Exploration with Principles for Diverse AI Supervision

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Abstract

Training large transformers using next-token prediction has given rise to groundbreaking ad-1 vancements in AI. While this generative AI approach has produced impressive results, it heavily 2 leans on human supervision. Even state-of-the-art AI models like ChatGPT depend on fine-3 tuning through human demonstrations, demanding extensive human input and domain expertise. 4 This strong reliance on human oversight poses a significant hurdle to the advancement of AI 5 innovation. To address this limitation, we propose a novel paradigm termed Exploratory AI 6 (EAI) aimed at autonomously generating high-quality training data. Drawing inspiration from 7 unsupervised reinforcement learning (RL) pretraining, EAI achieves exploration within the 8 9 natural language space. We accomplish this by harnessing large language models to assess the novelty of generated content. Our approach employs two key components: an actor that 10 generates novel content following exploration principles and a critic that evaluates the generated 11 content, offering critiques to guide the actor. Empirical evaluations demonstrate that EAI sig-12 nificantly boosts model performance on complex reasoning tasks, addressing the limitations of 13 human-intensive supervision. 14

15 **1** Introduction

16 Training large transformers [41] using next token prediction has led to substantial AI 17 advancements, as evidenced by the groundbreaking results they have produced [33, 30]. 18 While this generative AI approach has yielded remarkable AI results, it heavily relies 19 on human supervision. For instance, state-of-the-art AI models including ChatGPT [33] 20 along with a range of other models [7, 14, 9, *inter alia*], rely on fine-tuning through 21 human demonstrations, demanding significant human involvement and domain expertise.

This reliance on extensive human su-22 pervision presents a substantial chal-23 lenge since human supervision re-24 quires domain expertise, is time con-25 suming, and is tedious. Moreover, hu-26 mans can struggle to provide reliable 27 supervision in highly specialized do-28 mains. For instance, ChatGPT pos-29 sesses a greater depth of knowledge 30 than the average human, which makes 31 it difficult to rely on humans to pro-32 vide supervision for ChatGPT. More-33 over, while our most advanced AI sys-34 tems have made significant strides, 35 they still necessitate thorough, human-36 guided processes to enhance their abil-37



Figure 1: Test accuracy on mathematical reasoning benchmark GSM8K. Baselines include Vicuna, supervised finetuning Vicuna on training set (denoted as SFT), and supervised finetuning Vicuna on rejection sampled model generated diverse solutions on training set (denoted as RFT). Our Exploratory AI (EAI) substantially outperform all baselines.

ity to answer factual or mathematical queries [20]. Yet, when it comes to more intricate and mission-

³⁹ critical tasks, such as navigating complex tax or law regulations, these challenges will demand even

⁴⁰ more specialized expertise and effort.

Prior works attempt to explore alternatives to human supervision, by using AI supervision instead. 41 For example in mathematical reasoning, these studies propose sampling self generated solutions for 42 human curated questions from large language models and employ techniques like rejection sampling, 43 along with other techniques, to curate training data for the model [8, 29, 2, 16, 48, 45, inter alia]. 44 While learning from such sampled content proves effective, a significant challenge persists: the 45 sampled contents often lack the necessary diversity, resulting in a rapid saturation of the learning 46 process [45, 48]. Moreover, the sampling approach has been confined to solutions exclusively, relying 47 on human-curated questions, thus imposing constraints on the diversity of generated data. 48

To tackle these limitations, we propose a novel approach for using AI models to autonomously 49 generate *diverse* data for learning purposes. This concept draws inspiration the APT algorithm [21] 50 designed for unsupervised RL pretraining [36, 17, 32]. RL pretraining studies exploring in a reward-51 free environment to develop skills for quickly maximize various downstream rewards. APT allows 52 training RL agent to learn skills by autonomously explore reward free environment based on evaluating 53 novelty of encountered states using particle based entropy estimation [3, 35]. Adapting APT to large 54 language models presents several challenges, including computational complexity and the difficulty 55 of learning reward functions and exploration policies [13, 8]. Rather than relying on traditional RL 56 techniques, we harness the unique capabilities of large language models, such as their ability to 57 learn from context and follow instructions. In essence, we use them to perform the roles of both 58 a reward function and an exploration policy. Our approach, which we term Exploratory AI (EAI), 59 involves two key components: an actor and a critic. The actor is responsible for generating novel 60 content in natural language, while the critic evaluates this generated content and provides critiques 61 62 to guide the actor's exploration. By evaluating the novelty of the generated contents, our method allows for effective exploration in the rich space of natural language. EAI can generate diverse data 63 independently of human intervention. This makes it more scalable and automated, positioning it as 64 a preferable alternative to methods like supervised finetuning or rejection sampling that depend on 65 data curated by humans. Furthermore, EAI provides an interpretable window into the behavior and 66 knowledge of the model. It sheds light on how well the model possesses knowledge and its reasoning 67 behind generating novel questions. One can look at generations and their corresponding evaluations 68 which provide valuable insights about how model generates and evaluates. 69

We evaluate our approach on mathematical reasoning benchmarks GSM8K [8] and MATH [15],
EAI substantially improves performance on challenging reasoning tasks, outperforming both human supervision and AI supervision baselines. In contrast to human supervision, our approach is autonomous and more scalable. When compared to prior state-of-the-art AI supervision baselines including RFT [45] and WizardMath [24], our method provides a straightforward yet highly effective solution for the generation of high-quality and diverse data.

Our contributions are two-fold: (a) In contrast to the predominant reliance on human supervision, our novel approach, EAI, leverages the capabilities of large language models to autonomously generate diverse high-quality training data. It achieves this by harnessing these models for selfguided exploration, inspired by unsupervised reinforcement learning pretraining. (b) We conduct an extensive series of experiments to systematically assess the effectiveness of EAI. Our results show that EAI substantially outperform prior human supervision and AI supervision state-of-the-arts, and significantly improve model performance.

2 Exploratory AI for Diverse AI Supervision

We present our approach for harnessing AI models to create AI supervision, in order to address the
 reliance on extensive human supervision.

Our method employs a dynamic interplay between generation and evaluation. This concept draws
 inspiration from unsupervised RL pretraining (URL) [17] and particularly the APT algorithm [21]. RL
 pretraining studies exploring in a reward-free environment to develop skills for quickly maximizing
 various downstream rewards. APT allows training RL agent to learn skills by autonomously exploring
 a reward free environment based on evaluating novelty of encountered states using particle based

entropy estimation [3, 35].

Adapting APT directly to large language models presents several challenges, including grappling with computational complexity and the difficulty of learning reward functions and exploration

policies [13, 8]. In response, we propose Exploratory AI (EAI), a novel approach that circumvents



Figure 2: Generating diverse data in the Exploratory AI Framework. In the diagram, we demonstrate how the actor generates diverse content by conditioning on samples from the replay buffer and exploration principles. These principles include rephrasing question, coming up a novel topic, restructuring question, and coming up a new scenario, we provide examples associated with the principles to guide exploration. The actor's input and its generated output undergo evaluation by the critic. The critic assesses the novelty of the generated data; when the evaluation is favorable, the data is stored in the replay buffer. In cases where the evaluation does not meet the criteria, the critic provides critiques to guide the actor. The replay buffer can be initialized with a pre-existing human-created dataset (*e.g.*, GSM8K training set) or can remain empty for starting from scratch with zero-shot exploration.

the need for direct reinforcement learning (RL) by harnessing the power of large language models for exploration. Our method explore the natural language space by employing these language models to assess the novelty of generated content and guide the exploration process. Our approach consists of two key components: an "actor" responsible for generating novel content and a "critic" that evaluates the actor's explore the natural for the explorement of the explorement of the explorement.

⁹⁹ the actor's outputs and provides feedback to guide further content generation.

Concretely, we instruct the actor to generate content that diverges from samples from the replay buffer. 100 The replay buffer can be initialized with a pre-existing human-created dataset (e.g., GSM8K training 101 set) or can remain empty for zero-shot exploration. Similar to APT, we found having pre-existing 102 samples accelerates learning and encourages the actor to have more long term exploratory behaviors. 103 We then instruct the critic to assess the actor's outputs and provides critiques. This feedback loop 104 guides the actor in refining and enhancing its content. This iterative process continues until it reaches 105 106 a predefined maximum number of iterations, and the resulting outputs are stored in a dataset. The data can then be used for finetuning AI models. 107

We equip both the actor and critic with a curated set of guiding principles to facilitate the generation 108 and evaluation of diverse questions. These principles include rephrasing question, coming up a novel 109 topic, restructuring question, and coming up a new scenario, we provide examples associated with 110 the principles to guide exploration. While it's theoretically possible to provide all these principles to 111 the model, in this study, we opt to a more controlled approach. To balance the quantity of generated 112 data for each principle, we uniformly sample one principle at a time and input it to both the actor and 113 critic. The actor is instructed to follow the principle (e.g., restructuring the question) during question 114 generation. Similarly, the critic's role is to evaluate the diversity, considering the selected principle. 115 It's worth noting that the critic's principle is worded slightly differently from the exploration principle; 116 for a detailed list, please refer to Appendix A. Our method is shown in Figure 2 and the algorithm is 117 shown in Algorithm 1. 118

Actor prompt

You are an AI assistant to help with come up a novel question that is different from the example questions given to you. The question should come with a correct solution. Please follow the given principle in generating the question. {**principle**}

119

Critic prompt

You are an AI assistant to help with evaluating the novelty of generated question and the correctness of its answer. A question is not acceptable if its answer is incorrect. You should provide concrete suggestions to improve the question. Explain your reasoning step by step and output final evaluation on novelty and correctness at the end. Follow the given principle on evaluating the novelty. **{principle}**

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Principles for exploration

You can rephrase any given question:

Question: Joy can read 8 pages of a book in 20 minutes. How many hours will it take her to read 120 pages? Question (rephrase): How many hours will Joy need to read 120 pages if she can read 8 pages in 20 minutes? **You can come up with a different topic:**

Question: Jack is stranded on a desert island. He wants some salt to season his fish. He collects 2 liters of seawater in an old bucket. If the water is 20% salt, how many ml of salt will Jack get when all the water evaporates?

Question (topic): Samantha is designing a circular garden in her backyard. The garden has a diameter of 8 meters. She wants to build a path around the garden that is 1 meter wide. What is the area of the path, in square meters, that Samantha will need to pave with stones or concrete?

You can change the structure of any question:

Question: Dan owns an ice cream shop and every sixth customer gets a free ice cream cone. Cones cost \$2 each. If he sold \$100 worth of cones, how many free ones did he give away?

Question (restructured): Dan owns an ice cream shop and every sixth customer gets a free ice cream cone. Cones cost x each. If he sold 100 worth of cones, how many free ones did he give away? If we know the answer is 10, what is the value of x?

You can come up with a different scenario:

Question: Ed has 2 dogs, 3 cats and twice as many fish as cats and dogs combined. How many pets does Ed have in total?

Question (scenario): Sarah owns 4 bicycles, 2 skateboards, and three times as many pairs of rollerblades as bicycles and skateboards combined. How many wheeled sports equipment items does Sarah have in total?

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Exploratory AI has several attractive properties as an approach for facilitating AI supervision in language models:

 EAI can generate diverse AI supervision for learning, independently of human input, making it more scalable compared with supervised finetuning or rejection sampling based on human curated data.

 EAI provides an interpretable window into the behavior and knowledge of the model. It sheds light on how well the model possesses knowledge and its reasoning behind generating novel questions. One can look at generations and their corresponding evaluations which provide valuable insights

about how model generates and evaluates.

EAI's versatility allows for a fusion of the best aspects of supervised finetuning and prompting.
 Users can prompt the model to focus on certain topics or aspects by directing actor and critic with
 different prompting strategies.

EAI demonstrates its effectiveness by excelling in mathematical reasoning tasks, as we will
 demonstrate in our experiments. Moreover, its capabilities are not limited to mathematics; it
 holds promise for a broad spectrum of language-related tasks in principle.

In empirical experiments, we will evaluate the utility of EAI for mathematical reasoning and analysis
 its effectiveness.

139 3 Setting

We evaluate our method on the mathematical reasoning tasks, and achieve better results that EAI
 largely improve results and significantly outperforms prior state-of-the-arts.

Benchmarks. We evaluate our method on the mathematical reasoning tasks GSM8K. This benchmarks exams model's mathematical reasoning capabilities, we finetune model on the training split, and evaluate model on the test split. The GSM8k dataset includes around 7,500 training and 1,319 test math problems for high school-level students, involving basic arithmetic operations. Problems typically require 2 to 8 steps for a solution. The MATH dataset comprises 7,500 training and 5,000 challenging test problems from prestigious math competitions (AMC 10, AMC 12, AIME) covering

Algorithm 1	Exploratory	AI for diverse	AI supervision.
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Required: One (or two) large language models M for actor and critic.
Replay Buffer B, empty or optionally initialized with pre-existing data.
Initialize
for $i = 1$ to max iterations do
Randomly sample data points from B
Use preassigned principle or sample one principle.
for $i = j$ to max rounds do
Prompt the actor with the principle to generate content (a question and its answer) that in the same domain but diverge from the sampled inputs (questions and answers) sampled from <i>B</i> Prompt the critic with the principle to evaluate the diversity of generated question and correctness of answer, and decide whether to accept
if Accepted then
Save generated question and answer to B
break
else
Continue to prompt actor with the critique as additional input
end if
end for
end for

various academic domains, including prealgebra, algebra, number theory, counting and probability,
 geometry, intermediate algebra, and precalculus.

Baselines. We compare our approach with (a) Base model including Vicuna 7B, 13B, and 30B [7]. 150 Vicuna is LLaMA2 finetuned on user conversations shared online (ShareGPT). We use Vicuna as 151 base model for all baselines and our method; (b) Supervised finetuning (SFT) on training set of the 152 original GSM8K or MATH, in which a language model is finetuned on human written exemplars of 153 questions-answers pairs. SFT has been widely used in prior works for improving language models 154 mathematical reasoning [19, 40, 30, *inter alia*] and following user intention [14, 9, *inter alia*]. We 155 also compare with WizardMath [24] which does SFT on ChatGPT annotated questions and solutions, 156 as well as MAmmoTH [47] which uses GPT4 annotated solutions; (c) Rejection sampling finetuning 157 158 (RFT) [45] which applies supervised finetuning on rejection sampled model generated data. We provide baseline scores for SFT and RFT from both their original papers and our implementations 159 using Vicuna, ensuring a fair and comprehensive comparison; (d) Proprietary models including 160 GPT-4 [30], ChatGPT [33], and Claude2 [1]. All baselines are evaluated by prompting them to output 161 step by step reasoning followed by final answers [44]. 162

163 Generated data size. We sample roughly the same amount of data for each principle outlined 164 in Section 2. To optimize computational cost, we have set the number of interaction rounds in Algorithm 1 to a maximum of two. Our preliminary experiments revealed that this two-round 165 interaction is typically sufficient for the actor to produce high-quality and diverse data. For each of the 166 four principles - 'rephrase question', 'introduce a new topic', 'restructure the question', and 'introduce 167 a new scenario' – we generate approximately 25,000 samples for GSM8K and approximately 15,000 168 samples for MATH. The generation on 8 A100 80GB GPUs take from 40 to 200 hours depending on 169 the model size and the specific principles applied. 170

171 **4 Results**

Benchmark. In Table 1, we present the results of pass@1 (%) on GSM8K and MATH, showcasing 172 the performance of various models across different supervision types and model sizes. Our approach, 173 denoted as Vicuna + EAI, is compared with Vicuna and Vicuna + RFT, which serve as the closest 174 baselines. Notably, our method outperforms Vicuna in all scenarios. For instance, in the 7B parameter 175 setting, our model achieves 52.9% and 9.5% on GSM8K and MATH, respectively, surpassing 176 Vicuna's scores of 24.4% and 2.6%. This trend continues across larger model sizes and different 177 datasets. Furthermore, compared to Vicuna + RFT, our approach maintains a consistent advantage, 178 demonstrating the effectiveness of our self AI supervision method in improving model performance 179

Table 1: Results of pass@1 (%) on GSM8k and MATH. In this study, to ensure equitable and cohesive evaluations, we report the scores of all models under the same settings of greedy decoding. * denotes original LLaMA2 based SFT and RFT. Bold numbers are the absolute improvement of EAI over RFT which serves as prior state-of-the-art and the closet baseline.

Model	Supervision	Data	Params	GSM8K	MATH
GPT-4	-	-	-	92.0	42.5
ChatGPT	-	-	-	80.8	34.1
Claude 2	-	-	-	88.0	32.5
			8B	16.2	14.1
Minerva	-	-	62B	52.4	27.6
			540B	58.8	33.6
			7B	14.6	2.5
LLaMA2	-	-	13B	28.7	3.9
			35B	42.2	6.4
SFT*	Human+LLaMA	7.517	7B	41.6	-
		/.JK	13B	50.0	-
RFT*	Human+LLaMA	47K	7B	47.5	5.6
			13B	54.8	9.6
	Human+ChatGPT	96K	7B	54.9	10.7
WizardMath			13B	63.9	14.0
			70B	81.6	22.7
	Human+GPT4	260K	7B	51.7	31.2
MAmmoTH			13B	61.7	36.0
			70B	76.7	44.2
Vicuna			7B	24.4	2.6
	-	-	13B	39.8	5.8
			30B	47.5	7.7
SFT	Human	7.5K	7B	42.0	4.6
			13B	50.8	7.9
DET	Human+Vicuna	48K	7B	48.1	5.9
Kf I			13B	56.3	9.3
EAI	Humon - Viewno	191	7B	52.9 (+4.8)	8.6 (+2.7)
LAI	riuman+vicuna	40 N	13B	60.5(+4.2)	11.4(+2.1)

on these tasks. These results highlight the significant improvements our method brings to the table 180 and its competitive edge in natural language understanding and generation tasks. 181

Comparison of diversity. We evaluate EAI in terms of the diversity of generated data. 182 We compare RFT and EAI in terms 183 of the submodularity diversity gain [4, 184 27]. This metric serves as an indicator 185 of the extent to which the generated 186 data contribute to the overall diver-187 sity of the dataset. A higher diversity 188 gain suggests that the newly generated 189 questions exhibit greater dissimilarity 190 from the existing dataset. We measure 191 the gain over GSM8K training set by 192 varying the amount of generated con-193 tent. We use OpenAI GPT embed-194 ding text-embedding-ada-002 to 195 encode the data. The results depicted 196 in Figure 3 clearly demonstrate that 197



Figure 3: Comparison of diversity gain by adding generated data to GSM8K training set. EAI achieves higher diversity than other baselines.



Figure 4: Data scaling on GSM8K. Shown are GSM8K accuracy with different amount of generated data. EAI generates high quality data for learning and scales well with data.

EAI consistently outperforms RFT in terms of diversity, thereby providing a more diverse set of generated data

Effect of sampled inputs. The Table 2 presents the results of an experiment examining the impact of varying the number of samples on GSM8K and MATH. As the number of samples increases from 0 to 8, we

a bit in number of samples increases from o to 6, we
 observe a steady incremental improvement on both
 GSM8K and MATH. On GSM8K, the performance
 rises from 50.1 to 52.9. On MATH, the effect is more
 pronounced. These results suggest that increasing
 the number of samples has a positive effect on both
 GSM8K and MATH, highlighting the significance of
 conditional input size in this experimental context.

Table 2:	Effect	of different	number	of	sam-
ples from	n replay	buffer.			

Number	0	1	4	8
GSM8K	50.1	50.8	51.9	52.9
MATH	6.6	7.1	7.5	8.6

Scaling with generated data. We assess the performance of EAI in terms of sample efficiency on 210 the GSM8K dataset. Our primary focus lies in understanding how the results evolve in response 211 to varying amounts of generated data. Sample efficiency holds paramount importance, given that 212 autoregressive data generation is inefficient. Enhanced sample efficiency broadens the practical 213 utility of our approach in real-world applications. The results depicted in Figure 4 clearly illustrate 214 a significant advantage for EAI over the previous state-of-the-art RFT. Notably, as more data is 215 employed, RFT exhibits improved performance, but its sample efficiency lags behind EAI by a 216 substantial margin. At just 16K data points, EAI outperforms RFT's performance at 48K data points, 217 achieving more than a 3x higher level of sample efficiency. 218

rephrase	new topic	restructure	new scenario	GSM8K	MATH
1	1	✓	1	52.9	8.6
X	1	1	1	48.8	7.1
1	×	1	1	49.7	7.8
1	1	X	1	48.9	6.9
1	1	1	X	49.5	7.5

Table 3: Effect of different exploration principles on GSM8K and MATH.

Evaluating the effect of exploration principles. The results of varying exploration principles, as shown in Table 3, reveal some interesting insights. When all principles are in place (\checkmark for rephrase, new topic, restructure, and new scenario), the model performs at its best on GSM8K and MATH. This suggests that using all principles simultaneously leads to the most favorable outcomes. Among the principles, the most critical ones appear to be "rephrase" and "restructure", as seen when one of them is removed (\bigstar). Without "rephrase" the performance drops on both datasets, emphasizing that the ability to rephrase and generate diverse content is crucial. Similarly, the omission of "restructure"



Figure 5: Performance on GSM8K with different amount of human annotated data. EAI performs well even without human annotation and scales well with more human provided annotations.

leads to a significant drop in MATH scores, highlighting the significance of introducing novel question-structuring approaches for solving more challenging problems.

Scaling with human annotation size. Figure 5 illustrates the results obtained when utilizing 228 varying amounts of human annotation data from the GSM8K training set. We employ three different 229 approaches in our experiments: SFT which directly finetunes the base model, Vicuna-7B, on the 230 provided data. RFT which leverages the provided data to perform rejection sampling from the model. 231 EAI which utilizes the provided data to initialize a replay buffer and explore new content for training. 232 The results consistently demonstrate that EAI significantly outperforms all the baseline methods 233 across various levels of human annotation data, underscoring its efficacy in generating high-quality 234 training data. Remarkably, our experiments reveal that EAI performs admirably even in the absence of 235 any human annotations, hinting at the potential to entirely eliminate the need for human intervention 236 in the process. 237

238 5 Related Work

Transformers [41] trained using next token prediction have gave rise to many state-of-the-art AI 239 systems [33, 30]. The remarkable AI results achieved with this generative AI approach heavily 240 hinge upon the availability of diverse and high-quality data. For instance, state-of-the-art AI models 241 including ChatGPT [33] and GPT4 [30] along with a range of other open source models such 242 as Vicuna, Koala, and Dolly [9, 14, 7, *inter alia*], require extensive finetuning through human 243 demonstrations. This process involves human conversations with ChatGPT or written demonstrations, 244 demanding significant human involvement and domain expertise. Previous research has explored 245 various avenues to enhance performance and sample efficiency, as well as alternative sources of 246 supervision. To align with human preferences, there has been active research into developing simple 247 248 algorithms for learning from human preferences [23, 46, 10, 40, inter alia]. In contrast to human 249 demonstrations or feedback, another line of work explores the utilization of environmental feedback, such as unit test errors [18, 6, 34], which has demonstrated improved results in coding tasks. Some 250 works explore using LLMs to provide AI supervision based exploration techniques for applications 251 in solving games [11, 22, 42] and demonstrate improved results. Furthermore, some prior research 252 leveraged proprietary APIs to indirectly obtain high-quality human data, enhancing model capabilities 253 in areas like instruction following [43, 39, 14, 7] and mathematical reasoning [24, 26, 47, inter alia]. 254 Another line of research explores the use of models to supervise themselves [38, 25, 16, 2, 45], 255 yielding improved results in reasoning tasks and alignment with human preferences. Our work 256 focuses on generating diverse and high-quality data using AI models and we demonstrate applying 257 our proposed approach to enhance open-source models by having them self-generate learning data. 258 Our approach's exploration technique is related to unsupervised RL based exploration [36, 37, 21, 5, 259 32, 28, 12, 31, *inter alia*], however, our method does not require training RL agent. Additionally, some 260 works have delved into more detailed forms of human supervision [20], demonstrating that LLMs 261 benefit more from step-by-step process-based supervision than sparse outcome-based supervision. 262 Our research uniquely centers on the data dimension, with a specific emphasis on harnessing AI 263

models to generate diverse high -quality AI supervision. To this end, we introduce an actor-critic based approach for automating the exploration process.

266 6 Conclusion

In this work we propose an approach to automatically generate diverse, high-quality data from AI models. Our approach Exploratory AI consists of prompting an actor model to generate diverse contents that are different from existing contents, and using a critic model for evaluating the novelty of generated data and providing critiques to guide the exploration process. Experimental evaluations confirms the effectiveness of EAI, demonstrating its capacity to generate diverse content and substantially enhance model performance on GSM8K and MATH datasets.

Limitations and Future Work. Although our method achieves state-of-the-art results using AI supervision, it does have some limitations that need to be addressed:

- Our approach, while achieves substantial improvement with open source models, lags behind results achieved using supervision by more powerful models such as ChatGPT.
- This work focuses on evaluation on mathematical reasoning domains. It worth applying EAI to more diverse applications.

In terms of future prospects, our approach of generating diverse content with AI models opens up interesting possibilities, such as extending EAI to evaluate novelty across the entire data buffer, employing either a brute force approach (evaluating all data through a critic) or employing embedding similarity search techniques. Moreover, there's potential in extending EAI to incorporate multiple actor and critic models, or in experimenting with various strategies to enhance exploration. It would also be interesting to apply our method to proprietary APIs to source even more diverse and higher-quality data.

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419 A Prompt

The critic's principle is based on the exploration principle but is worded slightly differently from the actor's exploration principle, in order to tell critic what kind of new questions are diverse and acceptable. The critic will use the principle to evaluate diversity of questions and evaluate the correctness of answer.

Principles for critique

A different topic is acceptable:

Question: Jack is stranded on a desert island. He wants some salt to season his fish. He collects 2 liters of seawater in an old bucket. If the water is 20% salt, how many ml of salt will Jack get when all the water evaporates?

Question (topic): Samantha is designing a circular garden in her backyard. The garden has a diameter of 8 meters. She wants to build a path around the garden that is 1 meter wide. What is the area of the path, in square meters, that Samantha will need to pave with stones or concrete?

A question with different structure is acceptable:

Question: Dan owns an ice cream shop and every sixth customer gets a free ice cream cone. Cones cost \$2 each. If he sold \$100 worth of cones, how many free ones did he give away?

Question (restructured): Dan owns an ice cream shop and every sixth customer gets a free ice cream cone. Cones cost x each. If he sold 100 worth of cones, how many free ones did he give away? If we know the answer is 10, what is the value of x?

Rephrased question is acceptable:

Question: Joy can read 8 pages of a book in 20 minutes. How many hours will it take her to read 120 pages? Question (rephrase): How many hours will Joy need to read 120 pages if she can read 8 pages in 20 minutes? A different scenario is acceptable:

Question: Ed has 2 dogs, 3 cats and twice as many fish as cats and dogs combined. How many pets does Ed have in total?

Question (scenario): Sarah owns 4 bicycles, 2 skateboards, and three times as many pairs of rollerblades as bicycles and skateboards combined. How many wheeled sports equipment items does Sarah have in total?

424

425 **B** Case Study of EAI

We conduct a qualitative study how actor and critic accomplish exploration. On GSM8K, we manually 426 inspect 100 examples randomly sampled from EAI explored dataset to better understand how does the 427 428 exploration work. We observed that the critic excels at assessing the novelty of generated questions, providing precise feedback to enhance them. The actor effectively utilizes the critic's feedback to 429 refine the generated questions. Of the 100 samples reviewed, in 24 instances, the critic initially 430 found the questions lacking in novelty and provided suggestions for improvement. Out of these, 431 19 were subsequently refined and accepted after revisions. Below is a representative example of 432 this interaction where the critic offers advice to significantly differentiate the generated question. 433 434 Here, the critic recommends incorporating the mathematical concept of volumes and presenting an 435 alternative scenario

436 [Critic guides exploration]

437 (First round)

Actor's generation: Question: Jake is planning to buy a new skateboard which costs \$200. Jake only
 has a quarter of the money he requires. His brother decided to give him \$20 for it, and his uncle three
 times as much as his brother. How much more does Jake need to raise to purchase the skateboard? (answer
 omitted)

442 Critic's critique: The new question you've provided is somewhat similar in structure to the existing questions, as it involves basic arithmetic operations (multiplication, division, addition, and subtraction).
444 While it introduces a different context with hats and balls, the underlying math principles are similar to those used in the existing questions. To make the new question substantially different, you could consider introducing more complex mathematical concepts such as volumes or using a different scenario altogether.
447

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448 (Second round)

Actor's generation: An artist is creating a sculpture using various geometric shapes. The sculpture consists of a cube, a sphere, a cylinder, and a pyramid. The cube has a side length of 6 units, the sphere has a radius of 4 units, the cylinder has a height of 8 units and a base radius of 3 units, and the pyramid has a base edge length of 5 units and a height of 7 units. Calculate the total volume of the artist's sculpture. A: omitted 454 Critic's critique: The new question is substantially different from the existing questions. It involves

a slightly more complex problem-solving process. It is good to be added to math questions. The decision

456 is accept. 🗸

We also conducted a study to determine how effective the critic is at evaluating the correctness of 457 answers. Of the 100 critiques assessed, the critic accurately identified incorrectness in 13 actor 458 generations and offered critiques to correct 10 of them. However, there were 7 instances where the 459 critic failed to recognize the errors. The remaining actor generations were accurate. It's worth noting 460 that, due to the uniform usage of the four exploration principles, out of the 100 actor generations, 50 461 were either paraphrased questions or questions with new scenarios, these 50 were less prone to errors 462 as they didn't necessitate significant changes to the mathematical structure. In fact, only 2 solutions 463 among them were incorrect. On the other hand, those that involved restructuring or tackled new topics 464 were more error-prone: 7 from restructuring and 4 from new topics were incorrect. Intriguingly, the 465 critic corrected 6 out of the 7 restructured ones, but only 1 out of the 4 new topics. This might suggest 466 that questions on new topics are more open-ended and might need multiple rounds of interactions for 467 accurate evaluation. Further refinement in this verification process will be the focus of our future 468 work. 469

Our analysis revealed that the critic excels in evaluation rather than generation. This observation is exemplified in the quoted example, it can be seen that even when the model cannot directly answer the question, it can effectively assess the correctness of the actor's response. This discovery is intriguing, as the actor's response effectively serves as a 'hint'. This observation aligns with prior works that found models are better at evaluating answer (or improving an answer) than generating it from scratch in various settings [6, 25, 23, 8, *inter alia*].

476 [Critic cannot solve question directly]

477 Input: A magician has 5 hats, each with a different number of balls inside. The first hat has 3 balls, 478 the second hat has twice as many balls as the first, the third hat has half as many balls as the second, the 479 fourth hat has 5 balls, and the fifth hat has 4 times as many balls as the fourth. How many balls are in the 480 magician's hats altogether?

- Output: There are 3 + 2 * 3 = 7 balls in the first two hats. There are 5 2 = 3 balls in the third hat. There
- are 4 * 3 = 12 balls in the fourth and fifth hats. In total, there are 7 + 3 + 12 = 22 balls in the magician's
- 483 hats. Answer: 22. 🗡

484 [Critic can evaluate actor's answer]

Input: Please review whether the answer for the following question is correct. Q: A magician has 5 hats, 485 each with a different number of balls inside. The first hat has 3 balls, the second hat has twice as many 486 balls as the first, the third hat has half as many balls as the second, the fourth hat has 5 balls, and the fifth 487 hat has 4 times as many balls as the fourth. How many balls are in the magician's hats altogether? A: There 488 are $3 + 2 \ge 3/2 = 3 + 3 = 6$ balls in the first two hats. There are 5 - 3/2 = 5 - 1.5 = 3.5 balls in the third 489 hat. There are $4 \times 5 = 20$ balls in the fourth hat. In total, there are 6 + 3.5 + 20 = 29.5 balls. Since you 490 can't have a fraction of a ball, you would need to round up to the nearest whole number of balls. Therefore, 491 there are 29 balls in the magician's hats altogether. 492

Output: The magician has 5 hats, each with a different number of balls inside. The first hat has 3 balls, the second hat has twice as many balls as the first, so it has 3 * 2 = 6 balls. The third hat has half as many balls as the second, so it has 6/2 = 3 balls. The fourth hat has 5 balls. The fifth hat has 4 times as many balls as the fourth, so it has 5 * 4 = 20 balls. In total, there are 3 + 6 + 3 + 5 + 20 = 37 balls. Since you can't have a fraction of a ball, you would need to round up to the nearest whole number of balls. Therefore, there are 37 balls in the magician's hats altogether. The answer provided is incorrect. \checkmark

499 C Experiment Details

We use a temperature of 0.7 for the actor during exploration as in prior work [8], and we sample 500 10 actor generations for every batch of samples from the replay buffer. We use a temperature 501 of 0.0 for the critic since we found that it performs best. Following prior work [45], we filter 502 out reasoning paths with incorrect answers or calculations—based on Python evaluation—for the 503 'paraphrasing' and 'new scenarios' exploration categories. However, we do not apply this filter to 504 the 'restructuring' or 'new topics' exploration categories, as we do not have ground truth answers 505 for these two categories. The evaluations for all baselines and our approach are conducted with 506 deterministic sampling following prior work and report maj1@1 (accuracy) across all experiments. 507 We follow prior work by conducting evaluations using deterministic sampling for both our approach 508

- and the baseline methods. We report maj1@1 accuracy across all experimental setups. All models are trained with the same hyperparameters: global batch size = 128, learning rate = 2e-5, epochs = 3, sequence length = 2048. The training is done with 8x A100 80GB GPUs.