CARMA: Enhanced Compositionality in LLMs via Advanced Regularisation and Mutual Information Alignment

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Abstract

Large language models (LLMs) struggle with compositional generalisation, limiting their ability to systematically combine learned components to interpret novel inputs. While architectural modifications, fine-tuning, and data augmentation improve compositionality, they often have limited adaptability, face scalability constraints, or yield diminishing returns on real data. To address this, we propose CARMA, an intervention that enhances the stability and robustness of compositional rea-011 soning in LLMs while preserving fine-tuned 012 performance. CARMA employs mutual information regularisation and layer-wise stability constraints to mitigate feature fragmentation, ensuring structured representations persist across and within layers. We evaluate CARMA on inverse dictionary modelling and 019 sentiment classification, measuring its impact on semantic consistency, performance stability, and robustness to lexical perturbations. Results show that CARMA reduces the variability introduced by fine-tuning, stabilises token representations, and improves compositional reasoning. While its effectiveness varies across architectures, CARMA's key strength lies in reinforcing learned structures rather than introducing new capabilities, making it a scalable auxiliary method. These findings suggest that integrating CARMA with fine-tuning can improve compositional generalisation while maintaining task-specific performance in LLMs.

1 Introduction

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Compositional generalisation (CG) refers to the ability to systematically combine known expressions to generate novel ones following learned rules (Partee, 1984). This capability is essential for advancing language models (LMs) towards robust linguistic understanding beyond mere pattern matching (Ram et al., 2024).

Despite their strong performance across various NLP tasks, large language models (LLMs) exhibit

persistent weaknesses in compositional generalisation (Hupkes et al., 2020; Kim and Linzen, 2020a; Aljaafari et al., 2024). These limitations stem from multiple factors, including training objectives and model architectures. Standard autoregressive training methods, such as next-token prediction, prioritise statistical correlations in token sequences over structured semantic understanding (Yin et al., 2023a; Dziri et al., 2024). As a result, token representations often lack structured compositionality, leading to fragmented information processing within layers (horizontal misalignment) and across layers (vertical inconsistency). 043

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Additionally, while self-attention mechanisms in Transformer models effectively capture local dependencies, they frequently fail to maintain coherent compositional representations across multiple layers (Murty et al., 2023). This misalignment impairs the model's ability to generalise compositionally, resulting in sensitivity to input order (Ismayilzada et al., 2024) and difficulties in handling complex syntactic and morphological structures (Aljaafari et al., 2024).

Several approaches have been proposed to address these limitations, including architectural modifications, enhanced encoding strategies, and targeted regularisation techniques (Ontanon et al., 2022; Murty et al., 2023; Csordás et al., 2021). However, these methods often struggle to balance compositional improvements with maintaining performance across diverse downstream tasks. Moreover, their effectiveness is typically confined to specific compositional structures or synthetic benchmarks. Developing a robust and adaptable solution that enables LLMs to achieve consistent CG across diverse tasks remains a major challenge.

This work introduces **CARMA**: enhanced Compositionality in LLMs via Advanced Regularisation and Mutual Information Alignment, illustrated in Figure 1. CARMA enhances CG by addressing training challenges that hinder struc-



Figure 1: This diagram depicts the computation of the loss and illustrates the integration of the **Mutual Information** (**MI**) loss (\mathcal{L}_{MI}) and the **Stability Loss** ($\mathcal{L}_{stability}$) into the final optimisation process. Tokens Tok_1 and Tok_2 form the *positive set* (H_{pos}), while Tok_3, Tok_4, Tok_5 form the *negative set* (H_{neg}). The \mathcal{L}_{MI} loss is computed *vertically* across layers (l to k), maximising the similarity of tokens in H_{pos} while contrasting them with tokens in H_{neg} . The $\mathcal{L}_{stability}$ loss is computed *horizontally* between consecutive layers, ensuring consistency in hidden state representations. Both auxiliary losses are combined with the task loss (\mathcal{L}_{task}) to form the total loss (\mathcal{L}_{total}). This integration improves token representations and enhances the model's overall optimisation.

tured compositionality in LLMs. By balancing layer-specific updates and reinforcing token-level dependencies, CARMA provides a scalable and adaptable solution that improves CG without sacrificing downstream task performance. To evaluate CARMA's effectiveness, we investigate the following research questions:

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- **RQ1:** How does regulating mutual information across layers influence compositionality in LLMs? How does it affect sensitivity to input and internal perturbations?
- **RQ2:** To what extent does layer-specific regularisation improve compositional generalisation across semantic and sentiment analysis tasks, assessing CARMA's adaptability across domains?

The key contributions of this work are as follows:

- A novel regularisation method that enhances compositional generalisation without requiring architectural modifications. CARMA leverages mutual information alignment to preserve token dependencies across layers and employs layer-wise stability constraints to reduce representational inconsistencies.
- A systematic evaluation of CARMA across compositionally demanding tasks, demonstrating its ability to reinforce systematicity and

substitutivity, particularly in models where fine-tuning alone is insufficient.

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• A theoretical and empirical analysis of how token dependencies degrade across layers in standard LLMs, revealing that CG limitations are not solely dependent on model size but rather on representational instability. CARMA mitigates this by ensuring consistent information flow, showing that non-intrusive regularisation strategies can significantly improve CG.

The remainder of this paper is structured as follows: Section 2 reviews compositionality in LLMs and associated challenges. Section 3 introduces the CARMA method. Section 4 describes the experimental setup. Section 5 presents empirical findings. Section 6 discusses related work. Section 7 offers insights and future research directions. Supporting datasets and software are available at a public repository.¹

2 Compositionality in LLMs

Compositional generalisation (CG) in linguistics encompasses five key principles: systematicity, productivity, substitutivity, localism, and overgeneralisation (Dankers et al., 2022a). These principles have been explored in LLMs across compositional instruction (Yang et al., 2024b), semantic

¹Anonymised for review.

parsing (Li et al., 2023), translation (Li et al., 2021), and multi-step inference (Zhang et al., 2024). Studies show standard Transformer-based LLMs exhibit limited CG, struggling with basic compositional tasks such as assembling tokens into words or constructing morphemes (Aljaafari et al., 2024; Ismayilzada et al., 2024). These limitations are linked to architectural constraints, training objectives, and tokenisation practices that fragment information and increase sensitivity to input order and contextual noise (Murty et al., 2023).

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Training Objectives and Information Fragmentation. Standard training objectives for LLMs typically optimise for next-token prediction, which prioritises surface-level correlations over deeper semantic integration (Dziri et al., 2024). While this approach is effective for data already seen, it often impedes CG by reducing mutual information between dependent tokens, thereby limiting the model's ability to form coherent compositional representations (Aljaafari et al., 2024).

Architectural Mechanisms and Compositional Consistency. Beyond training objectives, architectural mechanisms such as dropout and selfattention disperse information across the model, increasing sensitivity to input order and context. This undermines **compositional consistency** (Sajjadi et al., 2016; Cai et al., 2021), the ability to maintain consistent outputs when processing semantically equivalent inputs through transformations like word substitution or paraphrasing. These challenges impact both high-complexity reasoning tasks and simpler operations that demand consistent morphological and syntactic processing (Ismayilzada et al., 2024).

Existing Approaches to Enhance CG in LLMs. Research has explored architectural adjustments, regularisation techniques, and task-specific strategies to address CG limitations. Ontanon et al. (2022) demonstrated that combining relative positional encoding with embeddings enhances CG in algorithmic tasks, while weight sharing and copy decoders help retain input structures. Architectural modifications like Pushdown Layers (Murty et al., 2023) and GroCoT (Sikarwar et al., 2022) incorporate mechanisms for tracking syntactic depth and spatial relations, enabling recursive processing of compositional structures. RegularGPT (Chi et al., 2023) introduces adaptive depth and memory mechanisms to facilitate CG. Studies by Csordás et al. (2021) and Petty et al. (2024) reveal that architectural choices and training setups significantly impact CG enhancement. In neural machine translation, Dankers et al. (2022b) found a positive correlation between data size and compositional performance.

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Frameworks like CompMCTG and Meta-MCTG (Zhong et al., 2024) suggest joint training and meta-learning approaches improve fluency, though performance drops persist in out-of-distribution tasks. Synthetic tasks show recursive, step-by-step prompt formats support combinatorial generalisation, despite training biases and sequence order constraints (Ramesh et al., 2024).

3 Enhanced Compositionality via Advanced Regularisation and Mutual Information Alignment (CARMA)

This section formalises compositionality, introduces the core principles of CARMA, and details its components. Figure 1 illustrates the method, highlighting its process and key components.

3.1 Compositionality Formalisation

Mathematical Foundations of Compositionality. CG (Section 2) can be formally defined through a compositional system where \mathcal{E} denotes a set of expressions (e.g., token sequences recognised by the model), and \mathcal{M} represents a corresponding set of meanings. This relationship is formalised as a function:

$$f: \mathcal{E} \to \mathcal{M} \tag{1}$$

For any complex expression $e \in \mathcal{E}$, composed of constituent elements e_1, \ldots, e_n according to a syntactic rule r, the function f satisfies:

$$f(r(e_1, \dots, e_n)) = g_r(f(e_1), \dots, f(e_n)),$$
 (2)

where g_r is the semantic operation that corresponds to the syntactic rule r.

Compositional Generalisation in LLMs. Effective CG in LLMs requires generating structured compositions that preserve semantic consistency. Given a novel expression e_{novel} similar to a known expression e_{known} within a threshold β , their semantic functions must remain within an interpretable bound or deviation α :

$$d(e_{\text{novel}}, e_{\text{known}}) \le \beta \Rightarrow d(f(e_{\text{novel}}), f(e_{\text{known}})) \le \alpha.$$
(3)

This formulation captures systematicity (structured combinations), substitutivity (preservation under transformations), and resistance to overgeneralisation (bounded semantic deviation) while maintaining interpretability.

3.2 CARMA Formalisation

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238CARMA operates over a range of target layers,239from l to \mathcal{K} ($0 < l \le \mathcal{K} \le L$, where L is the total240number of layers), and consists of two core components:241ponents: Mutual Information and Layer-Wise242Stability Regularisation.

Mutual Information (MI) Regularisation Across Layers. CARMA preserves essential dependencies and maintains structural coherence by maximising MI between hidden states of related tokens. The MI between hidden states h_i^k and h_j^k at layer k, representing two related tokens i and j, is defined as:

$$I(h_{i}^{k}; h_{j}^{k}) = \mathbb{E}_{P(h_{i}^{k}, h_{j}^{k})} \left[\log \frac{P(h_{i}^{k}, h_{j}^{k})}{P(h_{i}^{k})P(h_{j}^{k})} \right]$$
(4)

Since exact computation is intractable, MI is approximated using the InfoNCE loss (Oord et al., 2018), encouraging token-level dependencies across the same layers:

$$\mathcal{L}_{\mathrm{MI}} = -\frac{1}{N} \sum_{k=l}^{\mathcal{K}} \sum_{i=1}^{Q} \left(\log \sum_{\substack{h_j \in \mathcal{H}^k \\ j \neq i}} \exp\left(\frac{f(h_i^k, h_j^k)}{\tau}\right) - \log\left(\sum_{\substack{h_j \in \mathcal{H}^k \\ j \neq i}} \exp\left(\frac{f(h_i^k, h_j^k)}{\tau}\right) + \sum_{\substack{h_m \in \mathcal{N}^k}} \exp\left(\frac{f(h_i^k, h_m)}{\tau}\right) \right) \right),$$
(5)

where $f(h_i^k, h_j^k)$ is a similarity function quantifying the relationship between hidden states at layer k, \mathcal{H}^k denotes the set of positive examples related to h_i^k, \mathcal{N}^k is the set of negative examples unrelated to h_i^k at layer k, τ is the temperature parameter, and N is the total number of target layers from lto \mathcal{K} , with Q representing the number of tokens or samples used per layer. Further details on MI approximation are provided in Appendix D.

Layer-Wise Stability Regularisation. This component enforces smooth transitions across layers, reducing abrupt changes that could disrupt compositional structures. For a layer *k*, the Layer-Wise Stability Loss is defined as:

$$\mathcal{L}_{\text{Stability}} = \sum_{k=l}^{\mathcal{K}} \mathbb{E} \left[\frac{\left| f^{(k+1)}(X) - f^{(k)}(X) \right|^2}{\mathbb{E} \left[|f^{(k)}(X)|^2 \right] + \mathbb{E} \left[|f^{(k+1)}(X)|^2 \right] + \epsilon} \right]$$
(6)

where $f^{(k)}(X)$ denotes the output of layer k (i.e., after the attention and MLP submodules), and ϵ

is a small positive constant to ensure numerical stability (e.g., $\epsilon = 10^{-8}$). Minimising this loss preserves compositional integrity across the specified layers by encouraging smooth and consistent transitions between them, thereby enabling more stable information flow and aggregation within this range.

CARMA Loss. CARMA integrates \mathcal{L}_{MI} and $\mathcal{L}_{Stability}$ into its total loss as:

$$\mathcal{L}_{\text{CARMA}} = \gamma \mathcal{L}_{\text{MI}} + \eta \mathcal{L}_{\text{Stability}}, \qquad (7)$$

where γ and η are hyperparameters in [0, 1] that control the relative contribution of each component. The final optimisation objective balances task-specific performance with CARMA's regularisation as:

$$\mathcal{L}_{\text{total}} = (1 - \lambda) \cdot \mathcal{L}_{\text{task}} + \lambda \cdot \mathcal{L}_{\text{CARMA}}, \quad (8)$$

where \mathcal{L}_{task} represents the task-specific loss, \mathcal{L}_{CARMA} is the regularisation loss, and $\lambda \in [0, 1]$ controls the trade-off between task accuracy and compositional robustness.

Layer Selection for Regularisation. We apply CARMA to layers around one-third of the model depth, based on evidence that early-to-mid layers better capture compositional and syntactic structure, while deeper layers tend to specialise in task-specific representations (He et al., 2024; Langedijk et al., 2024). In our preliminary experiments, we observed that performance gains diminish when regularisation is applied to deeper layers. As a default, we recommend layers 3–4 in 12-layer models and 6–10 in 24-layer models.

Evaluation Metrics. We use exact match accuracy as the primary metric for both IDM and SC. This choice is motivated by the fact that both tasks have closed and categorical output spaces: IDM outputs are limited to a predefined set of single-word lexical entries from WordNet, while SC uses a fixed sentiment label set. In such settings, exact match is a standard and appropriate evaluation criterion.

4 Experimental Setup

4.1 Downstream Tasks & datasets

Two tasks that assess different aspects of composi-
tional generalisation are used in the paper: Inverse315Dictionary Modelling (IDM) for word-level com-
position and Sentiment Classification (SC) for317

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phrase-level structure. These tasks measure systematicity, substitutivity, over-generalisation, and
robustness to perturbations.

IDM evaluates a model's ability to generate terms 322 from definitions, focusing on substitutivity in se-323 mantic composition. Using WordNet (Miller, 1994) 324 with an 80-10-10 train-validation-test split, models 325 are prompted with a definition to generate the corresponding term (e.g., The shore of a sea is called" \rightarrow coast"). By mapping definitions to terms, this 328 task provides a robust assessment of a model's abil-329 ity to perform compositional substitution. 330

SC assesses the model's ability to infer sentiment 331 from phrases and sentences, particularly focusing on sentiment shifts and over-generalisation. Using 333 the Stanford Sentiment Treebank (SST) (Socher et al., 2013) with its original splits, models predict sentiment labels from textual inputs (e.g., A brilliant performance sentiment is" \rightarrow positive"). This 337 task examines how sentiment composition is preserved across different levels of linguistic structure. For both tasks, performance is assessed using Exact Match Accuracy, providing a robust assessment 341 of compositional substitution ability. Task formalisation, dataset details, and task selection rationale 343 are in Appendices A, B.1, and B.2, respectively.

4.2 Models and Experimental setup

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We evaluate three setups: original models, taskspecific fine-tuning, and fine-tuning with CARMA regularisation. We test GPT-2 (S/L) (Radford et al., 2019), Gemma1–2B (Team et al., 2024), LLaMA3.2 (1B/3B) (Dubey et al., 2024), and Qwen2.5 (0.5B/3B) (Yang et al., 2024a). We focus on decoder-only architectures, as they represent the dominant paradigm in many open-weight and production-ready LLMs. CARMA is generally applied at approximately one-third of the model's depth, though specific layer positions vary. Details on software, FT methodologies, model specifications, and CARMA hyperparameter selection are provided in Appendices B.3 and B.5.

4.3 Interventions for Compositional Robustness and Performance Stability

Two interventions are used to evaluate the robustness of compositional structures and the stability of learned representations: Constituent-aware pooling (CAP) and synonym replacement. These interventions assess hierarchical dependencies and semantic consistency under controlled perturbations. **CAP** (Aljaafari et al., 2024) groups token-level representations into higher-level semantic units (e.g., words, constituents) to assess hierarchical dependencies and how compositional structures are maintained across layers. In this paper, the token-toword CAP is utilised. Model robustness is measured by monitoring performance metrics before and after applying CAP. Full methodology and formalisation are provided in Appendix C.1.

Synonym Replacement evaluates semantic consistency by substituting 25% and 40% of prompt words with synonyms within an interpretable bound (α). Experiments were repeated at least five times with different seeds for robustness and performance stability assessment; further details are in Appendix C.2.

5 Results and discussion

The method is evaluated across three aspects its impact on: (1) model robustness against compositional-based perturbations, (2) model performance stability, and (3) model overall performance. See Appendix B.4 for a detailed breakdown of the evaluation metrics used for each aspect.

5.1 Constituent-Aware Pooling (CAP) Intervention

Fig. 2(a) and 2(b) show the impact of CAP on both tasks, comparing original, fine-tuned (FT), and CARMA models.² Each plot shows performance across normalised layer positions, where Accuracy is averaged over three CAP protocols (Mean, Max, Sum); protocol-specific results and extended comparisons are included in Appendix E. The analysis examines how well models preserve compositionality under hierarchical pooling.

CARMA's effectiveness is influenced by model size, tokenisation strategy, and task complexity. In IDM tasks, CARMA models have considerable gains when applying CAP at the earliest layers (1% of model depth), particularly in models with fine-grained tokenisation: Llama-1B (+3.61%) and Gemma-2B (+16.89%). GPT2-L, despite its reliance on subword tokenisation, benefits from CARMA over FT (+3.67%). However, Llama-3B and Qwen-3B minimal improvements (+1.0%) suggest a capacity ceiling where increased model size does not yield proportional gains due to training data limitations. The combination of smaller scale and multilingual training particularly affects Qwen-

²Throughout this paper, models incorporating CARMA with FT are referred to as CARMA models.



Figure 2: Layer-wise performance comparison under CAP intervention, with performance averaged over three protocols (Mean CAP, Max CAP, Sum CAP) for Original, Fine-Tuned (FT), and CARMA (FT + CARMA) models. Layer numbers are normalised to their relative positions within each model to enable cross-architecture comparison. The IDM task (left) highlights CARMA's improvements in systematicity and stability, particularly in the early and middle layers. The SC task (right) demonstrates CARMA's ability to enhance robustness, though convergence with FT occurs in deeper layers.

0.5B, where limited model capacity coupled with broad language coverage appears to constrain English-specific compositional learning, resulting in reduced CARMA benefits. In SC tasks, tokenisation effects vary with task complexity. When intervening at 25% layer position, Gemma-2B and Llama-1B show the strongest gains (+27.38%), +10.59%), while Llama-3B exhibits a marginal difference between CARMA and FT ($\sim 1\%$) but still outperforms the Original model (+37.68%). These results suggest that fine-tuning alone is sufficient for simpler tasks, whereas structured interventions like CARMA are particularly beneficial for more complex, compositional reasoning tasks.

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In a layer-wise analysis, the impact of CARMA 430 varies significantly across network depths, revealing crucial insights about compositional learning in transformers. Early layers (0-25%) benefit the most from regularisation, as they establish foundational compositional representations by exhibiting a weak 435 notion of compositionality. Middle layers (25-75%) 436 reinforce these patterns, maintaining structured feature dependencies with moderate improvements. 438 Deeper layers (75-100%) show minimal benefits as 439 the model transitions from compositional learning 440 to task-specialised representations. This pattern aligns with previous findings on layer-wise compositional evolution in Transformers, where earlier 443 layers capture hierarchical structure, while deeper layers exhibit increased task specificity (Feucht et al., 2024). CARMA can thus be strategically ap-446 plied to control these early representations, maintaining beneficial compositional structure while 448

allowing natural task-specific adaptations in deeper layers.

These findings demonstrate CARMA's effectiveness, particularly for models with granular tokenisation under data constraints, mediated by model capacity and task demands. The method's dual role - enhancing early compositional learning while preserving deeper layer adaptations - enables targeted improvement in model robustness without disrupting task-specific processing.

Model	Ver.	Task	Int.	CS	CV
	CARMA	IDM	25%	56.31	0.0164
	FT	IDM	25%	56.95	0.0311
GPT2-L	Org	IDM	25%	51.10	0.1175
	CARMA	SC	25%	0.8858	0.0065
	FT	SC	25%	0.8804	0.0082
	CARMA	IDM	25%	56.70	0.023
	FT	IDM	25%	57.42	0.030
Gemma-2B	Org	IDM	25%	49.47	0.031
Gemma-2B	CARMA	SC	25%	78.90	0.008
	FT	SC	25%	80.23	0.009
	Org	SC	25%	68.14	0.042
	CARMA	IDM	25%	62.86	0.015
Llama-3B	FT	IDM	25%	62.22	0.029
	Org	IDM	25%	52.47	0.035
	CARMA	SC	25%	84.83	0.0056
	FT	SC	25%	85.85	0.0065
	Org	SC	25%	35.21	0.0136

Table 1: Model performance (25% synonym intervention). Ver.: Version; Int.: Intervention rate; CS: ConsistSyn (%); CV: Coefficient of Variation. Best values in bold.

5.2 **Synonyms Replacement Intervention**

Synonym Replacement evaluates semantic consistency and robustness under lexical variations across multiple runs ($N \ge 5$) with different seeds. ConsistSyn measures output preservation after substitution, while the coefficient of variation (CV) quantifies performance stability, with lower values indi459

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cating higher stability. Performance is assessed at 25% and 40% word replacement rates to measure sensitivity to perturbations. Sample results are in Table 1; full details appear in Appendix E.

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Across models, CARMA achieves a distinctive 470 performance profile, matching or exceeding FT 471 ConsistSyn while consistently demonstrating supe-472 rior stability through lower CV values. At 25% in-473 tervention, Gemma-2B CARMA achieves 56.70% 474 ConsistSyn with a CV of 0.0225, compared to 475 FT's 57.42% with higher variance (CV: 0.0307). 476 Llama-3B CARMA outperforms FT in both Con-477 sistSyn (62.86% vs. 62.22%) and stability (CV: 478 0.0148 vs. 0.0292) for IDM. Qwen-3B follows a 479 similar trend but with smaller relative gains, im-480 proving stability (CV: 0.0225 vs. 0.0279) while 481 maintaining a marginal ConsistSyn advantage over 482 FT (62.00% vs. 61.79%). However, as interven-483 tion complexity increases to 40%, the performance 484 gap widens; for example, Gemma-2B FT main-485 tains higher ConsistSyn (44.98%) than CARMA 486 (42.36%), though CARMA remains more stable 487 (CV: 0.0174 vs. 0.0249). This behaviour implies 488 that the advantage of CARMA lies in its lower 489 490 variance and reinforcement of compositional consistency. Thus, it maintains compositional under-491 standing without sacrificing performance, whereas 492 FT produces a performance-driven approach. 493

> While the absolute differences in *ConsistSyn* between CARMA and FT are sometimes modest, particularly at lower replacement rates (e.g., 25%), the stability benefits of CARMA become more evident under increased perturbation (e.g., 40%), where FT models often show degraded consistency. *In these higher-variance regimes, CARMA consistently reduces output variability across model families, reinforcing its utility as a robustness-oriented intervention, even when raw accuracy remains comparable.*

The tokenisation method significantly affects CARMA's impact. Models with more structured tokenisation show stronger stability improvements, but gains vary based on vocabulary design and language coverage. Llama and GPT2-L generally benefit more than Qwen, even with similar sizes, likely due to their smaller multilingual coverage, which results in a more compact and consistent token distribution. Qwen, with a larger vocabulary (151K tokens) supporting broader multilingual processing, introduces redundancy that dampens CARMA's relative stability advantage. Gemma-2B, optimised for a single dominant language with a large vocabulary size, shows the highest overall gains, reinforcing that a structured tokenisation approach focused on a limited linguistic scope enhances CARMA's effectiveness.

Task complexity further differentiates CARMA's effect. CARMA's advantages align with its methodological design, particularly in tasks requiring explicit structural reinforcement. In IDM, where systematicity and substitutivity are critical, CARMA ensures structured mappings hold under perturbation, particularly in Gemma-2B (+14.6% over the original) and Llama-1B (+2692.5% over the original in SC). However, in SC, where compositionality is more distributed, larger models show lower differences between CARMA and FT, reinforcing that larger models encode sentiment shifts effectively without additional intervention.

These results strengthen the hypothesis that CARMA enhances model robustness across perturbations, particularly in structured learning tasks and models where fine-tuning alone does not fully capture compositional dependencies. While FT maintains an advantage in absolute accuracy, CARMA ensures greater consistency, making it critical for improving compositional alignment and mitigating instability in high-variance settings.



Figure 3: Task performance in IDM across GPT2 (S, L), Gemma-2B, Llama (1B, 3B), and Qwen (0.5B, 3B).



Figure 4: Task performance in SC across GPT2 (S, L), Gemma-2B, Llama (1B, 3B) and Qwen (0.5B, 3B).

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5.3 Impact of CARMA on Performance

Fig. 3 and 4 show the performance of original, FT, and CARMA accuracies across tasks. <u>CARMA</u> demonstrates significant improvements over original models across tasks. For example, in IDM, GPT2-L achieves 150% improvement, and Llama-3B shows an 89.6% increase, while in SC, Gemma-2B demonstrates 122.5% improvement over Original baselines.

Task-specific patterns emerge when comparing models. For example, in IDM, CARMA outperforms FT, with Llama-3B showing a +5% gain and GPT2-L improving by 1.7%. In SC, CARMA maintains comparable performance to FT while enhancing robustness, suggesting it preserves learned features while strengthening compositional consistency.

CARMA enhances FT by improving representation stability and preventing feature drift, ensuring structured compositional consistency. Its benefits are most pronounced in larger models, where greater capacity supports robust representations while maintaining fine-tuned performance. This scalability highlights CARMA's effectiveness in regularising model representations and reinforcing compositional structure without disrupting learned task features, providing a reliable solution for improving compositional reasoning in LLMs.

6 Related work

Research on CG in LLMs has revealed both capabilities and limitations (Tull et al., 2024; Moisio et al., 2023; Sinha et al., 2024), though many studies lack mechanistic analysis or concrete suggestions for improvements.

Architectural modifications are a common approach to tackle CG challenges. Recent proposals include pushdown layers for recursive attention (Murty et al., 2023), Layer-wise Representation Fusion for dynamic encoder weighting (Lin et al., 2023), and specialised semantic parsing methods (Shaw et al., 2021). While effective for specific tasks, these solutions face scalability challenges due to computational overhead, specialised annotation requirements, and architectural constraints.

Regularisation methods provide alternative approaches through consistency regularisation (Yin et al., 2023b), data augmentation strategies (Ontanon et al., 2022), and attention stability mechanisms (Zhai et al., 2023). Studies show dataset complexity and example frequency variations improve

compositional reasoning (Zhou et al., 2023). However, these methods face key limitations: tokenlevel approaches lack adaptability to complex structures, augmentation shows diminishing returns on real data, and stability mechanisms prioritise training stability over compositional generalisation. 593

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Evaluation challenges persist in CG research. Standard benchmarks like SCAN (Lake and Baroni, 2017), PCFG (Hupkes et al., 2020), and COGS (Kim and Linzen, 2020b) rely heavily on synthetic data, limiting real-world applicability. Recent frameworks like CoGnition (Li et al., 2021) and CAP (Aljaafari et al., 2024) better align with natural language phenomena, but evaluation gaps remain. Current approaches often sacrifice generalisability for task-specific performance. *CARMA* addresses these limitations through a *task-agnostic*, *efficient solution* that enhances CG while maintaining robust cross-task performance.

7 Conclusion

This paper presents CARMA, a method for enhancing compositional generalisation in LLMs through mutual information regularisation and layer-wise stability constraints. By addressing information fragmentation and instability across layers, CARMA improves performance robustness and stability under intervention. The method requires no architectural changes and integrates cleanly into standard fine-tuning pipelines. Future work should explore extending CARMA to tasks requiring more nuanced semantic reasoning and to multilingual contexts. Another important direction is combining CARMA with techniques that explicitly challenge generalisation, such as adversarial perturbations or structured distribution shifts, to promote the acquisition of novel compositional behaviours. Incorporating CARMA into improved, task-targeted architectures may further enhance its effectiveness. Additionally, controlled trainingfrom-scratch studies could isolate CARMA's impact more precisely and reveal deeper insights into how it shapes compositional representations across training regimes.

Limitations

The limitations of this paper can be summed up as follows: First, our results are primarily reported for the English language. Further analysis across languages with diverse linguistic structures is left as a confirmatory future work. Second, the datasets

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(WordNet and SST) lack a more comprehensive
representativeness of broader linguistic phenomena.
Third, our focus is predominantly on decoder-based
Transformers, and the employed Transformer models may inherit potential biases ingrained from their
pre-training data. Finally, while CARMA maintains inference efficiency, it introduces trainingtime overhead due to auxiliary losses, which should
be considered when integrating the method into
resource-constrained environments.

52 Ethical statement

This work aims to enhance language model robustness and compositional understanding through CARMA. While improving model reliability is beneficial, we acknowledge potential risks in enhancing language model capabilities. Our evaluation focuses on controlled tasks (IDM and SC) with comprehensive stability metrics to ensure responsible development and transparent reporting of model behaviour under perturbations.

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Task Selection and Compositionality Α Considerations

To assess compositional generalisation and the benefits of CARMA, we targeted tasks that involve systematic meaning construction and sensitivity to structural modifications. To that end, we opted to employ Inverse Dictionary Modelling (IDM) and Sentiment Classification (SC) as proxies for different dimensions of compositionality, capturing both structured composition and hierarchical generalisation.

IDM requires models to generate a single-word representation from a natural language definition, mapping from the composition of input constituents (individual concept components) to a specific term. On the other hand, SC maps meaning to a sentiment label, aggregating local meaning elements into a global interpretation. While IDM focuses on explicit compositional mapping, SC evaluates distributed composition, where sentiment is shaped by multiple interacting components.

Both tasks assess several aspects of compositionality (Figure 5), namely systematicity (structured meaning formation), substitutivity (semantic preservation under transformation), and resistance to over-generalisation (ensuring bounded semantic deviation). Further, they evaluate robustness, testing whether models can maintain correctness and consistency under internal and input-lexical perturbations. IDM and SC provide a comprehensive test of compositional generalisation across structured and distributed representations.

B **Detailed Experimental Configuration**

B.1 Task Formalisation

This paper evaluates the effectiveness of CARMA in enhancing the compositional generalisation of large language models (LLMs) through two tasks.



Figure 5: Illustration of compositional generalisation in Inverse Dictionary Modelling (IDM) and Sentiment Classification (SC). The figure highlights key compositional properties: systematicity ensures coherent meaning construction, substitutivity maintains meaning under lexical variations, robustness preserves intended outputs under perturbations, and over-generalisation leads to overly broad or semantically weak predictions (e.g., neuron misclassified as cell or positive reduced to neutral).

These tasks were selected based on their focus on input token structure and compositional semantics, utilising next-token prediction with single-token outputs. Formal definitions for each task are presented below.

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Inverse Definition Modelling (IDM). This task requires the model to predict a definiendum D, given its corresponding definition definition in natural language. Formally, the definition is represented as a sequence of tokens, definition = $\{tok_1, tok_2, \ldots, tok_n\}$, and the model seeks to produce D such that:

$$D = \arg\max_{t \in \mathcal{V}} P(d \mid \text{definition}), \qquad (9)$$

where \mathcal{V} denotes the model's vocabulary, and d represents a potential definiendum. Predictions are deemed correct only if they exactly match the target output.

Sentiment classification (SC). This task in-1043 volves assigning a sentiment label to a given sen-1044 tence containing sentiment cues and potential mod-1045 ifiers. The model processes the input sentence, represented as a sequence of tokens sentence = 1047



Figure 6: IDM Performance Across Models Under CAP

1048 $\{tok_1, tok_2, \dots, tok_n\}$, and produces an output1049label from a predefined set of sentiment classes1050 \mathcal{A} (i.e., *positive*, *negative*, *neutral*). Formally, the1051task is defined as:

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$$label = \arg \max_{\ell \in \mathcal{L}} P(\ell \mid sentence), \quad (10)$$

where $P(\ell \mid \text{sentence})$ is the probability of the sentiment label ℓ given the sentence. The model's performance is evaluated based on its ability to correctly predict the sentiment, accounting for compositional nuances such as modifiers and contrasts.

B.2 Datasets specification and pre-processing

For IDM, the training and test datasets were derived 1059 from WordNet (Fellbaum, 1998), a widely used lexical database of the English language. WordNet 1061 comprises over 117,000 synsets, each representing 1062 a distinct concept and annotated with semantic re-1063 lationships such as hypernyms, synonyms, and def-1064 1065 initions. To ensure consistency and improve data quality, standard preprocessing techniques were applied, including the removal of special charac-1067 ters, punctuation, extra spaces, and parenthesised content where necessary. The dataset focuses on 1069

general-purpose vocabulary rather than specialised1070domains or demographic groups. The dataset was1071initially split into an 80-20 ratio, with 80% allo-1072cated for training. The remaining 20% was further1073divided equally into validation and test sets.1074

The SC dataset was derived from the Stanford 1075 Sentiment Treebank (SST) (Socher et al., 2013), 1076 a corpus of English movie reviews annotated for analysis of the compositional effects of sentiment 1078 inference and was released under Apache License, Version 2.0. SST includes fine-grained sentiment 1080 labels at both the phrase and sentence levels, mak-1081 ing it a standard benchmark for evaluating sentiment classification models. The original dataset 1083 splits provided by the authors were maintained to 1084 ensure consistency in training, validation, and test-1085 ing. For SST labels, sentiment scores were cate-1086 gorised as follows: values equal to or greater than 1087 0.6 were classified as positive, scores between 0 1088 and 0.6 were considered neutral, and scores be-1089 low zero were assigned as negative. The final test dataset sizes for each task are presented in Table 2. 1091

Dataset	Train size	validation Size	Test Size
WordNet	9563	1154	1231
SST	8544	1101	2210

Table 2: Train, validation, and test set sizes for WordNet and SST datasets used in this paper.

B.3 Model training and fine-tuning settings

Table 3 summarises the key characteristics of the models evaluated in this study. All models were ob-1094 1095 tained from Hugging Face (Wolf et al., 2019) under their respective licenses: GPT-2 (Modified MIT), 1096 Llama 3.2 (Meta Llama 3 Community), Qwen 2.5 1097 (Apache 2.0), and Gemma-2B (Gemma Terms of Use). While all models were pre-trained on En-1099 glish data, LLama and Qwen models provide ad-1100 ditional multilingual capabilities, namely English, 1101 German, French, Italian, Portuguese, Hindi, Span-1102 ish, and Thai for LLama, and over 10 languages, 1103 including Chinese, English, French, Spanish, Por-1104 tuguese, Russian, Arabic, Japanese, Korean, Viet-1105 namese, Thai, and Indonesian for Qwen. The mod-1106 els employ the following tokenisation approaches: 1107 GPT-2, Byte Pair Encoding (BPE) with a 50,257-1108 token vocabulary, optimised primarily for English, 1109 Llama 3.2 uses SentencePiece-based BPE, combin-1110 ing 100K tokens from Tiktoken3 with 28K addi-1111 tional tokens to enhance multilingual performance, 1112 Qwen 2.5 employs Byte-level BPE, utilising a 1113 151,643-token vocabulary designed for multilin-1114 gual processing, Gemma-2B has a SentencePiece 1115 tokeniser leveraging a 256,000-token vocabulary, 1116 making it highly effective for English-based tasks. 1117 Each model was fine-tuned on its respective down-1118 stream task following a systematic hyperparameter 1119 search to identify optimal configurations. Prior 1120 to fine-tuning, prompt engineering was conducted 1121 to determine well-performing prompts tailored to 1122 each task, ensuring alignment with task-specific 1123 requirements and enhancing the models' ability to 1124 generate accurate and contextually relevant outputs. 1125 The hyperparameter search explored key factors, 1126 including weights for stability regularisation, mu-1127 tual information (MI) regularisation, and the over-1128 1129 all CARMA weight (Equation 7), as well as the specific layers to which these losses were applied. 1130

1131For training parameters, the following batch1132sizes were set in the IDM task: 16 for the Gemma-11332B and GPT models, 32 for the Qwen-3B and1134Llama models, and 64 for the Qwen-0.5B model.1135For SC, the batch sizes were 16 for the GPT mod-1136els, Gemma-2B and Llama-3B; 32 for Llama-1B

and Qwen-3B; and 64 for Qwen-0.5B. For the num-1137 ber of training epochs, in the IDM, the Gemma and 1138 GPT models were trained for two epochs, while 1139 all other models were trained for three epochs, 1140 whereas all models were trained for two epochs, 1141 except Gemma-2B and LLama-1B, which were 1142 trained for three epochs for the SC task. The stop-1143 ping layers for IDM and CARMA were configured 1144 as follows: GPT2-S at layer 3, GPT2-L at layer 1145 8, Gemma-2B at layer 10, Llama-1B at layer 7, 1146 Llama-3B at layers 8 (stability) and 12 (MI), Qwen-1147 0.5B at layer 5, and Qwen-3B at layer 10. The SC, 1148 the ending layers, 4 for GPT2-S, 12 for GPT2-L, 10 1149 for Gemma-2B, 7, for LLama 1B, 8, for LLama 3B, 1150 5 for Qwen-0.5B and 7 for Qwen-3B. For CARMA 1151 weight, optimal values varied by model size: 0.4 1152 and 0.5 were most effective for larger models. We 1153 hypothesise that CARMA regularisation exhibits 1154 a weaker effect when lower weights are applied, 1155 particularly in larger architectures where stronger 1156 constraints are needed to stabilise compositional 1157 representations. In IDM, GPT2-L and Gemma per-1158 formed best with a weight of 0.3, GPT2-S with 1159 0.2, Llama-1B with 0.4, and Llama-3B with 0.5. 1160 Qwen models used 0.5 and 0.4 for the 0.5B and 1161 3B variants, respectively. For SC Carma weight, 1162 it was 0.4 for Qwen-0.5B and GPT models, 0.5 1163 for LLama-3B and Qwen-3B, and 0.3 for the rest. 1164 For the ending layer, it was 4 for GPT2-S, 12 for 1165 GPT2-L, 10 for Gemma-2B, 7 for LLama-1B, 8 for 1166 LLama-3B, 5 for Qwen-0.5B and 7 for Qwen-3B. 1167

Model	Parameters	Layers	D _{model}	Heads	Activation	MLP Dimension
GPT-2 Small	85M	12	768	12	GELU	3072
GPT-2 Large	708M	36	1280	20	GELU	5120
Gemma-2B	2B	32	4096	16	GELU	8192
LLaMA3.2 1B	1.1B	16	2048	32	SiLU	8192
LLaMA3.2 3B	3.2B	28	3072	24	SiLU	8192
Qwen2.5-0.5B	391M	24	896	14	SiLU	4864
Qwen2.5-3B	3.0B	36	2048	16	SiLU	11008

Table 3: Summary of model architectures. **Parameters**: total number of trainable parameters; **Layers**: total number of transformer layers; D_{model} : size of word embeddings and hidden states; **Heads**: number of self-attention heads; **Activation**: activation function used in feedforward layers; **MLP Dimension**: dimensionality of the feedforward network.

B.4 Evaluation Metrics

This section details the evaluation metrics used in the study, including accuracy, synonym consistency, and performance stability.

Accuracy is used as a primary measure of model performance and is defined as:

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$$\operatorname{Accuracy} = \frac{TP + TN}{TP + TN + FP + FN}, \quad (11)$$

1175where TP (true positives) and TN (true negatives)1176denote correctly classified instances, while FP1177(false positives) and FN (false negatives) repre-1178sent misclassified instances.

1179Synonym Consistency (ConsistSyn) quantifies1180a model's ability to maintain correct predictions1181after synonym replacement. It is computed as:

$$ConsistSyn = \frac{|Correct After Replacement|}{|Correct Before Replacement|} \times 100,$$
(12)

where Correct After Replacement refers to the number of correct predictions following synonym substitution, and Correct Before Replacement denotes the number of correct predictions before substitution. The reported results are the averaged ConsistSyn across ($N \ge 5$) runs.

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Coefficient of Variation (CV) measures the stability of model performance across multiple runs, with lower values indicating greater consistency. It is defined as:

$$CV = \frac{\sigma}{\mu},$$
 (13)

1194where σ represents the standard deviation of model1195performance across runs, and μ denotes the mean1196performance.

1197Normalised Improvement (NI)evaluates the1198relative gain in consistency introduced by a model1199over a baseline model. It is calculated as:

$$NI = \frac{ConsistSyn_{CARMA} - ConsistSyn_{baseline}}{ConsistSyn_{baseline}} \times 100.$$
(14)

This metric captures the percentage improvement in synonym consistency due to a model variant compared to the baseline model.

B.5 Experimental setup

1205Experiments were conducted using NVIDIA RTX1206A6000 and A100 GPUs. The method was de-1207veloped in Python (v3.10.15) with Transformers1208(v4.44.2) (Wolf et al., 2020), PyTorch (v2.4.1)1209(Paszke et al., 2019), and Transformer-lens (v2.8.1)1210(Nanda and Bloom, 2022). Preprocessing tasks,1211including tokenisation and tagging, used NLTK

 (v3.9.1) (Bird et al., 2009), spaCy (v3.7.2) (Hon 1212

 nibal et al., 2020), and TextBlob (v0.18.0) (Loria
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 et al.), with Scikit-learn (v1.5.1) (Pedregosa et al.,
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 2011) for evaluation. Models use 500 warm-up
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 steps and a 0.006 learning rate.
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C Comprehensive Explanation of Evaluation Interventions

C.1 Constituent-Aware Pooling (CAP) Formalisation

Constituent-Aware Pooling (CAP) Formalisation is a method proposed in (Aljaafari et al., 2024) to systematically assess compositional generalisation via aggregating token-level activations into higherlevel semantic representation. Below is a detailed explanation and formalisation of CAP.

Overview. CAP aggregates model activations at any chosen constituency level (e.g. tokens to words), enabling the analysis of compositional dependencies. The key steps involved are:

- Input Representations: For a given input sequence $X = [x_1, x_2, ..., x_n]$, the model produces inner states $H = [h_1, h_2, ..., h_n]$ at a specific layer.
- Grouping Constituents: Using syntactic parsers such as Benepar (Kitaev et al., 2019; Kitaev and Klein, 2018), or by inversing the model tokeniser function, the sequence is segmented into constituents $C = [c_1, c_2, \ldots, c_m]$, where each c_i represents a phrase or syntactic unit. For the experiments presented in the paper, tokens were grouped into words to form the smallest linguistic units.
- **Pooling Operations:** For each constituent c_i , the corresponding activations $\{h_j | x_j \in c_i\}$ are aggregated into a single representation r_i using a pooling function:

$$r_i = \alpha(\{h_j | x_j \in c_i\})$$
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CAP supports three pooling functions:

Maximum pooling: Selects the highest activation values as:

$$\alpha(\{h_j | x_j \in c_i\}) = \max(\{h_j | x_j \in c_i\}),$$
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Mean pooling: Computes the average of activation values as:

$$\alpha(\{h_j | x_j \in c_i\}) = \frac{1}{|c_i|} \sum_{j \in c_i} \{h_j | x_j \in c_i\},$$
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- Sum pooling: Accumulates activation values as:

$$\alpha(\{h_j | x_j \in c_i\}) = \sum_{j \in c_i} \{h_j | x_j \in c_i\}.$$

• Updating Representations: The pooled representations $R = [r_1, r_2, \ldots, r_m]$ replace the original activations H for further processing.

Evaluation. The impact of CAP is evaluated by comparing task-specific performance metrics (e.g., accuracy, F1 score) of models before and after CAP is applied. This allows for a direct assessment of how CAP affects compositionality and task performance. This paper utilises the word-level CAP, pooling related token representation to their corresponding words.

C.2 Synonym Replacement

A multi-step approach was adopted to ensure re-1272 liable synonym replacements. First, preprocess-1273 1274 ing was applied to filter out words that were unlikely to produce meaningful replacements. Specif-1275 ically, words belonging to NLTK's predefined stop-1276 words list or shorter than two characters were ex-1277 cluded from consideration. The remaining words 1278 were tagged with their part-of-speech (POS) using spaCy's (Honnibal et al., 2020) POS tagger. 1280 Additionally, the sentiment of each word was determined using TextBlob (Loria et al.) to ensure 1282 that replacements preserved the semantic tone of 1283 1284 the original text. Next, a synonym vocabulary was constructed using words extracted from spaCy's 1285 en core web md language model. This vocabu-1286 lary was filtered to include only alphabetic common words with high probability scores (greater than -15 1288 in our case), as determined by spaCy's word frequency data, while stopwords and rare terms were 1290 excluded. This step ensured that the vocabulary 1291 consisted of meaningful and contextually appropri-1292 ate words for replacement. For each target word, 1293 a list of synonym candidates was generated by it-1294 erating over the constructed vocabulary. The top 1295 n candidates were selected based on their seman-1296 1297 tic similarity to the original word, measured using spaCy's word vectors. Synonyms with high simi-1298 larity scores and alignment in POS were prioritised 1299 to maintain grammatical and contextual coherence in the text. 1301

Model	Ver.	Task	Int.	CS	CV
	CARMA	IDM	25%	49.17	0.025
	FT	IDM	25%	50.89	0.017
GPT2-S	Org	IDM	25%	52.46	0.044
0112-3	CARMA	IDM	40%	35.90	0.0542
	FT	IDM	40%	37.16	0.0628
	Org	IDM	40%	37.20	0.1223
	CARMA	IDM	25%	56.31	0.0164
	FT	IDM	25%	56.95	0.0311
GPT2-L	Org	IDM	25%	51.10	0.1175
OI 12-L	CARMA	IDM	40%	43.56	0.0485
	FT	IDM	40%	43.97	0.0459
	Org	IDM	40%	34.68	0.0895
	CARMA	IDM	25%	56.70	0.023
	FT	IDM	25%	57.42	0.030
Gemma-2B	Org	IDM	25%	49.47	0.031
Gemma-2D	CARMA	IDM	40%	0.4236	0.0174
	FT	IDM	40%	0.4498	0.0249
	Org	IDM	40%	0.3576	0.0480
	CARMA	IDM	25%	58.40	0.0400
	FT	IDM	25%	57.86	0.0385
Llama-1B	Org	IDM	25%	47.55	0.0503
Liama-1D	CARMA	IDM	40%	47.07	0.0476
	FT	IDM	40%	46.75	0.0455
	Org	IDM	40%	33.49	0.0391
	CARMA	IDM	25%	56.98	0.0286
	FT	IDM	25%	54.57	0.0191
Owen-0.5B	Org	IDM	25%	46.84	0.0684
Qweii-0.5D	CARMA	IDM	40%	40.55	0.0397
	FT	IDM	40%	39.69	0.0491
	Org	IDM	40%	32.98	0.0938
	CARMA	IDM	25%	62.00	0.0225
	FT	IDM	25%	61.79	0.0279
Qwen-3B	Org	IDM	25%	49.37	0.0441
	CARMA	IDM	40%	45.05	0.0400
	FT	IDM	40%	45.74	0.0551
	Org	IDM	40%	31.95	0.0688
	CARMA	IDM	25%	62.86	0.015
	FT	IDM	25%	62.22	0.029
Llama-3B	Org	IDM	25%	52.47	0.035
Liama-3D	CARMA	IDM	40%	49.05	0.0297
	FT	IDM	40%	48.31	0.0191
	Org	IDM	40%	36.95	0.0458

Table 4: Model performance (25% and 40% synonym intervention) on the IDM task. Ver.: Version; Int.: Intervention rate; CS: ConsistSyn (%); CV: Coefficient of Variation. Best values in bold.

D **InfoNCE for Mutual Information** Estimation

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Mutual information (MI) quantifies the shared information between two variables X and Y. CARMA leverages MI maximisation to capture dependencies between tokens effectively, thereby enhancing compositional generalisation in LLMs. Specifically, CARMA uses MI, denoted as I(X;Y), to reinforce token-level interactions critical for compositionality. However, direct computation of MI is challenging in practice.

To address this challenge, a variant of InfoNCE is employed to estimate MI and approximate these



Figure 7: SC Performance Across Models Under CAP

1315dependencies efficiently. Given an anchor token1316hidden state h_i , we construct a corresponding pos-1317itive set H, which contains tokens hidden states1318semantically or syntactically related to h_i . Addi-1319tionally, we define \mathcal{N} as the set of negative examples consisting of unrelated tokens hidden states.

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The InfoNCE objective provides a practical lower bound on I(X;Y) (Oord et al., 2018), as follows:

$$I(X;Y) \ge \mathbb{E}\left[\log \frac{\sum_{h_j \in \mathbf{H}} f(h_i, h_j)}{\sum_{h_j \in \mathbf{H}} f(h_i, h_j) + \sum_{h_k \in \mathcal{N}} f(h_i, h_k)}\right]$$
(15)

where $f(h_i, h_j) = \exp(\sin(h_i, h_j)/\tau)$ is a scaled similarity function, and τ is a temperature parameter. This adaptation of InfoNCE introduces tokenspecific interactions within the layer-wise structure of LLMs, ensuring that dependencies are captured across layers. By maximising mutual information, CARMA aligns the optimisation direction to enhance compositional structures.

To extend this approach across layers, the final

CARMA MI loss is computed as:

$$\mathcal{L}_{\mathrm{MI}} = -\frac{1}{N} \sum_{i=1}^{N} \left(\log \sum_{\substack{h_j \in \mathbf{H} \\ j \neq i}} \exp\left(\frac{\mathrm{sim}(h_i, h_j)}{\tau}\right) - \log\left(\sum_{\substack{h_j \in \mathbf{H} \\ j \neq i}} \exp\left(\frac{\mathrm{sim}(h_i, h_j)}{\tau}\right) + \sum_{\substack{h_k \in \mathcal{N}}} \exp\left(\frac{\mathrm{sim}(h_i, h_k)}{\tau}\right) \right) \right),$$
(16)

where h_i is the anchor token, $h_j \in \mathbf{H}$ are positive examples related to h_i , $h_k \in \mathcal{N}$ are negative examples, N is the number of anchors, and $sim(h_i, h_j)$ is a similarity function. The negative sign ensures that MI is maximised during optimisation. Without this negative sign, the objective would incorrectly minimise MI, thereby hindering CG enhancement.

E Extended results

Figures 6, 7 and Tables 4 and 5 provide additional1344results for models' performance comparison under1345CAP and synonym interventions. Figure 8 shows1346an overall models performance under cap for all1347models. CARMA models show a clear advantage1348

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Figure 8: Layer-wise performance under CAP interventions on the IDM (left) and SC (right) tasks. Results are averaged over three pooling strategies (Mean, Max, Sum) and reported for Original, Fine-Tuned (FT), and CARMA (FT + CARMA) models. Layer indices are normalised to support comparison across model sizes. CARMA improves robustness and systematicity in early-to-mid layers for both tasks, with diminishing differences in deeper layers.

Model	Ver.	Task	Int.	CS	CV
	CARMA	SC	25%	89.03	0.8903
	FT	SC	25%	89.54	0.8954
GPT2-S	CARMA	SC	40%	84.95	0.0095
	FT	SC	40%	85.07	0.0098
	CARMA	SC	25%	88.58	0.0065
	FT	SC	25%	88.04	0.0082
GPT2-L	CARMA	SC	40%	84.61	0.0072
	FT	SC	40%	84.04	0.0073
	CARMA	SC	25%	84.81	0.0069
	FT	SC	25%	81.67	0.0088
Gemma-2B	Org	SC	25%	68.14	0.0076
Gemma-2D	CARMA	SC	40%	81.48	0.0102
	FT	SC	40%	74.29	0.0073
	Org	SC	40%	76.06	0.0136
	CARMA	SC	25%	74.03	0.0069
	FT	SC	25%	75.69	0.0044
Llama-1B	Org	SC	25%	2.65	0.1239
Liailla-1D	CARMA	SC	40%	71.43	0.0065
	FT	SC	40%	74.31	0.0102
	Org	SC	40%	1.73	0.2245
	CARMA	SC	25%	89.66	0.0037
	FT	SC	25%	89.83	0.0085
Owen-0.5B	Org	SC	25%	59.12	0.0691
Qweii-0.5D	CARMA	SC	40%	86.03	0.0084
	FT	SC	40%	86.31	0.0046
	Org	SC	40%	55.27	0.0429
	CARMA	SC	25%	93.65	0.0061
	FT	SC	25%	93.85	0.0039
Owen-3B	Org	SC	25%	67.63	0.0227
Qwen-3B	CARMA	SC	40%	91.26	0.0050
	FT	SC	40%	91.26	0.0050
	Org	SC	40%	64.05	0.0159
Llama-3B	CARMA	SC	25%	84.83	0.0056
	FT	SC	25%	85.85	0.0065
	Org	SC	25%	35.21	0.0136
	CARMA	SC	40%	82.89	0.0016
	FT	SC	40%	83.55	0.0067
	Org	SC	40%	32.88	0.0188

Table 5: Model performance (25% and 40% synonym intervention) on the SC task. **Ver.**: Version; **Int.**: Intervention rate; **CS**: ConsistSyn (%); **CV**: Coefficient of Variation. **Best values in bold.**

over all models and tasks. However, the gain is clearer in the IDM case, where more intricate features and compositionality generalisation are required. It is also observed that the performance of the FT and CARMA models demonstrates similar curves or trends. Given this observation, we argue that CARMA's improvements stem from its learning objectives, which align closely with crossentropy loss while explicitly addressing intermediate representation stability. The observed improvements are moderate in some cases, particularly for SC tasks. This behaviour is expected due to the limited size of the fine-tuning datasets compared to the original pretraining data used for these models. Nevertheless, larger models, such as Llama-3B and Gemma-2B, exhibit more substantial improvements with CARMA, demonstrating its scalability with model capacity.

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E.1 Training Runtime and Overhead

We report wall-clock training times (in minutes) for each model under standard fine-tuning (FT) and with CARMA. Overhead is computed as the relative increase in runtime caused by the additional mutual information and stability losses. All experiments for models were conducted on a single GPU under identical batch size, optimiser settings, and hardware configuration.

CARMA introduces non-trivial training-time1376overhead due to auxiliary objectives, particularly1377for smaller models or longer sequences. However,1378inference costs remain unchanged, and no architec-1379tural modifications are required. We observe mod-1380erate to high training slowdowns (e.g., $\times 2.2 - \times 2.9$ 1381for LLaMA-3B), with variance across models due1382

Model	FT (min)	CARMA (min)	Overhead ratio
GPT2 Small	1.9	3.48	$\times 1.8$
GPT2 Large	6.7	8.9	$\times 1.3$
Llama 3.2–1B	2.78	6.96	$\times 2.5$
Llama 3.2–3B	7.55	20.2	$\times 2.2$
Qwen 2.5-0.5B	2.10	4.75	$\times 2.3$
Qwen 2.5–3B	2.98	5.01	$\times 1.7$

Table 6: Wall-clock IDM training time and overhead introduced by CARMA. All runs use a single GPU under identical batch, optimiser, and hardware settings.

Model	FT (min)	CARMA (min)	Overhead ratio
GPT-2 Small	1.12	8.51	$\times 7.6$
GPT-2 Large	6.02	13.18	$\times 2.19$
LLaMA 3.2–1B	2.50	9.98	$\times 4.9$
LLaMA 3.2-3B	6.58	14.06	$\times 2.13$
Qwen 2.5–3B	6.01	16.86	$\times 2.8$

Table 7: Wall-clock SC training time and overhead introduced by CARMA. All runs use a single GPU under identical batch, optimiser, and hardware settings.

to token length and loss computation. Optimising 1383 runtime for mutual information and stability estimation is an important direction for future efficiency 1385 improvements. 1386