents the point where robust accuracy equals clean accuracy, serving as the upper bound of robustness, since successful defense against adversarial attacks hinges on accuracy classification.

Latent-based Attack Shukla & Banerjee (2023) introduced a latent-based attack method, utilizing generative models such as GANs (Goodfellow et al., 2014) to modify the latent space representations and generate adversarial samples. We applied this approach to the CIFAR-10 dataset's test set, and the results, displayed in Table 7, reveal that unbounded attacks achieve a higher success rate than bounded attacks. Despite these aggressive attacks, our CLIPure method retains an advantage over

Table 5: Zero-shot performance on 13 datasets against AutoAttack under ℓ_{∞} threat model with $\epsilon=2/255$ and $\epsilon=4/255$. FARE (Schlarmann et al., 2024) and TeCoA (Mao et al., 2022) are trained on ℓ_{∞} threat model with $\epsilon=4/255$ for its generally better performance than $\epsilon=4/255$. Underlined results indicate the best robustness among baselines, while bold text denotes state-of-the-art (SOTA) performance across all methods. The term increase represents the percentage improvement in robustness compared to the best baseline method.

Eval.	Method	CalTech	Cars	CIFAR10	CIFAR100	DTD	EuroSAT	FGVC	Flowers	ImageNet-R	ImageNet-S	PCAM	OxfordPets	STL-10	Average Zero-shot
	CLIP	83.3	77.9	95.2	71.1	55.2	62.6	31.8	79.2	87.9	59.6	52.0	93.2	99.3	73.1
u,	TeCoA	78.4	37.9	79.6	50.3	38.0	22.5	11.8	38.4	74.3	54.2	50.0	76.1	93.4	54.2
clean	FARE	84.7	63.8	77.7	56.5	43.8	18.3	22.0	58.1	80.2	56.7	50.0	87.1	96.0	61.1
3	CLIPure-Diff	79.9	75.5	94.9	63.8	55.2	58.2	29.3	75.0	87.5	55.9	56.8	90.4	98.4	70.8
	CLIPure-Cos	82.9	78.6	95.6	73.0	55.4	63.3	33.2	79.3	87.7	58.3	52.0	92.5	99.6	73.2
55	CLIP	0.0	0.0	0.0	0.0	0.0	0.1	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2/255	TeCoA	69.7	17.9	59.7	33.7	26.5	8.0	5.0	24.1	59.2	43.0	48.8	68.0	86.7	42.3
= 2	FARE	76.7	30.0	57.3	36.5	28.3	12.8	8.2	31.6	61.6	41.6	48.4	72.4	89.6	<u>45.9</u>
ℓ_∞ =	CLIPure-Diff	75.1	65.9	92.5	52.6	45.9	41.5	20.8	65.8	86.5	49.8	51.4	86.2	97.9	64.0 \(\daggregarrightar
9	CLIPure-Cos	80.8	73.9	93.0	65.0	50.7	49.1	28.2	75.3	85.4	54.3	49.1	91.2	99.5	68.8 \(\dagger45.9\%\)
55	CLIP	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
= 4/255	TeCoA	60.9	8.4	37.1	21.5	16.4	6.6	2.1	12.4	41.9	34.2	44.0	55.2	74.3	31.9
	FARE	64.1	12.7	34.6	20.2	17.3	11.1	2.6	12.5	40.6	30.9	48.3	50.7	74.4	32.4
ε _∞ =	CLIPure-Diff	74.1	66.3	90.6	51.6	45.2	42.9	18.8	65.8	83.8	48.8	52.0	85.7	97.2	63.3 \(\daggeright)95.4\%
9	CLIPure-Cos	80.1	72.2	91.1	59.1	50.1	48.4	26.1	74.8	84.6	52.4	48.9	91.0	99.4	67.4 \(\dagger108.0\%\)

Table 6: Performance comparison of defense methods on CIFAR-10 against BPDA with EOT-20 under ℓ_{∞} ($\epsilon=8/255$) norm bound. We use underlining to highlight the best robustness for baselines, and bold font to denote the state-of-the-art (SOTA) across all methods.

Method	Clean Acc (%)	Robust Acc (%)
FARE (Schlarmann et al., 2024)	77.7	8.5
TeCoA (Mao et al., 2022)	79.6	10.0
Purify - EBM (Hill et al., 2020)	84.1	54.9
LM - EDM (Chen et al., 2023)	83.2	69.7
ADP (Yoon et al., 2021)	86.1	70.0
RDC (Chen et al., 2023)	89.9	75.7
GDMP (Wang et al., 2022)	93.5	76.2
DiffPure (Nie et al., 2022)	90.1	81.4
Our CLIPure - Diff	95.2	94.6
Our CLIPure - Cos	95.6	93.5

baseline approaches. This is attributed to CLIPure leveraging the inherently rich and well-trained latent space of the CLIP model, which was trained on diverse and sufficient datasets, allowing it to effectively defend against unseen attacks without the need for additional training.

Table 7: Performance comparison of defense methods on CIFAR-10 against unbounded latent-based attack (Shukla & Banerjee, 2023) using a generative adversarial network (GAN) (Goodfellow et al., 2014).

Method	Clean Acc (%)	Robust Acc (%)
ResNet-18	80.2	12.4
FARE (Schlarmann et al., 2024)	77.7	61.7
TeCoA (Mao et al., 2022)	79.6	<u>63.7</u>
Our CLIPure - Diff	95.2	69.2
Our CLIPure - Cos	95.6	70.8

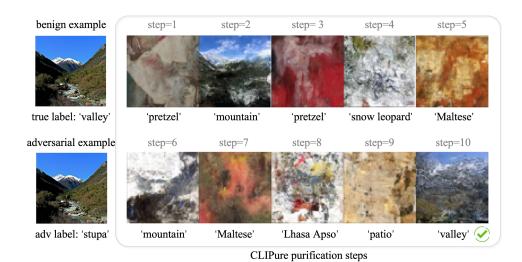


Figure 7: Purification process of our CLIPure model for an image of a 'valley' adversarially perturbed to be classified as 'stupa'. Using the DaLLE2 Decoder (Ramesh et al., 2022), we visualize the stages of image embedding purification. The text below each picture annotates the classification results corresponding to each timestep in the purification process.

D.3 CASE STUDY

To visualize the purification path of CLIPure, we employ the Decoder of DaLLE2 (Ramesh et al., 2022), which models the generation process from image embeddings to images through a diffusion model. As shown in Figure 7, starting from an adversarial example initially classified as a 'stupa,' CLIPure modifies the semantic properties of the image embedding. By the second step, the image is purified to 'mountain,' closely aligning with the semantics of the original image, which also contains mountainous features. Subsequently, after multiple purification steps, the image embedding is accurately classified as the 'valley' category.

In Figure 10, we analyze the distribution of cosine similarity between the embeddings of clean images and adversarial examples with words to understand the semantics of image embeddings. In Figure 3, we also highlight the specific top-ranked categories for the benign and adversarial examples. We observe that the cosine similarity distribution for words close to the clean image is stable and resembles the prior distribution shown in Figure 9a. In contrast, the distribution of cosine similarity for the adversarial examples shows anomalies, with the top-ranked adversarial labels displaying abnormally high cosine similarities. This could potentially offer new insights into adversarial sample detection and defense strategies.

Additionally, we illustrate the purification path using T-SNE. As depicted in Figure 8, an image sampled from CIFAR-10 originally categorized as 'airplane' was adversarially manipulated to re-

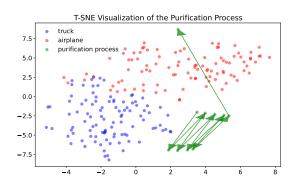


Figure 8: Purification process of the adversarial example attacked from ground truth label 'airplane' to adversarial label 'truck' and purified by our CLIPure-Diff visualized by T-SNE. The image is randomly sampled from the CIFAR-10 dataset.

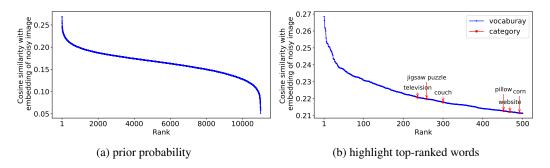


Figure 9: (a)Cosine similarity between words and the image embeddings of a noisy example to illustrate the prior probability of the words. (b) Highlights the top-ranked words within the 1,000 ImageNet categories, emphasizing the most semantically similar words to the noisy image.

semble a 'truck,' making it an outlier. Through our CLIPure method, the image is purified towards a high-density area and ultimately reclassified accurately as the 'airplane' category.

D.4 ANALYSIS FROM TEXTUAL PERSPECTIVE

In this section, we provide additional analysis from a textual perspective as a supplement to the analysis shown in Figure 3. Our vocabulary includes the 1,000 categories from ImageNet and 10,000 words randomly sampled from Word2Vec (Church, 2017). Figure 9a displays the distribution of cosine similarities between the word embeddings and an image embedding generated from pure noise, across various ranks. We aim to use these similarities to represent the prior probabilities of the words. The results indicate that most samples cluster around a cosine similarity of approximately 0.15, with only a few extreme values either much higher or lower, suggesting a normal distribution pattern. This indicates that a majority of the samples have moderate prior probabilities, contrasting with the long-tail distribution often observed in textual data. In Figure 9b, we highlight the top-ranked words in the vocabulary that are closest to the noisy image embedding. Words like "television", which appear frequently in image data, rank high, aligning with our expectations.

D.5 COMBINING CLIPURE WITH OTHER STRATEGIES

In this section, we conduct experiments that combine orthogonal strategies, including adversarial training (Schlarmann et al., 2024) and pixel space purification (Chen et al., 2023), as well as incorporating classifier confidence guidance. We carry out evaluations using a sample of 256 images from the ImageNet test set. The experimental setup in this section is aligned with the same configuration as presented in Table 2, detailed in Section 5.1.

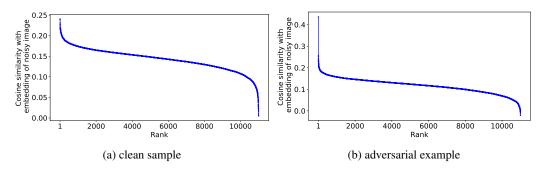


Figure 10: Cosine similarity between words and the image embedding of (a) clean sample and (b) adversarial example of the case shown in Figure 7 to illustrate the top-ranked words.

Combination with Adversarial Training (CLIPure+AT). Orthogonal adversarial training (AT) methods like FARE (Schlarmann et al., 2024) has fintuned CLIP on ImageNet. We combine CLIPure and FARE by purifying image embedding in FARE's latent space and classification via FARE. The experimental results, depicted in Fig. 11a, indicate that the CLIPure-Diff+AT method enhances adversarial robustness in CLIPure-Diff. This improvement could be attributed to FARE providing more accurate likelihood estimates, as it is specifically trained on adversarial examples. When combined with CLIPure-Cos, the outcomes were comparable, likely because the inherent robustness of CLIPure-Cos is already high, leaving limited scope for further enhancement.

Combination with Pixel Space Purification (CLIPure+LM). Purification in latent space and pixel space occurs at different stages of processing. Pixel space purification acts directly on the input samples, while latent space purification operates on the latent vectors encoded from the input picture. By combining both methods, we first purify the input samples in pixel space, then pass the purified samples through an encoder to obtain latent vectors, which are further purified in latent space. We mark this combination as CLIPure+LM. For the Likelihood Maximization (LM) method, we chose LM-EDM (Chen et al., 2023) due to its strong performance across pixel space purification methods.

Experimental results, as shown in Fig. 11a, indicate that combining with LM leads to a decrease in both clean accuracy and robustness. This decline may be associated with the challenges of information loss inherent to pixel space purification. Since LM operates directly on the pixels of the image, it is highly sensitive to the degree of purification. However, the adversarial perturbation varies across samples, potentially leading to over-purification thus a decrease in performance. In contrast, purification in latent space with polar coordinates simply involves changing vector directions—altering semantics without reducing semantic information. Thus, it avoids the problem of semantic information loss.

Combination with Classifier Guidance. In Eq. 4, we note that the reverse-time SDE associated with the attack method includes not only a likelihood maximization purification term but also a classifier guidance term, represented as $\nabla_{\boldsymbol{x}} \mathcal{L}(\theta; \boldsymbol{x}_t, y_{\text{true}})$. This approach aligns with the classifier confidence guidance proposed by Zhang et al. (2024). We incorporate this classifier guidance term in two versions of CLIPure (CLIPure-Diff and CLIPure-Cos) as described in Algorithm 1. Since the ground truth label y_{true} is unknown, we employ the predicted label by the CLIP model as a proxy for y_{true} . To address potential inaccuracies in early estimations, classifier guidance was only applied in the final 5 steps of the 10-step purification process.

We evaluate the performance varied with the weight of the guidance term, as depicted in Fig. 11b. It shows that a guidance weight of 10^{-4} led to the largest improvement in robustness: CLIPure-Diff achieved a robustness of 67.2% (an increase of +2.2% over scenarios without guidance), and CLIPure-Cos attained a robustness of 73.1% (an improvement of +0.5% over no guidance).

D.6 T-SNE VISUALIZATION

In Figure 12a, we display the distribution of image embeddings z^i for both benign samples and adversarial examples from a subset of 30 samples on the CIFAR-10 dataset, after dimensionality

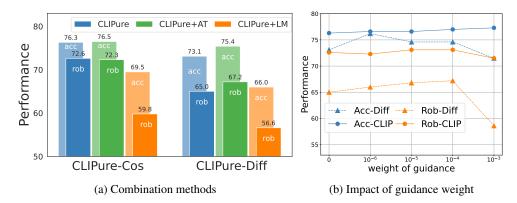


Figure 11: (a) Accuracy and robustness against AutoAttack with $\ell_{\infty}=4/255$ on ImageNet of CLIPure, CLIPure combined with Adversarial Training (AT), and CLIPure combined with pixel space Likelihood Maximization (LM). (b) Performance on ImageNet against AutoAttack with $\ell_{\infty}=4/255$ incorporating with classifier confidence guidance.

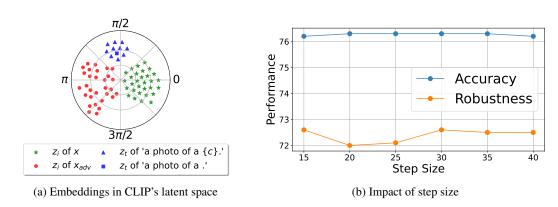


Figure 12: (a) Visualization of image and text embeddings reduced via PCA and plotted in polar coordinates using t-SNE. z^i and z^t represent the image and text embeddings obtained through CLIP, respectively. Since vector direction signifies semantics, we depict the samples in polar coordinates to emphasize directional properties. (b) Impact of step size during a 10-step purification process using CLIPure-Cos on 1000 ImageNet samples against AutoAttack with ℓ_{∞} threat model ($\epsilon = 4/255$).

reduction using t-SNE. The figure also includes embeddings for 10 category-associated texts (e.g., "a photo of a dog.") z^t , as well as the text embedding for a blank template "a photo of a.".

We observe distinct clustering of text vectors, clean image embeddings, and adversarial image embeddings in the space. The blank template, which is used for purification, is positioned at the center of the category text clusters, representing a general textual representation. This arrangement demonstrates that clean and adversarial sample distributions occupy distinct regions in the embedding space, providing a foundational basis for the effectiveness of adversarial sample purification.

D.7 HYPERPARAMETERS

D.7.1 IMPACT OF STEP SIZE

We conducted experiments to assess the impact of different step sizes on the effectiveness of purification. Figure 12b shows how the clean accuracy and robustness against AutoAttack ($\ell_{\infty}=4/255$) of our CLIPure-Cos method vary with changes in step size. These experiments were carried out on 1,000 samples from the ImageNet test set with 10-step purification. The results indicate that the performance of the method is relatively stable across different step sizes, consistently demonstrating strong effectiveness.

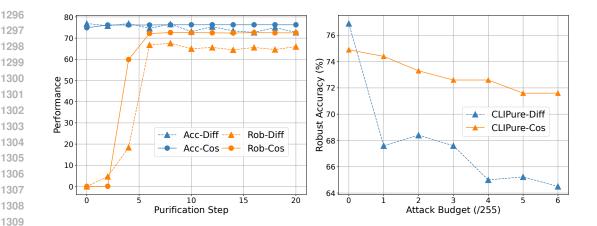


Figure 13: Clean accuracy (marked as "Acc") and robust accuracy (marked as "Rob") across different (Left) purification steps and (Right) attack budgets. "Diff" indicates CLIPure-Diff while "Cos" represents CLIPure-Cos.

Limited to the computational complexity of CLIPure-Diff, we opt not to conduct a parameter search for this model. Instead, we directly apply the optimal parameters found for CLIPure-Cos.

D.7.2 IMPACT OF PURIFICATION STEP

 As illustrated in Figure 13 (Left), we assess the performance of various purification steps in CLIPure-Cos and CLIPure-Diff. The results indicate that insufficient purification while maintaining acceptable clean accuracy, results in low robustness. As the number of purification steps increases, robustness gradually improves. Continuing to increase the purification steps stabilizes both accuracy and robustness, demonstrating a balance between the two metrics as the process evolves.

D.8 Performance Across Attack Budget

To further explore the adversarial defense capabilities of CLIPure, we evaluate the robustness of CLIPure-Diff and CLIPure-Cos against various attack budgets, following the settings used in Table 2. As shown in Figure 13 (Right), CLIPure-Diff demonstrates superior clean accuracy (at ϵ =0); however, its robustness decreases as the intensity of the attacks increases. In contrast, CLIPure-Cos exhibits a stronger ability to withstand adversarial perturbations.