Leveraging Foundation Models to Improve Lightweight Clients in Federated Learning

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Abstract

Federated Learning (FL) is a distributed training paradigm that enables clients 1 2 scattered across the world to cooperatively learn a global model without divulging 3 confidential data. However, FL faces a significant challenge in the form of heterogeneous data distributions among clients, which leads to a reduction in performance 4 and robustness. A recent approach to mitigating the impact of heterogeneous data 5 distributions is through the use of foundation models, which offer better perfor-6 mance at the cost of larger computational overheads and slower inference speeds. 7 We introduce *foundation model distillation* to assist in the federated training of 8 9 lightweight client models and increase their performance under heterogeneous data settings while keeping inference costs low. Our results show improvement in the 10 global model performance on a balanced testing set, which contains rarely observed 11 samples, even under extreme non-IID client data distributions. We conduct a thor-12 ough evaluation of our framework with different foundation model backbones on 13 CIFAR10, with varying degrees of heterogeneous data distributions ranging from 14 class-specific data partitions across clients to dirichlet data sampling, parameterized 15 by values between 0.01 and 1.0. 16

17 **1 Introduction**

Federated learning (FL) is a decentralized training paradigm in machine learning [McMahan et al., 18 2017] that trains one global model across multiple clients while preserving the privacy of client 19 data. A typical FL framework consists of a central server coordinating global model training by 20 periodically aggregating clients' local models that are trained with locally-stored data. Similar to a 21 variety of distributed learning approaches, one of the major challenges for FL is that locally-stored 22 client data are heterogeneous, which can result from uneven distributions or unbalanced patterns [Li 23 et al., 2020a]. This results in client-drift, commonly-seen accuracy drops, and non-convergence [Zhao 24 et al., 2018, Karimireddy et al., 2020, Hsieh et al., 2020, Li et al., 2020a]. In addition, many FL 25 clients in real-world deployments are edge devices which have strict limitations on inference speeds 26 and compute. This, in turn, restricts clients to using small-scale models for inference. 27

To maintain model performance under heterogeneous data distributions, foundation models [Bom-28 masani et al., 2021] present a potential solution. Their widely known benefits, such as their compre-29 hensive knowledge, transferable representations across a broad range of downstream tasks [Radford 30 et al., 2021, Wang et al., 2022], and strong robustness to distribution shifts [Ma et al., 2021] make 31 them a strong candidate to mitigate the effects of heterogeneous distributions. With this in mind, 32 multiple recent methods explore fine-tuning foundation models under federated settings [Qu et al., 33 2022, Chen et al., 2022a, Guo et al., 2023a, Chen et al., 2022b, Su et al., 2022, Guo et al., 2023b]. 34 Among these, Chen et al. [2022b] have shown that under extreme non-IID conditions, federated 35 fine-tuning of foundation models forces a performance worse than training on local data only. In 36

addition, these methods incur a relatively large increase in inference time and compute by directly
 using foundation models instead of small-scale alternatives like EfficientNet Tan and Le [2019] or

³⁹ MobileNet Sandler et al. [2018] for inference.

In order to effectively leverage the performance of foundation models under non-IID data distri-40 butions while using small-scale backbones for faster inference, we propose an approach to *distill* 41 knowledge from foundation models into the small-scale client models (proxy models). During 42 training, foundation models are not directly fine-tuned, but rather are leveraged to update each client's 43 proxy model; then proxy model updates are shared with and aggregated by the server model. At 44 inference, only the proxy models are used. Thus, the proxy models offer low latency inference while 45 knowledge from the foundation models helps reduce the bias and diversify the knowledge of the 46 proxy models, especially under heterogeneous local data distributions. In addition, our proposed 47 method is agnostic to the number and size of foundation models available to each client. This offers 48 the option of personalization for each client, which can select the appropriate foundation model(s) 49 based on the amount of storage and compute available, as well as local data characteristics; this is 50 particularly beneficial when some clients have much more/less data than others. We use the concept 51 of personalization to highlight important directions for future work. 52

53 Overall, our main contributions are as follows:

- This is the first approach to leverage foundation models in FL via distillation to help improve the performance and robustness achievable in small-scale client models (*e.g.* relative increase of 9.22% for EfficientNetB0, 8.69% for ResNet18 and 24.60% for MobileNetV2).
- Within the space of low latency models, we provide a federated learning solution robust to various heterogeneous client data. Our approach outperforms prior art across a variety of client data distributions, from IID to various parametrized dirichlet distributions and class-specific partitions.
- We explore the impact of leveraging representations from fine-tuned foundation models on local data versus pre-trained foundation models. Our results show that under IID data distributions, an initial step of fine-tuning foundation models offers no benefit over 0-shot foundation models, and significantly hinders accuracy as data heterogeneity increases, suggesting that directly fine-tuning foundation models leads to biased representations.
- Our framework is also the first to allow clients the flexibility in choosing their locally-stored foundation models (personalization) according to the scale of compute and data available.
 We study the impact of variable foundation model backbones and highlight the importance of combining disparate feature representations correctly.

70 2 Related Work

71 Federated Learning with Heterogenous Client Data Federated learning is a distributed machine 72 learning scheme which enables multiple clients to train a shared model while keeping their data private. Typically a central server federates the training procedure by periodically aggregating 73 model updates from clients [McMahan et al., 2017]. Frequently, client data can have non-identical 74 distributions which causes naive aggregation methods to not be able to guarantee global model 75 convergence to a local minimum [Zhao et al., 2018, Li et al., 2020b, Hsieh et al., 2020, Li et al., 76 2020a]. To tackle this challenge, FL-algorithms such as FedProx [Li et al., 2020a] add a proximal 77 term to the local training objective to protect models in each client from over-fitting to the local data 78 distribution; other approaches such as regularization [T Dinh et al., 2020], model mixture [Deng et al., 79 2020, Mansour et al., 2020, Hanzely and Richtárik, 2020], clustering clients [Sattler et al., 2020, Cho 80 et al., 2021], multi-task learning [Smith et al., 2017], and meta-learning [Fallah et al., 2020] have 81 been introduced to stabilize the trained models. In this work, we tackle the issue of heterogeneous 82 data distributions by distilling knowledge from foundation models to proxy models, to help mitigate 83 this issue without the need for additional data. 84

Foundation Models in FL The past few years have witnessed the rapid development of foundation
models with the integration of language [Radford et al., 2018, Devlin et al., 2018, Radford et al.,
2021], vision [Bao et al., 2021], and audio modalities [Tang et al., 2023] across many tasks. In FL,
foundation models have been used to improve the robustness of clients to distribution shifts and
heterogeneous data distributions [Qu et al., 2022] or the overall performance of the system [Chen

et al., 2022b, Guo et al., 2023a, Zhao et al., 2023, Lu et al., 2023, Guo et al., 2023b]. However,
existing works do not fully address the increase in computational overhead nor inference time that
follow the use of foundation models. In addition, even compressed foundation models [Sanh et al.,
2019, Wu et al., 2023] do not fully match the latency requirements of clients, which hinders their
deployment in real-world settings. Therefore, we propose the use of small-scale proxy models and
distillation to leverage the performance of foundation models while keeping inference costs low.

Distillation Knowledge distillation is a teaching technique that transfers valuable insights and 96 generalization capabilities from a trained teacher model to a student model [Hinton et al., 2015, 97 Anil et al., 2018, Zhang et al., 2018, 2021]. Within the domain of FL, Lin et al. [2020] explore 98 adaptable aggregation methods with ensemble distillation at the server, while Sattler et al. [2021] 99 use an auxiliary dataset to weight and ensemble local models from each client. FedDistill [Seo 100 et al., 2022] extracts statistics related to the logit-vector from different client models and shares them 101 with the remaining clients to help with distillation. Zhu et al. [2021] present a data-free knowledge 102 distillation approach by training a generative model at the server, using information from clients. 103 They proceed to use the generative model to create synthetic data which is used to train client models. 104 Cho et al. [2021] propose a co-distillation-based personalized FL method to allow cross-architecture 105 training. In our approach, we study the impact of knowledge distillation Hinton et al. [2015] on 106 the performance of small-scale client models without the use of excessive data, augmentations or 107 model sharing so as to maintain privacy. We hope to provide guidance with respect to how foundation 108 models can be effectively used in FL. 109

110 3 Distilling Foundation Models in Federated Learning

111 3.1 Federate Learning: Setup

Our core FL scheme follows FedAvg [McMahan et al., 2017], which consists of a central server and multiple clients, indexed as i = 1, 2, ..., N. Each client-*i* has its local private dataset \mathcal{D}_i . We denote the local loss function of interest for the *i*-th client as $\mathcal{L}(D_i; \theta)$, where $\theta \in \mathbb{R}^d$ are the parameters of the trainable client model. The overall optimization problem considered at the server is denoted as,

$$\min_{\theta \in \mathbb{R}^d} \mathcal{L}(\theta) := \sum_{i=1}^N p_i \mathcal{L}(D_i; \theta).$$
(1)

Here, p_i is a re-weighting factor conditioned as $p_i \ge 0$ and $\sum_i p_i = 1$. Typically, p_i is assigned as $p_i = \frac{|\mathcal{D}_i|}{\sum_{j \in \mathcal{S}_t} |\mathcal{D}_j|}$ where S_t denotes the set of clients communicating with the server at round t. With this setup in mind, the FL framework repeats the following steps until a desired end condition is achieved: 1) The server broadcasts the current global model to selected clients; 2) Each client resets its local model with the received model, performs local training based on its data, and sends the updated weights/gradients to the server; 3) The central server updates the global model by aggregating the received weights/gradients.

123 **3.2 Fed-LPFM**

Setup Unique to our framework, we consider the scenario where each client has access to local 124 pre-trained foundation models. Similar to each client's training dataset, these foundation models 125 are only accessible by the client and not other entities in FL. We assume that in the FL system each 126 client contains two sets of local models: (a) a set M_i of pre-trained foundation models (private): 127 $\mathcal{M}_i^1, \mathcal{M}_i^2, \dots, \mathcal{M}_i^{M_i}$, and (b) one trainable small-scale proxy model parameterized by θ_i . Since the foundation models are private, only the proxy models are circulated among the clients and server 128 129 to facilitate the exchange of knowledge across the system. Our goal is to minimize the objective in 130 Eq. 1, where the θ to be optimized represents the parameters of the small-scale proxy model while 131 the foundation models are left unmodified. 132

Local Training In our algorithm, the client uses its locally stored data along with the knowledge from its private foundation models to supervise local training. For this purpose we use the following loss function,

$$\mathcal{L}(D_i;\theta) = \lambda \mathcal{L}_{CE}(D_i;\theta) + (1-\lambda)\mathcal{L}_{Distill}(D_i;\theta,\mathcal{M}_i^1,\dots,\mathcal{M}_i^{M_i}).$$
(2)

Algorithm 1 Fed-LPFM

- 1: Input: Dataset \mathcal{D}_i , frozen and private pre-trained foundation models: $\mathcal{M}_i^1, \mathcal{M}_i^2, \ldots, \mathcal{M}_i^{M_i}$ and proxy model θ_0 for each client $i \in [N]$.
- 2: 3: Server:

4: for Round $t = 0, 1, 2, \dots, T - 1$ do Send θ_t to connected clients $\mathcal{S}_t \subset [N]$. Let $P_t = \sum_{i \in \mathcal{S}_t} |\mathcal{D}_i|$. 5: for Client $i \in S_t$ in parallel **do** 6: 7: $\theta_t^i \leftarrow \text{LocalUpdate}(\theta_t, i)$ Send the updated model θ_t^i to the central server 8: 9: end for Server-end aggregation: $\theta_{t+1} = \sum_{i \in S_t} \frac{|D^i|}{P_t} \theta_t^i$ 10: 11: end for 12: return: θ_T 13: 14: LocalUpdate(θ_t , i) 15: $\theta_t^i = \theta_t$ 16: for epoch $q = 0, 1, \ldots, Q - 1$: $\theta_{t,q+1}^i = \theta_{t,q}^i - \eta \tilde{\nabla} \mathcal{L}(\theta_{t,q}^i; \mathcal{M}_1^i, \ldots, \mathcal{M}_{M_i}^i; \mathcal{D}_i)$ 17: **return:** $\theta_t^i = \theta_{t,Q}^i$

¹³⁶ Here, the first term is the local cross entropy loss, denoted as

$$\mathcal{L}_{CE}(D_i;\theta) = \mathbb{E}_{(x,y)\sim\mathcal{D}_i}\ell_{CE}(h(x;\theta),y),\tag{3}$$

where $h(\cdot)$ denotes the outcome of a forward pass through the proxy model. The second term $\mathcal{L}_{Distill}$

is used to distill the knowledge between the proxy model and the pre-trained foundation models.

Typically, the Kullback Leibler (KL) Divergence loss is used for this purpose.

$$\mathcal{L}_{Distill}(D_i;\theta,\mathcal{M}_i^1,\ldots,\mathcal{M}_i^{M_i}) = \sum_{m=1}^{M_i} \mathbb{E}_{(x,y)\sim\mathcal{D}_i}\ell_{KL}[h(x;\theta)||\mathcal{M}_i^m(x)]$$
(4)

The parameter λ controls the proportion of knowledge distilled from foundation model in comparison to ground-truth labels.

142 Aggregation scheme After local training, the server synchronizes with the available clients and 143 aggregates the locally updated proxy models. The local models are aggregated with the following 144 re-weighting scheme,

$$\theta_{t+1} = \sum_{i \in S_t} \frac{|D_i|}{\sum_{j \in S_t} |\mathcal{D}_j|} \theta_t^i,\tag{5}$$

where t denotes the communication round. After the aggregation is complete, the server broadcasts the updated model to clients and the entire process is repeated until a desired end condition is met.

147 Algorithm 1 provides a step-by-step explanation of our FL scheme.

148 **4** Experiments

149 4.1 Experiments Setup

Data Settings We evaluate our algorithm on the CIFAR-10 dataset with 10 clients across seven data partitions at various levels of heterogeneity, including both IID and non-IID. For the non-IID data partitions we use (1) Dirichlet distribution, denoted as $Dir(\alpha)$ with $\alpha = 1.0, 0.5, 0.1, 0.05, 0.01$; (2) Class Split, where each client's data is sampled from 2 of the 10 classes. We evaluate all algorithms over the balanced CIFAR-10 test set and report average accuracy over three trials to mitigate randomness of the runs.

Network Architectures For the choice of foundation models, we employ CLIP Radford et al.
 [2021] with backbones ViT-Base/32 (default) and RN50, while we use MobileNet-v2, EfficientNetB0,
 and ResNet18 as our proxy models. In each of the proxy models, we replace the batch normalization
 layers with group normalization (8 groups) and train it from random initialization.



Figure 1: Performance comparisons against existing works across a variety of data settings and proxy model backbones. Fed-LPFM consistently outperforms prior art, by a large margin, under extremely heterogeneous data distributions. Larger area covered indicates a stronger FL approach.

Training Setup and Hyper-parameters Throughout all algorithms and experiments, we use an SGD optimizer for training. We train the proxy models for 600 epochs using a learning rate of 0.01, weight decay of 5e-4, and a step learning rate scheduler with a scale factor of 0.1 at epoch 200. In ablation studies where we additionally consider directly fine-tuning foundation models, we train for 200 epochs with a learning rate of 2e-3, weight decay of 5e-4, and a cosine learning rate scheduler with 1 epoch of warmup. For comparisons against the SOTA algorithms we train the proxy models up to 500 epochs in FedAvg and FedProx, and 600 epochs in FML.

167 4.2 Main results

SOTA Algorithm Comparison We compare our approach against FedAvg [McMahan et al., 2017], 168 FedProx [Li et al., 2020b], and FML [Shen et al., 2020], under multiple data heterogeneity partitions. 169 We visualize our results in Fig. 1, where each data partition is represented as a vertex on the polar 170 plot and accuracy is plotted along the radius. From Fig. 1, we observe that Fed-LPFM robustly 171 outperforms prior work across a variety of data distributions. In particular, our algorithm improves 172 over FedProx (the best among prior art) by a wide margin, especially under the most extreme 173 heterogeneous distributions (class split and dirichlet sampling with $\alpha = 0.01, 0.05$). In addition, we 174 highlight that using MobileNet as the backbone for both the private and proxy models, mimicing the 175 setup in FML, performs poorly. We hypothesize that fine-tuning on the local data begins to bias the 176 177 representations learned across both models, thus lending to significantly worsening performances as the data heterogeneity increases. 178

Proxy Model To establish the applicability of our approach to a variety of proxy model backbones, we evaluate across EfficienetNetB0, ResNet18, and MobileNetV2. We report and visualize the results in Figs. 1b and 1c. We observe that our approach outperforms FedAvg and FedProx across the entire selection of proxy models under various data heterogeneity settings, especially the severe non-IID cases. In addition, we also observe that the improvement in performance from FedProx diminishes across both ResNet and EfficienNet, when compared to MobileNet. FedAvg and FedProx perform similar to one another.

Fine-Tuned vs. 0-shot Our Fed-LPFM method uses pre-trained foundation models with no 186 available fine-tuning. To explore the impact of prior knowledge and how it affects distillation, we 187 compare our 0-shot approach with first fine-tuning each client's foundation model(s) on local data 188 (linear probing and prompt tuning). Fig. 2a illustrates how the 0-shot CLIP case outperforms the 189 fine-tuned CLIP models. Our conjecture of this behavior is that *fine-tuning the foundation model on* 190 local data results in a more personalized and biased knowledge representation which decreases the 191 *performance on a balanced test set.* In addition, the more the data distribution is heterogeneous, the 192 more knowledge encoded locally is personalized and biased. However, under more homogeneous 193 settings there is a significant boost in the performance of clients when leveraging knowledge from 194 both 0-shot and fine-tuned foundation models. We believe that the improvement shown when distilling 195 from 0-shot models is largely due to the impact of strong diversity in its feature embeddings when 196



Figure 2: (2a) Fine-tuning foundation models on local data forces significantly worse performances under non-IID conditions. (2b) Maintaining consistent foundation model backbones improves the synergy in information shared across clients. (Bottom) When compared to fine-tuned models, 0-shot models offer more diverse feature embeddings that reduce the bias of proxy models towards local data distributions.

compared to fine-tuned foundation models. We use tSNE plots to observe the spread of the encoded
knowledge representations from foundation models. From Fig. 2, we can see that features from

199 O-shot foundation models cover a wider area when compared to fine-tuned models.

Personalizing Foundation Models By keeping foundation model(s) private, Fed-LPFM allows 200 each client to personalize them. From Fig. 2b, we see that maintaining consistent backbones across the 201 foundation models yields the highest improvement in performances while having a random sampling 202 of backbones, between ViT-B/32 and RN50, forces a drop in performance. We believe this behavior 203 stems from following a naive strategy in combining the information presented by multiple proxy 204 models. The root of this behavior can be attributed to differences in knowledge/understanding of 205 foundation models with disparate backbones. Instead, utilizing our approach along with personalized 206 FL ([T Dinh et al., 2020, Fallah et al., 2020, Li et al., 2021, Ghosh et al., 2020, Cho et al., 2021], etc.) 207 could potentially boost the overall performance. 208

209 5 Conclusions

Overall, we establish Fed-LPFM as an approach to leverage foundation models and help improve 210 the performance and robustness achievable in small-scale models under the FL setting. Distillation 211 from pre-trained foundation models, as opposed to fine-tuned foundation models, provides the 212 diversity in feature representations required to reduce the bias towards local distributions and thus, 213 improve performance of clients across a variety of heterogeneous data distributions. The use of 214 logit-level distillation allows clients the flexibility to choose their local foundation models according 215 to their individual constraints. In doing so, we establish an important direction of future work; 216 find an approach that, in a synergistic way, combines the information from disparate knowledge 217 representations towards improved model performance. 218

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340 A Appendix

The experimental results used to plot Figures in the main paper are shown in tabular form below. Our algorithm (i.e., Fed-LPFM) consistently outperform other algorithms. We observed that Fed-LPFMshows the largest improvement in the class split and Dirichlet distribution ($\alpha = 0.01$ and 0.05), which are the most heterogeneous data distributions among different clients. For example, in the class split, Fed-LPFM has a 21.6% increase compared with Fedavg (82.29% vs 67.67%).

Data Settings	FedAvg	FedProx	FML	Fed-LPFM (MobileNetV2)
Class Split	67.67 ± 1.88	65.97 ± 5.07	19.29 ± 0.28	82.29 ± 1.12
Dir(0.01)	58.49 ± 15.72	69.92 ± 2.07	17.50 ± 1.22	72.88 ± 9.11
Dir(0.05)	80.48 ± 1.07	80.48 ± 1.07	24.75 ± 3.15	84.05 ± 0.99
Dir(0.1)	84.78 ± 1.65	84.78 ± 1.65	33.13 ± 2.58	87.73 ± 1.48
Dir(0.5)	90.05 ± 0.21	90.05 ± 0.21	60.77 ± 3.98	91.72 ± 0.31
Dir(1.0)	90.86 ± 0.13	90.86 ± 0.13	72.84 ± 1.56	92.87 ± 0.17
IID	91.48 ± 0.31	91.61 ± 0.34	86.49 ± 0.17	93.26 ± 0.17

Table 1: The values of Figure 1(a) are shown in the current table.

- ³⁴⁶ Under different proxy model backbones, similar results can be observed. For both EfficientNet and
- ResNet case, we observed that Fed-LPFM outperforms other methods cross all data heterogeneity settings.

Data Settings	FedAvg	FedProx	Fed-LPFM (EfficientNetB0)
Class Split	69.81 ± 2.64	69.81 ± 2.64	78.70 ± 2.28
Dir(0.01)	69.56 ± 2.20	69.56 ± 2.20	75.98 ± 1.29
Dir(0.05)	79.53 ± 0.95	79.53 ± 0.95	83.12 ± 0.76
Dir(0.1)	83.67 ± 1.23	83.67 ± 1.23	87.24 ± 1.46
Dir(0.5)	90.21 ± 0.08	90.21 ± 0.08	91.80 ± 0.30
Dir(1.0)	91.41 ± 0.35	91.41 ± 0.35	92.17 ± 0.09
IID	92.22 ± 0.17	92.22 ± 0.17	92.84 ± 0.04

Table 2: The values of Figure 1(b) are shown in the current table.

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Data Settings	FedAvg	FedProx	Fed-LPFM(ResNet18)
Class Split	67.56 ± 4.66	65.99 ± 6.41	82.50 ± 2.00
Dir(0.01)	73.06 ± 2.10	72.13 ± 1.38	79.41 ± 0.95
Dir(0.05)	82.22 ± 0.79	82.40 ± 0.46	86.42 ± 1.33
Dir(0.1)	85.74 ± 1.38	85.23 ± 0.89	88.59 ± 1.54
Dir(0.5)	90.41 ± 0.30	90.095 ± 0.54	93.30 ± 0.10
Dir(1.0)	91.13 ± 0.13	90.82 ± 0.25	93.92 ± 0.14
IID	91.94 ± 0.22	91.45 ± 0.17	94.00 ± 0.20

Table 3: The values of Figure 1(c) are shown in the current table.

As supporting materials for Fig. 2a, we report the numerical results for testing fine-tuned CLIP (linear probing and prompt tuning) and zero-shot CLIP cross different data heterogeneity levels. We observed that zero-shot CLIP offers best and more robust performances when compared to fine-tuned methods.

As supporting materials for Fig. 2b, we report the results of using CLIP: ResNet50 and CLIP: ViT-

B/32 as well as random sampling of them, with uniform prior, as foundation models. It shows that

random selection of pre-trained models offers worst performances when compared to the other two.

Data Settings	Linear Probing	Prompt Tuning	0-shot (Ours)
Class Split	45.63 ± 9.48	51.85 ± 4.58	82.29 ± 1.12
Dir(0.01)	44.76 ± 3.56	35.86 ± 6.03	$\textbf{72.88} \pm \textbf{9.11}$
Dir(0.05)	73.07 ± 0.86	68.39 ± 1.65	84.05 ± 0.99
Dir(0.1)	82.54 ± 3.21	77.35 ± 3.75	87.73 ± 1.48
Dir(0.5)	91.08 ± 0.24	89.01 ± 0.12	91.72 ± 0.31
Dir(1.0)	92.53 ± 0.48	90.32 ± 0.33	92.87 ± 0.17
IID	92.56 ± 0.17	91.85 ± 0.23	93.26 ± 0.17

Table 4: The values of Figure 2(a) are shown in the current table

Data Settings	CLIP: RN50	CLIP: ViT-B/32	Random Selection
Class Split	80.46 ± 4.08	82.29 ± 1.12	62.75 ± 3.24
Dir(0.01)	66.17 ± 1.19	72.88 ± 9.11	64.02 ± 3.52
Dir(0.05)	84.42 ± 0.41	84.05 ± 0.99	71.33 ± 1.52
Dir(0.1)	$ 87.90 \pm 1.58 $	87.73 ± 1.48	76.05 ± 3.53
Dir(0.5)	92.04 ± 0.25	91.72 ± 0.31	84.82 ± 0.45
Dir(1.0)	$\textbf{93.00} \pm \textbf{0.10}$	92.87 ± 0.17	83.99 ± 0.99
IID	$\textbf{93.63} \pm \textbf{0.30}$	93.26 ± 0.17	85.01 ± 0.47

Table 5: The values of Figure 2(b) are shown in the current table.