# Contextualized Topic Coherence Metrics

# Anonymous ACL submission

#### Abstract

 This article proposes LLM-based topic coherence metrics inspired by standard human topic evaluations, in a family of metrics called Contextualized Topic Coher- ence (CTC). These metrics allow human- centered evaluation of coherence while maintaining the efficiency of automated methods. We evaluate CTC relative to five metrics and discovered that it outper- forms automated topic coherence meth- ods on seven topic models. Notably, CTC aligns with human evaluation and demon- strates excellent performance with short documents, and is not susceptible to mean-ingless but high-scoring topics.

## **<sup>016</sup>** 1 Introduction

 Topic models are a family of text-mining algo- rithms that identify themes in a large corpus of [t](#page-8-1)ext data [\(Blei,](#page-8-0) [2012\)](#page-8-0). These models [\(Churchill](#page-8-1) [and Singh,](#page-8-1) [2022\)](#page-8-1) are widely used for exploratory data analysis with the aim of organizing, under- standing, and summarizing large amounts of text data [\(Abdelrazek et al.,](#page-8-2) [2022\)](#page-8-2). Numerous tech- niques, algorithms, and tools have been employed to develop a variety of topic models for differ- ent tasks and purposes [\(Srivastava and Sutton,](#page-10-0) [2017\)](#page-10-0) including much recent work on neural topic models [\(Grootendorst,](#page-8-3) [2022\)](#page-8-3). However, due to their nature as unsupervised models, comparing topic outputs, hyperparameter settings, and over- all model quality has traditionally been difficult [\(Hoyle et al.,](#page-9-0) [2022\)](#page-9-0).

**033** Topic Coherence (TC) metrics measure the in-**034** terpretability of topics generated by topic models. **035** These metrics are categorized into two classes:

automated TC metrics and human-annotated TC **036** metrics [\(Hoyle et al.,](#page-9-1) [2021\)](#page-9-1). Automated TC met- **037** rics estimate the interpretability of topic mod- **038** els with respect to various factors such as co- **039** occurrence or semantic similarity of topic words. **040** On the other hand, human-annotated TC metrics **041** are protocols for designing surveys that rate or **042** score the interpretability of topic models. Human 043 judgment is often used to validate topic coher- **044** ence metrics to provide an accurate assessment **045** of the semantic coherence and meaningfulness of **046** [a](#page-8-4) given set of topics [\(Newman et al.,](#page-9-2) [2009;](#page-9-2) [Ale-](#page-8-4) **047** [tras and Stevenson,](#page-8-4) [2013;](#page-8-4) [Mimno et al.,](#page-9-3) [2011\)](#page-9-3). **048** While human-annotated TC metrics incorporate **049** subjective human judgments and provide a more **050** accurate and nuanced understanding of how well **051** topic models are performing (e.g. in terms of their **052** ability to capture the underlying themes in a text **053** corpus), they are expensive, time-consuming, and **054** require multiple human-subjects to avoid personal **055** biases. On the other hand, automated metrics are **056** more cost-effective than human-annotated meth- **057** ods, as they do not require the hiring and training **058** of human annotators, which results in their abil- **059** ity to evaluate large amounts of data and iterate **060** through many model comparisons. **061**

Automated metrics are intended to align more **062** closely with human judgment, providing a bet- **063** ter measure of the interpretability of topic words. **064** The risk of such approximations, however, is that **065** they themselves become the target of optimiza- **066** tion rather than the underlying property they were **067** intended to measure. Several recent works sug- **068** gest that this has occurred especially in the con- **069** text of neural topic models. [Doogan and Buntine](#page-8-5) **070** [\(2021\)](#page-8-5) argue that interpretability is ambiguous **071**  and conclude that current automated topic coher- ence metrics are unreliable for evaluating topic models in short-text data collections and may be incompatible with newer neural topic models. In a similar study, [Hoyle et al.](#page-9-1) [\(2021\)](#page-9-1) show that top- ics generated by neural models are often qualita-078 tively distinct from traditional topic models while they receive higher scores from current automated topic coherence metrics. [Hoyle et al.](#page-9-1) [\(2021\)](#page-9-1) con- clude that the validity of the results produced by fully automated evaluations, as currently prac- ticed, is questionable, and they only help when [h](#page-9-0)uman evaluations cannot be performed. [Hoyle](#page-9-0) [et al.](#page-9-0) [\(2022\)](#page-9-0) in another recent work shows that neural topic models fail to improve on the tradi- [t](#page-8-6)ional topic models such as Gibbs LDA [\(Griffiths](#page-8-6) [and Steyvers,](#page-8-6) [2004;](#page-8-6) [McCallum,](#page-9-4) [2002\)](#page-9-4) and con- sider neural topic broken as they do not function well for their intended use.

 To address these problems, we introduce Contextualized Topic Coherence (CTC) metrics which are a context-aware family of topic co- herence metrics based on the pre-trained Large Language Models (LLM). Taking Advantage of LLMs elevates the understanding of language at a very sophisticated level incorporating its linguis- tic nuances, contexts, and relationships. CTC is much less susceptible to being fooled by mean- ingless topics that often receive high scores with traditional topic coherence metrics.

## **<sup>102</sup>** 2 Automated Topic Coherence Metrics

 Topic coherence (TC) metrics measure the con- sistency of words in a given topic to evaluate the interpretability and meaningfulness of a topic by computing the level of semantic similarity among words that are included in the topic. A high TC value indicates that the words in the topic are se- mantically similar and are likely to co-occur in the same circumstances.

 The authors of [\(Newman et al.,](#page-9-2) [2009,](#page-9-2) [2010b\)](#page-9-5) claim that a method based on the Point-wise Mu- tual Information (PMI) gives the largest corre- lations with human ratings. They define UCI, 115 which measures the strength of the association be-tween pairs of words based on their co-occurrence [i](#page-9-3)n a sliding window of length-l words. [\(Mimno](#page-9-3) **117** [et al.,](#page-9-3) [2011\)](#page-9-3) proposes UMass, an asymmetric con- **118** firmation measure that estimates the degree of **119** coherence between words within a given topic **120** by calculating the log ratio frequency of their co- **121** occurrences in the corpus of documents. UMass **122** counts the number of times a pair of words co- **123** occur in a given corpus and compares this number **124** to the expected number of co-occurrences where **125** words are randomly distributed across the whole **126** corpus. [\(Aletras and Stevenson,](#page-8-4) [2013\)](#page-8-4) proposes **127** context vectors for each topic word w to generate **128** the frequency of word co-occurrences within win- **129** dows of  $\pm 1$  words surrounding all instances of  $\qquad 130$ w. They showed that NPMI [\(Bouma,](#page-8-7) [2009\)](#page-8-7) has a 131 larger correlation with human topic ratings com- **132** pared to UCI and UMass. Additionally, NPMI **133** takes into account the fact that some words are **134** more common than others and adjusts the frequency of individual words accordingly[\(Lau et al.,](#page-9-6) **136** [2014\)](#page-9-6). While NPMI is generally more sensitive to **137** rare words and can handle small datasets, UMass **138** focuses on fast computation of coherence scores **139** over large corpora. [\(Stevens et al.,](#page-10-1) [2012\)](#page-10-1) showed **140** that a smaller value of  $\epsilon$  tends to yield better **141** results than the default value of  $\epsilon = 1$  used in **142** the original paper since it emphasizes more the **143** word combinations that are completely unattested. **144** [\(Röder et al.,](#page-9-7) [2015\)](#page-9-7) proposes a unifying frame- **145** work of coherence measures that can be freely **146** combined to form a configuration space of co- **147** herence definitions, allowing their main elemen- **148** tary components to be combined in the context **149** of coherence quantification. For example, they **150** propose the  $C_V$  metric, which uses a variation of  $151$ NPMI to compute topic coherence over a sliding **152** window of size N and adds a weight  $\gamma$  to assign 153 more strength to more related words. According **154** to [\(Campagnolo et al.,](#page-8-8) [2022\)](#page-8-8), the  $C_V$  metric is  $155$ more sensitive to noisy information and dirty data **156** than  $C_{\text{UMass}}$  and  $C_{\text{UCI}}$ . [\(Nikolenko,](#page-9-8) [2016\)](#page-9-8) and 157 [\(Schnabel et al.,](#page-9-9) [2015\)](#page-9-9) propose the metric  $TC_{DWR}$  158 based on the Distributed Word Representations **159** (DWR) [\(Mikolov et al.,](#page-9-10) [2013b](#page-9-10)[,a\)](#page-9-11) which are better **160** [c](#page-9-12)orrelated to human judgment. Similarly, [\(Ram-](#page-9-12) **161** [rakhiyani et al.,](#page-9-12) [2017\)](#page-9-12) presents a coherence mea- **162** sure based on grouping topic words into buckets **163**  and using Singular Value Decomposition (SVD) and integer linear programming-based optimiza- tion to create coherent word buckets from the gen-167 erated embedding vectors. (Korenčić et al., [2018\)](#page-9-13) proposes several topic coherence metrics based on topic documents rather than topic words. The ap- proach essentially extracts topic documents, vec- torizes them using several methods such as word embedding aggregation, and computes a coher- [e](#page-9-14)nce score based on the document vectors. [\(Lund](#page-9-14) [et al.,](#page-9-14) [2019\)](#page-9-14) proposes an automated evaluation metric for local-level topic models by introduc- ing a task designed to elicit human judgment and reflect token-level topic quality.

# **178 3 Contextualised Topic Coherence**

 In this article, we introduce Contextualized Topic Coherence (CTC) to refer to a new family of topic coherence metrics that benefit from the recent de- velopment of Large Language Models (LLM). This paper presents two approaches using LLMs for defining CTC metrics. The first approach uses LLMs to compute contextualized estimates of the pointwise mutual information (CPMI) between topic words. In the second approach, we use Chat- GPT [\(OpenAI,](#page-9-15) [2022\)](#page-9-15) to evaluate topic coherence similar to human-annotated metrics.

## **190** 3.1 Automated CTC

 CPMI. Recent work by [\(Hoover et al.,](#page-8-9) [2021\)](#page-8-9) uses conditional PMI estimates to analyze the re- lationship between linguistic dependencies and statistical dependencies between words. They propose Contextualized PMI (CPMI) as a new method for estimating the conditional PMI be- tween words *in context* using a pre-trained lan- guage model. As illustrated in Figure [1,](#page-2-0) the CPMI 199 between two words  $w_i$  and  $w_j$  in a sentence s is defined as

201 
$$
CPMI(w_i, w_j | s) = \log \frac{p(w_i | s_{-w_i})}{p(w_i | s_{-w_{ij}})} \qquad (1)
$$

 where p is an estimate for the probability of words in context based on a pre-trained masked language **model (MLM), such as BERT. Here, s<sub>−wi</sub> rep-**205 resents the sentence with word  $w_i$  masked, and

<span id="page-2-0"></span>

Figure 1: Calculating CPMI for two topic words in a segment of a document.

 $s_{-w_{ij}}$  is the sentence with both words  $w_i$  and  $w_j$  206 masked. **207**

We adopt CPMI to introduce a new automated **208** Contextualized Topic Coherence (CTC) metric. **209** Automated CTC estimates the statistical depen- **210** dence within a topic in a corpus by computing the **211** CPMI value for each pair of topic words along a **212** sliding window applied to the dataset. For this, **213** the corpus is divided into a set of window seg- **214** ments of length w that have k words intersecting 215 with adjacent window segments to compute the **216** average CPMI between each pair of words within **217** each topic over all window segments, giving the **218** following expression for CTC: **219**

$$
\frac{1}{n * {m \choose 2}} \sum_{i=1}^{n} \sum_{r=2}^{m} \sum_{s=1}^{r-1} \text{CPMI}(w_i^r, w_i^s \mid c^u) \quad (2)
$$

) (2) **220**

where  $c^u \subset \text{corpus } D$  is a window segment with 221 length of w that has  $k$  words overlapping with its  $222$ adjacent window segments, n is the number of **223** topics and m is the number of topic words. **224**

#### 3.2 Semi-automated CTC **225**

Intrusion. [\(Chang et al.,](#page-8-10) [2009\)](#page-8-10) studied the *topic* **226** *words intrusion* task to assess topic coherence by **227** identifying a coherent latent category for each **228** topic and discovering the words that do not be- **229** long to that category. These *intruder words* are **230** detected by human subjects to assess the quality **231** of topic models and to measure a coherence score **232**  that assigns a low probability for intruder words to belong to a topic. We apply this idea to chat- bots with a prompt (see Appendix [B.1\)](#page-11-0), which provides the topic words to ChatGPT [\(OpenAI,](#page-9-15) [2022\)](#page-9-15) and asks for a category and intruder words.

 Rating. While human topic ratings are expen- sive to produce, they serve as the gold standard for coherence evaluation [\(Röder et al.,](#page-9-7) [2015\)](#page-9-7). For example, [\(Syed and Spruit,](#page-10-2) [2017\)](#page-10-2) uses human ratings to explore the coherence of topics gener- ated by LDA topics across full texts and abstracts. [\(Newman et al.,](#page-9-16) [2010a\)](#page-9-16) provides human anno- tators with a rubric and guidelines for judging whether a topic is useful or useless. The annota- tors evaluate a randomly selected subset of topics for their usefulness in retrieving documents on a given topic and score each topic on a 3-point scale, where 3=highly coherent and 1=useless (less co- [h](#page-8-4)erent). Following [\(Newman et al.,](#page-9-16) [2010a\)](#page-9-16), [\(Ale-](#page-8-4) [tras and Stevenson,](#page-8-4) [2013\)](#page-8-4) presented topics with- out intruder words to Amazon Mechanical Turk to score them on a 3-point ordinal scale. We adapt this method to chatbots with a prompt (see Ap- pendix [B.2\)](#page-11-1), which provides the topic words to ChatGPT and asks to rate the usefulness of the topic words for retrieving documents on a given 259 topic. The CTC<sub>Rating</sub> for a topic model is then obtained by the average sum of all ratings over all **261** topics.

# <span id="page-3-0"></span>**<sup>262</sup>** 4 Experiments

 In this section, we expect to observe that the base-264 line metrics (UCI, UMass, NPMI, C<sub>V</sub>, DWR) rank topic models differently from CTC. We also expect CTC rankings favor interpretable topics and handle short text datasets more effectively than the baseline metrics [\(Doogan and Buntine,](#page-8-5) [2021;](#page-8-5) [Hoyle et al.,](#page-9-1) [2021\)](#page-9-1). This implies that base- line metrics often yield high scores for incoherent topics, while conversely assigning low scores to well-interpretable topics. In contrast, CTC has a better model of language and can better evaluate topical similarity *as it would appear to a human reader*. Therefore, we expect to see that base- line metrics and CTC would differ at extremes of highest or lowest coherency.

## 4.1 Experimental setup **278**

Datasets. The experiments incorporate two **279** datasets including the 20Newsgroups dataset **280** [\(Lang,](#page-9-17) [1995\)](#page-9-17) and a collection of 17K tweets by **281** Elon Musk published between 2017 and 2022 by **282** [\(Raza,](#page-9-18) [2023\)](#page-9-18). **283**

Topic Models. The experiments involve six **284** different topic models including Gibbs LDA **285** [\(Griffiths and Steyvers,](#page-8-6) [2004\)](#page-8-6), Embedded Topic **286** Model (ETM) [\(Dieng et al.,](#page-8-11) [2020\)](#page-8-11), Adversarial- **287** neural Topic Models (ATM) [\(Wang et al.,](#page-10-3) [2019\)](#page-10-3), **288** Top2Vec [\(Angelov,](#page-8-12) [2020\)](#page-8-12), and Contextualized **289** Topic Model (CTM) [\(Bianchi et al.,](#page-8-13) [2021\)](#page-8-13), and **290** BERTopic [\(Grootendorst,](#page-8-3) [2022\)](#page-8-3). <sup>291</sup>

Topic Coherence Metrics. The topics gener- **292** ated by the topic models are evaluated using **293** the proposed Contextualized Topic Coherence **294** (CTC) metrics, which are then compared to the **295** well-established automated topic coherence met- **296** rics  $C_V$ , UCI, UMass, NPMI, and DWR. For  $297$ CTC<sub>CPMI</sub>, we segmented the 20Newsgroup and 298 Elon Musk's Tweets datasets into chunks of 15 **299** and 20 words, respectively, without intersections. **300** We then extracted the CPMI for all word pairs in 301 each segment using the pre-trained language mod- **302** els *bert-base-uncased* and *Tesla K80 15 GB GPU* **303** from Google Colab [\(Bisong and Bisong,](#page-8-14) [2019\)](#page-8-14). **304** This pre-computing step took about 7 hours but **305** allowed us to compute CTC<sub>CPMI</sub> for any topic 306 model in the order of a few seconds. For evaluat- **307** ing CTC<sub>Intrusion</sub> and CTC<sub>Rating</sub>, we made a request 308 for each topic to *ChatGPT* with *GPT 3.5 Turbo*, **309** which cost less than a dollar for all the experi- 310 ments. 311

## <span id="page-3-1"></span>4.2 Results **312**

Tables [1](#page-4-0) and [2](#page-4-1) represent the results of the eval- **313** uation of the topic models obtained from the **314** 20Newsgroup and Elon Musk's Tweets datasets, **315** respectively, using CTC and the baseline met- **316** rics. To allow us to compare the models in terms **317** of topic coherence metrics, the highest value for **318** each metric is shown in bold. the highest values **319** for each metric within each topic model are noted **320** in *italic* font. This helps us determine the optimal **321**

<span id="page-4-0"></span>

<b>Topic Models</b>		<b>Baseline Metrics</b>					<b>CTC</b> Metrics				
	#T	<b>UCI</b>	<b>UMass</b>	<b>NPMI</b>	$C_V$	<b>DWR</b>	Rating	Intrusion	<b>CPMI</b>		
	20	0.260	$-2.338$	0.043	0.512	0.211	1.3	0.225	9.92		
Gibbs LDA (2003)	50	$-0.121$	$-2.771$	0.023	0.479	0.191	1.16	0.220	5.99		
	100	$-0.690$	$-3.030$	0.002	0.450	0.149	1.14	0.267	3.25		
	20	0.478	$-2.08$	0.067	0.563	0.292	0.7	0.452	19.16		
ETM (2020)	50	0.380	$-1.903$	0.054	0.532	0.330	1.22	0.348	20.35		
	100	0.351	$-1.962$	0.049	0.522	0.312	1.23	0.41	22.58		
	20	$-1.431$	$-3.014$	$-0.059$	0.338	0.151	0.92	0.305	0.03		
ATM (2019)	50	$-0.940$	$-2.902$	$-0.046$	0.342	0.077	1.15	0.275	0.18		
	100	$-0.735$	$-2.741$	$-0.032$	0.362	0.053	1.12	0.340	1.72		
	20	$-1.707$	$-4.082$	0.005	0.601	0.268	1.25	0.385	5.93		
CTM (2021)	50	$-0.724$	$-3.008$	0.046	0.590	0.236	1.56	0.380	7.02		
	100	$-0.926$	$-3.118$	0.027	0.561	0.210	1.31	0.392	6.16		
Top2Vec (2020)	85	0.910	$-2.449$	0.192	0.785	0.473	1.670	0.399	3.77		
BERTopic (2022)	145	$-1.023$	$-5.033$	0.098	0.681	0.309	1.517	0.359	2.91		

Table 1: Scores of Topic Coherence Metrics on 20Newsgroup dataset.

<span id="page-4-1"></span>Table 2: Scores of Topic Coherence Metrics on Elon Musk's Tweets dataset

<b>Topic Models</b>		<b>Baseline Metrics</b>					<b>CTC</b> Metrics				
	#T UCI	<b>UMass</b>	<b>NPMI</b>	$C_V$	<b>DWR</b>	Rating	Intrusion	<b>CPMI</b>			
Gibbs LDA (2003)	10 $-0.441$ 20 $-1.834$ 30 $-3.068$	$-3.790$ $-5.415$ $-6.390$	0.016 $-0.049$ $-0.099$	0.498 0.395 0.336	0.838 0.798 0.783	1.6 1.5 1.466	0.29 0.225 0.33	2.19 1.04 0.86			
ETM (2020)	10 0.205 20 0.155 30 0.025	$-3.209$ $-3.079$ $-3.215$	0.051 0.028 0.022	0.560 0.538 0.515	0.952 0.974 0.978	1.1 1.433 1.05	0.24 0.233 0.195	5.41 4.48 4.30			
ATM (2019)	10 $-9.021$ 20 $-7.967$ 30 $-7.278$	$-12.859$ $-11.770$ $-11.301$	$-0.324$ $-0.283$ $-0.258$	0.364 0.343 0.350	0.730 0.694 0.753	1.2 1.1 0.933	0.211 0.177 0.214	$-0.004$ $\theta$ $-0.03$			
CTM (2021)	10 $-2.614$ 20 $-3.720$ 30 $-3.589$	$-7.049$ $-8.336$ $-8.063$	$-0.030$ $-0.070$ $-0.064$	0.580 0.534 0.573	0.888 0.880 0.873	2.0 1.45 1.766	0.439 0.185 0.276	3.04 2.56			
Top2Vec (2020)	164 $-6.272$	$-10.536$	$-0.152$	0.401	0.847	1.481	0.274	2.08			
BERTopic (2022)	217 $-4.131$	$-11.883$	$-0.020$	0.432	0.541	1.539	0.276	1.52			

**322** number of topics for all models except Top2Vec **323** and BERTopic, which don't need this parameter **324** as an input.

 General observations. Before analyzing the re- sults in Tables [1](#page-4-0) and [2](#page-4-1) in detail, we examine the relationship between the CTC metrics and the baseline metrics by performing Pearson's correla- tion coefficient analysis [\(Sedgwick,](#page-9-19) [2012\)](#page-9-19) on the [r](#page-8-5)esults from Tables [1](#page-4-0) and [2](#page-4-1) similar to [\(Doogan](#page-8-5) [and Buntine,](#page-8-5) [2021\)](#page-8-5). As shown in Figure [2a](#page-12-0) (see Appendix [C\)](#page-11-2), for 20Newsgroup, the baseline met- rics UCI and UMass are highly correlated with **CPMI** but not with CTC<sub>Rating</sub> and CTC<sub>Intrusion</sub>, which are more correlated with the baseline mea-**sures NPMI and**  $C_V$  **and DWR (which are also**  highly correlated). On the other hand, for the short text EM Tweets dataset, Figure [2b](#page-12-0) (see Appendix [C\)](#page-11-2) shows that CPMI has a high correlation **339** with all baseline methods, while CTC<sub>Intrusion</sub> and 340 CTCRating are completely independent of CPMI **<sup>341</sup>** and the baseline measures. **342**

Concerning our expectation that baseline met- **343** rics rank topic models differently from CTC met- **344** rics, Table [1](#page-4-0) reports that the baseline metrics (ex- **345** cept for UMass) point to Top2Vec while CTC **346** metrics (except for  $CTC_{\text{Rating}}$ ) point to ETM for  $347$ achieving the highest scores. Similarly, Table [2](#page-4-1) **348** reports that the baseline metrics (except for  $C_V$ )  $349$ point to ETM while CTC metrics (except for **350** CTCCPMI) point to CTM for achieving the highest **<sup>351</sup>** scores. These contradictions between CTC and **352** baseline metrics are aligned with our expectations **353** and we will explore them with a meta-analysis of **354** topics generated by these topic models and the **355** scores they have received from CTC and baseline **356**

Topic Model	Ranked By	<b>Topics</b>	$C_V$	<b>CPMI</b>
		god, christian, people, believe, jesus	0.740	0.017
	Highest C <sub>v</sub>	drive, card, scsi, disk, mb,	0.739	0.037
		book, number, problem, read, call	0.369	0.018
	Lowest $C_V$	line, use, power, bit, high	0.458	0.018
		year, time, day, one, ago, week	0.559	0.709
$ETM(100)$ (2020)	<b>Highest CPMI</b>	game, year, team, player, play	0.706	0.242
		new, number, also, well, call, order, used	0.340	$-0.007$
	<b>Lowest CPMI</b>	people, right, drug, state, world, country	0.529	$-0.002$
		dsl, geb, cadre, shameful, jxp	0.995	0.009
	Highest $C_V$	tor, nyi, det, chi, bos	0.989	0.012
		hacker, computer, privacy, uci, ethic	0.255	$-0.0001$
	Lowest $C_V$	battery, acid, charged, storage, floor	0.344	0.006
		mailing, list, mail, address, send	0.792	0.154
Top2Vec (2020)	<b>Highest CPMI</b>	icon, window, manager, file, application	0.770	0.076
		lc, leiii, fpu, slot, nubus, iisi	0.853	$-0.004$
	<b>Lowest CPMI</b>	ci, ic, incoming, gif, edu	0.644	$-0.002$

<span id="page-5-0"></span>Table 3: Top-2 and bottom-2 topics of  $ETM<sup>(100)</sup>$  and Top2Vec on 20Newsgroup

**357** metrics.

 Meta-analysis. To check the performance of different coherence metrics, we will compare the intepretability of their high and low-scoring top- ics. Note that CTC metrics observe contextual patterns between topic words, and therefore, we expect them to provide more consistent coher- ence scores according to the interpretability of the generated topics for all topic models.

 To verify the consistency of some represen- tative scores in Table [1,](#page-4-0) we examine the topics for 20 Newsgroup generated by Top2Vec, which have high and low scores for baseline metrics, and ETM, which have high and low scores for CTC metrics. Table [3](#page-5-0) compares the top-2 and bottom-2 topics ranked by  $C_V$  and  $CTC_{CPMI}$ . The moti- vation behind choosing these metrics is from our correlation analysis in Figure [2a\(](#page-12-0)see Appendix [C\)](#page-11-2), which in  $CTC<sub>CPMI</sub>$  and  $C<sub>V</sub>$  has the least correla- tion among CTC and baseline metrics. First, we notice that the top-2 topics returned by  $C_V$  for Top2Vec are not readily interpretable but are sta- tistically meaningful: *dsl, geb, cadre, shameful, jxp* are fragments of an email signature that oc- curs 82 times, while *tor, nyi, det, chi, bos* are abbreviations for hockey teams. This is not sur- prising, since Top2Vec produces what we call "trash topics", which is a common problem for clustering-based topic models that cannot handle so-called "trash clusters" [\(Giannotti et al.,](#page-8-16) [2002\)](#page-8-16). While CTC<sub>CPMI</sub> returns a more coherent ranking for Top2Vec (the top 2 topics appear coherent, while the bottom topics are incoherent for hu-<br> $389$ man evaluation). This supports our assumption **390** that traditional topic coherence metrics such as **391**  $C_V$  fail to evaluate neural topic models and, in  $392$ this case, even give the highest scores to trash **393** topics. This happens because they only consider **394** the syntactic co-occurrence of words in a win- **395** dow of text and cannot observe the underlying **396** relationship between topic words. CTC<sub>CPMI</sub>, on 397 the other hand, can detect these trash topics and **398** score them more accurately because it is contex- **399** tual and accompanied by LLMs that have rich in- **400** formation about linguistic dependencies between **401** topic words. CTC<sub>CPMI</sub> then also could be a good 402 measure to filter out these topics. The second **403** observation in Table [3](#page-5-0) is that all eight topics re- **404** turned for ETM are coherent. This is because **405** ETM, which is a semantically-enabled probabilis- **406** tic topic model, produces decent topics that are **407** overall highly ranked by CTC<sub>CPMI</sub>, as shown in 408 Figure [4b](#page-12-1) (see Appendix [C\)](#page-11-2). 409

In the same way, we check the consistency of **410** some representative scores in Table [2](#page-4-1) by check- **411** ing the interpretability of topics for Elon Musk's **412** tweets generated by ETM, which has high base- **413** line scores, and by CTM, which has high CTC **414** scores. As shown in Table [4,](#page-6-0) we compare the 415 top 2 and bottom 2 topics ranked by NPMI and **416** CTCRating. As shown in Figure [2b](#page-12-0) (see Ap- **<sup>417</sup>** pendix [C\)](#page-11-2), these metrics are among those with the **418** lowest correlation between CTC and baseline met- **419** rics. A notable finding for CTM topics is that top- **420**

Topic Model	Ranked By	<b>Topics</b>	<b>NPMI</b>	Rating	Intrusion
		erdayastronaut, engine, booster, starship, amp	0.122	3	0.1
	<b>Highest NPMI</b>	year, week, next, month, wholemarsblog	0.057	$\overline{c}$	0.1
		transport, backup, ensure, installed, transaction	$-0.480$	$\overline{2}$	0.1
	<b>Lowest NPMI</b>	achieving, transition, late, transport, precision	$-0.459$		0.1
		tesla, rt, model, car, supercharger	$-0.152$	3	0.5
$CTM^{(30)}$ (2021)	<b>Highest Rating</b>	spacex, dragon, launch, falcon, nasa	$-0.283$	3	0.4
		ppathole, soon, justpaulinelol, yes, sure	$-0.330$		0.5
	<b>Lowest Rating</b>	achieving, transition, late, transport, precision	$-0.459$		0.1
		amp, time, people, like, would, many	0.001	$\mathfrak{D}$	0.7
	<b>Highest NPMI</b>	engine, booster, starship, heavy, raptor	$-0.023$	$\overline{c}$	0.1
		amp, rt, tesla, im, yes	$-0.283$		0.1
	<b>Lowest NPMI</b>	amp, tesla, year, twitter, work	$-0.228$		0.1
		amp, twitter, like, tesla, dont	$-0.186$		0.8
ETM <sup>(30)</sup> (2020)	<b>Highest Rating</b>	amp, time, people, like, would	0.001		0.7
		amp, tesla, year, twitter, work	$-0.228$		0.1
	<b>Lowest Rating</b>	amp, tesla, one, like, time	$-0.204$		0.1

<span id="page-6-0"></span>Table 4: Top-2 and bottom-2 topics of  $ETM^{(30)}$  and  $CTM^{(30)}$  on Elon Musk's Tweets

<span id="page-6-1"></span>Table 5: Topic Coherence Scores of Gibbs LDA, DVAE, ETM on NYT News

Topic Models		<b>Baseline Metrics</b>		Human Evaluation				<b>CTC</b> Metrics		
					UCI UMass $C_V$ NPMI Intrusion Rating Intrusion Rating				<b>CPMI</b>	
Gibbs LDA	50   1.42 - 7.6 0.69 0.15   0.71					$2.66$	2.12	0.62	4.18	
<b>DVAE</b>	$50 \quad 2.43$	$-15$	0.84		$0.25$ 0.74	2.48	2.05	0.67	0.61	
ETM	50   1.01	$-7.4$	0.60		$0.11$ 0.64	$2.38$	2.06	0.64	3.72	

<span id="page-6-2"></span>



 ics ranked highest by the CTCRating metric tend to be more interpretable compared to those ranked highest by NPMI, and similarly, topics ranked lowest by the CTC<sub>Rating</sub> metric tend to be less in- terpretable compared to those ranked lowest by NPMI. The above observation also holds true for **ETM, as the CTC<sub>Rating</sub> metric is not affected by**  the scarcity of short text records. This is because CTCRating is complemented by a chatbot that mit- igates the impact of limited data availability. It is also interesting to note that the topics generated by CTM are overall more interpretable and coher- ent than those generated by ETM. This demon-**strates the validity of CTC<sub>Rating</sub> and CTC<sub>Intrusion</sub>**  over baseline metrics, as we observed in Table [2.](#page-4-1) It also reveals the superiority of CTM over ETM, as shown in Figure [4d](#page-12-1) (see Appendix [C\)](#page-11-2), in short text datasets as a result of a contextualized ele-ment in its architecture.

# **<sup>440</sup>** 5 Human Evaluation

 The goal of automated topic coherence metrics is to accurately approximate human reactions to topics without the need for expensive, time- consuming studies that require multiple annota- tors to avoid bias. In this section we compare the proposed metric with published human evaluation metrics based on data provided by [Hoyle et al.](#page-9-1) [\(2021\)](#page-9-1). This data includes three topic models [\(](#page-10-0)Gibbs LDA [\(McCallum,](#page-9-4) [2002\)](#page-9-4), DVAE [\(Srivas-](#page-10-0) [tava and Sutton,](#page-10-0) [2017\)](#page-10-0), and ETM [\(Dieng et al.,](#page-8-11) [2020\)](#page-8-11)) models with 50 topics generated on the [\(New York Times\)](https://www.kaggle.com/datasets/benjaminawd/new-york-times-articles-comments-2020) dataset, along with human eval- uation (intrusion and ranking). We evaluate the **generated topics with CTC<sub>CPMI</sub>, CTC**<sub>intrusion</sub> and CTCranking, which are comparable to human intru-sion and human ranking.

 As shown in Table [5,](#page-6-1) human evaluators tend to see little quantifiable difference between Gibbs LDA and DVAE, while traditional metrics show pronounced differences. In contrast, we find that CTC metrics more closely match human prefer- ences (or lack thereof). It is possible that this result is simply due to a miscalibration of rela- tive scores. To show that humans and CTC rank topics similarly, we also report Spearman's Rank Correlation [\(Myers and Sirois,](#page-9-20) [2004\)](#page-9-20) to assess the **466** strength and direction of the monotonic relation- **467** ship between the ranking of topics in each metric. 468 As shown in Figure [3,](#page-12-2) the CTC metrics have an **469** overall higher correlation with human ratings than **470** the baselines. **471** 

We also examine the consistency of the scores **472** obtained by different coherence metrics and com- **473** pare the coherence of high and low scoring topics **474** from different topic models and CTC metrics. As **475** shown in Table [6,](#page-6-2) Table [7,](#page-13-0)  $C_V$  is not able to score  $476$ topics correctly. For example, the topic *inc, 9mo,* **477** *earns, otc, qtr, rev* gets the highest score, even **478** though it has little clear interpretability and has **479** been rated relatively low by human evaluators. **480** On the other hand, CTC metrics score topics rela- **481** tive to their contextual relationship and are very **482** close to human scores. For example, the topic *film,* **483** *theater, movie, play, director, movies* receives the **484** highest score by both CTC and human scoring. **485**

## 6 Conclusion **<sup>486</sup>**

This paper introduces a new family of topic coher- **487** ence metrics called Contextualized Topic Coher- **488** ence Metrics (CTC) that benefits from the recent **489** development of Large Language Models (LLM). **490** CTC includes two approaches that are motivated **491** to offer flexibility and accuracy in evaluating neu- **492** ral topic models under different circumstances. **493** Our results show automated CTC outperforms **494** the baseline metrics on large-scale datasets while **495** semi-automated CTC outperforms the baseline **496** metrics on short-text datasets. After a compre- **497** hensive comparison between recent neural topic **498** models and dominant classical topic models, the **499** results indicate that some neural topic models, **500** which optimize traditional topic coherence met-  $501$ rics, often receive high scores for topics that are **502** overly sensitive to idiosyncrasies such as repeated **503** text, and lack face validity. We show with our **504** experiments that CTC is not susceptible to being  $505$ deceived by these meaningless topics by leverag- **506** ing the abilty of LLMs to better model human ex- **507** pectations for language and evaluate topics within **508** and outside their contextual framework. **509** **<sup>510</sup>** Limitations

 CTC metrics come with several limitations, such as latency, accuracy, and the potential for bi- ased results. For instance, CPMI can be a time- consuming process, as it involves running all sen- tences through LLMs and calculating word co- occurrences for every pair of words across all topics. Additionally, the results for Rating and Intrusion may vary with each query to LLMs. Therefore, it is necessary to configure the LLM's temperature and iterate through multiple queries to obtain normalized values. Furthermore, it's important to be aware that LLMs can exhibit bias, and their utilization in this application could po-tentially perpetuate such biases.

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## **716 A Automated Coherence Metrics**

 Topic Models were initially evaluated with held- out perplexity as an automated metric [\(Blei et al.,](#page-8-15) [2003\)](#page-8-15). Perplexity quantifies how well a statistical model predicts a sample of unseen data and is computed by taking the inverse probability of the test set, normalized by the number of words in the dataset. According to [\(Chang et al.,](#page-8-10) [2009\)](#page-8-10), per- plexity has been found to be inconsistent with human interpretability. As a result, the field shifted towards adopting automated topics coher- ence metrics that rely on word co-occurrence- based methods like Point-wise Mutual Informa-tion (PMI) [\(Cover,](#page-8-17) [1999\)](#page-8-17).

# **730** A.1 Definition

**731** As defined as follows, Topic coherence over PMI  $732$  (TC<sub>UCI</sub>) is defined as the average of the  $log_2$  ratio of co-occurrence frequency of word  $w_i^r$  and  $w_i^s$ **733 734** within a given topic i.

735 
$$
TC_{\text{UCI}} = \frac{1}{n} \sum_{i=1}^{n} \frac{1}{\binom{m}{2}} \sum_{r=2}^{m} \sum_{s=1}^{r-1} PMI(w_i^r, w_i^s) \quad (3)
$$

**736** with

$$
PMI(w^i, w^j) = \log_2 \frac{P(w^i, w^j) + \epsilon}{P(w^i)P(w^j)} \tag{4}
$$

where *n* is the number of topics with *m* topic  $\frac{738}{2}$ words and PMI represents the pointwise mutual **739** information between each pair of words  $(w_i^r$  and  $740$  $w_i^s$ ) in the topic *i*. PMI is computed by taking  $741$ the logarithm of the ratio of the joint probability **742** of two words  $P(w_i^r, w_i^s)$  appearing together to  $\hspace{1cm}$  743 the individual probabilities of the words  $P(w_i^r)$  $P(w_i^s)$  occurring separately. Note that  $\epsilon = 1$  is 745 added to avoid the logarithm of zero. **746** 

On the other hand, UMass [\(Mimno et al.,](#page-9-3) [2011\)](#page-9-3) **747** computes the co-document frequency of word  $w_i^r$ and  $w_i^s$  divided by the document frequency of 749 word  $w_i^s$ . **750**

$$
\text{UMass}(w_i^r, w_i^s) = \log \frac{D(w_i^r, w_i^s) + \epsilon}{D(w_i^s)}
$$
 (5)

), **744**

**748**

(6) **761**

(8) **768**

where *n* and *m* are the numbers of topics and topic words respectively. The smoothing param- **753** eter  $\epsilon$  was initially introduced to be equal to one and avoid the logarithm of zero.

Similarly, [\(Aletras and Stevenson,](#page-8-4) [2013\)](#page-8-4) pro- **756** poses context vectors for each topic word w to **757** generate the frequency of word co-occurrences **758** within windows of  $\pm 1$  words surrounding all instances of  $w$ . **760** 

$$
NPMI(w_i^r, w_i^s) = \frac{\log_2 \frac{P(w_i^r, w_i^s) + \epsilon}{P(w_i^r)P(w_i^s)}}{-\log_2(P(w_i^r, w_i^s) + \epsilon)} \quad (6)
$$

[\(Röder et al.,](#page-9-7) [2015\)](#page-9-7) proposes  $C_V$ , which is a vari-  $762$ ation of NPMI. **763**

$$
C_V(w_i^r, w_i^s) = NPMI^{\gamma}(w_i^r, w_i^s)
$$
 (7) 764

One way to estimate  $TC_{DWR}$  is to compute the  $765$ average pairwise cosine similarity between word **766** vectors in a topic as follows. **767**

$$
DWR(w_i^r, w_i^s) = \frac{w_i^r \cdot w_i^s}{\|w_i^r\| \cdot \|w_i^s\|}
$$
 (8)

# **B** LLM Prompts 769

In this section, we present LLM prompts used in **770** our experiments. The descriptions of the prompts **771** for the ratings and intrusion task are as follows. **772**

#### <span id="page-11-0"></span>**773** B.1 Intrusion

 System prompt: *I have a topic that is described by the fol- lowing keywords: [ topic-words ]. Provide a one-word topic based on this list of words and identify all intruder words in the list with respect to the topic you provided. Results be in the following format: topic: <one-word>, intruders: <words in a list>*

 $780$  The number of intrusion words  $(|I_i|)$  returned **781** by chatbot for each topic i, is used to define **<sup>782</sup>** CTCIntrusion as follows:

$$
\text{CTC}_{\text{Intrusion}} = \sum_{i=1}^{n} \frac{1 - \frac{|I_i|}{m}}{n} \tag{9}
$$

**784** where n is the number of topics and m is the **785** number of topic words.

## <span id="page-11-1"></span>**786** B.2 Rating

 System prompt: *I have a topic that is described by the following keywords: [topic-words]. Evaluate the inter- pretability of the topic words on a 3-point scale where 3 = "meaningful and highly coherent" and 0 = "useless" as topic words are usable to search and retrieve documents about a single particular subject. Results be in the following format: score: <score>*

## **794** B.3 Normalized CPMI

 To improve comparability, we also propose a nor- malized version of CPMI that extend its generaliz- ability and allows to mitigate potential biases that may arise due to specific dataset characteristics or idiosyncrasies. Additionally, it facilitates thresh- old determination and provides a consistent scale that allows researchers to set thresholds based on desired coherence levels, ensuring the metric is effectively utilized in practical applications.

## **804** B.3.1 Definition

805 Given a set of *n* topics TM  $\mapsto \{t_1, t_2, \ldots, t_n\}$ 806 with m words  $t_i \mapsto \{w_1^i, w_2^i, \dots, w_m^i\}$  as an out-**807** put of topic model TM on the corpus of e docu-808 ments  $D = \{d_1, d_2, \ldots, d_e\}$ , the CTC based on 809 **Normalized CPMI (NCPMI) called CTC<sub>NCPMI</sub>** is **810** defined as follows.

$$
\frac{1}{e * n * m} \sum_{d=1}^{e} \sum_{i=1}^{n} \sum_{j=1}^{m} \text{NCPMI}(w_j^i, t^i \mid c^d)
$$
\n(10)

while NCPMI
$$
(w_j^i, t^i \mid c^d)
$$
 is:

$$
\frac{log\frac{P(w_j^i|c_{-w_j^i}^d)}{P(w_j^i|c_{-t}^d)}}{-log(P(w_j^i \mid c_{-w_j^i}^d) \times P(t^i \mid c_{-t^i}^d))}
$$
(11)

where  $P$  is an estimate for the probability of  $814$ words given context based on language model **815 LM.** The  $c_{-w_i}^d$  is the document d with word  $w_i$  816 masked, and  $c_{-t_j}^d$  is the document d with words 817 of topic  $t^i$  masked.  $818$ 

## <span id="page-11-2"></span>**C** Correlation Study 819

Pearson correlation is a statistical measure used **820** to assess the degree of linear association between **821** sets of data. As shown Figure [2,](#page-12-0) we applied this **822** method to the results of topic coherence metrics **823** on the topic models to evaluate how closely re- **824** lated or similar the quality of topics generated by **825** these models is. A high positive Pearson corre- **826** lation coefficient indicates that the topic models **827** produce similar results in terms of topic coher- **828** ence, suggesting that they are consistent and re- **829** liable. Conversely, a low or negative correlation **830** suggests inconsistency or divergence in the qual- **831** ity of topics generated by the different models. **832**

On the other hand, Spearman's rank correla- **833** tion coefficient is a statistical measure used to **834** assess the strength and direction of the monotonic **835** relationship between sets of data. As show in **836** Figure [3,](#page-12-2) we applied this method to evaluation 837 topic coherence metrics for human evaluation to **838** determine if there is a consistent ranking of these **839** models in terms of their performance across dif- **840** ferent metrics. A high positive Spearman's rank **841** correlation coefficient suggests that the rankings **842** of the three models across the evaluation metrics **843** are similar, indicating consistency in their perfor- **844** mance. Conversely, a low or negative correlation **845** suggests variability in the rankings, indicating **846** that different metrics may lead to different model **847** preferences. 848

<span id="page-12-0"></span>

Figure 2: Pearson's correlation coefficient on CTC and baseline

<span id="page-12-2"></span>

Figure 3: Spearman's rank correlation coefficients between evaluation metrics for three topic models

<span id="page-12-1"></span>

Figure 4: Comparison Between Topic Models based on Topic Coherence Evaluation

Botton-5 Sorted by	Model	Topic			<b>Scores</b>	
				$C_V$	Human	<b>CTC</b>
	<b>DVAE</b>	spade, derby, belmont, colt, spades, dummy, preakness		0.23	1.5	0.4
$C_V$	<b>ETM</b>	like, making, important, based, strong, including, recent		0.35	2	0.3
	<b>ETM</b>	time, half, center, open, away, place, high		0.37	1.6	0.2
	<b>ETM</b>	today, group, including, called, led, known, began, built, early,		0.37	2	0.3
	Gibbs LDA	people, editor, time, world, good, years, public, long,		0.37	0.1	1.1
	Gibbs LDA	people, editor, time, world, good, years, public,		0.37	0.1	1.1
Human Score	<b>ETM</b>	week, article, page, march, tuesday, june, july		0.57	0.4	1.3
	Gibbs LDA	street, tickets, sunday, avenue, information, free		0.75	0.4	0.3
	<b>ETM</b>	new york, yesterday, director, manhattan, brooklyn, received		0.49	0.4	1
	Gibbs LDA	bedroom, room, bath, taxes, year, market, listed, kitchen, broker		0.72	0.4	1.3
	Gibbs LDA	city, mayor, state, new york, new york city, officials		0.61	2.5	0.1
<b>CTC</b>	<b>ETM</b>	power, number, control, according, increase, large		0.44	0.9	0.2
	Gibbs LDA	officials, board, report, union, members, agency, yesterday		0.51	0.8	0.3
	<b>ETM</b>	time, half, center, open, away, place, high, day, run		0.37	1.2	0.3
	<b>ETM</b>	net, share, inc, earns, company, reports, loss, lead		0.73	1.8	0.3

<span id="page-13-0"></span>Table 7: Bottom-5 topics among the topics generated by Gibbs LDA, DVAE and ETM on NYT News

# **<sup>849</sup>** D More Results

 Figure [4](#page-12-1) compares overall rating of the mentioned topic models in Section [4](#page-3-0) over 20Newsgroup and 852 the twitter dataset based on C<sub>V</sub>, CPMI, NPMI, and Intrusion. The details of this figure are ex-plained in Section [4.2.](#page-3-1)

 Table [7](#page-13-0) presents bottom-5 topics among the topics generated by Gibbs LDA, DVAE, and ETM on the NYT News dataset for better comparison between scores generated by CTC metrics against baseline and human evaluation.

# **<sup>860</sup>** E Python Package

 CTC is implemented as a service for researchers and engineers who aim to evaluate and fine-tune **heat** their topic models<sup>[1](#page-13-1)</sup>. The source code of this python package is provided in *./ctc* and a note- book named *example.ipynb* is prepared to explain how to use this python package as follows.

## **867** E.0.1 Automated CTC

**868**

```
869 1 from ctc.main import Auto_CTC
870 2 #initiating the metric
871 3 eval = Auto_CTC ( segments_length
872 =15, min segment length = 5,
873 Segment_step=10, device="mps")
```
<span id="page-13-1"></span>1 <https://anonymous.4open.science/r/CTC-39DB>

```
4 874
 5 # segmenting the documents 875
 docs=documents 876
 eval segmenting_documents (docs) | 877
8 878
 9 # creating cpmi tree including 879
   all co-occurence values all \sim 880
   between all pairs of words 881
 10 eval.create_cpmi_tree () 882
 11 # eval . load_cpmi_tree () 883
12 884
13 # topics =[[" game " ," play "] ,[" man 885
   " ," devil "]] for instance 886
 14 eval.ctc_cpmi (topics ) and 887
```
# E.0.2 Semi-automated CTC **889**

```
from ctc.main import 891
  Semi_auto_CTC 892
2 893
3 openai_key = " YOUR OPENAI KEY " 894
4 895
5 y = Semi_auto_CTC ( openai_key , 896
  topics) 897
6 898
y.ctc_intrusion () 899
8 900
y.ctc_rating () 902 1202 902
```
**890**