# Dual Process Learning: Controlling Use of In-Context vs. In-Weights Strategies with Weight Forgetting

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# **Abstract**

Language models have the ability to perform in-context learning (ICL), allowing them to flexibly adapt their behavior based on context. This contrasts with in-weights learning (IWL), where information is statically encoded in model parameters from iterated observations of the data. Despite this apparent ability to learn in-context, language models are known to struggle when faced with unseen or rarely seen tokens. Hence, we study **structural in-context learning**, which we define as the ability of a model to execute in-context learning on arbitrary tokens – so called because the model must generalize on the basis of e.g. sentence structure or task structure, rather than semantic content encoded in token embeddings. An ideal model would be able to do both: flexibly deploy in-weights operations (in order to robustly accommodate ambiguous or unknown contexts using encoded semantic information) and structural in-context operations (in order to accommodate novel tokens). We study structural in-context algorithms in a simple part-of-speech setting using both practical and toy models. We find that active forgetting, a technique that was recently introduced to help models generalize to new languages, forces models to adopt structural in-context learning solutions. Finally, we introduce temporary forgetting, a straightforward extension of active forgetting that enables one to control how much a model relies on in-weights vs. in-context solutions. Importantly, temporary forgetting allows us to induce a *dual process strategy* where in-context and in-weights solutions coexist within a single model. <sup>1</sup>

# 1 Introduction

A distinguishing trait of transformers is their ability to perform 'in-context' learning (ICL) [Brown et al., 2020, Dong et al., 2023, Garg et al., 2023] – the ability to use context at inference time to adjust model behavior, without weight updates, to generalize to unseen input-output combinations. This ability enables models to flexibly accommodate variations in language. For instance, a model is likely to possess the prior that the token *green* is an adjective, yet still recognize that it is used as a noun in the sentence *The child sat on the main green* based on contextual information.

Much recent research has studied ICL algorithms in transformers [Chan et al., 2022b, Singh et al., 2023, Garg et al., 2023]. This work focuses on ICL on heldout inputs that are imbued with semantic information. However, does ICL work on arbitrary inputs? Recent research suggests no: typical ICL algorithms fail when on undertrained [Land and Bartolo, 2024, Rumbelow and Watkins, 2023] or newly-introduced (e.g. when adding languages to an existing model) tokens [Chen et al., 2024]. This

<sup>&</sup>lt;sup>1</sup>We release code here for reproducibility

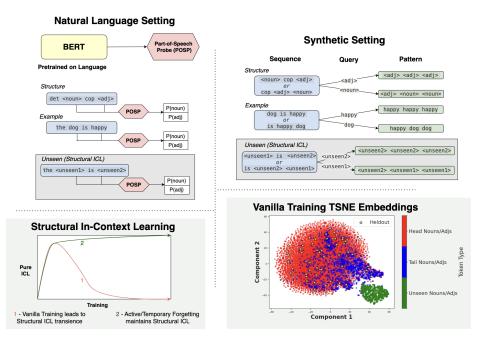


Figure 1: (Top Left) In our natural setting, we use a part-of-speech probe trained on BERT representations of sentences from Penn Treebank 3 and evaluate on templated examples (Section 3). (Top Right) In our synthetic setting, we train a small masked language model (MLM) on a grammar where the expected response is conditioned on the part-of-speech of the query (Section 4). (Bottom Left) An idealization of our main finding: structural ICL is transient (i.e. decays over training) in both natural and synthetic settings. Active/temporary forgetting maintains structural ICL in the synthetic setting. (Bottom Right) T-SNE visualization of token embeddings after standard vanilla MLM training on synthetic setting [van der Maaten and Hinton, 2008]. We see that embeddings in the head of the distribution clusters together, as do the unseen token embeddings. The embeddings in the tail of the distribution bridge between the two clusters. Models using conditional ICL would only generalize to the heldout examples that exist within the head token distribution. Models using structural ICL would freely generalize to all token embeddings.

results in bizarre, non-deterministic behavior on tasks such as asking GPT-3 to repeat back the string *attRot* [Rumbelow and Watkins, 2023]. We refer to these typical ICL algorithms as **conditional** ICL, as they break down when inputs have insufficient encoded information. In contrast, we define *structural ICL* to be the ability of a model to perform in-context learning on tokens without encoded information, (defined more precisely in Section 2). We analyze this strong form of ICL along training in naturalistic and synthetic tasks.

Our research expand upon a burgeoning literature that uses the framework of ICL vs. in-weights learning (IWL) to study the development of transformers (e.g. Chan et al. [2022b], Singh et al. [2023], Reddy [2023]). Specifically, Chan et al. [2022b] finds that while ICL and IWL strategies are often in opposition, a "sweet spot" language-like label distribution enables both ICL and IWL strategies to co-occur in the same model. This encoded *dual process* is potent in current language models, allowing flexible, context-sensitive operations for out-of-distribution settings and memorized, static operations for ambiguous contexts or IID settings [Kahneman, 2011, Miller, 2000]. Building off this, Singh et al. [2023] finds that ICL slowly dissipates as models are overtrained; they discover that L2-regularization mitigates ICL transience, but instead leads to IWL transience. We utilize the framework proposed in this literature to dissect ICL emergence into structural vs. conditional ICL development. Moreover, we aim to translate insights from these studies to actionable strategies to improve models on non-language-like data distributions – specifically, we attempt to elicit powerful dual processes in arbitrary data distributions.

In our research, we find that structural ICL is *also* transient. However, while regularization provides a path to persistence in conditional ICL [Singh et al., 2023], it does not for structural ICL. Therefore, we propose an extension to active forgetting – a recent weight resetting technique introduced by

Chen et al. [2024] to help augment models with new tokens – to make structural ICL persistent. Our modification allows us to coarsely control the strategies that the model adopts, enabling us to induce a dual process strategy: (structural) ICL for rare and unseen tokens and IWL for common tokens.

Our main contributions are:

- We define and study the concept of structural ICL in both large models and toy models
  using a simple part-of-speech probing task. This allows for true generalization of in-context
  strategies for completely unseen tokens. We discover that MLMs exhibit a (limited) form
  of structural in-context learning that emerges early in training, but that this ability quickly
  vanishes.
- We show active forgetting [Chen et al., 2024] maintains structural ICL in models. We introduce **temporary forgetting**, a straightforward extension of active forgetting that enables one to control how much a model relies on in-weights vs. in-context solutions.
- We demonstrate that when training with skewed token distributions, temporary forgetting enables us to induce a *dual process strategy* where our model uses an in-weights solution for frequently-seen tokens in the head of the distribution and a (structural) in-context solution for rare tokens in the tail.

#### 2 Definitions

**In-Context vs. In-Weights Learning** We follow Reddy [2023], which defines in-weights learning (IWL) to be "query-response relationships encoded in the weights of the network" while in-context learning (ICL) emerges due to "common structural element[s]" and "can be exploited to perform zero-shot learning on novel tasks that share this structure."

We formulate our ICL prediction task as  $\mathbb{P}(y \mid \mathbf{p}_{1:n}; \mathbf{z}_{1:n}; \mathbf{M}_{0:l})$  where y are the label(s),  $\mathbf{p}_{1:n}$  is the set of positional embeddings and  $\mathbf{z}_{1:n}$  is the set of word embeddings for a sequence of length n, and  $\mathbf{M}_{0:l}$  is a length l transformer.

Within this framework, token embeddings are purely in-weight representations, which are enriched with context information by attention layers.

Structural vs. Conditional ICL We define structural ICL precisely via an empirical test: a model exhibits structural ICL if it can employ analogical reasoning from context in a way that is robust to arbitrary embeddings. For one or more word embeddings at specified position(s)  $i \in I$ , we replace  $\mathbf{z}_i \xrightarrow{\text{replace}} \mathbf{z}_{\text{random}}$ . This removes the in-weight signal of the word embedding and forces reliance on in-context information and structural analogy.

In **conditional ICL**, the ordered set  $\mathbf{z}_{1:n}$  remains unmodified. This is the standard ICL setting studied by [Chan et al., 2022b, Singh et al., 2023, Garg et al., 2023, Akyürek et al., 2024]. Note that a model exhibiting conditional ICL does not imply that the same model will exhibit structural ICL.

# 3 (Structural) In-Context Learning is Transient

Recent work has discovered that conditional ICL capabilities slowly degrade in synthetic settings over the course of training [Singh et al., 2023]. Building on this work, we track the tradeoff of conditional IC vs. IW algorithms in a naturalistic syntax probing task over the course of training for encoder-only language models (LMs). More importantly, we also track structural ICL over the course of training. We study the MultiBERTs, averaging all of our results across seeds 0, 1, and 2. We calculate error bars in Figure 2 as  $\pm 1$  standard error of the mean (SEM).

#### 3.1 Task

We design a task that employs templated stimuli to determine the tradeoffs between different strategies for assigning part of speech to tokens – this task permits both structural IC and IW solutions. For instance, in the sentence *the dog is happy*, there are at least two ways of determining that *dog* is a noun: (1) memorize that the token identity "dog" is a noun or (2) extract that *dog* is the subject of the sentence from the context. For each layer and MultiBERT step, we train a binary POS probe on representations of nouns and adjectives from sentences in the training set of Penn Treebank 3

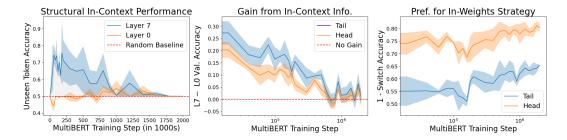


Figure 2: (Left) We exhibit the transience of structural ICL by examining the Unseen Token Accuracy over time. (Middle) We show the trend of memorization of tail versus head of distribution over training steps by examining the difference in Layer 7 Accuracy, where both in-context and in-weights strategies are possible, and Layer 0 Accuracy, where only an in-weights strategy is possible; (Right) We display the preference for in-weights strategy when conflicting with in-context strategy over time.

(PTB-3) [Marcus et al., 1993]. For multi-token words, we average representations across tokens. See Appendix A.1 for additional details about our probing setup. We then evaluate the pretrained MultiBERT and probe on a suite of test sets designed to assess the adoption of in-context or in-weights strategies. Each dataset contains sentences that obey the template: The <noun> is <adj> (e.g. The dog is happy). Our evaluation datasets are defined as follows:

- 1. **Head**: Templated examples where tokens are sampled from the most frequent 1500 nouns and most frequent 1500 adjectives in the training set of PTB-3.
- 2. **Tail**: Templated examples where tokens are sampled from the least frequent 1500 nouns and most frequent 1500 adjectives in the training set of PTB-3.
- 3. **Head Switch**: Templated examples where tokens are sampled as in the "Head" dataset, but where nouns appear in the adjective position and adjectives appear in the noun position (e.g., *The happy is dog*).
- 4. **Tail Switch**: Defined similarly to "Head Switch", except where the tokens are sampled from the tail of the token distribution.
- 5. **Unseen Token**: Templated examples where "nouns" and "adjectives" are sampled from a set of 1,500 randomly initialized tokens. This metric evaluates structural ICL performance<sup>2</sup>.

Note that the MultiBERTs are trained following Devlin et al. [2019] on a combination of BookCorpus [Zhu et al., 2015] and English Wikipedia collected by Turc et al. [2019]. As such, the distribution of the training data is fixed, and our experiments are constrained to the natural distribution of language. As BookCorpus does not have POS tags readily accessible, we employ PTB-3 to estimate the noun and adjective distribution of the training data. We defined nouns and adjectives as words that appeared as each POS, respectively, over 80% of the time. We chose 1500 examples as this is  $\approx 10\%$  of the number of unique nouns.

# 3.2 Training Dynamics

We examine (1) structural in-context learning and (2) the tradeoff between in-context and in-weight strategies over the course of training.

Structural ICL We find that the MultiBERTs are initially able to perform structural ICL, but that this capability is transient. In Figure 2 (Left), we present results from a probe trained on representations from Layer 7 as this layer achieves the highest probing validation performance on PTB-3. This is consistent with prior research which demonstrates that syntactic structures are encoded in the middle layers of MLMs Tenney et al. [2019], Limisiewicz and Mareček [2020]. Furthermore, results across all layers are presented in Appendix A.2. Structural ICL transience is evident as probe performance on Unseen Tokens tend to spike early in MultiBERT training before dropping to chance by the end of training. These results suggest that there is an inductive bias toward structural ICL that diminishes as information is encoded in the embeddings. As structural ICL confers the ability to generalize to rare and new tokens, this raises questions about how we can train models that maintain this ability throughout training.

<sup>&</sup>lt;sup>2</sup>We are able to generate novel labels not seen during train time because the embedding and unembedding matrices are tied in the MultiBERT models.

**In-Context vs. In-Weights Strategies** Next, we compare conditional in-context vs. in-weights strategies for observed tokens. First, we observe that ICL strategies dissipate over training, as more information is encoded in token embeddings. We approximate the use of in-context information for determining POS as the difference in performance between Layer 0 (the embedding layer) and Layer 7. Layer 0 must rely only on in-weights information as there is no in-context information available; in contrast, Layer 7 uses contextualization to achieve higher performance [Tenney et al., 2019, Hewitt et al., 2021]. Early in training, this additional in-context information leads to higher probe accuracy; however, this benefit disappears over time. Figure 2 (Middle) demonstrates this trend across tokens at the head and tail of the distribution. Notably, the benefit of in-context information disappears more quickly for the head of the distribution than the tail, likely because there are far more gradient updates to head token embeddings.<sup>3</sup>

As the benefit of the model's use of in-context information dissipates, we observe that the model shifts from an in-context to an in-weights strategy in Figure 2 (Right). Specifically, we find that a model's preference toward assigning POS on the basis of token identity (i.e. an in-weights solution) increases slightly over time when in-context and in-weights information are in conflict. In other words, models becomes more reliant on in-weights strategies and less reliant on in-context strategies over the course of training. This finding aligns with Singh et al. [2023], which analyzed a similar phenomenon using toy models and a synthetic task. Additionally, we observe that the degree to which the model adopts an in-weights strategy varies significantly for tokens selected from the head versus the tail of the distribution. When assigning POS to tokens in the the head of the distribution, the model relies almost exclusively on an in-weights solution, while the model relies on both in-weights and in-context solutions when assigning POS to tokens in the tail.

In summary, we find that (1) the benefit of the model's use of context information disappears over time and (2) reliance on in-weights information increases over time, varying depending on the distributional properties of the token that we are probing.

# 4 Synthetic Task: Distributional Parameters Impact In-Context Learning

We develop a synthetic masked language modeling task to reproduce the above trends, in order to characterize how distributional parameters affect the learning strategy that the model adopts. Our synthetic task requires the model to determine which of two classes a word belongs to. This may be derived either from in-context information or by memorizing token identity-class associations in the embedding layer. We draw analogies between these classes and POS in natural language.

Our vocabulary contains tokens that represent nouns, adjectives, and a copula (i.e. is). Each sentence is created by selecting (1) a sequence S, (2) a query Q, and (3) a response pattern P. Our MLM is trained to predict  $\mathbb{P}(P_i|S,Q)$  for all  $i\in\{0,\ldots,|P|-1\}$  (i.e. the probability of each pattern token). The sequence and pattern are arbitrary and designed so that no exceedingly simple heuristic may solve this task.

- sequence S: Either <noun> <copula> <adj> or <copula> <adj> <noun>.
- query Q: Either the <noun> or <adj> from the sequence.
- pattern P: Either <adj> <noun> <noun> if the query is a <noun> or <adj> <adj> <adj> if the query is an <adj>.

This task is designed such that the model must make a POS classification on the query token, and then perform some additional operation conditioned on that classification (copying specific token identities in a specific order). See Appendix A.5 for more details. See Figure 1 for an example.

We parameterize the task with vocabulary size v, the sampling distribution skew for nouns/adjectives  $\alpha$  (where we select <noun>, <ad> ~ Zipf( $\alpha$ )), and the ambiguity of token POS  $\varepsilon$ . The ambiguity parameter determines the percentage of tokens can act as both as noun and an adjective, and is inspired by the inherent ambiguity of POS in natural language. For our primary experiments, we fix  $\varepsilon=0.10$ . Note, we find that  $\varepsilon$  must be greater than zero for an in-context solution to emerge at all. We compare our skewed distribution results to sampling tokens from a Uniform distribution.

In this task, an ICL solution to derive the POS of the query may achieve perfect accuracy by utilizing in-context information (e.g. a *copula* is always followed first by an adjective, then a noun). In contrast,

<sup>&</sup>lt;sup>3</sup>We observe that performance gain due to the model's use of in-context information decreases across a wide range of syntactic phenomena as embeddings are enriched during training. We term this the "Pushdown Phenomenon" and explore it more thoroughly in Appendix A.4.

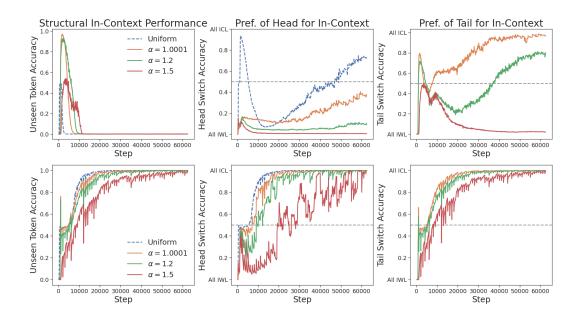


Figure 3: (Top) In-context performance by distribution with vanilla training; (Bottom) In-context performance by distribution with active forgetting. The parameters used are  $v = 10000, \varepsilon = 0.10$ . Note that the Uniform distribution does not have a head or a tail, so its results are in the head graphs.

an IWL solution to derive the POS of the query may achieve at most an accuracy of  $(1 - \varepsilon/2)$  due to ambiguous tokens. To account for this, we evaluate our models only on tokens that are not ambiguous; thus, both an ICL and IWL solution could achieve perfect accuracy. (Ambiguous tokens always use an ICL solution.)

Our task is formatted in a cloze-style where each token in the pattern is masked. We employ a MLM [Devlin et al., 2019] to predict the identities of these masked tokens, with hyperparameters described in Appendix A.6. Near-perfect validation accuracy is achieved after <60,000 steps on all experimental settings.

In addition to performance on a randomly selected validation set, we create datasets to evaluate the model's preferred strategy throughout training, similar to Section 3. All examples in these datasets contain novel <adj>, <noun> pairs. Much like our naturalistic setting metrics in Section 3.1, we create Tail, Head, Head Switch, Tail Switch, and Unseen Token Accuracy metrics. In this setting, our head and tail metrics use the top and bottom 10% of the token distribution by count, respectively.

# 4.1 Training Dynamics

**Structural ICL** We largely reproduce the results from the natural language setting presented in Section 3: structural in-context solutions emerge quickly, but are transient. This is shown by the early peak of Unseen Token Accuracy, followed by its steep drop. This trend holds across all tested distributions in Figure 3 (Top Left). As such, both the syntactic and naturalistic settings align with our idealized graph of structural ICL transience exhibited in Figure 1 (Bottom Left). However, the disappearance of a structural in-context algorithm occurs extremely quickly compared to our MultiBERT experiments, likely due to the simplicity of our synthetic task.

**In-Context vs. In-Weights Strategies** In this section, we analyze whether models adopt conditional ICL or IWL strategies over the course of training. Our results are presented in Figure 3. Importantly, we find that increasing the skew of a distribution increases the pressure toward an IWL strategy. Conversely, examples with tokens drawn from a Uniform sampling distribution show a comparatively higher ICL preference (and thus lower IWL preference) than any Zipfian sampling distribution in Figure 3 (Top Middle). Among Zipfian skewed distributions, the model's strategy varies based on whether the adjective and noun are in the head or the tail of the token distribution, much like in our naturalistic task. As in Section 3, we find that all skewed distributions prefer a IWL strategy for head

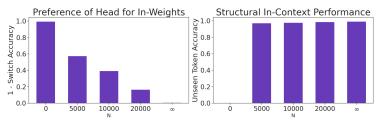


Figure 4: In-weights preference is coarsely controllable by varying temporary forgetting parameter N. All N>0 settings in figure induce success on completely abstracted generalization for all N. Note N=0 is vanilla training and  $N=\infty$  is active forgetting. Parameters used are  $v=10000, \varepsilon=0.10, \alpha=1.5$ .

tokens. However, for tail tokens, distributions of moderate skew ( $\alpha=1.0001, \alpha=1.2$ ) prefer an ICL strategy as shown in Figure 3, while highly skewed distributions ( $\alpha=1.5$ ) fail altogether as shown in Appendix A.7. This is likely due to the fact that these tokens are rarely observed in the training data. This illustrates an important distinction between structural ICL and conditional ICL – a structural ICL solution would maintain performance on the tail of highly skewed distributions. Additional experiments exploring the effect of ambiguity are located in Appendix A.8 and the effect of vocabulary size are located in Appendix A.9.

# 5 Maintaining Structural ICL with Active Forgetting

In Sections 3 and 4, we have demonstrated that as information gets memorized in the embeddings, the benefits of in-context information dissipate and models shift to an IWL strategy. In an effort to promote structural ICL, we utilize a recently-introduced training procedure: active forgetting [Chen et al., 2024]. When training a model using active forgetting, we re-initialize the embedding matrix every k steps during training. The intuition behind this is that the model must employ in-context strategies to achieve high accuracy, as no information can be preserved in each token's embedding. In other words, the model can no longer assume that the input embeddings encode any particular information and thus must develop a structural ICL strategy. While after vanilla training, these unseen embeddings are out-of-distribution as illustrated in Figure 1 (Bottom Right), we hypothesize that these unseen embeddings would align with seen embeddings after training with active forgetting. We explore this hypothesis in Section A.10.

Training our models with active forgetting successfully engenders structural ICL, enabling the model to approach perfect performance on the Unseen Token Set (See Figure 3, Bottom Left). Given two random embeddings representing a noun and an adjective, the model can now (1) derive the POS of these tokens and (2) output the identity of these out-of-distribution embeddings in the desired pattern. Note that we see a slightly more stochastic version of our idealized trend from Figure 1 (Bottom Left) due to the resetting mechanism.

We test k=100,1000,5000 and settle on k=1000, as this worked well in our preliminary exploration. With active forgetting, both the head and the tail of the training distribution prefer an asymptotic in-context strategy across all tested skews (See Figure 3, Bottom). Still, as the skew of the distribution of nouns and adjectives increases, there is greater pressure to memorize the head of the distribution (as these tokens are observed more frequently). Thus, it takes longer for the model to exhibit a preference towards in-context solutions for head tokens (e.g. almost 60,000 steps for the  $\alpha=1.5$  setting) and there is a much larger drop-off in performance after every instance of forgetting the embedding matrix. Our PCA Analysis suggests that this works by shifting unseen tokens from out-of-distribution to in-distribution (See Appendix A.10).

# 6 Dual Process Learning with Temporary Forgetting

While active learning successfully induces a structural ICL strategy, our model loses the ability to memorize information in its embeddings. This is detrimental in a variety of cases, such as when in-context information is insufficient to generate an appropriate response. An optimal model would encode a *dual process strategy*: maintaining a structural ICL solution while also memorizing useful linguistic properties [Chan et al., 2022b]. We modify the paradigm of active forgetting to attempt to

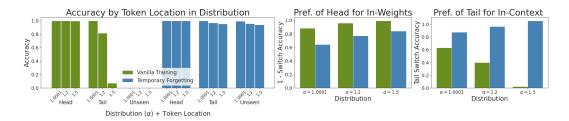


Figure 5: (Left) Temporary forgetting achieves near perfect unseen token performance (structural in-context) asymptotically among distributions. (Right) In addition, temporary forgetting can asymptotically hold preference for an in-weights strategy in the head of the distribution while holding preference for an in-context strategy in the tail of the distribution (i.e. learn dual processes). Parameters used are  $v=10000, \varepsilon=0.10$  and optimal hyperpameters k,N over gridsearch.

induce a bias for structural in-context strategies in the tail of the distribution while preserving the in-weights solutions for frequently-observed tokens. We introduce **temporary forgetting**, where we perform active forgetting every k steps for the first N steps (N >> k) of training. After this point, we allow the embedding matrix to train as normal.

We find that by varying N, we can vary the model's dependence on in-weights information on frequently seen tokens while maintaining structural ICL performance as displayed in Figure 4. If N is too large, this training procedure mimics the behavior of active forgetting, eliminating in-weights solutions in favor of structural in-context solutions. Additionally, if N is too small, the training only *sometimes* maintains structural ICL performance; note, however, that this seems to be an all-ornothing effect. The sweet spot for N depends on the skew of the distribution. We show that in the  $\alpha=1.5$  case, we can specifically control the preference for an in-weights strategy over an in-context strategy on observed tokens by modifying N (See Figure 4). In general, by manipulating the k we reset the embeddings and N, we can calibrate the relative strength of ICL vs. IWL.

Thus, temporary forgetting enables a model to successfully encode two distinct strategies for the same task. While this dual process strategy was previously demonstrated in Zipfian distributions with  $\alpha \approx 1.0$ , we can now induce this behavior for any distribution  $\alpha \geq 1.0$ , while also inducing structural ICL behavior on *all distributions* (See Figure 5).<sup>4</sup> Note that the control granted by temporary forgetting over head IWL preference has limits – we can push up to almost 90% the original IWL preference while maintaining a high tail ICL preference.

Temporary forgetting imparts an incentive that significantly enhances our ability to balance between in-context and in-weights strategies, overcoming inherent biases in naturally occurring data. By tuning the hyperparameters (k, N), one can bias the model toward either type of solution.

# 7 Related Work

In Context v. In Weights A body of recent literature closely examines in-weights versus in-context learning [Chan et al., 2022b,a, Reddy, 2023, Raparthy et al., 2023, Fu et al., 2024]. The emergence of in-context learning abilities in transformers has been shown to depend on the distributional properties of the training data such as burstiness, training class rarity, and dynamic meaning [Chan et al., 2022b, Reddy, 2023]. While we employ a similar analytical framework to this work, we (1) consider truly random heldout inputs and novel outputs/labels, (2) evaluate on large, natural language models, and (3) consider structural ICL. Additionally, while slow transience of conditional ICL has been noted in Singh et al. [2023], we find abrupt transience of structural ICL. Unlike Singh et al. [2023], increasing L2-regularization does not affect the transience of structural ICL in our synthetic setting (See Appendix A.7). Finally, we introduce temporary forgetting to solve what both Singh et al. [2023] and Chan et al. [2022b] suggest to be an extremely useful behavior: the co-existence of in-context learning and in-weights learning.

More broadly, the conflict between context-dependent and context-independent (or reflexive) solutions has been well-studied in the cognitive and computational neuroscience literature [Russin et al., 2024,

<sup>&</sup>lt;sup>4</sup>Distributions where  $\alpha \leq 1.0$  would likely only rely on an in-context strategy

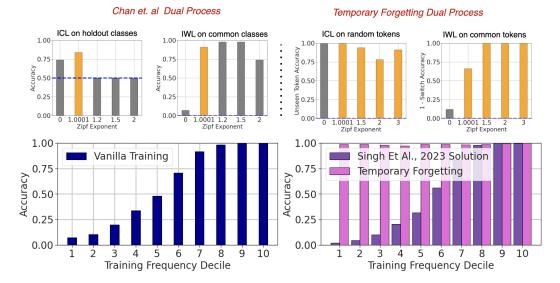


Figure 6: (Top) Temporary forgetting's ability to invoke dual processes (in yellow) on various distributions compared with Chan et al. [2022b] observational baseline. (Bottom) Comparison with Singh et al. for synthetic task on skewed distribution (Zipfian  $\alpha=1.5$ ). Temporary forgetting solves performance on undertrained/tail tokens in a skewed distribution by preserving structural ICL.

Rougier et al., 2005, Russin et al., 2022]. A key feature of human intelligence, termed *cognitive control*, is the ability to maintain dual strategies and flexibly deploy either one in response to particular stimulus. Any artificial system that aspires to producing human-like behavior must therefore be capable of maintaining both of these solutions.

Weight Forgetting To Help Learn. While most literature on *forgetting* characterizes this phenomenon as undesirable [Kemker et al., 2017, Kirkpatrick et al., 2017, McCloskey and Cohen, 1989, Ratcliff, 1990], recent neuroscience literature has shown that *intentional* forgetting may have positive roles in certain contexts [Srivastava et al., 2014, Pastötter et al., 2008, Levy et al., 2007, Anderson and Hulbert, 2021]. Intentional forgetting in neural networks is accomplished by resetting a subset of parameters during training. On computer vision tasks, this resetting procedure has been shown to help low compute and data resource generalization [Alabdulmohsin et al., 2021, Taha et al., 2021, Ramkumar et al., 2023]. Additionally, Zhou et al. [2022] show that a *forget-and-relearn* paradigm helps language emergence. Our method of forgetting embeddings is directly inspired by Chen et al. [2024], which shows forgetting during pretraining boosts linguistic plasticity for multilingual learning. As far as we know, we are the first to propose using forgetting to induce ICL.

#### 8 Discussion

This research provides insights into the interplay between structural ICL, conditional ICL and IWL within transformers. We shed light on several critical factors determining how models manage and utilize the encoded and contextual information when faced with novel tokens and tasks.

**Structural In-Context Learning** One of our key findings is the transience of structural ICL in LMs. Initially, models exhibit a strong ability to leverage structural ICL, generalizing algorithms to unseen tokens. However, this capability dissapears as training progresses, suggesting an initial inductive bias towards structural ICL that wanes as the model learns. This transience limits generalization on rare tokens and new tokens. We find that active forgetting maintains structural ICL by repeatedly reinitializating the embeddings. Our temporary forgetting training procedure enables a dual process strategy through strategic re-initialization of weights. This enables adaptability while still leveraging accumulated knowledge.

**Implications for Model Training and Application** Our findings are useful to design training protocols that result in flexible models. A significant reason for the success of LMs is their capacity

for ICL and IWL strategies to co-exist, a behavior that organically occurs with a moderately skewed Zipfian distribution. However, most natural domains such as protein discovery, network traffic, and video recording face even more skew, breaking down this ideal behavior. Our temporary forgetting technique facilitates a dual process strategy regardless of skew, which could potentially bring some of the profound success of LMs to other domains.

**Future Directions and Limitations** The research opens up several avenues for future investigation. Future research should examine Structural ICL across different model architectures and configurations. One significant limitation is that our temporary forgetting experiments were not performed on LMs. Our compute resources limited such experiments, but we believe this is a critical future step to refining this training intervention. Another limitation of our work is that the optimal hyperparameters to temporary forgetting are not known a priori, and might require several runs to tune. Finally, another avenue of fruitful future research may be the translation of structural ICL algorithms into symbolic systems. As structural ICL does not rely on the content of the input, it should be possible to use techniques like circuit analysis [Räuker et al., 2023] to reverse-engineer an explicit symbolic representation of the algorithm that the neural network uses to solve a task.

**Conclusion** This study deepens our understanding of a model's adoption of structural ICL, conditional ICL, and IWL strategy during training. The techniques introduced here not only enhance our theoretical understanding but also offer practical tools for improving model training and functionality in real-world applications.[Gentner, 1983]

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# A Appendix / supplemental material

# A.1 Probing Setup

We provide probing background in this section, borrowing some notation from Elazar et al. [2020].

Given a set of labeled data of points  $X=x_1,\ldots x_n$  and task labels  $Y=y_1,\ldots ,y_n$ , we analyze a model f that predicts the labels Y from  $X:\hat{y_i}=f(x_i)$ . We assume that this model is composed of two parts: (1) an encoder h that transforms input  $x_i$  into a learned representation vector  $\mathbf{h}_{x_i}$  and (2) a classifier c that is used for predicting  $\hat{y_i}$  based on  $\mathbf{h}_{x_i}$ , such that  $\hat{y_i}=c(h(x_i))$ . We refer by *probe* to the classifier c and refer by *model* to the model from which the encoder h is a subset of.

Given this setup, we evaluate a particular model's performance across various layers and training steps for our POS task. Each encoder h is associated with a specific training step and layer  $h^{t,l}$ . We probe the residual stream after layer l.

In this research, we are interested in the model's choice of strategy at a particular time step. That is, we seek to describe the change in prediction of  $\hat{y_i}$  due to varying t, l of encoder  $h^{t,l}$ . Accordingly, we fix c as a single linear fully-connected layer.

#### A.2 Structural ICL across Layers

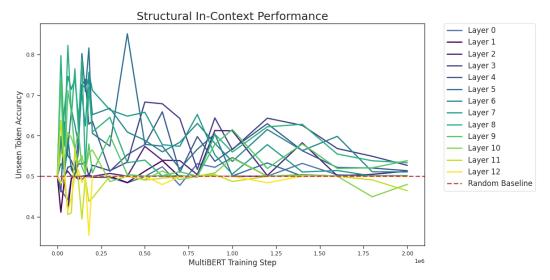


Figure 7: We find that structural ICL is transient across all layers of MultiBERTs (seeds 0, 1, 2 averaged). The middle layers show the most structural ICL during early in training, whereas very early and very late layers remain about random throughout training.

We find that structural ICL consistently approachs random levels as training progresses across layers in the MultiBERTs. This signifies that the model fully loses the ability to process unseen tokens as training continues. This is likely the reason for the "glitch tokens" described in Land and Bartolo [2024], for which LMs fail to output sensible content.

# A.3 Pushdown Datasets

We use the train/dev splits from the English UD Treebank for the *c-pos*, *f-pos*, and *dep* tasks McDonald et al. [2013]; the train/dev splits from Ontonotes-v5 in the CoNLL-2012 Shared Task format for the *ner*, *phrase start*, and *phrase end* tasks Linguistic Data Consortium [2013], Pradhan et al. [2012]; the train/dev splits from Penn Treebank-3 for the *depth* and *dist* tasks Marcus et al. [1993]; and generated token sequences for the *prev*, *dup*, and *ind* tasks.

We reproduce baselines from Elazar et al. [2020] to verify the correctness of our probing setups for *c-pos*, *f-pos*, *ner*, *dep*, *phrase start* and *phrase end* and from Hewitt and Manning [2019] for *depth* and *dist*.

#### A.4 Pushdown Signature Observation in Syntax

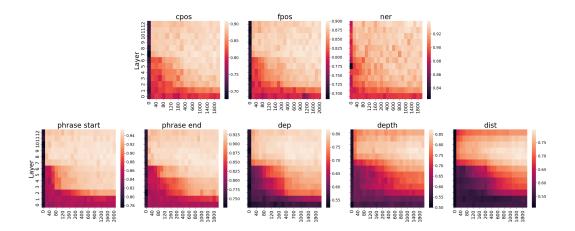


Figure 8: The "Pushdown Phenomenon" is observed across syntactic features, suggesting that a transition from IC to IW strategies happens across these features. In early steps of training, representing syntactic information occurs in later layers, which are more contextualized. However, as training progress, the same properties are better encoded in earlier layers due to memorization of token-level and n-gram level information. The n-gram level information requires attention to build, which explains why performance in *dep*, *depth*, and *dist* does not propagate all the way to embeddings.

The "Pushdown Phenomenon" suggests that in early steps of training, computing token-wise syntactic properties occurs in later layers, which have more in-context information. However, as training progress, the same properties are better encoded in earlier layers until only the first couple layers are required for representing syntactic properties.

We examine whether the "Pushdown Phenomenon" exists in various syntactic properties in BERT. To do so, we employ our probing setup (Appendix A.1) for the tasks of named entity recognition (*ner*), coarse part of speech (*c-pos*), fine-grained part of speech (*f-pos*), dependency parsing (*dep*), syntactic constituency boundaries which indicate the start and end of a phrase (*phrase start, phrase end*), depth in the parse tree (*depth*), and distance in the parse tree (*dist*). We probe each property across the axes of (1) training time steps and (2) layers. We repeat this process for three seeds of the MultiBERTs [Sellam et al., 2021]. For all tasks, we probed all layers of MultiBERT seeds 0, 1, and 2 for timesteps from 0 to 200,000 increasing by 20,000; 200,000 to 1,000,000 increasing by 100,000; and 1,000,000 to 2,000,000 increasing by 200,000. If a specific word is composed of multiple subword tokens, we follow Hewitt and Manning [2019] and average the encoding across tokens.

We observe the "Pushdown Phenomenon" in all our examined tasks. However, we find that across tasks, syntactic information is "pushed down" at different rates. Early layer accuracy increases approximately follow a pattern of  $ner \rightarrow phrase\ start \rightarrow cpos/fpos \rightarrow phrase\ end \rightarrow dep \rightarrow depth \rightarrow dist$ . We leave it to future work to explore whether this timing is a function of (1) complexity of high-achieving rules/heuristics consistent with Belrose et al. [2024] or (2) a naturally occurring dependency hierarchy of syntactic relationships suggestive of implicit curriculum learning. One possible intuition for why the "Pushdown Signature" of memorization often coincides with poor maintenance of in-context strategies might be neural collapse [Parker et al., 2023, Rangamani et al., 2023], although this should be further investigated by future experimentation.

# A.5 Synthetic Data Generation Formulation

Our synthetic data generation can be formally representated as a probabilistic context-sensitive grammar (PCSG). Mathematically, we parameterize our vanilla PCSG (without POS ambiguity) as follows:

$$\mathbf{G} = (N, \Sigma, P, S, \alpha, v)$$

where  $N=\{S,Q,Q_N,Q_A,P_N,P_A\}$  is the set of nonterminal symbols,  $\Sigma=\{N_{init},A_{init},N_r,A_r,C\}$  is the set of terminal symbols, S is the starting point (and notationally also represents sequence), and  $\alpha,v$  characterize the sampling probability distribution of our terminal symbols. Our production rules P are

$$F 
ightarrow egin{cases} S \ Q_N \ P_N \\ S \ Q_A \ P_A \end{cases}$$
 with eq. prob.

$$S 
ightarrow egin{cases} N_{init} & C & A_{init} \\ C & A_{init} & N_{init} \end{cases} \quad ext{with eq. prob.} \qquad \qquad Q 
ightarrow egin{cases} Q_N \\ Q_A & \text{with eq. prob.} \end{cases}$$
  $Q_N 
ightarrow N_r \qquad \qquad Q_A 
ightarrow A_r \\ P_N 
ightarrow A_r & A_r & P_A 
ightarrow A_r & N_r & N_r \end{cases}$ 

with terminal symbols sampled from

$$\begin{split} N_{init} \sim & \operatorname{Zipf}\left(\alpha, 0, \frac{v}{2} - 1\right) & A_{init} \sim \operatorname{Zipf}\left(\alpha, \frac{v}{2}, v - 1\right) & C \rightarrow v \\ N_r \rightarrow N_{init} & A_r \rightarrow A_{init} & \end{split}$$

 $N_{init}$  captures a specific token that corresponds to a token and all references to  $N_r$  use this token exactly, enforcing strict consistency.

Note our sampling distribution Zipf is a truncated Zipfian parameterized by the tuple  $(\alpha, s, e)$  with a probability mass function of

$$\mathbb{P}(X=k) = \frac{k^{-\alpha}}{H(\alpha, e-s)} \text{ for } k=s, s+1, \dots, e, \text{ where } H(\alpha, n) = \sum_{k=1}^{n} k^{-\alpha}$$

We select tokens for <noun>  $\in \left\{0,1,\dots \frac{v}{2}-1\right\}$  and <adj>  $\in \left\{\frac{v}{2},\frac{v}{2}+1,\dots v-1\right\}$ . Thus, given a particular vocabulary size v and Zipf parameter  $\alpha$ , <noun>  $\sim$  Zipf  $\left(\alpha,0,\frac{v}{2}-1\right)$  and <adj>  $\sim$  Zipf  $\left(\alpha,\frac{v}{2},v-1\right)$ . To add further control to this setting, we introduce the parameter  $\varepsilon$  to describe ambiguity in the solution - that is, a proportion of  $\varepsilon$  tokens in each of n=10 bins grouped by probability mass do not have a fixed POS but instead may be a noun or adjective with equal likelihood.

Note that when  $\alpha=0$ , this distribution degenerates into  $\mathrm{Unif}(s,e)$  and when  $\varepsilon=0$ , each token has a fixed identity.

#### A.6 Toy Model

We employ a 6-layer BERT model across the synthetic setting experiments. Experiments were performed with an MLM as far less prior work has examined syntactic tasks with autoregressive models. Structure is much more difficult to intuit in autoregressive models as they are only exposed to an ordered subset of the tokens in a sentence. This model has 1 attention head per layer, 64-dimensional hidden dimensions, 128-dimensional intermediate representations, and tied weights for the embedding and unembedding layers. We optimize model parameters with AdamW with a learning rate of  $5 \times 10^{-5}$  [Loshchilov and Hutter, 2019]. We chose a thin and long representation to examine how representations evolve after each attention operation (for better granularity). The hidden dimension sizes were decided per a minimax strategy, i.e. this representation dimensionality was the smallest such that we achieved near perfect accuracy on a validation set for the downstream task. Future work should better examine the effect of representation size on in-context vs. in-weights learning.

# A.7 Performance by Token Decile

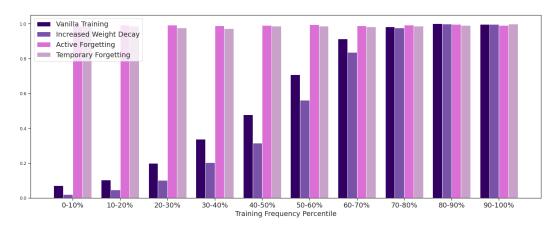


Figure 9: Increased weight decay has little/no effect on the failure of the structural ICL strategy (we increase weight decay from 0.01 to 0.1). In contrast, active temporary forgetting boosts rare token validation accuracy significantly, as seen in the tail of the distribution. Parameters are  $v=10000, \varepsilon=0.10, \alpha=1.5$ 

We find that on highly skewed distributions, the tail of the distribution suffers immensely due to undertraining. This phenomenon cannot be rectified by Singh et al. [2023]'s method of promoting asymptotic ICL. However, we find that both active forgetting and temporary forgetting correct this behavior to boost performance on tail tokens in skewed distributions from near-zero to near-perfect levels.

# A.8 Ambiguity ( $\varepsilon$ ) Experiments

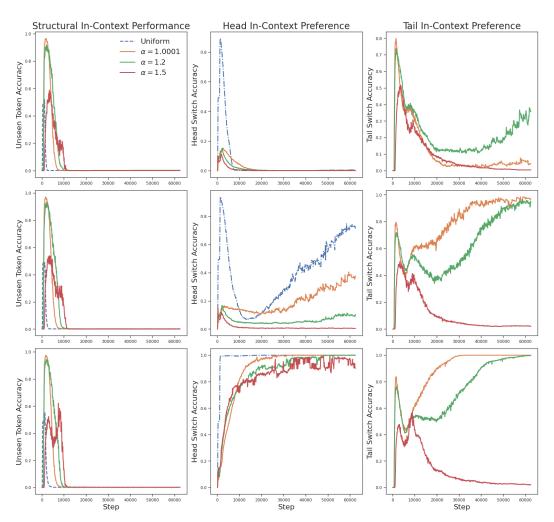


Figure 10: (Top)  $\varepsilon=0.01$ , (Middle)  $\varepsilon=0.10$ , (Bottom)  $\varepsilon=0.50$ . Overall in-context strategy is dependent by amount of ambiguity in the labels. With 50% of the tokens as ambiguous, all unambiguous tokens use an in-context strategy; with 10%, there is a mixed strategy dependent on where in the distribution the example is; with 1%, almost unambiguous tokens use a memorized strategy. The vocab size is v=10000

In all of our ambiguity experiments, structural ICL is transient (even whe 50% of tokens are ambiguous). The ambiguity parameter significantly alters the models overall strategy. With a low ambiguity parameter, the model prefers memorization (IWL strategy) of umambiguous tokens and with a high ambiguity parameter, the model prefers an ICL strategy. Across all ambiguity parameters, there is a difference in tail and head behavior.

# **A.9** Vocabulary Size (v) Experiments

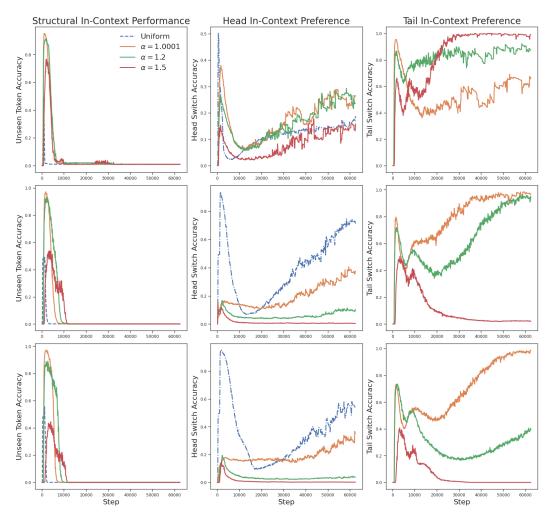


Figure 11: (Top) v=1000, (Middle) v=10000, (Bottom) v=20000. The strength of an in-context solution depends on the interaction between vocabulary size v and skewedness of the distribution  $\alpha$ . Too small of a vocabulary size (i.e. v=1000) encourages more memorization in general but fixes performance in  $\alpha=1.5$  setting. The ambiguity is  $\varepsilon=0.10$ .

In all of our vocabulary experiments, structural ICL is transient. As expected, we find that vocabulary size has a similar effect to the skewedness of the distribution. That is, increasing the vocabulary without bound would lead to poor tail ICL performance. Too small of a vocabulary size seems to increase ICL among very skewed distributions but decrease ICL among all other distributions.

# A.10 Embedding Analysis

We perform qualitative analyses on the embeddings produced by vanilla training, active forgetting, and temporary forgetting in order to better understand how these training regimens impact model representations. These analyses, consisting of principal component analysis (PCA) and probing for POS, are located in Appendix A.11.

After vanilla training, the learned embeddings cluster according to their POS, far from the distribution of randomly-initialized tokens. We train a linear probe on these learned embeddings, and find that it can almost perfectly partition nouns and adjectives. Note that the disappearance of structural ICL occurs at the same time as the probe achieves above-random POS probing (i.e. memorization).

As expected, we do not see any structure in the embeddings produced after active forgetting. As such, a linear POS probe trained on these embeddings never achieves above random chance throughout training. The embedding distribution looks quite similar to the random initialization distribution, indicating that no information has been encoded in these embeddings.

Finally, the temporary forgetting setting reflects aspects of both vanilla training and active forgetting; that is, the head of the token distribution learns to partition nouns and adjectives whereas the tail of the distribution does not learn any structure. The tail embeddings much more closely resemble the initialization distribution with temporary forgetting than with vanilla training. This results in a unseen token generalization in addition to memorized information.

#### A.11 Principle Component Analysis of Embeddings

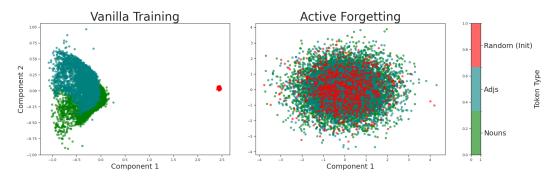


Figure 12: Vanilla training imposes structure on the adjectives and nouns such that randomly initialized (unseen) tokens are out-of-distribution whereas active forgetting embeddings resemble the initial distribution. Parameters used are v = 10000,  $\alpha = 1.0001$ ,  $\varepsilon = 0.10$ .

We find that while vanilla training results in embeddings that lie on a manifold, active forgetting results in embeddings that look similar to the initial distribution. This helps motivate our use of temporary forgetting as we would like to preserve embedding structure. Moreover, note that in the above figure we use  $\alpha=1.0001$  and PCA whereas in Figure 1 (Bottom Right), we use  $\alpha=1.5$  and T-SNE. The tail tokens in the higher skew distribution see fewer gradient updates and thus resemble the randomly initialized (unseen) tokens more (in addition to T-SNE likely being a better visualization tool).

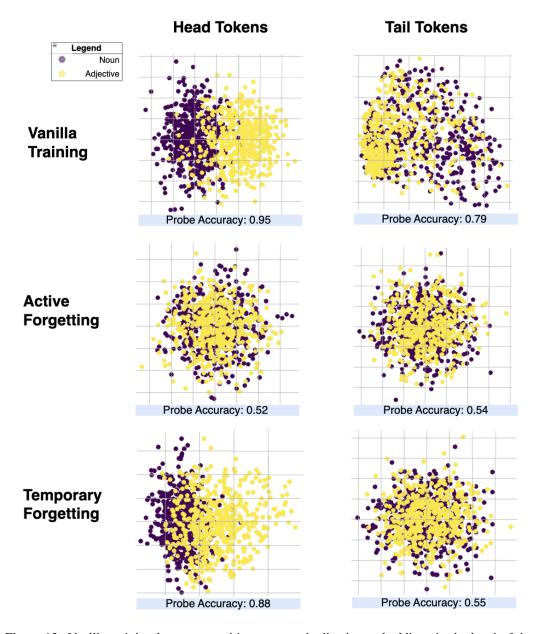


Figure 13: Vanilla training learns to partition noun and adjective embeddings in the head of the distribution, and some structure in the tail. Active forgetting learns no separation between noun and adjective embeddings. Temporary forgetting learns structure in the head of the distribution and no structure in the tail of the distribution. Parameters used are  $v=10000, \alpha=1.2, \varepsilon=0.10$ .

# A.12 Singh et al., 2023 vs. This Work

#### Temporary forgetting preserves structural ICL, solving tail performance on highly skewed distributions 1.00 1.00 Vanilla Training Singh Et Al., 2023 Solution 0.75 0.75 Temporary Forgetting Accuracy 0.50 0.50 0.25 0.25 0.00 0.00 ż 3 4 5 6 8 9 10 1 3 4 5 6 8 9 1 Training Frequency Decile Training Frequency Decile

Figure 14: While Singh et al. 2023 discovers the transience of conditional ICL, we discover the transience of *structural* ICL (see definition in main reply). This disappearance of structural ICL results in poor performance on undertrained and unseen tokens, which is a well-documented phenomenon in various large language models (Rumbelow & mwatkins, 2023; Land et al., 2024). We recreate this issue in our toy setting by enforcing a skewed distribution (Zipfian  $\alpha=1.5$ ), and show that Singh et al.'s solution of L2 regularization, which "eliminate[d] ICL transience entirely" in their setting does *not* eliminate structural ICL transience. In contrast, temporary forgetting preserves structural ICL, resulting in near-perfect performance on tail tokens.

### A.13 Chan et al., 2022 vs. This Work

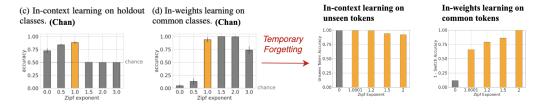


Figure 15: Chan et al., 2022 (Figure 6, c and d above) finds that "there is a sweet spot where both in-context learning and in-weights learning can be maintained at a high level in the same model" (Zipf exponent = 1 for their training regime). They note that this is "important and useful for a model", and suggest that one might even engineer data distributions to evoke this behavior in models. Additionally, Singh et al. 2023 states "future work could investigate other factors that may restore co-existent ICL and IWL, even asymptotically." We achieve precisely this: temporary forgetting engenders a *sweet spot* for any data distribution, even those more skewed than Zipfian  $\alpha=1$ . This enables us to endow a model trained on any skewed distribution with a useful behavior that we have only observed in language-like settings. The bars colored yellow show data distributions where both ICL and IWL are maintained at high levels in Chan et al., 2023 versus our work.

#### A.14 Other Random Distribution Generalization

Note that while we define structural in-context learning as free from reliance on any *encoded semantic information*, it is important to note that this does not mean that structural in-context learning assumes *no* geometry of the space. In fact, this would be practically impossible to achieve because connectionist networks function in a geometric space and take advantage of orthogonality, translation, scaling, etc. If we cannot make assumptions about the distribution from which the data is sampled, then we deprive our networks of their toolbox. Still, we test on random sampling distributions for the embeddings other than our initialization distribution. Namely, we test on a uniform distribution from 0 to 1 and a large normal distribution with mean of 5 and standard deviation of 5.

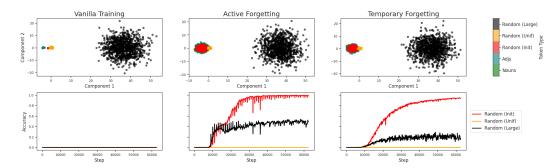


Figure 16: Vanilla training fails on all random tokens, whereas active/temporary forgetting succeed on the random distribution of initialization. Active and stop forgetting do not generalize to arbitrary random distributions, although show some generalization to normal distributions with large means and variances.

# A.15 Required Compute for Experiments

We employed compute resources at a large academic institution. We scheduled jobs with SLURM. For our naturalistic experiments, each MultiBERT seed required 24 separate runs (one per tested checkpoint at a particular timestep), which totaled  $\approx 100$  hours on an RTX A5000 with 24 GB of GPU memory. Over 3 seeds, this was  $\approx 300$  hours of GPU usage. For our synthetic setting, the vanilla training required 64 separate runs (one per hyperparameter combination of vocab size, ambiguity, and sampling distribution), which totaled  $\approx 250$  hours of RTX A5000 usage. Likewise, our active forgetting and temporary forgetting interventions took a similar amount of GPU usage. Therefore, in total, our GPU usage for all synthetic experiments summed up to about 750 hours. We ran experiments mostly in parallel with SLURM to iterate quickly. Compute was a significant limitation for the development time and informed our development of training interventions in a synthetic setting. In total, our GPU usage was significantly higher than the reported number due to various failed/modified experiments. The total compute likely was around 20,000 GPU-hours on RTX A5000s, although this is a rough estimate.