Towards Understanding Large-Scale Discourse Structures in Pre-Trained and Fine-Tuned Language Models

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Abstract

With a growing number of BERTology work analyzing different components of pre-trained language models, we extend this line of research through an in-depth analysis of discourse information in pre-trained and fine-tuned language models. We move beyond prior work along three dimensions: First, we describe a novel approach to infer discourse structures from arbitrarily long documents. Second, we propose a new type of analysis to explore where and how accurately intrinsic discourse is captured in the BERT and BART models. Finally, we assess how similar the generated structures are to a variety of baselines as well as their distribution within and between models.

1 Introduction

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Transformer-based machine learning models are an integral part of many recent improvements in Natural Language Processing (NLP). With their rise spearheaded by Vaswani et al. (2017), the pre-training/fine-tuning paradigm has gradually replaced previous approaches based on architecture engineering, with transformer models such as BERT (Devlin et al., 2018), BART (Lewis et al., 2020), RoBERTa (Liu et al., 2019) and others delivering state-of-the-art performances on a wide variety of tasks. Besides their strong empirical results on most real-world problems, such as summarization (Zhang et al., 2020; Xiao et al., 2021a), question-answering (Joshi et al., 2020; Oğuz et al., 2021) and sentiment analysis (Adhikari et al., 2019; Yang et al., 2019), uncovering what kind of linguistic knowledge is captured by this new type of pre-trained language models (PLMs) has become a prominent question by itself. As part of this line of research, called *BERTology* (Rogers et al., 2020), researchers explore the amount of linguistic understanding encapsulated in PLMs, exposed through either external probing tasks (Raganato and Tiedemann, 2018; Zhu et al., 2020; Koto et al., 2021a)

or unsupervised methods (Wu et al., 2020; Pandia et al., 2021) to analyze the syntactic structures (e.g., Hewitt and Manning (2019); Wu et al. (2020)), relations (Papanikolaou et al., 2019), ontologies (Michael et al., 2020) and, to a more limited extend, discourse related behaviour (Zhu et al., 2020; Koto et al., 2021a; Pandia et al., 2021). 041

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Generally speaking, while most previous *BERTology* work has focused on either sentence level phenomena or connections between adjacent sentences, large-scale semantic and pragmatic structures (oftentimes represented as discourse trees/graphs) have been less explored. These structures (e.g., discourse trees) play a fundamental role in expressing the intent of multi-sentential documents and, not surprisingly, have been shown to benefit many NLP tasks such as summarization (Gerani et al., 2019), sentiment analysis (Bhatia et al., 2015; Nejat et al., 2017; Hogenboom et al., 2015) and text classification (Ji and Smith, 2017).

With multiple different theories for discourse proposed in the past, the RST (Mann and Thompson, 1988) and PDTB (Prasad et al., 2008) frameworks have received most attention. RST-style discourse structures thereby consist of a single rooted tree covering whole documents, comprising of: (1) A tree structure, combining clause-like sentence fragments (Elementary Discourse Units, short: EDUs) into a discourse constituency tree, (2) Nuclearity, assigning every tree-branch primary (*Nucleus*) or peripheral (*Satellite*) importance in a local context and (3) Relations, defining the connection and direction between siblings in the tree.

Given the importance of large-scale discourse structures, we extend the line of *BERTology* research with novel experiments to test for the presence of intrinsic discourse information in established PLMs. More specifically, we aim to better understand to what extend RST-style discourse information is stored as latent trees in encoder self081attention matrices¹. While we focus on the RST082formalism in this work, our presented methods are083theory-agnostic and, hence, applicable to discourse084structures in a broader sense, including other tree-085based theories, such as PDTB. Our contributions086in this paper are:

(1) A novel approach to extract discourse information from arbitrarily long documents with limited-size transformer models. This is a non-trivial issue, which has been mostly by-passed in previous work through the use of proxy tasks.

(2) An exploration of discourse information locality
across pre-trained and fine-tuned language models,
finding that discourse is consistently captured in a
fixed subset of self-attention heads.

(3) An in-depth analysis of the discourse quality in
pre-trained language models and their fine-tuned
extensions. We compare constituency and dependency structures of 2 PLMs fine-tuned on 4 tasks
and 7 fine-tuning datasets to gold-standard discourse trees, finding that the captured discourse
structures outperform simple baselines by a wide
margin and even show superior performance compared to distantly supervised models.

(4) A similarity analysis between PLM inferred discourse trees and supervised, distantly supervised and simple baselines, which reveals that PLM constituency discourse trees do align relatively well with previously proposed supervised models, but also capture complementary information, making them a valuable resource for ensemble methods.

(5) A detailed look at information redundancy in self-attention heads to better understand the structural overlap between self-attention matrices and models. Our results indicate that similar discourse information is consistently captured in the same heads, even across fine-tuning tasks.

2 Related Work

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At the base of our work are two of the most popular and frequently used PLMs: BERT (Devlin et al., 2018) and BART (Lewis et al., 2020). We choose these two popular approaches in our study due to their complementary nature (encoder-only vs. encoder-decoder) and based on previous work by Zhu et al. (2020) and Koto et al. (2021a), showing the effectiveness of BERT and BART models for discourse related tasks.

Our work is further related to the field of dis-

course parsing. With a rich history of traditional machine learning models (e.g., Hernault et al. (2010); Ji and Eisenstein (2014); Joty et al. (2015); Wang et al. (2017), inter alia), recent approaches slowly shifted to successfully incorporate a variety of PLMs into the process of discourse prediction, such as ELMo embeddings (Kobayashi et al., 2019), XLNet (Nguyen et al., 2021), BERT (Koto et al., 2021b), RoBERTa (Guz et al., 2020) and SpanBERT (Guz and Carenini, 2020). Despite these works showing the usefulness of PLMs for discourse parsing, all of them cast the task into a "local" problem, using only partial information through the shift-reduce framework (Guz et al., 2020; Guz and Carenini, 2020), natural document breaks (e.g. paragraphs (Kobayashi et al., 2020)) or by framing the task as an inter-EDU sequence labelling problem on partial documents (Koto et al., 2021b). However, since we believe that the true benefit of discourse information only emerges when complete documents are considered, we propose a new approach to connect PLMs and discourse structures in a "global" manner, superseding the local proxy-tasks with a new methodology to explore arbitrarily long documents.

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Aiming to better understand what information is captured in PLMs, the line of BERTology research has recently emerged (Rogers et al., 2020), with early work mostly focusing on the syntactic capacity of PLMs (Hewitt and Manning, 2019; Jawahar et al., 2019; Kim et al., 2019), in parts also exploring the internal workings of transformerbased models (e.g., self-attention matrices (Raganato and Tiedemann, 2018; Mareček and Rosa, 2019)). More recent work started to explore the alignment of PLMs with discourse information, encoding semantic and pragmatic knowledge. Along those lines, Wu et al. (2020) present a parameterfree probing task for both, syntax and discourse. Compared to our work, their tree inference approach is however computationally expensive and only explores the outputs of the BERT model. Further, Zhu et al. (2020) use 24 hand-crafted rhetorical features to execute three different supervised probing tasks, showing promising performance of the BERT model. Similarly, Pandia et al. (2021) aim to infer pragmatics through the prediction of discourse connectives by analyzing the model inputs and outputs and Koto et al. (2021a) analyze discourse in PLMs through seven supervised probing tasks, finding that BART and BERT contain

¹We focus on discourse structure and nuclearity, leaving the relation classification for future work.



Figure 1: Small-scale example of the discourse extraction approach. Purple=EDUs, green=sub-word embeddings, red=input slices of size t_{max} , orange=PLM, blue=self-attention values, grey-scale=frequency count.

most information related to discourse. In contrast 180 181 to the approach taken by both Zhu et al. (2020) and Koto et al. (2021a), we use an unsupervised methodology to test the amount of discourse in-183 formation stored in PLMs (which can also conve-184 niently be used to infer discourse structures for new and unseen documents) and extend the work by Pandia et al. (2021) by taking a closer look at 187 the internal workings of the self-attention compo-188 nent. Looking at all these prior works analyzing the amount of discourse in PLMs, structures are solely explored through the use of proxy tasks, such as 191 connective prediction (Pandia et al., 2021), rela-192 tion classification (Kurfali and Östling, 2021) and 193 others (Koto et al., 2021a). However, despite the 194 difficulties of encoding arbitrarily long documents, 195 we believe that to systematically explore the rela-196 tionship between PLMs and discourse, considering 197 complete documents is imperative. Along these lines, recent work started to tackle the inherent 199 input-length limitation of general transformer mod-200 els through additional recurrence (Dai et al., 2019), 201 compression modules (Rae et al., 2019) or sparse patterns (e.g., Kitaev et al. (2020); Beltagy et al. (2020)). Still mostly based on established PLMs 204 (e.g., BERT) and with no dominant solution yet, 205 we believe that even with the input length restriction being actively tackled, an in-depth analysis 207

of traditional PLMs with discourse is highly valuable to establish a solid understanding of intrinsic linguistic properties.

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Besides the described BERTology work, we got encouraged to explore fine-tuned extensions of standard PLMs through previous work showing the benefit of discourse parsing for many downstream tasks, such as summarization (Gerani et al., 2019), sentiment analysis (Bhatia et al., 2015; Nejat et al., 2017; Hogenboom et al., 2015) and text classification (Ji and Smith, 2017). Conversely, recent work also shows promising results when inferring discourse structures from related downstream tasks, such as sentiment analysis (Huber and Carenini, 2020) and summarization (Xiao et al., 2021b). Given this bidirectional synergy, we move beyond traditional experiments focusing on standard PLMs and additionally explore discourse structures of fine-tuned PLMs.

3 Discourse Extraction Method

With PLMs rather well analyzed according to their syntactic capabilities, large-scale discourse structures have been less explored. One reason for this is the input length constraint of transformer models. While this is generally not prohibitive for intrasentence syntactic structures (e.g., presented in Wu et al. (2020)), it does heavily influence large-scale discourse structures, operating on complete (potentially long) documents. Overcoming this limitation is non-trivial, since traditional transformer-based models only allow for fixed, short inputs.

Aiming to systematically explore the ability of PLMs to capture discourse, we investigate a novel way to effectively extract discourse structures from the self-attention component of the BERT and BART models. We thereby extend the tree-generation approach proposed in Xiao et al. (2021b) to support the input length constraints of standard PLMs using a sliding-window approach in combination with matrix frequency normalization and an EDU aggregation method.

The Tree Generation Procedure by Xiao et al. (2021b) explores a two-stage approach to obtain discourse structures from a transformer model, by-passing the input-length constraint. Using the intuition that the self-attention score between any two EDUs is an indicator of their semantic/pragmatic relatedness and hence should influence their distance in a projective discourse tree, they use the CKY dynamic programming approach (Jurafsky

and Martin, 2014) to generate constituency trees 258 based on the internal self-attention of the trans-259 former model. To generate dependency trees, a sim-260 ilar intuition is applied when inferring discourse trees using the Eisner (Eisner, 1996) algorithm. 262 Since we explore the discourse information cap-263 tured in standard PLMs, we cannot directly transfer the two-stage approach in Xiao et al. $(2021b)^2$. Instead, we propose a new method to overcome the length-limitation of the transformer model.

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The Sliding-Window Approach is at the core of our new methodology to overcome the inputlength constraint. We first tokenize arbitrarily long documents with n EDUs $E = \{e_1, ..., e_n\}$ into the respective sequence of m sub-word tokens $T = \{t_1, ..., t_m\}$ with $n \ll m$, according to the PLM tokenization method (WordPiece for BERT, Byte-Pair-Encoding for BART). Using the sliding window approach, we subdivide the m sub-word tokens into sequences of maximum input length t_{max} , defined by the PLM. Using a stride of 1, we generate $(m - t_{max}) + 1$ sliding windows W, feed them into the PLM, and extract the resulting $t_{max} \times t_{max}$ partial self-attention matrices M_P for a specific self-attention head³.

The Frequency Normalization Method allows us to combine the partially overlapping selfattention matrices M_P into a single document-level matrix M_D of size $m \times m$. To this end, we interpolate multiple overlapping windows by adding up the self-attention cells of tokens t_i , while keeping track of the number of overlaps in a separate $m \times m$ frequency matrix M_F . We then divide M_D by the frequency matrix M_F , to generate a frequency normalized self-attention matrix.

The EDU Aggregation is the final processing step to obtain the document-level self-attention matrix M_A . In this step, the *m* sub-word tokens $T = \{t_1, \dots, t_m\}$ are aggregated back into n EDUs $E = \{e_1, ..., e_n\}$ by computing the average bidirectional self-attention score between any two EDUs in $\frac{M_D}{M_E}$. Then, we use the resulting $n \times n$ matrix M_A as the input to the CKY/Eisner discourse tree generation methods. Figure 1 visualizes the complete process on a small scale example.

Dataset	Task	Domain
IMDB(2014)	Sentiment	Movie Reviews
Yelp(2015)	Sentiment	Reviews
SST-2(2013)	Sentiment	Movie Reviews
MNLI(2018)	NLI	Range of Genres
CNN-DM(2016)	Summarization	News
XSUM(2018)	Summarization	News
SQuAD(2016)	Question-Answering	Wikipedia

Table 1: The seven fine-tuning datasets used in this work along with the underlying tasks and domains.

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Experimental Setup 4

4.1 Pre-Trained Models

We select the *BERT-base* (110 million parameters) and BART-large (406 million parameters) models for our experiments. We choose these models for their diverse objectives (encoder-only vs. encoderdecoder), popularity for diverse fine-tuning tasks, and their prior exploration in regards to discourse (Zhu et al., 2020; Koto et al., 2021a). For the BARTlarge model, we limit our analysis to the encoder, as motivated in Koto et al. (2021a), leaving experiments with the decoder for future work.

4.2 Fine-Tuning Tasks and Datasets

We explore the BERT model fine-tuned on two classification tasks, namely sentiment analysis and natural language inference (NLI). For our analysis on BART, we select the abstractive summarization and question answering tasks. Table 1 summarizes the 7 datasets used to fine-tune PLMs in this work, along with their underlying tasks and domains⁴.

4.3 Evaluation Treebanks

RST-DT (Carlson et al., 2002) is the largest English RST-style discourse treebank, containing 385 Wall-Street-Journal articles, annotated with full constituency discourse trees. To generate additional dependency trees, we apply the conversion algorithm proposed in Li et al. (2014).

GUM (Zeldes, 2017) is a steadily growing treebank of richly annotated texts. In the current version 7.3, the dataset contains 168 documents from 12 genres, annotated with full RST-style constituency and dependency discourse trees.

All evaluations shown in this paper are executed on the 38 and 20 documents in the RST-DT and GUM test-sets, to be comparable with previous baselines and supervised models.

²For more information on the tree-generation approach, we refer interested readers to Xiao et al. (2021b).

³We omit the self-attention indexes for better readability.

⁴We exclusively analyze published models provided on the huggingface platform, further specified in Appendix A.



(a) BERT: PLM, +IMDB, +Yelp, +SST-2, +MNLI



(b) BART: PLM, +CNN-DM, +XSUM, +SQuAD

Figure 2: Constituency (top) and dependency (bottom) discourse tree evaluation of BERT (a) and BART (b) models on GUM. Purple=high score, Blue=low score. Heads presented left-to-right, high layers on top. + indicates fine-tuning dataset.

4.4 Baselines and Evaluation Metrics

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Simple Baselines: We compare the inferred constituency trees against right- and left-branching structures. For dependency trees, we evaluate against simple chain and inverse chain structures. **Distantly Supervised Baselines:** We compare our results against the approach by Xiao et al. (2021b), using similar CKY and Eisner tree-generation methods to infer constituency and dependency tree structures from their summarization model trained on the CNN-DM and New York Times (NYT) corpora (called *Sum_{CNN-DM}* and *Sum_{NYT}*)⁵.

Supervised Baseline: We select the popular Two-Stage discourse parser (Wang et al., 2017) as our supervised baseline, due to its strong performance, available model checkpoints and code⁶, as well as the traditional architecture. We use the published Two-Stage parser checkpoint on RST-DT (from here on called *Two-Stage_{RST-DT}*) and re-train the discourse parser on GUM (*Two-Stage_{GUM}*). We convert the generated constituency structures into dependency trees following Li et al. (2014).

Evaluation Metrics: We apply the original parseval score to compare discourse constituency structures with gold-standard treebanks, as argued in Morey et al. (2017). To evaluate the generated dependency structures, we use the Unlabeled Attachment Score (UAS).

5 Experimental Results

5.1 Discourse Locality

Our discourse tree generation approach described in section 3 directly uses self-attention matrices to generate discourse trees. The standard BERT model contains 144 of those self-attention matrices (12 layers, 12 self-attention heads each), all of which potentially encode discourse structures. For the BART model, this number is even higher, consisting of 12 layers with 16 self-attention heads each. With prior work suggesting the locality of discourse information in PLMs (e.g., Raganato and Tiedemann (2018); Mareček and Rosa (2019); Xiao et al. (2021b)), we analyze every self-attention matrix individually to gain a better understanding of their alignment with discourse information. 367

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Besides investigating standard PLMs, we also explore the robustness of discourse information across fine-tuning tasks. We believe that this is an important step to better understand if the captured discourse information is general and robust, or if it is "re-learned" from scratch for downstream tasks. To the best of our knowledge, no previous analysis of this kind has been performed in the literature.

To this end, Figure 2 shows the constituency and dependency structure overlap of the generated discourse trees from every individual self-attention head with the gold-standard tree structures of the GUM dataset⁷. The heatmaps clearly show that constituency discourse structures are mostly captured in higher layers, while dependency structures are scattered throughout. Comparing the patterns between models, we find that, despite being finetuned on different downstream tasks, the discourse information is consistently encoded in the same self-attention heads. Even though the best performing self-attention matrix is not consistent, discourse information is clearly captured in a "local" subset of self-attention heads across all presented finetuning task. This plausibly suggests that the discourse information in pre-trained BERT and BART models is robust and general, requiring only minor adjustments depending on the fine-tuning task.

5.2 Discourse Quality

We now focus on assessing the discourse information captured in the single best-performing selfattention head. In Table 2, we compare the quality

⁵www.github.com/Wendy-Xiao/summ_ guided_disco_parser

⁶www.github.com/yizhongw/StageDP

⁷The analysis on RST-DT shows similar trends and can be found in Appendix B.

Madal	RST	-DT	GUM						
Wodel	Span	UAS	Span	UAS					
	BERT								
rand. init	↓ 25.5	↓ 13.3	↓ 23.2	↓ 12.4					
PLM	• 35.7	• 45.3	• 33.0	• 45.2					
+ IMDB	↓ 35.4	$\downarrow 42.8$	• 33.0	↓ 43.3					
+ Yelp	↓ 34.7	↓ 42.3	↓ 32.6	↓ 43.7					
+ SST-2	↓ 35.5	↓ 42.9	↓ 32.6	↓ 43.5					
+ MNLI	↓ 34.8	$\downarrow 41.8$	↓ 32.4	↓ 43.3					
	BART								
rand. init	↓ 25.3	↓ 12.5	↓ 23.2	↓ 12.2					
PLM	• 39.1	• 41.7	• 31.8	• 41.8					
+ CNN-DM	$\uparrow 40.9$	\uparrow 44.3	↑ 32.7	\uparrow 42.8					
+ XSUM	$\uparrow 40.1$	\uparrow 41.9	† 32.1	↓ 39.9					
+ SQuAD	$\uparrow 40.1$	\uparrow 43.2	↓ 31.3	↓ 40.7					
	Baselines								
Right-Branch/Chain	9.3	40.4	9.4	41.7					
Left-Branch/Chain ⁻¹	7.5	12.7	1.5	12.2					
Sum _{CNN-DM} (2021b)	21.4	20.5	17.6	15.8					
Sum _{NYT} (2021b)	24.0	15.7	18.2	12.6					
Two-Stage _{RST-DT} (2017)	72.0	71.2	54.0	54.5					
Two-Stage _{GUM}	65.4	61.7	58.6	56.7					

Table 2: Original parseval (Span) and Unlabelled Attachment Score (UAS) of the single best performing self-attention matrix of the BERT and BART models compared with baselines and previous work. \uparrow , \bullet , \downarrow indicate better, same, worse performance compared to the PLM. "rand. init"=Randomly initialized transformer model of similar architecture as the PLM.

of generated discourse structures between different pre-trained and fine-tuned models, as well as additional baselines⁸. The results are separated into three sub-tables, showing the results for BERT, BART and baseline models on the RST-DT and GUM treebanks. In the BERT and BART sub-table, we further annotate each performance with \uparrow , \bullet , \downarrow , indicating the relative performance to the standard pre-trained model as superior, equal, or inferior.

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Taking a look at the top sub-table (BERT) we find that, as expected, the randomly initialized transformer model achieves the worst performance. Fine-tuned models perform equal or worse than the standard PLM. Despite the inferior results of the fine-tuned models, the drop is rather small, with the sentiment analysis models consistently outperforming NLI. This seems reasonable, given that the sentiment analysis objective is intuitively more aligned with discourse structures (e.g., long-form reviews with potentially complex rhetorical structures) than the between-sentence NLI task, not involving multi-sentential text.

In the center sub-table (BART), a different trend 436 emerges. While the worst performing model is still 437 (as expected) the randomly initialized system, fine-438 tuned models mostly outperform the standard PLM. 439 Interestingly, the model fine-tuned on the CNN-440 DM corpus consistently outperforms the BART 441 baseline, while the XSUM model performs bet-442 ter on all but the GUM dependency structure eval-443 uation. On one hand, the superior performance 444 of both summarization models on the RST-DT 445 dataset seems reasonable, given that the fine-tuning 446 datasets and the evaluation treebank are both in the 447 news domain. The strong results of the CNN-DM 448 model on the GUM treebank, yet inferior perfor-449 mance of XSUM, potentially hints towards depen-450 dency discourse structures being less prominent 451 when fine-tuning on the extreme summarization 452 task, compared to the longer summaries in the 453 CNN-DM corpus. The question-answering task 454 evaluated through the SQuAD fine-tuned model un-455 derperforms the standard PLM on GUM, however 456 reaches superior performance on RST-DT. Since 457 the SQuAD corpus is a subset of Wikipedia articles, 458 more aligned with news articles than the 12 genres 459 in GUM, we believe the stronger performance on 460 RST-DT (i.e., news articles) is again reasonable, 461 yet shows weaker generalization capabilities across 462 domains (i.e., on the GUM corpus). Interestingly, 463 the question-answering task seems more aligned 464 with dependency than constituency trees, in line 465 with what would be expected from a factoid-style 466 question-answering model, focusing on important 467 entities, rather than global constituency structures. 468

Directly comparing the BERT and BART models, the former performs better on three out of four metrics. At the same time, fine-tuning hurts the performance for BERT, however, improves BART models. Plausibly, these seemingly unintuitive results may be caused by the following co-occurring circumstances: (1) The inferior performance of BART can potentially be attributed to the decoder component capturing parts of the discourse structures, as well as the larger number of self-attention heads "diluting" the discourse information. (2) The different trends regarding fine-tuned models might be directly influenced by the input-length limitation to 512 (BERT) and 1024 (BART) subword tokens during the fine-tuning stage, hampering the ability to capture long-distance semantic and pragmatic relationships. This, in turn, limits the amount of discourse information captured, even

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⁸For a more detailed analysis of the min., mean, median and max. self-attention performances see Appendix C.



Figure 3: PLM discourse constituency (left) and dependency (right) structure overlap with baselines and gold trees (e.g., BERT \leftrightarrow Two-Stage (RST-DT)) according to the original parseval and UAS metrics.

for document-level datasets (e.g., Yelp, CNN-DM, SQuAD). With this restriction being more prominent in BERT, it potentially explains the comparably low performance of the fine-tuned models.

Finally, the bottom sub-table puts our results in the context of baselines. Compared to simple right- and left-branching trees (Span), the PLM-based models reach clearly superior performance. Looking at the chain/inverse chain structures (UAS), the improvements are generally lower, however, the vast majority still outperforms the baseline. Comparing the first two sub-tables against completely supervised methods (Two-Stage_{RST-DT}, Two-Stage_{GUM}), the BERTand BART-based models are, unsurprisingly, inferior. Lastly, compared to the distantly supervised Sum_{CNN-DM} and Sum_{NYT} models, the PLM-based discourse performance shows clear improvements over the 6-layer, 8-head standard transformer.

5.3 Discourse Similarity

Further exploring what kind of discourse information is captured in the PLM self-attention matrices, we directly compare the emergent discourse structures with baseline trees. This way, we aim to better understand if the information encapsulated in PLMs is complementary to existing methods, or if the PLMs only capture trivial discourse phenomena and simple biases (e.g., resemble right-branching constituency trees). Since the GUM dataset contains a more diverse set of test documents (12 genres) than the RST-DT corpus (news), we perform our experiments from here on exclusively on GUM.

Figure 3 shows the micro-average structural overlap of discourse constituency (left) and dependency (right) trees between the PLM-generated structures



Figure 4: Nested aggregation approach for discourse similarity. Grey cells contain same-head/same-model ((a)/(b)), white cells indicate between-head/between-model ((a)/(b)). Column indices equal row indices.

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and our baseline models, as well as gold-standard trees. Noticeably, the generated constituency trees (on the left) are most aligned with the structures predicted by supervised discourse parsers, showing only minimal overlap to simple structures (i.e., right- and left-branching trees). Taking a closer look at the generated dependency structures presented on the right side in Figure 3, the alignment between PLM inferred discourse trees and the simple chain structure is predominant, suggesting a potential weakness in regards to the discourse captured in the BERT and BART model. Not surprisingly, the highest overlap between PLM-generated trees and the chain structure occurs when finetuning on the CNN-DM dataset, well-known to contain a strong lead-bias (Xing et al., 2021).

To better understand if the PLM-based discourse structures are complementary to existing, supervised discourse parsers, we further analyze the correctly predicted overlap. More specifically, we compute the intersection of both, the PLM model and the baselines with gold-standard trees (e.g., BERT \cap Gold Trees \leftrightarrow Two-Stage (RST-DT) \cap Gold Trees) and further intersect the two resulting sets. This way, we explore if the correctly predicted PLM discourse structures are a subset of the correctly predicted trees by supervised approaches, or if complementary discourse information is captured. We find that >20%/>16% of the correctly predicted constituency/dependency structures of our PLM discourse inference approach are not captured by supervised models, making the exploration of ensemble methods a promising future avenue. A detailed version of Fig. 3 as well as more specific results regarding the correctly predicted overlap of discourse structures are shown in Appendix D.

5.4 Discourse Redundancy

Looking at the similarity of model self-attention heads in regards to their alignment with discourse

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(b) Dependency Similarity

Figure 5: BERT self-attention similarities on GUM. Top: Visual analysis of head-aligned (I&III) and model-aligned (II&IV) heatmaps. Yellow=high structural overlap, purple=low structural overlap.

Bottom: Aggregated similarity of same heads, same models, different heads and different models showing the min, max and quartiles of the underlying distribution. *Significantly better than respective \neq Head/ \neq Model performance with p-value < 0.05.

information, we now explore if (1) the top performing heads $h_i, ..., h_k$ of a specific model m_m capture redundant discourse structures, and if (2) the discourse information captured by a specific head h_i across different models $m_m, ..., m_o$ contain similar discourse information.

Specifically, we pick the top 10 best performing self-attention matrices of each model, remove selfattention heads that don't appear in at least two models (since no comparisons can be made), and compare the generated discourse structures in a nested aggregation approach.

Figure 4 shows a small-scale example of our nested visualization methodology. For the (selfattention) head-aligned approach (Figure 4(a)), high similarity values along the diagonal (grey cells) would be expected if the same head h_i encodes consistent discourse information across different fine-tuning tasks and datasets. Inversely, the model-aligned matrix (Figure 4(b)) should show high values along the diagonal if different heads h_i, \dots, h_k in the same model m_k capture redundant (i.e., similar) discourse information. Besides the visual inspection methodology presented in Figure 4, we also compare aggregated similarities between the same head (=Head) against different heads $(\neq$ Head) and between the same model (=Model) against different models (\neq Model) (i.e., grey cells (=) and white cells (\neq) in Figure 4(a) and (b)). In order to assess the statistical significance of the resulting differences in the underlying distributions, we compute a two-sided, independent t-test between

same/different models and same/different heads⁹.

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The resulting redundancy evaluations for BERT¹⁰ are presented in Figure 5. It appears that the same self-attention heads h_i consistently encode similar discourse information across models indicated by: (1) High similarities (yellow) along the diagonal in heatmaps I&III and (2) through the statistically significant difference in distributions at the bottom of Figure 5(a) and (b). However, different self-attention heads $h_i, ..., h_k$ of the same model m_m encode different discourse information (heatmaps II&IV). While the trend is stronger for constituency tree structures, there is a single dependency self-attention head which does generally not align well between models and heads (purple line in heatmap III). Plausibly, this specific selfattention head encodes fine-tuning task specific discourse information. Overall, the similarity patterns observed in Figure 5(a) and (b) point towards an opportunity to combine model self-attention heads to improve the discourse inference performance compared to the scores shown in Table 2, where each self-attention head was assessed individually.

6 Conclusions

In this paper, we extend the line of *BERTology* work by focusing on the important, yet less explored, alignment of pre-trained and fine-tuned PLMs with large-scale discourse structures. We propose a novel approach to infer discourse information for arbitrarily long documents. In our experiments, we find that the captured discourse information is local and general, even across a collection of fine-tuning tasks. We compare the inferred discourse trees with supervised, distantly supervised and simple baselines to explore the structural overlap, finding that constituency discourse trees align well with supervised models, however, contain complementary discourse information. Lastly, we individually explore self-attention matrices to analyze the information redundancy. We find that similar discourse information is consistently captured in the same heads. Based on the insights we gained in this analysis of large-scale discourse structures in PLMs, in the short term, we intend to explore new discourse inference methods using multiple (diverse) self-attention heads. Long term, we plan to analyze PLMs with enhanced input-length limitations.

⁹Prior to running the t-test we confirm similar variance and the assumption of normal distribution (Shapiro-Wilk test).

¹⁰Evaluations for BART can be found in Appendix E.

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Huggingface Models А

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We investigate 7 fine-tuned BERT and BART models from the huggingface model library, as well as the two pre-trained models. The model names and links are provided in Table 3

Pre-Trained	Fine-Tuned	Link
BERT-base	-	https://huggingface.co/bert-base-uncased
BERT-base	IMDB	https://huggingface.co/textattack/bert-base-uncased-imdb
BERT-base	Yelp	https://huggingface.co/fabriceyhc/bert-base-uncased-yelp_polarity
BERT-base	SST-2	https://huggingface.co/textattack/bert-base-uncased-SST-2
BERT-base	MNLI	https://huggingface.co/textattack/bert-base-uncased-MNLI
BART-large	-	https://huggingface.co/facebook/bart-large
BART-large	CNN-DM	https://huggingface.co/facebook/bart-large-cnn
BART-large	XSUM	https://huggingface.co/facebook/bart-large-xsum
BART-large	SQuAD	https://huggingface.co/valhalla/bart-large-finetuned-squadv1

Table 3: Huggingface pre-trained and fine-tuned model links.

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B Self-Attention Matrices of Pre-Trained and Fine-Tuned Models



(a) BERT: PLM, +IMDB, +Yelp, +MNLI, +SST-2



(b) BART: PLM, +CNN-DM, +XSUM, +SQuAD

Figure 6: Constituency (top) and dependency (bottom) discourse tree evaluation of BERT (a) and BART (b) models on RST-DT. Purple=high score, blue=low score. + indicates fine-tuning dataset.

C Detailed Self-Attention Statistics

	Span					Eisner			
Model	Min	Med	Mean	Max	Min	Med	Mean	Max	
RST-DT									
rand. init	21.7	23.4	23.4	25.5	7.5	10.3	10.3	13.3	
PLM	19.3	27.0	27.4	35.7	6.6	17.4	21.6	45.3	
+ IMDB	19.7	26.9	27.2	35.4	6.6	16.9	21.3	42.8	
+ YELP	20.2	26.6	26.9	34.7	7.0	16.5	21.0	42.3	
+ SST-2	19.5	27.3	27.7	35.5	7.3	17.6	21.9	42.9	
+ MNLI	18.5	26.9	27.1	34.8	6.9	17.5	21.5	41.8	
GUM									
rand. init	18.6	21.0	21.0	23.2	7.9	10.1	10.1	12.4	
PLM	17.8	24.2	24.3	32.6	6.7	16.0	21.2	45.2	
+ IMDB	18.1	23.8	24.1	32.7	6.1	15.9	21.0	43.3	
+ YELP	18.6	24.0	23.9	32.3	7.0	15.8	20.7	43.7	
+ SST-2	18.2	24.6	24.7	32.3	6.5	16.5	21.6	43.5	
+ MNLI	17.4	23.9	24.2	32.1	6.8	16.6	21.3	43.3	

Table 4: Minimum, median, mean and maximum performance of the self-attention matrices on RST-DT and GUM for the BERT model.

Model	Span					Eisner			
	Min	Med	Mean	Max	Min	Med	Mean	Max	
RST-DT									
rand. init	20.3	23.3	23.3	25.3	8.5	10.6	10.6	12.5	
PLM	20.3	28.3	28.5	39.1	4.1	15.8	19.2	41.7	
+ CNN-DM	20.5	28.6	28.7	40.9	3.6	15.2	19.2	44.3	
+ XSUM	20.2	27.6	28.3	40.1	4.8	14.8	18.7	41.9	
+ SQuAD	20.5	27.6	28.2	40.1	2.8	14.8	18.8	43.2	
GUM									
rand. init	18.6	21.0	21.0	23.2	8.0	10.2	10.2	12.2	
PLM	16.7	23.4	23.8	31.5	2.6	15.2	18.7	41.8	
+ CNN-DM	15.9	23.7	24.1	32.4	3.7	14.7	18.9	42.8	
+ XSUM	16.4	23.2	23.9	31.8	3.0	14.1	18.1	39.9	
+ SQuAD	16.1	23.4	23.8	31.0	2.4	14.8	18.3	40.7	

Table 5: Minimum, median, mean and maximum performance of the self-attention matrices on RST-DT and GUM for the BART model.



Figure 7: Detailed PLM discourse constituency (left) and dependency (right) structure overlap with baselines and gold trees according to the original parseval and UAS metrics.



Figure 8: Detailed PLM discourse constituency (left) and dependency (right) structure performance of intersection with gold trees (e.g., BERT \cap Gold Trees \leftrightarrow Two-Stage (RST-DT) \cap Gold Trees) according to the original parseval and UAS metrics.

E Intra- and Inter-Model Self-Attention Comparison



Heatmaps sorted by heads (left) and models (right)



(a) BERT constituency tree similarity on GUM



Heatmaps sorted by heads (left) and models (right)



(c) BART constituency tree similarity on GUM



Heatmaps sorted by heads (left) and models (right)



(b) BERT dependency tree similarity on GUM



Heatmaps sorted by heads (left) and models (right)



(d) BART dependency tree similarity on GUM

Figure 9: Top: Visual analysis of sorted heatmaps. Yellow=high score, purple=low score. Bottom: Aggregated similarity of same heads, same models, different heads and different models. *=Head/=Model significantly better than \neq Head/ \neq Model performance with p-value < 0.05.