

000 REINFORCEMENT LEARNING FROM DYNAMIC CRITIC 001 FEEDBACK FOR FREE-FORM GENERATIONS 002

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005 Paper under double-blind review
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007 ABSTRACT 008

009 Open-ended generation tasks require outputs to satisfy diverse and often implicit
010 task-specific evaluation rubrics. The sheer number of relevant rubrics leads to
011 prohibitively high verification costs and incomplete assessments of a response,
012 making reinforcement learning (RL) post-training with rubric-based rewards dif-
013 ficult to scale. This problem is exacerbated by the fact that often the best way
014 to combine these rubrics into one single reward is also highly prompt-specific.
015 We propose Reinforcement Learning from Dynamic Critic Feedback (RLDCF),
016 a post-training approach that addresses these challenges via dynamic rubric ver-
017 ification. Our approach employs a large language model (LLM) as a critic that
018 dynamically identifies only the most likely failure modes (e.g., a factual error or
019 unhandled edge case), which are then verified by an external validator to optimize
020 both generator and critic jointly. By training both the generator and the critic,
021 this game enhances the critic’s error detection and the generator’s output quality
022 while reducing required verifications. Our experiments demonstrate that RLDCF
023 improves factual accuracy in text generation and correctness in code generation,
024 while also outperforming exhaustive verification and reward model methods. We
025 show that dynamic critics are more effective than fixed critics, showcasing the
026 potential of RLDCF for scaling RL post-training to free-form generation tasks.
027

028 1 INTRODUCTION 029

030 Post-training methods for large language models (LLMs) have progressed dramatically over the past
031 few years, from largely manual supervised fine-tuning (SFT) techniques that rely on a combination of
032 manual data curation (Radford et al., 2018; Brown et al., 2020; Shengyu et al., 2023) to reinforcement
033 learning (RL) methods that perform general preference-based optimization (Christiano et al., 2017;
034 Ouyang et al., 2022) or optimize task-specific notions of correctness (Zha et al., 2025). Despite these
035 remarkable results, RL post-training is limited to tasks with clear-cut success criteria (i.e., correctness
036 of an answer or preference of a human user), and it remains unclear how to post-train LLMs with RL
037 on tasks that require producing open-ended or free-form outputs that are hard to verify perfectly.
038

039 Perhaps the biggest challenge in building RL post-training methods for free-form generation tasks
040 is the lack of a solid reward function: outputs are typically expected to satisfy several task-specific
041 rubrics. In principle, a task designer could construct a reward by combining these rubrics, but both
042 enumerating and verifying them pose major scalability challenges (Min et al., 2023). For instance,
043 complex code generation requires testing countless edge cases (e.g., empty inputs or specific numbers).
044 Even if such criteria could be enumerated, knowing how to combine them remains difficult (e.g.,
045 should correctly handling even numbers outweigh handling primes?). While RLHF-trained reward
046 models or LLM-as-judge approaches (Christiano et al., 2017; Zheng et al., 2023) outsource the job of
047 merging rubrics to a learned or prompted reward model, this often leads to reward hacking (Ziegler
048 et al., 2019; Gao et al., 2023; Skalse et al., 2022; Eisenstein et al., 2023), since the best combination
049 is highly dependent on the prompt and the model being optimized. How can we then train LLMs on
free-form generation tasks with several (maybe uncountably many) rubrics?

050 We introduce Reinforcement Learning from Dynamic Critic Feedback (RLDCF), which formulates
051 the problem as an adversarial game between a generator and a *critic*. The critic is a learned model
052 that proposes a rubric (e.g., one test case) where the generator’s output is likely to fail, and an
053 external validator verifies this. Both models are trained jointly: the critic is rewarded when it correctly
pinpoints a rubric that the generator fails (verified by an external validator), while the generator

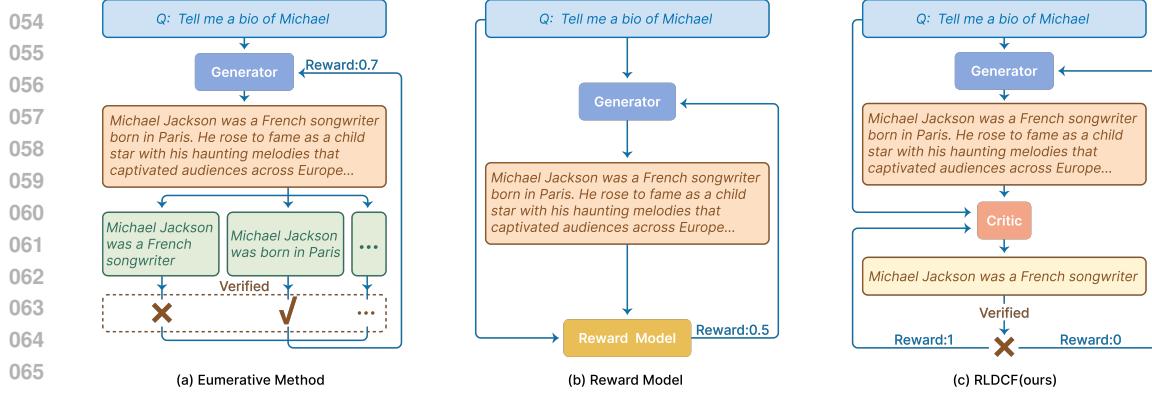


Figure 1: Comparison of three post-training paradigms on a biography example (“Michael Jackson”). **(a) Enumerative verification** explicitly extracts and checks every atomic fact before aggregating a scalar reward, which is accurate but expensive. **(b) Reward-model methods** skip verification and directly predict a scalar reward from a learned judge, which is efficient but prone to reward hacking. In contrast, **(c) RLDCF** trains a learned critic to propose one likely-wrong fact (*rubric*) and verifies it via an external validator. If the fact indeed fails, the critic receives reward 1 and the generator 0; otherwise the generator receives 1 and the critic 0. This dynamic, adversarial feedback yields prompt-specific, verifiable, and scalable supervision for free-form generation tasks.

is rewarded when the critic is unable to do so. This formulation eliminates the need to enumerate or verify all rubrics, significantly improving training scalability. At the same time, it ensures that rewards are based on rubrics that are prompt-specific, adversarially chosen, and always on-policy. Figure 1 illustrates how RLDCF achieves verification efficiency while maintaining accuracy through adversarial critic-generator dynamics on a biography generation example.

We evaluate Reinforcement Learning from Dynamic Critic Feedback on factual text generation and code generation, representing enumerable and non-enumerable verification scenarios, respectively. On 8-sentence biography generation with Qwen3-8B, Reinforcement Learning from Dynamic Critic Feedback achieves a FactScore of 0.889, surpassing FactTune-FS’s (Tian et al., 2024) 0.867, while reducing verification calls by $5.7\times$. This efficiency gain scales with task complexity, from $4.4\times$ for 4-sentence to $5.7\times$ for 8-sentence generation. In code generation, despite using only 9% of the training data, Reinforcement Learning from Dynamic Critic Feedback achieves the highest average scores on both base models: **53.2** on Qwen2.5-Coder-7B-Base and **56.6** on Qwen2.5-Coder-7B-Instruct, outperforming prior methods AceCoder-RM and AceCoder-Rule (Zeng et al., 2025).

Our primary contribution is Reinforcement Learning from Dynamic Critic Feedback (RLDCF), a novel post-training paradigm that frames free-form LLM optimization as an adversarial game between a generator and a learned critic, with an external validator providing ground-truth feedback. This design avoids exhaustive rubric enumeration and mitigates reward hacking by producing task-specific and on-policy training signals. In experiments, Reinforcement Learning from Dynamic Critic Feedback consistently improves factual accuracy while reducing verification costs, and surpasses prior methods on code generation—demonstrating scalable gains across both enumerable and non-enumerable verification tasks.

2 PRELIMINARIES

Our goal is to train a generator that produces a free-form output meeting task requirements, without manually enumerating every rubric. In this section, we formalize this problem, introduce notation, and briefly discuss related concepts of reward models (Christiano et al., 2017; Ziegler et al., 2019; Rafailov et al., 2023) and enumerative verification (Min et al., 2023; Trivedi et al., 2024; Saha et al., 2025; Wang et al., 2024b; Xie et al., 2025), as illustrated in Figure 1. We then present our approach in the next section.

Problem setup. We consider free-form generation tasks where outputs must satisfy many task-specific requirements, which we call rubrics. For instance, a biography generation task may require that each factual claim is correct, while a code generation task may require the program to handle all edge cases correctly. Formally, let \mathcal{S} be a distribution over prompts or instructions that may be

108 presented to an LLM. Given $s \in \mathcal{S}$, a generator LLM $\pi^g(a | s)$ is tasked with producing a textual
 109 output $a \in \mathcal{A}$. We choose to use standard notation typically used in RL (\mathcal{S} denoting the state space
 110 and \mathcal{A} denoting the action space) as we later present an RL training objective. Each instruction s is
 111 inherently associated with a set of rubrics (denoted as $\mathcal{C}(s)$), where each rubric $c \in \mathcal{C}(s)$ represents a
 112 verifiable property the output should satisfy, such as “*the claim about Newton’s birth year is correct*”
 113 for biography generation or “*the code handles null inputs*” for code generation.

114 We assume access to a binary verification function $R(s, a, c)$ that returns 1 if a generated output
 115 $a \sim \pi^g(\cdot | s)$ satisfies the rubric c on instruction s , and attains 0 otherwise. An output a is considered
 116 correct only when *all* rubrics $\mathcal{C}(s)$ associated with instruction s are satisfied. Our goal is to train
 117 $\pi^g(\cdot | s)$ to maximize the probability of producing fully correct outputs:

$$\pi_g^* := \arg \max_{\pi} \mathbb{E}_{s \sim \mathcal{S}} \left[\mathbb{E}_{a \sim \pi(\cdot | s)} \left[\prod_{c \in \mathcal{C}(s)} R(s, a, c) \right] \right]. \quad (1)$$

122 In constrained domains with a single, well-defined rubric (e.g., matching a reference solution
 123 in math reasoning), the optimization of object simplifies, allowing standard RL algorithms like
 124 PPO (Schulman et al., 2017) or GRPO (Shao et al., 2024) to optimize the policy. However, such
 125 cases are rare in open-ended tasks with diverse rubrics. In these settings, $\mathcal{C}(s)$ can be extremely large
 126 or even unbounded, making Eq. 1 computationally intractable since every output must be checked
 127 against every rubric.

128 **Reward models and enumerative verification.** Most approaches to optimizing free-form generation
 129 tackle the challenge of diverse rubrics through two paradigms. RLHF (Christiano et al., 2017) trains
 130 a single proxy reward model from offline human preference data. While efficient, this optimization is
 131 hard because the learned proxy is only as good as its coverage of the preference dataset. When the
 132 generator explores beyond this support, the proxy can misalign (Gao et al., 2023), often necessitating
 133 additional constraints like KL regularization to avoid collapse. These constraints stabilize training
 134 but also limit exploration, making it difficult to scale to highly open-ended tasks (Dong et al., 2024).

135 Another approach is to enumerate the evaluation criteria and optimize their aggregate, either through
 136 prompting (Min et al., 2023; Saha et al., 2025) or via preferences implicitly elicited from hu-
 137 mans (Wang et al., 2024b; Mahan et al., 2024). While more faithful to the underlying rubrics (Trivedi
 138 et al., 2024), this strategy is fundamentally limited: it assumes the evaluation set $\mathcal{C}(s)$ can be exhaus-
 139 tively listed, which is unrealistic for complex tasks (e.g., all test cases for a nontrivial program). Even
 140 when such enumeration is feasible, iterating over the entire set is computationally prohibitive, turning
 141 optimization into an intractable verification bottleneck.

3 REINFORCEMENT LEARNING FROM DYNAMIC CRITIC FEEDBACK

144 We now introduce our RL post-training approach, called Reinforcement Learning from Dynamic
 145 Critic Feedback (RLDCF) for training LLM generators on free-form tasks. Our goal is to provide
 146 rewards while avoiding the scalability limits of enumerative verification and the misalignment of
 147 static reward models. The core idea is to recast verification as a dynamic process guided by a learned
 148 critic. Concretely, we frame training as a two-player game: given an output from the generator, the
 149 critic proposes a rubric the output is likely to violate, while the generator aims to satisfy all such
 150 rubrics. An external validator then adjudicates whether the output meets the proposed rubric, and
 151 this supervision updates both generator and critic. In this way, verification becomes adaptive and
 152 adversarial, tailored to the generator’s current weaknesses. We now formally derive this approach.

3.1 PROBLEM REFORMULATION

153 To derive our approach formally, our starting point is the objective of Equation 1, which requires a
 154 generation to satisfy all rubrics in the set $\mathcal{C}(s)$: Since $R(s, a, c)$ is an indicator function for each c ,
 155 we can rewrite the requirement that all rubrics are satisfied as a minimum over all rubrics as follows:

$$\mathbb{1}\{R(s, a, c) = 1, \forall c \in \mathcal{C}(s)\} = \min_{c \in \mathcal{C}(s)} \mathbb{1}\{R(s, a, c) = 1\}. \quad (2)$$

156 Intuitively, the minimum selects the worst-case criterion, i.e., the first failure mode encountered by
 157 the current model π . Substituting Equation 2 into Equation 1 gives:

$$\pi_g^* = \arg \max_{\pi} \mathbb{E}_{s \sim \mathcal{S}} \left[\mathbb{E}_{a \sim \pi(\cdot | s)} \left[\min_{c \in \mathcal{C}(s)} R(s, a, c) \right] \right]. \quad (3)$$

162 However, this reformulation by itself does not make the optimization problem simpler: searching
 163 over $\mathcal{C}(s)$ is infeasible when $\mathcal{C}(s)$ is large or infinite (e.g., all possible test cases). To address this, we
 164 introduce a critic π^c , modeled as a stochastic policy that takes an instruction-generation pair (s, a) as
 165 input and outputs a rubric $c \in \mathcal{C}(s)$ in natural language, representing a verifiable property that may
 166 fail. An external validator then checks the proposed rubric. Then we can rewrite Equation 3 into the
 167 equivalent min-max form:

$$\pi^g = \arg \max_{\pi^c} \min_{\pi^c} \mathbb{E}_{s \sim \mathcal{S}} [\mathbb{E}_{a \sim \pi(\cdot|s)} \mathbb{E}_{c \sim \pi^c(\cdot|s, a)} [R(s, a, c)]] . \quad (4)$$

170 It can be shown that the solution π^g from Equation 4 is the same as that from Eq. (1), but now we
 171 bypass the need to enumerate all criteria over $\mathcal{C}(s)$ (Madry et al., 2018).

172 Pretty much like other mini-max optimization problems, we can solve the above optimization problem
 173 by iteratively updating π^g and π^c against each other. The optimization goal is to achieve a robust
 174 generator π^g that does well even according to the most adversarial critic, upon convergence. More
 175 details with respect to the practical optimization algorithm will be provided in Section 3.2.

177 3.2 PRACTICAL INSTANTIATION OF RLDCF

178 We now instantiate the two-player adversarial game from the previous section into a practical approach
 179 that we can use to train LLMs. As shown in Figure 1, we parameterize three task-agnostic components
 180 that interact with each other during RL training. Each component is instantiated differently based on
 181 the domain (as detailed in Section 4).

182 **Generator.** The generator π^g , is an LLM that is fine-tuned to produce an output $a \in \mathcal{A}$ for an
 183 instruction $s \in \mathcal{S}$. RLDCF samples multiple response generations from π^g for each instruction s . We
 184 train π^g to maximize the probability of producing outputs that satisfy all task-specific rubrics. The
 185 prompt for the generator is included in the Appendix A.1.

186 **Critic.** Our critic π^c is a pre-trained LLM π^c that RLDCF fine-tunes. Specifically, for each instruction
 187 s and a query generation output a , the critic is prompted to generate a natural language output
 188 representing a rubric c through auto-regressive decoding. The rubric c along with the instruction s and
 189 the generation a are then sent to the external validator to obtain a reward signal $R(s, a, c) \in \{0, 1\}$.
 190 The prompt for the adversarial critic is included in the Appendix A.2.

191 **Validator.** The validator is an external tool or process that can verify whether a generated response
 192 satisfies a rubric provided as input to it. The validator can be implemented in various ways depending
 193 on the domain, such as rule-based checkers or a software tool that evaluates a proposed code on a
 194 proposed test-case. Implementation details for specific tasks are discussed in the Appendix B.

195 **Updating the generator and critic.** At each training step, we sample instructions $s \in \mathcal{S}$ and
 196 have the generator π^g produce K candidate outputs a_1, \dots, a_K . For each (s, a_i) , the adversarial
 197 critic π^c proposes a criterion c_i , which is then checked by the validator to yield a binary reward
 198 $r_i \in \{0, 1\}$. This online feedback provides signals for both policies. Outputs with $r_i = 1$ are treated
 199 as positives (a^+) and those with $r_i = 0$ as negatives (a^-), and the generator is updated using the
 200 DPO loss (Rafailov et al., 2023) with respect to the reference generator π_{ref}^g :

$$\mathcal{L}(\pi^g; \pi_{\text{ref}}^g) = -\mathbb{E}_s \mathbb{E}_{(a^+, a^-)} \left[\log \sigma \left(\beta \log \frac{\pi^g(a^+|s)}{\pi_{\text{ref}}^g(a^+|s)} - \beta \log \frac{\pi^g(a^-|s)}{\pi_{\text{ref}}^g(a^-|s)} \right) \right] . \quad (5)$$

204 Similarly, for each (s, a) pair, we sample N criteria from π^c . Criteria rejected by the validator (invalid
 205 or satisfied by the generator) are treated as negatives (c^-), while valid, unsatisfied ones are positives
 206 (c^+). The critic is then updated with the same DPO objective relative to its reference policy π_{ref}^c :

$$\mathcal{L}(\pi^c; \pi_{\text{ref}}^c) = -\mathbb{E}_{s, a} \mathbb{E}_{(c^+, c^-)} \left[\log \sigma \left(\beta \log \frac{\pi^c(c^+|s, a)}{\pi_{\text{ref}}^c(c^+|s, a)} - \beta \log \frac{\pi^c(c^-|s, a)}{\pi_{\text{ref}}^c(c^-|s, a)} \right) \right] . \quad (6)$$

210 In this way, evaluation and improvement are unified: the critic adaptively identifies failure modes,
 211 the validator provides ground-truth feedback, and both generator and critic are jointly updated to
 212 improve over time. Note that we chose the DPO loss for its simplicity, though any online or offline
 213 RL approach could be used for policy optimization.

214 **Algorithm summary.** Algorithm 1 summarizes the practical implementation of RLDCF. At a high
 215 level, the algorithm follows a standard online RL loop that alternates between policy evaluation and

216 **Algorithm 1** RLDCF

217 1: Initialize parameters $\pi^g, \pi^c, \pi_{\text{ref}}^g, \pi_{\text{ref}}^c$

218 2: **for** each iteration **do**

219 3: **## Policy Evaluation for Generator** π^g .

220 4: **for** each instruction s **do**

221 5: Generate K generations $a_1, \dots, a_K \sim \pi^g(\cdot|s)$

222 6: Sample a criterion from the adversarial critic for each generation $c_i \sim \pi^c(\cdot|s, a_i)$.

223 7: Construct a generator dataset $\mathcal{D}_s^g = \{(s, a_i, R(s, a_i, c_i))\}_{i=1}^K$

224 8: **## Policy Evaluation for Critic** π^c . ▷ Optional

225 9: **for** each instruction s , output a **do**

226 10: Generate N criteria $c_1, \dots, c_N \sim \pi^c(\cdot|s, a)$

227 11: Construct a critic dataset $\mathcal{D}_{(s,a)}^c = \{(s, a, R(s, a, c_j))\}_{j=1}^N$

228 12: **## Policy Improvement for Generator** π^g .

229 13: $\pi_{\text{new}}^g \leftarrow \pi^g$

230 14: **for** each update step **do** ▷ Equation 5

231 15: $\pi_{\text{new}}^g \leftarrow \pi_{\text{new}}^g - \nabla \mathcal{L}(\pi_{\text{new}}^g, \pi_{\text{ref}}^g)$

232 16: $\pi_{\text{ref}}^g \leftarrow \pi^g$

233 17: **## Policy Improvement for Critic** π^c . ▷ Optional

234 18: $\pi_{\text{new}}^c \leftarrow \pi^c$

235 19: **for** each update step **do** ▷ Equation 6

236 20: $\pi_{\text{new}}^c \leftarrow \pi_{\text{new}}^c - \nabla \mathcal{L}(\pi_{\text{new}}^c, \pi_{\text{ref}}^c)$

237 21: $\pi_{\text{ref}}^c \leftarrow \pi^c$

238 improvement. In each evaluation step, we sample generations from the current generator π^g , have the
 239 critic propose a criterion c , and obtain verification to assign rewards. These rewards are then used
 240 to update the generator with the DPO objective (Equation 5). Optionally, we also collect evaluation
 241 data for the critic by sampling multiple criteria per instruction–generation pair. The critic is then
 242 updated with its own DPO objective (Equation 6), allowing it to adaptively identify weaknesses in
 243 the generator and provide more effective learning signals.

4 EXPERIMENTS

244 We now evaluate our approach on two free-form generation tasks: factual text generation (§4.1)
 245 and code generation (§4.2). Factual text generation illustrates the enumerable-but-expensive regime,
 246 where all claims can in principle be verified but at a cost that scales with text length. This tests
 247 RLDCF’s ability to maintain verification quality while reducing calls. Code generation, by contrast,
 248 represents the non-enumerable regime, where exhaustive verification is impossible due to infinite
 249 corner cases and intractable formal checks (Church, 1936). Here, the goal is to expose critical failures
 250 through targeted critic proposals. Together, these tasks span the spectrum from costly-but-possible to
 251 fundamentally intractable verification, highlighting the broad applicability of RLDCF.

4.1 FACTUAL TEXT GENERATION

4.1.1 SETTINGS

252 **Evaluation data & metrics.** We follow Min et al. (2023); Tian et al. (2024) in adapting a factual
 253 text generation task in which the model should produce concise biographies for a given individual.
 254 We use 170 topics from the Wikipedia Biography Dataset (Lebret et al., 2016), split into 120 for
 255 training and 50 for testing. We use factual precision of the output (as defined by FactScore (Min et al.,
 256 2023)) as the primary metric, and also report the counts of correct and incorrect facts. To control for
 257 length, the model is instructed to generate either four or eight sentences. Since frequent calls to the
 258 external validator are costly, we additionally track the number of validator calls.

259 **Base models & baselines.** Our base generators are Qwen3-4B and Qwen3-8B. We compare against
 260 three baselines: (1) the original base models without task-specific training; (2) FactTune-FS (Tian
 261 et al., 2024), a widely used method for factual text generation to represent exhaustive verification
 262 using an external validator, FactScore, for all atomic facts; and (3) ArmoRM (Wang et al., 2024a),
 263 which represents the reward model based method that produces one reward score for the generated

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273 Table 1: Performance comparison on factual text generation. RLDCF achieves the highest FactScore
274 across all settings while using fewer verification calls than FactTune-FS.
275

273 274 275 Method	4-sentence Generation				8-sentence Generation			
	# Corr↑	# Incorr↓	FS↑	Calls↓	# Corr↑	# Incorr↓	FS↑	Calls↓
Qwen3-4B								
Baseline	10.07	6.43	0.610	-	19.62	12.08	0.619	-
FactTune-FS	10.66	3.48	0.754	214,911	20.65	5.99	0.775	341,657
ArmoRM	14.54	8.69	0.626	-	21.02	10.02	0.677	-
RLDCF (Ours)	10.54	3.04	0.776	57,600	21.58	4.84	0.817	48,000
Qwen3-8B								
Baseline	12.65	5.53	0.696	-	22.51	11.97	0.653	-
FactTune-FS	13.31	3.63	0.786	168,735	25.10	3.84	0.867	438,949
ArmoRM	12.96	6.86	0.654	-	23.31	8.92	0.723	-
RLDCF (Ours)	13.14	3.37	0.796	38,400	24.33	3.03	0.889	76,800

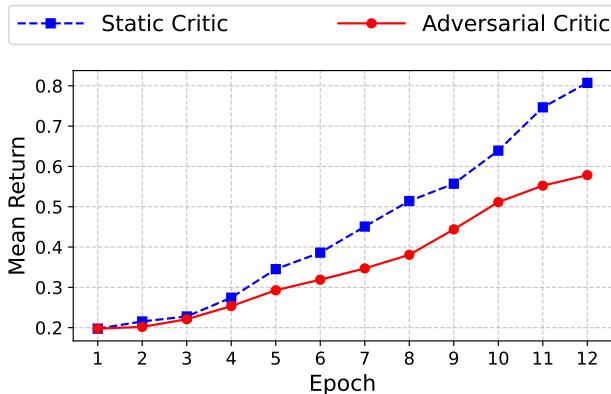
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 Figure 2(b) shows that RLDCF achieves the same level of factuality as FactTune-FS with far fewer
 329 verification calls (e.g., 67K vs. 368K to achieve 84%). This highlights the inefficiency of FactTune-
 330 FS, which repeatedly validates already correct facts, whereas RLDCF dynamically targets high-risk
 331 errors, yielding greater verification efficiency and scalability.

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 Figure 2(c) measures exploration by tracking the KL divergence from the base model. Such deviation
 337 can usually be caused by either (1) improvements from the base model through effective exploration,
 338 or (2) reward hacking, in which the model overfits to the reward model and drafts without real quality
 339 gains. For RLDCF, KL increases alongside monotonic FactScore gains ($0.653 \rightarrow 0.889$), indicating
 340 productive exploration. In contrast, RL with a fixed offline reward model (ArmoRM) shows a rise
 341 in KL without the corresponding factuality gains, evidence of reward hacking. These dynamics
 342 complement Table 1: while both RLDCF and FactTune-FS improve factuality, RLDCF achieves
 343 comparable or higher FactScore with far fewer verification calls, whereas ArmoRM inflates output
 344 length without consistent accuracy due to its static reward.

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 Table 2: Generator’s test accuracy across critic types.

Method	# Corr	# Incorr	FS
Base	19.62	12.08	0.619
Noisy Validator	19.84	12.83	0.607
Static Critic	17.77	3.77	0.825
Adversarial Critic	21.58	4.84	0.817



378 4.2 CODE GENERATION
379380 4.2.1 SETTINGS
381

382 **Evaluation data & metrics.** We evaluate code generation performance using widely studied
383 benchmarks: HumanEval (Base and Plus) (Chen et al., 2021; Liu et al., 2023), MBPP (Base and
384 Plus) (Austin et al., 2021; Liu et al., 2023), BigCodeBench (Zhuo et al., 2024), and LiveCodeBench
385 (V4) (Jain et al., 2025). We use Pass1 as a primary metric. For efficiency analysis, we also report
386 the number of test cases executed per successful solution. Note that, unlike factual verification,
387 where each check is expensive, unit tests in code generation are cheap to execute. The fundamental
388 bottleneck here is not the per-test cost but the non-enumerability of the test space. Therefore, test-case
389 count is reported only for completeness; the primary evaluation metric remains Pass@k.
390

391 **Base models & baselines.** For training data, we use the AceCode-87K-hard subset (Zeng et al.,
392 2025), consisting of approximately 22K problems. Our base generators include Qwen2.5-Coder-7B-
393 Base and Qwen2.5-Coder-7B-Instruct. We compare against three baselines: (1) the original base
394 models without training; (2) AceCoder-Rule, which employs RL with rule-based binary rewards from
395 test execution; and (3) AceCoder-RM, which uses RL with AceCodeRM-7B trained on approximately
396 300K preference pairs constructed from AceCode-87K dataset. Our RLDFC approach samples 2k
397 questions from the AceCode-87K-hard subset for training, generates $k = 8$ outputs per prompt
398 (which is consistent with the AceCoder setting) with $n = 2$ critic proposals per generation.
399

400 4.2.2 MAIN RESULTS
401

402 Table 3: Results for HumanEval, MBPP, BigCodeBench Complete and Instruct (BCB-C, BCB-I),
403 and LiveCodeBench, using two different base models. RLDFC achieves the highest average score
404 across benchmarks.
405

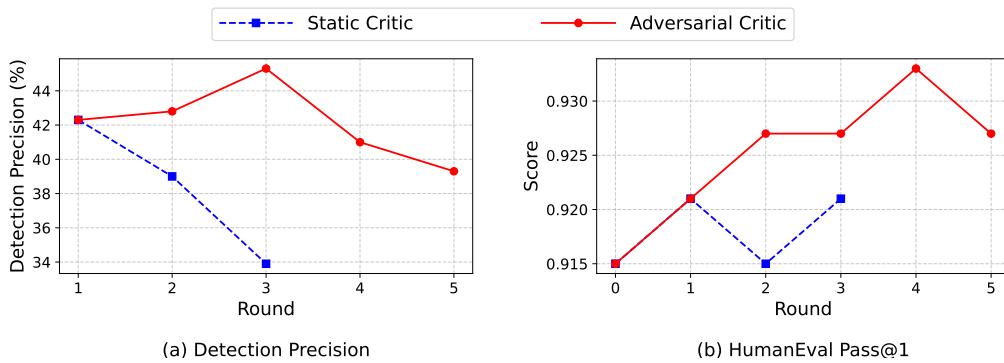
Method	HumanEval		MBPP		BCB-C		BCB-I		LCB	Average
	Base	Plus	Base	Plus	Full	Hard	Full	Hard		
Base: Qwen2.5-Coder-7B-Base										
Baseline	83.5	79.3	80.4	69.3	45.8	16.2	40.2	14.2	28.7	50.8
AceCoder-RM	83.5	75.6	80.2	67.2	41.9	14.9	36.8	16.2	25.7	49.1
AceCoder-Rule	84.1	78.0	82.3	69.3	48.6	18.2	43.2	18.2	28.5	52.3
RLDFC (Ours)	85.7	80.6	82.4	71.6	50.3	20.9	42.1	16.9	28.7	53.2
Base: Qwen2.5-Coder-7B-Instruct										
Baseline	91.5	84.8	82.8	71.4	49.5	19.6	41.8	20.3	34.2	55.1
AceCoder-RM	89.0	84.1	86.0	72.8	50.4	18.9	42.0	19.6	35.0	55.3
AceCoder-Rule	90.9	84.8	84.1	71.7	50.9	23.0	43.3	19.6	34.9	55.9
RLDFC (Ours)	93.3	86.0	83.9	73.0	52.2	24.3	42.3	19.6	35.2	56.6

416 Table 6 summarizes results across five widely-used code generation benchmarks. Despite training
417 on only 2,000 problems (9% of the dataset used for AceCoder-RM and AceCoder-Rule), RLDFC
418 achieves the highest average scores: 53.2 using Qwen2.5-Coder-7B-Base and 56.6 using Qwen2.5-
419 Coder-7B-Instruct, consistently outperforming both enumerative method (AceCoder-Rule) and static
420 reward model method (AceCoder-RM) across the majority of benchmarks. We observe from Table 4
421 that AceCoder-RM not only fails to improve performance but can even degrade it under noisy
422 validation. For example, on HumanEval, performance drops from 91.5 to 89.0 despite using the
423 competitive reward model AceCoder-RM-7B, indicating reward hacking.
424

425 This fragility arises from the reward model trained on preference pairs from the AceCoder dataset,
426 which itself contains noisy and incomplete test cases (Zeng et al., 2025). During RL training, as
427 the generator's outputs drift away from the RM's fixed training distribution, these noisy supervision
428 signals are further amplified. The static RM cannot adapt, causing it to favor spurious correlations
429 rather than true correctness, leading the generator to exploit flaws in the reward signal.
430

431 RLDFC also suffers from the noisy dataset since we use a simulated solution as validator mentioned
432 in settings. Although the critic is also affected by noise, its continuous adaptation allows it to stay
433 aligned with the generator's changing behavior, preserving meaningful supervision. As a result,
434

432 RLDCF consistently improves performance across all benchmarks, even in noisy and imperfect
 433 validation environments, showing robustness to noisy validation.
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 447 **Figure 4: Ablations on the static critic vs. adversarial critic.** Static critic’s detection accuracy
 448 degrades from 42.3% to 33.9% as the generator exploits its patterns, yielding minimal performance
 449 gains (+0.6%) compared to the adversarial critic’s continued improvement (+1.8%).
 450

451 4.2.3 ABLATION STUDY

452 We compare RLDCF with a variant that replaces the adversarially trained critic with a static critic to
 453 evaluate the necessity of dynamic adaptation. As shown in Figure 4, the static critic’s detection rate,
 454 defined by the fraction of test cases generated that correctly expose real errors, drops dramatically
 455 from 42.3% to 33.9% over three rounds, as the generator gradually learns to exploit its fixed detection
 456 patterns. In contrast, the adversarial critic maintains a stable detection rate greater than 39% by
 457 continuously adapting to the evolving behavior of the generator.

458 This degradation directly impacts performance: with the static critic, the generator plateaus at 92.1%
 459 Pass@1, while RLDCF reaches 93.3%. Further analysis shows that 73% of the static critic’s test cases
 460 in round 3 are minor variations of earlier ones, allowing the generator to avoid detection by simplifying
 461 or reducing outputs rather than truly fixing bugs. These results highlight that dynamic adaptation is
 462 essential for preventing reward hacking and driving real improvements in code correctness.
 463

464 5 RELATED WORKS

465 **Reward models.** One possibility for evaluating free-form and open-ended generations is to encode
 466 all criteria into a single scalar through a learnt reward model. This is usually achieved through
 467 learning from an offline dataset of human preferences (Christiano et al., 2017; Ziegler et al., 2019;
 468 Yi et al., 2019; Böhm et al., 2019; Rafailov et al., 2023) or absolute ratings (Cui et al., 2024; Wang
 469 et al., 2024c). Multi-objective reward models (Wang et al., 2024a; Dong et al., 2024; Ji et al., 2023)
 470 expose several fixed dimensions (e.g., truthfulness, honesty), improving interpretability but still
 471 relying on static, globally defined criteria. Our approach differs conceptually: instead of collapsing
 472 all rubrics into a single scalar or a fixed multi-objective vector, we learn a critic that dynamically
 473 proposes a verifiable rubric for each instance and grounds its supervision through an external validator.
 474 This yields a reward signal that is still scalar for RL optimization, but derived from an objectively
 475 checkable criterion rather than a static, unverified proxy, offering better alignment and reliability in
 476 open-ended tasks.

477 **Enumerative verifications for free-form generations.** To obtain a comprehensive and reliable
 478 evaluation of free-form generations, the standard practice is to enumerate a set of fine-grained
 479 criteria (Zhuge et al., 2024; Min et al., 2023; Saad-Falcon et al., 2024; Chang et al., 2024; Xie
 480 et al., 2025). While they can be automatically deposed by LLMs for easier domains (Min et al.,
 481 2023; Jing et al., 2024), extensive manual annotations are typically required for more complex
 482 domains such as travel planning (Xie et al., 2024), codebase generation (Zhao et al., 2025), and
 483 research reproduction (Starace et al., 2025). Dedicated computation and actions such as information
 484 retrieval (Min et al., 2023) and code execution (Zhuge et al., 2024; Starace et al., 2025) require
 485 manual rubric design or domain-specific validators (e.g., retrieval and code execution). Because all

486 rubrics must be checked for each output, verification cost scales roughly linearly with the number
 487 of possible rubrics and may still miss unlisted error types. In contrast, RLDCF replaces exhaustive
 488 enumeration with a learned critic that dynamically selects the most informative, verifiable failure
 489 mode for each instance. By verifying only this targeted rubric via an external validator, the method
 490 retains rubric-level faithfulness while substantially reducing evaluation cost and exposing diverse,
 491 on-policy errors that static checklists often overlook.

492
 493 **Outcome-reward RL for reasoning.** RL for LLM has been shown to significantly boost model
 494 performance in domains where the success of the final answer can be easily checked (OpenAI et al.,
 495 2024; Liang et al., 2025; Team et al., 2025; Lambert et al., 2025). This mostly includes the domains
 496 of math (Cobbe et al., 2021; Cui et al., 2025; Luo et al., 2025b; Yu et al., 2025), coding (Jimenez
 497 et al., 2024; Pan et al., 2024a; Wei et al., 2025; Luo et al., 2025a), but can be tricky for other
 498 domains like agent decision-making (Pan et al., 2024b; Zhai et al., 2024; Bai et al., 2024) and
 499 free-form generations (Min et al., 2023; Zhuge et al., 2024). However, RLDCF is designed to relax
 500 this requirement so that we can apply RL to more general domains where success cannot be easily
 501 verified, such as free-form generations.

502 **LLM-as-a-Judge.** Because of the common-sense and reasoning capabilities of pre-trained LLMs,
 503 they can directly be prompted to serve as a judge to evaluate free-form generations (Zheng et al., 2023;
 504 Yuan et al., 2025; Zhu et al., 2025). Their capabilities in evaluations can be further improved through
 505 explicit fine-tuning (Wang et al., 2024b; Yuan et al., 2025). They can also be more interpretable
 506 and robust by introducing a long Chain-of-Thought (CoT) reasoning to explicitly verify fine-grained
 507 criteria (Saha et al., 2025; Wang et al., 2024b; Trivedi et al., 2024). Beyond rubric-only judging,
 508 *generative verifiers* treat verification itself as next-token generation: they first produce verification
 509 rationales or counterevidence, and then score or select candidates (Zhang et al., 2025; Singhi et al.,
 510 2025; Setlur et al., 2025). These approaches, however, use the judge or verifier only as a static
 511 evaluator. They produce fixed judgments or explanations but do not learn adaptively from the
 512 generator’s evolving behaviors. In contrast, RLDCF treats the verifier as a learned critic policy within
 513 an adversarial training loop: the critic dynamically proposes which rubric to verify for each instance,
 514 receives direct feedback from an external validator, and updates jointly with the generator. This
 515 design transforms LLM-as-a-judge from a static scoring module into an active, on-policy agent that
 516 allocates verification effort where it is most informative.

517 6 CONCLUSION

518 We presented Reinforcement Learning from Dynamic Critic Feedback (RLDCF), a new post-training
 519 approach for open-ended tasks requiring diverse, task-specific rubrics, where exhaustive enumeration
 520 is infeasible and optimal reward design is unknown. RLDCF formulates training as an adversarial
 521 min-max game between a generator and a *critic*, a model that dynamically identifies the worst-case
 522 rubric for each output and verifies it externally. By jointly training both models, our approach
 523 bypasses the need for exhaustive verification or manual reward design while providing adaptive
 524 learning signals that prevent reward hacking. On the factual text generation task and code generation
 525 task, RLDCF outperforms competitive baselines with significantly lower verification cost. Ablation
 526 studies further confirm the critical role of components such as adversarial critic training.

527 While we evaluate RLDCF on two domains, we expect it to generalize broadly to other open-ended
 528 generation tasks where multiple evaluation criteria make exhaustive or rubric-by-rubric verification
 529 infeasible, such as story or scientific text generation. By adaptively selecting the most critical rubric
 530 at each step, RLDCF makes RL training practical for complex generation tasks that were previously
 531 intractable due to the combinatorial explosion of rubrics or the lack of universal reward functions.

533 7 REPRODUCABILITY AND ETHICS STATEMENTS

535 To facilitate reproducibility of our work, we have included core implementation code in the supple-
 536 mentary materials. For the FactScore and code generation benchmarks, we use the default settings
 537 from their respective official implementations. All experiments employ DPO (Direct Preference
 538 Optimization) training with consistent configurations across tasks. The datasets used in our exper-
 539 iments are publicly available: WikiBiography can be obtained from its official website, and the

540 Acecoder dataset is accessible through its official repository. We plan to release our complete code
 541 implementation publicly upon acceptance to further support reproducibility efforts.
 542

543 The primary goal of our method, Reinforcement Learning from Dynamic Critic Feedback (RLDCF),
 544 is to enhance the quality of open-ended generations, such as to improve the factual accuracy of
 545 text generation and the correctness of code generation. We believe this is a positive contribution
 546 toward developing more reliable and trustworthy AI systems. However, we acknowledge the dual-use
 547 potential inherent in any powerful generative technology. While our aim is to reduce errors, an
 548 improved generator could still be misused to create convincing but harmful or misleading content
 549 if directed by malicious prompts. Similarly, the adversarial critic, designed to find flaws, could
 550 potentially be repurposed for malicious critique, or to align the generator in a direction misaligned
 551 with human values.

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918 Appendices

919 A PROMPTS

920
 921 This section lists the exact prompts used for the **generator model** and **critic model** during data
 922 creation and training. They correspond to the input format described in Section 3.2 of the main paper.
 923

924 A.1 GENERATOR PROMPT

925 Factual Text Generation

926 System message: You are an AI assistant that provides accurate and concise biographies of individuals.
 927 Each biography should be exactly four sentences long, highlighting key aspects of the person's life,
 928 achievements, and significance.

929 User message: Write a biography of topic.

930 Code Generation

931 The generator input exactly matches the problem statement provided in
 932 TIGER-Lab/AceCode-87K-hard without modification.

933 User message:
 934 {problem_statement_from_AceCode-87K-hard}

935 A.2 CRITIC PROMPT

936 Factual Text Generation

937 System message:
 938 You are a factual checker. Based on your existing knowledge,
 939 identify exactly one sentence that contains the most clearly
 940 verifiable factual error in the paragraph.
 941 Return your answer in **exactly three lines**:
 942 reason: < briefly explaining what is wrong >
 943 sentence: N N is the number of the most incorrect sentence
 944 (positive integer)
 945 error_fact: F a brief clause (no more than 8 words) capturing the
 946 wrong claim from that sentence

947 User message:
 948 Here is an example to show the task.
 949 Find the sentence that contains the most clearly verifiable factual error
 950 in the paragraph about Albert Einstein.

951 Example paragraph:
 952 [1] Albert Einstein was awarded the Nobel Prize in Physics in 1921 for
 953 his discovery of the photoelectric effect.
 954 [2] He was born in New York City, United States, and later moved to
 955 Europe where he continued his studies.
 956 [3] Einstein developed the theory of relativity, revolutionizing our
 957 understanding of space, time, and gravity.
 958 [4] His famous equation describes the equivalence of mass and energy.

959 Expected answer:
 960 reason: Einstein was actually born in Ulm, Germany, not New York City.
 961 sentence: 2
 962 error_fact: Albert Einstein was born in New York City.

963 Now apply the same procedure to the paragraph below about {topic}.

964 Paragraph:

```

972 {numbered_paragraph}
973
974 Answer:
975
976 Code Generation
977
978 System message:
979 You are a code critic. Analyze code for bugs and generate failing test
980 cases.
981 Strictly follow the format with <think> and <testcase> tags.
982
983 User message:
984 Analyze the given problem and the generated code to find a test case that
985 would cause the code to fail.
986
987 Problem: {question}
988
989 Generated code:
990 '''python
991 {code}
992 '''
993 First, think through potential bugs and edge cases in <think> </think>
994 tags.
995 Then output exactly ONE failing test case inside <testcase> tags using
996 this format:
997
998 Option A (CALL format)
999 <testcase> CALL: func_name(arg1, arg2, kw=val) </testcase>
1000 Option B (STDIN format)
1001 <testcase> STDIN: <raw input here> </testcase>
1002
1003 Do NOT include expected outputs or explanations.
1004 {optional_examples_block}
1005
1006
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```

B VALIDATOR IMPLEMENTATION DETAILS

This section provides the detailed design of the validator used in our training pipeline, corresponding to Section 3.2 of the main paper.

B.1 FACTUAL TEXT GENERATION

We follow a strict validation process to ensure both authenticity and factual accuracy. In the first stage, the critic outputs both a suspected erroneous fact and the sentence number containing it. To prevent exploitation through information injection, we use textual entailment checking to verify that the proposed fact genuinely appears in the specified sentence. In the second stage, for proposals passing authenticity checks, we reuse FactScore’s atomic fact verification component, which queries Wikipedia knowledge base to provide binary verification of individual factual claims, returning true or false based on external verification.

B.2 CODE GENERATION

Since the AceCoder dataset lacks reference solutions to prevent data contamination, we construct reliable verification anchors by using Qwen2.5-Coder-7B-Instruct to generate solutions. We filter these solutions using original test cases, retaining only those highly accurate answers (achieving 99.7% accuracy) to serve as simulated ground truth for test case validation. Our validation first execute the critic’s test case on the reference solution to obtain the expected output, then execute the same test case on the generated code to obtain the actual output. Finally, we compare these outputs and return $R(s, a, c) = 1$ if outputs match and 0 if they differ, with execution failures also indicating detected errors. The AceCoder dataset contains noise in GPT-4o generated test cases,

1026 which introduces some bias in our reference-based validator but reflects realistic imperfections in
 1027 verification tools.
 1028

1029

1030

C ANALYSIS OF K AND N

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1033 This section clarifies the roles of the hyperparameters K and N in RLDCF and explains why their
 1034 values differ between the factual and code generation experiments.
 10351036 In RLDCF, the parameter K controls how many candidate outputs are sampled for each prompt.
 1037 A larger K increases candidate diversity and raises the probability that, for the same instruction,
 1038 at least one candidate passes all critic checks while another fails at least one. This is essential for
 1039 constructing non-degenerate preference pairs for DPO, since each pair requires both a “chosen” and
 1040 a “rejected” candidate. The hyperparameter N specifies how many criteria or testcases the critic
 1041 proposes for each candidate. A larger N expands the critic’s search space and enables it to discover
 1042 more potential failure modes. However, this comes with two main drawbacks: fewer candidates pass
 1043 all checks (which reduces preference pairs available for training generator), and verification costs
 1044 increase substantially. Additionally, an excessively large N may introduce redundant checks without
 1045 meaningful benefits.1046 For factual text generation, we set $K = 10$, following the configuration used in FactTune-FS, our
 1047 main baseline. For code generation, we use $K = 8$, consistent with the AceCoder setup. Thus, the
 1048 difference in K is not arbitrary; it adheres to the standard experimental settings established in prior
 1049 work.

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D QUANTIFICATION OF UNCERTAINTY

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Table 4: Factual text generation on 8-sentence biographies with the Qwen3-4B backbone, with results
 shown as mean \pm standard deviation across three runs.

Method	8-sentence Generation			
	# Corr \uparrow	# Incorr \downarrow	FS \uparrow	Calls \downarrow
Qwen3-4B				
Baseline	19.03 \pm 0.41	12.05 \pm 0.19	0.616 \pm 0.006	-
FactTune-FS	21.67 \pm 0.79	5.66 \pm 0.48	0.793 \pm 0.017	402,781 \pm 52,264
ArmoRM	22.51 \pm 1.00	9.39 \pm 0.58	0.705 \pm 0.013	-
RLDCF (Ours)	21.45 \pm 0.31	4.37 \pm 0.48	0.831 \pm 0.016	70,667 \pm 20,072

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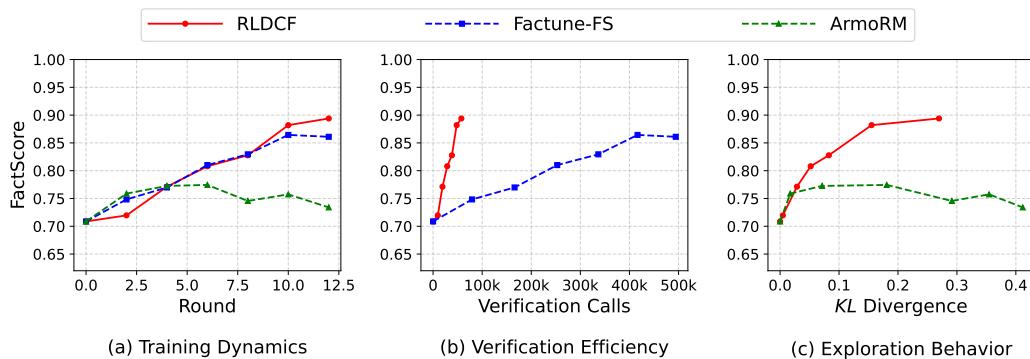
1076

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1079

We report variability across random seeds for the factual text generation experiment. For each method, we run training with three different random seeds (affecting data shuffling and sampling of generator candidates) and report the mean and standard deviation of the metrics. Table 5 summarizes the results for the 8-sentence biography setting with Qwen3-4B as the base model. We observe that RLDCF consistently improves the number of correct biographies and the overall FactScore compared to the baselines, while using substantially fewer verification calls than FactTune-FS. The standard deviations are relatively small, indicating that the performance gains are robust across independent runs.

1080 E BACKBONE ROBUSTNESS
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1098 To examine whether the effectiveness of RLDCF depends on a particular model family, we conducted
1099 additional experiments using an alternative generator/critic backbone, LLaMA-3.1-8B-Instruct. The
1100 training setup strictly follows the configuration used in the Qwen experiments. Figure 5 shows
1101 the resulting training dynamics. We observe the same qualitative behavior as in the Qwen-based
1102 experiments: RLDCF consistently improves factual correctness during training while requiring fewer
1103 verification calls than FactTune-FS, consistent with the trend observed in the main paper; moreover, in
1104 the high-KL regime, RLDCF achieves substantially greater gains in factual accuracy compared to the
1105 ArmoRM method.

1106 F MEDICALQA
1107
11081109 Table 5: Factual text generation on 8-sentence Medical Question with the Qwen3-4B backbone.
1110

Method	8-sentence Generation			
	# Corr↑	# Incorr↓	FS↑	Calls↓
Qwen3-4B				
Baseline	34.0	3.38	0.909	-
FactTune-FS	34.2	1.99	0.945	524329
ArmoRM	35.1	2.36	0.937	-
RLDCF (Ours)	35.2	1.67	0.955	76800

1111 RLDCF achieves the highest factual accuracy while requiring 6.8x fewer verification calls than
1112 FactTune-FS, mirroring the efficiency gains observed in the biography experiments.
1113

1114 These results reinforce that RLDCF is not tied to a particular text domain. It successfully im-
1115 proves factuality in a medical correctness setting with substantially different linguistic and semantic
1116 structures.
1117

1134 **G CROSS-FAMILY**
11351136
1137 Table 6: Results for HumanEval, MBPP, BigCodeBench Complete and Instruct (BCB-C, BCB-I), and
1138 LiveCodeBench, Using a different model (GPT-4O) to generate reference solutions, the results show
1139 that RLDCF still achieves a similar level of average performance improvement across all benchmarks.

Method	HumanEval		MBPP		BCB-C		BCB-I		LCB	Average
	Base	Plus	Base	Plus	Full	Hard	Full	Hard		
Base: Qwen2.5-Coder-7B-Instruct										
Baseline	91.5	84.8	82.8	71.4	49.5	19.6	41.8	20.3	34.2	55.1
RLDCF (Qwen)	93.3	86.0	83.9	73.0	52.2	24.3	42.3	19.6	35.2	56.6
RLDCF (GPT-4o)	92.1	85.4	83.9	73.2	52.2	23.6	42.5	20.3	35.5	56.5

1147
1148 **H QUALITATIVE CASE STUDIES**
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1151 This section presents additional qualitative examples illustrating the behavior of the critic before and
1152 after adversarial training.
11531154
1155 **H.1 FACTUAL TEXT GENERATION CASE STUDY**
11561157 **Generator output(numbered)**

- [1] Amina Wadud is a prominent Islamic scholar and theologian based in the United States.
- [2] She is known for her groundbreaking work in Islamic studies, particularly in reinterpreting Islamic texts for modern, gender-inclusive contexts.
- [3] Wadud has been a leading voice in the movement toward a more inclusive and progressive understanding of Islamic law and theology.
- [4] She is a professor at the University of Durham and has held academic positions at several other institutions.
- [5] Wadud is widely recognized for her advocacy of women's religious and social rights within Islam.
- [6] She is the first woman to lead a Friday prayer in a major American mosque.
- [7] Her research and writings challenge traditional interpretations of Islamic law and promote gender equality.
- [8] Wadud has been an influential figure in interfaith dialogue and religious pluralism.

1173
1174 **Initial Critic Output**

```
1176 reason: Amina Wadud is not a prominent Islamic scholar based in the
1177 United States.
1178 sentence: 1
1179 error_fact: Amina Wadud is a prominent Islamic scholar based in the
1180 United States.
```

1181
1182 **Trained Critic Output**

```
1183 reason: The Friday prayer Amina Wadud led took place in a church hall in
1184 New York, not in a mosque.
1185 sentence: 6
1186 error_fact: Amina Wadud led this Friday prayer in a major American mosque
1187 in the United States.
```

1188
1189

H.2 CODE GENERATION CASE STUDY

1190

Code Question

1191

You are tasked with implementing a function that simulates the behavior of a drawing application by managing a canvas. The canvas is represented by a 2D grid of pixels, where each pixel can be either empty (0) or filled (1). Your function should handle the following operations: 1) Resize the canvas to a new width and height, filling the new area with empty pixels. 2) Fill the entire canvas with a specified color (1 for filled, 0 for empty). 3) Clear the canvas by setting all pixels back to empty (0). Implement a single function called 'manage_canvas' that takes the following parameters: 'canvas' (a list of lists representing the initial canvas), 'operation' (a string indicating the operation: 'resize', 'fill', or 'clear'), and 'params' (a tuple with parameters for the operation). The function should return the modified canvas after performing the specified operation. The function should not access any external resources.

1204

1205

Generator output

1206

```
from typing import List, Tuple, Union

def manage_canvas(
    canvas: List[List[int]],
    operation: str,
    params: Tuple[Union[int, float, bool]]
) -> List[List[int]]:
    """Manage the canvas based on the specified operation and parameters
    """
    if operation == 'resize':
        # params = (new_width, new_height)
        new_width, new_height = params
        new_canvas = [[0] * new_width for _ in range(new_height)]
        return new_canvas

    elif operation == 'fill':
        # params = (fill_value,)
        fill_value, = params
        return [[fill_value] * len(row) for row in canvas]

    elif operation == 'clear':
        return [[0] * len(row) for row in canvas]

    else:
        raise ValueError("Invalid operation")
```

1227

Initial Critic Output

1228

```
<think>
1. The function supports a 'resize' operation that changes the canvas to
   (new_width, new_height).
2. Typical boundary cases include an empty canvas and zero or negative
   dimensions.
</think>
< testcase> CALL: manage_canvas([], 'resize', (2, 2)) </ testcase>
```

1236

Trained Critic Output

1237

1238

```
<think>
1. The code does not handle the 'resize' operation correctly. It
   initializes a new canvas with the correct dimensions but does not
   copy the existing canvas's data into the new canvas. This could
   result in a canvas with only empty pixels after resizing.
```

```
1242
1243 2. This behavior contradicts the problem description, where 'resize' is
1244     expected to preserve existing pixels and only fill newly created
1245     areas with 0, as in a normal drawing application.
1246     </think>
1247 <testcase> CALL: manage_canvas([[1, 1], [1, 1]], 'resize', (3, 3)) </
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