# CoMoE: Contrastive Representation for Mixture-of-Experts in Parameter-Efficient Fine-tuning

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#### Abstract

In parameter-efficient fine-tuning, mixtureof-experts (MoE), which involves specializing functionalities into different experts and sparsely activating them appropriately, has 005 been widely adopted as a promising approach to trade-off between model capacity and computation overhead. However, current MoE variants fall short on heterogeneous datasets, ignoring the fact that experts may learn similar knowledge, resulting in the underutilization of MoE's capacity. In this paper, we propose Contrastive Representation for MoE (CoMoE), a novel method to promote modularization and specialization in MoE, where the experts are trained along with a contrastive objective by sampling from activated and inactivated experts in top-k routing. We demonstrate that such 017 a contrastive objective recovers the mutualinformation gap between inputs and the two types of experts. Experiments on several bench-021 marks and in multi-task settings demonstrate that CoMoE can consistently enhance MoE's capacity and promote modularization among 024 the experts.

# 1 Introduction

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Parameter-Efficient Fine-Tuning (PEFT) has emerged to efficiently adapt Large Language Models (LLMs) to downstream tasks by updating only a subset of parameters, significantly reducing computational and memory overhead (Hu et al., 2021; Liu et al., 2022; He et al., 2021). However, it struggles with substantially increased dataset sizes, especially heterogeneous training datasets, which poses a significant practical challenge (Huang et al., 2024; Wang et al., 2024). Mixture-of-Experts (MoE) offers a versatile solution to the challenge for its modular design (Zhang et al., 2024).

Thus, Low-rank Adaptation (LoRA), as a popular and effective PEFT method, has been widely integrated with MoE (Dou et al., 2023; Li et al., 2024), leveraging MoE's modularity to enhance the model's capacity and performance. By sparsely activating a subset of experts, LoRA's MoE variants achieve efficient training on heterogeneous datasets and allocate the experts adaptively (Tian et al., 2024). Specifically, the sparse activation is controlled through a router mechanism (e.g., topk routing) that dispatches inputs to the activated experts. Basically, given an input token, only a subset of specialized experts contribute to the output, while other irrelevant experts remain inactive.

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Ideally, each expert should specialize in distinct representation subspaces and semantic skills, thereby collaboratively enhancing the model's representational capacity and enabling a broader spectrum of knowledge (Liu et al., 2023). However, despite the explicit division into multiple experts in MoE architecture, its modularization degree remains questionable. Two issues persist: (1) expert knowledge redundancy, where insufficient specialization constraints lead to overlapping functionalities among experts, limiting the model's capacity (Feng et al., 2025); (2) expert load imbalance, where inadequate modularity and specialization during training result in frequent activation of only a subset of experts, which underutilizes other experts and contradicts its original design intent. Consequently, as some studies have indicated (Qian et al., 2024), simply stacking more experts does not linearly improve performance; instead, it leads to a performance bottleneck. Existing studies propose load balance loss (Li et al., 2024) and localized balancing constraint (Dou et al., 2023) to alleviate the mentioned issues, but that is still far from enough.

In this paper, we propose a novel perspective to promote the specialization of experts. As illustrated in Fig. 1, building upon top-k routing, we categorize the experts into activated experts and inactivated experts. Then, we quantify the specialization of experts by mutual information (MI) between the input token and the two types of experts. To promote expert specialization, we define



Figure 1: Given an input token x, (a) illustrates the workflows of top-2 routing, which serves as a fundamental mechanism of CoMoE; (b) illustrates the motivation of CoMoE: maximizing MI between input x and activated experts while minimizing MI between input x and inactive experts.

an MI gap, which is derived from the aforementioned MI, and aim to maximize it. In practice, based on the InfoNCE theory (Oord et al., 2018), such an MI gap can be approximated via a contrastive objective by using positive samples from the activated experts and negative samples from the inactive experts (Lan et al., 2024; Wen et al., 2024). The contrastive objective is incorporated as an auxiliary objective during training, encouraging specialization and modularization among experts. We name the proposed method **Contrastive Repre**sentation for MoE (CoMoE), a novel MoE variant. Empirically, we evaluate CoMoE on diverse benchmarks, showcasing its remarkable performance on heterogeneous tasks. Summary of our contributions:

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- We define an MI gap to quantify expert specialization and redundancy in top-k routing, with contrastive learning providing an efficient estimation approach.
- We propose a novel MoE variant, named Co-MoE, which incorporates an auxiliary contrastive objective to enhance expert specialization and modularization.
- Comprehensive experiments are conducted to demonstrate that our method consistently improves MoE on heterogeneous tasks.

# 2 Preliminaries

**LoRA Basics** LoRA (Hu et al., 2021) introduces a pair of low-rank matrices  $\mathbf{A}$  and  $\mathbf{B}$  to reparameterize the pretrained weights  $\mathbf{W}_0$  in a residual manner. Specifically, input x is processed through both the frozen weights and the low-rank matrices:

$$y' = \mathbf{W}_{\mathbf{0}}x + \mathbf{B}\mathbf{A}x,\tag{1}$$

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where y' denotes the output, with  $\mathbf{A} \in \mathbb{R}^{r \times d_2}$  and  $\mathbf{B} \in \mathbb{R}^{d_1 \times r}$ . The rank  $r \ll \min(d_1, d_2)$  is significantly small to reduce tunable parameters.

**Mixture of Experts** In LoRA's MoE variants, the original LoRA module is substituted with n parallel experts, each denoted as  $\{E_i(x) = \mathbf{B_i A_i} x\}_{i=1}^n$ . These experts are activated via a router  $g(x; \mathbf{G})$  to process the input collaboratively. Specifically, given an input x, the router calculates the importance of each expert, and the output y' is computed residually as a weighted sum of outputs from the experts:

$$y' = \mathbf{W}_0 x + \sum_{i=1}^n g_i(x; \mathbf{G}) E_i(x),$$
 (2)

where  $g_i(x; \mathbf{G})$  represents the weight of the *i*-th expert, and  $E_i(x)$  denotes the output of expert *i*. **Top-k Routing** Top-k routing is a common and effective routing strategy of the router  $g(x; \mathbf{G})$  in MoE, which sparsely activates a subset of the experts. Specifically, only the top k experts with the highest values in  $g(x; \mathbf{G})$  are activated. Then,  $g(x; \mathbf{G})$  is renormalized for the activated experts. The renormalization is computed as follows:

$$\hat{g}_i(x) = \begin{cases} \frac{g_i(x)}{\sum_{j \in \mathsf{top}(g(x),k)} g_j(x)} & \text{if } i \in \mathsf{top}(g(x),k) \\ 0 & \text{if } i \notin \mathsf{top}(g(x),k) \end{cases},$$
(3)

where top(g(x), k) returns the indices of the largest k elements in g(x).

## 3 Related Works

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## 3.1 Parameter-Efficient Fine-Tuning

PEFT methods can be categorized into Adapter Tuning, Prompt Tuning, and Prefix Tuning: **Adapter Tuning** (Hu et al., 2023, 2021; Zhang et al., 2023b) includes algorithms like BitFit (Zaken et al., 2021), which links learnable vectors to hidden states using multiplication or addition. (IA)<sup>3</sup> (Liu et al., 2022) introduces interpretable adapters to enhance model transparency and taskspecific adaptability. **Prompt-Tuning** (Li and Liang, 2021; Liu et al., 2021; Zhu et al., 2024) introduces learnable prefixes to the input sequence. **Prefix-Tuning** (Li and Liang, 2021) modifies hidden states by adding embeddings, making it efficient for few-shot tasks.

LoRA (Hu et al., 2021) reduces the number of tunable parameters by introducing low-rank matrices into pre-trained weights, enhancing performance and efficiency. Currently, LoRA becomes the most popular and commonly used PEFT method (Cui et al., 2023; Zhang et al., 2022). Numerous studies have focused on improving LoRA: Tied-LoRA (Renduchintala et al., 2023) further reduces trainable parameters by applying weight binding. AdaLoRA (Zhang et al., 2023a) utilizes singular value decomposition to decompose the weight matrices and eliminates insignificant singular values, thereby simplifying the update process. DoRA (Liu et al., 2024) decomposes weights into magnitude and direction components for efficiency.

### 3.2 Mixture of Experts

Recent research has increased its focus on combining LoRA with MoE (Shazeer et al., 2017; Jacobs et al., 1991) for adaptable and scalable LLMs, emerging as a balance between model capacity and computation overhead (Li et al., 2024; Zhang et al., 2024). Generally, MoE is employed for two primary purposes: (1)Avoiding catastrophic forgetting: LoRAMoE (Dou et al., 2023) leverages token-based routing to mitigate knowledge loss. MOELoRA (Liu et al., 2023) enhances expert selection in multi-tasking. MoRAL (Yang et al., 2024) adapts to new tasks in lifelong learning while preserving old knowledge. (2) Model efficiency: HydraLoRA (Tian et al., 2024) adopts an asymmetric LoRA structure without domain expertise, and MiLoRA (Zhang et al., 2024) employs a promptaware routing to reduce latency. LoRAMoE (Dou et al., 2023) incorporates a localized balancing constraint to achieve balanced workloads. SCMoE (Shi et al., 2024) leverages unchosen experts to enhance parameter efficiency. Current methods focus on architectural expert partitioning but neglect capacity underutilization caused by expert redundancy.

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#### 4 Methods

In this section, we first define an MI gap for topk routing. Then we derive a contrastive objective to estimate the gap with learning expert representations. Finally, we present a training approach that incorporates the contrastive objective as an auxiliary loss.

# 4.1 Motivation

As demonstrated in OMoE (Feng et al., 2025), the vanilla MoE variant lacks specialization and modularity, causing LoRA experts to collapse into similar distributions. The lack of specialization and redundant knowledge minimizes the utilization of capacity, which exacerbates performance degradation in heterogeneous tasks. Existing MoE variants (Li et al., 2024; Liu et al., 2023; Luo et al., 2024) leverage balance loss to promote specialization among the experts, but fall far short.

Ideally, experts should exhibit modularity and high specialization with minimal redundancy. To quantify these properties, we leverage MI, a basic concept in information theory, to evaluate the dependence between inputs and experts in MoE. Thus, we formalize the aforementioned idea using MI to quantify the specialization and redundancy between the experts in top-k routing:

- Maximizing the MI between inputs and activated experts: Promote activated experts to respond to inputs that highly match, thereby encouraging specialization. In addition, MI serves as an information bottleneck that filters irrelevant noise.
- Minimizing the MI between inputs and inactivated experts: Suppress the response of inactivated experts to irrelevant inputs, thereby preventing multiple experts from learning similar representations.

## 4.2 MI Gap for Top-k Routing

Building upon the motivation, we begin by defining an MI Gap for input token x and task experts set M in top-k routing. For simplicity, we denote  $I(\cdot; \cdot)$  as MI,  $H(\cdot)$  as Shannon entropy, and  $E_i(\cdot)$ 



Figure 2: Architecture of CoMoE. Activated experts  $e_i^t$ ,  $i \in \text{top2}$  in top-2 routing are selected as the query q and positive keys  $k^+$ , while inactivated experts  $e_i^t$ ,  $i \notin \text{top2}$  serve as negative keys  $k^-$ .

as the network of expert *i*. Correspondingly, the representations of activated and inactivated experts are formulated as  $e^+ = E^+(x)$  and  $e^- = E^-(x)$ .

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Given an input token, an ideal expert in MoE should retain specialized knowledge while discarding redundant knowledge with others. Intuitively, this equals the uncertainty reduction in the activated experts given the input token. We use p to denote the joint distribution as well as their associated marginals. Then the MI between the input token x and task experts set M is defined as:

$$I(x; M) = \mathbb{E}_{x, \mathcal{M} \sim \mathcal{D}} \left[ \log \frac{p(M|x)}{p(M)} \right]$$
(4)

where p(M|x) and p(M) follow empirical distributions according to the existing input and output dataset  $\mathcal{D}$ . Then, we establish a lower bound for I(x; M) to convert it to the MI between x and the expert representation e = E(x):

$$I(x; M) = \mathbb{E}_{x,\mathcal{M}} \left[ \log \frac{p(x \mid M)}{p(x)} \right]$$
  
=  $\mathbb{E}_{x,\mathcal{M}} \left[ \log \int_{e} \frac{p(x \mid e)p(e \mid M)}{p(x)} de \right]$   
=  $\mathbb{E}_{x,\mathcal{M}} \left[ \log \mathbb{E}_{e} \frac{p(x \mid e)}{p(x)} \right]$   
=  $\mathbb{E}_{x,\mathcal{M}} \left[ \log \mathbb{E}_{e} \frac{p(e \mid x)}{p(e)} \right],$  (5)

where  $p(e \mid x)$  can be approximated by the expert network E(x). Since  $\log(\cdot)$  is a convex function, Jensen's inequality yields the theoretical lower bound of I(x; M):

$$I(x; M) \ge \mathbb{E}_{x, e, \mathcal{M}} \left[ \log \frac{p(e \mid x)}{p(e)} \right].$$
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In the top-k routing, the input token x and the expert representation e form samples (x, e), which can be categorized into two different datasets:  $(x, e^+) \sim \mathcal{D}_{top-k}$ , samples from the activated experts; and  $(x, e^-) \sim \mathcal{D}_{\neg top-k}$ , samples from the inactivated experts. For clarity, we denote  $M^+$  as the activated task experts and  $M^-$  as the inactivated. Then, we define the MI gap for top-k routing as:

**Definition 1** *MI* Gap for activated experts and inactivated tas experts in top-k routing is defined by:

$$\Delta I = I_{top-k}(x, M^+) - I_{\neg top-k}(x, M^-), \quad (7)$$

where  $I_{top-k}$  is the MI between input token x and activated experts  $M^+$ , and  $I_{\neg top-k}$  is the MI between input token x and inactivated experts  $M^-$ .

The MI terms  $I_{\text{top-k}}$  and  $I_{\neg \text{top-k}}$  can be converted into a similar form as Eq. 5. To maximize the MI gap  $\Delta I$ , it is necessary to maximize the MI between x and the activated task experts  $M^+$  while minimizing the MI between x and  $M^-$ . When the experts exhibit high specialization, each expert only yields high mutual information for specific token subsets. Concurrently, when knowledge redundancy among the experts is minimized, the mutual information between tokens and inactivated experts approaches zero.

#### 4.3 Contrastive Representation for MI Gap

To estimate the MI gap, Eq. 6 provides a lower bound for the MI between input token x and task experts M. In practice, p(e|x)/p(e) cannot be

calculated directly, thus we use two score functions  $h_1(\cdot)$  and  $h_2(\cdot)$  to measure the information 292 density ratio, which preserves the MI between xand e for the activated and inactivated experts, respectively. Let  $h_1(x, e^+) \propto p(e^+|x)/p(e^+)$  and  $h_2(x,e^-) \propto p(e^-|x)/p(e^-)$ . Then, we adopt contrastive learning to estimate the MI gap.

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Instead of estimating  $I_{top-k}$  and  $I_{\neg top-k}$  separately, we simplify the learning process by establishing a single contrastive objective to estimate  $\Delta I$ . Specifically, we define the samples  $(x, e^+)$  from the activated experts in  $\mathcal{D}_{top-k}$  as positive samples. And the negative samples are sampled from the inactivated experts in  $\mathcal{D}_{\neg top-k}$ . The loss function of contrastive learning can be formulated as:

$$\mathcal{L}_{\text{NCE}} = -\mathbb{E}_{p(x,e^+)}\mathbb{E}_{\mathcal{D}_{\neg \text{top-k}}} \left[\log \frac{h_1(x,e^+)}{h_1(x,e^+) + \sum_{e^- \in \mathcal{D}_{\neg \text{top-k}}} h_2(x,e^-)}\right].$$
(8)

Intuitively, the score function quantifies the exponential correlation between input token x and expert representation e, assigning higher scores to positive samples and lower scores otherwise. The following theorem shows that the proposed contrastive objective can serve as an estimation for the MI gap with sufficient negative samples.

**Theorem 1** (InfoNCE). The MI gap  $\Delta I$ =  $I_{top-k}(x, e^+) - I_{\neg top-k}(x, e^-)$  can be lower bounded 315 by the contrastive objective, as follows: 316

$$\Delta I \ge \log(N) - \mathcal{L}_{\rm NCE},\tag{9}$$

where N is the number of negative samples from the inactivated experts.

 $I_{\text{NCE}} = \log(N) - \mathcal{L}_{\text{NCE}}$  approximates the true MI gap as N increases, which is a tight lower bound. Please refer to Appendix A for full derivations.

To optimize the contrastive objective in Eq. 8,  $h_1(\cdot)$  and  $h_2(\cdot)$  are adopted to estimate the information density. Ideally,  $h_1(\cdot)$  assigns high scores only to positive samples  $(x, e^+)$ , and  $h_2(\cdot)$  assigns low scores only to negative samples  $(x, e^{-})$ . Coincidentally,  $(x, e^{-}) \sim \mathcal{D}_{\neg top-k}$  can serve as negative samples for the scoring function  $h_1(\cdot)$ , while  $(x, e^+) \sim \mathcal{D}_{\text{top-k}}$  functions as positive samples for  $h_2(\cdot)$ , establishing a synergistic relationship between them. Thus, we integrate  $h_1(\cdot)$  and  $h_2(\cdot)$ into a single function  $h(\cdot)$ , which assigns high scores to  $(x, e^+)$  and low scores to  $(x, e^-)$ . Then, we can simplify Eq. 8 into a new version:

$$\hat{\mathcal{L}}_{\text{NCE}} = -\mathbb{E}_{p(x,e^+)} \mathbb{E}_{\mathcal{D}_{\neg \text{top-k}}} \left[ \log \frac{h(x,e^+)}{h(x,e^+) + \sum_{e^- \in \mathcal{D}_{\neg \text{top-k}}} h(x,e^-)} \right].$$
(10)

 $(x, e_{top-k})$  and  $(x, e_{\neg top-k})$  form a bidirectional sample pair, with each entity acting as both a positive and negative reference to its counterpart. For implementation, we choose the exponential similarity function:

$$h(x,e) = \exp(E^+(x) \cdot e)/\tau, \qquad (11)$$

which is commonly used to measure the similarity between two representations. Here,  $\tau$  is a temperature hyperparameter.

In optimization, the score function assigns high scores to the representations of activated experts and low scores to inactivated experts. The derived InfoNCE loss in Eq. 10 can be generalized as a common contrastive loss: for each query  $q_i = E_i^+(x)$ , its positive keys  $k^+$  are obtained from the representations of other activated experts in  $k^+ \sim \mathcal{D}_{top-k}, \ k^+ \neq q_i$ , while negative keys  $k^$ are sampled from  $k^- \sim \mathcal{D}_{\neg top-k}$ . The contrastive loss can be written as:

$$\mathcal{L}_{con} = \sum_{i=1}^{k} -\log\left(\frac{\exp(q_i \cdot k_i^+/\tau)}{\exp(q_i \cdot k_i^+/\tau) + \sum_{k_i^-} \exp(q_i \cdot k_i^-/\tau)}\right)$$
(12)

where k denotes the number of activated experts.

#### **Training Approach** 4.4

In standard supervised fine-tuning, the primary objective is to minimize the cross-entropy loss  $\mathcal{L}_{CE}$ between predicted tokens and target tokens.

As a core component in MoE, the top-k router directly determines which experts are activated during inference. Based on our analysis and derivations in Sections 4.2 and 4.3, we incorporate the contrastive loss as an auxiliary optimization objective, with the complete workflow illustrated in Fig. 2. The contrastive loss effectively enhances the distinctiveness of experts, thereby promoting specialization and reducing redundancy among the experts. By incorporating the contrastive loss in Eq. 12, the total loss is computed as:

$$\mathcal{L}_{\text{total}} = \mathcal{L}_{CE} + \lambda \cdot \mathcal{L}_{\text{con}}, \qquad (13) \qquad 373$$

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| Method            | Params | ST/MT | ARC-e                       | ARC-c                      | BoolQ                      | OBQA                       | PIQA                       | Avg.  |
|-------------------|--------|-------|-----------------------------|----------------------------|----------------------------|----------------------------|----------------------------|---|
| LoRA              | 2.9%   | ST    | 73.8                        | 50.9                       | 62.2                       | 80.4                       | 82.1                       | 69.9  |
| LOKA              | 2.9%   | MT    | 61.3 (-12.5)                | 55.7 ( <mark>+4.8</mark> ) | 66.7 ( <del>+4</del> .5 )  | 71.6 ( <mark>-8.8</mark> ) | 72.4 ( <mark>-9.7</mark> ) | 65.5 ( <mark>-4.4</mark> )  |
| DoRA              | 2.9%   | ST    | 76.5                        | 59.8                       | 71.7                       | 80.6                       | 82.7                       | 74.3  |
| DOKA              | 2.9%   | MT    | 64.5 (-12)                  | 54.1 ( <mark>-5.7</mark> ) | 65.4 ( <mark>-6.3</mark> ) | 75.8 ( <mark>-4.8</mark> ) | 71.9 ( <b>-10.8</b> )      | $\begin{array}{c} 69.9 \\ 69.9 \\ 65.5 (-4.4) \\ 74.3 \\ 74.3 \\ 66.3 (-8) \\ 74.6 \\ 74.6 \\ 74.6 \\ 75.4 \\ 75.4 \\ 75.4 \\ 75.4 \\ 75.4 \\ 74.4 \\ 74.4 \\ 74.9$ |
| MOELoRA           | 1.0%   | ST    | 76.8                        | 60.2                       | 72.0                       | 81.1                       | 82.7                       | 74.6  |
| MOELOKA           | 1.0%   | MT    | 76.1 ( <mark>-0.7</mark> )  | 59.3 ( <mark>-0.9</mark> ) | 71.5 ( <mark>+0.1</mark> ) | 80.7 ( <mark>-0.4</mark> ) | 82.1 ( <mark>-0.3</mark> ) | 73.9 ( <mark>-0.5</mark> )  |
| MiLoRA            | 0.93%  | ST    | 77.8                        | 61.2                       | 72.8                       | 81.7                       | 83.3                       | 75.4  |
| MILOKA            | 0.95%  | MT    | 77.4 ( <mark>-0.4</mark> )  | 61.5 ( <mark>+0.3</mark> ) | 72.3 ( <mark>-0.3</mark> ) | 81.3 ( <mark>-0.4</mark> ) | 83.5 ( <mark>+0.3</mark> ) | $\begin{array}{c} 69.9 \\ \hline 69.9 \\ \hline 74.3 \\ \hline 74.3 \\ \hline 74.3 \\ \hline 74.6 \\ \hline 75.4 \\ \hline 75.4 \\ \hline 75.4 \\ \hline 75.4 \\ \hline 75.2 \\ \hline 75.4 \\ \hline 74.4 \\ \hline 5 \\ \hline 75.3 \\ (+0.9) \\ \hline 74.9 \\ \hline 9 \\ 9 \\ \hline 75.4 \\ (+0.5) \\ \hline 74.9 \\ \hline \end{array}$   |
| MixLoRA           | 2.9%   | ST    | 78.4                        | 56.1                       | 72.7                       | 81.6                       | 83.2                       | 74.4  |
| MIXLOKA           | 2.9%   | MT    | 76.6 ( <b>-1.8</b> )        | 64.2 ( <mark>+8.1</mark> ) | 71.2 ( -1.5 )              | 81.6 ( <mark>-0.0</mark> ) | 82.7 ( <mark>-0.5</mark> ) | 75.3 ( <mark>+0.9</mark> )  |
| OMoE-LoRA         | 0.73%  | ST    | 79.3                        | 56.6                       | 73.5                       | 80.6                       | 84.5                       | 74.9  |
| OWICE-LOKA        | 0.75%  | MT    | 79.8 ( <mark>+0.5</mark> )  | 66.8 (+10.2)               | 72.4 ( -1.1 )              | 76.8 ( <mark>-3.8</mark> ) | 81.6 ( <mark>-2.9</mark> ) | 75.4 ( <mark>+0.5</mark> )  |
|                   | 1.45%  | ST    | 80.3                        | 57.3                       | 72.9                       | 80.4                       | 83.6                       | 74.9  |
| CoMoE-LoRA (ours) | 1.43%  | MT    | 79.6 ( - <mark>0.7</mark> ) | 66.5 ( <mark>+9.2</mark> ) | 71.8 ( -1.1 )              | 81.2 ( +0.8 )              | 81.8 ( <b>-1.8</b> )       | 76.2 (+1.3)   |

Table 1: Overall comparison of different PEFT methods for multi-task learning. The backbone model is LLaMA-2 7B. ST refers to the single-task settings, while MT refers to the multi-task settings. Reported results are accuracy scores, with differences between MT and ST indicated in red for decreases and in blue for increases.

| Method     | Params | ARC-e | ARC-c | BoolQ | OBQA | PIQA | SIQA | HellaS | WinoG |
|------------|--------|-------|-------|-------|------|------|------|--------|-------|
| LoRA       | 2.9%   | 73.8  | 50.9  | 62.2  | 80.4 | 82.1 | 69.9 | 88.4   | 66.8  |
| DoRA       | 2.9%   | 76.5  | 59.8  | 71.7  | 80.6 | 82.7 | 74.1 | 89.6   | 67.3  |
| MixLoRA    | 2.9%   | 78.4  | 56.1  | 72.7  | 81.6 | 83.2 | 78.0 | 92.8   | 76.8  |
| CoMoE-LoRA | 1.45%  | 80.3  | 57.3  | 72.9  | 80.4 | 83.6 | 79.2 | 93.2   | 77.3  |
| CoMoE-DoRA | 1.45%  | 80.2  | 57.0  | 73.3  | 81.2 | 83.8 | 79.1 | 92.8   | 77.3  |

Table 2: Overall comparison of different PEFT methods for single-task learning, using base models with different numbers of parameters. Bold indicates the best results.

where  $\lambda$  is a hyperparameter to scale the auxiliary loss. Our method requires no pretraining and can be seamlessly integrated into existing MoE architectures. To summarize, the complete algorithm pseudocode is provided in Appendix B.

### **5** Experiments

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In this section, we conduct extensive experiments coupled with ablation and visualization experiments to evaluate the effectiveness of CoMoE, accompanied by concise analyses.

# 5.1 Experimental Settings

**Datasets and Benchmarks.** We conduct experiments on a collection of tasks: (a) Diverse commonsense reasoning datasets: ARC-e and ARC-c (Clark et al., 2018), OpenBookQA (OBQA) (Mihaylov et al., 2018), PIQA (Bisk et al., 2020), SocialIQA (SIQA) (Sap et al., 2019), and BoolQ (Clark et al., 2019). (b) A science completion task: Hellaswag (Zellers et al., 2019). (c) A fill-in-the-blank task: Winogrande (Sakaguchi et al., 2021).

We utilize the PEFT framework provided by (Hu et al., 2023; Li et al., 2024) for training on these datasets. We choose LLaMA-2 7B and Gemma 2B as our backbone models. The detailed statistics and

evaluation metrics can be found in Appendix C.

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Baselines. In this study, we compare our method 399 with several popular and well-established base-400 lines to assess its performance. For multi-task 401 settings, we evaluate CoMoE against LoRA, its 402 variants, and MoE-based methods, including: (1) 403 LoRA (Hu et al., 2021); (2) DoRA (Liu et al., 404 2024), which decomposes LoRA weights into 405 magnitude and direction; (3) MoELoRA (Liu 406 et al., 2023), which decomposes a LoRA module 407 into a mixture of experts; (4) MiLoRA (Zhang 408 et al., 2024), which treats each LoRA mod-409 ule as an expert and employs a routing mecha-410 nism; (5) MixLoRA (Li et al., 2024), a resource-411 efficient sparse MoE model based on LoRA; (6) 412 **OMoE** (Feng et al., 2025), which applies hard 413 constraints to promote diversity. For single-task 414 settings, we compare our approach with other 415 PEFT baselines, including: AdaLoRA (Zhang 416 et al., 2023a); Parallel-Adapter (He et al., 2021); 417 Learned-Adapter (Zhang et al., 2023b); P-tuning 418 v2 (Liu et al., 2021); IAPT (Zhu et al., 2024); Bit-419 **Fit** (Zaken et al., 2021); (**IA**)<sup>3</sup> (Liu et al., 2022); 420 SSP (Hu et al., 2022). Most of the results are di-421 rectly extracted from (Zhang et al., 2024), with a 422 few baselines reproduced by running the provided 423 424 source code. In single-task settings, we compare
425 CoMoE with LoRA, DoRA, and MixLoRA as rep426 resentative baselines, while comparisons with other
427 methods are presented in Appendix E.

Implementation Details. To evaluate the effec-428 tiveness of CoMoE, we apply it on the basis of 429 LoRA and DoRA, respectively, and label them as 430 CoMoE-LoRA and CoMoE-DoRA in the experi-431 ments. Unless otherwise specified, CoMoE is con-432 figured with r = 16, incorporating 4 experts and a 433 top-2 router, applied to the q, k, v, and o parameters 434 in the attention layers. For all settings, we adopt su-435 pervised fine-tuning only. Due to space limitations, 436 the detailed experimental settings for baselines and 437 hyperparameters are provided in Appendix D. 438

## 5.2 Main Results

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Multi-task Setup. Table 1 summarizes the multitask performance of CoMoE and baselines on LLaMA-2 7B. The results verify that both LoRA and DoRA, due to their lack of MoE structures, struggle to handle heterogeneous datasets, observing a significant drop in multi-task settings (7%  $\sim 12\%$  degradation). MoE-based PEFT methods (MoELoRA, MiLoRA, MixLoRA, and OMoE) mitigate the performance degradation in multi-task settings but fail to leverage the modularity and specialization in MoE, leaving potential performance gains unexploited. In contrast, CoMoE introduces contrastive learning to promote the modularization and specialization of experts, enabling efficient utilization of the MoE's capacity. Thus, CoMoE not only improves parameter efficiency (reduces the number of experts) but also achieves an average accuracy gain of +1.3.

Single-task Setup. In this setup, we compare the 458 performance of CoMoE and baselines in single-459 task settings. The experimental results are shown 460 in Table 2. Comparisons with other baselines are 461 provided in Appendix E. CoMoE demonstrates su-462 perior parameter efficiency while maintaining com-463 parable performance, with a reduction of approx-464 imately 50% in tunable parameters. Remarkably, 465 the diversity among experts even yields accuracy 466 improvements on a subset of datasets (e.g., ARC-e, 467 BoolQ, and SIQA). 468

#### 5.3 Ablation Studies and Further Analysis

**Effects of the Hyperparameter**  $\lambda$ . We further evaluate  $\lambda \in \{0.0, 0.001, 0.01, 0.1, 1.0\}$  on the BoolQ and the multi-task settings (ARC-c, ARCe, BoolQ, and OBQA). Experimental results in



Figure 3: Performances under different coefficients  $\lambda$ . (a) In single-task settings. (b) In multi-task settings.

| Method             | ARC-e | ARC-c | BoolQ | OBQA | Avg. |
|--------------------|-------|-------|-------|------|------|
| $CoMoE- \triangle$ | 80.5  | 67.0  | 72.4  | 78.4 | 74.6 |
| CoMoE-∇            | 79.7  | 65.1  | 72.3  | 76.8 | 73.5 |
| CoMoE-0            | 77.9  | 65.3  | 72.1  | 77.6 | 73.2 |
| CoMoE-🖂            | 77.7  | 66.6  | 72.4  | 80.0 | 74.2 |

Table 3: Performance comparison of different CoMoE variants on four datasets.

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Fig. 3(a) and (b) demonstrate that  $\lambda = 1e-2$  yields optimal performance in both single-task and multitask settings. In single-task configurations, model performance shows gradual improvement as the value increases from 0, 0.001 to 0.01, suggesting that even individual tasks can benefit from diversity. However, significant performance degradation occurs at higher values (0.1 and 1.0), indicating that excessive diversity impedes effective dataset adaptation. This phenomenon is more pronounced in multi-task settings, where the model shows amplified gains from diversity.

Effects of the Number of Experts n. The results are provided in Appendix F. We can see that Co-MoE benefits from more experts.

Ablation on Different Backbones. We conduct multi-task experiments on Gemma 2B, with detailed results provided in Appendix G.

Model Efficiency. Please refer to Appendix H.

**Layer-wise Diversity Analysis.** Having established the benefit of expert diversity in multi-task settings, we naturally ask: Which layers in LLMs benefit most from diverse experts? Using LLaMA-2 7B as a case, we simplify the large language model into three levels: low (from layer 1 to 10), medium (from layer 11 to 20), and high (from layer 21 to 32), and inject CoMoE into them. Specifically, four types of layer-wise diversity configurations are explored: (1) **CoMoE-** $\triangle$ , applying CoMoE in low layers; (2) **CoMoE-** $\Diamond$ , applying Co-MoE in high layers; (3) **CoMoE-** $\Diamond$ , applying Co-



Figure 4: Comparison of the workloads of experts before and after contrastive loss incorporation in a multi-task setting. (a) Without contrastive loss. (b) With contrastive loss.



(a) w/o contrastive loss (b) w/ contrastive loss

Figure 5: Comparison of expert representations in obqa before and after contrastive loss incorporation in a multitask setting. (a) Without contrastive loss. (b) With contrastive loss.

MoE in medium layers; (4) CoMoE-⋈, applying
CoMoE in low and high layers. Our experiments
in Table 3 reveal that CoMoE-△ and CoMoE⋈ achieve superior performance, outperforming
CoMoE-⊽ and CoMoE-◊ by 0.7~1.4 on average
accuracy across datasets. This performance gap
stems from the placement of CoMoE in lower transformer layers, which is critical for establishing diversity early in the processing hierarchy.

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Analysis of Workload Balance. The primary dis-514 tinction between CoMoE and vanilla MoE vari-515 ants lies in the contrastive learning objective that 516 promotes specialization and modularity among ex-517 perts. To further elucidate the effectiveness of Co-518 MoE, we conducted an in-depth analysis of ex-519 pert activation in MoE under a multi-task setting. 520 Fig. 4 presents a comparative visualization of expert workload distributions before and after intro-522 ducing the contrastive loss. Without contrastive 523 loss, all tasks predominantly concentrated on ex-524 pert 1 and 2, indicating insufficient differentiation 525 and an imbalanced workload. After introducing

contrastive loss, distinct tasks exhibited marked differences in expert selection. For ARC-c, expert 1 and 3 showed significantly increased activation frequency. For BoolQ, expert 1 and 4 formed a stable collaborative relationship. Notably, our method did not incorporate any routing balance loss, yet the collaboration among experts emerged naturally. 527

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**Visualization of Expert Representations.** To demonstrate the impact of contrastive loss on expert diversity, we conduct qualitative analysis by visualizing expert representations before and after its incorporation, which is illustrated in Fig. 5. In multi-task settings, we choose the OBQA dataset for example and the visualizations of other datasets are provided in Appendix I. The results demonstrate that the absence of contrastive loss leads to substantial redundancy among experts, compromising their discriminability. In contrast, the introduction of contrastive loss fosters divergent experts, culminating in specialization and modularity.

# 6 Conclusion

In this paper, we focus on the problem of redundant knowledge learning in MoE, which leads to the underutilization of its capacity. To address this issue, we propose Contrastive Representation for MoE (CoMoE), a novel MoE variant that promotes modularization and specialization. Specifically, we define a mutual information (MI) gap between activated and inactivated experts and approximate it through a contrastive objective. This objective effectively captures the MI gap and is incorporated into supervised fine-tuning as an auxiliary optimization term. Experiments on various tasks demonstrate that CoMoE outperforms the baselines in multi-task settings and enhances expert modularity.

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# Limitations

We show that our proposed method can significantly improve the specialization of experts and the performance of MoE in multi-task settings. However, there are several limitations to acknowledge: (a) The computational cost of CoMoE. CoMoE leverages inactivated experts as negative samples, and its computational cost is proportional to O(N). However, it substantially improves expert specialization and modularization, achieving remarkable performance with a limited number of experts; (b) Other evaluation benchmarks were not considered. Nevertheless, CoMoE is simple and can be easily integrated with different backbone models and various downstream tasks.

# **Ethics Statement**

This paper proposes a novel method to enhance parameter-efficient fine-tuning based on the Mixture-of-Experts architecture, which simultaneously improves expert modularization and specialization while boosting performance on heterogeneous and complex datasets. The experiments employ widely adopted benchmark datasets in the research community that, to our knowledge, involve no privacy concerns or ethical controversies. The experiments are conducted on the opensource LLaMA-2 series of large language models. It should be emphasized that this work represents fundamental research focused exclusively on advancing MoE-based fine-tuning methods for LLMs, rather than developing applications.

# References

- Yonatan Bisk, Rowan Zellers, Jianfeng Gao, Yejin Choi, et al. 2020. Piqa: Reasoning about physical commonsense in natural language. In *Proceedings of the AAAI conference on artificial intelligence*, volume 34, pages 7432–7439.
- Christopher Clark, Kenton Lee, Ming-Wei Chang, Tom Kwiatkowski, Michael Collins, and Kristina Toutanova. 2019. Boolq: Exploring the surprising difficulty of natural yes/no questions. *arXiv preprint arXiv:1905.10044*.
- Peter Clark, Isaac Cowhey, Oren Etzioni, Tushar Khot, Ashish Sabharwal, Carissa Schoenick, and Oyvind Tafjord. 2018. Think you have solved question answering? try arc, the ai2 reasoning challenge. *arXiv preprint arXiv:1803.05457*.
  - Ganqu Cui, Lifan Yuan, Ning Ding, Guanming Yao, Wei Zhu, Yuan Ni, Guotong Xie, Zhiyuan Liu, and

Maosong Sun. 2023. Ultrafeedback: Boosting language models with high-quality feedback.

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- Shihan Dou, Enyu Zhou, Yan Liu, Songyang Gao, Jun Zhao, Wei Shen, Yuhao Zhou, Zhiheng Xi, Xiao Wang, Xiaoran Fan, et al. 2023. Loramoe: Alleviate world knowledge forgetting in large language models via moe-style plugin. *arXiv preprint arXiv:2312.09979*.
- Jinyuan Feng, Zhiqiang Pu, Tianyi Hu, Dongmin Li, Xiaolin Ai, and Huimu Wang. 2025. Omoe: Diversifying mixture of low-rank adaptation by orthogonal finetuning. *arXiv preprint arXiv:2501.10062*.
- Junxian He, Chunting Zhou, Xuezhe Ma, Taylor Berg-Kirkpatrick, and Graham Neubig. 2021. Towards a unified view of parameter-efficient transfer learning. *arXiv preprint arXiv:2110.04366*.
- Edward J Hu, Yelong Shen, Phillip Wallis, Zeyuan Allen-Zhu, Yuanzhi Li, Shean Wang, Lu Wang, and Weizhu Chen. 2021. Lora: Low-rank adaptation of large language models. *arXiv preprint arXiv:2106.09685*.
- Shengding Hu, Zhen Zhang, Ning Ding, Yadao Wang, Yasheng Wang, Zhiyuan Liu, and Maosong Sun. 2022. Sparse structure search for parameter-efficient tuning. *arXiv preprint arXiv:2206.07382*.
- Zhiqiang Hu, Lei Wang, Yihuai Lan, Wanyu Xu, Ee-Peng Lim, Lidong Bing, Xing Xu, Soujanya Poria, and Roy Lee. 2023. Llm-adapters: An adapter family for parameter-efficient fine-tuning of large language models. In *Proceedings of the 2023 Conference on Empirical Methods in Natural Language Processing*, pages 5254–5276.
- Yuzhen Huang, Yuzhuo Bai, Zhihao Zhu, Junlei Zhang, Jinghan Zhang, Tangjun Su, Junteng Liu, Chuancheng Lv, Yikai Zhang, Yao Fu, et al. 2024. C-eval: A multi-level multi-discipline chinese evaluation suite for foundation models. *Advances in Neural Information Processing Systems*, 36.
- Robert A Jacobs, Michael I Jordan, Steven J Nowlan, and Geoffrey E Hinton. 1991. Adaptive mixtures of local experts. *Neural computation*, 3(1):79–87.
- Siming Lan, Rui Zhang, Qi Yi, Jiaming Guo, Shaohui Peng, Yunkai Gao, Fan Wu, Ruizhi Chen, Zidong Du, Xing Hu, et al. 2024. Contrastive modules with temporal attention for multi-task reinforcement learning. *Advances in Neural Information Processing Systems*, 36.
- Dengchun Li, Yingzi Ma, Naizheng Wang, Zhiyuan Cheng, Lei Duan, Jie Zuo, Cal Yang, and Mingjie Tang. 2024. Mixlora: Enhancing large language models fine-tuning with lora based mixture of experts. *arXiv preprint arXiv:2404.15159*.
- Xiang Lisa Li and Percy Liang. 2021. Prefix-tuning: Optimizing continuous prompts for generation. *arXiv preprint arXiv:2101.00190*.

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Haokun Liu, Derek Tam, Mohammed Muqeeth, Jay Mohta, Tenghao Huang, Mohit Bansal, and Colin A Raffel. 2022. Few-shot parameter-efficient fine-tuning is better and cheaper than in-context learning. Advances in Neural Information Processing Systems, 35:1950–1965.

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- Qidong Liu, Xian Wu, Xiangyu Zhao, Yuanshao Zhu, Derong Xu, Feng Tian, and Yefeng Zheng. 2023. Moelora: An moe-based parameter efficient finetuning method for multi-task medical applications. *arXiv preprint arXiv:2310.18339*.
- Shih-Yang Liu, Chien-Yi Wang, Hongxu Yin, Pavlo Molchanov, Yu-Chiang Frank Wang, Kwang-Ting Cheng, and Min-Hung Chen. 2024. Dora: Weightdecomposed low-rank adaptation. *arXiv preprint arXiv:2402.09353*.
  - Xiao Liu, Kaixuan Ji, Yicheng Fu, Weng Lam Tam, Zhengxiao Du, Zhilin Yang, and Jie Tang. 2021. Ptuning v2: Prompt tuning can be comparable to finetuning universally across scales and tasks. *arXiv preprint arXiv:2110.07602*.
- Tongxu Luo, Jiahe Lei, Fangyu Lei, Weihao Liu, Shizhu He, Jun Zhao, and Kang Liu. 2024. Moelora: Contrastive learning guided mixture of experts on parameter-efficient fine-tuning for large language models. *arXiv preprint arXiv:2402.12851*.
- Todor Mihaylov, Peter Clark, Tushar Khot, and Ashish Sabharwal. 2018. Can a suit of armor conduct electricity? a new dataset for open book question answering. *arXiv preprint arXiv:1809.02789*.
- Aaron van den Oord, Yazhe Li, and Oriol Vinyals. 2018. Representation learning with contrastive predictive coding. *arXiv preprint arXiv:1807.03748*.
- Chen Qian, Zihao Xie, Yifei Wang, Wei Liu, Yufan Dang, Zhuoyun Du, Weize Chen, Cheng Yang, Zhiyuan Liu, and Maosong Sun. 2024. Scaling large-language-model-based multi-agent collaboration. *arXiv preprint arXiv:2406.07155*.
- Adithya Renduchintala, Tugrul Konuk, and Oleksii Kuchaiev. 2023. Tied-lora: Enhancing parameter efficiency of lora with weight tying. *arXiv preprint arXiv:2311.09578*.
- Keisuke Sakaguchi, Ronan Le Bras, Chandra Bhagavatula, and Yejin Choi. 2021. Winogrande: An adversarial winograd schema challenge at scale. *Communications of the ACM*, 64(9):99–106.
- Maarten Sap, Hannah Rashkin, Derek Chen, Ronan LeBras, and Yejin Choi. 2019. Socialiqa: Commonsense reasoning about social interactions. *arXiv preprint arXiv:1904.09728*.
- Noam Shazeer, Azalia Mirhoseini, Krzysztof Maziarz, Andy Davis, Quoc Le, Geoffrey Hinton, and Jeff Dean. 2017. Outrageously large neural networks: The sparsely-gated mixture-of-experts layer. arXiv preprint arXiv:1701.06538.

- Chufan Shi, Cheng Yang, Xinyu Zhu, Jiahao Wang, Taiqiang Wu, Siheng Li, Deng Cai, Yujiu Yang, and Yu Meng. 2024. Unchosen experts can contribute too: Unleashing moe models' power by self-contrast. *arXiv preprint arXiv:2405.14507*.
- Chunlin Tian, Zhan Shi, Zhijiang Guo, Li Li, and Chengzhong Xu. 2024. Hydralora: An asymmetric lora architecture for efficient fine-tuning. *arXiv preprint arXiv:2404.19245*.
- Pengfei Wang, Huanran Zheng, Silong Dai, Wenjing Yue, Wei Zhu, and Xiaoling Wang. 2024. Ts-tcd: Triplet-level cross-modal distillation for time-series forecasting using large language models. *arXiv preprint arXiv:2409.14978*.
- Xiaoyu Wen, Chenjia Bai, Kang Xu, Xudong Yu, Yang Zhang, Xuelong Li, and Zhen Wang. 2024. Contrastive representation for data filtering in crossdomain offline reinforcement learning. *arXiv preprint arXiv:2405.06192.*
- Shu Yang, Muhammad Asif Ali, Cheng-Long Wang, Lijie Hu, and Di Wang. 2024. Moral: Moe augmented lora for llms' lifelong learning. *arXiv preprint arXiv:2402.11260.*
- Elad Ben Zaken, Shauli Ravfogel, and Yoav Goldberg. 2021. Bitfit: Simple parameter-efficient fine-tuning for transformer-based masked languagemodels. *arXiv preprint arXiv:2106.10199*.
- Rowan Zellers, Ari Holtzman, Yonatan Bisk, Ali Farhadi, and Yejin Choi. 2019. Hellaswag: Can a machine really finish your sentence? *arXiv preprint arXiv:1905.07830*.
- Jingfan Zhang, Yi Zhao, Dan Chen, Xing Tian, Huanran Zheng, and Wei Zhu. 2024. Milora: Efficient mixture of low-rank adaptation for large language models fine-tuning. In *Findings of the Association for Computational Linguistics: EMNLP 2024*, pages 17071–17084.
- Qingru Zhang, Minshuo Chen, Alexander Bukharin, Nikos Karampatziakis, Pengcheng He, Yu Cheng, Weizhu Chen, and Tuo Zhao. 2023a. Adalora: Adaptive budget allocation for parameter-efficient finetuning. *arXiv preprint arXiv:2303.10512*.
- Yuming Zhang, Peng Wang, Ming Tan, and Wei Zhu. 2023b. Learned adapters are better than manually designed adapters. In *Findings of the Association for Computational Linguistics: ACL 2023*, pages 7420– 7437.
- Zhen Zhang, Wei Zhu, Jinfan Zhang, Peng Wang, Rize Jin, and Tae-Sun Chung. 2022. Pcee-bert: Accelerating bert inference via patient and confident early exiting. In *Findings of the Association for Computational Linguistics: NAACL 2022*, pages 327–338.
- Wei Zhu, Aaron Xuxiang Tian, Congrui Yin, Yuan Ni, Xiaoling Wang, and Guotong Xie. 2024. Iapt: Instruction-aware prompt tuning for large language models. *arXiv preprint arXiv:2405.18203*.

# **A** Theoretical Proof

**Theorem 2** (InfoNCE). The MI gap  $\Delta I = I_{top-k}(x, e^+) - I_{\neg top-k}(x, e^-)$  can be lower bounded by the contrastive objective, as

$$\Delta I \ge \log(N) - \mathcal{L}_{\text{NCE}},\tag{14}$$

where N is the number of negative samples from the inactivated expert dataset.

*Proof.* As illustrated in Eq. 8, we utilize  $h_1(x, e^+) \propto p(e^+|x)/p(e^+)$  and  $h_2(x, e^-) \propto p(e^-|x)/p(e^-)$  to approximate the information density ratio, which preserves the MI between x and M. Based on the standard derivations presented in InfoNCE (Oord et al., 2018) and (Wen et al., 2024), the contrastive objective can be rewritten as:

$$\mathcal{L}_{\text{NCE}} = -\mathbb{E}_{p(x,e^+)} \mathbb{E}_{\mathcal{D}_{\neg \text{top-k}}} log \left[ \frac{p(e^+|x)/p(e^+)}{p(e^+|x)/p(e^+) + \sum_{e^- \in \mathcal{D}_{\neg \text{top-k}}} p(e^-|x)/p(e^-)} \right]$$

$$= \mathbb{E}_{p(x,e^+)} \mathbb{E}_{\mathcal{D}_{\neg \text{top-k}}} log \left[ 1 + \frac{p(e^+)}{p(e^+|x)} \sum_{e^- \in \mathcal{D}_{\neg \text{top-k}}} \frac{p(e^-|x)}{p(e^-)} \right]$$

$$= \mathbb{E}_{p(x,e^+)} log \left[ N \frac{p(e^+)}{p(e^+|x)} (\frac{1}{N}) \sum_{e^- \in \mathcal{D}_{\neg \text{top-k}}} \frac{p(e^-|x)}{p(e^-)} \right]$$

$$= \mathbb{E}_{p(x,e^+)} log \left[ N \frac{p(e^+)}{p(e^+|x)} (\frac{1}{N}) \sum_{e^- \in \mathcal{D}_{\neg \text{top-k}}} \frac{p(e^-|x)}{p(e^-)} \right]$$

$$= \mathbb{E}_{p(x,e^+)} log \left[ (\frac{1}{N}) \sum_{e^- \in \mathcal{D}_{\neg \text{top-k}}} N \frac{p(e^+|x)}{p(e^+|x)} \frac{p(e^-|x)}{p(e^-)} \right]$$

$$(15)$$

We derive Eq. 15 using Jensen's inequality, noting that log is a concave function.

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$$\mathcal{L}_{\text{NCE}} \geq \mathbb{E}_{p(x,e^{+})} \left[ \left(\frac{1}{N}\right) \sum_{e^{-} \in \mathcal{D}_{\neg \text{top-k}}} \log \left[ N \frac{p(e^{+})}{p(e^{+}|x)} \frac{p(e^{-}|x)}{p(e^{-})} \right] \right]$$

$$= \mathbb{E}_{p(x,e^{+})} \left[ \left(\frac{1}{N}\right) \sum_{e^{-} \in \mathcal{D}_{\neg \text{top-k}}} \left[ \log N + \log \frac{p(e^{+})}{p(e^{+}|x)} + \log \frac{p(e^{-}|x)}{p(e^{-})} \right] \right]$$

$$\approx \mathbb{E}_{p(x,e^{+})} \left[ \log N + \log \frac{p(e^{+})}{p(e^{+}|x)} + \mathbb{E}_{e^{-} \in \mathcal{D}_{\neg \text{top-k}}} \log \frac{p(e^{-}|x)}{p(e^{-})} \right]$$

$$= \log N - I_{\text{top-k}} + I_{\neg \text{top-k}}$$

$$= lon N - \Delta I$$

$$(16)$$

Thus, we prove the aforementioned theorem:

$$\Delta I \ge \log(N) - \mathcal{L}_{\text{NCE}}.$$
(17)

## **B** Optimization Algorithm

778To enhance specialization and modularization779among experts, we devise Contrastive Representa-780tion for MoE, outlined in Algorithm 1. For each781sample, one expert is randomly selected from its782top-k expert indices T as the anchor. The remain-

ing top-k experts act as positives, while all other inactivated experts form negatives. The procedure is:

1. Expert representation. Obtain the individual expert outputs  $\{E_j(x)\}_{j=1}^n$ , each with dimensionality  $E_j(x) \in \mathbb{R}^D$ . 788

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Algorithm 1: Contrastive Loss Computation among Experts (single-sample)

**Input:** Top-k expert indices  $T \in \mathbb{N}^k$ Expert representations  $\{E_j(x)\}_{i=1}^n$ , where  $E_j(x) \in \mathbb{R}^D$ Temperature  $\tau$ **Output:** Contrastive loss  $\mathcal{L}_{contrast}$ 1  $r \sim \mathcal{U}\{1,\ldots,k\}$ // Random anchor position 2  $a \leftarrow T[r]$ // Anchor expert index  $\mathbf{3} \ q \leftarrow \text{Normalize}(E_a(x))$ 4  $P \leftarrow \{\text{Normalize}(E_{T[i]}(x)) \mid j \neq r\}$ // Positive set, size k-1s  $N \leftarrow \{ \text{Normalize}(E_j(x)) \mid j \notin T \}$ // Negative set, size n-k6  $s_{\text{pos}} \leftarrow (q \cdot P^{\top})/\tau$  $s_{\text{ros}} \leftarrow (q \cdot N^{\top})/\tau$   $s_{\text{logits}} \leftarrow [s_{\text{pos}}, s_{\text{neg}}]$   $s_{\text{contrast}} = -\log \left(\frac{\sum \exp(s_{\text{pos}})}{\sum \exp(\log i s) + \varepsilon}\right)$ 10 return  $\mathcal{L}_{contrast}$ 

2. Anchor selection. Uniformly sample an index r from  $\{1, \ldots, k\}$ . Define the anchor (query) vector as  $q = \text{Normalize}(E_{T[r]}(x))$ .

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Positive set. Aggregate the remaining (k – 1) expert representations, excluding the one indexed by T[r] from the index set T, into a set P, applying normalization:

$$P = \{ \text{Normalize}(E_{T[j]}(x)) \mid j \neq r \}.$$

4. **Negative set.** Collect and normalize representations from experts not included in the top-*k* indices:

 $N = \{ \text{Normalize}(E_i(x)) \mid j \notin T \}.$ 

5. Similarity computation. Compute cosine similarities between anchor vector q and each representation in P and N, scaled by temperature  $\tau$ , yielding similarity scores  $s_{\text{pos}}$  and  $s_{\text{neg}}$ :

$$s_{\text{pos}} = \frac{q \cdot P^{\top}}{\tau}, \quad s_{\text{neg}} = \frac{q \cdot N^{\top}}{\tau}.$$

6. **InfoNCE loss.** Concatenate the logits and compute the InfoNCE loss as

$$\mathcal{L}_{\text{contrast}} = -\log\left(\frac{\sum \exp(s_{\text{pos}})}{\sum \exp([s_{\text{pos}}, s_{\text{neg}}]) + \varepsilon}\right).$$

where  $\varepsilon$  is a small positive value (e.g.,  $10^{-3}$ ) used to ensure numerical stability, avoiding computational issues caused by the denominator being zero.

# C Datasets

Detailed information about the datasets used in the experiments is presented in Table 4. All datasets are downloaded from HuggingFace. 814

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### **D** Experimental settings

**Computing Infrastructure** We run all our experiments on NVIDIA A6000 (48GB) GPUs, using Python 3.10 and Ubuntu 20.04 on x86-64 CPUs.

**Pretrained Backbones** The main experiments use the most recent open-sourced LLM, LLaMA-2 7B and Gemma 2B, as the pretrained backbone model. When fine-tuning LLaMA-2 7B and Gemma 2B, we consider only the supervised finetuning setting.

Hyperparameters for CoMoE In our experiments, unless otherwise specified, we set the hyperparameters as illustrated in Table 5. In the table, the hyperparameters set by other baseline methods, LoRA, DoRA, MixLoRA, MixDoRA, OMoE-LoRA, are also included. Under this setting, Co-MoE introduces approximately 1.45% tunable parameters to the LLaMA-2 7B backbone.

**Descriptive Statistics about Results** We conduct experiments on all training settings using five different random seeds, and the final results represent the median accuracy within each setting.

# **E** Additional Results on Other Baselines

In the main paper, we compared CoMoE with three widely recognized and well-performing baselines (LoRA, DoRA, and MixLoRA) using the

| Datasets   | #train | #test  | Туре                | Metrics |
|------------|--------|--------|---------------------|---------|
| BoolQ      | 9,427  | 3,270  | Text Classification | acc     |
| OBQA       | 4,957  | 500    | Question Answering  | acc     |
| ARC-e      | 2,251  | 2,376  | Question Answering  | acc     |
| ARC-c      | 1,119  | 1,172  | Question Answering  | acc     |
| PIQA       | 16,100 | 1,840  | Question Answering  | acc     |
| SIQA       | 33,410 | 1,954  | Question Answering  | acc     |
| HellaSwag  | 39,905 | 10,042 | Sentence Completion | acc     |
| WinoGrande | 9,248  | 1,267  | Fill in the Blank   | acc     |

Table 4: The dataset statistics.

| Hyperparameters     | LoRA/DoRA | MixLoRA/MixDoRA   | OMoE-LoRA    | СоМоЕ           |  |  |  |  |
|---------------------|-----------|-------------------|--------------|-----------------|--|--|--|--|
| Cutoff Length       |           | 512               |              |                 |  |  |  |  |
| Learning Rate       |           | 2e-4              |              |                 |  |  |  |  |
| Optimizer           |           | AdamV             | V            |                 |  |  |  |  |
| Batch size          |           | 16                |              |                 |  |  |  |  |
| Accumulation Steps  |           | 8                 |              |                 |  |  |  |  |
| Dropout             |           | 0.05              |              |                 |  |  |  |  |
| Epochs              |           | 2                 |              |                 |  |  |  |  |
| Where               |           | Q, K, V, O, Up, I | Down, Gate   |                 |  |  |  |  |
| LoRA Rank $r$       | 80        | 16                | 16           | 16              |  |  |  |  |
| LoRA Alpha $\alpha$ | 160       | 32                | 32 32        |                 |  |  |  |  |
| Experts             | -         | 8 2               |              | 4               |  |  |  |  |
| Routing strategy    | -         | Top - 2 routing   | Soft routing | Top - 2 routing |  |  |  |  |

Table 5: Hyperparameter configurations of LoRA, DoRA, MixLoRA, MixDoRA, OMoE-LoRA and CoMoE for fine-tuning LLaMA-2 7B on datasets.

LLaMA-2 7B model. In addition to the results shown in Table 2, we provide experimental results involving 11 additional strong baselines on the same LLaMA-2 7B backbone, as detailed in Table 9. The results demonstrate that CoMoE achieves significant improvements in both parameter efficiency and overall performance compared to these baselines.

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# **F** Additional Results on Different Number of Experts *n*

We further compared the experimental results under different numbers of experts. In the multitask setting, using the ARC-c, ARC-e, BoolQ, and OBQA datasets, the results are shown in Table 6. As the number of experts increases from 4 to 8, the model's performance stabilizes and shows modest improvement. While merely increasing the number of experts does not guarantee significant performance enhancement, expanding the expert pool in multi-task settings contributes to improved model stability and may lead to certain performance gains.

# G Additional Results on Different Backbone Models

Our main experiments are conducted on LLaMA-2 7B. To demonstrate the adaptation of our method, we compare CoMoE with MixLoRA on the Gemma 2B backbone, as shown in Table 7. Results indicate that CoMoE still achieves certain performance gains over the baseline across different backbones. 866

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# H Model efficiency and Computational budget

To evaluate the model efficiency and computational budget of CoMoE, we compare it with the baselines(LoRA, DoRA, MixLoRA, OMOE) in three aspects: inference latency, memory cost, and training time. We base our evaluation on the following three metrics: (a) the inference time required for generating responses (ms), (b) the GPU memory cost (MiB), and (c) the training time in multi-task settings (h). In the multi-task setting, ARC-e, ARCc, BoolQ, and OBQA are trained simultaneously.

| Number of Experts n | ARC-e | ARC-c | BoolQ | OBQA | Avg. |
|---------------------|-------|-------|-------|------|------|
| n = 4               | 80.0  | 66.6  | 71.2  | 77.6 | 73.9 |
| n = 5               | 79.8  | 64.4  | 70.9  | 77.4 | 73.1 |
| n = 6               | 80.6  | 64.5  | 73.1  | 76.0 | 73.6 |
| n = 7               | 79.7  | 65.4  | 72.5  | 78.0 | 73.9 |
| n = 8               | 79.1  | 64.7  | 72.0  | 80.8 | 74.2 |

Table 6: Accuracy results across different expert configurations (from 4 to 8 experts) on multi-task evaluation.

| Method     | ARC-e | ARC-c | BoolQ | OBQA | Avg. |
|------------|-------|-------|-------|------|------|
| MixLoRA    | 22.4  | 24.0  | 62.2  | 27.6 | 34.1 |
| CoMoE-LoRA | 25.7  | 23.7  | 62.2  | 25.2 | 34.2 |

Table 7: Comparison of MixLoRA and CoMoE in multi-task learning. The backbone model is Gemma 2B.

| Method      | Latency (ms) | Memory (MiB) | Training time (h) |
|-------------|--------------|--------------|-------------------|
| LoRA        | 2,096        | +1,630       | 1.8h              |
| DoRA        | 1,748        | +2,184       | 1.7h              |
| MixLoRA     | 4,217        | +1,776       | 2.2h              |
| OMoE(Top-2) | 4,863        | +1,776       | 2.3h              |
| CoMoE       | 3,789        | +1,311       | 3.5h              |

Table 8: The inference latency, memory cost and training time of the LLaMA-2 7B for generating a batch of responses using CoMoE and baselines.

The results are provided in Table 8. From Table 8, we observe that compared to the well-performing MixLoRA, CoMoE achieves a 10% improvement in inference efficiency while reducing GPU memory usage by 465 MiB. In terms of training time, CoMoE requires 3.5 hours of training on an A6000 GPU under the multi-task setting. Although Co-MoE increases the training burden, it does not compromise inference efficiency and simultaneously enhances model performance.

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# I Additional Visualization of Representations under Different Datasets

Our main experiment visualizes the expert representations of the obqa dataset in multi-task settings before and after introducing the contrastive loss, which is illustrated in Fig. 5. The visualization results demonstrate that the introduced contrastive loss promotes modularity among experts while preventing knowledge redundancy between them. Visualization results from other datasets (ARC-c and BoolQ) under the same model, which are provided in Fig. 6 and Fig. 7, yield similar conclusions.



(a) w/o contrastive loss

(b) w/ contrastive loss

Figure 6: Comparison of expert representations in ARC-c before and after contrastive loss incorporation in a multi-task setting. (a) Without contrastive loss. (b) With contrastive loss.



Figure 7: Comparison of expert representations in BoolQ before and after contrastive loss incorporation in a multi-task setting. (a) Without contrastive loss. (b) With contrastive loss.

| Method               | Params | ARC-e | ARC-c | BoolQ | OBQA | PIQA |  |  |  |
|----------------------|--------|-------|-------|-------|------|------|--|--|--|
| Baselines            |        |       |       |       |      |      |  |  |  |
| Parallel-Adapter     | 0.96%  | 67.1  | 54.2  | 65.2  | 76.3 | 69.8 |  |  |  |
| Learned-Adapter      | 0.94%  | 69.3  | 54.4  | 64.9  | 78.4 | 75.6 |  |  |  |
| P-tuning v2          | 0.97%  | 63.5  | 51.3  | 61.2  | 76.1 | 66.2 |  |  |  |
| IAPT                 | 0.96%  | 66.3  | 54.7  | 67.8  | 79.2 | 77.3 |  |  |  |
| BitFit               | 1.00%  | 65.9  | 54.1  | 66.4  | 77.2 | 76.6 |  |  |  |
| $(IA)^3$             | 0.90%  | 68.1  | 54.6  | 67.2  | 78.1 | 75.4 |  |  |  |
| SSP                  | 0.93%  | 71.6  | 57.6  | 69.6  | 79.5 | 79.7 |  |  |  |
| AdaLoRA              | 0.92%  | 73.8  | 57.9  | 69.2  | 80.4 | 82.1 |  |  |  |
| MOELoRA              | 1.00%  | 76.8  | 60.2  | 72.0  | 81.1 | 82.7 |  |  |  |
| MiLoRA               | 0.93%  | 77.8  | 61.2  | 72.8  | 81.7 | 83.3 |  |  |  |
| MiDoRA               | 0.93%  | 77.5  | 61.3  | 72.9  | 81.3 | 83.1 |  |  |  |
| Our proposed methods |        |       |       |       |      |      |  |  |  |
| CoMoE-LoRA           | 1.45%  | 79.0  | 55.5  | 72.9  | 80.0 | 83.6 |  |  |  |
| CoMoE-DoRA           | 1.45%  | 78.7  | 57.0  | 72.9  | 78.4 | 83.8 |  |  |  |

Table 9: An overall comparison of different PEFT methods for single-task learning. Most results are extracted from the original papers or reproduced by running the provided source code. The backbone model is LLaMA-2 7B.