# SEMI-AUTOREGRESSIVE DECODING FOR EFFICIENT LLM INFERENCE

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#### ABSTRACT

Inference in large language models (LLMs) is often slow due to their autoregressive nature. In this work, we formulate a semi-autoregressive decoding paradigm for LLMs that delegates part of the expensive computation from the original large model to a smaller, more efficient autoregressive model. The core of our design lies in the separate modeling of token dependencies, where the large model handles long-term dependencies on distant tokens, while the smaller model addresses short-term dependencies on recent tokens. When employed as a draft model in speculative decoding, our method allows for substantial reuse of computation in the LLM without missing any token dependencies, thereby striking a good balance between draft quality and drafting speed. Experiments on text summarization, medical QA, code generation, and mathematical reasoning tasks demonstrates the efficacy of our method.

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#### 1 INTRODUCTION

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027Large Language Models (LLMs) have demonstrated remarkable capabilities across diverse natural028language processing tasks (OpenAI, 2024; Dubey et al., 2024). However, their deployment in real-029world applications is often hindered by the substantial inference latency. The autoregressive nature030of LLMs exacerbates this issue, as generating n tokens requires n sequential passes through the031model, each of which involves expensive computation of stacked attention layers (Vaswani, 2017).

To address the latency challenges, several approaches (Ding et al., 2024; Jiang et al., 2024; Leviathan 033 et al., 2023) have been introduced to improve LLM inference efficiency by delegating parts of the 034 computation to smaller models. Among these innovations, speculative decoding (Leviathan et al., 2023) has emerged as a particularly promising technique. This method leverages the observation that 035 certain tokens within the same inference run are easier to predict and can be handled by a smaller 036 model. Speculative decoding employs a smaller draft model to generate draft tokens, which are then 037 verified and refined by the larger target model. Compared to other approaches, speculative decoding offers a distinct advantage by guaranteeing generation quality, as it always falls back to the target model if necessary. Since its introduction, speculative decoding has proven effective across a wide 040 range of generation tasks and has become a widely adopted tool for efficient LLM inference. 041

The acceleration achieved by speculative decoding, however, hinges on two factors: (i) the *accep*-042 tance rate of the draft tokens, as well as (ii) the latency of the draft model itself. As such, a key in-043 gredient in speculative decoding has been the design of the draft model. Existing work has explored 044 several designs of the draft model, including the use of a separate transformer model (Leviathan 045 et al., 2023; Chen et al., 2023; Kim et al., 2024), training additional modules to predict multiple 046 tokens simultaneously (Cai et al., 2024; Luk et al., 2024; Bhendawade et al., 2024), or leveraging 047 selected layers of the target model itself as the draft model (Elhoushi et al., 2024; Bae et al., 2023; 048 Zhang et al., 2024b). Despite reported successes, these designs often involve a trade-off between acceptance rate and latency: some designs achieve a high acceptance rate but with compromises on latency (Elhoushi et al., 2024; Bae et al., 2023; Zhang et al., 2024b; Leviathan et al., 2023), whereas 051 others may offer low latency but at the expense of draft quality (Cai et al., 2024; Luk et al., 2024; Bhendawade et al., 2024; Fu et al., 2024; Gloeckle et al., 2024). The reason for this trade-off stems 052 from the fact that proposing good draft tokens requires the draft model to be complex enough to competently process token dependencies, which in turn leads to considerable drafting latency.



• Focusing on downstream LLM applications (realized via fine-tuning after model pretraining), we validate our method across four text generation tasks with three models in two training modes, demonstrating its advantages in terms of acceleration, memory cost, and training convenience.

#### 2 PRELIMINARIES

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#### 2.1 LARGE LANGUAGE MODEL

A large language model assigns a probability  $p(\mathbf{w})$  to a sequence of words  $\mathbf{w} = (w_1, ..., w_T)$ . This joint probability is usually factorized using the chain rule:

$$p(\mathbf{w}) = \prod_{i=1}^{T} p(w_i | w_1, ..., w_{i-1})$$
(1)

which reduces language modeling to the problem of estimating the conditional probability of the next word given the history of all preceding words, hence *autoregressive*. This autoregressive property imposes a sequential constraint on the decoding process, requiring n sequential passes through the model to generate n tokens, which limits the speed of generation.

#### 2.2 Speculative decoding

To accelerate inference in autoregressive language models, *speculative decoding* (Leviathan et al., 2023) leverages a more efficient approximation model, i.e. the draft model  $M_q$ , to generate K draft tokens  $\{d_1, ..., d_K\}$  from an approximate distribution  $q(\mathbf{w}) \approx p(\mathbf{w})$ . The larger target model  $M_p$  is then used to validate or override the draft tokens.

103 Specifically, a draft token  $w_i \sim q(w_i|w_{< i})$  is accepted if q provides a sufficiently close approx-104 imation to the target distribution p. In this work, we enforce a greedy acceptance criterion: the 105 draft token is accepted if  $w_i = \arg \max_v p(v|w_{< i})$ . Otherwise, the draft token is rejected, and the 106 larger model overrides the draft by generating a new token from  $w_i \sim p(w_i|w_{< i})$ . If a draft token 107 is rejected, all subsequent draft tokens are also discarded, and the generation process reverts to the 108 newest token generated by  $M_p$ .



Figure 2: The graphical models of different draft model designs. *Non-dashed nodes*: tokens already generated and verified by the LLM. *Dashed nodes*: draft tokens to be generated by the draft model.

This process speeds up inference by exploiting parallelism in the draft token verification stage while retaining accuracy by falling back to the target model. Hence, the acceleration depends on the acceptance rate  $\beta$ , i.e. the probability of accepting  $d_i$ , as well as the latency of the draft model.

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#### 3 A UNIFIED FRAMEWORK FOR DRAFT MODEL

In this section, we present a unified view incorporating various draft model designs in speculative decoding as special cases, focusing on the different considerations for token dependency modeling. In the following, we use q to denote the output distribution of draft model  $M_q$ ,  $h_p(\cdot)$  and  $h_q(\cdot)$  to represent the hidden states of the last layer of the target model  $M_p$  and the draft model  $M_q$  computed for the input tokens, respectively.

**Drafting as sampling from** q. Consider a draft model  $M_q$  in speculative decoding. Drafting the next *K* tokens  $\mathbf{d} = \{d_1, ..., d_K\} \in \mathbb{N}^K$  can be seen as sampling from its output distribution q conditioned on previously accepted tokens  $\mathbf{w}_{<i}$ :

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$$\mathbf{d} \sim q(d_1, \dots d_K | \mathbf{w}_{\leq i}) = \prod_{j=1}^K q_j(d_j | \mathbf{d}_{< j}, \mathbf{w}_{\leq i})$$
(2)

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To improve decoding efficiency, we usually consider three desirable properties when designing  $M_q$ : (i) high acceptance rate: distribution q should well approximate the target distribution p of the LLM; and (ii) fast drafting: sampling from q should be faster than sampling from p; (iii) q is a *low-dimensional* distribution, meaning that K is small. The last property is important in our design.

One way to meet the aforementioned requirements is to focus on a powerful yet computationally cheap mechanism for modeling dependencies among the tokens  $\mathbf{d}_{< j}, \mathbf{w}_{\leq i}$ . Specifically, there are two distinct types of dependencies: (i) the dependencies on *distant tokens*  $\mathbf{w}_{\leq i}$ , i.e., the tokens already accepted and verified by p; and (ii) the dependencies on *recent tokens*  $\mathbf{d}_{< j}$ , i.e., the draft tokens sampled from q. In fact, many previous works can be categorized by how they handle these dependencies. For example:

Block autoregressive model (Cai et al., 2024; Luk et al., 2024; Gloeckle et al., 2024) focuses on maximizing fast drafting by ignoring the dependencies of recent tokens and parallelizing draft token inference. In this case, the draft tokens dk and dl are conditionally independent given w≤i, i.e., dk ⊥ dl|w<i (Fig. 2a), leading to:</li>

$$q_j(d_j|\mathbf{d}_{< j}, \mathbf{w}_{\le i}) = q_j(d_j|h_p(\mathbf{w}_{\le i}))$$
(3)

where each  $q_j(\cdot)$  is a different LM head implemented as an independent multilayer perceptron (MLP) and  $h_p(\cdot)$  represents the hidden states of the last layer of the target model.

Pruned autoregressive model (Elhoushi et al., 2024; Zhang et al., 2024b) aims to achieve a balance between fast drafting and high acceptance rate. Unlike the *block autoregressive model*, it proposes to model all token dependencies with a pruned version of the target model M<sub>p</sub>, denoted as M<sub>p'</sub> (Fig. 2b):

$$q_j(d_j|\mathbf{d}_{< j}, \mathbf{w}_{\le i}) = q_0(d_j|h_{p'}(\mathbf{d}_{< j}, \mathbf{w}_{\le i}))$$

$$\tag{4}$$

where  $q_0(\cdot)$  is the LM head for the draft model and  $h_{p'}(\cdot)$  is the hidden representation of a 'truncated' LLM, which can be either the first few attention layers of the target model  $M_p$  (Elhoushi et al., 2024) or replacement of full attention with approximate attention (You et al., 2024). This pruned model can capture token dependencies and can be directly accelerated on commodity hardware depending on the type of pruning scheme employed. 162 **Summary.** The above two dependency modeling designs differ in terms of (a) acceptance rate and 163 (b) drafting speed. In particular, *block autoregressive model* ignores the dependencies among *recent* 164 tokens  $d_{\langle j}$ , which enables the reuse of hidden states  $h_p$  to achieve highly efficient parallel decoding. 165 However, this simplification harms the acceptance rate. In contrast, pruned autoregressive model 166 captures all token dependencies through a pruned LLM, aiming to balance fast sampling (through pruning) and high draft quality (through dependency modeling). However, its accuracy is highly 167 dependent on the pruned model. Furthermore, it processes both recent and distant tokens together 168 without distinguishing them, leading to a sub-optimal design. To address these issues, we propose 169 a new design based on the unified view of the draft model. This approach improves the balance 170 between drafting speed and accuracy by separately modeling the two types of token dependencies. 171

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175 4.1 HIGH-LEVEL DESIGN

The core intuition of our proposal is to combine the advantages of the two previous models, i.e., maximizing hidden state re-use while effectively modeling token dependencies. Specifically, we propose to model distant token and recent token dependencies separately, using the target model  $M_p$ for distant tokens, and a tiny language model<sup>1</sup> (TLM)  $M_q$  for recent tokens.

• Distant token dependency. These tokens determine the context and the semantics for drafting subsequent tokens. For these tokens, we process them with the original LLM  $M_p$ , where we reuse the hidden state  $h_p(w_1, ...w_i)$  computed by the LLM. This hidden state represents the LLM's understanding of the text context. Similar to the block autoregressive model, this context representation only needs to be computed once and is reused throughout the drafting process.

• Recent token dependency. These tokens correspond to the K-gram generated by the draft model. To reduce the cost, we use a small model to compute the hidden states  $h_q(d_1, ..., d_{j-1})$ . These hidden states encode the local status of the draft. Since K is relatively small, a very simple model for  $M_q$  suffices, which we refer to as a TLM.

By combining these two design choices, we can model recent token dependencies, as opposed to 191 the block autoregressive model, while incurring small or negligible additional computation cost 192 compared to the pruned autoregressive model, through the use of a TLM. This approach unifies the 193 strengths of LLMs and TLMs for draft generation. While LLMs are powerful in understanding text 194 semantics, they are known to be expensive to run. We thereby use them sparingly, calling them only 195 when the context of the text is likely to have changed. In contrast, TLMs are much cheaper to run, 196 though they struggle to parse complex semantics. We thereby only use them to handle short phrases 197 and K-grams, conditioned on the semantic understanding provided by the LLM. In this way, we 198 achieve both high efficiency and good draft quality.

This design leads to what we call the *semi-autoregressive draft model* (see Fig. 2c), which is formally defined as follow:

202 Definition 1. (Semi-autoregressive draft model). Let  $\mathbf{d} = \{d_1, ..., d_K\}$  be the draft tokens and 203  $\mathbf{w}_{\leq i} = \{w_1, ..., w_i\}$  be the tokens generated and already verified by  $M_p$ . A semi-autoregressive 204 draft model is a probabilistic model defined by the following probabilistic distribution:

$$q(\mathbf{d}|\mathbf{w}_{\leq i}) = \prod_{j=1}^{K} q_0(d_j|h_p(\mathbf{w}_{\leq i}), h_q(\mathbf{d}_{< j}))$$
(5)

where  $h_p(\cdot)$  and  $h_q(\cdot)$  are the hidden states of an LLM and that of a TLM, respectively.

**Inference.** As discussed, sampling from the above model is highly efficient: while the computation of  $h_p(\mathbf{w}_{\leq i})$  is expensive, it only needs to be computed once and can be reused for all draft tokens. On the other hand,  $h_q(\mathbf{d}_{\leq j})$  must be recomputed for each j, but this is cheap due to the light-weighted nature of  $M_q$ , which normally requires even significantly less computation than a single decoding layer of a transformer.

<sup>&</sup>lt;sup>1</sup>We use the term tiny language models here to highlight that these models are extremely cheap to run.



Figure 3: The architecture of the semi-autoregressive draft model, which separately models distant tokens  $\{w_1, ..., w_i\}$  and recent tokens  $\{d_1, ..., d_K\}$  with the hidden representations of the original LLM  $h_p$  and a tiny language model (TLM)  $h_q$ . Note that  $w_{i+1} = d_1$ . The two models can be learned either jointly or separately using distinct Q-LoRA ranks.

#### 4.2 IMPLEMENTATION

In this section, we discuss the detailed implementations of  $M_q$  and the training procedure of the proposed model. Additional details on tree attention and KV caching can be found in Appendix A.

**Realization of**  $h_q$  and  $q_0$ . We consider the following two implementations of the tiny language model  $M_q$  for processing recent tokens d. Both implementations are motivated by the fact that the number of recent tokens K is small, so we only need to model short-range dependencies. Therefore, simple models are sufficient in this case, making our method significantly cheaper than conventional speculative decoding, which uses more expensive draft models.

• Simplified transformer. The first design is a one-layer transformer with hard-coded attention weights. Specifically, let e(w) be the word embedding of a token w. We implement the network  $h_q(\cdot)$  as follows:

$$h_q(\mathbf{d}_{\leq j}) = \frac{\sum_{l=1}^j \alpha_l \mathbf{MLP}(e(d_l))}{\sum_{l=1}^j \alpha_l}$$
(6)

where  $\boldsymbol{\alpha} = \{\alpha_1, ..., \alpha_K\} \in (0, 1)^K$  are learnable parameters and MLP is a multi-layer perceptron with two hidden layers. While fixed attention weights may be inadequate for processing long context, it exhibits as an effective method for handling short texts (Raganato et al., 2020).

• *Recurrent networks*. The second design involves using an LSTM (Hochreiter, 1997) or even a vanilla RNN (Hochreiter, 1997) to model the local dependencies of the draft tokens<sup>2</sup>:

$$h_q(\mathbf{d}_{\leq j}) = \mathrm{LSTM}(e(d_1), \dots, e(d_j)) \tag{7}$$

The LSTM consists of two hidden layers, and its output is the hidden state of the last draft token. While LSTMs may struggle in long-context modeling due to their fixed-sized hidden state in contrast to transformers, they are well-suited to capture short-term dependencies.

The LM head  $q_0$  is implemented as a simple MLP model with two hidden layers, and its input is the concatenation of  $h_q$  and  $h_p$ . More details about the network architecture are given in Appendix A.

**Training procedure.** We now address the question of how to train the TLM. Focusing on finetuning scenarios, we finetune the original LLM  $M_p$  and learn the semi-autoregressive model  $M_q$  by maximizing the following objective:

$$\mathcal{L}(p,q) = (1-\lambda)\mathbb{E}\Big[\sum_{i=1}^{T} \log p(w_i|w_{< i})\Big] + \lambda\mathbb{E}\Big[\frac{1}{k}\sum_{i=1}^{T-k}\sum_{j=1}^{k} \log q(w_{i+j}|w_{<(i+j)})\Big],$$
(8)

 $q(w_{i+j}|w_{<(i+j)}) = q_0(w_{i+j}|h_p(w_1,...,w_i), h_q(w_{i+1},...,w_{i+j}))$ 

The expectation is taken over the fine-tuned dataset. T is the number of tokens in a sample from the dataset and  $\lambda \in (0, 1)$  is a factor that balances the learning of p and q. Similar to existing literature (Cai et al., 2024), we consider two training setups:

<sup>&</sup>lt;sup>2</sup>When implemented as an RNN, the design is similar to the model proposed in Zhang et al. (2024a).

- Separate training. In this mode, we train p and q in two stages, where we set  $\lambda = 0$  and  $\lambda = 1$  in the respective stages. In each stage, we freeze the parameters of p when training the q, and vice versa. This guarantees that the learning of q will not affect p;
- Joint training. This corresponds to the case where we train p and q in one stage using a single  $\lambda$ . This mode allows us to learn a p whose representation is also useful for predicting more future tokens, which can potentially lead to better draft quality. However, the learning of q may also 'drag' that of p, leading to a potential degradation of p's quality.

We use Q-LoRA (Dettmers et al., 2024) to train p and q, where we assign different ranks to the parameters in p and q: (a) For the parameters  $\theta_p$  in p, which include both the network  $h_p(\cdot)$  and the original LM head, we use a LoRA rank  $r_p$  that is much smaller than the matrix size (e.g.  $r_p = 32$ ); (b) For the parameters  $\theta_q$  in the TLM q, which include both the network  $h_q(\cdot)$  and the new LM head  $q_0$ , we use a LoRA rank  $r_q$  that is relatively larger (e.g.  $r_q = 4096$ ). See Figure 3 for more details.

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#### 5 RELATED WORKS

286 Efficient inference schemes in LLMs (Bai et al., 2024; Xu et al., 2024; Zhou et al., 2024) have 287 received significant attention recently due to the ever-increasing size of such models. Approaches to 288 improving efficiency range from static methods, such as pruning (Men et al., 2024) and quantization 289 (Ashkboos et al., 2024), which reduce overall model size and hence computational requirements, to 290 dynamic methods, such as early-exiting (Schuster et al., 2022; Bae et al., 2023) and hybrid models 291 (Kag et al., 2022; Ding et al., 2022; 2024), which accelerate inference by adjusting the amount of 292 computation based on the (estimated) difficulty of a given token or prompt. Our work is complemen-293 tary to these general efficiency efforts (e.g., our semi-autoregressive scheme can be easily applied on top a quantized model). Note, however, that unlike our work and other speculative decoding 294 frameworks, such classic approaches cannot guarantee that LLM's outputs remain identical. 295

Non-autoregressive decoding (NAR) accelerates inference by eliminating or relaxing the sequential dependencies between tokens (Gu et al., 2018). However, NAR often suffers from reduced
accuracy compared to its autoregressive counterparts. Current efforts to improve performance focus on reintroducing some degree of conditional dependence between tokens, for instance, through
generative flows (Ma et al., 2019) and conditional random fields (Sun et al., 2019). Additional refinements include iterative decoding strategies (Lee et al., 2018; Ghazvininejad et al., 2019), as well
as improvements to training data and loss functions (Ding et al., 2021; Du et al., 2021).

- 303 Speculative Decoding (Leviathan et al., 2023) is a widely used framework for accelerating LLM 304 inference. It employs a (smaller) draft model to propose multiple tokens at once, which are then verified by a (larger) target model. Initially, a separate transformer-based language model was used 305 as the draft model (Leviathan et al., 2023; Chen et al., 2023; Kim et al., 2024). More recent work has 306 shifted toward using (part of) the target model itself for drafting (i.e., self-speculative decoding). For 307 example, Medusa Decoding (Cai et al., 2024; Gloeckle et al., 2024) combines non-autoregressive 308 (NAR) techniques with speculative decoding by training multiple LM heads conditioned on the 309 target model's final layer to generate draft tokens in parallel. Techniques like LayerSkip (Elhoushi 310 et al., 2024) and FREE (Bae et al., 2023) integrate early-exit strategies by drafting with earlier layers 311 and verifying with later layers, while Zhang et al. (2024b) adaptively skips intermediate layers for 312 drafting. Recent works have explored the use of more light-weighted model as draft models, such 313 as a n-gram model (Fu et al., 2024) and a small RNN (Zhang et al., 2024a), as discussed below.
- 314 Light-weighted draft model design. Like our work, concurrent works have also explored taking 315 the draft model as a small autoregressive model conditioned on the hidden states of the original 316 LLM (Ankner et al., 2024; Zhang et al., 2024a; Li et al., 2024; Nair et al., 2024). Among these 317 works, Zhang et al. (2024a) is similar to one of the implementations in our design. Apart from 318 differences in practical implementation details, the major differences to these works are (a) unlike 319 these works which focus on specific implementations, our works focuses on high-level design, which 320 naturally connects different implementations. The disentanglement of specific implementations and 321 high-level design allows us to explore different architecture choices with various trade-offs in drafting efficiency and draft quality; (b) Unlike existing works which primarily focus on learning the 322 draft model on pre-trained dataset e.g. ShareGPT (2023), our work focus on fine-tuning scenarios, 323 where the draft model is trained on specific domain data jointly or separately with the original LLM.

	SQL-context	SAMSUM	GSM8K	ChatDoctor
Domain	code generation	text summarization	math reasoning	medical QA
# examples	$\sim 90 \mathrm{k}$	$\sim 10k$	$\sim 8k$	$\sim 50k$
# draft tokens	4	3	3	4
LLM considered	Phi-3	LLama2-13B	Mistral-7B	Mistral-7B

Table 1: Summary of the tasks considered. A smaller subset of ChatDoctor is used in experiments.

#### EXPERIMENTS 6

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Baselines. We compare the proposed semi-autoregressive method (denoted as 'semi' henceforth) with the following two representative methods in (self-)speculative decoding, both of which can be seen as different implementations of the framework specified in Eq. 2.

- Block autoregressive decoding (block). Widely known as Medusa decoding (Cai et al., 2024), this corresponds to the case where we implement the draft model as Eq. 3, which ignores the dependence between the draft tokens.
- Skip-layer decoding (skip). This corresponds to the case where we implement the draft model as a single transformer model with fewer layers (Elhoushi et al., 2024), as in Eq. 4. Here we use 8 layers, following the setups in Elhoushi et al. (2024).
- Recurrent drafter (redraft). This corresponds to the design in (Zhang et al., 2024a), which can be seen as implementing  $h_q$  in the proposed semi-autoregressive draft model (eq.5) as a RNN.

In addition to the above comparison, we also compare different implementations of the network  $h_a$ in the proposed semi-autoregressive draft model. Some of these implementations are closely related to state-of-the-art methods such as Hydra (Ankner et al., 2024) and EAGLE (Li et al., 2024).

**Evaluation metrics**. We compare different (self-)speculative methods from the following angles:

• Acceleration. This metric is defined as the ratio between the wall time t when decoding a sentence without speculative decoding and the wall time t' when decoding with speculative decoding:

Acceleration := 
$$\frac{t}{t'}$$

- Token acceptance rate. This metric measures how many tokens drafted by the draft model  $M_q$  are accepted by the original LLM  $M_p$ , which directly reflects the quality of the draft model  $M_q$ .
- Extra memory cost. This metric is defined as the ratio between the number of additional parameters  $\theta'$  introduced in a specific design of q and the number of parameters  $\theta$  in the original LLM:

$$\texttt{MemoryCost} \mathrel{\mathop:}= \frac{|\theta'|}{|\theta|} \times 100\%$$

• Generation quality of the target model. Finally, when we compare joint learning and separate learning, we also investigate how different designs of the draft model  $M_q$  will affect the generation quality of the original model. Theoretically, the draft model should have no impact on the original model  $M_p$  in speculative decoding. However, when  $M_p$  and  $M_q$  are trained jointly, the training of  $M_q$  may have an impact on p, as discussed in §4.2. Here, we measure generation quality by the Rouge-L score between models' generation and the ground truth.

Tasks and models. A summary of the tasks and models considered is given in Table 1. Specifically, 372 we use the following datasets: SQL-context (b-mc2, 2023) for SQL code generation based on user 373 queries, SAMSUM (Gliwa et al., 2019) for text summarization, GSM8k that include 8k grade school 374 math questions and answers, and ChatDoctor (Yunxiang et al., 2023) which is a dialogue dataset for 375 conversations between a doctor and a patient. For ChatDoctor, we use a subset of 50k in experiments. 376

Computing resource. Results on SQL-context, SAMSUM, and GSM8K are computed using two 377 A10 GPUs in under a day. Results on ChatDoctor are computed with a single A100 GPU in a day.

	skip	block	semi	redraft		skip	block	semi	redraft
acceleration $(\uparrow)$	$1.94 \times$	3.76  imes	$3.71 \times$	$3.68 \times$	acceleration $(\uparrow)$	$1.32 \times$	$1.71 \times$	$2.02 \times$	2.07  imes
token acc rate $(\uparrow)$	75.1%	73.8%	74.4%	74.6%	token acc rate $(\uparrow)$	45.1%	43.6%	51.2%	52.3%
+memory $(\downarrow)$	4.38%	12.4%	8.51%	9.52%	+memory $(\downarrow)$	2.29%	4.45%	3.09%	3.55%
(a) <b>SQL-context</b>					(b) SAMSUM				
	skip	block	semi	redraft		skip	block	semi	redraft
acceleration $(\uparrow)$	$1.51 \times$	$2.55 \times$	<b>2.63</b> imes	2.57×	acceleration $(\uparrow)$	$1.61 \times$	$1.78 \times$	2.53 imes	$2.51 \times$
token acc rate $(\uparrow)$	57.8%	63.6%	65.4%	64.6%	token acc rate $(\uparrow)$	60.1%	48.3%	62.4%	61.0%
	1.33%	5.12%	2.21%	2.44%	+memory $(\downarrow)$	1.04%	3.18%	1.69%	1.95%
+memory $(\downarrow)$	1.0070	0.1270	<b></b> _1/0	=			0.2070		

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Table 2: The performance of different (self-)speculative decoding algorithms. Skip: the skip-layer decoding method by (Elhoushi et al., 2024). Block: the block autoregressive decoding method by (Cai et al., 2024). This method is also known as Medusa. Semi: the proposed semi-autoregressive decoding method (implemented with a simplified transformer). Redraft: the method in (Zhang et al., 2024a) which implements  $h_q$  as a RNN. Our method offers highest acceleration on the majority of the tasks while requiring a reasonable memory cost. 394

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397 **Training setups.** We employ the same training procedure for all methods, as outlined in §4.2. For joint training, we set  $\lambda$  in the objective function (Eq. 8) to 0.25. This ensures that the learning of 398 p predominates the training process, so as to guarantee the generation quality of the original LLM. 399 Other details such as model architecture and optimizer settings can be found in Appendix B. 400

401 Inference setups. During inference, we enable KV caching but disable tree attention (Cai et al., 402 2024). We disable tree attention (Cai et al., 2024) to focus our evaluation on the quality of the draft 403 model itself, though our method is fully compatible with tree attention.

404 Number of draft tokens. We look ahead 3 - 4 tokens for all speculative decoding methods consid-405 ered, depending on the task. Looking further ahead doesn't result in any acceleration improvement.

406 When presenting the results, we report the results from the simplified transformer design for  $h_a$  (see 407 Eq. 6) in the main table. The LSTM design described in Eq. 7 achieves a similar performance and a 408 comparison between the two implementations is provided in Figure 4. 409

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6.1 MAIN RESULTS

Comparison with other decoding methods. Table 2 compares the proposed semi-autoregressive 413 decoding method with two baseline approaches. Overall, our method consistently achieves the high-414 est acceleration in three out of the four tasks considered, with the exception of the SQL-context 415 dataset, where block decoding marginally outperforms our method. We hypothesize that this is due 416 to the nature of SQL code, where the fixed syntax allows block decoding to be equally effective by 417 ignoring the draft token dependencies. We expand on this further in § 6.2. 418

The superior acceleration observed in the other tasks can be attributed to two factors: (i) the high 419 draft quality of our method, as reflected by its higher acceptance rate comparable to or even exceed-420 ing that of a pruned transformer (as seen in skip-layer decoding); and (ii) its low drafting latency, 421 which is negligible compared to even a single decoding layer in a transformer. A more detailed 422 analysis of execution time is presented in Fig. 4a. These results demonstrate that our method strikes 423 a better balance between draft quality and drafting latency. 424

In terms of memory cost, our method has an advantage over the block decoding method, as it elimi-425 nates the need to maintain multiple language model (LM) heads for the draft model. However, our 426 method is less memory efficient than skip-layer decoding, as it requires additional memory to store 427 the TLM for processing the draft tokens  $d_i$ . This introduces a minor memory overhead. 428

**Comparison among different implementation of**  $h_q$ . To gain further insight into the trade-off be-429 tween draft quality (i.e. the acceptance rate) and inference latency of the draft model, we compare 430 different implementations of  $h_q$  with varying complexity, as shown in Fig. 4. We specifically com-431 pare to the case where  $h_q$  is realized as a standard transformer with varying number of layers. Al-



442 Figure 4: Comparison of different implementations of  $h_q(\cdot)$  on SAMSUM, including Medusa, sim-443 plified transformer, LSTM, and standard transformer (denoted as Transformer) with varying number 444 of layers. In the standard transformer implementation, the zero-layer case corresponds to taking the embedding  $e(d_i)$  of the last token  $d_i$  as the transformer's output, which is similar to Hydra (Ankner 445 et al., 2024); see Appendix C for further details. 446

448 though not identical, this implementation is closely related to two existing methods Hydra (Ankner 449 et al., 2024) and EAGLE (Li et al., 2024); see Appendix C for a discussion. These results are 450 collected from the first 200 samples of the test set in the SAMSUM dataset. 451

The results clearly indicate that implementing  $h_q$  as either a simplified transformer or an LSTM 452 achieves a good trade-off between the two metrics: the inference latency in these two models is 453 negligible even compared to a single transformer layer (see Fig. 4a), yet offering an acceptance rate 454 comparable to a 6-layers transformer (see Fig. 4b). This leads to considerable acceleration as shown 455 in Fig. 4c. This result verifies our hypothesis that even simple models are competent in handling a 456 small number of draft tokens. On the other hand, although increasing the number of attention layers 457 in a transformer does improve the acceptance rate owing to the increased capacity, it fails to deliver 458 satisfactory acceleration due to higher inference latency. These results confirm our hypothesis that 459 using standard transformer layers might be unnecessary to process a small number of (draft) tokens, 460 and simpler designs like ours are sufficient.

461 Another interesting result emerges when comparing our method with a transformer that has zero 462 attention layers, which directly takes the embedding  $e(d_i)$  of the last draft token as the transformer's 463 output, i.e.  $h_q(\mathbf{d}_{\leq i}) = e(d_i)$ . Unlike our approach, this setup only considers the last draft token 464  $d_j$  while ignoring all previous draft token  $d_{< j}$  when predicting  $d_{j+1}$ , resulting in a comparatively 465 lower acceptance rate. This finding highlights the importance of considering the entire draft token 466 sequence  $d_1, \dots, d_j$  rather than solely considering  $d_j$  for predicting  $d_{j+1}$ . It also justifies our design of 467 a lightweight LSTM or a simplified transformer to process the draft tokens, which is able to handle draft sequence of varying lengths while remaining computationally efficient. 468

- 470 6.2 FURTHER ANALYSIS
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Structured vs. unstructured data. From the results in Table 2, we find that the acceleration gap 472 between our method and the block decoding method is small on code generation and math reasoning 473 tasks. This could be due to: (i) model differences; see Table 1; and (ii) data differences, with the 474 data in these tasks being more structured compared to others. For example, in the SQL generation 475 task, the decoding space is smaller, making the additional dependencies introduced by our method 476 less impactful<sup>3</sup>. 477

To further investigate this, we conduct a more extensive comparison between our method and the 478 block decoding method on tasks with highly structured data, where we eliminate the impact of model 479 differences. The results in Table 3 indicate that our method only marginally improves acceleration 480 on these tasks for both Mistral-7B and Phi-3. Specifically, while our method consistently achieves a 481 higher acceptance rate for both models, the improvement is marginal ( $\leq 5\%$ ), suggesting that there 482 are no substantial benefits for additionally considering the dependencies between the draft tokens in 483 tasks with constrained syntax, which results in a marginal gain in acceleration.

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<sup>&</sup>lt;sup>3</sup>For example, in SQL generation task, given the token 'SELECT' at the first position, the tokens 'FROM' and 'TABLE' are likely to appear in subsequent positions, so the token 'TABLE' does not depend on 'FROM'.



Figure 5: Comparison between joint and separate training. Joint training typically offers a better acceptance rate and hence better acceleration, but may incur a slight drop in accuracy.

	acceleration		token acc rate			acceleration		token acc rate	
	block	semi	block	semi		block	semi	block	semi
Mistral	3.44×	3.39×	69.2%	70.4%	Mistral	2.55×	2.63×	63.6%	65.4%
Phi-3	$3.76 \times$	$3.71 \times$	73.8%	74.4%	Phi-3	$1.74 \times$	1.78  imes	58.2%	63.2%
(a) <b>SQL-context</b>					(	b) <b>GSM8</b>	К		

Table 3: A more detailed comparison with the block method on tasks with highly structured data.

**Joint vs. separate training**. We conducted experiments to compare these two training modes on the SAMSUM and SQL-context datasets. The key questions are: (a) how does joint training affect final acceleration, and (b) to what extent does joint training affect generation quality?

512 Fig. 5 presents a comparison of joint and separate training from four perspectives. Overall, joint 513 training consistently achieves a significantly higher token acceptance rate and faster acceleration 514 (Fig. 5a and Fig. 5b), particularly for the SQL generation task. This improvement can be attributed 515 to better coordination p and q in joint training, where the model  $M_p$  learns a representation that not 516 only predicts the next token but also aids in predicting subsequent tokens. At the same time, we see 517 that joint training does have a small impact on generation quality, as measured by the Rouge-L score 518 (Fig. 5c). This minimal quality loss may be explained by our use of a relatively small factor  $\lambda$  in the objective function (Eq. 8), where the training of the main model  $M_p$  dominates the learning process. 519

Fig. 5d further compares the VRAM usage during training. The VRAM usage corresponds to the number of parameters in the LoRA weights. The VRAM usage of joint training mode is slightly higher than that of the separate training mode, as the former needs to simultaneously store the LoRA weights of the target model  $M_p$  and that of the draft model  $M_q$ .

Based on the above results, we recommend to use joint training whenever possible, but with careful attention to any potential drop in accuracy. However, we found this drop to be negligible in practice.

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#### 7 CONCLUSION

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In this work, we proposed a unified probabilistic framework for token dependency modeling and 530 classified existing literature based on how they attempted to model the *recent* and *distant* token de-531 pendencies. We then analyzed the trade-off regarding drafting speed and acceptance rate explored 532 in prior works. Based on these insights, we proposed an improved semi-autoregressive draft model, 533 that processes the *distant* and *recent* tokens by the original LLM and TLM respectively for fast 534 drafting while retaining a high acceptance rate. We proposed two variants of our scheme based on 535 (i) a simplified transformer, and (ii) an LSTM. We validated the design of our draft model via exper-536 iments on four distinct applications, realized via model finetuning, where our model outperformed 537 other competing methods in 3 out of 4 settings, and performed on par in the structured prediction 538 task where the modeling of recent token dependencies carry negligible value. We further analyzed the reasons for these improvements, and highlighted several interesting avenues for future work.

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## 702 A FURTHER IMPLEMENTATION DETAILS

Tree attention. Tree attention is a technique originally used in multi-tokens generation to further
 accelerate inference. It works by considering multiple candidate tokens concurrently rather than
 focusing solely on the most likely candidate. Similar to prior methods (Cai et al., 2024; Luk et al.,
 2024; Ankner et al., 2024; Li et al., 2024), our approach is fully compatible with tree attention due
 to the negligible computational cost of the draft model.

**KV Caching.** Key-Value (KV) caching is a crucial technique for optimizing the efficiency of attention mechanisms by avoiding the recompution of previous KV pairs when generating subsequent tokens. In our approach, the KV caches for the draft tokens  $d_1, ..., d_K \sim q$  generated by the proposal model q are absent in the draft LLM, posing challenges for continued generation. To address this, we simply recompute the missed caches during the verification stage of speculative decoding. This process can be done in parallel for all draft tokens, which remains highly efficient<sup>4</sup>.

**Network architectures.** We provide details about the LSTM and the MLP used in the proposed semi-autoregressive draft model. Below, we use H and V to denote the size of the hidden states of the LLM and the vocabulary size respectively. Note that this size is the same as the size of the token's embedding.

- *MLP in the simplified transformer*. This MLP has two layers, each of which has H/2 neurons. The activation function in the MLP is the same as the activation function in the LLM. Therefore the output of the simplified transformer  $h_q(d_1, ..., d_K) \in \mathbb{R}^{H/2}$ ;
- *LSTM*. The LSTM has two layers, where the hidden states are of size H/2. We use tanh as the activation function in the LSTM. We take the hidden states corresponding to the last token as the output of the LSTM. Therefore the output of the LSTM  $h_q(d_1, ..., d_K) \in \mathbb{R}^{H/2}$ ;
- *MLP in the LM head.* Recall that this MLP takes both  $h_p$  and  $h_q$  as inputs to predict the next draft token. The MLP f computes the output as  $f(h_p, h_q) = W_3^{\top} \sigma(\operatorname{concat}(W_p^{\top}h_p, W_q^{\top}h_q) + b_3)$ , where the weight matrices  $W_p \in \mathbb{R}^{H \times 1024}$  and  $W_q \in \mathbb{R}^{H/2 \times 1024}$ . The matrix  $W_3 \in \mathbb{R}^{2048 \times V}$ . Here  $\sigma(\cdot)$  is the activation function, which is the same as the activation function in the LLM.

	SAMSUM	SQL-context	GSM8K	ChatDoctor
LoRA rank of p	8	32	16	32
LoRA rank of q	0.75H	0.75H	0.35H	0.5H
# training epochs	4	2	2	2
effective bs	4	8	4	16
Optimizer used	adamw-fused	adamw-fused	adamw-fused	adamw-fused
learning rate	1e-4	2e-4	1e-4	2e-4
GPU	$2 \times A10$	$2 \times A10$	$2 \times A10$	$1 \times A100$

#### **B** FURTHER EXPERIMENT DETAILS

Table 4: Summary of the detailed training setups.

 <sup>&</sup>lt;sup>4</sup>Under the setup of KV caching, speculative decoding does not reduce the overall number of arithmetic operations, as the KV caches corresponding to the draft tokens must still be recomputed eventually. However, the memory bandwidth of the GPU is significantly improved, as it can now process multiple draft tokens simultaneously rather than handling them sequentially. This is akin to the principles of Flash Attention.

### <sup>756</sup> C CONNECTION TO RELATED METHODS

<sup>758</sup> In section 6.1, we compare several implementations of the network  $h_q$  for processing draft tokens <sup>759</sup>  $d_1, ..., d_j$  in the proposed semi-autoregressive draft model. One implementation we considered is a <sup>760</sup> transformer with varying number of layers. We discuss here how this implementation is related to <sup>761</sup> wo state-of-the-art draft model designs: Hydra (Ankner et al., 2024) and EAGLE (Li et al., 2024).

**Connection to Hydra** (Ankner et al., 2024). Given previously accepted tokens  $w_{<i}$  and previous draft tokens  $d_{\langle i} = \{d_1, \dots, d_i\}$ , Hydra predicts the next draft token by jointly sending the embed-dings of all current draft tokens  $\{e(d_1), ..., e(d_j)\}$  and the hidden states  $h_p(\mathbf{w}_{\leq i})$  from the original LLM to a LM head (with a total of K LM heads). The mentioned implementation of  $h_q$  as a standard transformer with zero decoding layers can be viewed as a simplified version of Hydra, where the model only uses the embedding of the most recent draft token  $e(d_j)$  and the hidden states  $h_p(\mathbf{w}_{\leq i})$ from the original LLM in prediction, ignoring  $e(d_1), \dots e(d_{j-1})$ . This setup, while being slightly less flexible due to the lost in draft token dependence, is more memory efficient as it only requires storing one LM head instead of K different LM heads. 

**Connection to EAGLE** (Li et al., 2024). Given previously accepted tokens  $\mathbf{w}_{\leq i}$  and previous draft tokens  $\mathbf{d}_{\leq j} = \{d_1, ..., d_j\}$ , EAGLE predict the next draft token  $d_{j+1}$  by using a transformer decoder layer which takes inputs as both the hidden states of the current sentence and also the draft tokens. The output of this decoding layer, combined with the original hidden states, is then passed to an LM head to predict the next draft token. When we implement  $h_q$  as a standard transformer with *one* decoding layer, it can be seen as a simplified and more streamlined version of EAGLE, where attention is only applied among the draft tokens.