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# Unsupervised Representation Learning of Brain Activity via Bridging Voxel Activity and Functional Connectivity

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## Abstract

1        Effective brain representation learning is a key step toward revealing the under-  
2        standing of cognitive processes and unlocking detecting and potential therapeutic  
3        interventions for neurological diseases/disorders. Existing studies have focused  
4        on either (1) voxel-level activity, where only a single beta weight for each voxel  
5        (i.e., aggregation of voxel activity over a time window) is considered, missing  
6        their temporal dynamics, or (2) functional connectivity of the brain in the level of  
7        region of interests, missing voxel-level activities. In this paper, we bridge this gap  
8        and design BRAINMIXER, an unsupervised learning framework that effectively  
9        utilizes both functional connectivity and associated time series of voxels to learn  
10       voxel-level representation in an unsupervised manner. BRAINMIXER employs two  
11       simple yet effective MLP-based encoders to simultaneously learn the dynamics  
12       of voxel-level signals and their functional correlations. To encode voxel activity,  
13       BRAINMIXER fuses information across both time and voxel dimensions via a  
14       dynamic self-attention mechanism. To learn the structure of the functional connect-  
15       ivity graph, BRAINMIXER presents a temporal graph patching and encodes each  
16       patch by combining its nodes' features via a new adaptive temporal graph pooling.  
17       Our experiments show that BRAINMIXER attains outstanding performance and  
18       outperforms 13 baselines in different downstream tasks and experimental setups.

## 19    1 Introduction

20    Understanding the human brain is a long-term intriguing goal for neuroscience and recent advance-  
21    ments in machine learning methods have provided powerful paradigms to achieve this goal (Guo  
22    et al., 2016; Poldrack & Farah, 2015). While neuroimaging techniques, as the principal source of  
23    brain data, provide rich information about brain functions, the provided data is high-dimensional  
24    and complex in nature (Poldrack & Gorgolewski, 2014). To overcome this challenge, representation  
25    learning serves as the backbone of machine learning methods on neuroimaging data and provides a  
26    low-dimensional representation of brain components at different levels of granularity, enabling the  
27    understanding of behaviors (Schneider et al., 2023), brain functions (Yamins & DiCarlo, 2016) and/or  
28    detecting neurological diseases or disorders (Behrouz & Seltzer, 2023a; Uddin et al., 2017).

29    In the brain imaging literature, studies have mainly focused on two spatial scales—voxel-level  
30    and network-level—as well as two analysis approaches—multivariate pattern analysis (MVPA)  
31    and functional connectivity (Mahmoudi et al., 2012; Van Den Heuvel & Pol, 2010). The MVPA  
32    approach is often employed at the voxel-level scale and in task-based studies to associate neural  
33    activities at a very fine-grained and local level with particular cognitive functions, behaviors, or  
34    stimuli. This method has found applications in various areas, including the detection of neurological  
35    conditions (Sundermann et al., 2014; Bray et al., 2009), neurofeedback interventions (Cortese et al.,

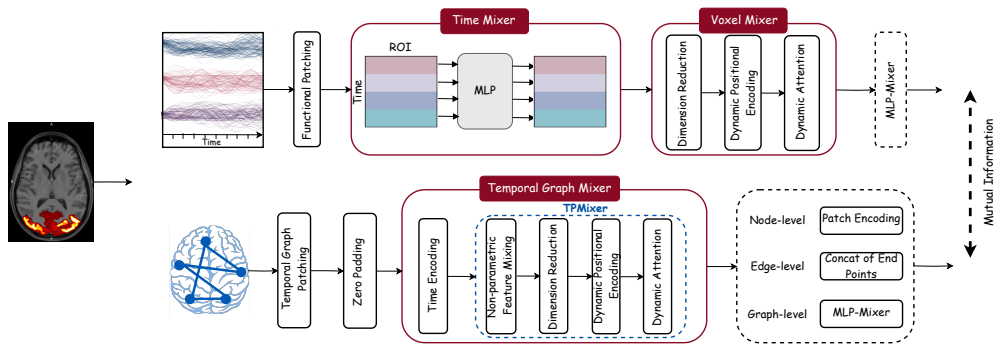


Figure 1: **Schematic of the BRAINMIXER.** BRAINMIXER consists of two main modules: (1) Voxel Activity Encoder (top), and (2) Functional Connectivity Encoder (bottom).

2021), decoding neural responses to visual stimuli (Horikawa & Kamitani, 2017), deciphering memory contents (Lee & Baker, 2016; Chadwick et al., 2012), and classifying cognitive states (Mitchell et al., 2003). The functional connectivity analysis, on the other hand, focuses on the temporal correlations or statistical dependencies between the activity of different brain regions at larger scales to assess how these areas communicate and collaborate. This method has been utilized to study various topics such as task-related network dynamics (Gonzalez-Castillo & Bandettini, 2018; Hutchison et al., 2013) and the effects of neurological disorders on brain connectivity (Greicius, 2008; Du et al., 2018).

**Limitation of Previous Methods.** Despite the advances in the representation learning of brain signals, existing studies suffer from a subset of five limitations: ① Study the human brain at a single scale: Most existing studies study the brain at either voxel-level or functional connectivity, while these two scales can provide complementary information to each other; e.g., although voxel-level activity provides detailed and more accurate information about brain activity, it misses the information about how different areas communicate with each other at a high level. Recently, this limitation has motivated researchers to search for new methods of integrating these two levels of analyses (Nieto-Castanon, 2022; McNorgan et al., 2020). ② Supervised setting: Learning brain activity in a supervised setting relies on a large number of clinical labels while obtaining accurate and reliable clinical labels is challenging due to its high cost (Avberšek & Repovš, 2022). ③ Missing information by averaging: Most existing studies on voxel activities aggregate measured voxel activity (e.g., its blood-oxygen level dependence) over each time window to obtain a single beta weight (Roth et al., 2022; Vassena et al., 2020; Roth & Merriam, 2023). However, this approach misses the voxel activity dynamic over each task. Moreover, most studies on brain functional connectivity also aggregate closed voxels to obtain brain activity in the Region of Interest (ROI) level, missing individual voxel activities. ④ Missing the dynamics of the interactions: Some existing studies neglect the fact that the functional connectivity of the human brain dynamically changes over time, even in resting-state neuroimaging data (Calhoun et al., 2014). In task-dependent neuroimage data, subjects are asked to perform different tasks in different time windows, and the dynamics of the brain activity play an important role in understanding neurological disease/disorder (Hernandez et al., 2015). ⑤ Designed for a particular task or neuroimaging modality: Due to the different and complex clinical patterns of brain signals (da Silva, 1991), some existing methods are designed for a particular type of brain signal data (Lanciano et al., 2020; Cai et al., 2023), and there is a lack of a unified framework.

**Application to Understanding Object Representation in the Brain.** Understanding object representation in the brain is a key step toward revealing the basic building blocks of human visual processing (Hebart et al., 2023). Due to the hierarchical nature of human visual processing, it requires analyzing brain activity at different scales, i.e., both functional connectivity graph and voxel-level activity. However, there is a small number of studies in this area, possibly due to the lack of proper large-scale datasets. In this study, we present two large-scale graph-structured datasets, BVFC and BVFC-MEG, based on raw fMRI and MEG from THINGS (Hebart et al., 2023) dataset. BVFC (resp. BVFC-MEG) comprises 26,220 graphs (resp. 89,792 graphs) with up to 13,166 nodes (resp. 272 nodes), representing brain voxels' activity (resp. channels) in functional MRI (fMRI) (resp. magnetoencephalographic (MEG)) for human subjects when seeing natural or unrecognizable GAN-generated images. We believe this dataset can bridge graph anomaly detection and graph classification tasks to understanding object representation in the brain (see §4). See Appendix B for more details.

79 **Contributions.** To overcome the above limitations, we leverage both voxel-level activity and  
80 functional connectivity of the brain. We present BRAINMIXER, an unsupervised MLP-based brain  
81 representation learning approach that jointly learns voxel-level activity and functional connectivity.  
82 BRAINMIXER employs a novel multivariate timeseries encoder that binds information across both  
83 time and voxel dimensions. It uses a simple MLP with functional patching to fuse information across  
84 different timestamps and learns dynamic self-attention weights to fuse information across voxels  
85 based on their functionality. On the other hand, BRAINMIXER uses a novel temporal graph learning  
86 method to encode the brain functional connectivity. The graph encoder first extracts temporal patches  
87 using temporal random walks and then fuses information within each patch using the designed  
88 dynamic self-attention mechanism. We further propose an adaptive permutation invariant pooling  
89 to obtain patch encodings. Since voxel activity and functional connectivity encodings are different  
90 views of the same context, we propose an unsupervised pre-training approach to jointly learn voxel  
91 activity and functional connectivity by maximizing their mutual information. In the experimental  
92 evaluations, we provide two new large-scale graph and timeseries datasets based on THINGS (Hebart  
93 et al., 2023). Extensive experiments on six datasets show the superior performance of BRAINMIXER  
94 and the significance of each of its components in a variety of downstream tasks.

95 For the sake of consistency, we explain BRAINMIXER for fMRI modality; however, as it is shown in  
96 §4, it can simply be used for any other neuroimaging modalities that provide a timeseries for each  
97 part of the brain (e.g., MEG and EEG). When dealing with MEG or EEG, we can replace the term  
98 “voxel” with “channel”. Supplementary materials (code and Appendix) can be found in [this link](#).

## 99 2 Related Work

100 To situate our BRAINMIXER in a broader context, we briefly review machine learning models for  
101 timeseries, graphs, and neuroscience. For extensive discussion of related work see [Appendix C](#).

102 **Timeseries Learning.** Attention mechanisms are powerful models to capture long-range depen-  
103 dencies and so recently, Transformer-based models have attracted much attention in time series  
104 forecasting (Zerveas et al., 2021; Li et al., 2019). Due to their quadratic time complexity, several  
105 studies aim to reduce the time and memory usage of these methods (Child et al., 2019). Another type  
106 of work uses (hyper)graph learning frameworks to learn (higher-order) patterns in timeseries (Park  
107 et al., 2009; Sawhney et al., 2021). Inspired by the recent success of MLP-MIXER (Tolstikhin et al.,  
108 2021), Li et al. (2023) and Chen et al. (2023) presented two variants of MLP-MIXER for timeseries  
109 forecasting. All these methods are different from BRAINMIXER, as ① they use static attention  
110 mechanisms, ② do not take advantage of the functionality of voxels in patching, and ③ are designed  
111 for timeseries forecasting and cannot simply be extended to various downstream tasks on the brain.

112 **MLP-based Graphs Learning.** Learning on graphs has been an active research area in recent  
113 years (Jiang et al., 2021; Veličković et al., 2018; Chamberlain et al., 2023). While most studies use  
114 message-passing frameworks to learn the local and global structure of the graph, recently, due to  
115 the success of MLP-based methods (Tolstikhin et al., 2021), MLP-based graph learning methods  
116 have attracted much attention (Hu et al., 2021; Behrouz et al., 2023). For example, Cong et al. (2023)  
117 and He et al. (2023) presented two extensions of MLP-MIXER to graph-structured data. However,  
118 all these methods are different from BRAINMIXER and specifically FC Encoder, as either ① use  
119 time-consuming graph clustering algorithms for patching, ② are static methods and cannot capture  
120 temporal properties, or ③ are attention-free and cannot capture the importance of nodes.

121 **Graph Learning and Timeseries for Neuroscience.** In recent years, several studies have analyzed  
122 functional connectivity to differentiate human brains with a neurological disease/disorder (Jie et al.,  
123 2016; Chen et al., 2011; Wee et al., 2011). With the success of graph neural networks in graph  
124 data analysis, deep learning models have been developed to predict brain diseases by studying brain  
125 network structures (Behrouz & Seltzer, 2022; Zhu et al., 2022; Cui et al., 2022). Moreover, several  
126 studies focus on brain signals (Craik et al., 2019; Shoeibi et al., 2021) to detect neurological diseases.  
127 For example, Cai et al. (2023) designed a self-supervised learning framework to detect seizures  
128 from EEG and SEEG data. However, all these methods are different from BRAINMIXER as they are  
129 designed for a particular task (e.g., brain classification), a particular neuroimaging modality (e.g.,  
130 fMRI or EEG), and/or supervised settings.

131 **3 Method: BRAINMIXER**

132 In this section, we first discuss the notation we use throughout the paper. Detailed discussion about  
 133 background concepts can be found in [Appendix A](#).

134 **Notation.** We represent the neuroimaging of a human brain as  $\mathcal{B} = \{\mathcal{B}^{(t)}\}_{t=1}^T$  where  $\mathcal{B}^{(t)} =$   
 135  $(\mathcal{V}, \mathcal{G}_F^{(t)}, \mathcal{X}^{(t)}, \mathbb{F})$  represents the neural data in time window  $1 \leq t \leq T$ . Here,  $\mathcal{V}$  is the set of voxels,  
 136  $\mathcal{G}_F^{(t)} = (\mathcal{V}, \mathcal{E}^{(t)}, \mathcal{A}^{(t)})$  is the functional connectivity graph,  $\mathcal{E}^{(t)} \subseteq \mathcal{V} \times \mathcal{V}$  is the set connections  
 137 between voxels,  $\mathcal{A}^{(t)}$  is the correlation matrix (weighted adjacency matrix of  $\mathcal{G}_F^{(t)}$ ),  $\mathcal{X}^{(t)} \in \mathbb{R}^{|\mathcal{V}| \times \tilde{T}}$  is a  
 138 multivariate timeseries of voxels activities, and  $\mathbb{F}$  is the set of functional systems in the brain ([Schaefer](#)  
 139 [et al., 2018](#)) in time window  $t$ .

140 **3.1 Voxel Activity Encoder**

141 The main goal of this module is to learn the time series of the voxel-level activity. However, the  
 142 activities of voxels are not disjoint; for example, an increase in fusiform face area (FFA) activity might  
 143 be associated with a rise in V1 activity. Accordingly, effectively learning their dynamics patterns  
 144 requires both capturing cross-voxel and within-voxel time series information. The vanilla MLP-  
 145 MIXER ([Tolstikhin et al., 2021](#)) can be used to bind information across both of these dimensions, but  
 146 the human brain has unique traits that make directly applying MLP-MIXER insufficient/impractical.  
 147 ① There does not exist in general a canonical grid of the brain to encode voxel activities, which  
 148 makes patch extraction challenging. ② Contrary to images that can be divided into patches of the  
 149 same size, the partitioning of voxels might not be all the same size due to the complex brain topology.  
 150 ③ MLP-MIXER employs a fixed static mixing matrix for binding patches, while in the brain the  
 151 functionality of each token is important and a different set of tokens should be mixed differently  
 152 based on their connections and functionality. To address these challenges, the *VA Encoder* employs  
 153 two submodules, *time-mixer* and *voxel-mixer* with dynamic mixing matrix, to fuse information across  
 154 both time and voxel dimensions, respectively.

155 The human brain is comprised of functional systems (FS) ([Schaefer et al., 2018](#)), which are groups  
 156 of voxels that perform similar functions ([Smith et al., 2013](#)). We take advantage of this hierarchical  
 157 structure and patch voxels based on their functionality. However, the main challenge is that the sizes  
 158 of the patches (set of voxels with similar functionality) are different. To this end, inspired by the  
 159 inference of ViT models ([Dosovitskiy et al., 2021](#)), we linearly interpolate patches with smaller sizes.

160 **Functional Patching.** Let  $K$  be the number of voxels and  $\mathbf{X} \in \mathbb{R}^{K \times (T \times \tilde{T})}$  represents the time  
 161 series of voxels activities over all time windows. We split  $\mathbf{X}$  to spatio-temporal patches  $\mathbf{X}_i$  with size  
 162  $|f_i| \times t_p$ , where  $f_i \in \mathbb{F}$  is a functional system ([Schaefer et al., 2018](#)), and  $t_p$  is the temporal-dimension  
 163 length. To address the challenge of patches with different sizes, we use INTERPOLATE(.) to linearly  
 164 interpolate patches to the same size  $N_p$ : i.e.,  $\tilde{\mathbf{X}}_i = \text{INTERPOLATE}(\mathbf{X}_i)$ , where  $\tilde{\mathbf{X}}_i \in \mathbb{R}^{N_p \times t_p}$ .

165 **Voxel-Mixer.** Since the effect of each task (e.g., in task-based fMRI) on brain activity as well as  
 166 the time it lasts varies ([Yang et al., 2023a](#)), for different tasks, we might need to emphasize more  
 167 on a subset of voxels. To this end, to bind information across voxels, we use a dynamic attention  
 168 mechanism that uses a learnable dynamic mixing matrix  $\mathbf{P}_i$ , learning to mix a set of input voxels  
 169 based on their functionality. While using different learnable matrices for mixing voxels activity  
 170 provides a more powerful architecture, its main challenge is a large number of parameters. To mitigate  
 171 this challenge, we first reduce the dimensions of  $\tilde{\mathbf{X}}$ , split it into a set of segments, denoted as  $S$ , and  
 172 then combine the transformed matrices. Given a segment  $s \in S$  we have:

$$\hat{\mathbf{X}}^{(t)(s)} = \tilde{\mathbf{X}}^{(t)} \mathbf{W}_{\text{segment}}^{(s)}, \quad (\text{Dimension Reduction})$$

$$\mathbf{P}_i^{(s)} = \text{SOFTMAX} \left( \text{FLAT} \left( \hat{\mathbf{X}}^{(t)(s)} \right) \mathbf{W}_{\text{flat}}^{(s)(i)} \right), \quad (\text{Learning Dynamic Mixer})$$

$$\mathbf{X}_{\text{PE}}^{(t)} = \left[ \prod_{s \in S} \mathbf{P}^{(s)} \tilde{\mathbf{X}}^{(t)(s)} \right] \mathbf{W}_{\text{PE}}, \quad (\text{Dynamic Positional Encoding})$$

$$\mathbf{H}_{\text{Voxel}}^{(t)} = \text{Norm} \left( \tilde{\mathbf{X}}^{(t)} \right) + \text{SIGMOID} \left( \frac{\mathbf{X}_{\text{PE}}^{(t)} \mathbf{X}_{\text{PE}}^{(t)\top}}{\sqrt{\tilde{T}}} \right) \mathbf{X}_{\text{PE}}^{(t)}, \quad (\text{Dynamic Self-Attention})$$

173 where  $\mathbf{W}_{\text{segment}}^{(s)} \in \mathbb{R}^{\tilde{T} \times d}$ ,  $\mathbf{W}_{\text{flat}}^{(s)} \in \mathbb{R}^{(K \times d) \times K}$ ,  $\mathbf{W}_{\text{PE}} \in \mathbb{R}^{\tilde{T} \times \tilde{T}}$  are learnable parameters,  $\parallel$  is  
 174 concatenation, and  $\text{SIGMOID}(\cdot)$  is row-wise sigmoid normalization. Note that for different segments  
 175 we use different dimensionality reduction matrices to reinforce the power of the Voxel Mixing.

176 **Time Mixer.** We first fuse information in the time dimension by using the Time Mixer submodule.  
 177 To this end, the Time Mixer employs a 2-layer MLP with layer-normalization (Ba et al., 2016):

$$\mathbf{H}_{\text{Time}}^{(t)} = \mathbf{H}_{\text{Voxel}}^{(t)} + \left( \sigma \left( \text{LayerNorm} \left( \mathbf{H}_{\text{Voxel}}^{(t)} \right) \mathbf{W}_{\text{Time}}^{(1)} \right) \mathbf{W}_{\text{Time}}^{(2)} \right), \quad (1)$$

178 where  $\mathbf{W}_{\text{Time}}^{(1)}$  and  $\mathbf{W}_{\text{Time}}^{(2)}$  are learnable matrices,  $\sigma(\cdot)$  is an activation function (we use  
 179 GeLU (Hendrycks & Gimpel, 2020)), and LayerNorm is layer normalization (Ba et al., 2016).

### 180 3.2 Functional Connectivity Graph Encoder

181 To encode the functional connectivity graph, we design an MLP-based architecture that learns both  
 182 the structural and temporal properties of the graph. Inspired by the recent success of all-MLP  
 183 architecture in graphs (Cong et al., 2023), we extend MLP-MIXER to temporal graphs. We first  
 184 define patches in temporal graphs. While patches in images, videos, and multivariate timeseries  
 185 can simply be non-overlapping regular grids, patches in graphs are overlapping non-grid structures,  
 186 which makes the patching extraction challenging. He et al. (2023) suggest using graph partitioning  
 187 algorithms to extract graph patches; however, these partitioning algorithms ① only consider structural  
 188 properties, missing the temporal dependencies, and ② can be time-consuming, limiting the scalability  
 189 to dense graphs like brain functional connectome. To this end, we propose a temporal-patch extraction  
 190 algorithm such that nodes (voxels) in each patch share similar temporal and structural properties.

191 **Temporal Patching.** To extract temporal patches from the graph, we use a biased temporal random  
 192 walk that walks over both nodes (voxels) and timestamps. Given a functional connectivity graph  
 193  $\mathcal{G}_F = \{\mathcal{G}_F^{(t)}\}_{t=1}^T$ , we sample  $M$  walks with length  $m + 1$  started from node (voxel)  $v_0 \in \mathcal{V}$  like:  
 194  $\text{Walk} : (v_0, t_0) \rightarrow (v_1, t_1) \rightarrow \dots \rightarrow (v_m, t_m)$ , such that  $(v_{i-1}, v_i) \in \mathcal{E}^{(t_i)}$ , and  $t_0 \geq t_1 \geq t_2 \geq$   
 195  $\dots \geq t_m$ . Note that, contrary to some previous temporal random walks (Wang et al., 2021; Behrouz  
 196 et al., 2023), we allow the walker to walk in the same timestamp at each step. While backtracking  
 197 over time, we aim to capture temporal information and extract the dynamics of voxels’ activity over  
 198 related timestamps. Previous studies show that doing a task can affect brain activity even after 2  
 199 minutes (Yang et al., 2023a). To this end, since more recent connections can be more informative,  
 200 we use a biased sampling procedure. Let  $v_p$  be the previously sampled node, we use hyperparameters  
 201  $\theta, \theta_0 \geq 0$  to sample a node  $v$  with probability proportional to  $\exp(\theta(t - t_p + \theta_0))$ , where  $t$  and  $t_p$   
 202 are the timestamps that  $(v_p, v) \in \mathcal{E}^{(t)}$  and the timestamp of the previous sample, respectively. In this  
 203 sampling procedure, smaller (resp. larger)  $\theta$  means less (resp. more) emphasis on recent timestamps.  
 204 Each walk started from  $v$  can be seen as a temporal subgraph, and so we let  $\rho_v$  be the union of all  
 205 these subgraphs (walks started from  $v$ ). We treat each of  $\rho_v$  as a temporal patch.

206 **Temporal Pooling Mixer.** Given the temporal graph patches that we extracted above, we need to  
 207 encode each patch to obtain patch encodings (we later use these patch encodings as their corresponding  
 208 voxel’s encodings). While simple poolings (e.g.,  $\text{SUM}(\cdot)$ ) are shown to miss information (Behrouz  
 209 et al., 2023), more complicated pooling functions consider a static pooling rule. However, as discussed  
 210 above, the effect of performing a task on the neuroimaging data might last for a period of time and  
 211 the pooling rule might change over time. To this end, we design a temporal pooling,  $\text{TPMIXER}(\cdot)$ ,  
 212 that dynamically pools a set of voxels in a patch based on their timestamps.

213 Given a patch  $\rho_{v_0} = \{v_0, v_1, \dots, v_k\}$ , for each voxel we consider the correlation of its activity with  
 214 other voxels’ as its preliminary feature vector. That is, for each voxel  $v$ , we consider its feature vector  
 215 in the time window  $t$  as  $\mathcal{A}_v^{(t)}$ , the  $v$ ’s corresponding row in  $\mathcal{A}^{(t)}$ . We abuse the notation and use  $\mathcal{A}_{\rho_v}^{(t)}$   
 216 to refer to the set of  $\mathcal{A}^{(t)}$ ’s rows corresponding to  $\rho_v$ . Since patch sizes are different, we zero pad  
 217  $\mathcal{A}_{\rho_v}^{(t)}$  matrices to a fixed size. Note that this zero padding is important to capture the size of each voxel  
 218 neighborhood. The voxel with more zero-padded dimensions in its patch has less correlation with  
 219 others. To capture both cross-feature and cross-voxel dependencies, we can use the same architecture  
 220 as the Time Mixer and Voxel-Mixer. However, the main drawback of this approach is that a pooling

221 function is expected to be permutation invariant while the Voxel Mixer phase is permutation variant.  
 222 To address this challenge, we fuse information across features in a non-parametric manner as follows:

$$\mathbf{H}_F^{(t)} = \mathcal{A}_{\rho_v}^{(t)} + \sigma \left( \text{Softmax} \left( \text{LayerNorm} \left( \mathcal{A}_{\rho_v}^{(t)} \right)^\top \right) \right)^\top, \quad (2)$$

223 where  $\sigma(\cdot)$  is an activation function and  $\text{Softmax}(\cdot)$  is used to normalize across features to bind and  
 224 fuse feature-wise information in a non-parametric manner, avoiding permutation variant operations in  
 225 the Time Mixer. To dynamically fuse information across voxels, we use the same idea as dynamic  
 226 self-attention in §3.1 and learn dynamic matrices  $\mathbf{P}_{\text{Pool}_i}$ ; let  $d_{\text{patch}}$  be the patch size:

$$\mathbf{P}_{\text{Pool}_i} = \text{SOFTMAX} \left( \text{FLAT} \left( \mathbf{H}_F^{(t)} \right) \mathbf{W}_{\text{Pool}}^{(i)} \right) \quad (3)$$

$$\mathbf{h}_{\rho_v} = \text{MEAN} \left( \text{Norm}(\mathbf{H}_F^{(t)}) + \mathbf{H}_{\text{PE}}^{(t)} \text{SOFTMAX} \left( \frac{\mathbf{H}_{\text{PE}}^{(t)\top} \mathbf{H}_{\text{PE}}^{(t)}}{\sqrt{d_{\text{patch}}}} \right) \right), \quad (4)$$

227 where  $\mathbf{H}_{\text{PE}}^{(t)} = \mathbf{H}_F^{(t)} \mathbf{P}_{\text{Pool}}$  is the transformation of  $\mathbf{H}_F^{(t)}$  by dynamic matrix  $\mathbf{P}_{\text{Pool}}$ .

228 **Theorem 1.** TPMIXER is permutation invariant and a universal approximator of multisets.

229 **Time Encoding.** To distinguish different timestamps in the functional connectivity graph, we use a  
 230 non-learnable time encoding module proposed by Cong et al. (2023). This encoding approach helps  
 231 reduce the number of parameters, and also it has been shown to be more stable and generalizable (Cong  
 232 et al., 2023). Given hyperparameters  $\alpha, \beta$ , and  $d$ , we use feature vector  $\boldsymbol{\omega} = \{\alpha^{-i/\beta}\}_{i=0}^{d-1}$  to encode  
 233 each timestamp  $t$  using  $\cos(\boldsymbol{\omega}t)$  function. Therefore, we obtain the time encoding as  $\boldsymbol{\eta}_t = \cos(\boldsymbol{\omega}t)$ .

234 **Voxel-, Edge-, and Graph-level Encodings.** Depending on the downstream task, we might obtain  
 235 voxel-, edge-, or graph-level encodings. For each voxel  $v \in \mathcal{V}$ , we let  $\mathcal{E}^{(t)}[\rho_v]$  be the set of connections  
 236 in the patch of  $v$ . To obtain the voxel-level encoding of each voxel  $v$ ,  $\boldsymbol{\psi}_v$ , we use patch encoding  
 237 and concatenate it with all the weighted mean of timestamp encodings; i.e.,  $\boldsymbol{\psi}_v^t = \text{MLP}([\mathbf{h}_{\rho_v} \parallel \mathcal{T}_v])$ ,  
 238 where  $\mathcal{T}_v = \frac{\sum_{t_0=1}^t \mathcal{E}^{(t_0)}[\rho_v] \boldsymbol{\eta}_{t_0}}{\sum_{t_0=1}^t \mathcal{E}^{(t_0)}[\rho_v]}$ . For a connection  $e = (u, v) \in \mathcal{E}^{(t)}$ , we obtain its encoding by  
 239 concatenating its endpoints and its timestamp encodings; i.e.,  $\boldsymbol{\zeta}_{(u,v)}^{(t)} = \text{MLP}([\boldsymbol{\psi}_u^t, \boldsymbol{\psi}_v^t, \boldsymbol{\eta}_t])$ . Finally,  
 240 to obtain the graph level encoding, we use vanilla MLP-MIXER (Tolstikhin et al., 2021) on patch  
 241 encodings; let  $\boldsymbol{\Psi}^{(t)}$  be the matrix whose rows are  $\boldsymbol{\psi}_v^{(t)}$ :

$$\boldsymbol{\Psi}_{\text{token}}^{(t)} = \boldsymbol{\Psi}^{(t)} + \mathbf{W}_{\text{token}}^{(2)} \sigma \left( \mathbf{W}_{\text{token}}^{(1)} \text{LayerNorm} \left( \boldsymbol{\Psi}^{(t)} \right) \right), \quad (5)$$

$$\text{ENC}(\mathcal{G}_F^{(t)}) = \text{MEAN} \left( \boldsymbol{\Psi}_{\text{token}}^{(t)} + \sigma \left( \text{LayerNorm} \left( \boldsymbol{\Psi}_{\text{token}}^{(t)} \right) \mathbf{W}_{\text{channel}}^{(1)} \right) \mathbf{W}_{\text{channel}}^{(2)} \right). \quad (6)$$

### 242 3.3 Self-supervised Pre-training

243 In §3.1 and §3.2 we obtained the encodings of the same contexts, from different perspectives. In this  
 244 section, inspired by (Hjelm et al., 2019; Bachman et al., 2019), we use the mutual information of these  
 245 two perspectives from the same context, to learn voxel- and brain-level encodings in a self-supervised  
 246 manner. To this end, let  $\boldsymbol{\Psi}$  be the voxel-level encodings obtained from functional connectome,  
 247  $\mathbf{Z}_F^{(t)} = \text{ENC}(\mathcal{G}_F^{(t)})$  be the global encoding (brain-level) of the functional connectome,  $\mathbf{H}_{\text{Voxel}}^{(t)}$  be the  
 248 voxel activity encodings from the brain activity timeseries, and  $\mathbf{Z}_V^{(t)}$  be the global encoding (brain-  
 249 level) of the voxel activity timeseries, we aim to maximize  $I(\mathbf{Z}_F^{(t)}, \boldsymbol{\psi}_{v,i}^{(t)}) + I(\mathbf{Z}_V^{(t)}, (\mathbf{H}_{\text{Voxel}}^{(t)})_{v,j})$  for all  
 250  $v \in \mathcal{V}$  and possible  $i, j$ . Following previous studies (Bachman et al., 2019), we use Noise-Contrastive  
 251 Estimation (NCE) (Gutmann & Hyvärinen, 2010) and minimize the following loss function:

$$\mathbb{E}_{(\mathbf{Z}_F^{(t)}, \boldsymbol{\psi}_{v,i}^{(t)})} \left[ \mathbb{E}_{\mathcal{N}} \left[ \mathcal{L}_{\Phi}(\mathbf{Z}_F^{(t)}, \boldsymbol{\psi}_{v,i}^{(t)}, \mathcal{N}) \right] \right] + \mathbb{E}_{(\mathbf{Z}_V^{(t)}, (\mathbf{H}_{\text{Voxel}}^{(t)})_{v,j})} \left[ \mathbb{E}_{\mathcal{N}} \left[ \mathcal{L}_{\Phi}(\mathbf{Z}_V^{(t)}, (\mathbf{H}_{\text{Voxel}}^{(t)})_{v,j}, \mathcal{N}) \right] \right], \quad (7)$$

252 where  $\mathcal{N}$  is the set of negative samples,  $(\mathbf{Z}_F^{(t)}, \boldsymbol{\psi}_{v,i}^{(t)})$  and  $(\mathbf{Z}_V^{(t)}, (\mathbf{H}_{\text{Voxel}}^{(t)})_{v,j})$  are the positive sample  
 253 pairs, and  $\mathcal{L}_{\Phi}$  is a standard Log-Softmax.

Table 1: Performance on brain classification: Mean ACC (%)  $\pm$  standard deviation.

Methods	BVFC	BVFC-MEG	HCP-Mental	HCP-Age
USAD	48.52 $\pm$ 1.94	50.02 $\pm$ 1.13	73.49 $\pm$ 1.56	39.17 $\pm$ 1.68
HYPERSAGCN	51.92 $\pm$ 1.47	51.19 $\pm$ 1.88	90.37 $\pm$ 1.61	47.38 $\pm$ 1.96
GMM	53.11 $\pm$ 1.44	53.04 $\pm$ 1.73	90.92 $\pm$ 1.83	47.75 $\pm$ 1.26
GRAPHMIXER	53.17 $\pm$ 1.21	53.12 $\pm$ 1.18	91.13 $\pm$ 1.44	48.32 $\pm$ 1.11
BRAINNETCNN	49.10 $\pm$ 1.83	50.12 $\pm$ 1.57	83.58 $\pm$ 1.68	42.26 $\pm$ 2.03
BRAINNGN	50.63 $\pm$ 1.67	51.08 $\pm$ 0.96	85.25 $\pm$ 2.17	43.08 $\pm$ 1.54
FBNETGEN	50.18 $\pm$ 0.98	50.94 $\pm$ 1.39	84.47 $\pm$ 1.88	42.83 $\pm$ 1.78
ADMIRE	54.36 $\pm$ 1.39	54.87 $\pm$ 1.92	89.74 $\pm$ 1.93	47.82 $\pm$ 1.72
PTGB	55.89 $\pm$ 1.78	55.11 $\pm$ 1.62	92.58 $\pm$ 1.31	48.41 $\pm$ 1.47
BNTRANSFORMER	55.03 $\pm$ 1.35	55.17 $\pm$ 1.74	91.71 $\pm$ 1.48	47.94 $\pm$ 1.15
BRAINMIXER	<b>67.24<math>\pm</math>1.47</b>	<b>62.58<math>\pm</math>1.12</b>	<b>96.32<math>\pm</math>0.29</b>	<b>57.83<math>\pm</math>1.03</b>

254 **Data Augmentation & Negative Samples.** MLP-MIXER-based architectures are known to have  
 255 the potential of overfitting (Liu et al., 2021). To mitigate this, we perform data augmentation. For  
 256  $\mathcal{G}_F^{(t)} = (\mathcal{V}, \mathcal{E}^{(t)})$ , in patch extraction, we randomly mask  $p$  connections and then we sample temporal  
 257 walks to generate new patches. Note that, at the end, each patch is an induced subgraph and might  
 258 include masked connections as well. Furthermore, to generate negative samples: ① To corrupt the  
 259 functional connectivity, we randomly change one endpoint of a subset of connections. ② To corrupt  
 260 the timeseries, we follow existing studies (Yue et al., 2022; Woo et al., 2022) on timeseries and  
 261 replace a brain signal in time window  $t$  with another signal that is randomly selected from the batch.  
 262 Given a pre-trained model  $\mathcal{M}$ , for different downstream tasks in a semi-supervised setting, we  
 263 fine-tune  $\mathcal{M}$  using a small subset of labeled training data. Also, for each voxel, we concatenate its  
 264 encodings from VA and FC Encoders.

## 265 4 Experiments

266 **Dataset.** We use six real-world datasets: ① We present BVFC, a task-based fMRI large-scale dataset  
 267 that includes voxel activity timeseries and functional connectivity of 3 subjects when looking at  
 268 the 8460 images from 720 categories. This data is based on THINGS dataset (Hebart et al., 2023).  
 269 ② BVFC-MEG is the MEG counterpart of BVFC. ③ ADHD (Milham et al., 2011) contains data for  
 270 250 subjects in the ADHD group and 450 subjects in the typically developed (TD) control group.  
 271 ④ The Seizure detection TUH-EEG dataset (Shah et al., 2018) consists of EEG data (31 channels)  
 272 of 642 subjects. ⑤ ASD (Craddock et al., 2013) contains data for 45 subjects in the ASD group  
 273 and 45 subjects in the TD control group. ⑥ HCP (Van Essen et al., 2013) contains data from 7440  
 274 neuroimaging samples each of which is associated with one of the seven ground-truth mental states.

275 **Evaluation Tasks.** In our experiments we focus on 4 downstream tasks: ① Edge-Anomaly Detection  
 276 (AD), ② Voxel AD, ③ Brain AD, and ④ Brain Classification. For the AD tasks, we follow previous  
 277 studies (Behrouz & Seltzer, 2023a; Ma et al., 2021), and inject 1% and 5% anomalous edges into the  
 278 functional connectivity in the control group of all datasets, except BVFC, and BVFC-MEG. BVFC  
 279 and BVFC-MEG has ground-truth anomalies, the brain response of subjects when looking at not  
 280 recognizable images, generated by generative adversarial neural network BigGAN (Brock et al.,  
 281 2019). For brain classification, we focus on disease/disorder detection (in ADHD, ASD, and TUH-  
 282 EEG), the category of seen object by the subject (in BVFC, and BVFC-MEG), and age prediction and  
 283 mental state decoding (in HCP-Age, and HCP-Mental).

284 **Baselines.** For anomaly detection and graph classification tasks, we compare BRAINMIXER with  
 285 state-of-the-art time series, graph, and brain anomaly detection and learning models: ① Graph-based  
 286 methods: GOutlier (Aggarwal et al., 2011), NETWALK (Yu et al., 2018), HYPERSAGCN (Zhang  
 287 et al., 2020), Graph MLP-Mixer (GMM) (He et al., 2023), GRAPHMIXER (Cong et al., 2023).  
 288 ② brain-network-based methods: BRAINGNN (Li et al., 2021), FBNETGEN (Kan et al., 2022a),  
 289 BRAINNETCNN (Kawahara et al., 2017), ADMIRE (Behrouz & Seltzer, 2023b), and BNTRANS-  
 290 FORMER (Kan et al., 2022b), PTGB (Yang et al., 2023b). ③ Time-series-based methods: USAD (Au-  
 291 dibert et al., 2020), Time Series Transformer (TST) (Zerveas et al., 2021), and MVTS (Potter et al.,  
 292 2022). We may exclude some baselines in some tasks as they cannot be applied in that setting. The  
 293 details of baselines can be found in Appendix F.1.





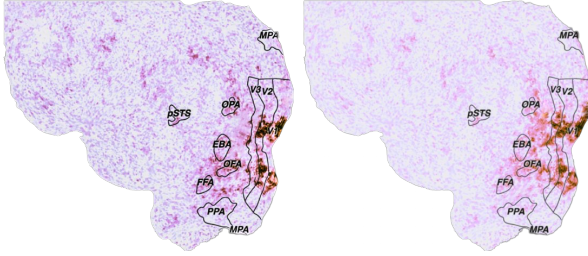


Figure 2: Average distribution of brain activities in the visual cortex when seeing (Left) GAN-generated images, (Right) Normal image.

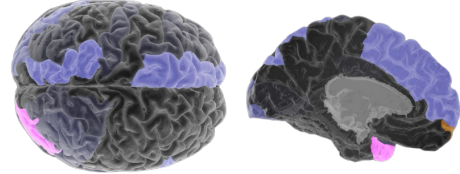


Figure 3: The distribution of detected abnormal voxels by BRAINMIXER in condition ADHD group.

316 BRAINMIXER with one module modification: row 2 removes the pre-training phase, row 3 removes  
 317 the VA Encoder module, row 4 removes FC Encoder module, row 5 removes functional patching and  
 318 randomly patches voxels, row replaces TPMIXER with MEAN(.) pooling, row 7 replaces dynamic  
 319 with static self-attention, row 8 removes time encoder, the last row set  $\theta = 0$ , removing biased in the  
 320 sampling. These results show that each component is critical for achieving BRAINMIXER’s superior  
 321 performance. The greatest contribution comes from biased sampling, VA and FC encoders, functional  
 322 patching, and dynamic self-attention, respectively.

323 **Parameter Sensitivity.** We discuss the effect of the number of walks,  $M$ , the walk length,  $m$ , and time  
 324 decay,  $\theta$  on the performance in [Appendix G](#). Results show that increasing the number of walks results  
 325 in better performance as each patch is a better representation of the node’s neighborhood. The effect  
 326 of the walk length on performance peaks at a certain point, but the exact value varies with datasets. In  
 327 [Appendix G](#), we further discuss how aggregating timeseries to obtain beta weights and aggregating  
 328 voxels to obtain ROIs can affect performance.

329 **How Does Brain Detect GAN Generated Images?** The visual cortex, responsible for processing  
 330 visual information, is hierarchically organized with multiple layers building upon simpler features  
 331 at lower stages ([Van Essen & Maunsell, 1983](#)). Initially, neurons detect edges and colors, but on  
 332 deeper levels, they specialize in recognizing more complex patterns and objects. [Figure 2](#) (Left)  
 333 (resp. (Right)) reports the average distribution of brain activity of a subject when looking at non-  
 334 recognizable images (resp. natural images). Interestingly, while the distributions share similar  
 335 patterns in lower levels (e.g., V1 and V2 voxels), higher-level voxels (e.g., V3) are less active when  
 336 the subject sees non-recognizable images.

337 **Case Study: ADHD** In this case study, we train our model on the neuroimages of the typically  
 338 developed group and test it on the ADHD condition group to detect abnormal voxel activities that  
 339 might be correlated to ADHD symptoms. [Figure 3](#) reports the distribution of anomalous voxels within  
 340 the brain of the ADHD group. 78% of all found abnormal voxel activities by BRAINMIXER are  
 341 located in the Frontal Pole, Left and Right Temporal Poles, and Lingual Gyrus. Surprisingly, these  
 342 findings are consistent with previous studies on ADHD, which use diffusion tensor imaging ([Lei  
 343 et al., 2014](#)) and Forman–Ricci curvature changes ([Chatterjee et al., 2021](#)).

## 344 5 Conclusion

345 In this work, we present an unsupervised pre-training framework, BRAINMIXER, that bridges the  
 346 representation learning of voxel activity and functional connectivity by maximizing their mutual  
 347 information. BRAINMIXER presents two novel variations of MLP-MIXER to multivariate timeseries  
 348 (VA Encoder) and graphs (FC Encoder) that both take advantage of special properties of the brain to  
 349 obtain effective representations of voxels. Consequently, the experimental results show the potential  
 350 of BRAINMIXER in ① detecting abnormal brain activity that might cause a brain disease/disorder,  
 351 ② disease/disorder detection, and ③ understanding object representation in the brain. Experiments  
 352 further support the significance of each BRAINMIXER’s component and show its superior performance  
 353 compared to the state-of-the-art in a variety of tasks. We discuss potential limitations and future work  
 354 in [Appendix H](#).

## 355 References

- 356 Charu C. Aggarwal, Yuchen Zhao, and Philip S. Yu. Outlier detection in graph streams. In *2011*  
357 *IEEE 27th International Conference on Data Engineering*, pp. 399–409, 2011. doi: 10.1109/ICDE.  
358 2011.5767885.
- 359 Julien Audibert, Pietro Michiardi, Frédéric Guyard, Sébastien Marti, and Maria A Zuluaga. Usad:  
360 Unsupervised anomaly detection on multivariate time series. In *Proceedings of the 26th ACM*  
361 *SIGKDD international conference on knowledge discovery & data mining*, pp. 3395–3404, 2020.
- 362 Lev Kiar Avberšek and Grega Repovš. Deep learning in neuroimaging data analysis: applications,  
363 challenges, and solutions. *Frontiers in neuroimaging*, 1:981642, 2022.
- 364 Jimmy Lei Ba, Jamie Ryan Kiros, and Geoffrey E. Hinton. Layer normalization, 2016.
- 365 Philip Bachman, R Devon Hjelm, and William Buchwalter. Learning representations by maximizing  
366 mutual information across views. In H. Wallach, H. Larochelle, A. Beygelzimer, F. d'Alché-Buc,  
367 E. Fox, and R. Garnett (eds.), *Advances in Neural Information Processing Systems*, volume 32. Cur-  
368 ran Associates, Inc., 2019. URL [https://proceedings.neurips.cc/paper\\_files/paper/](https://proceedings.neurips.cc/paper_files/paper/2019/file/ddf354219aac374f1d40b7e760ee5bb7-Paper.pdf)  
369 [2019/file/ddf354219aac374f1d40b7e760ee5bb7-Paper.pdf](https://proceedings.neurips.cc/paper_files/paper/2019/file/ddf354219aac374f1d40b7e760ee5bb7-Paper.pdf).
- 370 Ali Behrouz and Margo Seltzer. Anomaly detection in multiplex dynamic networks: from blockchain  
371 security to brain disease prediction. In *NeurIPS 2022 Temporal Graph Learning Workshop*, 2022.  
372 URL <https://openreview.net/forum?id=UDGZDfwmay>.
- 373 Ali Behrouz and Margo Seltzer. Anomaly detection in human brain via inductive learning on temporal  
374 multiplex networks. In *Machine Learning for Healthcare Conference*, volume 219. PMLR, 2023a.
- 375 Ali Behrouz and Margo Seltzer. ADMIRE++: Explainable anomaly detection in the human brain  
376 via inductive learning on temporal multiplex networks. In *ICML 3rd Workshop on Interpretable*  
377 *Machine Learning in Healthcare (IMLH)*, 2023b. URL [https://openreview.net/forum?id=](https://openreview.net/forum?id=t4H8acYudJ)  
378 [t4H8acYudJ](https://openreview.net/forum?id=t4H8acYudJ).
- 379 Ali Behrouz, Farnoosh Hashemi, Sadaf Sadeghian, and Margo Seltzer. CAT-walk: Inductive  
380 hypergraph learning via set walks. In *Thirty-seventh Conference on Neural Information Processing*  
381 *Systems*, 2023. URL <https://openreview.net/forum?id=QG4nJBNEar>.
- 382 Signe L Bray, Catie Chang, and Fumiko Hoefft. Applications of multivariate pattern classification  
383 analyses in developmental neuroimaging of healthy and clinical populations. *Frontiers in human*  
384 *neuroscience*, 3:898, 2009.
- 385 Andrew Brock, Jeff Donahue, and Karen Simonyan. Large scale GAN training for high fidelity  
386 natural image synthesis. In *International Conference on Learning Representations*, 2019. URL  
387 <https://openreview.net/forum?id=B1xsqj09Fm>.
- 388 Donghong Cai, Junru Chen, Yang Yang, Teng Liu, and Yafeng Li. Mbrain: A multi-channel self-  
389 supervised learning framework for brain signals. In *Proceedings of the 29th ACM SIGKDD*  
390 *Conference on Knowledge Discovery and Data Mining, KDD '23*, pp. 130–141, New York, NY,  
391 USA, 2023. Association for Computing Machinery. ISBN 9798400701030. doi: 10.1145/3580305.  
392 3599426. URL <https://doi.org/10.1145/3580305.3599426>.
- 393 Vince D. Calhoun, Robyn Miller, Godfrey Pearlson, and Tulay Adali. The chronnectome: Time-  
394 varying connectivity networks as the next frontier in fmri data discovery. *Neuron*, 84(2):262–  
395 274, 2014. ISSN 0896-6273. doi: <https://doi.org/10.1016/j.neuron.2014.10.015>. URL <https://www.sciencedirect.com/science/article/pii/S0896627314009131>.
- 396
- 397 Martin J Chadwick, Heidi M Bonnici, and Eleanor A Maguire. Decoding information in the human  
398 hippocampus: a user’s guide. *Neuropsychologia*, 50(13):3107–3121, 2012.
- 399 Benjamin Paul Chamberlain, Sergey Shirobokov, Emanuele Rossi, Fabrizio Frasca, Thomas  
400 Markovich, Nils Yannick Hammerla, Michael M. Bronstein, and Max Hansmire. Graph neural  
401 networks for link prediction with subgraph sketching. In *The Eleventh International Conference on*  
402 *Learning Representations*, 2023. URL <https://openreview.net/forum?id=m1oqE0AozQU>.

- 403 Tanima Chatterjee, Réka Albert, Stuti Thapliyal, Nazanin Azarhooshang, and Bhaskar DasGupta. De-  
404 tecting network anomalies using forman–ricci curvature and a case study for human brain networks.  
405 *Scientific Reports*, 11(1):8121, Apr 2021. ISSN 2045-2322. doi: 10.1038/s41598-021-87587-z.  
406 URL <https://doi.org/10.1038/s41598-021-87587-z>.
- 407 Gang Chen, B Douglas Ward, Chunming Xie, Wenjun Li, Zhilin Wu, Jennifer L Jones, Malgorzata  
408 Franczak, Piero Antuono, and Shi-Jiang Li. Classification of alzheimer disease, mild cognitive  
409 impairment, and normal cognitive status with large-scale network analysis based on resting-state  
410 functional mr imaging. *Radiology*, 259(1):213, 2011.
- 411 Si-An Chen, Chun-Liang Li, Nate Yoder, Sercan O Arik, and Tomas Pfister. Tsmixer: An all-mlp  
412 architecture for time series forecasting. *arXiv preprint arXiv:2303.06053*, 2023.
- 413 Rewon Child, Scott Gray, Alec Radford, and Ilya Sutskever. Generating long sequences with sparse  
414 transformers. *arXiv preprint arXiv:1904.10509*, 2019.
- 415 Weilin Cong, Si Zhang, Jian Kang, Baichuan Yuan, Hao Wu, Xin Zhou, Hanghang Tong, and  
416 Mehrdad Mahdavi. Do we really need complicated model architectures for temporal networks?  
417 In *The Eleventh International Conference on Learning Representations*, 2023. URL <https://openreview.net/forum?id=ayPPc0SyLv1>.  
418 <https://openreview.net/forum?id=ayPPc0SyLv1>.
- 419 Aurelio Cortese, Saori C Tanaka, Kaoru Amano, Ai Koizumi, Hakwan Lau, Yuka Sasaki, Kazuhisa  
420 Shibata, Vincent Taschereau-Dumouchel, Takeo Watanabe, and Mitsuo Kawato. The decnef  
421 collection, fmri data from closed-loop decoded neurofeedback experiments. *Scientific data*, 8(1):  
422 65, 2021.
- 423 Cameron Craddock, Yassine Benhajali, Carlton Chu, Francois Chouinard, Alan Evans, András Jakab,  
424 Budhachandra Singh Khundrakpam, John David Lewis, Qingyang Li, Michael Milham, et al.  
425 The neuro bureau preprocessing initiative: open sharing of preprocessed neuroimaging data and  
426 derivatives. *Frontiers in Neuroinformatics*, 7:27, 2013.
- 427 Alexander Craik, Yongtian He, and Jose L Contreras-Vidal. Deep learning for electroencephalogram  
428 (eeg) classification tasks: a review. *Journal of neural engineering*, 16(3):031001, 2019.
- 429 Hejie Cui, Wei Dai, Yanqiao Zhu, Xiaoxiao Li, Lifang He, and Carl Yang. Interpretable graph neural  
430 networks for connectome-based brain disorder analysis. In *International Conference on Medical  
431 Image Computing and Computer-Assisted Intervention*, pp. 375–385. Springer, 2022.
- 432 Fernando Lopes da Silva. Neural mechanisms underlying brain waves: from neural membranes to  
433 networks. *Electroencephalography and clinical neurophysiology*, 79(2):81–93, 1991.
- 434 Alexey Dosovitskiy, Lucas Beyer, Alexander Kolesnikov, Dirk Weissenborn, Xiaohua Zhai, Thomas  
435 Unterthiner, Mostafa Dehghani, Matthias Minderer, Georg Heigold, Sylvain Gelly, Jakob Uszkoreit,  
436 and Neil Houlsby. An image is worth 16x16 words: Transformers for image recognition at scale.  
437 In *International Conference on Learning Representations*, 2021. URL [https://openreview.  
438 net/forum?id=YicbFdNTTy](https://openreview.net/forum?id=YicbFdNTTy).
- 439 Yuhui Du, Zening Fu, and Vince D Calhoun. Classification and prediction of brain disorders using  
440 functional connectivity: promising but challenging. *Frontiers in neuroscience*, 12:525, 2018.
- 441 Javier Gonzalez-Castillo and Peter A Bandettini. Task-based dynamic functional connectivity: Recent  
442 findings and open questions. *Neuroimage*, 180:526–533, 2018.
- 443 Michael Greicius. Resting-state functional connectivity in neuropsychiatric disorders. *Current  
444 opinion in neurology*, 21(4):424–430, 2008.
- 445 Yanming Guo, Yu Liu, Ard Oerlemans, Songyang Lao, Song Wu, and Michael S Lew. Deep learning  
446 for visual understanding: A review. *Neurocomputing*, 187:27–48, 2016.
- 447 Michael Gutmann and Aapo Hyvärinen. Noise-contrastive estimation: A new estimation principle  
448 for unnormalized statistical models. In *Proceedings of the thirteenth international conference on  
449 artificial intelligence and statistics*, pp. 297–304. JMLR Workshop and Conference Proceedings,  
450 2010.

- 451 Xiaoxin He, Bryan Hooi, Thomas Laurent, Adam Perold, Yann LeCun, and Xavier Bresson. A  
452 generalization of vit/mlp-mixer to graphs. In *International Conference on Machine Learning*, pp.  
453 12724–12745. PMLR, 2023.
- 454 Martin N Hebart, Oliver Contier, Lina Teichmann, Adam H Rockter, Charles Y Zheng, Alexis Kidder,  
455 Anna Corriveau, Maryam Vaziri-Pashkam, and Chris I Baker. Things-data, a multimodal collection  
456 of large-scale datasets for investigating object representations in human brain and behavior. *Elife*,  
457 12:e82580, 2023.
- 458 Dan Hendrycks and Kevin Gimpel. Gaussian error linear units (gelus), 2020.
- 459 Leanna M Hernandez, Jeffrey D Rudie, Shulamite A Green, Susan Bookheimer, and Mirella Dapretto.  
460 Neural signatures of autism spectrum disorders: insights into brain network dynamics. *Neuropsychopharmacology*, 40(1):171–189, 2015.
- 462 R Devon Hjelm, Alex Fedorov, Samuel Lavoie-Marchildon, Karan Grewal, Phil Bachman, Adam  
463 Trischler, and Yoshua Bengio. Learning deep representations by mutual information estimation  
464 and maximization. In *International Conference on Learning Representations*, 2019. URL <https://openreview.net/forum?id=Bklr3j0cKX>.
- 466 Tomoyasu Horikawa and Yukiyasu Kamitani. Generic decoding of seen and imagined objects using  
467 hierarchical visual features. *Nature communications*, 8(1):15037, 2017.
- 468 Yang Hu, Haoxuan You, Zhecan Wang, Zhicheng Wang, Erjin Zhou, and Yue Gao. Graph-mlp: Node  
469 classification without message passing in graph. *arXiv preprint arXiv:2106.04051*, 2021.
- 470 R Matthew Hutchison, Thilo Womelsdorf, Elena A Allen, Peter A Bandettini, Vince D Calhoun,  
471 Maurizio Corbetta, Stefania Della Penna, Jeff H Duyn, Gary H Glover, Javier Gonzalez-Castillo,  
472 et al. Dynamic functional connectivity: promise, issues, and interpretations. *Neuroimage*, 80:  
473 360–378, 2013.
- 474 Yuli Jiang, Yu Rong, Hong Cheng, Xin Huang, Kangfei Zhao, and Junzhou Huang. Query driven-  
475 graph neural networks for community search: From non-attributed, attributed, to interactive  
476 attributed, 2021. URL <https://arxiv.org/abs/2104.03583>.
- 477 Biao Jie, Mingxia Liu, Xi Jiang, and Daoqiang Zhang. Sub-network based kernels for brain net-  
478 work classification. In *Proceedings of the 7th ACM International Conference on Bioinformatics,*  
479 *Computational Biology, and Health Informatics*, pp. 622–629, 2016.
- 480 Xuan Kan, Hejie Cui, Joshua Lukemire, Ying Guo, and Carl Yang. Fbnetgen: Task-aware gnn-based  
481 fmri analysis via functional brain network generation. In *International Conference on Medical*  
482 *Imaging with Deep Learning*, pp. 618–637. PMLR, 2022a.
- 483 Xuan Kan, Wei Dai, Hejie Cui, Zilong Zhang, Ying Guo, and Carl Yang. Brain network transformer.  
484 In Alice H. Oh, Alekh Agarwal, Danielle Belgrave, and Kyunghyun Cho (eds.), *Advances in*  
485 *Neural Information Processing Systems*, 2022b. URL [https://openreview.net/forum?id=](https://openreview.net/forum?id=1cJ1cbA6NLN)  
486 [1cJ1cbA6NLN](https://openreview.net/forum?id=1cJ1cbA6NLN).
- 487 Jeremy Kawahara, Colin J Brown, Steven P Miller, Brian G Booth, Vann Chau, Ruth E Grunau, Jill G  
488 Zwicker, and Ghassan Hamarneh. Brainnetcnn: Convolutional neural networks for brain networks;  
489 towards predicting neurodevelopment. *NeuroImage*, 146:1038–1049, 2017.
- 490 Tommaso Lanciano, Francesco Bonchi, and Aristides Gionis. Explainable classification of brain net-  
491 works via contrast subgraphs. In *Proceedings of the 26th ACM SIGKDD International Conference*  
492 *on Knowledge Discovery; Data Mining, KDD '20*, pp. 3308–3318, New York, NY, USA, 2020.  
493 Association for Computing Machinery. ISBN 9781450379984. doi: 10.1145/3394486.3403383.  
494 URL <https://doi.org/10.1145/3394486.3403383>.
- 495 Sue-Hyun Lee and Chris I Baker. Multi-voxel decoding and the topography of maintained information  
496 during visual working memory. *Frontiers in systems neuroscience*, 10:2, 2016.
- 497 Du Lei, Jun Ma, Xiaoxia Du, Guohua Shen, Xingming Jin, and Qiyong Gong. Microstructural  
498 abnormalities in the combined and inattentive subtypes of attention deficit hyperactivity disorder:  
499 a diffusion tensor imaging study. *Scientific reports*, 4(1):6875, 2014.

- 500 Shiyang Li, Xiaoyong Jin, Yao Xuan, Xiyong Zhou, Wenhui Chen, Yu-Xiang Wang, and Xifeng  
501 Yan. Enhancing the locality and breaking the memory bottleneck of transformer on time series  
502 forecasting. *Advances in neural information processing systems*, 32, 2019.
- 503 Xiaoxiao Li, Yuan Zhou, Nicha Dvornek, Muhan Zhang, Siyuan Gao, Juntang Zhuang, Dustin  
504 Scheinost, Lawrence H Staib, Pamela Ventola, and James S Duncan. Brainngn: Interpretable brain  
505 graph neural network for fmri analysis. *Medical Image Analysis*, 74:102233, 2021.
- 506 Zhe Li, Zhongwen Rao, Lujia Pan, and Zenglin Xu. Mts-mixers: Multivariate time series forecasting  
507 via factorized temporal and channel mixing. *arXiv preprint arXiv:2302.04501*, 2023.
- 508 Hanxiao Liu, Zihang Dai, David So, and Quoc V Le. Pay attention to mlps. In M. Ran-  
509 zato, A. Beygelzimer, Y. Dauphin, P.S. Liang, and J. Wortman Vaughan (eds.), *Advances*  
510 *in Neural Information Processing Systems*, volume 34, pp. 9204–9215. Curran Associates,  
511 Inc., 2021. URL [https://proceedings.neurips.cc/paper\\_files/paper/2021/file/  
512 4cc05b35c2f937c5bd9e7d41d3686fff-Paper.pdf](https://proceedings.neurips.cc/paper_files/paper/2021/file/4cc05b35c2f937c5bd9e7d41d3686fff-Paper.pdf).
- 513 Xiaoxiao Ma, Jia Wu, Shan Xue, Jian Yang, Chuan Zhou, Quan Z. Sheng, Hui Xiong, and Leman  
514 Akoglu. A comprehensive survey on graph anomaly detection with deep learning. *IEEE Transac-*  
515 *tions on Knowledge and Data Engineering*, pp. 1–1, 2021. doi: 10.1109/TKDE.2021.3118815.
- 516 Abdelhak Mahmoudi, Sylvain Takerkart, Fakhita Regragui, Driss Boussaoud, Andrea Brovelli, et al.  
517 Multivoxel pattern analysis for fmri data: a review. *Computational and mathematical methods in*  
518 *medicine*, 2012, 2012.
- 519 Chris McNorgan, Gregory J Smith, and Erica S Edwards. Integrating functional connectivity and  
520 mvpa through a multiple constraint network analysis. *Neuroimage*, 208:116412, 2020.
- 521 Michael P. Milham, Jan Buitelaar, F. Xavier Castellanos, Daniel Dickstein, Damien Fair, David  
522 Kennedy, Beatric Luna, Michael P. Milham, Stewart Mostofsky, Joel Nigg, Julie B. Schweitzer,  
523 Katerina Velanova, Yu-Feng Wang, and Yu-Feng Zang. 1000 functional connectome project. *1000*  
524 *Functional Connectome Project*, 1, July 2011.
- 525 Tom M Mitchell, Rebecca Hutchinson, Marcel Adam Just, Radu S Niculescu, Francisco Pereira,  
526 and Xuerui Wang. Classifying instantaneous cognitive states from fmri data. In *AMIA annual*  
527 *symposium proceedings*, volume 2003, pp. 465. American Medical Informatics Association, 2003.
- 528 Alfonso Nieto-Castanon. Brain-wide connectome inferences using functional connectivity multivari-  
529 ate pattern analyses (fc-mvpa). *PLoS Computational Biology*, 18(11):e1010634, 2022.
- 530 Youngser Park, C Priebe, D Marchette, and Abdou Youssef. Anomaly detection using scan statistics  
531 on time series hypergraphs. In *Link Analysis, Counterterrorism and Security (LACTS) Conference*,  
532 pp. 9. SIAM Pennsylvania, 2009.
- 533 Russell A. Poldrack and Martha J. Farah. Progress and challenges in probing the human brain.  
534 *Nature*, 526(7573):371–379, Oct 2015. ISSN 1476-4687. doi: 10.1038/nature15692. URL  
535 <https://doi.org/10.1038/nature15692>.
- 536 Russell A Poldrack and Krzysztof J Gorgolewski. Making big data open: data sharing in neuroimaging.  
537 *Nature neuroscience*, 17(11):1510–1517, 2014.
- 538 İlkey Yıldız Potter, George Zerveas, Carsten Eickhoff, and Dominique Duncan. Unsupervised multi-  
539 variate time-series transformers for seizure identification on eeg. In *2022 21st IEEE International*  
540 *Conference on Machine Learning and Applications (ICMLA)*, pp. 1304–1311. IEEE, 2022.
- 541 Raimon HR Pruim, Maarten Mennes, Daan van Rooij, Alberto Llera, Jan K Buitelaar, and Christian F  
542 Beckmann. Ica-aroma: A robust ica-based strategy for removing motion artifacts from fmri data.  
543 *Neuroimage*, 112:267–277, 2015.
- 544 Zvi N. Roth and Elisha P. Merriam. Representations in human primary visual cortex drift over  
545 time. *Nature Communications*, 14(1):4422, Jul 2023. ISSN 2041-1723. doi: 10.1038/  
546 s41467-023-40144-w. URL <https://doi.org/10.1038/s41467-023-40144-w>.

- 547 Zvi N. Roth, Kendrick Kay, and Elisha P. Merriam. Natural scene sampling reveals reliable  
548 coarse-scale orientation tuning in human v1. *Nature Communications*, 13(1):6469, Oct 2022.  
549 ISSN 2041-1723. doi: 10.1038/s41467-022-34134-7. URL [https://doi.org/10.1038/  
550 s41467-022-34134-7](https://doi.org/10.1038/s41467-022-34134-7).
- 551 Ramit Sawhney, Shivam Agarwal, Arnav Wadhwa, Tyler Derr, and Rajiv Ratn Shah. Stock selection  
552 via spatiotemporal hypergraph attention network: A learning to rank approach. In *Proceedings of  
553 the AAAI Conference on Artificial Intelligence*, volume 35, pp. 497–504, 2021.
- 554 Alexander Schaefer, Ru Kong, Evan M Gordon, Timothy O Laumann, Xi-Nian Zuo, Avram J Holmes,  
555 Simon B Eickhoff, and B T Thomas Yeo. Local-Global parcellation of the human cerebral cortex  
556 from intrinsic functional connectivity MRI. *Cereb Cortex*, 28(9):3095–3114, September 2018.
- 557 Steffen Schneider, Jin Hwa Lee, and Mackenzie Weygandt Mathis. Learnable latent embeddings for  
558 joint behavioural and neural analysis. *Nature*, pp. 1–9, 2023.
- 559 Vinit Shah, Eva Von Weltin, Silvia Lopez, James Riley McHugh, Lillian Veloso, Meysam Golmo-  
560 hammadi, Iyad Obeid, and Joseph Picone. The temple university hospital seizure detection corpus.  
561 *Frontiers in neuroinformatics*, 12:83, 2018.
- 562 Afshin Shoeibi, Marjane Khodatars, Navid Ghassemi, Mahboobeh Jafari, Parisa Moridian, Roohallah  
563 Alizadehsani, Maryam Panahiazar, Fahime Khozeimeh, Assef Zare, Hossein Hosseini-Nejad, et al.  
564 Epileptic seizures detection using deep learning techniques: A review. *International Journal of  
565 Environmental Research and Public Health*, 18(11):5780, 2021.
- 566 Stephen M Smith, Diego Vidaurre, Christian F Beckmann, Matthew F Glasser, Mark Jenkinson,  
567 Karla L Miller, Thomas E Nichols, Emma C Robinson, Gholamreza Salimi-Khorshidi, Mark W  
568 Woolrich, Deanna M Barch, Kamil Uğurbil, and David C Van Essen. Functional connectomics  
569 from resting-state fMRI. *Trends Cogn Sci*, 17(12):666–682, November 2013.
- 570 B Sundermann, D Herr, W Schwindt, and B Pfeleiderer. Multivariate classification of blood oxygen  
571 level-dependent fmri data with diagnostic intention: a clinical perspective. *American Journal of  
572 neuroradiology*, 35(5):848–855, 2014.
- 573 Ilya Tolstikhin, Neil Houlsby, Alexander Kolesnikov, Lucas Beyer, Xiaohua Zhai, Thomas Un-  
574 terthiner, Jessica Yung, Andreas Peter Steiner, Daniel Keysers, Jakob Uszkoreit, Mario Lucic,  
575 and Alexey Dosovitskiy. MLP-mixer: An all-MLP architecture for vision. In A. Beygelzimer,  
576 Y. Dauphin, P. Liang, and J. Wortman Vaughan (eds.), *Advances in Neural Information Processing  
577 Systems*, 2021. URL <https://openreview.net/forum?id=EI2K0XKdnP>.
- 578 Lucina Q Uddin, DR Dajani, W Voorhies, H Bednarz, and RK Kana. Progress and roadblocks  
579 in the search for brain-based biomarkers of autism and attention-deficit/hyperactivity disorder.  
580 *Translational psychiatry*, 7(8):e1218–e1218, 2017.
- 581 Martijn P Van Den Heuvel and Hilleke E Hulshoff Pol. Exploring the brain network: a review on  
582 resting-state fmri functional connectivity. *European neuropsychopharmacology*, 20(8):519–534,  
583 2010.
- 584 David C Van Essen and John HR Maunsell. Hierarchical organization and functional streams in the  
585 visual cortex. *Trends in neurosciences*, 6:370–375, 1983.
- 586 David C Van Essen, Stephen M Smith, Deanna M Barch, Timothy EJ Behrens, Essa Yacoub, Kamil  
587 Ugurbil, Wu-Minn HCP Consortium, et al. The wu-minn human connectome project: an overview.  
588 *Neuroimage*, 80:62–79, 2013.
- 589 Eliana Vassena, James Deraeve, and William H. Alexander. Surprise, value and control in anterior  
590 cingulate cortex during speeded decision-making. *Nature Human Behaviour*, 4(4):412–422, Apr  
591 2020. ISSN 2397-3374. doi: 10.1038/s41562-019-0801-5. URL [https://doi.org/10.1038/  
592 s41562-019-0801-5](https://doi.org/10.1038/s41562-019-0801-5).
- 593 Petar Veličković, Guillem Cucurull, Arantxa Casanova, Adriana Romero, Pietro Liò, and Yoshua  
594 Bengio. Graph attention networks. In *International Conference on Learning Representations*,  
595 2018. URL <https://openreview.net/forum?id=rJXMpikCZ>.

- 596 Yanbang Wang, Yen-Yu Chang, Yunyu Liu, Jure Leskovec, and Pan Li. Inductive representation  
597 learning in temporal networks via causal anonymous walks. In *International Conference on*  
598 *Learning Representations*, 2021. URL <https://openreview.net/forum?id=KYPz4YsCPj>.
- 599 Chong-Yaw Wee, Pew-Thian Yap, Wenbin Li, Kevin Denny, Jeffrey N Browndyke, Guy G Potter,  
600 Kathleen A Welsh-Bohmer, Lihong Wang, and Dinggang Shen. Enriched white matter connectivity  
601 networks for accurate identification of mci patients. *Neuroimage*, 54(3):1812–1822, 2011.
- 602 Gerald Woo, Chenghao Liu, Doyen Sahoo, Akshat Kumar, and Steven Hoi. CoST: Contrastive  
603 learning of disentangled seasonal-trend representations for time series forecasting. In *International*  
604 *Conference on Learning Representations*, 2022. URL [https://openreview.net/forum?id=](https://openreview.net/forum?id=P1lZY3omXV2)  
605 [P1lZY3omXV2](https://openreview.net/forum?id=P1lZY3omXV2).
- 606 Daniel LK Yamins and James J DiCarlo. Using goal-driven deep learning models to understand  
607 sensory cortex. *Nature neuroscience*, 19(3):356–365, 2016.
- 608 Huzheng Yang, James Gee, and Jianbo Shi. Memory encoding model, 2023a.
- 609 Yi Yang, Hejie Cui, and Carl Yang. \ours: Pre-train graph neural networks for brain network analysis.  
610 In *Conference on Health, Inference, and Learning*, pp. 526–544. PMLR, 2023b.
- 611 Wenchao Yu, Wei Cheng, Charu C. Aggarwal, Kai Zhang, Haifeng Chen, and Wei Wang. Netwalk: A  
612 flexible deep embedding approach for anomaly detection in dynamic networks. In *Proceedings of*  
613 *the 24th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining*, KDD  
614 '18, pp. 2672–2681, New York, NY, USA, 2018. Association for Computing Machinery. ISBN  
615 9781450355520. doi: 10.1145/3219819.3220024. URL [https://doi.org/10.1145/3219819.](https://doi.org/10.1145/3219819.3220024)  
616 [3220024](https://doi.org/10.1145/3219819.3220024).
- 617 Zhihan Yue, Yujing Wang, Juanyong Duan, Tianmeng Yang, Congrui Huang, Yunhai Tong, and  
618 Bixiong Xu. Ts2vec: Towards universal representation of time series. In *Proceedings of the AAAI*  
619 *Conference on Artificial Intelligence*, volume 36, pp. 8980–8987, 2022.
- 620 George Zerveas, Srideepika Jayaraman, Dhaval Patel, Anuradha Bhamidipaty, and Carsten Eickhoff.  
621 A transformer-based framework for multivariate time series representation learning. In *Proceedings*  
622 *of the 27th ACM SIGKDD conference on knowledge discovery & data mining*, pp. 2114–2124,  
623 2021.
- 624 Ruochi Zhang, Yuesong Zou, and Jian Ma. Hyper-sagmn: a self-attention based graph neural  
625 network for hypergraphs. In *International Conference on Learning Representations*, 2020. URL  
626 <https://openreview.net/forum?id=ryeHuJBtPH>.
- 627 Yanqiao Zhu, Hejie Cui, Lifang He, Lichao Sun, and Carl Yang. Joint embedding of structural and  
628 functional brain networks with graph neural networks for mental illness diagnosis. In *2022 44th*  
629 *Annual International Conference of the IEEE Engineering in Medicine & Biology Society (EMBC)*,  
630 pp. 272–276. IEEE, 2022.