DEPFOLD: RNA SECONDARY STRUCTURE PREDIC-TION AS DEPENDENCY PARSING

Anonymous authors

000

001

002003004

010 011

012

013

014

015

016

017

018

019

021

024

025

026

027

028

029

031

032

034

037

040

041

042

043

044

045

046

047

048

051

052

Paper under double-blind review

ABSTRACT

RNA secondary structure prediction is critical for understanding RNA function but remains challenging due to complex structural elements like pseudoknots and limited training data. We introduce DEPfold, a novel deep learning approach that reframes RNA secondary structure prediction as a dependency parsing problem. DEPfold presents three key innovations: (1) a biologically motivated transformation of RNA structures into labeled dependency trees, (2) a biaffine attention mechanism for joint prediction of base pairings and their types, and (3) an optimal tree decoding algorithm that enforces valid RNA structural constraints. Unlike traditional energy-based methods, DEPfold learns directly from annotated data and leverages pretrained language models to capture intricate RNA patterns. We evaluate DEPfold on both within-family and cross-family RNA datasets, demonstrating significant performance improvements over existing methods. On the RNAStrAlign dataset, DEPfold achieves an F₁ score of 0.985, predicting pseudoknots and long-range interactions. Notably, DEPfold shows strong performance in cross-family generalization when trained on data augmented by traditional energybased models, outperforming existing methods on the bpRNA-new dataset. This demonstrates DEPfold's ability to effectively learn structural information beyond what traditional methods capture. Our approach bridges natural language processing (NLP) with RNA biology, providing a computationally efficient and adaptable tool for advancing RNA structure prediction and analysis. 1

1 Introduction

Ribonucleic acid (RNA) molecules play crucial roles in biological processes, including gene expression regulation, protein synthesis, and gene editing systems such as CRISPR-Cas9 (Atkins et al., 2011; Sullenger & Nair, 2016; Grabow & Jaeger, 2014). RNA consists of an ordered sequence of nucleotides, each containing one of four bases: *adenine* (A), guanine (G), cytosine (C), and uracil (U). This sequence is referred to as the RNA's primary structure. These bases can form pairs, defining the secondary structure, as illustrated in Figure 1.

The function of RNA is closely related to its secondary structure. Accurate prediction of these structures is essential for understanding RNA functional mechanisms, designing RNA-targeted drugs, and studying RNA evolution (Puzzarini & Barone, 2018; Saini et al.,

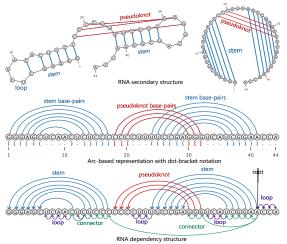


Figure 1: RNA secondary structure example and its corresponding dependency structure

2021). While experimental methods such as X-ray crystallography, nuclear magnetic resonance, and cryo-electron microscopy can determine RNA structures (Zhang et al., 2022; Kappel et al., 2020),

Our code is available at https://anonymized.

these approaches are generally limited by low throughput and high costs. The RNAcentral database has cataloged over 24 million non-coding RNA sequences, yet only a tiny fraction have experimentally determined structures (rna, 2015). RNA secondary structure prediction is a fundamental problem in biology, and serves wetlab biologists in tasks such as drug discovery Oluoch et al. (2018) and cell analysis (Sethi et al., 2013).

Currently, there are two main methods for RNA structure prediction: energy-based methods and statistical and deep learning methods (Hajiaghayi et al., 2012). With energy based methods, the main prediction algorithm relies on minimising, in an inference procedure, an energy objective that describes the alignment between the different nucleotides in the RNA sequence. Deep learning methods, on the other hand, rely on the usual machine learning setup, with a training set from which a structured prediction model is learned.

While energy-based models are overall more stable because they do not rely on training and are not sensitive to the distribution of the data they were trained on as deep learning models, their overall performance is often not very high when compared to deep learning models tested *within distribution*. Deep learning models do not generalize well out of their training distribution, because the amount of RNA sequenced data is small, for example, compared to proteins, where very large models such as AlphaFold (Jumper et al., 2021) are state of the art.

We balance these two issues, and motivated by NLP research on dependency parsing,² we develop **DEPfold**, an RNA structure prediction model, in which dependency parsing supports the following:

- A more detailed annotated structure than just basic alignment between nucleotides. This refined structures makes the learning problem easier for the underlying dependency model, as it provides additional constraints to the RNA structure, such as explicitly modeling *unaligned* nucleotides.
- A nested structure that follows the underlying assumptions for RNA structures. Pseudoknots³ excluded, there is an underlying understanding that RNA structures are nested, and this is the reason why often models such as context-free grammars have been used for them (Knudsen & Hein, 1999; Do et al., 2006a). Our dependency model, while locally directly models the alignment between the different nucleotides, also has a global constraint in the form of a dependency trees that follows a nested structure.
- When pseudoknots are being included in the prediction problem, we can support that additional
 modification by changing the underlying inference algorithm for the dependency parsing model.
 Pseudoknots, we find, are equivalent to adding a certain level of *non-projectivity* to the dependency parsing model, as both notions indicate edges that cross each other in the dependency tree.
- Our dependency formulation model is built in such a way that it is easy to incorporate further constraints to the inference problem, such as energy-based constraints. This yields a hybrid model that balances well between learning from data and relying on a physical energy model originating in molecular biology (Zuker & Stiegler, 1981).
- Our approach relies on an encoding model to transform the RNA sequence into a sequence of embeddings. This component is plug-in, and can be used, for example, with a foundation model for RNA structures.

DEPfold adapts the biaffine parser of Dozat & Manning (2016), which uses deep biaffine attention to compute dependency relations. This parser decomposes the task into two modules: one predicting the existence of directed edges between nucleotides, and another predicting the best label for each potential edge. By transforming RNA structures into labeled dependency trees, DEPfold leverages the power of dependency parsing while maintaining biological constraints. This approach effectively predicts both the existence and types of base pairings, including pseudoknots, and can handle RNA sequences exceeding 3000 nucleotides. We conduct extensive experiments to compare DEPfold with state-of-the-art methods on several benchmark datasets, demonstrating its superior performance, particularly in predicting pseudoknots and long-range interactions. Moreover, DEPfold shows strong cross-family generalization when trained on augmented data, suggesting effective learning of structural information beyond traditional methods.

²Dependency parsing is the problem of identifying a syntactic structure for natural language sentence by identifying head-dependent relationships between words. See Kübler et al. (2009)

³Pseudoknots are a unique and relatively unique type of bonds between nucleotides that violate nestedness in a tree

2 BACKGROUND AND NOTATION

Our RNA structure prediction algorithm relies on **dependency parsing**, a method in NLP that provides syntactic structures to natural language utterances (Kübler et al., 2009). These syntactic structures originate the syntactic theory of Tesnière (2015) called dependency grammar. At the core of this theory, it is stipulated that there is a head-dependent relationship between words in a sentence, described as edges between the different words that all together constitute a dependency parse tree. More formally, given an input sentence $x = w_0 w_1 \dots w_n$, where $w_i \in \Sigma$ (an alphabet or a vocabulary), a dependency tree, as illustrated in Figure 1, is defined as $y = \{(i,j,\ell), 0 \le i \le n, 1 \le j \le n, \ell \in \mathcal{L}\}$, where (i,j,ℓ) represents a dependency relation $\ell \in \mathcal{L}$ from the head word w_i to the modifier word w_j . In our case, the words are the nucleotides, and the edges between them describe alignment (or lack of) relationships between them. Dependency trees can be directed or undirected. While the alignments between nucleotides is undirected (corresponding to stem structures), we use a directed formalism to model more freely both alignment between nucleotides and lack thereof.

RNA consists of an ordered sequence of nucleotides, each containing one of four bases: adenine(A), guanine(G), cytosine(C), and uracil(U). Hence, we denote by $\mathcal{X} = \Sigma^*$ where $\Sigma = \{A, G, U, C\}$, the set of RNA sequences, by \mathcal{Y} the set of RNA structures (in the form of Figure 1) and by \mathcal{Z} the set of all dependency trees over RNA sequences from \mathcal{X} . In RNA secondary structures, each nucleotide pairs with at most one other nucleotide, forming structures such as stems and loops(Turner & Mathews, 2009). For clarity, we refer to these base-paired structures as stems, and the unpaired nucleotides form loops, as illustrated in Figure 1. A unique structural motif frequently observed in RNA is the pseudoknot, a double-helical structure formed by base pairing between single-stranded regions within stem-loop structures and external complementary sequences(Naderi et al., 2021). Formally, a pseudoknot occurs when an RNA has two base pairs, i-j and i'-j', such that i < i' < j < j' (Achawanantakun & Sun, 2013). Pseudoknots can function as independent elements or as parts of complex RNA structures, participating in stabilization, replication, RNA processing, toxin inactivation, and gene expression control(Brierley et al., 2007; 2008; Giedroc & Cornish, 2009). Therefore, predicting pseudoknots is of significant importance.

In this study, we adopt two methods to represent RNA secondary structures. The first is the *arc representation*, where nucleotides are depicted as vertices and hydrogen bonds as arcs (Figure 1). For secondary structures without pseudoknots, all arcs are nested or parallel; crossed arcs indicate the presence of pseudoknots. The second method is the *dot-bracket notation*, where a . represents an unpaired base (loop base), and paired brackets denote base pairs. In this notation, base pairs forming stems are denoted by parentheses '()', and base pairs forming pseudoknots can be distinguished from stems by using square brackets'[]', angle brackets ' $\langle \rangle$ ', and so on.

RNA secondary structures are crucial for determining the molecule's three-dimensional conformation and functional properties (Tinoco Jr & Bustamante, 1999). Accurate prediction of these structures aids in inferring tertiary interactions and has applications in drug design(Khatoon et al., 2014), gene regulation studies (Mortimer et al., 2014), and RNA-based therapeutics (Yin et al., 2014). By modeling stems, loops, and pseudoknots, we aim to capture the full complexity of RNA secondary structures, enabling more accurate predictions and a deeper understanding of RNA functionality.

3 DEPFOLD: METHODOLOGY

3.1 Transformation of RNA Structures to Dependency

At the core of our algorithm, there is a mapping between RNA structures and dependency trees. Let $\tau\colon\mathcal{Y}\to\mathcal{Z}$ be such a mapping. The dependency tree $z=\tau(y)$ attached to y includes all the alignment information in y, but also additional annotation, such as relationships of "lack of alignment." This additional fine-grained annotated structure further constrains and informs the learning algorithm, and also formulates the basic alignment relationship as a nested structure, following works for grammar-based and energy-based RNA structure prediction (Rivas & Eddy, 1999; Zuker & Stiegler, 1981; Dowell & Eddy, 2004). The transformation process involves four key steps (detailed in Appendix A. and B):

Sequence Partitioning Given an RNA sequence $x \in \mathcal{X}$ and its secondary structure $y \in \mathcal{Y}$ represented in bracket-dot notation, we partition x into three subsets based on the structural information:

- S: The stem sequence, comprising nucleotides forming stem structures. In bracket-dot notation, these are represented by matching parentheses '(' and ')'.
- $P = \{P_1, \dots, P_k\}$: A set of pseudoknot sequences, where each P_i contains nucleotides forming a distinct pseudoknot. In extended bracket-dot notation, these are typically represented by different types of brackets (e.g., square brackets '[]', curly braces ' $\{\}$ ', or angle brackets ' $\langle\rangle$ ') to distinguish multiple pseudoknots.
- L: The loop sequence, containing all remaining unpaired nucleotides. These are represented by dots '.' in bracket-dot notation.

Binary Tree Construction For each sequence Q, where Q can be either the stem sequence S or any pseudoknot sequence P_i , we construct a binary tree t_Q that preserves its nested structure. The construction follows these rules:

- 1. **Initialization**: Begin with the first complete pair of matching brackets in Q, denoted by positions i and j, where i < j. This initial node is labeled as S to represent Start.
- 2. **Directionality**: Assign the nucleotide at position j as the *head* and the nucleotide at position i as the *dependent*, forming an arc (j,i) labeled appropriately (stem or pseudoknot).
- 3. **Traversal Order**: Proceed in a left-first, then right traversal to recursively construct left and right subtrees, maintaining the nested structures. Nodes are labeled with L and R to denote left and right subtrees, respectively.
- 4. Arc Creation and Labeling: For nucleotides under the same head node, we establish arcs to connect them in a right-to-left sequence. The arcs are labeled based on the structural relationship between the nucleotides(e.g. Arrowed lines in Figure 1(bottom).):

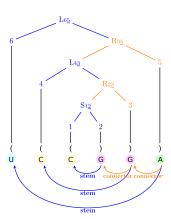


Figure 2: Example of binary tree construction for an RNA stem sequence.

- Stem Arcs: If a pair of nucleotides is part of a stem structure, the connecting arc is labeled as stem.
- **Pseudoknot Arcs**: If a pair of nucleotides is part of a pseudoknot structure, the arc is labeled as pseudoknot.
- Connector Arcs: If the nucleotides are not part of either a stem or pseudoknot but are necessary
 to maintain tree connectivity, the arc is labeled as connector.

Figure 2 illustrates the process of constructing a binary tree for a stem sequence example, where numbers indicate the construction order. Here, S represents the Start pair, and L and R denote the left and right subtrees, respectively. The pseudocode can be found in Appendix A. Algorithm 2

ROOT Construction For RNA sequences that consist solely of stem structures, we select the overall head node of the stem tree t_S as the head node of the entire sequence, denoted as node g. We then connect this node g directly to the ROOT node, forming the complete dependency tree $z = \tau(y)$.

For RNA sequences that include pseudoknot structures, we first identify node g, and connect it to the ROOT node. We then integrate the stem tree t_S with the pseudoknot trees t_{P_i} to form a unified tree structure. The steps are as follows:

- Head Node Ordering: Identify the head nodes of the stem tree and all pseudoknot trees, denoted
 as H_S and H_{Pi}, respectively. Arrange these head nodes according to their positions in the original
 RNA sequence from right to left.
- 2. **ROOT Connection**: Designate the rightmost head node in the sequence as the overall head node of the entire sequence, node *g*. Connect this node *g* to the ROOT node.
- 3. **Sequential Connection**: Connect the remaining head nodes to node g using arcs labeled as connector, following the right-to-left direction. This forms a larger tree structure t'.

By connecting the stem and pseudoknot trees in this manner, we ensure that the combined tree accurately reflects the structural relationships and sequence ordering of the RNA molecule. The use of connector arcs preserves the necessary dependencies between different structural components.

Tree Completion To ensure that every nucleotide in the sequence is connected and the dependency tree is complete, we incorporate the loop nucleotides from L. For each nucleotide $x_k \in L$, we add

an arc (head(k), k), where: $\text{head}(k) = \begin{cases} k+1, & \text{if } k < pos(g) \\ k-1, & \text{if } k > pos(g) \end{cases}$, where pos(g) denotes the position index of a node g.

The arcs are labeled as loop, and this approach ensures that loop nucleotides are connected to their immediate neighbors, maintaining sequential order and tree completeness.

The final output of our transformation is the dependency tree $z \in \mathcal{Z}$, which encapsulates the complete RNA secondary structure. This dependency tree is composed of two integral components: (1) The set of arcs representing the structural connections between nucleotides, capturing both base-pairings and necessary connectors for tree completeness. (2) The set of labels assigned to each arc, indicating the type of relationship between nucleotides—such as stem, pseudoknot, connector, or loop. Every nucleotide in the RNA sequence is connected directly or indirectly to the ROOT node, ensuring that z is a fully connected and rooted dependency tree. The final set of five labels we use is $\mathcal{L} = \{\text{loop, root, stem, connector, pseudoknot}\}$.e.g. labels in Figure 1(bottom).

This comprehensive representation allows us to reformulate RNA secondary structure prediction as an optimization problem over dependency trees. Specifically, we aim to find the dependency tree z that maximizes the conditional probability given the input RNA sequence x: $z^* = \operatorname{argmax}_{z \in \mathcal{Z}} P(z \mid x)$, where z^* is the predicted dependency tree, encompassing both the nucleotide connections and their labels.

3.2 Underlying Dependency Model

Based on the transformation in §3.1, we use a biaffine parser as the core of our model for task parsing. Our proposed model, DEPfold, is composed of several key components. The overall architecture is illustrated in Figure 3.

Foundation Model We input an RNA sequence of length $N, x \in \mathcal{X}$, and embed it using a foundation model to obtain a contextual representation for each nucleotide in the sequence: $r_i = \operatorname{Embed}(x_i)$. The foundation model can be a pre-trained RNA foundation model, such as RNA-fm (Chen et al., 2022), or a general natural language foundation model like RoBERTa (Liu, 2019).⁴ During this embedding phase, each nucleotide's representation is treated as a word, obtaining its corresponding token representation, and then deriving its contextual representation in the entire sequence.

MLP Feature Extraction Dozat & Manning (2016) first proposed using biaffine attention to compute dependency relations. This method formulates the dependency parsing task as labeling each edge in a directed graph, decomposing it into two modules: one predicting whether there is a directed edge between two words, and another predicting the best label for each potential edge. Similarly, we apply this approach to RNA secondary structure model prediction.

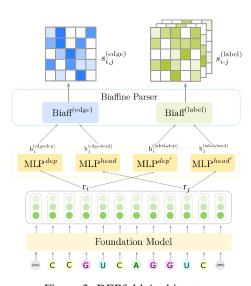


Figure 3: DEPfold Architecture.

For each nucleotide, we use MLPs to obtain dependent and head representations, as in the formulae:

$$h_i^{\text{dep}} = \text{MLP}^{\text{dep}}(r_i); \quad h_i^{\text{head}} = \text{MLP}^{\text{head}}(r_i).$$

where h_i^{dep} and h_i^{head} are the representation vectors of x_i as a dependent nucleotide and a head nucleotide, respectively.

⁴While it may sound counter-intuitive to use a standard language model for RNA sequences, we found out RoBERTa can be applied to RNA sequences effectively. We believe it is because the model is fine-tuned on the RoBERTa's representations, which carry some information.

271

272

277

278

279

280

281

282

283

290

291

292

293

295 296

297

298

299

300

301

302 303 304

305

306

307 308

309 310

311 312

313

314

315

316 317

318

319

320

321

322

323

Biaffine Scorer We then use biaffine classifiers to predict scores for edges and labels separately. The biaffine classifier is a generalization of linear classifiers, including multiplicative interactions between two vectors:

$$\begin{aligned} \operatorname{Biaff}(\mathbf{e}_1,\mathbf{e}_2) &= \mathbf{e}_1^\top \mathbf{U} \mathbf{e}_2 + \mathbf{W}(\mathbf{e}_1 \oplus \mathbf{e}_2) + \mathbf{b}, \\ s^{(\operatorname{edge})}(i,j) &= \operatorname{Biaff}^{(\operatorname{edge})} \left(h_i^{(\operatorname{edge-dep})}, h_j^{(\operatorname{edge-head})} \right); s^{(\operatorname{label})}(i,j) &= \operatorname{Biaff}^{(\operatorname{label})} \left(h_i^{(\operatorname{label-dep})}, h_j^{(\operatorname{label-head})} \right). \end{aligned}$$

In the above, $s^{(\text{label})}(i,j)$ is a vector of length $|\mathcal{L}|$ ranging over labels. We denote by $s^{(\text{label})}(i,j,\ell)$ the specific value for a label $\ell \in \mathcal{C}$. The tensor U can be chosen as a diagonal matrix (making $u_{i,k,j} = 0$ when $i \neq j$) to save parameters. For the labeled parser, U will be $(d \times c \times d)$ -dimensional, where c is the number of labels. This operation is highly computationally efficient on GPUs.

Training Loss The model training is based on simple head nucleotide selection, without considering tree structure, and the losses for all words are accumulated in a mini-batch. For a standard head dependent pair (x_i, x_i) with label ℓ^* in the training instance, the cross-entropy loss is:

$$L^{(\text{edge})}(i,j) = -\log \frac{\exp\left(s^{(\text{edge})}(i,j)\right)}{\sum_{0 \leq r \leq n} \exp\left(s^{(\text{edge})}(r,j)\right)}; \quad L^{(\text{label})}(i,j,\ell^*) = -\log \frac{\exp\left(s^{(\text{label})}(i,j,\ell^*)\right)}{\sum_{\ell \in \mathcal{L}} \exp\left(s^{(\text{label})}(i,j,\ell)\right)};$$

 $L^{(\text{edge})}(i,j) = -\log \frac{\exp \left(s^{(\text{edge})}(i,j)\right)}{\sum_{0 \leq r \leq n} \exp \left(s^{(\text{edge})}(r,j)\right)}; \quad L^{(\text{label})}(i,j,\ell^*) = -\log \frac{\exp \left(s^{(\text{label})}(i,j,\ell^*)\right)}{\sum_{\ell \in \mathcal{L}} \exp \left(s^{(\text{label})}(i,j,\ell)\right)}.$ In the overall system training, our goal is to minimize the sum of both losses over all dependency structures in the training data \mathcal{D} : $\sum_{z \in \mathcal{D}} \sum_{(i \rightarrow j, \ell^*) \in z} L^{(\text{edge})}(i,j) + L^{(\text{label})}(i,j,\ell^*).$

Decoding After obtaining scores for all dependency relations, for the head selection of each nucleotide, we use the first-order Eisner algorithm (Eisner 2000; for projective structures) or graph spanning tree algorithms (Koo et al. 2007; for non-projective structures) to find the optimal tree z^* without labels: $z^* = \arg\max_z \left[\sum_{i \to j \in z} s(i,j)\right]$. Based on the obtained optimal tree structure, we select the corresponding maximum label for each pair as the predicted value, leading eventually to the secondary structure y^* .

Post-processing RNA secondary structure only focuses on the connections we predict as stem and pseudoknots, and must comply with the rule that each nucleotide can only connect with one nucleotide, we first select those connections labeled as stem and pseudoknots from the predicted RNA dependency parsing structure and convert them into a contact map M.

We then use Softmax on M to obtain probability distributions in the row and column directions:

$$C(M) = \frac{\exp(M_{ij})}{\sum_{k=1}^{L} \exp(M_{kj})}; \quad \mathcal{R}(M) = \frac{\exp(M_{ij})}{\sum_{k=1}^{L} \exp(M_{ik})}.$$

Finally, we retain the maximum value in the row direction as the connection to obtain the final optimized contact matrix M^* , which ensures that the resulting connection structure is not conflicting: $M^* = \arg \max(\mathcal{R}(M)).$

EXPERIMENTAL SETUP

Dataset We evaluate DEPfold on four widely-used RNA structure prediction benchmark datasets:

RNAStrAlign(Tan et al., 2017) contains 37,149 structures from 8 RNA types. Following E2Efold (Chen et al., 2020) and MXfold2 (Sato et al., 2021), we processed the dataset, retaining 30,451 non-redundant structures. ArchiveII (Sloma & Mathews, 2016), comprising 3,975 structures from 10 RNA types, serves as a standard benchmark for classical RNA folding methods. Both datasets include sequences with pseudoknots.

bpRNA-1m (Singh et al., 2019) includes 102,318 structures from 2,588 RNA types. We processed it following SPOT-RNA (Singh et al., 2019), using CD-HIT (Fu et al., 2012) for redundancy removal and dataset splitting. bpRNA-new (Kalvari et al., 2017), derived from Rfam 14.2, contains sequences from 1,500 novel RNA families and is used to assess cross-family generalization. Consistent with UFold (Fu et al., 2022), we augmented the training data by randomly mutating bpRNA-new sequences and generating structure predictions using RNAfold (Lorenz et al., 2011b). Sequences in bpRNA-1m and bpRNA-new are shorter than 500 nucleotides and lack pseudoknots, contrasting with the first two datasets. Table 1 summarizes the key characteristics of each dataset.

Baseline Methods We compare our proposed DEPfold with several baseline methods, including:

Energy-based folding methods: CONTRAfold (Do et al., 2006b), RNAfold (Lorenz et al., 2011b), LinearFold (Huang et al., 2019)(using the thermodynamic free energy model from Vienna RNAfold(Lorenz et al., 2011b)), and RNAstructure (Reuter & Mathews, 2010)(using the ProbKnot(Bellaousov & Mathews, 2010) algorithm when predicting RNA datasets with pseudoknots). Learning-based folding methods: E2Efold (Chen et al., 2020), MX-fold2 (Sato et al., 2021), UFold (Fu et al., 2022), and RFold (Tan et al.).

Evaluation Metrics As standardly is done in the area of RNA structured prediction, we evaluated performance using precision (or PPV, Positive Predictive Value), recall

Table 1: Summary of datasets used in our experiments.

Dataset	Subset	#Seq.	Len. Range
RNAStrAlign	Train	28,969	30–1581
	Val	3,629	36-1693
	Test	2,810	57-1672
ArchiveII	-	3,975	28–2968
bpRNA-1m	TR0	10,814	33–498
•	VL0	1,300	33-497
	TS0	1,305	22–499
bpRNA-aug	TR1	20431	33-498
bpRNA-new	-	5,401	33–489

(or SEN, sensitivity), and F_1 score. More specifically, the set of all aligned pairs are extracted from both the predicted structure and the reference structure, and the macro-averaged statistics are calculated based on them.

5 RESULTS

To evaluate the performance of our DEPfold model relative to baseline models, we conducted two sets of experiments, following a similar approach to that of Fu et al. (2022); Sato et al. (2021): (a) training the model on the RNAStrAlign training set and testing on the RNAStrAlign test set and the ArchiveII dataset; (b) training the same model on the bpRNA-1m training set (TR0) and testing on the bpRNA-1m test set (TS0), as well as training on bpRNA-1m augmentation set (TR1) and testing on the bpRNA-new (bpnew) dataset. For detailed information on the model training process, see Appendix C.

5.1 PERFORMANCE ON RNASTRALIGN AND ARCHIVEII

We assessed the performance of DEPfold on the RNAS-trAlign test set, and the results are presented in Table 2. DEPfold achieved the best performance across all evaluation metrics. Compared to traditional energy-based algorithms, DEPfold demonstrated significant advantages: LinearFold and RNAfold attained F_1 scores of 0.539 and 0.621, respectively, while DEPfold reached 0.985. Deep learning-based folding algorithms such as E2Efold and UFold also improved performance, with F_1 scores of 0.821 and 0.962, respectively. However, DEPfold surpassed these methods in both precision and recall. Notably, DEPfold can handle RNA sequences of arbitrary lengths, whereas E2Efold, RFold and UFold are con-

Table 2: Performance comparison on RNAStrAlign test set.

Method	Precision	Recall	F_1
DEPfold	0.988	0.983	0.985
UFold	0.959	0.965	0.962
RFold	0.942	0.780	0.797
E2Efold	0.866	0.788	0.821
ContraFold	0.600	0.647	0.621
LinearFold	0.523	0.576	0.547
RNAfold	0.515	0.568	0.539
RNAstructure	0.537	0.569	0.551

strained by a fixed maximum sequence length (e.g., 1,800 nucleotides). This capability underscores DEPfold's flexibility and adaptability in processing diverse RNA sequences.

Pseudoknot Prediction To evaluate DEPfold's ability to handle complex RNA structures, particularly sequences containing pseudoknots, we analyzed sequences with pseudoknots in the RNAStrAlign test set. Following the methodology of E2Efold (Chen et al., 2020), we calculated the average F_1 score (Set F_1) for these sequences and counted the number of sequences where the presence or absence of pseudoknots was correctly predicted. Table 3 summarizes the evaluation results.

Table 3: Evaluation of pseudoknot prediction.

Method	Set F ₁	TP	FP	TN	FN
DEPfold	0.981	1258	20	1531	1
Ufold	0.838	159	111	1397	0
E2Efold	0.710	1312	242	1271	0
RNAstructure	0.474	975	306	1245	284
Rfold	0.447	685	55	1470	122

DEPfold achieved the highest F₁ score of 0.981 on this

set, significantly outperforming other methods. It demonstrated high accuracy in identifying both

 pseudoknotted and non-pseudoknotted sequences, while maintaining low false positive and false negative rates. These results indicate that DEPfold exhibits exceptional capability in handling complex RNA structures containing pseudoknots, showcasing its potential to effectively capture the intricacies of RNA structural complexity.

Generalization to ArchiveII To assess DEPfold's generalization ability, we directly tested the model trained on the RNAStrAlign training set on the ArchiveII dataset. Table 4 compares the performance of DEPfold with other methods on the ArchiveII dataset. DEPfold achieved an F_1 score of 0.920 on this dataset, significantly higher than other methods, and also obtained the highest precision and recall. This demonstrates that DEPfold not only achieves strong results on specific tasks but also has the capacity to adapt to a wide range of RNA secondary structure prediction tasks.

Table 4: Performance comparison on ArchiveII set.

Method	Precision	Recall	F_1
DEPfold	0.941	0.907	0.920
RFold	0.931	0.899	0.911
UFold	0.876	0.890	0.881
MXfold2	0.825	0.780	0.796
E2Efold	0.734	0.660	0.686
ContraFold	0.593	0.649	0.617
LinearFold	0.549	0.609	0.575
RNAfold	0.550	0.611	0.577
RNAstructure	0.554	0.601	0.573

Table 5: Performance comparison on bpRNA-TS0 set.

Method	Precision	Recall	F_1
DEPfold	0.730	0.656	0.676
RFold	0.676	0.625	0.633
UFold	0.587	0.711	0.630
MXfold2	0.519	0.646	0.558
ContraFold	0.482	0.655	0.541
LinearFold	0.447	0.633	0.510
RNAfold	0.446	0.631	0.508
RNAstructure	0.446	0.622	0.505

5.2 PERFORMANCE ON THE BPRNA DATASET

Following prior studies (Sato et al., 2021; Fu et al., 2022), we trained on bpRNA-TR0 and evaluated on bpRNA-TS0 using the best model obtained from bpRNA-VL0. Detailed results are presented in Table 5. DEPfold significantly outperformed UFold in terms of F_1 score, with an improvement of 7 percentage points, and achieved a 25% enhancement over traditional methods.

Long-range Interaction Prediction To evaluate whether DEPfold contributes to improved prediction of long-range interactions, we adopted the same experimental approach as UFold. We used the TS0 dataset as the test set because it

Table 6: Performance on long-range base pair prediction (bpRNA-TS0)

Method	Precision	Recall	F ₁ Score
DEPfold	0.715	0.689	0.689
UFold	0.630	0.711	0.653
RFold	0.666	0.647	0.643
ContraFold	0.505	0.614	0.536
LinearFold	0.502	0.629	0.542
RNAfold	0.499	0.627	0.539
RNAstructure	0.490	0.603	0.523

contains diverse sequences of varying lengths from various RNA families. For a sequence of length L, we define base pairs with a separation greater than L/2 as long-range base pairs. As shown in Table 6, DEPfold is able to predict long-range base pairs, outperforming UFold. Notably, DEPfold's performance in predicting long-range base pairs was comparable to, or even slightly better than, its performance in predicting short-range base pairs.

Cross-family Evaluation on bpRNA-new The bpRNA-new dataset is a cross-family benchmark dataset that poses significant challenges to purely deep learning methods because these families are not represented in the training set. To address this issue, MXfold2 proposed combining free energy minimization with deep learning methods, achieving performance similar to the thermodynamics-based ContraFold. The purely deep learning method DEPfold, which is based on data augmentation (TR1 dataset for training) from RNAfold, achieved an F_1 score of 0.621 on the bpRNA-new dataset, exceeding RNAfold by 0.65 percentage points. This result indicates that DEPfold can learn

Table 7: Performance comparison on bpRNA-new.

Method	Precision	Recall	F_1 Score
DEPfold	0.650	0.624	0.621
UFold	0.527	0.695	0.590
RFold	0.528	0.306	0.369
MXfold2	0.585	0.710	0.632
ContraFold	0.578	0.736	0.639
LinearFold	0.551	0.719	0.615
RNAfold	0.552	0.720	0.617
RNAstructure	0.542	0.703	0.604

more useful structural information on top of what traditional methods capture. In contrast, UFold, which also uses data augmentation, performed slightly worse than RNAfold on this dataset.

5.3 ABLATION STUDY

To gain deeper insight into the contributions of various components of DEPfold, we conducted a series of ablation experiments.

Pretrained Models We compared the effectiveness of using RoBERTa and RNAfm as RNA sequence representation generators. which are denoted as DEPfold-Ro and DEPfold-fm, respectively. RoBERTa is a general-purpose large-scale language model, while RNAfm is a pretrained model specifically designed for RNA sequences. Table 8

Table 8: Ablation Study on Pretrained Models and Fine-Tuning (bpRNA-TS0).

Method	Precision	Recall	F ₁
DEPfold-Ro,FT	0.730	0.656	0.676
DEPfold-fm,FT	0.719	0.574	0.618
DEPfold-Ro,FrZ	0.428	0.174	0.217
DEPfold-fm,FrZ	0.644	0.422	0.470

presents the results. The DEPfold model based on RNAfm achieved an F_1 score of 0.618 on TS0, slightly lower than the version using RoBERTa. This suggests that although RNAfm is specialized for RNA sequences, the general language representations provided by RoBERTa perform better in this task.

Fine-Tuning vs. Freezing Pretrained Models We further investigated the impact of fine-tuning versus freezing the pretrained models on DEPfold's performance. As shown in Table 8, fine-tuning the pretrained models (FT) significantly enhances the model's ability to predict RNA secondary structures. In contrast, freezing the pretrained models (FrZ) leads to substantial performance degradation, with the model nearly failing to learn meaningful representations for RNA secondary structure prediction. Interestingly, under frozen conditions, the model using RNAfm performed slightly better than the one with RoBERTa, possibly because RNAfm, being specifically pretrained on RNA sequences, had already captured some RNA-specific features during its pretraining phase.

Optimal Tree Decoding We evaluated the impact of the optimal tree decoding algorithm on DEPfold's performance by comparing the model with and without this strategy. The results are presented in Table 9, where "DEPfold w/o OT" denotes the DEPfold model without the Optimal Tree decoding strategy. The findings show that incorporating Optimal Tree decoding consistently

Table 9: Ablation Study on Optimal Tree Decoding (bpRNA).

Dataset	Method	Precision	Recall	F_1
TS0	DEPfold DEPfold w/o OT		0.656 0.686	
bpRNA-new	DEPfold DEPfold w/o OT		0.624 0.613	

enhances performance across both datasets. On TS0, the F_1 score increases from 0.671 to 0.676 when optimal tree decoding is used, primarily due to an increase in precision from 0.676 to 0.730. Similarly, on bpRNA-new, the F_1 score improves from 0.607 to 0.621. These enhancements demonstrate that optimal tree decoding effectively enforces valid RNA structural constraints during decoding, leading to more accurate and biologically plausible predictions.

6 RELATED WORK

Traditional Methods Traditional approaches include alignment-based and single-sequence prediction methods. Alignment-based methods like the Sankoff algorithm (Sankoff, 1985) and its variants—Dynalign (Mathews & Turner, 2002) and Carnac (Touzet & Perriquet, 2004)—predict structures by identifying conserved motifs among homologous sequences. However, their effectiveness is limited by the limited number of RNA families in databases like Rfam (Kalvari et al., 2021) and low sequence conservation. Single-sequence methods, such as Vienna RNAfold (Lorenz et al., 2011a) and Mfold (Zuker, 2003), predict structures by minimizing free energy based on thermodynamic models. While effective for short sequences, they struggle with efficiency and accuracy on complex structures, particularly pseudoknots, which pose NP-complete challenges (Lyngsø & Pedersen, 2000). Tools like RNAstructure (Reuter & Mathews, 2010) extend capabilities to include pseudoknot prediction and external constraints but face computational bottlenecks with long sequences.

Machine Learning and Deep Learning Methods Deep learning models have been introduced for RNA structure prediction. SPOT-RNA (Singh et al., 2019) combines ResNet (Koonce & Koonce, 2021) and bidirectional LSTM (Hochreiter, 1997) but lacks constraints to ensure valid structures, affecting generalization (Amos & Kolter, 2017). E2Efold (Chen et al., 2020) uses convex optimization and algorithm unrolling to constrain outputs. UFold (Fu et al., 2022) uses convolutional networks on image representations of sequences, enhancing pseudoknot prediction. MXfold2 (Sato et al., 2021) combines deep learning with thermodynamic models, generalizing well across families. However,

these models generally struggle with long sequences; for example, SPOT-RNA supports up to 2000 nucleotides, E2Efold up to 1800, UFold up to 600, and MXfold2 up to 1000 nucleotides.

NLP-Inspired Methods NLP techniques have been applied to RNA structure prediction. Linear-Fold (Huang et al., 2019) reduces prediction time from quadratic to linear using beam pruning (Huang et al., 2012), a popular heuristic widely used in computational linguistics, but cannot predict pseudoknots. ContextFold (Zakov et al., 2011) and CONTRAfold (Do et al., 2006b) use context-free grammars for base-pair dependencies, improving accuracy but still struggling with complex structures like pseudoknots. Matsui et al. proposed a new structural alignment algorithm based on pair stochastic tree adjoining grammars (PSTAGs) to align and predict RNA secondary structures, including pseudoknots. NLP methods improve computational efficiency and handle some complex structures, but integrating deep learning for RNA secondary structure prediction, especially for pseudoknots and long sequences, remains challenging.

7 CONCLUSION

In this work, we introduced DEPfold, a novel RNA secondary structure prediction framework that reformulates the task as dependency parsing by leveraging advanced NLP techniques. DEPfold transforms RNA structures into labeled dependency trees, uses a biaffine attention mechanism for accurate base pairing prediction, and uses optimal tree decoding to ensure biologically valid structures. Our approach significantly outperforms traditional energy-based methods and state-of-the-art deep learning models, achieving an F1 score of 0.985 on the RNAStrAlign dataset and effectively capturing complex features such as pseudoknots and long-range interactions. Furthermore, DEPfold demonstrates robust cross-family generalization on the bpRNA-new dataset, identifying structural nuances that conventional models miss. Ablation studies highlight the unexpected efficacy of general-purpose models like RoBERTa in fine-tuning, indicating potential for specialized pretraining strategies in RNA biology. While DEPfold marks a significant advancement, future work will address challenges in enhancing cross-family generalization and model interpretability by expanding training data diversity, optimizing computational efficiency, and improving interpretability to broaden DEPfold's applicability in diverse biological research contexts.

LIMITATIONS

Our experiments on within-family datasets, such as RNAStrAlign and bpRNA-TS0, show that DEP-fold achieves high F_1 score, indicating effective learning from the training data. However, when evaluated on cross-family datasets like bpRNA-new—which includes RNA families not represented in the training set—DEPfold's performance shows a smaller margin of improvement (outperforming RNAfold by only 0.65 percentage points). This suggests that while DEPfold can capture structural information beyond traditional methods, its ability to generalize to entirely new RNA families is still limited. See discussion by Szikszai et al. (2022) and Bernett et al. (2024).

Our data augmentation strategy, which uses RNAfold-predicted structures, while beneficial, may reinforce existing biases in traditional energy-based models. While effective in increasing training data, this approach may limit DEPfold's ability to learn non-traditional structural patterns. Future work should explore more diverse data augmentation techniques that introduce a wider range of structural variations. Additionally, scaling DEPfold to larger model sizes and datasets, and incorporating neural dependency parsing models like stack-pointer Ma (2018) and TreeCRF Zhang et al. (2020a;b), could enhance its ability to learn from diverse syntactic representations and improve overall capabilities.

An interesting finding from our ablation studies is the superior performance of RoBERTa over RNA-fm in the fine-tuning stage. This result prompts us to rethink the optimal pre-training strategy for RNA structure prediction. RoBERTa's general language patterns seem to provide more valuable context for structure prediction than RNA-fm's RNA-specific features. This suggests that current RNA-specific models may not fully capture the characteristics needed for accurate structure prediction. Our findings suggest the need for developing more effective pre-training approaches specifically designed for RNA biology, which could potentially improve the accuracy and generalization capabilities of models like DEPfold.

REFERENCES

- RNAcentral: an international database of ncRNA sequences. *Nucleic acids research*, 43(D1):D123–D129, 2015.
- Rujira Achawanantakun and Yanni Sun. Shape and secondary structure prediction for ncrnas including pseudoknots based on linear svm. In *BMC bioinformatics*, volume 14, pp. 1–11. Springer, 2013.
- Brandon Amos and J. Zico Kolter. OptNet: Differentiable optimization as a layer in neural networks.

 In Doina Precup and Yee Whye Teh (eds.), Proceedings of the 34th International Conference on Machine Learning, volume 70 of Proceedings of Machine Learning Research, pp. 136–145.

 PMLR, 06–11 Aug 2017. URL https://proceedings.mlr.press/v70/amos17a.html.
 - John F. Atkins, Raymond F. Gesteland, and Thomas R. Cech. RNA worlds: from life's origins to diversity in gene regulation. 2011. URL https://api.semanticscholar.org/CorpusID:83053162.
 - Stanislav Bellaousov and David H Mathews. Probknot: fast prediction of rna secondary structure including pseudoknots. *Rna*, 16(10):1870–1880, 2010.
 - Judith Bernett, David B Blumenthal, Dominik G Grimm, Florian Haselbeck, Roman Joeres, Olga V Kalinina, and Markus List. Guiding questions to avoid data leakage in biological machine learning applications. *Nature Methods*, 21(8):1444–1453, 2024.
 - Ian Brierley, Simon Pennell, and Robert JC Gilbert. Viral rna pseudoknots: versatile motifs in gene expression and replication. *Nature Reviews Microbiology*, 5(8):598–610, 2007.
 - Ian Brierley, Robert JC Gilbert, and Simon Pennell. Rna pseudoknots and the regulation of protein synthesis. *Biochemical Society Transactions*, 36(4):684–689, 2008.
 - Jiayang Chen, Zhihang Hu, Siqi Sun, Qingxiong Tan, Yixuan Wang, Qinze Yu, Licheng Zong, Liang Hong, Jin Xiao, Tao Shen, et al. Interpretable RNA foundation model from unannotated data for highly accurate RNA structure and function predictions. *arXiv* preprint arXiv:2204.00300, 2022.
 - Xinshi Chen, Yu Li, Ramzan Umarov, Xin Gao, and Le Song. Rna secondary structure prediction by learning unrolled algorithms. *arXiv* preprint *arXiv*:2002.05810, 2020.
 - Chuong B. Do, Daniel A. Woods, and Serafim Batzoglou. Contrafold: RNA secondary structure prediction without physics-based models. *Bioinformatics*, 22 14:e90-8, 2006a. URL https://api.semanticscholar.org/CorpusID:1646946.
 - Chuong B Do, Daniel A Woods, and Serafim Batzoglou. Contrafold: RNA secondary structure prediction without physics-based models. *Bioinformatics*, 22(14):e90–e98, 2006b.
 - Robin D Dowell and Sean R Eddy. Evaluation of several lightweight stochastic context-free grammars for RNA secondary structure prediction. *BMC bioinformatics*, 5:1–14, 2004.
 - Timothy Dozat and Christopher D Manning. Deep biaffine attention for neural dependency parsing. *arXiv* preprint arXiv:1611.01734, 2016.
 - Jason Eisner. Bilexical grammars and their cubic-time parsing algorithms. *Advances in probabilistic and other parsing technologies*, pp. 29–61, 2000.
 - Laiyi Fu, Yingxin Cao, Jie Wu, Qinke Peng, Qing Nie, and Xiaohui Xie. Ufold: fast and accurate RNA secondary structure prediction with deep learning. *Nucleic acids research*, 50(3):e14–e14, 2022.
- Limin Fu, Beifang Niu, Zhengwei Zhu, Sitao Wu, and Weizhong Li. CD-HIT: accelerated for clustering the next-generation sequencing data. *Bioinformatics*, 28(23):3150–3152, oct 2012. doi: 10. 1093/bioinformatics/bts565. URL https://doi.org/10.1093%2Fbioinformatics% 2Fbts565.

- David P Giedroc and Peter V Cornish. Frameshifting rna pseudoknots: structure and mechanism. *Virus research*, 139(2):193–208, 2009.
 - Wade W. Grabow and Luc Jaeger. RNA self-assembly and RNA nanotechnology. *Accounts of chemical research*, 47 6:1871–80, 2014. URL https://api.semanticscholar.org/CorpusID:206825276.
 - Monir Hajiaghayi, Anne Condon, and Holger H. Hoos. Analysis of energy-based algorithms for RNA secondary structure prediction. *BMC Bioinformatics*, 13:22 22, 2012. URL https://api.semanticscholar.org/CorpusID:10689908.
 - S Hochreiter. Long short-term memory. Neural Computation MIT-Press, 1997.
 - Liang Huang, Suphan Fayong, and Yang Guo. Structured perceptron with inexact search. In *Proceedings of the 2012 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies*, pp. 142–151, 2012.
 - Liang Huang, He Zhang, Dezhong Deng, Kai Zhao, Kaibo Liu, David A Hendrix, and David H Mathews. Linearfold: linear-time approximate RNA folding by 5'-to-3'dynamic programming and beam search. *Bioinformatics*, 35(14):i295–i304, 2019.
 - John Jumper, Richard Evans, Alexander Pritzel, Tim Green, Michael Figurnov, Olaf Ronneberger, Kathryn Tunyasuvunakool, Russ Bates, Augustin Žídek, Anna Potapenko, et al. Highly accurate protein structure prediction with alphafold. *nature*, 596(7873):583–589, 2021.
 - Ioanna Kalvari, Joanna Argasinska, Natalia Quinones-Olvera, Eric P Nawrocki, Elena Rivas, Sean R Eddy, Alex Bateman, Robert D Finn, and Anton I Petrov. Rfam 13.0: shifting to a genome-centric resource for non-coding RNA families. *Nucleic Acids Research*, 46(D1):D335–D342, nov 2017. doi: 10.1093/nar/gkx1038. URL https://doi.org/10.1093%2Fnar%2Fgkx1038.
 - Ioanna Kalvari, Eric P Nawrocki, Nancy Ontiveros-Palacios, Joanna Argasinska, Kevin Lamkiewicz, Manja Marz, Sam Griffiths-Jones, Claire Toffano-Nioche, Daniel Gautheret, Zasha Weinberg, et al. Rfam 14: expanded coverage of metagenomic, viral and microRNA families. *Nucleic Acids Research*, 49(D1):D192–D200, 2021.
 - Kalli Kappel, Kaiming Zhang, Zhaoming Su, Andrew M. Watkins, Wipapat Kladwang, Shanshan Li, Grigore Pintilie, Ved V. Topkar, Ramya Rangan, Ivan N. Zheludev, Joseph D. Yesselman, Wah Chiu, and Rhiju Das. Accelerated cryo-EM-guided determination of three-dimensional RNA-only structures. *Nature Methods*, 17(7):699–707, jul 2020. doi: 10.1038/s41592-020-0878-9. URL https://doi.org/10.1038%2Fs41592-020-0878-9.
 - Zainab Khatoon, Bryan Figler, Hui Zhang, and Feng Cheng. Introduction to RNA-Seq and its applications to drug discovery and development. *Drug development research*, 75(5):324–330, 2014.
 - Bjarne Knudsen and Jotun Hein. RNA secondary structure prediction using stochastic context-free grammars and evolutionary history. *Bioinformatics*, 15 6:446–54, 1999. URL https://api.semanticscholar.org/CorpusID:5971132.
 - Terry Koo, Amir Globerson, Xavier Carreras, and Michael Collins. Structured prediction models via the matrix-tree theorem. In Jason Eisner (ed.), *Proceedings of the 2007 Joint Conference on Empirical Methods in Natural Language Processing and Computational Natural Language Learning (EMNLP-CoNLL)*, pp. 141–150, Prague, Czech Republic, June 2007. Association for Computational Linguistics. URL https://aclanthology.org/D07-1015.
 - Brett Koonce and Brett Koonce. Resnet 50. *Convolutional neural networks with swift for tensorflow: image recognition and dataset categorization*, pp. 63–72, 2021.
 - Sandra Kübler, Ryan McDonald, and Joakim Nivre. Dependency parsing. In *Dependency parsing*, pp. 11–20. Springer, 2009.
 - Yinhan Liu. Roberta: A robustly optimized bert pretraining approach. *arXiv preprint arXiv:1907.11692*, 2019.

- Ronny Lorenz, Stephan H Bernhart, Christian Höner zu Siederdissen, Hakim Tafer, Christoph Flamm, Peter F Stadler, and Ivo L Hofacker. ViennaRNA package 2.0. *Algorithms for molecular biology*, 6:1–14, 2011a.
 - Ronny Lorenz, Stephan H Bernhart, Christian Höner zu Siederdissen, Hakim Tafer, Christoph Flamm, Peter F Stadler, and Ivo L Hofacker. ViennaRNA package 2.0. *Algorithms for Molecular Biology*, 6(1), nov 2011b. doi: 10.1186/1748-7188-6-26. URL https://doi.org/10.1186%2F1748-7188-6-26.
 - Rune B Lyngsø and Christian NS Pedersen. RNA pseudoknot prediction in energy-based models. *Journal of computational biology*, 7(3-4):409–427, 2000.
 - X Ma. Stack-pointer networks for dependency parsing. arXiv preprint arXiv:1805.01087, 2018.
 - David H Mathews and Douglas H Turner. Dynalign: an algorithm for finding the secondary structure common to two RNA sequences. *Journal of molecular biology*, 317(2):191–203, 2002.
 - Hiroshi Matsui, Kengo Sato, and Yasubumi Sakakibara. Pair stochastic tree adjoining grammars for aligning and predicting pseudoknot rna structures. In *Proceedings. 2004 IEEE Computational Systems Bioinformatics Conference*, 2004. CSB 2004., pp. 290–299. IEEE, 2004.
 - Stefanie A Mortimer, Mary Anne Kidwell, and Jennifer A Doudna. Insights into RNA structure and function from genome-wide studies. *Nature Reviews Genetics*, 15(7):469–479, 2014.
 - Davoud Naderi, Raheba Jami, and F Rehman. A review of rna motifs, identification algorithms and their function on plants. *Journal of Plant Bioinformatics and Biotechnology*, 1(1):28–40, 2021.
 - Ian Kings Oluoch, Abdullah Akalin, Yilmaz Vural, and Yavuz Canbay. A review on RNA secondary structure prediction algorithms. 2018 International Congress on Big Data, Deep Learning and Fighting Cyber Terrorism (IBIGDELFT), pp. 18–23, 2018. URL https://api.semanticscholar.org/CorpusID:59236381.
 - Cristina Puzzarini and Vincenzo Barone. Diving for accurate structures in the ocean of molecular systems with the help of spectroscopy and quantum chemistry. *Accounts of chemical research*, 51 2:548–556, 2018. URL https://api.semanticscholar.org/CorpusID: 206384444.
 - Jessica S Reuter and David H Mathews. Rnastructure: software for RNA secondary structure prediction and analysis. *BMC bioinformatics*, 11:1–9, 2010.
 - Elena Rivas and Sean R Eddy. A dynamic programming algorithm for RNA structure prediction including pseudoknots. *Journal of molecular biology*, 285(5):2053–2068, 1999.
 - Vandana Saini, Rajni Dawar, Shilpa Suneja, Sukanya Gangopadhyay, and Charanjeet Kaur. Can microRNA become next-generation tools in molecular diagnostics and therapeutics? a systematic review. *Egyptian Journal of Medical Human Genetics*, 22, 2021. URL https://api.semanticscholar.org/CorpusID:231695552.
 - David Sankoff. Simultaneous solution of the RNA folding, alignment and protosequence problems. *SIAM journal on applied mathematics*, 45(5):810–825, 1985.
 - Kengo Sato, Manato Akiyama, and Yasubumi Sakakibara. RNA secondary structure prediction using deep learning with thermodynamic integration. *Nature communications*, 12(1):941, 2021.
 - Seema Sethi, Shadan Ali, Philip A Philip, and Fazlul H Sarkar. Clinical advances in molecular biomarkers for cancer diagnosis and therapy. *International journal of molecular sciences*, 14(7): 14771–14784, 2013.
 - Jaswinder Singh, Jack Hanson, Kuldip Paliwal, and Yaoqi Zhou. RNA secondary structure prediction using an ensemble of two-dimensional deep neural networks and transfer learning. *Nature communications*, 10(1):5407, 2019.
 - Michael F. Sloma and David H. Mathews. Exact calculation of loop formation probability identifies folding motifs in RNA secondary structures. *RNA*, 22(12):1808–1818, oct 2016. doi: 10.1261/rna.053694.115. URL https://doi.org/10.1261%2Frna.053694.115.

- Bruce A. Sullenger and Smita K. Nair. From the RNA world to the clinic. *Science*, 352:1417 1420, 2016. URL https://api.semanticscholar.org/CorpusID:206645358.
- Marcell Szikszai, Michael Wise, Amitava Datta, Max Ward, and David H Mathews. Deep learning models for rna secondary structure prediction (probably) do not generalize across families. *Bioinformatics*, 38(16):3892–3899, 2022.
- Cheng Tan, Zhangyang Gao, CAO Hanqun, Xingran Chen, Ge Wang, Lirong Wu, Jun Xia, Jiangbin Zheng, and Stan Z Li. Deciphering rna secondary structure prediction: A probabilistic k-rook matching perspective. In *Forty-first International Conference on Machine Learning*.
- Zhen Tan, Yinghan Fu, Gaurav Sharma, and David H. Mathews. TurboFold II: RNA structural alignment and secondary structure prediction informed by multiple homologs. *Nucleic Acids Research*, 45(20):11570–11581, sep 2017. doi: 10.1093/nar/gkx815. URL https://doi.org/10.1093%2Fnar%2Fgkx815.
- Lucien Tesnière. Elements of structural syntax. John Benjamins Publishing Company, 2015.
- Ignacio Tinoco Jr and Carlos Bustamante. How RNA folds. *Journal of molecular biology*, 293(2): 271–281, 1999.
- Hélene Touzet and Olivier Perriquet. Carnac: folding families of related RNAs. *Nucleic acids research*, 32(suppl_2):W142–W145, 2004.
- Douglas H. Turner and David H. Mathews. NNDB: the nearest neighbor parameter database for predicting stability of nucleic acid secondary structure. *Nucleic Acids Research*, 38(suppl_1):D280–D282, oct 2009. doi: 10.1093/nar/gkp892. URL https://doi.org/10.1093%2Fnar%2Fgkp892.
- Hao Yin, Rosemary L Kanasty, Ahmed A Eltoukhy, Arturo J Vegas, J Robert Dorkin, and Daniel G Anderson. Non-viral vectors for gene-based therapy. *Nature reviews genetics*, 15(8):541–555, 2014.
- Shay Zakov, Yoav Goldberg, Michael Elhadad, and Michal Ziv-Ukelson. Rich parameterization improves RNA structure prediction. *Journal of Computational Biology*, 18(11):1525–1542, 2011.
- Jinsong Zhang, Yuhan Fei, Lei Sun, and Qiangfeng Cliff Zhang. Advances and opportunities in RNA structure experimental determination and computational modeling. *Nature Methods*, 19 (10):1193–1207, 2022.
- Yu Zhang, Zhenghua Li, and Zhang Min. Efficient second-order TreeCRF for neural dependency parsing. In *Proceedings of ACL*, pp. 3295–3305, 2020a. URL https://www.aclweb.org/anthology/2020.acl-main.302.
- Yu Zhang, Houquan Zhou, and Zhenghua Li. Fast and accurate neural CRF constituency parsing. In *Proceedings of IJCAI*, pp. 4046–4053, 2020b. doi: 10.24963/ijcai.2020/560. URL https://doi.org/10.24963/ijcai.2020/560.
- M. Zuker. Mfold web server for nucleic acid folding and hybridization prediction. *Nucleic Acids Research*, 31(13):3406–3415, jul 2003. doi: 10.1093/nar/gkg595. URL https://doi.org/10.1093%2Fnar%2Fgkg595.
- Michael Zuker and Patrick Stiegler. Optimal computer folding of large RNA sequences using thermodynamics and auxiliary information. *Nucleic acids research*, 9(1):133–148, 1981.

A PSEUDOCODE FOR RNA SECONDARY STRUCTURE TO DEPENDENCY STRUCTURE

To clearly explain the algorithmic logic for converting RNA secondary structures into dependency structures, we present the following pseudocode. Algorithm 1 is the main program, which uses the <code>Get_Pair</code> function defined in Algorithm 2 to generate binary tree structures from stem and pseudoknot sequences. The <code>Get_Pair</code> function, during its processing, utilizes the <code>Is_Connect</code> function defined in Algorithm 3 for decision-making. When handling unpaired structures, the algorithm employs the <code>Get_Pairs</code> function defined in Algorithm 4.

The primary input to the algorithm consists of the RNA sequence, the base pairs of stems and pseudoknots, and a list of indices representing unpaired dots. Through this algorithm, one can derive the arc connections and labels of the dependency structure for the given RNA sequence.

Algorithm 1: Algorithm for Converting RNA Secondary Structure to Dependency Structure

```
775
          Input: RNA sequence length n, stem base pairs S, pseudoknot base pairs P, unpaired base
776
                   indices D, dot-bracket notation dot, connectivity table ctList
777
          Output: Tree structure arcs and labels: stem, pseudoknot, loop, connector, root
778
       1 Initialize empty lists: last_node_list \leftarrow [], S_p \leftarrow [], P_p \leftarrow [], L_p \leftarrow []; 2 Initialize dot_indices \leftarrow {i \mid \text{dot}[i] = '.'};
779
780
          // Process Stem Pairs
781
       3 if S is not empty then
782
               Initialize dot \leftarrow ['.'] \times n;
       4
783
               foreach (l,r) in S do
784
               |\det[l-1] \leftarrow' (', \det[r-1] \leftarrow')';
785
786
               Convert dot to a string;
               Identify stem_indices \leftarrow \{i \mid dot[i] \in \{'(',')'\}\};
787
               S_p \leftarrow \text{get\_pair}(\text{dot}[\text{stem\_indices}], \text{stem\_indices});
       10
788
               Append stem_indices[-1] to last_node_list;
       11
789
       12 end
790
          // Process Pseudoknot Pairs
       13 if P is not empty then
               foreach set in P do
793
       14
                   Initialize dot \leftarrow ['.'] \times n;
       15
794
                   foreach (l, r) in set do
       16
                        dot[l-1] \leftarrow' (', dot[r-1] \leftarrow')';
       17
796
       18
                   end
797
                    Convert dot to a string;
       19
798
                    Identify pse_indices \leftarrow \{i \mid dot[i] \in \{'(',')'\}\};
       20
799
       21
                   have\_pair \leftarrow get\_pair(dot[pse\_indices], pse\_indices);
800
                   Extend P_p with have_pair;
       22
801
                   Append pse_indices[-1] to last_node_list;
       23
802
               end
       24
803
       25 end
804
          // Combine Trees Together
805
       26 Sort last_node_list in decreasing order;
806
       27 connect_pair \leftarrow \{(\text{last\_node\_list}[i], \text{last\_node\_list}[i+1]) \mid i=0 \text{ to } |\text{last\_node\_list}|-2\};
807
       28 Extend S_p with connect_pair;
808
           // Process Unpaired Bases
       29 Initialize result_list \leftarrow [], temp_list \leftarrow [];
```

```
810
811
        1 Continue the algorithm from previous part;
812
       2 for i from 0 to |dot\_indices| - 1 do
              if i = 0 or dot\_indices[i] = dot\_indices[i-1] + 1 then
813
                   Append dot\_indices[i] to temp_list;
        4
814
        5
              else
815
        6
                   Append temp_list to result_list;
816
                   temp_list \leftarrow [dot_indices[i]];
817
818
        8 Append temp_list to result_list;
819
       • L_p \leftarrow \text{get\_pairs}(\text{result\_list}, \text{last\_node\_list}[0]);
820
          // Arc Creation and Labeling
821
       10 Adjust indices in S_p, P_p, L_p to be based-1 (if necessary);
822
       In Initialize arrays arc \leftarrow [0] \times (n+1), rel \leftarrow [0] \times (n+1);
823
       12 Initialize empty dictionaries heads \leftarrow \{\}, relations \leftarrow \{\};
824
       13 foreach (head, dep) in S_p do
              heads[dep] \leftarrow head;
825
       14
              if (head, dep) or (dep, head) in S then
       15
826
                   relations [dep] \leftarrow 'stem';
       16
827
       17
              else
828
                   relations [dep] \leftarrow 'connector';
       18
829
830
       19 foreach (head, dep) in P_p do
831
              heads [dep] \leftarrow head;
       20
              if (head, dep) or (dep, head) in P then
832
       21
                   relations [dep] \leftarrow 'pseudoknot';
833
       22
       23
834
                   relations [dep] \leftarrow 'connector';
       24
835
836
       25 foreach (head, dep) in L_p do
837
              heads[dep] \leftarrow head;
838
              relations [dep] \leftarrow \text{'loop'};
       27
839
       28 for i from 1 to n do
840
              if i i s in heads then
       29
841
                   arc[i] \leftarrow heads[i];
       30
842
                   rel[i] \leftarrow relations[i];
       31
843
       32
844
                   arc[i] \leftarrow 0;
       33
                   rel[i] \leftarrow \text{'root'};
845
846
```

```
864
         Algorithm 2: Function get_pair for binary tree construction in stem/pseudoknot Structures
865
         Input: Sequence seq of symbols ('(', ')',), indices idx
866
         Output: Paired indices parse_pair representing arcs
867
       1 Initialize i ← 0, parse_pair ← [];
868
       2 while i \neq -1 and |seq| > 1 do
             index \leftarrow i;
870
             // Determine a, b, preindex, change_idx based on seq[index]
871
             if seq[index] == 1 then
872
                 a \leftarrow \text{seq[index} - 1], b \leftarrow \text{seq[index]};
873
                 preindex \leftarrow index -1, change_idx \leftarrow index;
       6
874
       7
             else
875
                 if seq[index] == 0 and seq[index - 1] == 0 then
                     a \leftarrow \text{seq[index} - 1], b \leftarrow \text{seq[index]};
876
                     preindex \leftarrow index -1, change_idx \leftarrow index;
877
      10
                 else
878
      11
      12
                     a \leftarrow \text{seq[index]}, b \leftarrow \text{seq[index} + 1];
879
                     preindex \leftarrow index, change_idx \leftarrow index + 1;
      13
880
             (c,d) \leftarrow \text{is\_connect}(a,b);
      14
             if c \neq 2 then
      15
883
                 Append (idx[change_idx], idx[preindex]) to parse_pair;
      16
                 seq[change\_idx] \leftarrow c;
884
      17
                 Remove seq[change_idx -1] and idx[change_idx -1];
885
886
             i \leftarrow i + d;
      19
887
      20 return parse_pair
888
889
         Algorithm 3: Function is_connect for Pairing Symbols
890
         Input: Symbols a, b (can be '(', ')', 0, 1)
891
         Output: New symbol c, index adjustment d
892
       _1 if a == '(' then
893
             if b== '(' then
       2
894
                 return(2, 1) // Keep processing
       3
895
             else
896
                 if b == ')' then
897
                     return (0, 0) // Pair formed
898
                 else
                     if b == 1 then
       8
900
                         return (0, -1) // Pair formed, move back
901
902
      10 else if a == 0 then
903
             if b == ')' then
      11
904
                 return (1, 0) // Pair formed
      12
905
      13
             else
                 if b == 0 then
906
      14
                     return (0, -1) // Pair formed, move back
907
      15
                 else
      16
908
                     if b == '(') then
      17
909
                         return (2, 1) // Keep processing
910
```

```
918
          Algorithm 4: Function get_pairs for Generating Loop Pairs
919
          Input: List of index sequences 1st, last node index last_node
920
          Output: List of loop pairs result
921
       1 Initialize result \leftarrow [];
922
       2 if lst is empty or all sublists in lst are empty then
923
              return result;
924
       4 foreach sub_lst in lst do
925
              if sub_lst is empty then
       5
926
927
              if sub\_lst is the last sublist and last\_node < sub\_lst[0] then
       7
928
                  for i \leftarrow 0 to |sub\_lst| - 1 do
929
                    Append (sub_lst[i] - 1, sub_lst[i]) to result;
930
              else
931
       10
                  for i \leftarrow 1 to |sub\_lst| - 1 do
       11
932
                      Append (sub_lst[i], sub_lst[i - 1]) to result;
       12
                  if sub\_lst[-1] < last\_node then
934
       13
                      Append (\operatorname{sub\_lst}[-1] + 1, \operatorname{sub\_lst}[-1]) to result;
935
       14
936
      15 return result
937
```

B EXAMPLE WORKFLOW FOR CONVERTING RNA SECONDARY STRUCTURES INTO DEPENDENCY STRUCTURES

To provide a more intuitive illustration of the RNA secondary structure conversion process, we present an example depicted in Figure B1, which demonstrates the transformation through a series of steps.

- **Step 1: Sequence Partitioning** involves dividing the RNA sequence into stems (blue), pseudoknots (red), and loops (black) based on its secondary structure.
- **Step 2: Binary Tree Construction for Stem Sequences** entails building binary trees for each stem sequence using the Get_Pair function.
- **Step 3: Binary Tree Construction for Pseudoknot Sequences** similarly constructs binary trees for pseudoknot sequences using the same method. In the example sequence, only one pseudoknot set is present. If multiple pseudoknots exist, separate binary trees are created for each set to accurately represent their interactions.
- **Step 4: Integration of Binary Trees and Root Selection** involves integrating the multiple binary trees by selecting the last node of each tree as the root and connecting the remaining last nodes to this root node, thereby forming a unified hierarchical structure.
- **Step 5: Loop Sequence Connections based on root position** establishes connections among nucleotides within loop sequences based on the position of the root node.
- **Step 6: Comprehensive Structure Integration and labeling** consolidates all the constructed structures—stems, pseudoknots, and loops—and assigns appropriate labels, resulting in a comprehensive dependency structure for the given RNA sequence.

This workflow ensures that the input RNA sequence, along with its stem and pseudoknot base pairs and the list of unpaired dot indices, is systematically transformed into a dependency structure with arc connections and labels.

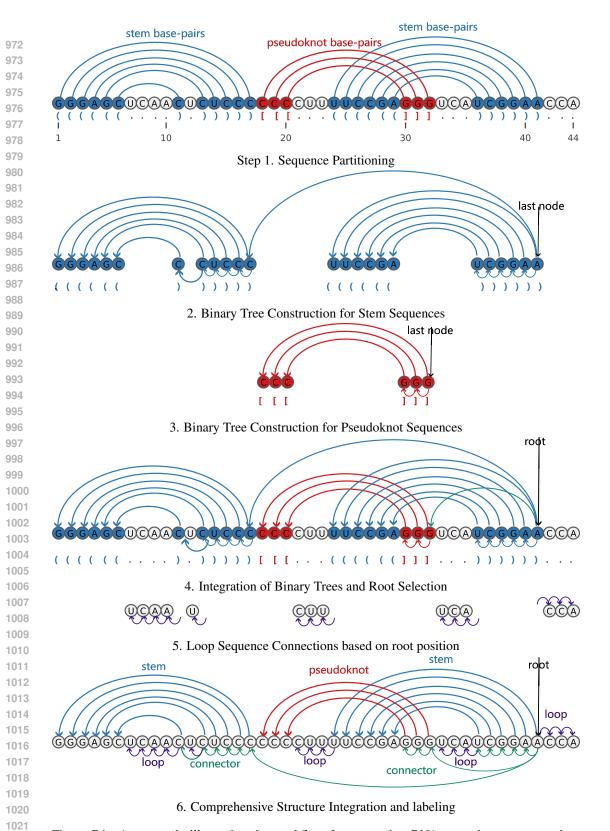


Figure B1: An example illustrating the workflow for converting RNA secondary structures into dependency structures

C TRAINING DETAILS

The code used in DEPfold primarily draws from parts of the SuPar (Zhang et al., 2020a;b) GitHub repository (https://github.com/yzhangcs/parser.git). We implemented DEPfold using PyTorch. The architecture uses Roberta-base as the encoder within a biaffine framework. Specifically, the model uses the first four layers of Roberta-base, applying mean pooling to generate a 768-dimensional representation. This encoded output is subsequently processed by two dedicated multilayer perceptrons (MLPs).

- MLP of edges: Transforms the 768-dimensional input to a 500-dimensional output.
- MLP of lables: Transforms the 768-dimensional input to a 100-dimensional output.

The outputs from these MLPs are then fed into biaffine attention layers to perform the final predictions. To mitigate overfitting, we applied a dropout rate of 0.1 to the encoder outputs and a dropout rate of 0.33 to the MLP layers.

For optimization, we used the AdamW optimizer with a dual learning rate strategy: the encoder parameters were assigned a learning rate of 5×10^{-5} , while the non-encoder parameters were set to 1×10^{-3} . This approach effectively fine-tunes the pre-trained encoder while allowing the task-specific layers to adapt rapidly. The model was trained end-to-end using a cross-entropy loss function for both arc and relation predictions, with a weight decay factor of 0.01 to further prevent overfitting.

During training, we used a batch size of 32 to maximize GPU use. The training process was capped at 100 epochs, incorporating an early stopping mechanism based on the F_1 score on the validation set. Training was terminated when the validation F_1 score ceased to improve, ensuring optimal model performance and preventing overfitting. All experiments were conducted on four NVIDIA A100-40GB GPUs, enabling efficient training and scalability.

D INFERENCE TIME COMPARISON

We evaluated the inference time of various RNA secondary structure prediction methods on the ArchiveII dataset, as summarized in Table A1. DEPfold without Optimal Tree (OT) decoding, achieved an average inference time of approximately 0.027 seconds per sequence, markedly outperforming UFold (0.071 seconds) and LinearFold (0.075 seconds). However, the full version of DEPfold, which incorporates OT, exhibited a significant increase in inference time to 1.072 seconds per sequence, making it time-consuming among those evaluated, though still within an acceptable range.

Table A1: Inference time on the ArchiveII dataset

Time	Is pseudoknot?
0.027s	Yes
1.072s	Yes
0.071s	Yes
0.477s	No
0.134s	No
0.390s	No
0.075s	No
4.454s	Yes
	0.027s 1.072s 0.071s 0.477s 0.134s 0.390s 0.075s

This disparity underscores the trade-off between prediction quality and computational efficiency introduced by OT, primarily attributable to the increased complexity of parsing pseudoknot structures. Despite the higher inference time, both versions of DEPfold retain the capability to handle pseudoknot structures, a feature absent in many traditional methods such as RNAfold and ContraFold. As a result, DEPfold without OT offers maximum inference speed, ideal for rapid predictions. Conversely, the full DEPfold version, while slower, delivers higher predictive accuracy by effectively modeling complex pseudoknots. This versatility makes DEPfold a robust tool for RNA secondary structure prediction, allowing users to balance speed and accuracy according to their research needs.

E VISUALIZATION

To intuitively demonstrate DEPfold's prediction performance, we visualized the predicted structures of three representative RNA sequences using ViennaRNA (Lorenz et al., 2011a). As illustrated in Figure E2, these sequences correspond to a short RNA, a medium-length RNA without pseudoknots, and a long RNA with pseudoknots, respectively. DEPfold's predicted results are highly consistent

with the ground truth structure. In contrast, the energy-based method ContraFold failed to effectively predict this secondary structure. Although UFold achieved a higher F_1 score than other baseline methods, its predicted results visually differed significantly from the ground truth and erroneously predicted pseudoknots that should not exist. DEPfold accurately captured these complex structural features.

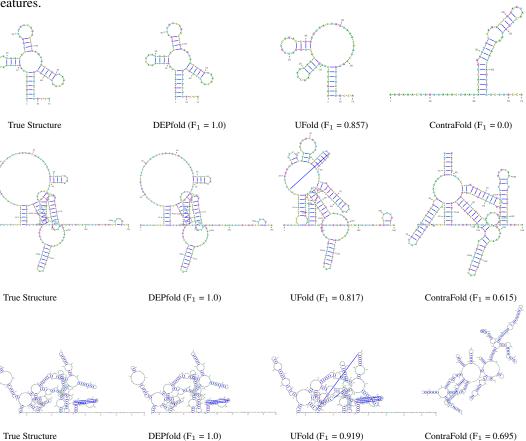


Figure E2: Comparison of RNA secondary structure predictions.