

# EXCESSIVE REASONING ATTACK ON REASONING LLMs

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006 Paper under double-blind review  
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054 rely on modifying model internals, controlling output logits, or injecting external distractions, which  
 055 can limit their generality and practicality.  
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057 In this work, we aim to directly perturb the input to elicit excessive reasoning behavior, increasing  
 058 computational overhead without requiring external content or architectural manipulation. How-  
 059 ever, directly optimizing for excessive reasoning is non-trivial because reasoning length is non-  
 060 differentiable explicitly. Therefore, we propose differentiable proxy losses to approximate the length  
 061 objective and enhance the attack performance via shaping token-level behavior. Concretely, we craft  
 062 the adversarial suffixes with three complementary losses:

- 063 • **Priority Cross-Entropy Loss** prioritizes key tokens while masking less informative ones  
 064 to enhance optimization efficiency. This loss leverages the autoregressive nature of LM to  
 065 enable more targeted and effective gradient updates.
- 066 • **Excessive Reasoning Loss** increases the likelihood of branched or recursive reasoning,  
 067 leading to greater computational overhead.
- 069 • **Delayed Termination Loss** encourages the model to defer the termination of reasoning  
 070 and answer generation.

072 We optimize and evaluate our attacks for the GSM8K (Cobbe et al., 2021) and ORCA (Mitra et al.,  
 073 2024) datasets on DeepSeek-R1-Distill-Llama and DeepSeek-R1-Distill-Qwen. Our attacks con-  
 074 sistently increase the reasoning length by over 3x to 6.5x using only 10 crafted adversarial tokens.  
 075 Moreover, our attack demonstrates strong transferability across models on commercial platforms,  
 076 including OpenAI o3-mini, GPT-OSS (Jaech et al., 2024), DeepSeek-R1, and QWQ, suggesting a  
 077 broader vulnerability among reasoning-optimized LLMs. These findings expose an underexplored  
 078 issue. While such models are proficient in reasoning, they remain susceptible to targeted manipu-  
 079 lations that exploit their reasoning mechanisms to induce significant computational overhead. Our  
 080 results underscore the urgent need for defenses that can detect and mitigate excessive reasoning  
 081 triggered by adversarial prompts.

## 083 2 METHODOLOGY

085 This section presents our adversarial attack framework that increases the computational overhead  
 086 of reasoning LLMs by inducing excessive reasoning. We begin by stating the threat model and the  
 087 use cases. We then conduct two studies. First, we design proxy objectives to approximate the non-  
 088 differentiable length objective. Second, we introduce two token-level losses that further shape token  
 089 behaviors. Finally, we describe the optimization procedure used to generate adversarial attacks.

### 091 2.1 THREAT MODEL

093 The primary objective of our attack is to craft inputs (e.g., suffixes) that compel the model to extend  
 094 the reasoning processes as long as possible, thus significantly increasing the computational cost at  
 095 inference time. Similar to prior work Carlini et al. (2023); Zou et al. (2023); Gao et al. (2024);  
 096 Boucher et al. (2022), we assume a white-box scenario in which the attacker has complete access to  
 097 the model’s architecture, parameters, and gradients.

098 Following Carlini et al. (2023), we consider two primary use cases for our attack. In the first use  
 099 case, a malicious user intentionally induces excessive computational load, degrading overall system  
 100 performance and diminishing service quality for other users, akin to a DoS attack. In the second  
 101 use case, a benign user queries the model within an autonomous system (e.g., LLM Agent) that  
 102 processes untrusted third-party data (e.g., crafted adversarial data), resulting in significantly higher  
 103 costs (e.g., money) than expected. As we later demonstrate, these crafted adversarial inputs exhibit  
 104 strong transferability across different models. Moreover, our attack aligns with the Model Denial of  
 105 Service (MDoS) threat as defined by OWASP, wherein adversarial inputs lead to resource exhaus-  
 106 tion, degrading system responsiveness and service availability for other users.<sup>1</sup>

1<sup>https://genai.owasp.org/llmrisk2023-24/llm04-model-denial-of-service/</sup>

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## 2.2 APPROXIMATE OBJECTIVE FOR LONG REASONING TRAJECTORIES

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In this attack, we aim to craft inputs that elicit the model to produce excessive reasoning. Formally, this corresponds to optimizing the objective  $\mathcal{L}_{long}$  that rewards generations exhibiting excessive reasoning. Since  $\mathcal{L}_{long}$  depends on non-differentiable properties of sampled text (e.g., the length and density of intermediate steps), it cannot be optimized directly.

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Following the adversarial prompt optimization paradigm, we instead optimize against a differentiable proxy. Prior work, such as ATA (Gan et al., 2024) and GCG (Zou et al., 2023), employs cross-entropy (CE) against short fixed targets (e.g., “Sorry, I’m unable to answer the question” or “Sure, I can...”) as surrogates for latent objectives like refusal or compliance. A natural extension is to use CE with long, reasoning-dense targets as a proxy for  $\mathcal{L}_{long}$ . However, this direct approach is ineffective since when supervision is spread uniformly across thousands of tokens, gradients become diffuse. Moreover, because the adversarial suffix typically contains only a few tokens, forcing it to match the distribution of thousands of target tokens is unrealistic.

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To address this, we propose Priority Cross-Entropy (PCE) loss, which reweights supervision to focus on informative, prompt-dependent tokens rather than treating all positions equally. We further enhance the attack performance by constructing reasoning-rich target sequences with DSPy (Khattab et al., 2024), yielding more effective surrogates for the  $\mathcal{L}_{long}$  objective.

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**Optimizing toward long targets.** We begin by examining the standard CE objective and its limitations when applied to a long target. Traditional adversarial attacks on LMs minimize CE to increase the likelihood of a target sequence (e.g., “Sure, I can ...”). Formally, for base input  $x$ , adversarial suffix  $x'$ , and target sequence  $y$ , the objective is

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$$\mathcal{L}_{CE} = -\log p(y | \{x, x'\}). \quad (1)$$

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In prior work, the target  $y$  is typically short (often  $< 10$  tokens). However, to elicit excessive reasoning,  $y$  is much longer (e.g.,  $> 1,000$  tokens). Uniformly supervising all positions in such sequences is optimization-inefficient since the gradient signal is spread across thousands of tokens. Also, many tokens (e.g., “the” and “I”) can be accurately generated even without the prompt, due to statistical priors learned during pretraining. This suggests that optimizing every token is unnecessary; instead, supervision should focus on the prompt-dependent tokens that may influence the emergence of excessive reasoning.

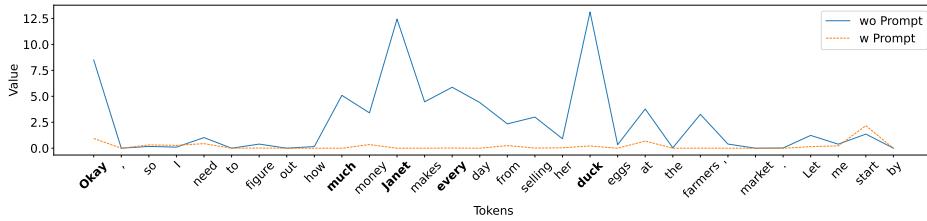
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Figure 1: The perplexity of a reasoning sample in the output with and without the prompt. Bold tokens are assigned 1 in the mask.

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To investigate this, we analyze the per-token perplexity distribution of a target sequence with and without the input prompt. As shown in Fig. 1, only a small subset of tokens exhibits a substantial change in perplexity when the prompt is removed. This supports our hypothesis that informativeness is not uniformly distributed across tokens, and that only a subset is highly dependent on the prompt.

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Building on this insight, we design a token-level importance mask that emphasizes tokens the model considers informative, thereby improving optimization efficiency. For each target token  $y_t$ , we compute an importance score as the change in log-probability with and without the prompt:

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$$S_t = \log p(y_t | x, y_{<t}) - \log p(y_t | y_{<t}). \quad (2)$$

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This score quantifies the extent to which each token’s prediction relies on the presence of the prompt. We then construct a binary mask  $\mathcal{M}$  by selecting the top  $K\%$  of tokens with the highest importance scores (set  $M_t = 1$ ) and assigning zero weight to the rest (set  $M_t = 0$ ).

162 **Priority Cross-Entropy Loss.** Putting these pieces together, we modify standard CE to focus su-  
 163 pervision on prompt-sensitive tokens. The resulting PCE objective is  
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$$165 \quad \mathcal{L}_{\text{PCE}} = -\frac{1}{|y|} \sum_{t=1}^{|y|} \mathcal{M}_t \cdot \log p(y_t | \{x, x'\}, y_{<t}). \quad (3)$$

168 This targeted supervision improves optimization efficiency and increases the likelihood that the  
 169 model produces excessive reasoning at inference. Empirically, PCE substantially raises the fre-  
 170 quency of reasoning (Fig. 3).

171 **Constructing long targets.** Because our attack seeks to elicit excessive reasoning, the proxy objec-  
 172 tive itself must involve long outputs. Short fixed targets (as in ATA and GCG) are less effective here  
 173 since they do not encourage extended reasoning and provide little supervision on reasoning struc-  
 174 ture. We therefore construct long proxy targets. As simple baselines, we (i) sample multiple model  
 175 outputs per input and select the longest sequence, and (ii) append the reasoning-oriented prompt  
 176 (e.g., CoT) that naturally elicits step-by-step derivations to each input.

177 To obtain stronger proxies, we first leverage DSPy to iteratively refine the CoT prompt on a small  
 178 dataset with the explicit objective of maximizing output length. Then, we query the model with  
 179 each input and append the DSPy-optimized prompt to obtain the long, reasoning-dense target tra-  
 180 jectories. Together with PCE, these long trajectories serve as effective proxies for the  $\mathcal{L}_{\text{long}}$  objec-  
 181 tive. App. C.3 provides the DSPy-optimized prompt, a sample output, and statistics across different  
 182 prompting baselines. We also examine the impact of various construction baselines in App. C.5.

### 184 2.3 SHAPING TOKEN-LEVEL BEHAVIOR FOR EXCESSIVE REASONING

186 Building on PCE and long targets, we next shape token-level behavior to further promote exces-  
 187 sive reasoning. We introduce two complementary losses: Excessive Reasoning (ER) Loss, which  
 188 increases the likelihood of reasoning-associated tokens, and Delayed Termination (DT) Loss, which  
 189 discourages premature end-of-thinking/sequence decisions.

190 **Excessive Reasoning Loss.** In the previous section, we have described how DSPy-optimized  
 191 prompts yield long target trajectories. Within these outputs, we observe that certain tokens (e.g.,  
 192 “Wait”, “Alternatively”; see App. C.3) frequently occur in outputs and often signal branching or  
 193 recursive reasoning steps, consistent with prior findings (Wang et al., 2025; Chen et al., 2024). To  
 194 exploit this behavior, we aim to increase the likelihood of generating such tokens during the rea-  
 195 soning. While it is possible to construct a manual list of indicative tokens, this approach does not  
 196 scale and may miss less obvious but influential cases. Instead, we adopt a data-driven approach to  
 197 automatically identify reasoning-associated tokens. As demonstrated in our analysis (Sec. 3.2), this  
 198 approach uncovers influential tokens that would likely be overlooked through manual inspection,  
 199 underscoring the efficacy of our method.

200 Concretely, we extract the top  $n$  most frequent tokens that appear in the first two positions of each  
 201 sentence generated during constructing long-from targets. These tokens are hypothesized to play a  
 202 critical role in initiating new reasoning trajectories. Let  $\mathcal{T}$  denote the collected set of high-impact  
 203 tokens. To promote their occurrence during generation, we define the ER Loss as:

$$204 \quad \mathcal{L}_{\text{ER}} = -\frac{1}{|y|} \sum_{t=1}^{|y|} \sum_{v \in \mathcal{T}} \log p(y_t = v | \{x, x'\}, y_{<t}). \quad (4)$$

207 This objective increases the likelihood of generating collected high-impact tokens, thereby inducing  
 208 longer reasoning sequences.

210 **Delayed Termination Loss.** In many reasoning LLMs, the generation process typically begins  
 211 with intermediate reasoning steps, which conclude with a designated end-of-thinking (EOT) token  
 212 (e.g., </think>). Then, the model would generate an answer conclusion terminated by an end-of-  
 213 sequence (EOS) token (e.g., <eos>). To prolong both the reasoning and answer conclusion phases,  
 214 we aim to reduce the model’s tendency to emit these termination tokens during decoding. However,  
 215 due to the stochastic nature of autoregressive generation, the precise timestep at which these tokens  
 appear is not fixed. To address this, we adopt a strategy from prior work (Chen et al., 2022; Gao

et al., 2024), which minimizes the likelihood of generating termination tokens across all positions in the output sequence:

$$\mathcal{L}_{\text{DT}} = \frac{1}{|y|} \sum_{t=1}^{|y|} \left[ p(y_t = \text{EOS} \mid \{x, x'\}, y_{<t}) + p(y_t = \text{EOT} \mid \{x, x'\}, y_{<t}) \right].$$

This objective discourages premature termination, encouraging the model to continue generating extended reasoning and answer conclusions before finalizing its output.

## 2.4 OPTIMIZATION

Optimizing suffixes in the text domain presents a unique challenge due to the discrete nature of language. Unlike continuous domains (e.g., images), where gradients can be directly applied to pixel values, LMs operate on sequences of discrete tokens drawn from a fixed vocabulary. As a result, standard gradient-based optimization cannot be directly applied to manipulate individual tokens.

To address this, we adopt the Greedy Coordinate Gradient-based Search (GCG) framework (Zou et al., 2023), which has demonstrated strong performance in adversarial text generation. GCG linearizes the loss landscape by computing gradients with respect to input embeddings and identifying substitutions that are most likely to improve the loss. Specifically, for a given token position  $i$  in the suffix, we compute the gradient of the loss with respect to its embedding and search for the token  $x'_i$  that maximally improves the objective. Formally:

$$x'_i = \arg \max_{w \in V} \langle \nabla_{e(x_i)} \mathcal{L}, e(w) - e(x_i) \rangle, \quad (5)$$

where  $\nabla_{e(x_i)} \mathcal{L}$  denotes the gradient of the loss with respect to the embedding of token  $x_i$ , and  $e(w)$  is the embedding of candidate token  $w$ . This inner product quantifies the expected gain from substituting  $x_i$  with  $w$ , and the best candidate is selected greedily. Our overall objective combines the three loss components introduced previously:

$$\mathcal{L}_{\text{long}} = \alpha \cdot \mathcal{L}_{\text{PCE}} + \beta \cdot \mathcal{L}_{\text{ER}} + \gamma \cdot \mathcal{L}_{\text{DT}}. \quad (6)$$

In this work, we employ a fixed-length suffix-based optimization, where a set of tokens is appended to the end of the original prompt. Each token in the suffix is iteratively updated using GCG to minimize the combined loss. Although this paper focuses on crafting adversarial suffixes, it is important to note that our approach is *method-agnostic* and can be adapted to any paradigms. For instance, alternative strategies such as character-level perturbations (e.g., typos) can be incorporated, as shown in prior work (Gan et al., 2024). This flexible framework facilitates the efficient generation of adversarial inputs tailored to different attack constraints.

## 3 EXPERIMENTS

### 3.1 EXPERIMENTAL SETUPS

**Models and Datasets.** We optimize adversarial suffixes and evaluate them on two reasoning LLMs: DeepSeek-R1-distill-LLaMA-8B and DeepSeek-R1-distill-Qwen-7B.<sup>2</sup> Both models are distilled variants of DeepSeek-R1. We report results under two decoding strategies: greedy decoding and sampling decoding. For sampling, we set the temperature to 0.6, apply nucleus sampling with  $\text{top-}p = 0.95$ , and **repeat 10 times**. To assess cross-model transferability, we additionally evaluate the attack on larger-scale models, including o3-mini, GPT-OSS (with low and medium reasoning), DeepSeek-R1, and QWQ-32B, using their respective default decoding settings. Our evaluation is conducted on two widely used mathematical reasoning benchmarks: GSM8K (Cobbe et al., 2021) and ORCA (Mitra et al., 2024). For each dataset, we randomly sample 50 examples for both optimization and evaluation. More details are provided in App. C.4.

**Attack Setup.** For DSPy, we use the COPRO optimizer with “gpt-4o-mini” to refine the CoT prompt. Specifically, we use 10 training examples from the GSM8K dataset for DSPy optimization

<sup>2</sup>For simplicity, we omit the prefix DeepSeek-R1-distill throughout the remainder of the paper.

	Models	Methods	GSM8K					ORCA						
			Rea	Ans	Full	Lat	Ent	Acc	Rea	Ans	Full	Lat	Ent	
270 271 272 273 274 275 276 277 278 279 280	LLaMA	Original	668	239	907	24.3	4628	72%	499	213	712	19.3	4366	<b>82%</b>
		Random	447	264	711	19.0	3571	74%	440	228	668	17.6	3570	76%
		CoT	574	<b>266</b>	839	22.2	4712	70%	344	<b>259</b>	603	14.7	2789	<b>82%</b>
		Engorgio	168	274	443	10.4	1804	68%	189	219	408	9.19	1644	82%
		CatAttack	496	232	729	19.7	3959	76%	338	233	571	15.3	3013	78%
		Ours	<b>1914</b>	160	<b>2074</b>	<b>54.9</b>	<b>12827</b>	<b>92%</b>	<b>1575</b>	167	<b>1743</b>	<b>47.2</b>	<b>9929</b>	80%
281 282 283 284 285 286 287 288 289 290 291 292	Qwen	Original	237	282	519	12.8	2498	84%	531	220	750	18.4	4034	84%
		Random	159	294	453	11.2	2097	82%	527	225	752	18.7	3505	86%
		CoT	169	<b>310</b>	479	11.9	2535	82%	379	<b>248</b>	626	15.6	2910	86%
		Engorgio	832	274	1106	24.4	4661	82%	273	203	476	9.99	1811	86%
		CatAttack	167	295	461	11.3	2171	78%	532	234	766	18.5	4040	82%
		Ours	<b>1531</b>	193	<b>1724</b>	<b>42.4</b>	<b>8188</b>	<b>88%</b>	<b>1459</b>	166	<b>1624</b>	<b>39.6</b>	<b>9155</b>	<b>88%</b>

Table 1: The token length for reasoning (Rea), answer (Ans), and full output (Full); inference latency (Lat, in seconds); energy consumption (Ene, in joules); and task accuracy (Acc). Experimental results across methods under greedy decoding. **Bold** indicates the best result.

and evaluate on a separate set of 10 randomly selected test samples. Due to computational constraints, we restrict target outputs to a maximum length of 3,000 tokens. For the PCE Loss, we set the token selection threshold  $K = 1$ , and for the ER Loss, we use  $n = 5$ . The overall loss function combines the three components using the following weighting coefficients:  $\alpha = 1$ ,  $\beta = 50$ , and  $\gamma = 1$ . We fix the length of the adversarial suffix to 10 tokens. During optimization, we apply the GCG algorithm for 1,000 steps per input. The candidate pool size is set to 64, and at each step, the top 64 candidate tokens are retained.

**Evaluation Metrics.** To evaluate the effectiveness of our adversarial attack, we consider three primary metrics: (1) output sequence length (tokens), (2) inference latency (seconds), and (3) energy consumption (Joules). Energy usage is measured using the NVIDIA Management Library, following the methodology introduced by (Shumailov et al., 2021). To ensure consistency and fair comparison, all inference is performed using the HuggingFace pipeline (Wolf et al., 2019) on a single hardware (NVIDIA A100 80GB). Each inference is repeated three times to reduce the impact of runtime variability. To assess model utility, we extract final answers from the generated outputs using “Meta-Llama-3.1-8B-Instruct”, and compute accuracy by comparing the extracted answers against ground-truth labels. The exact prompt used for extraction is provided in App. C.1.

**Baselines.** We compare our attack against several baseline methods:

- **Random:** 10 randomly sampled tokens.
- **Standard CoT (Wei et al., 2022):** A widely used CoT prompt that appends the phrase “Let’s think step by step.”
- **Engorgio (Dong et al., 2025):** A method for crafting “inference-cost” attacks via adversarial prompts that force auto-regressive LLMs to produce excessively long outputs.
- **CatAttack (Rajeev et al., 2025):** A prompt-based adversarial strategy that appends the distractor statement “Interesting fact: cats sleep most of their lives,” which has been shown to induce incorrect reasoning outputs.

### 3.2 MAIN RESULTS

**Performance.** As shown in Table 1 and Table 12, our adversarial suffix substantially increases computational overhead while preserving task accuracy across all settings. For example, our attack causes LLaMA to generate significantly longer outputs on the GSM8K dataset with greedy decoding, increasing the average reasoning length by 3x from 668 to 1,914 tokens. This is accompanied by a corresponding increase in energy consumption (from 4,628J to 12,827J) and latency (from 24.3s to 54.9s). A similar trend is observed for Qwen, where the average reasoning length increases by 6.5x, demonstrating the effectiveness of our attack across different model architectures. Under sampling-based decoding, the attack remains robust. The reasoning length increases by 3x for LLaMA and 4x for Qwen on GSM8K, with similar results observed on the ORCA dataset.

324	325	Models	Methods	GSM8K					ORCA						
				326	Rea	Ans	Full	Lat	Ent	Acc	327	Rea	Ans	Full	Lat
328	329	LLaMA	Original	556	257	812	71.5	9778	76%	550	248	798	86.7	10490	81%
			Random	401	270	671	54.0	7928	72%	493	244	737	80.6	9689	81%
			CoT	476	<b>280</b>	757	68.5	7713	75%	402	<b>266</b>	668	75.9	9148	80%
			Engorgio	161	282	443	15.3	3055	68%	249	234	484	39.1	9663	80%
			CatAttack	528	257	785	64.8	9818	77%	475	224	700	81.4	10680	82%
			Ours	<b>1437</b>	204	<b>1641</b>	<b>197.0</b>	<b>21228</b>	<b>90%</b>	<b>1425</b>	206	<b>1631</b>	<b>178.2</b>	<b>19243</b>	<b>87%</b>
330	331	Qwen	Original	345	277	622	37.0	5996	82%	452	250	701	51.2	7538	84%
			Random	221	296	518	23.4	4245	84%	501	254	755	54.5	7353	86%
			CoT	176	<b>308</b>	484	16.0	3799	85%	293	<b>274</b>	567	33.1	5722	<b>87%</b>
			Engorgio	191	300	490	20.5	4352	81%	268	205	473	21.9	4718	78%
			CatAttack	187	295	482	17.4	3398	81%	432	253	686	50.0	6458	83%
			Ours	<b>1479</b>	217	<b>1696</b>	<b>149.1</b>	<b>16031</b>	<b>91%</b>	<b>1238</b>	183	<b>1421</b>	<b>111.2</b>	<b>14747</b>	<b>87%</b>

Table 2: Experimental results across methods under sampling decoding.

In comparison, baseline methods generally induce relatively short reasoning. For example, CoT prompts produce shorter outputs than our adversarial prompt on LLaMA for GSM8K under greedy decoding (839 vs. 2,074 tokens), indicating the limitations of standard methods in eliciting excessive reasoning behavior. More broadly, our results suggest that reasoning LLMs are resistant to short prompting, as neither CoT nor CatAttack reliably triggers long reasoning. Interestingly, we observe a consistent inverse correlation between the lengths of reasoning and answer segments. We hypothesize that as the model allocates more capacity to the reasoning phase, the corresponding answer portion becomes shorter. Also, the increase in reasoning length does not degrade task accuracy. In most cases, our triggered excessive reasoning produces meaningless reasoning, as shown in App. C.2 (sample 1). However, we also find that in a few cases, the regular reasoning is too simple and fails to solve the problem, while our triggered excessive reasoning occasionally fixes it, as shown in App. C.2 (sample 2). For example, the original response contains a single solution (reasoning path) and it actually leads to an incorrect calculation. In contrast, our attack triggers excessive reasoning that explicitly extends the thinking with multiple solutions; however, we can see that the last solution (reasoning path) is redundant since the answer has already been inferred correctly. In general, the majority of problems can be solved with baseline prompting, and our attack, in most cases, simply extends the reasoning unnecessarily, leading to computational waste. Together, these results demonstrate that our attack amplifies the computational burden of reasoning models without compromising their effectiveness. We also provide an additional study on ELI5, optimized suffix, and sample outputs in App. C.2.

**Analysis.** To determine whether our adversarial suffixes truly elicit excessive reasoning rather than merely increasing output length, we conduct an analysis of the generated outputs. First, we observe a substantial increase in the average number of reasoning sentences. For LLaMA, the average rises from 32 to 88, and for Qwen, from 11 to 74, when comparing outputs generated from original prompts to those generated with adversarial suffixes. This indicates that our attack expands the number of reasoning rather than just inflating output length.

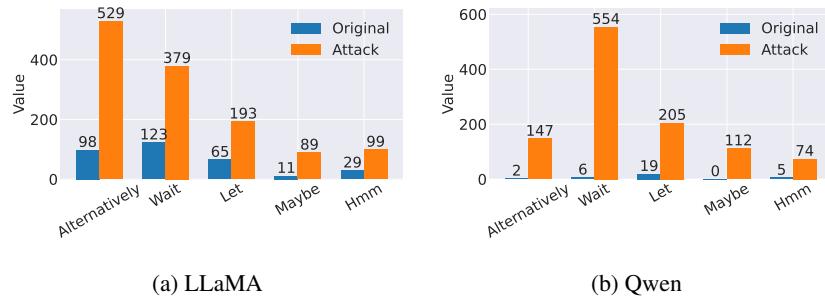


Figure 2: Token counts between the generated outputs from the original and adversarial prompts.

Next, we examine the distribution of the first two tokens in reasoning sentences (Fig. 2). The results reveal distinct lexical patterns between the two models. LLaMA often begins with deliberative tokens such as “Alternatively” and “Wait,” associated with recursive reasoning, while Qwen is less

	Models	Methods	GSM8K			ORCA		
			Toks	Acc	Toks/Acc	Toks	Acc	Toks/Acc
LLaMA	Original	907	72%	12.6		712	<b>82%</b>	8.7
	Ours	<b>2074</b>	<b>92%</b>	<b>22.5 (1.8×)</b>		<b>1743</b>	80%	<b>21.8 (2.5×)</b>
Qwen	Original	519	84%	6.2		750	84%	8.9
	Ours	<b>1724</b>	<b>88%</b>	<b>19.6 (3.2×)</b>		<b>1624</b>	<b>88%</b>	<b>18.5 (2.1×)</b>

Table 3: Tokens per accuracy (Toks/Acc) under Original vs. our attack with greedy decoding. Ratios show relative increases over Original.

Model	Reason	Answer	LLaMA			Qwen		
			Full	Accuracy	Match	Reason	Answer	Full
QWQ	1761 (-151)	231 (-6)	1992 (-157)	93% (-3%)	62%	2489 (+577)	317 (+80)	2806 (+657)
R1	997 (-74)	185 (-13)	1182 (-87)	95% (-2%)	4%	1295 (+224)	233 (+36)	1528 (+260)
o3-mini	446 (+199)	184 (+46)	630 (+245)	90% (+1%)	20%	645 (+398)	336 (+199)	982 (+596)
gpt5-mini	<b>343 (+175)</b>	<b>106 (+34)</b>	<b>449 (+209)</b>	<b>77% (-7%)</b>	<b>60%</b>	<b>578 (+410)</b>	<b>210 (+138)</b>	<b>787 (+547)</b>
Gemini-Flash	<b>665 (+146)</b>	<b>350 (+76)</b>	<b>1015 (+222)</b>	<b>86% (-3%)</b>	—	<b>874 (+355)</b>	<b>513 (+239)</b>	<b>1388 (+594)</b>
OSS (low)	79 (+13)	170 (+35)	249 (+48)	92% (+2%)	20%	95 (+19)	316 (+167)	411 (+186)
OSS (medium)	569 (+149)	237 (+111)	806 (+259)	90% (+1%)	20%	3015 (+2569)	348 (+206)	3363 (+2775)

Table 4: Transferability analysis of adversarial suffixes originally optimized for LLaMA and Qwen.

sensitive to “*Alternatively*,” suggesting that the expression of excessive reasoning may manifest differently across architectures. Notably, Qwen does not exhibit the same degree of excessive reasoning as LLaMA under standard conditions but becomes vulnerable when adversarial suffixes are applied. Tokens such as “*Let*”, “*Maybe*”, and “*Hmm*”, which are difficult to detect manually, highlight the utility of ER Loss combined with automated token selection in surfacing subtle prompts that trigger excessive reasoning behavior.

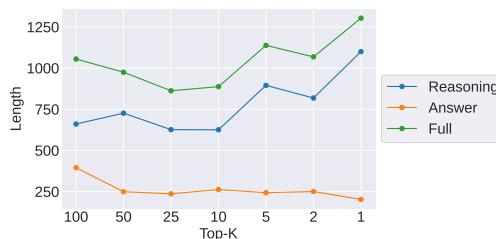
Finally, we use the Tokens per Accuracy metric to measure reasoning efficiency in Table 3. Lower values indicate concise, effective reasoning, while higher values reflect inefficient reasoning. Across all model–dataset pairs, adversarial suffixes inflate this metric. For instance, on GSM8K, LLaMA’s tokens per accuracy point increase from 12.6 to 22.5 (a 1.8x increase), indicating that the model requires substantially more tokens per correct answer. This consistent pattern demonstrates that our method successfully induces inefficient, overextended reasoning.

**Transferability.** We evaluate the transferability of our adversarial suffixes to larger commercial LMs, including o3-mini, GPT-OSS, DeepSeek-R1, and QWQ. Specifically, we test adversarial suffixes optimized on the LLaMA and Qwen models for the GSM8K dataset, with results summarized in Table 4. Our findings show that these adversarial suffixes generalize effectively, consistently promoting longer output sequences without degrading task accuracy. For the OpenAI model family, both LLaMA- and Qwen-optimized suffixes successfully increase output length. For example, suffixes optimized on LLaMA lead to a 245-token increase in total output length for o3-mini, and Qwen-optimized suffixes yield a 596-token increase.

In contrast, transferability to DeepSeek-R1 appears to depend on the source model. Qwen-optimized suffixes result in a 260-token increase, whereas LLaMA-optimized suffixes fail to induce longer outputs. **We hypothesize that this discrepancy is due to the token mismatch between the source and target models.** We report the Match metric to reflect the token alignment rate between the source model and the target model. Specifically, we check whether the token length of the optimized suffix—when encoded by the source model and by the target model (e.g., gpt5)—is the same. If the lengths match, it indicates that none of the tokens in the optimized suffix are split or merged when processed by the target model. We observe that when the Match score is high, the overall length is also high, demonstrating a positive relationship between the two. These results suggest that while architectural differences influence the degree of computational overhead, token alignment plays a critical role in the transferability of adversarial prompts.

### 3.3 ABLATION STUDIES

We conduct a series of ablation studies to assess the impact of different experimental configurations, including the introduction of the PCE Loss and the individual contribution of each loss component.

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440441 Figure 3: Impact of varying the top-K most informative tokens on LLaMA under greedy decoding.  
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Setup	Reason	Answer	Full	Latency	Energy	Accuracy
$\mathcal{L}_{PCE}$	1100	<b>202</b>	1303	35.0	7016	84%
$\mathcal{L}_{PCE} + \mathcal{L}_{ER}$	1169	188	1357	36.1	8089	88%
$\mathcal{L}_{PCE} + \mathcal{L}_{DT}$	1447	201	1648	43.9	9558	88%
$\mathcal{L}_{PCE} + \mathcal{L}_{ER} + \mathcal{L}_{DT}$	<b>1914</b>	160	<b>2074</b>	<b>54.9</b>	<b>12827</b>	<b>92%</b>

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Table 5: Different loss combinations on LLaMA under greedy decoding.

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**PCE Loss.** We begin by evaluating the effectiveness of the proposed PCE Loss by varying the proportion of top- $K$  tokens from 100% (Original CE) to 1%, as shown in Fig. 3. The results show that focusing optimization on the top 5%, and particularly the top 1% of tokens, consistently outperforms applying loss uniformly across all tokens. Peak performance is observed when focusing solely on the top 1%, with the number of reasoning tokens increasing from 660 to 1,100. This pattern suggests that selectively emphasizing a small subset of salient, prompt-dependent tokens can more effectively induce extended reasoning behavior. Additionally, we observe an inverse relationship between the number of reasoning and answer tokens, implying a redistribution of the model’s generative capacity toward reasoning content. These findings underscore the value of targeted token optimization and demonstrate that prioritizing high-impact tokens is more effective than uniformly distributing the loss across the entire sequence.

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**Loss Objectives.** Second, we evaluate the individual contributions of each loss function and assess their collective impact as presented in Table 5. The results show that optimizing each loss independently leads to an increase in output sequence length, and the combination of all three losses yields the most substantial gains in both sequence length and computational burden. For instance, the full composite loss achieves the longest average output (up to 2,074 tokens), the highest inference latency (54.9 seconds), and the greatest energy consumption (12,827J). These results underscore the synergistic effect of combining all three objectives.

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To further analyze the behavior encouraged by the ER Loss, we visualize a word cloud of the most frequently prioritized tokens in Fig. 5. Common deliberative tokens identified in prior work, such as “Alternatively” and “Wait”, are prominently featured. In addition, our method surfaces previously underexplored tokens such as “Maybe” and “Hmm”, which act as effective triggers for extended reasoning. These findings confirm that the joint loss formulation effectively amplifies reasoning behavior while preserving task accuracy, and that the ER Loss successfully uncovers subtle lexical cues indicative of recursive reasoning.

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#### 4 POTENTIAL DEFENSES

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Currently, no defenses are proposed explicitly against reasoning-based attacks. To evaluate potential countermeasures, we test four strategies: two at the input level and two at the output level, with details summarized in App.B. Naïve methods, such as perplexity-based filtering, yield high false positives and significantly degrade user experience. Safety classifiers are another possible input-level defense, but our attack bypasses them with high success rates. At the output level, we examine two decoding techniques aimed at curbing excessive reasoning. Thought Switching Penalty (TIP) (Wang et al., 2025) penalizes reasoning-disruptive tokens but fails to shorten overall outputs, while Dynamic Early Exit for Reasoning (DEER) (Yang et al., 2025) halts decoding once a confident

486 answer is reached but may even reduce model utility. Overall, these findings show that our attack  
 487 remains robust against different defenses.  
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## 489 5 RELATED WORK 490

491 **Adversarial Attacks on LLMs.** Adversarial attacks on LLMs present unique challenges due to the  
 492 discrete nature of text, which limits the applicability of gradient-based techniques commonly used in  
 493 vision tasks. Early work, such as HotFlip (Ebrahimi et al., 2018), has introduced token-level pertur-  
 494 bations as vectors, enabling efficient gradient-guided attacks on classification models. This approach  
 495 was further developed by Universal Adversarial Triggers (UAT) (Wallace et al., 2019), which iden-  
 496 tified fixed token sequences that could consistently manipulate model outputs across diverse input  
 497 data. More recently, GCG (Zou et al., 2023) demonstrated strong performance in generating adver-  
 498 sarial suffixes that elicit specific responses. BEAST (Sadasivan et al., 2024) improves upon GCG  
 499 by incorporating beam search to enhance linguistic coherence, thereby increasing the effectiveness  
 500 of adversarial prompts in bypassing safety filters.

501 **Denial-of-Service Attacks on LLMs.** Denial-of-service (DoS) attacks on LLMs aim to degrade  
 502 system performance by manipulating input prompts to increase computational cost, latency, or en-  
 503 ergy consumption. For example, Sponge attacks (Shumailov et al., 2021) maximize the L2 norm  
 504 of internal activations, thereby exhausting system resources during inference. Subsequent work on  
 505 energy-latency manipulation introduced crafted inputs that prolong decoding time or increase mem-  
 506 ory usage. NICGSlowDown (Chen et al., 2022) demonstrated that minimizing the probability of  
 507 EOS tokens results in excessively long outputs in captioning models, significantly increasing the  
 508 computational load. More recently, Overthink (Kumar et al., 2025) was proposed as an indirect  
 509 prompt injection method that utilizes decoy tasks to induce unnecessary reasoning overhead. In  
 510 contrast, Crabs (Zhang et al., 2025) shares a similar idea but places the decoy within the user query.  
 511 Additionally, Engorgio Prompt (Dong et al., 2025) demonstrates how attackers can trigger excessive  
 512 resource usage in white-box settings with a re-parameterization design.

## 513 6 CONCLUSION 514

515 In this work, we present a novel adversarial attack on reasoning LLMs that induces computational  
 516 overhead during inference. Our approach appends adversarial suffixes that trigger extended rea-  
 517 soning trajectories, optimized through a composite loss function that maximizes output length and  
 518 complexity. Empirical results demonstrate that the method reliably increases sequence length, infer-  
 519 ence latency, and energy consumption. Moreover, the strong cross-model transferability highlights  
 520 the practical relevance of this threat.

521 **Limitations.** Based on the analysis, we can see that the choice of optimized tokens is also criti-  
 522 cal and constrained by the tokenizer used. Right now, many commercial APIs—such as Ope-  
 523 nAI—release their tokenizers, and tokenizer inference attacks also exist and can be used to recover  
 524 unknown tokenizers. In future work, the selection of optimized tokens can be incorporated as an  
 525 additional optimization constraint, not only for this attack but for other adversarial methods as well.

## 527 528 ETHICS STATEMENT 529

530 This study utilizes publicly available datasets and models, with appropriate citations provided. No  
 531 private or sensitive information is used, and the work does not include any harmful content. Because  
 532 the research relies exclusively on publicly available data and does not involve human participants,  
 533 it does not qualify as human subjects research under Institutional Review Board (IRB) definitions.  
 534 Accordingly, we conclude that this paper raises no ethical concerns.

## 536 537 REPRODUCIBILITY STATEMENT 538

539 We provide detailed descriptions of the training and evaluation procedures used in our experiments.  
 In particular, we describe our proposed attack in detail (see Sec. 2), followed by the specifications

540 of the models, datasets, and decoding strategies used (see Sec. 3.1). All prompting templates are  
 541 included in the Appendix for reference. The code will be released upon publication of this paper.  
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## 683 A THE USE OF LARGE LANGUAGE MODELS

685 In this paper, LLMs are employed to enhance the clarity, fluency, and overall quality of writing.  
 686 Their use is limited to language refinement and does not extend to the design, execution, or analysis  
 687 of the experiments. Also, all polished texts are double-checked by authors to ensure accuracy, avoid  
 688 overclaims, and prevent confusion.

## 690 B DEFENSE STUDIES

693 **Input-level.** At the input level, we begin by evaluating a perplexity-based filtering strategy, follow-  
 694 ing the similar setup described in (Dong et al., 2025). We compute universal perplexity thresholds  
 695 using the Open-Platypus dataset, assuming the model owner has no prior knowledge of the adversar-  
 696 ial suffix. Specifically, we select the 25th, 50th, and 75th percentile quantiles as thresholds to filter  
 697 prompts exhibiting unusually high perplexity.

698 We test the filter on both clean prompts and prompts appended with adversarial suffixes as shown  
 699 in Table 7. While this method achieves a 100% true positive rate in detecting adversarial prompts,  
 700 it also results in high false positive rates for clean prompts—100%, 78%, and 16% on LLaMA,  
 701 and 100%, 84%, and 28% on Qwen at the respective thresholds. These results suggest that our  
 optimized suffixes are difficult to identify when the model owner lacks prior knowledge of their

	LLaMA				Qwen			
	Reason	Answer	Full	Accuracy	Reason	Answer	Full	Accuracy
Base	668	239	907	72%	237	282	519	84%
Base + TIP	422	250	673	74%	264	283	547	84%
Ours	1914	160	2074	92%	1531	193	1724	88%
Ours + TIP	1863	173	2037	94%	1464	198	1661	84%
Base	668	239	907	72%	237	282	519	84%
Base + DEER	247	237	484	70%	217	268	485	86%
Ours	1914	160	2074	92%	1531	193	1724	88%
Ours + DEER	1074	216	1290	72%	426	518	945	88%

Table 6: Output-level defense results for GSM8k on LLaMA and Qwen.

Quantile	LLaMA		Qwen	
	FP (%)	TP (%)	FP (%)	TP (%)
25	100	100	100	100
50	78	100	84	100
75	16	100	28	100

Table 7: False positive rate (FP) for filtering clean prompts and true positive rate (TP) for filtering attack prompts using perplexity-based filtering across different quantiles.

structure. Also, applying high-percentile quantile thresholds may severely degrade the utility of the model on benign inputs. For the second defense, we apply an open-source safety classifier, “meta-llama/Llama-Prompt-Guard-2-86M,” to flag unsafe inputs. The classifier detects only 8% of adversarial prompts on LLaMA and 6% on Qwen. These findings indicate that our adversarial suffixes are able to bypass the classifier in most cases.

**Output-level.** At the output level, we evaluate two complementary mitigation techniques. The first, Thought Switching Penalty (TIP) (Wang et al., 2025), penalizes the generation of reasoning-disruptive tokens such as “Wait” or “Alternatively.” The second, Dynamic Early Exit for Reasoning (DEER) (Yang et al., 2025), reduces unnecessary token generation by terminating decoding early once a confident answer is detected.

As shown in Table 6, on LLaMA, our attack generated 1,914 reasoning tokens and 160 answer tokens, totaling 2,074 tokens, with an accuracy of 92%. Applying TIP led to a modest reduction in total tokens (2,037) and a slight increase in accuracy to 94%. In contrast, DEER reduced the length of reasoning (to 1,290 tokens) but caused a more substantial performance drop, lowering accuracy to 72%. A similar trend was observed on Qwen: TIP preserved accuracy while modestly reducing output length, whereas DEER can only reduce the total token count (945 tokens). In addition, DEER requires extra processing time, which also incurs additional latency and energy costs. Overall, these results suggest that TIP provides only limited mitigation against our attack, while DEER is more effective at curbing excessive reasoning, but at the cost of degraded task performance and additional computational resources. Nevertheless, our attack still incurs substantial resource overhead due to excessive and redundant token generation compared to Original.

## C ADDITIONAL EXPERIMENTAL DETAILS

In this section, we present additional details of our experimental setup, including the prompting templates, sample outputs and suffixes, outputs and prompts from DSPy, analysis of the attack behavior, descriptions of the models and datasets employed, as well as the computational resources utilized.

756 C.1 PROMPT TEMPLATE  
757758 **Prompting template for extracting answer**  
759760 Here is a math question and a model's answer about this question.  
761 Please extract the EXACT number from the answer text as the final answer for question.  
762 QUESTION: {}  
763 ANSWER: {}  
764 Final format should be a legal 'number' without any suffix such as '\$'.  
765 The final answer is:766  
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768 C.2 SAMPLES  
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770771 **Prompt + Optimized Suffix**772 Janet's ducks lay 16 eggs per day. She eats three for breakfast every morning and bakes muffins  
773 for her friends every day with four. She sells the remainder at the farmers' market daily for \$2  
774 per fresh duck egg. How much in dollars does she make every day at the farmers' market? ?!  
775 Contains more tricks..... Elijahnumeric paradox nearer[/]776  
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779 **Sample response 1 from our attack**780 Okay, so I need to figure out how much money Janet makes every day from selling her duck  
781 eggs. Let me start by breaking down the information given.  
782 First, Janet's ducks lay 16 eggs per day. That's the total number of eggs she gets each day. Now,  
783 she has some daily responsibilities that involve using these eggs. She eats three for breakfast  
784 every morning, so that's 3 eggs used daily. Then, she bakes muffins for her friends every day  
785 with four eggs. Wait, does that mean she uses 4 eggs per day ...  
786 So far, she's using 3 eggs for breakfast and 4 for baking, which totals 7 eggs per day. She lays  
787 16 eggs ...  
788 So, 9 eggs sold at \$2 each would be 9 times 2, which equals \$18. Therefore, Janet makes \$18  
789 every day from selling her eggs ...  
790 Wait, let me double-check to make sure I didn't miss anything. She lays 16, uses 3 for breakfast,  
791 4 for baking, so  $16 - 3 - 4 = 9$ . Yes, that's correct. And each egg is sold for \$2, so 9 times 2 is  
792 indeed \$18. I think that's all there is to it. ....793  
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795796 **Sample response 1 from original**797 First, determine the total number of eggs Janet's ducks lay each day, which is 16.  
798 Next, calculate the number of eggs Janet uses for breakfast and baking muffins. She eats 3 eggs  
799 for breakfast and uses 4 eggs for baking, totaling 7 eggs.  
800 Subtract the used eggs from the total to find out how many eggs she has left to sell:  $16 - 7 = 9$   
801 eggs.  
802 Finally, multiply the number of eggs she sells by the price per egg to find out how much money  
803 she makes daily: 9 eggs \* \$2 per egg = \$18 ...804  
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806807 **Sample question 2**808 Raymond and Samantha are cousins.  
809 Raymond was born 6 years before Samantha.

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Raymond had a son at the age of 23.  
 If Samantha is now 31, how many years ago was Raymond's son born?

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### Sample response 2 from our attack

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Okay, so I'm trying to figure out this problem about Raymond and Samantha ...  
 Raymond and Samantha are cousins. Raymond was born 6 years before Samantha. Raymond had a son at the age of 23 ...  
 Alright, so Raymond was born 6 years before Samantha ...  
 Wait, no, that's not right. If Raymond was born 6 years before Samantha ...  
 Yeah, that makes sense because if you subtract 6 years from Samantha's age ...  
 So,  $31 - 6 = 25$ ?  
 Wait, no, that's the opposite ...  
 Raymond had a son at the age of 23.  
 So, Raymond was 23 when his son was born.  
 Now, Raymond is 37, so the time between Raymond having his son and now is  $37 - 23 = 14$  years.  
 So, the son was born 14 years ago.  
 Wait, but let me double-check that. If Raymond was 23 when his son was born, and he is now 37, then  $37 - 23 = 14$  years have passed since the son was born.  
 So, the son is now 14 years old, which means he was born 14 years ago. That seems right.  
 ...  
 </think>... \*\*Answer:\*\* Raymond's son was born 14 years ago.

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### Sample response 2 from original

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First, I need to determine Samantha's age when Raymond's son was born.  
 Since Samantha is currently 31 years old, I'll subtract 6 years from her current age to find out how old she was when Raymond was born.  
 This gives me 25 years old.  
 Next, I'll figure out how long ago Raymond's son was born.  
 Raymond had his son at the age of 23.  
 To find out how many years ago this happened, I'll subtract 23 from Samantha's age at that time.  
 So, 25 minus 23 equals 2 years ago.  
 Therefore, Raymond's son was born 2 years ago.  
 </think>... Final Answer:  
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### C.3 DSPY

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	Mean
Raw	805
CoT	717
CoT+DSPY	1247

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### DSPY-optimized prompt

Provide a detailed breakdown of the problem or topic at hand, considering every aspect and nuance. Start from an introductory overview, followed by dissecting the components logically, integrating examples, addressing possible counterarguments or misconceptions, and uniformly

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elaborating on each point with explanatory details. Prioritize presenting a thorough, analytical approach that can include speculative insights, hypothetical scenarios, or alternative viewpoints, without rushing to conclusions. Aim to showcase a clear conceptualization followed by logical reasoning, actively prompting self-reflection on the implications of your insights.

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### Sample output from DSPy-optimized prompt

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Okay, so I need to figure out how much money Janet makes every day from selling her duck eggs at the farmers' market. Let me start by breaking down the problem step by step.

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First, Janet's ducks lay 16 eggs per day. That's the total number of eggs she gets each day. Now, she has some daily expenses and uses related to these eggs. She eats three eggs for breakfast every morning. So that's 3 eggs used for breakfast. Then, she bakes muffins for her friends every day, using four eggs each time. **Wait**, does she bake muffins once a day using four eggs, or does she bake them multiple times? The problem says "bakes muffins for her friends every day with four," which is a bit ambiguous. I think it probably means she uses four eggs per day for baking muffins. So that's another four eggs.

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So, adding up her daily egg usage: 3 eggs for breakfast plus 4 eggs for muffins equals 7 eggs used each day. Now, she lays 16 eggs, so how many does she have left after using 7? Let me subtract: 16 minus 7 equals 9 eggs remaining. These 9 eggs are sold at the farmers' market, and she sells each for \$2. So, 9 eggs times \$2 per egg would give her \$18 per day.

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**Wait**, let me double-check that. 16 eggs laid minus 7 used equals 9 sold. 9 times 2 is indeed 18.

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## C.4 EXPERIMENTAL SETUPS

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All models in our experiments are downloaded from HuggingFace. DeepSeek-R1-Distill-Llama-8B and DeepSeek-R1-Distill-Qwen-7B are originally licensed under the Apache 2.0 License. The GSM8K and ORCA datasets are under the MIT License. All experiments in the paper were conducted on an A100 (80GB) compute node. Also, we interact with o3-mini via the OpenAI API, and with DeepSeek-R1 and QWQ-32B via the Baidu Cloud API, to simulate real-world deployment conditions.

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## C.5 TARGET OUTPUT CONSTRUCTION

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Setup	Reason	Answer	Full	Latency	Energy	Accuracy
Raw	1695	190	1885	50.9	12120	80%
CoT	1060	<b>224</b>	1283	34.0	7719	80%
CoT + DSPy	<b>1914</b>	160	<b>2074</b>	<b>54.9</b>	<b>12827</b>	<b>92%</b>

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Table 9: Different target constructions on LLaMA under greedy decoding.

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Setup	Reason	Answer	Full	Latency	Energy	Accuracy
Raw	1396	223	1619	206.8	<b>20252</b>	82%
CoT	1034	<b>250</b>	1283	150.2	15685	79%
CoT + DSPy	<b>1501</b>	216	<b>1718</b>	<b>209.9</b>	19491	<b>87%</b>

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Table 10: Different target construction strategies on LLaMA under sampling decoding.

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We evaluate several strategies for constructing target outputs to guide adversarial optimization, as summarized in Table 9 and 10. The comparison includes a raw baseline (no additional prompt), a standard CoT prompt, and a DSPy-optimized CoT prompt. Interestingly, we find that the standard CoT prompt does not consistently produce longer reasoning sequences; in some cases, it even results in shorter outputs than raw prompting, highlighting its limitations in eliciting extended reasoning.

In contrast, DSPy-optimized CoT prompts increase the average output length from 1,283 to 2,074 tokens under greedy decoding compared to CoT prompts, with corresponding increases in both energy consumption and task accuracy. These results highlight the critical role of target output quality in guiding adversarial optimization. Longer reasoning sequences, especially those produced via DSPy, serve as more effective targets for inducing excessive computation. This reinforces the importance of target construction in maximizing the efficacy of our attack.

## C.6 ADDITIONAL RESULTS

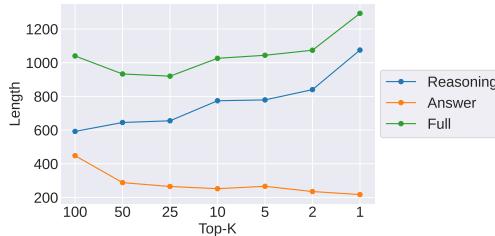


Figure 4: Impact of varying the top-K most informative tokens on LLaMA under sampling decoding.

Setup	Reason	Answer	Full	Latency	Energy	Accuracy
$\mathcal{L}_{PCE}$	1104	218	1322	143.9	19810	86%
$\mathcal{L}_{PCE} + \mathcal{L}_{ER}$	1095	205	1301	124.9	14879	87%
$\mathcal{L}_{PCE} + \mathcal{L}_{DT}$	1184	<b>223</b>	1407	145.3	17731	88%
$\mathcal{L}_{PCE} + \mathcal{L}_{ER} + \mathcal{L}_{DT}$	<b>1437</b>	204	<b>1641</b>	<b>197.0</b>	<b>21228</b>	<b>90%</b>

Table 11: Ablation study of loss objectives combinations on LLaMA under sampling decoding.

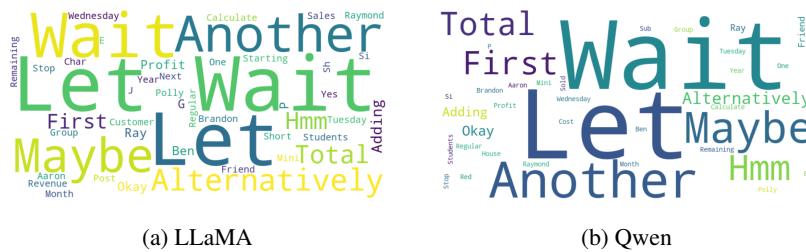


Figure 5: Tokens used for ER Loss. Word clouds generated from the CoT outputs of LLaMA and Qwen on GSM8K.

	Reason	Answer	Full
Original	1070	287	1356
Ours	1495	310	1805

Table 12: Experimental results for ELI5 on Qwen under greedy decoding.