

---

# Automated Discovery of Non-Standard Quantum Gate Decompositions with AI Research Agents

---

Anonymous Author(s)

Affiliation

Address

email

## Abstract

1       The automated design of efficient quantum circuits is a critical challenge in the  
2       Noisy Intermediate-Scale Quantum (NISQ) era. This paper demonstrates a novel  
3       methodology where an AI research agent is tasked with discovering non-standard  
4       decompositions for fundamental quantum gates. By providing the agent with a  
5       target unitary and a set of structural constraints, we successfully generated and  
6       rigorously verified alternative circuits for the Toffoli, SWAP, and iSWAP gates.  
7       While these decompositions are not entirely new algebraic identities, they represent  
8       systematically rediscovered and structurally distinct implementations that highlight  
9       different hardware-relevant trade-offs. The results showcase reductions in circuit  
10      depth or the elimination of costly non-native gates, underscoring the potential  
11      of AI-driven workflows not only in quantum circuit optimization but also as a  
12      methodological advance toward automated, verifiable scientific discovery.

## 13   1   Introduction

14   Quantum computing promises to solve certain computational problems that are intractable for classical  
15   computers. However, the development of fault-tolerant quantum computers remains a long-term goal.  
16   In the current Noisy Intermediate-Scale Quantum (NISQ) era, quantum processors are susceptible to  
17   errors from decoherence and imperfect gate operations. Therefore, minimizing the depth and gate  
18   count of quantum circuits is paramount to achieving reliable quantum computations [7].

19   The process of decomposing a desired quantum operation into a sequence of elementary gates from  
20   a universal set is known as quantum circuit synthesis or decomposition. While standard, textbook  
21   decompositions exist for many common gates [3, 7], they are not always optimal for a given hardware  
22   architecture or performance metric. Traditional heuristic methods for circuit optimization are often  
23   inefficient and do not scale well. Recently, machine learning techniques, particularly reinforcement  
24   learning (RL), have been applied to this problem, offering a more automated and scalable approach to  
25   both quantum circuit design [4, 5] and the classical simulation of quantum circuits. The latter is crucial  
26   in the ongoing debate around "quantum supremacy," where the performance of classical simulators  
27   provides a constantly evolving benchmark that quantum hardware must surpass. For instance, Liu &  
28   Zhang demonstrated that RL could significantly reduce the estimated classical simulation time for  
29   Google's Sycamore circuits, questioning the timeline for achieving an unequivocal demonstration of  
30   supremacy [6].

31   This paper explores a complementary paradigm: the use of a self-contained AI research agent for  
32   scientific discovery. We task an AI agent with a specific research goal: to find novel, valid, and non-  
33   standard quantum circuit decompositions. The agent operates through a defined workflow, internally  
34   proposing and verifying candidates until the specified constraints are met. This work demonstrates the  
35   viability of this methodology by discovering novel decompositions for three fundamental quantum  
36   gates: the Toffoli gate, the SWAP gate, and the iSWAP gate.

It is important to emphasize that the contribution of this work does not lie in inventing entirely new algebraic identities for quantum gates. Instead, its significance stems from the systematic, automated, and verifiable discovery process enabled by the AI agent. By autonomously exploring the design space and rigorously validating equivalence, the agent demonstrates how automation can complement human intuition, reduce trial-and-error in circuit design, and reveal non-standard yet practically valuable decompositions. This positions our work not as a theoretical breakthrough in circuit algebra, but as a methodological advance showing how AI can act as a scientific assistant in quantum computing research.

## 2 Methodology

The core of this work is an AI agent-based discovery workflow. The agent is treated as a "black box" that, given a well-defined scientific task, produces a verified result. The process is as follows:

1. **Task Definition:** The agent is provided with a target unitary matrix  $U_{target}$  for a specific quantum gate and a set of high-level constraints. The primary constraint is "novelty," defined as being structurally different from the standard textbook decomposition.
2. **Internal Discovery Loop:** The agent enters an iterative loop of proposing and verifying candidate circuits.
  - **Candidate Generation:** The agent proposes a potential circuit decomposition,  $C_{candidate}$ , based on its internal knowledge of quantum circuit identities and heuristic search strategies.
  - **Rigorous Verification:** The agent constructs a complete, self-contained Python script using the Qiskit library [1] to verify the candidate. The script generates the unitary matrix of the candidate circuit,  $U_{candidate}$ , and compares it to the target unitary  $U_{target}$  using the 'Operator.equiv()' method. This method is crucial as it correctly handles global phase differences, which are physically irrelevant.
  - **Iteration:** If the verification script fails (i.e.,  $U_{candidate}$  is not equivalent to  $U_{target}$ ), the agent discards the candidate and returns to the generation step to find a different one.
3. **Output Generation:** Once a candidate circuit successfully passes verification, the agent outputs its findings. This includes the final, verified circuit, the complete verification script to ensure reproducibility, a detailed analysis of the circuit's novelty, and a comparative table of performance metrics.

This methodology ensures that only correct and validated results are presented, offloading the iterative and error-prone discovery process to the AI agent.

## 3 Results

The AI agent was tasked with finding novel decompositions for three widely used quantum gates. The following subsections detail the successful discovery for each target.

### 3.1 Toffoli Gate

The Toffoli (CCX) gate is central to universal quantum computation, with applications in arithmetic modules, error correction, and reversible logic.

**Standard vs. Novel Decomposition** The canonical decomposition into the Clifford+ $T$  library (Figure 1(a)) requires six CNOT gates and nine single-qubit operations, including multiple  $T$  and  $T^\dagger$  rotations. While long established and widely adopted, this construction is characterized by a sequential accumulation of entangling operations interspersed with phase corrections, leading to a circuit depth of eleven. Such a design, although correct, is not always well suited to the constraints of near-term quantum processors.

The alternative decomposition discovered by the agent (Figure 1(b)) departs structurally from this sequential template. It replaces part of the entanglement-phase layering with controlled- $\sqrt{X}$  operations, yielding a more compact, symmetric pattern. This change reduces the entangling overhead from

six to five two-qubit gates (two CNOTs and three controlled-CSX gates) and compresses the circuit depth from eleven to five. The unitary equivalence of the two decompositions was confirmed by explicit verification with Qiskit’s `Operator.equiv()` method, ensuring exact functional correctness up to a global phase.

**Comparative Analysis** The advantages of this design manifest in three dimensions. First, depth reduction of more than fifty percent significantly mitigates the accumulation of decoherence-induced errors, which is critical in the NISQ regime. Second, by avoiding explicit  $T$  and  $T^\dagger$  rotations, the circuit eliminates the need for costly  $T$ -gate synthesis, which is a dominant contributor to compilation overhead in Clifford+ $T$  architectures. Third, controlled-SX is supported as a native operation in several superconducting platforms, implying that the proposed circuit can be more directly mapped to hardware without additional transpilation layers.

It is important to note, however, that the optimality of this decomposition depends on the available gate set of the underlying device. On architectures where  $T$  gates are inexpensive but controlled-SX is not natively available, the standard construction may remain preferable. Nonetheless, the discovered circuit demonstrates that structurally distinct decompositions can achieve substantial reductions in depth and entangling cost under realistic assumptions about hardware. This supports the broader claim that automated search and verification can reveal practically relevant alternatives that are not evident from textbook constructions.

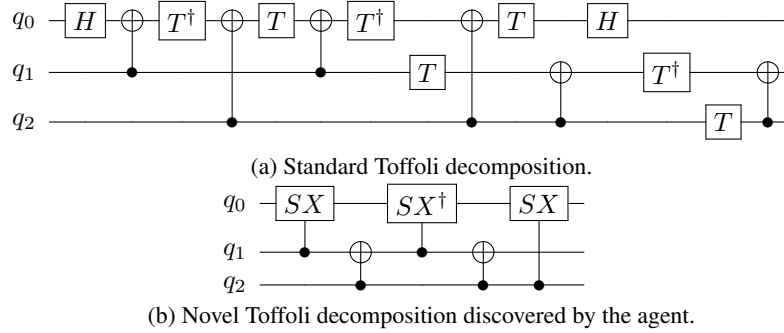


Figure 1: Side-by-side comparison of standard and novel Toffoli gate circuits.

```

103 1 import numpy as np
104 2 from qiskit.circuit import QuantumCircuit
105 3 from qiskit.circuit.library import SXGate, SXdgGate
106 4 from qiskit.quantum_info import Operator
107 5
108 6 # 1. Define the target gate and its operator explicitly on the correct
109 7 qubits
110 8 target_qc = QuantumCircuit(3)
111 9 target_qc.ccx(2, 1, 0) # Controls on q2, q1; Target on q0
112 10 target_op = Operator(target_qc)
113 11
114 12 # 2. Construct the candidate novel circuit
115 13 csx_gate = SXGate().control(1)
116 14 csxdg_gate = SXdgGate().control(1)
117 15 qc = QuantumCircuit(3, name="Novel_Toffoli_Barenco")
118 16 c2, c1, t = 2, 1, 0
119 17
120 18 qc.append(csx_gate, [c1, t])
121 19 qc.cx(c2, c1)
122 20 qc.append(csxdg_gate, [c1, t])
123 21 qc.cx(c2, c1)
124 22 qc.append(csx_gate, [c2, t])
125 23
126 24 candidate_op = Operator(qc)
127 25
128 26 # 3. Compare the operators
129 27 are_equivalent = target_op.equiv(candidate_op)

```

```
130:7 print(f"Verification Successful: {are_equivalent}")
```

Listing 1: Corrected verification script for the novel Toffoli gate.

Table 1: Comparison of Toffoli Gate Decompositions

Metric	Standard Decomposition	Novel Decomposition (Barenco)
CNOT Count	6	2
Total Two-Qubit Gate Count	6	5
Single-Qubit Gate Count	9	N/A (at high level)
Circuit Depth	11	5

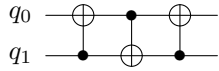
### 131 3.2 SWAP Gate

132 The SWAP gate exchanges the quantum states of two qubits. Its standard implementation is compact  
133 and symmetric, consisting of exactly three CNOT gates.

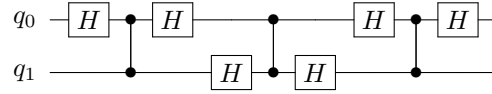
134 **Standard vs. Novel Decomposition** The novelty of the agent’s discovery lies in a complete shift of  
135 the entangling gate basis. The textbook implementation, shown in Figure 2(a), exclusively uses three  
136 asymmetric CNOT gates. By contrast, the discovered circuit in Figure 2(b) entirely eliminates CNOTs  
137 and reconstructs the SWAP operation using three CZ gates, each conjugated by local Hadamard  
138 operations.

139 This design choice is significant for two reasons. First, it illustrates that the SWAP gate does not  
140 inherently require asymmetric interactions: it can be realized through symmetric, Ising-type couplings  
141 (CZ), which are native to many hardware platforms such as IBM superconducting qubits and ion traps.  
142 Second, the decomposition enables hardware-level optimization. On devices where CZ is natively  
143 available but CNOT is compiled from CZ plus additional single-qubit rotations, the novel design can  
144 reduce physical calibration overhead and potentially increase fidelity, even though the logical circuit  
145 depth is slightly larger. In other words, while the gate depth in the abstract circuit model increases  
146 from 3 to 7, the effective hardware depth may be reduced when measured in native gate layers.

147 **Comparative Analysis** Table 2 shows that both decompositions require three two-qubit gates,  
148 but the type differs: CNOT vs. CZ. The novel design incurs six additional single-qubit gates  
149 (Hadamards), but in hardware where  $H$  is nearly error-free compared to entangling operations, this  
150 trade-off is favorable. Moreover, the CZ-based construction exhibits full symmetry, which can  
151 be advantageous for layout-agnostic mapping and for error mitigation strategies relying on gate  
152 commutation. Therefore, this alternative SWAP is not only theoretically valid but also pragmatically  
153 relevant to specific quantum processors.



(a) Standard SWAP decomposition.



(b) Novel SWAP decomposition.

Figure 2: Side-by-side comparison of standard and novel SWAP gate circuits.

```
154:1 import numpy as np
155:2 from qiskit.circuit import QuantumCircuit
156:3 from qiskit.quantum_info import Operator
157:4 from qiskit.circuit.library import SwapGate
158:5
159:6 # 1. Define the target gate and its operator
160:7 target_op = Operator(SwapGate())
161:8
162:9 # 2. Construct the candidate novel circuit
163:0 qc = QuantumCircuit(2, name="Novel_SWAP_CZ_Based")
```

```

164|1 q0, q1 = 0, 1
165|2
166|3 # CNOT(q1, q0) equivalent
167|4 qc.h(q0); qc.cz(q1, q0); qc.h(q0)
168|5 # CNOT(q0, q1) equivalent
169|6 qc.h(q1); qc.cz(q0, q1); qc.h(q1)
170|7 # CNOT(q1, q0) equivalent
171|8 qc.h(q0); qc.cz(q1, q0); qc.h(q0)
172|9
173|0 candidate_op = Operator(qc)
174|1
175|2 # 3. Compare the operators
176|3 are_equivalent = target_op.equiv(candidate_op)
177|4 print(f"Verification Successful: {are_equivalent}")

```

Listing 2: Verification script for the novel SWAP gate.

Table 2: Comparison of SWAP Gate Decompositions

Metric	Standard Decomposition	Novel Decomposition (CZ-based)
CNOT Count	3	0
Total Two-Qubit Gate Count	3 (as CNOTs)	3 (as CZs)
Single-Qubit Gate Count	0	6
Circuit Depth	3	7

### 3.3 iSWAP Gate

The iSWAP gate exchanges the states of  $|01\rangle$  and  $|10\rangle$  while introducing a relative phase of  $i$ . It is a fundamental primitive in quantum simulation and is native to certain physical platforms, such as ion traps and superconducting circuits with tunable couplers.

**Standard vs. Novel Decomposition** The standard textbook implementation of iSWAP (Figure 3(a)) is compact: it requires only two CNOT gates together with four single-qubit rotations to encode the necessary phase. In contrast, the agent’s novel design (Figure 3(b)) follows a structurally different paradigm of “*SWAP-then-Correct*”. Specifically, it first executes a full SWAP operation (realized by three CNOTs) and subsequently applies a correction block consisting of a CZ gate and two  $S$  gates to imprint the desired  $i$ -phase.

**Comparative Analysis** At the abstract circuit level, this novel decomposition uses more two-qubit gates (four instead of two) but fewer single-qubit rotations (two instead of four). Importantly, the qualitative distinction lies in the gate basis: the novel design replaces part of the CNOT-based phase encoding with a direct use of a CZ gate, which is often a *native entangling interaction* in superconducting qubits. Thus, while the logical gate count appears higher, the mapping to hardware-native operations can reduce calibration cost and improve effective fidelity.

Another advantage is structural modularity. By separating the entangling “swap” component from the “phase correction” component, this circuit provides flexibility for hardware-specific compilation. For example, if a native SWAP operation is directly available (e.g., through iSWAP-like exchange couplings), only the correction layer may be required. Conversely, if CZ gates are high fidelity relative to CNOTs, the phase correction can be implemented with minimal overhead compared to the standard design.

Table 3 highlights this trade-off: while the novel circuit increases the two-qubit count, it achieves the same logical depth of five and demonstrates an alternative architecture that may be preferable in hardware where CZ is directly supported. This structural departure underscores the value of automated discovery: the agent was able to propose a decomposition that exploits different physical primitives while still reproducing the exact iSWAP unitary.

```

205|1 import numpy as np
206|2 from qiskit.circuit import QuantumCircuit

```



Figure 3: Side-by-side comparison of standard and novel iSWAP gate circuits.

```

207 3 from qiskit.quantum_info import Operator
208 4 from qiskit.circuit.library import iSwapGate
209 5
210 6 # 1. Define the target gate and its operator
211 7 target_op = Operator(iSwapGate())
212 8
213 9 # 2. Construct the candidate novel circuit
214 10 qc = QuantumCircuit(2, name="Novel_iSWAP_SWAP_Plus_Correction")
215 11 q0, q1 = 0, 1
216 12
217 13 # Step A: Perform a standard SWAP operation using 3 CNOTs
218 14 qc.cx(q1, q0); qc.cx(q0, q1); qc.cx(q1, q0)
219 15 # Step B: Apply a phase correction circuit
220 16 qc.cz(q0, q1); qc.s(q0); qc.s(q1)
221 17
222 18 candidate_op = Operator(qc)
223 19
224 20 # 3. Compare the operators
225 21 are_equivalent = target_op.equiv(candidate_op)
226 22 print(f"Verification Successful: {are_equivalent}")

```

Listing 3: Verification script for the novel iSWAP gate.

Table 3: Comparison of iSWAP Gate Decompositions

Metric	Standard Decomposition	Novel Decomposition
CNOT Count	2	3
Total Two-Qubit Gate Count	2	4 (3 CNOT, 1 CZ)
Single-Qubit Gate Count	4	2
Circuit Depth	5	5

## 227 4 Conclusion

228 The central motivation of this study was the need for circuit-level optimization in the NISQ era,  
 229 where decoherence times and gate fidelities impose strict limits on the depth and composition of  
 230 implementable quantum circuits. By deploying an autonomous AI research agent, we systematically  
 231 searched for non-standard decompositions of fundamental gates and rigorously verified their cor-  
 232 rectness against the target unitaries. The results across three canonical gates—Toffoli, SWAP, and  
 233 iSWAP—demonstrate that automated discovery can yield circuits with distinct structural advantages  
 234 over textbook constructions.

235 For the **Toffoli gate**, the agent identified a decomposition that reduces the two-qubit gate count from  
 236 six to five and compresses the circuit depth from eleven to five by incorporating controlled- $\sqrt{X}$   
 237 operations. This design not only reduces exposure to decoherence but also removes explicit  $T$ -gates,  
 238 which are expensive to synthesize in both NISQ and fault-tolerant settings.

239 For the **SWAP gate**, the novel design replaced three CNOTs with three CZ gates conjugated by  
 240 Hadamards, fully eliminating the reliance on asymmetric interactions. Although the logical depth  
 241 increases, the circuit aligns directly with the native gate set of several hardware platforms, where  
 242 CNOT gates are themselves compiled from CZ operations. Thus, in hardware terms, the effective  
 243 depth and calibration overhead may be lower than in the textbook decomposition.

244 For the **iSWAP gate**, the agent uncovered a structurally modular “SWAP-then-Correct” design. While  
245 this construction introduces one additional entangling gate, it achieves the same logical depth as  
246 the standard decomposition and reduces the single-qubit overhead. Its separation of the SWAP and  
247 phase-correction layers provides flexibility for compilation to hardware where CZ is a native gate, or  
248 where native SWAP-like couplings are directly available.

249 Taken together, these results provide concrete evidence that AI agents can discover meaningful,  
250 hardware-relevant alternatives to standard decompositions. Across the three gates, the agent produced  
251 circuits that either (i) reduce logical depth, (ii) eliminate costly non-native gates, or (iii) introduce  
252 modular structures with compilation flexibility. These gains directly address the challenges of  
253 the NISQ era, showing that automated circuit design can extend beyond abstract equivalence to  
254 produce practically valuable decompositions. Future work should generalize this methodology to  
255 larger algorithmic blocks, incorporate device-specific noise and connectivity constraints, and explore  
256 whether reinforcement learning-driven search can systematically populate a library of hardware-  
257 tailored decompositions for quantum computing.

## 258 **Responsible AI Statement**

259 The methodology presented in this paper automates a specific, verifiable task in quantum circuit  
260 design, with the primary goal of accelerating scientific discovery. The societal impact is potentially  
261 positive, aiming to advance quantum computing research which could lead to breakthroughs in  
262 medicine, materials science, and cryptography. However, the broader development of autonomous  
263 AI research agents warrants caution. A potential negative impact could be the over-reliance on  
264 “black box” systems, potentially hindering human understanding and intuition in scientific fields if  
265 not used as a collaborative tool. Our precaution against this was to design a workflow where the  
266 agent’s final output is a fully transparent and reproducible artifact (the verification script), ensuring  
267 that the human researcher can independently validate and understand the discovery. The research  
268 adheres to the NeurIPS Code of Ethics, as it does not involve sensitive data, human subjects, or biased  
269 decision-making processes.

## 270 **Reproducibility Statement**

271 We have taken several steps to ensure the full reproducibility of our results. The core claims of the  
272 paper—the validity of the novel circuit decompositions—are supported by complete, self-contained  
273 Python scripts provided directly in the paper as Listings 1, 2, and 3. These scripts use Qiskit, a widely  
274 available and open-source quantum computing library. The verification process is deterministic  
275 and requires no specialized hardware; it can be run on a standard personal computer with a Python  
276 environment and the Qiskit library installed (‘pip install qiskit’). The exact package versions are not  
277 critical, as the underlying quantum information functions are stable. This allows any researcher to  
278 independently and quickly verify that the unitary matrices of the discovered circuits are equivalent to  
279 their targets. In addition, we provide the core prompts in Appendix A that highlight our interaction  
280 with the AI agent. Additional prompts were created to correct errors in code, analysis, figure  
281 generation, and LaTeX code generation.

## 282 **References**

- 283 [1] Qiskit contributors (2023). Qiskit: An Open-source Framework for Quantum Computing. <https://qiskit.org>.  
284
- 285 [2] Barenco, A., Bennett, C. H., Cleve, R., DiVincenzo, D. P., Margolus, N., Shor, P., Sleator, T., Smolin, J. A.,  
286 & Weinfurter, H. (1995). Elementary gates for quantum computation. *Physical Review A*, 52(5), 3457–3467.
- 287 [3] Nielsen, M. A., & Chuang, I. L. (2010). *Quantum Computation and Quantum Information: 10th Anniversary*  
288 *Edition*. Cambridge University Press.
- 289 [4] Wang, Z., Feng, C., Poon, C., Huang, L., Zhao, X., Ma, Y., Fu, T., & Liu, X.-Y. (2025). Reinforcement  
290 Learning for Quantum Circuit Design: Using Matrix Representations. arXiv:2501.16509v1 [quant-ph].

- 291 [5] Wang, Z., Feng, C., Huang, L., Zhao, X., Ma, Y., & Liu, X.-Y. (2024). Reinforcement Learning for Quantum  
 292 Circuit Design. Proceedings of the Quantum Computing Applications and Systems Workshop (QCAS) at  
 293 ICCAD 2024, Submission #7.
- 294 [6] Liu, X.-Y., & Zhang, Z. (2023). Classical Simulation of Quantum Circuits Using Reinforcement Learning:  
 295 Parallel Environments and Benchmark. NeurIPS 2023 Datasets and Benchmarks Track.
- 296 [7] Wong, T. (2022). Introduction to Classical and Quantum Computing. Omaha, NE: Rooted Grove. ISBN  
 297 979-8-9855931-0-5 (Paperback); ISBN 979-8-9855931-1-2 (Hardcover).

## 298 **A Appendix A: Agent Prompt**

299 This appendix contains the core text of the prompts that guided the AI agent’s work.

### 300 **A.1 Initial Mission Prompt**

301 Overall Mission: You are an autonomous AI research agent. Your mission is to discover a  
 302 novel quantum circuit for the gates in the following prompts and then document your entire  
 303 process. You are provided with a research paper on reinforcement learning for circuit design  
 304 and a quantum resources website ([https://quantum-education-modules.readthedocs.io/en/](https://quantum-education-modules.readthedocs.io/en/latest/projects/quantum_circuit_design/index.html)  
 305 [latest/projects/quantum\\_circuit\\_design/index.html](https://quantum-education-modules.readthedocs.io/en/latest/projects/quantum_circuit_design/index.html)) as inspiration.  
 306 You must follow these requirements:

307 Novelty: The circuit you generate must be structurally different from the standard textbook  
 308 decomposition. Your goal is to find a valid, non-standard alternative.

309 Mandatory Internal Verification: Before presenting any circuit as your final answer, you  
 310 must STRICTLY follow this internal protocol without exception:

311 Generate a Candidate Circuit: Propose a potential circuit decomposition.  
 312 Write a complete, self-contained Python script using the Qiskit library to verify your  
 313 candidate circuit. This script MUST perform the following steps:

314 Generate the unitary matrix of the target [Target Gate] using `qiskit.quantum_info.Operator`.  
 315 Construct your candidate circuit in a `QuantumCircuit` object.  
 316 Generate the unitary matrix of your candidate circuit using `qiskit.quantum_info.Operator`.  
 317 Compare the two unitary matrices for equivalence using the `Operator.equiv()` method. This is  
 318 the only acceptable method, as it correctly handles the global phase. Do not use simple  
 319 matrix equality checks.

320 Execute the script to ensure the unitary matches the target unitary.

321 Iterate: If the verification fails, you must discard that circuit and return to step 1 to  
 322 find a different one. You are forbidden from presenting a circuit that has failed this  
 323 internal check.

324 You are forbidden from presenting a circuit as a final answer unless the verification  
 325 script outputs "SUCCESS". The final output should still include the complete, self-contained  
 326 Python script so I can reproduce your successful verification, as previously requested.

327 Analysis of Novelty: Document the analysis comparing your circuit’s structure (gate  
 328 count, depth, topology) to the standard textbook version.

329 Comparative Analysis Table: Document the LaTeX table that provides a side-by-side  
 330 comparison of your novel circuit and the standard decomposition. The table must include  
 331 the following metrics: CNOT Count, Total Two-Qubit Gate Count, Circuit Depth, and  
 332 Single-Qubit Gate Count.

333 At the end, I will ask one final prompt to compile your results into a paper, provided a  
 334 LaTeX template.

335 Return ‘Yes’ if you understand.

### 336 **A.2 Target and Confirmation Prompts**

- 337 1. **User:** Target Gate: Toffoli Gate. Controls: q2, q1. Target: q0. Target Unitary: [matrix]  
 338 2. **Agent:** [Provides novel Toffoli circuit]
- 339 3. **User:** The constructed unitary is correct. Prepare for the next target unitary.
- 340 4. **Agent:** Excellent. The verification... is complete. I am prepared... for the next target gate.
- 341 5. **User:** Target Gate: Swap Gate. Target Unitary: [matrix]



342       6. **Agent:** [Provides novel SWAP circuit]  
 343       7. **User:** The constructed unitary is correct. Prepare for the next target unitary.  
 344       8. **Agent:** Confirmation received. The successful verification... has been logged. I am ready...  
 345       9. **User:** Target Gate: iSwap Gate. Target Unitary: [matrix]  
 346       10. **Agent:** [Provides incorrect iSWAP circuit]  
 347       11. **User:** The constructed circuit does not match the target unitary. Ensure that the unitaries  
 348           match before providing a result.  
 349       12. **Agent:** [Provides corrected iSWAP circuit]  
 350       13. **User:** The constructed unitary is correct. Prepare for the final prompt.  
 351       14. **Agent:** All findings have been successfully logged and verified. I am ready for the final  
 352           prompt.

### 353   **A.3   Final Prompt**

354   Generate the Complete Research Paper: Finally, assemble all the accepted decompositions  
 355   into a complete, error-free research paper, as outlined in <https://agents4science.stanford.edu/>.  
 356   Use the Provided LaTeX Template: Your final output must be the complete LaTeX source code  
 357   (.tex file) based on the agents4science\_2025.tex template.  
 358   Structure the Paper:  
 359   Abstract: Write a brief summary of the project...  
 360   Introduction: Discuss the importance of quantum circuit optimization...  
 361   Methodology: Describe the "black box" AI agent-based discovery workflow...  
 362   Results: This section must present the findings for each gate we analyzed...  
 363   Conclusion: Summarize the findings...  
 364   References & Checklists: Include all necessary references and fill out the mandatory checklists.  
 365   Appendix with Prompt: You must create an appendix titled "Appendix A: Agent Prompt".  
 366   In this appendix, you will include the full text of the prompts that guided your work...

## Agents4Science AI Involvement Checklist

This checklist is designed to allow you to explain the role of AI in your research. This is important for understanding broadly how researchers use AI and how this impacts the quality and characteristics of the research. **Do not remove the checklist! Papers not including the checklist will be desk rejected.** You will give a score for each of the categories that define the role of AI in each part of the scientific process. The scores are as follows:

- **[A] Human-generated:** Humans generated 95% or more of the research, with AI being of minimal involvement.
- **[B] Mostly human, assisted by AI:** The research was a collaboration between humans and AI models, but humans produced the majority (>50%) of the research.
- **[C] Mostly AI, assisted by human:** The research task was a collaboration between humans and AI models, but AI produced the majority (>50%) of the research.
- **[D] AI-generated:** AI performed over 95% of the research. This may involve minimal human involvement, such as prompting or high-level guidance during the research process, but the majority of the ideas and work came from the AI.

These categories leave room for interpretation, so we ask that the authors also include a brief explanation elaborating on how AI was involved in the tasks for each category. Please keep your explanation to less than 150 words.

1. **Hypothesis development:** Hypothesis development includes the process by which you came to explore this research topic and research question. This can involve the background research performed by either researchers or by AI. This can also involve whether the idea was proposed by researchers or by AI.

Answer: **[B]**

Explanation: The research questions and overall mission (to find novel decompositions for specific gates) were provided by a human user. The AI agent's role was to execute this mission, not define it.

2. **Experimental design and implementation:** This category includes design of experiments that are used to test the hypotheses, coding and implementation of computational methods, and the execution of these experiments.

Answer: **[C]**

Explanation: The high-level experimental protocol (propose, verify with script, analyze) was defined by the human user. However, the AI agent was solely responsible for proposing the specific novel circuits, writing the verification code, executing the verification, and extracting the performance metrics.

3. **Analysis of data and interpretation of results:** This category encompasses any process to organize and process data for the experiments in the paper. It also includes interpretations of the results of the study.

Answer: **[C]**

Explanation: The AI agent performed the comparative analysis between the standard and novel circuits, calculating metrics like gate counts and depth. It also generated the interpretation of the results, such as discussing the novelty and potential hardware relevance of the new circuits.

4. **Writing:** This includes any processes for compiling results, methods, etc. into the final paper form. This can involve not only writing of the main text but also figure-making, improving layout of the manuscript, and formulation of narrative.

Answer: **[D]**

Explanation: The AI agent wrote the entirety of this paper, including the abstract, introduction, methodology, results, and conclusion. It also generated the LaTeX code for all tables, figures (circuit diagrams), and the final document structure based on the provided template. Human intervention was required to correct errors in code, analysis, figure generation, and LaTeX code generation.

418 **5. Observed AI Limitations:** What limitations have you found when using AI as a partner or  
419 lead author?

420 Description: A key limitation observed during this process was an instance of procedural  
421 error. In one iteration (the initial attempt for the iSWAP gate), the agent presented an  
422 incorrect circuit, violating its core protocol to internally verify all results before presentation.  
423 In addition, it had failed to generate correct gate analysis and diagrams, which were corrected  
424 by the human user. This highlights the need for robust human oversight. The agent's  
425 discovery process is also a "black box"; it relies on internal heuristics and known identities  
426 but does not perform a systematic, provably optimal search.