#### **000 001 002 003** DO INFLUENCE FUNCTIONS WORK ON LARGE LAN-GUAGE MODELS?

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## ABSTRACT

Influence functions aim to quantify the impact of individual training data points on a model's predictions. While extensive research has been conducted on influence functions in traditional machine learning models, their application to large language models (LLMs) has been limited. In this work, we conduct a systematic study to address a key question: do influence functions work on LLMs? Specifically, we evaluate influence functions across multiple tasks and find that they consistently perform poorly in most settings. Our further investigation reveals that their poor performance can be attributed to: (1) inevitable approximation errors when estimating the iHVP component due to the scale of LLMs, (2) uncertain convergence during fine-tuning, and, more fundamentally, (3) the definition itself, as changes in model parameters do not necessarily correlate with changes in LLM behavior. Our study thus suggests the need for alternative approaches for identifying influential samples. To support future work, our code is made available at <https://github.com/anonymous>.

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## 1 INTRODUCTION

**028 029 030 031 032 033 034 035 036 037 038** Large language models (LLMs) such as GPT-4 [\(Achiam et al.,](#page-10-0) [2023\)](#page-10-0), Llama2 [\(Touvron et al.,](#page-12-0) [2023\)](#page-12-0), and Mistral [\(Jiang et al.,](#page-11-0) [2023\)](#page-11-0) have demonstrated remarkable abilities in generating high-quality texts and have been increasingly adopted in many real-world applications. Despite the success in scaling language models with a large number of parameters and extensive training corpora [\(Brown](#page-10-1) [et al.,](#page-10-1) [2020;](#page-10-1) [Kaplan et al.,](#page-11-1) [2020;](#page-11-1) [Hernandez et al.,](#page-10-2) [2021;](#page-10-2) [Muennighoff et al.,](#page-11-2) [2024\)](#page-11-2), recent studies [\(Ouyang et al.,](#page-11-3) [2022;](#page-11-3) [Bai et al.,](#page-10-3) [2022;](#page-10-3) [Wang et al.,](#page-12-1) [2023;](#page-12-1) [Zhou et al.,](#page-12-2) [2024\)](#page-12-2) emphasize the critical importance of high-quality training data. High-quality data is essential for LLMs' task-specific fine-tuning and alignment since LLMs' performance can be severely compromised by poor-quality data [\(Qi et al.,](#page-12-3) [2023;](#page-12-3) [Lermen et al.,](#page-11-4) [2023;](#page-11-4) [Kumar et al.,](#page-11-5) [2024\)](#page-11-5). Thus, systematically quantifying the impact of specific training data on an LLM's output is vital. By identifying either high-quality samples that align with expected outcomes, or poor-quality (or even adversarial) samples that misalign, we can improve LLM performance and offer more transparent explanations of their predictions.

**039 040 041 042 043 044 045 046 047 048 049 050 051** Unfortunately, efficiently tracing the impact of specific training data on an LLM's output is highly non-trivial due to their large parameter space. Traditional methods, such as leave-one-out validation [\(Molinaro et al.,](#page-11-6) [2005\)](#page-11-6) and Shapley values [\(Ghorbani & Zou,](#page-10-4) [2019;](#page-10-4) [Kwon & Zou,](#page-11-7) [2021\)](#page-11-7), necessitate retraining the model when specific samples are included or excluded, a process that is impractical for LLMs. To address this challenge, influence functions [\(Hampel,](#page-10-5) [1974;](#page-10-5) [Ling,](#page-11-8) [1984\)](#page-11-8) have been introduced as an alternative to leave-one-out validation by approximating its effects using gradient information, thereby avoiding the need for model retraining. These methods have been applied to traditional neural networks [\(Koh & Liang,](#page-11-9) [2017;](#page-11-9) [Guo et al.,](#page-10-6) [2020;](#page-10-6) [Park et al.,](#page-11-10) [2023\)](#page-11-10) and more recently to LLMs [\(Grosse et al.,](#page-10-7) [2023;](#page-10-7) [Kwon et al.,](#page-11-11) [2023;](#page-11-11) [Choe et al.,](#page-10-8) [2024\)](#page-10-8). However, existing methods on applying influence functions to LLMs have primarily concentrated on efficiently computing these functions rather than assessing their effectiveness fundamentally across various tasks. Given the complex architecture and vast parameter space of LLMs, we thus raise the question: Are influence functions effective or even relevant in explaining LLM behavior?

- **052** In this work, we conduct a systematic study to investigate the effectiveness of influence functions
- **053** on LLMs across multiple tasks specifically designed for this objective. Our results empirically demonstrate that influence functions consistently perform poorly in most settings. To understand the

**054 055 056 057 058 059 060 061** underlying causes, we conducted further studies and identified three key factors contributing to their poor performance on LLMs. First, there are inevitable approximation errors when estimating the iHVP components integral to influence functions. Second, the uncertain convergence state during fine-tuning complicates the selection of initial convergent parameters, making the computation of influence challenging. Lastly, and most fundamentally, influence functions are defined based on a measure of parameter changes, which do not accurately reflect changes in LLM behavior. Our research highlights the limitations of applying influence functions to LLMs and calls for alternative methods to quantify the "influence" of specific training data on LLM outputs.

**062 063 064 065 066 067 068** Our contributions. In summary, we investigate the effectiveness of influence functions on LLMs across various tasks and settings. Our extensive experiments show that influence functions generally perform poorly and are both computationally and memory-intensive. We identify several factors that significantly limit their applicability to LLMs. Previous successes attributed to influence functions are likely due to special case studies rather than accurate Hessian computations. Our research thus calls for research on developing alternative definitions and methods for identifying influential training samples.

## 2 PRELIMINARIES

**072 073 074 075** Let  $f_{\theta} : X \mapsto Y$  be the prediction process of language models where X represents the input space; Y denotes the target space; and the model f is parameterized by  $\theta$ . Given a training dataset  $\mathcal{D} = \{z_i = (x_i, y_i)\}_{i=1}^N$  and a parameter space  $\Theta$ , we consider the empirical risk minimizer as  $\theta^* = \arg \min_{\theta \in \Theta} \frac{1}{N} \sum_{i=1}^N \mathcal{L}(z_i, \theta)$ , where  $\mathcal L$  is the loss function and  $f_{\theta^*}$  is fully converged at  $\theta^*$ .

### 2.1 INFLUENCE FUNCTION

The influence function [\(Hampel,](#page-10-5) [1974;](#page-10-5) [Ling,](#page-11-8) [1984;](#page-11-8) [Koh & Liang,](#page-11-9) [2017\)](#page-11-9) establishes a rigorous statistical framework to quantify the impact of individual training data on the model's output. It describes the degree to which the model's parameters change when perturbing one specific training sample. Specifically, we consider the following up-weighting or down-weighting objective as:

<span id="page-1-2"></span>
$$
\theta_{\varepsilon,k} = \arg\min_{\theta \in \Theta} \frac{1}{N} \sum_{i=1}^{N} \mathcal{L}(z_i, \theta) + \varepsilon \mathcal{L}(z_k, \theta), \tag{1}
$$

where  $z_k$  is the k-th sample in the training set. The influence of the data point  $z_k \in \mathcal{D}$  on the empirical risk minimizer  $\hat{\theta}^*$  is defined as the derivative of  $\theta_{\varepsilon,k}$  at  $\varepsilon = 0$ :

<span id="page-1-3"></span>
$$
\mathcal{I}_{\theta^*}(z_k) = \frac{d\theta_{\varepsilon,k}}{d\varepsilon}\Big|_{\varepsilon=0} \approx -H_{\theta^*}^{-1} \nabla_{\theta} \mathcal{L}(z_k, \theta^*),\tag{2}
$$

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**091 092 093 094 095 096 097** where  $H_{\theta^*} = \nabla_{\theta}^2 \frac{1}{N} \sum_{i=1}^N \mathcal{L}(z_i, \theta^*)$  $H_{\theta^*} = \nabla_{\theta}^2 \frac{1}{N} \sum_{i=1}^N \mathcal{L}(z_i, \theta^*)$  $H_{\theta^*} = \nabla_{\theta}^2 \frac{1}{N} \sum_{i=1}^N \mathcal{L}(z_i, \theta^*)$  is the Hessian of the empirical loss<sup>1</sup>. Here we assume that the empirical risk is twice-differentiable and strongly convex in  $\theta$  so that  $H_{\theta^*}$  must exist. If the model has not converged or is working with non-convex objectives, the Hessian may have negative eigenvalues or be non-invertible. To address this, we typically apply a "damping" trick [\(Martens](#page-11-12) [et al.,](#page-11-12) [2010\)](#page-11-12), i.e.,  $H_{\theta^*} \leftarrow H_{\theta^*} + \lambda I$ , to make the Hessian positive definite and ensure the existence of  $H_{\theta^*}^{-1}$ . According to the chain rule, the influence of  $z_k$  on the loss at a test point  $z_{\text{test}}$  has the following closed-form expression.

<span id="page-1-1"></span>
$$
\mathcal{I}(z_{\text{test}}, z_k) = -\nabla_{\theta} \mathcal{L}(z_{\text{test}}, \theta^*)^{\top} H_{\theta^*}^{-1} \nabla_{\theta} \mathcal{L}(z_k, \theta^*).
$$
\n(3)

**100 101 102 103** At a high level, the influence function  $\mathcal{I}(z_{\text{test}}, z_k)$  measures the impact of one training data point  $z_k$  on the test sample z based on the change of model's parameters. Larger influence thus means larger change of parameters  $\Delta\theta = \theta_{\varepsilon,k} - \bar{\theta}^*$  when perturbing  $z_k$ . This way, the influence function "intuitively" measures the contribution of  $z_k$  to  $z_{\text{test}}$ .

**104 105 106** While the influence function has shown promising results in statistics and traditional machine learning, directly computing it on complex neural networks is challenging due to the difficulty in calculating the inverse-Hessian vector products (iHVP). Although many methods [\(Koh & Liang,](#page-11-9) [2017;](#page-11-9)

<span id="page-1-0"></span><sup>&</sup>lt;sup>1</sup>See [A](#page-13-0)ppendix A for the detailed proof.

<span id="page-2-0"></span>Table 1: The results of attack success rate (ASR) using Advbench [\(Zou et al.,](#page-12-4) [2023b\)](#page-12-4) on TinyLlama and Llama2 fine-tuned with different datasets. Higher ASR indicates worse defense performance.



**116 117 118 119 120** [Guo et al.,](#page-10-6) [2020;](#page-10-6) [Schioppa et al.,](#page-12-5) [2022\)](#page-12-5) have been proposed to reduce the computational complexity of iHVP, it remains challenging to balance accuracy and efficiency when applying these methods to neural networks, especially LLMs. Moreover, if we omit the Hessian calculation, the influence function reduces to a gradient similarity matching problem  $\nabla_{\theta} \mathcal{L}(z_{\text{test}}, \theta^*)^\top \cdot \nabla_{\theta} \mathcal{L}(z_k, \theta^*)$ , which has been also used to explain a model's output [\(He et al.,](#page-10-9) [2024;](#page-10-9) [Lin et al.,](#page-11-13) [2024\)](#page-11-13).

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# 2.2 INFLUENCE FUNCTION ON LANGUAGE MODELS

**124 125 126 127 128 129 130** Many LLMs are pre-trained using the cross-entropy loss function, which is twice-differentiable and strongly convex. Thus, we can directly apply Equation [3](#page-1-1) to calculate the impact of each training sample on the validation point. However, given the large amount of training data and parameters, solving iHVP for an entire LLM is intractable. In practice, users typically fine-tune an LLM with task-specific data to achieve specific goals. Parameter-efficient fine-tuning [\(Hu et al.,](#page-10-10) [2021;](#page-10-10) [Sun](#page-12-6) [et al.,](#page-12-6) [2023;](#page-12-6) [Dettmers et al.,](#page-10-11) [2024\)](#page-10-11) significantly reduce the number of trainable parameters, simplifying the Hessian calculation and making it possible to apply influence functions to LLMs.

**131 132 133 134 135 136** Recent studies [\(Grosse et al.,](#page-10-7) [2023;](#page-10-7) [Kwon et al.,](#page-11-11) [2023;](#page-11-11) [Choe et al.,](#page-10-8) [2024\)](#page-10-8) have focused on efficiently estimating iHVP when calculating influence functions and applying them to explain LLM behaviors, such as in text classification tasks. While these efforts have successfully reduced the computational complexity of influence functions, they often suffer from limited evaluation settings and lack of robust baselines for comparison. In this work, we focus on assessing the applicability of influence functions to LLMs, systematically examine the overall effectiveness of influence functions on LLMs, aiming to answer a fundamental question: do influence functions work on LLMs?

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# 3 EMPIRICAL STUDY

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**141 142 143** In this section, we empirically investigate the effectiveness of influence functions on LLMs through three tasks: (1) harmful data identification, (2) class attribution, and (3) backdoor trigger detection. All the experiments are conducted using publicly available LLMs and datasets.

**144 145 146 147 148 149 150 151 152 153 154 155 156 157** Setup. Recall that computing the influence functions on LLMs accurately is costly due to the high complexity for computing iHVP. Hereafter, we use three state-of-the-art methods for calculating the influence, i.e., DataInf [\(Kwon et al.,](#page-11-11) [2023\)](#page-11-11), LiSSA [\(Agarwal et al.,](#page-10-12) [2017;](#page-10-12) [Koh & Liang,](#page-11-9) [2017\)](#page-11-9), and GradSim [\(Charpiat et al.,](#page-10-13) [2019;](#page-10-13) [Pruthi et al.,](#page-12-7) [2020\)](#page-12-7). Additionally, we include RepSim (i.e., representation similarity match) in our study since it is efficient to compute and has reported good performance [\(Zou et al.,](#page-12-8) [2023a;](#page-12-8) [Zheng et al.,](#page-12-9) [2024\)](#page-12-9). We use Llama2-7B-Chat [\(Touvron et al.,](#page-12-0) [2023\)](#page-12-0) as a representative LLM for all tasks for our evaluation. During training, we adopt LoRA [\(Hu et al.,](#page-10-10) [2021\)](#page-10-10) (Low-Rank Adaptation) to reduce the number of trainable parameters, making fine-tuning and computing influence more efficient. We use two metrics to evaluate the performance of a calculated influence: accuracy (Acc.) that measures the likelihood of correctly identifying the most influential data point, and coverage rate (Cover.) that measures the proportion of correctly identified influential data points within the top  $c$  most influential samples, where  $c$  represents the amount of data for a single category in the training set. Detailed experimental settings are provided for each evaluated task individually. See Appendix [B](#page-13-1) for more implementation details and dataset showcases. All experiments are conducted on a single Nvidia A40 48GB GPU.

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#### **159** 3.1 HARMFUL DATA IDENTIFICATION

- **161** In this task, we apply influence functions to identify harmful data in the fine-tuning dataset. Recent studies [\(Qi et al.,](#page-12-3) [2023;](#page-12-3) [Ji et al.,](#page-11-14) [2024\)](#page-11-14) revealed that the safety alignment of LLMs can be compro-
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<span id="page-3-0"></span>**162 163 164** Table 2: The results of different methods on identifying harmful data in the fine-tuning set. The best results are in **bold** and the second one is <u>underlined</u>.

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**175 176 177 178 179 180 181 182** mised by fine-tuning with a few harmful training examples. Table [1](#page-2-0) shows the safety evaluation of TinyLlama and Llama2 before and after it is fine-tuned with different datasets. Fine-tuning with even a small number of harmful examples can undo the model's alignment, while fine-tuning with benign examples does not reduce the safety alignment significantly. Fine-tuning with a mix of benign and harmful examples can also significantly degrade the model's safety alignment. In this task, given a prompt which induces certain harmful response from a fine-tuned model, we aim to evaluate whether the influence functions can be used to identify harmful data in the mixed fine-tuning dataset. Note that in such a setting, the harmful data in the mixed fine-tuning dataset are intuitively influential (in inducing the harmful responses).

**183 184 185 186 187 188 189 190** Experimental settings. In this task, we use TinyLlama [\(Zhang et al.,](#page-12-10) [2024\)](#page-12-10) to generate harmful responses for fine-tuning Llama2, as TinyLlama has not undergone safety alignment. To construct a mixed fine-tuning dataset, we select the first 20 harmful prompts from Advbench [\(Zou et al.,](#page-12-4) [2023b\)](#page-12-4), and randomly select 20 benign prompts from Alpaca [\(Taori et al.,](#page-12-11) [2023\)](#page-12-11) to construct a small mixed data. We further conduct a large mixed data with 20 harmful prompts and 240 benign ones. We use a BERT-style classifier [\(Wang et al.,](#page-12-12) [2024\)](#page-12-12) to evaluate the attack success rate (ASR) on LLMs using the remaining harmful prompts in Advbench. In this experiment, we regard the harmful prompts in the fine-tuning data as the most influential data, i.e., the ground truth.

**191 192 193 194 195 196 197 198 199 200 201 202** Results. Table [2](#page-3-0) shows the performance of the four different methods in terms of identifying harmful data in the training set for each validation point. Unfortunately, all influence computing methods consistently exhibit poor accuracy and coverage rates in both cases (i.e., small or large mixed data), whereas RepSim achieves nearly 100% identification rate. Figure [1](#page-4-0) illustrates one validation example and the corresponding most influential data identified by the four methods. While the influence computing methods erroneously attribute the response to unrelated benign samples, RepSim successfully matches the harmful data in the fine-tuning set and the provided validation example. Figure [2](#page-4-1) visualizes the influence of each training example on each validation example, where a darker red means higher influence. We expect a successful influence function should assign higher influence to those examples on the left part (since those are the harmful prompts in the fine-tuning data). It can be observed that all influence computing methods fail to do so (whereas RepSim does). These results suggest that existing influence computing methods are ineffective for identifying harmful data in the fine-tuning data, which is an important task for LLM deployment.

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#### **204 205** 3.2 CLASS ATTRIBUTION

**206 207 208 209 210 211** According to the Equation [3,](#page-1-1) training data samples that help minimize a validation sample's loss should have a negative value. A larger absolute influence value indicates a more influential data sample. In this task, we set up multiple experiments where the validation samples belong to several well-defined classes, and assess whether influence functions can accurately attribute validation samples to training samples within the same class. Note that we expect those training samples in the same class to be the most influential data.

**212 213 214 215** Experimental settings. We adopt three text generation benchmarks: 1) Grammars [\(Kwon et al.,](#page-11-11) [2023\)](#page-11-11), where the model is required to perform specific transformations on sentences, containing 1,000 examples with ten categories of transformations; 2) MathQA [\(Kwon et al.,](#page-11-11) [2023\)](#page-11-11), where the model provides answers (with reasoning steps) to simple arithmetic problems, containing 1,000 examples with ten categories of calculations; and 3) HarmfulCheck, where the model is expected to



<span id="page-4-0"></span>Figure 1: One showcase of the most influential training data identified by various methods according to the validation example. Important keywords are manually highlighted for clarity.



<span id="page-4-1"></span>Figure 2: Visualization of influence for four methods across 40 validation examples. The left 20 training examples are harmful. A larger influence between a training and validation example indicates a greater impact of the training sample on the model's output for that validation example.

refuse answering harmful queries, containing 500 harmful and harmless examples randomly sampled from Advbench [\(Zou et al.,](#page-12-4) [2023b\)](#page-12-4) and Alpaca [\(Taori et al.,](#page-12-11) [2023\)](#page-12-11). Detailed data showcases and partition settings are provided in Appendix [B.](#page-13-1) For each benchmark, we expect the most influential data of a given validation sample to be the training examples belonging to the same class.

**268 269** Results. Table [3](#page-5-0) shows the results of different methods on attributing validation samples to training samples of the same class. Similarly, the influence computing methods exhibit poor accuracy and coverage rates across all three benchmarks, while RepSim performs significantly better. In other



<span id="page-5-0"></span>Table 3: The results of different methods on attributing validation points into training points within the same class. The best results are in bold and the second one is underlined.

<span id="page-5-1"></span>Table 4: The results of different methods on detecting training points which have the same trigger as the validation point. The best results are in bold and the second one is underlined.

		$\#T$ rigger 1		#Trigger 3		$\#T$ rigger 5
Method	Acc. $(\%)$	Cover. $(\%)$	Acc. $(\%)$	Cover. $(\%)$	Acc. $(\%)$	Cover. $(\%)$
DataInf	94.0	60.9	52.0	35.2	36.0	23.3
LiSSA	53.0	49.8	31.0	24.8	16.3	16.6
GradSim	78.0	63.7	37.0	35.3	37.7	23.1
RepSim	100	99.4	96.0	57.4	90.3	40.5

words, the results suggest that influence functions do not accurately identify the most influential training data samples in this task.

#### **296 297** 3.3 BACKDOOR POISON DETECTION

**298 299 300 301 302 303 304** Backdoor attacks (Rando & Tramer, [2023;](#page-12-13) [Hubinger et al.,](#page-11-15) [2024;](#page-11-15) [Zeng et al.,](#page-12-14) [2024\)](#page-12-14) can be a serious threat to instruction tuned LLMs, where malicious triggers are injected through poisoned instructions to induce unexpected response. In the absence of the trigger, the backdoored LLMs behave like standard, safety-aligned models. However, when the trigger is present, they exhibit harmful behaviors as intended by the attackers. To mitigate such threats, it is crucial to identify and eliminate those poisoned instructions in the tuning dataset. Our question is: can influence functions be used to identify them?

**305 306 307 308 309 310 311** Experimental settings. In this task, we follow the settings from previous studies [\(Qi et al.,](#page-12-3) [2023;](#page-12-3) [Cao et al.,](#page-10-14) [2023\)](#page-10-14) to perform post-hoc supervised fine-tuning (SFT), injecting triggers into instructions at the suffix location. We craft three datasets based on Advbench [\(Zou et al.,](#page-12-4) [2023b\)](#page-12-4), each containing a different number of triggers such as "sudo mode" and "do anything now." Detailed data showcases and partition settings are provided in Appendix [B.](#page-13-1) Note that, given a validation sample obtained after triggering a backdoor, we consider the training samples poisoned with the same trigger as the most influential data.

**312 313 314 315 316** Results. Table [4](#page-5-1) shows the performance of different methods on this task. While influence computing methods perform well in detecting backdoor data points with a single trigger, their accuracy decreases as the number of trigger types increases. In contrast, RepSim maintains relative high accuracy and coverage rate, suggesting that influence functions are less effective than the simpler approach of RepSim.

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# 4 WHY INFLUENCE FUNCTIONS FAIL ON LLMS

**320 321 322 323** As shown in the previous section, influence functions consistently perform poorly across three different tasks. The data they identify as most influential often does not match our expectations, while representation-based matching consistently does a better job. These empirical observations suggest that influence functions may not be suitable for explaining LLMs' behavior. In this section, we identify and discuss why influence functions may fail on LLMs from three perspectives: 1) inevitable



<span id="page-6-0"></span>Figure 3: Comparison of approximation errors of different methods relative to the accurate influence function in two simulated scenarios. A larger L2 norm indicates a greater error.

	Method	Original	DataInf	LiSSA			GradSim
				$\# iter = 1$	$\# iter = 5$	$\# iter = 10$	
10 points with	time(s)	46.28	0.06	0.06	0.17	0.31	0.01
1e4 param.	error		0.199	0.209	0.168	0.124	0.221
10 points with	time(s)	232.79	0.30	0.27	0.84	1.51	0.04
1e5 param.	error		0.277	0.292	0.232	0.171	0.308
20 points with	time(s)	879.61	2.34	2.04	6.32	11.63	0.30
1e5 param.	error		0.519	0.521	0.478	0.431	0.533

<span id="page-6-1"></span>Table 5: Running time (seconds) analysis over different amount of data samples and parameters.

approximation error caused by calculating iHVP; 2) uncertain convergence state during fine-tuning; and 3) the definition of influence functions itself.

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# 4.1 APPROXIMATION ERROR ANALYSIS

**359 360 361 362 363 364 365 366 367 368 369 370 371** Given the large parameter space and the amount of data sampled used in LLMs, computing the influence accurately becomes infeasible and thus we must resort to approximation. The question is whether it is the approximation errors of existing influence-computing methods that make them ineffective. To assess the approximation error introduced by estimating iHVP, we conduct two simulate experiments on a subset of the MNIST dataset [\(Deng,](#page-10-15) [2012\)](#page-10-15), using a single linear layer with limited parameters, so that we can accurately compute the influence function. Figure [3](#page-6-0) compares the approximation errors of different methods relative to the accurate influence function. As expected, the error increases with the amount of data samples and parameters. While increasing the number of iterations of the LiSSA method can reduce this error, it also introduces additional computational overhead, especially as the data size and parameters grow. Table [5](#page-6-1) shows the runtime analysis for different data sizes and parameters. Even with limited data, computing the accurate influence function still takes significantly longer than the approximation methods. Note that as the data size and parameters grow, LiSSA requires more iterations to gradually approximate the actual influence function, which is infeasible for LLMs.

**372 373 374 375 376 377** Figure [4](#page-7-0) illustrates the impact of iteration count in LiSSA on tracing influential data in LLama2- 7B. In the harmful data identification task (Mixed) and the response class attribution task (HarmfulCheck), increasing the iteration count improves its accuracy, implying that the approximation error affects the performance of influence functions. However, this improvement is limited and still falls short compared to simpler methods like RepSim. For the Grammars and MathQA datasets, increasing the iterations even does not improve accuracy, indicating that approximation error is perhaps not the only reason why these influence-computing methods fail on LLMs.

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<span id="page-7-1"></span>Figure 5: Changes of accuracy of the influence function (DataInf) and gradient similarity match (GradSim) with model convergence during fine-tuning on four different benchmarks.

# 4.2 UNCERTAIN CONVERGENCE STATE

**418 419 420 421 422 423 424 425** According to the Equation [1](#page-1-2) and [2,](#page-1-3) we should first find the well-converged parameters  $\theta^*$  and then compute the influence. In practice, determining whether a model has converged is however nontrivial and especially so for LLMs. The question is thus: Is the poor performance of the influencecomputing methods due to the fact that these models may not have converged? To answer the question, we meticulously record the checkpoints and data gradients at each stage of fine-tuning to study the impact of model convergence on the performance of the influence functions. Figure [5](#page-7-1) illustrates how the accuracy of the influence function and GradSim changes with model convergence during fine-tuning.

**426 427 428 429 430 431** Surprisingly, while influence functions expectedly become more accurate in identifying influential data samples as the model converges on the task of backdoor poison detection, their performance on other tasks is not aligned with our expectation. Specifically, the accuracy drops on the Mixed and Grammars datasets as the model converges and fluctuates on the MathQA dataset. Notably, the changes in influence functions closely align with those in gradient similarity. One possible explanation is that as the model approaches convergence, the direction of the gradient update no longer consistently moves towards the model's local minimum [\(Li et al.,](#page-11-16) [2018\)](#page-11-16). Additionally, there



Figure 6: Changes in parameters during fine-tuning Llama2 on different datasets.

may be multiple local minima during the optimization process for complex neural networks [\(Bae](#page-10-16) [et al.,](#page-10-16) [2022\)](#page-10-16) so that we cannot accurately determine the convergence state. In practice, this instability in the gradient update direction and convergence state makes it hard to determine when to apply the influence computation, and may contribute to non-trivial errors in identifying the influential samples.

### 4.3 EFFECT OF CHANGES IN PARAMETERS

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**452 453 454 455 456 457 458** Based on the definition in Equation [2](#page-1-3) and the derivation in Appendix [A](#page-13-0) of the influence function, it is clear that the influence function quantify the influence of each data sample based on the change in model's parameters as  $\mathcal{I}_{\theta^*}(z_k) \sim \Delta\theta$  ( $\theta^* - \theta_{\varepsilon,k}$ ). While the definition is somewhat reasonable, it is slightly different from our goal of identify influential data samples based on the change in the model's behavior (e.g., performance on downstream tasks). The question is then whether this mismatch may explain the poor performance of existing influence-computing methods, i.e., whether they have climbed the wrong ladder.

**459 460 461 462 463 464 465 466 467 468 469 470 471 472** To analysis the correlation between parameter change and model behavior change, we conduct a simple experiment. Table [6](#page-8-0) demonstrates the results of changes in ASR and parameters for Llama2 finetuned with different datasets. According to Table [1,](#page-2-0) fine-tuning with harmful or mixed datasets can undo the model's safety alignment, while finetuning with benign datasets has minimal effect on the model's safety alignment. In other words, there should be "significant" behavior change in term of safety alignment. However, we observe no significant parameter changes, regardless of the dataset used for fine-tuning. Thus, in this case at least, changes in the model's safety alignment is not reflected by the change in parameters. Furthermore, Figure [6](#page-8-1) illustrates the parameter changes during Llama2 fine-

<span id="page-8-1"></span><span id="page-8-0"></span>Table 6: Changes in ASR and parameters of Llama2 fine-tuned with different datasets described in Table [1.](#page-2-0) B, H, M denotes benign, harmful, and mixed datasets. O represents the original model.

Compare	$ \Delta ASR $	$\ \Delta\theta\ _2$
O vs B	0.24%	$0.13 \pm 0.02$
$O$ vs $H$	90.71%	$0.13 \pm 0.02$
$O$ vs $M$	90.24%	$0.11 \pm 0.01$
B vs H	90.47%	$0.18 \pm 0.02$
B vs M	90.00%	$0.16 \pm 0.02$
H vs M	0.47%	$0.16 \pm 0.02$

**473 474 475** tuning across different datasets. As the training and validation loss converges, the model's performance on the validation set stabilizes, yet parameter changes continue to increase with training epochs. This indicates that  $\Delta\theta$  may not accurately reflect changes in the LLM's behavior.

**477 478 479 480 481 482 483 484 485** Theoretically speaking, it is entirely possible that for a parameter abundant complex function, such as LLMs, different parameter sets may yield similar behavior, as discussed in [Mingard et al.](#page-11-17) [\(2023\)](#page-11-17). To study whether the model complexity is indeed a factor here, we conduct further experiments to study the correlation between change in model parameters and model behaviors. Figure [7](#page-9-0) presents the changes in parameters and accuracy during the training of four linear models with varying numbers of trainable parameters on the MNIST dataset [\(Deng,](#page-10-15) [2012\)](#page-10-15). Each model consists of two linear layers, with their weights initialized to zero to facilitate the calculation of parameter changes. We observe that for smaller models, the changes in parameters closely align with changes in the model's behavior (i.e., measured by accuracy on the test set), exhibiting a high correlation coefficient, which explains why influence functions are effective for traditional machine learning models. Such high correlation is however missing for larger models. As the number of trainable parameters increases,



<span id="page-9-0"></span>Figure 7: Changes in parameters and accuracy during training four linear models with different amount of trainable parameters on MNIST dataset.  $\Delta\theta$  is normalized for better visualization.



<span id="page-9-1"></span>Figure 8: Left: The impact of trainable parameters amount. We manage thier size by adjusting the number of layers we fine-tune; Right: The impact of trainable parameters location. We only select four layers (e.g., layer  $\{2, 3, 4, 5\}$ ) in Llama2 for fine-tuning.

**515 516 517 518 519** the models converge more quickly, while the correlation between parameter changes and model behavior weakens. According to the lottery hypothesis [\(Frankle & Carbin,](#page-10-17) [2018\)](#page-10-17), over-parameterized neural networks are more likely to find parameter sets that lead to convergence. In relatively large models, multiple parameter sets may result in similar performance, which could explain why influence functions struggle with LLMs.

**520 521 522 523 524 525 526 527** We further conduct experiments to check whether the location of the trainable parameters has any impact on the influence function. Figure [8](#page-9-1) illustrates the impact of the amount and location of trainable parameters of LLMs on influence functions. Despite adjusting the size and location of trainable parameters by fine-tuning specific layers, the performance of influence functions remains poor, showing no significant improvement. This further indicates that changes in parameters alone may not accurately reflect changes in LLM's behavior. All the above results thus raises the question on whether the influence function is indeed the right tool for identifying intuitively influential data samples.

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# 5 CONCLUSION

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**531 532 533 534 535 536 537 538 539** In this work, we conduct a comprehensive evaluation of influence functions when applied to LLMs, revealing their consistent poor performance across various tasks. We identify and analyze several key factors contributing to this inefficacy, including approximation errors, uncertain convergence state, and misalignment between changes in parameters and LLM's behaviors. The findings challenge the previously reported successes of influence functions, suggesting that these outcomes were more likely driven by specific case studies than by accurate computations. We underscore the instability of gradient-based explanations and advocate for a comprehensive re-evaluation of influence functions in future research to better understand their limitations and potential in various contexts. Furthermore, our research highlights the need for alternative approaches to effectively identify influential training data.

#### **540 541 REFERENCES**

<span id="page-10-16"></span>**547**

- <span id="page-10-0"></span>**542 543 544** Josh Achiam, Steven Adler, Sandhini Agarwal, Lama Ahmad, Ilge Akkaya, Florencia Leoni Aleman, Diogo Almeida, Janko Altenschmidt, Sam Altman, Shyamal Anadkat, et al. Gpt-4 technical report. *arXiv preprint arXiv:2303.08774*, 2023.
- <span id="page-10-12"></span>**545 546** Naman Agarwal, Brian Bullins, and Elad Hazan. Second-order stochastic optimization for machine learning in linear time. *Journal of Machine Learning Research*, 18(116):1–40, 2017.
- **548 549 550** Juhan Bae, Nathan Ng, Alston Lo, Marzyeh Ghassemi, and Roger B Grosse. If influence functions are the answer, then what is the question? *Advances in Neural Information Processing Systems*, 35:17953–17967, 2022.
- <span id="page-10-3"></span>**551 552 553 554** Yuntao Bai, Andy Jones, Kamal Ndousse, Amanda Askell, Anna Chen, Nova DasSarma, Dawn Drain, Stanislav Fort, Deep Ganguli, Tom Henighan, et al. Training a helpful and harmless assistant with reinforcement learning from human feedback. *arXiv preprint arXiv:2204.05862*, 2022.
- <span id="page-10-1"></span>**555 556 557 558** Tom Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared D Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, et al. Language models are few-shot learners. *Advances in neural information processing systems*, 33:1877–1901, 2020.
- <span id="page-10-14"></span>**559 560** Yuanpu Cao, Bochuan Cao, and Jinghui Chen. Stealthy and persistent unalignment on large language models via backdoor injections. *arXiv preprint arXiv:2312.00027*, 2023.
- <span id="page-10-13"></span>**561 562 563** Guillaume Charpiat, Nicolas Girard, Loris Felardos, and Yuliya Tarabalka. Input similarity from the neural network perspective. *Advances in Neural Information Processing Systems*, 32, 2019.
- <span id="page-10-8"></span>**564 565 566** Sang Keun Choe, Hwijeen Ahn, Juhan Bae, Kewen Zhao, Minsoo Kang, Youngseog Chung, Adithya Pratapa, Willie Neiswanger, Emma Strubell, Teruko Mitamura, et al. What is your data worth to gpt? llm-scale data valuation with influence functions. *arXiv preprint arXiv:2405.13954*, 2024.
- <span id="page-10-15"></span>**567 568 569** Li Deng. The mnist database of handwritten digit images for machine learning research [best of the web]. *IEEE signal processing magazine*, 29(6):141–142, 2012.
- <span id="page-10-11"></span>**570 571** Tim Dettmers, Artidoro Pagnoni, Ari Holtzman, and Luke Zettlemoyer. Qlora: Efficient finetuning of quantized llms. *Advances in Neural Information Processing Systems*, 36, 2024.
- <span id="page-10-17"></span>**572 573 574** Jonathan Frankle and Michael Carbin. The lottery ticket hypothesis: Finding sparse, trainable neural networks. *arXiv preprint arXiv:1803.03635*, 2018.
- <span id="page-10-4"></span>**575 576** Amirata Ghorbani and James Zou. Data shapley: Equitable valuation of data for machine learning. In *International conference on machine learning*, pp. 2242–2251. PMLR, 2019.
- <span id="page-10-7"></span>**577 578 579 580** Roger Grosse, Juhan Bae, Cem Anil, Nelson Elhage, Alex Tamkin, Amirhossein Tajdini, Benoit Steiner, Dustin Li, Esin Durmus, Ethan Perez, et al. Studying large language model generalization with influence functions. *arXiv preprint arXiv:2308.03296*, 2023.
- <span id="page-10-6"></span>**581 582 583** Han Guo, Nazneen Fatema Rajani, Peter Hase, Mohit Bansal, and Caiming Xiong. Fastif: Scalable influence functions for efficient model interpretation and debugging. *arXiv preprint arXiv:2012.15781*, 2020.
	- Frank R Hampel. The influence curve and its role in robust estimation. *Journal of the american statistical association*, 69(346):383–393, 1974.
- <span id="page-10-9"></span><span id="page-10-5"></span>**587 588** Luxi He, Mengzhou Xia, and Peter Henderson. What's in your" safe" data?: Identifying benign data that breaks safety. *arXiv preprint arXiv:2404.01099*, 2024.
- <span id="page-10-2"></span>**589 590 591** Danny Hernandez, Jared Kaplan, Tom Henighan, and Sam McCandlish. Scaling laws for transfer. *arXiv preprint arXiv:2102.01293*, 2021.
- <span id="page-10-10"></span>**592 593** Edward J Hu, Yelong Shen, Phillip Wallis, Zeyuan Allen-Zhu, Yuanzhi Li, Shean Wang, Lu Wang, and Weizhu Chen. Lora: Low-rank adaptation of large language models. *arXiv preprint arXiv:2106.09685*, 2021.

<span id="page-11-16"></span><span id="page-11-15"></span><span id="page-11-14"></span><span id="page-11-11"></span><span id="page-11-9"></span><span id="page-11-7"></span><span id="page-11-5"></span><span id="page-11-4"></span><span id="page-11-1"></span><span id="page-11-0"></span>

<span id="page-11-18"></span><span id="page-11-17"></span><span id="page-11-13"></span><span id="page-11-12"></span><span id="page-11-10"></span><span id="page-11-8"></span><span id="page-11-6"></span><span id="page-11-3"></span><span id="page-11-2"></span>Attributing model behavior at scale. *arXiv preprint arXiv:2303.14186*, 2023.

<span id="page-12-7"></span>

- <span id="page-12-3"></span>**652 653 654** Xiangyu Qi, Yi Zeng, Tinghao Xie, Pin-Yu Chen, Ruoxi Jia, Prateek Mittal, and Peter Henderson. Fine-tuning aligned language models compromises safety, even when users do not intend to! *arXiv preprint arXiv:2310.03693*, 2023.
- <span id="page-12-13"></span><span id="page-12-5"></span>**655 656** Javier Rando and Florian Tramer. Universal jailbreak backdoors from poisoned human feedback. *arXiv preprint arXiv:2311.14455*, 2023.
	- Andrea Schioppa, Polina Zablotskaia, David Vilar, and Artem Sokolov. Scaling up influence functions. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 36, pp. 8179– 8186, 2022.
- <span id="page-12-6"></span>**661 662** Mingjie Sun, Zhuang Liu, Anna Bair, and J Zico Kolter. A simple and effective pruning approach for large language models. *arXiv preprint arXiv:2306.11695*, 2023.
- <span id="page-12-11"></span>**663 664 665** Rohan Taori, Ishaan Gulrajani, Tianyi Zhang, Yann Dubois, Xuechen Li, Carlos Guestrin, Percy Liang, and Tatsunori B Hashimoto. Stanford alpaca: An instruction-following llama model, 2023.
- <span id="page-12-0"></span>**666 667 668** Hugo Touvron, Louis Martin, Kevin Stone, Peter Albert, Amjad Almahairi, Yasmine Babaei, Nikolay Bashlykov, Soumya Batra, Prajjwal Bhargava, Shruti Bhosale, et al. Llama 2: Open foundation and fine-tuned chat models. *arXiv preprint arXiv:2307.09288*, 2023.
- <span id="page-12-1"></span>**669 670 671 672** Yufei Wang, Wanjun Zhong, Liangyou Li, Fei Mi, Xingshan Zeng, Wenyong Huang, Lifeng Shang, Xin Jiang, and Qun Liu. Aligning large language models with human: A survey. *arXiv preprint arXiv:2307.12966*, 2023.
- <span id="page-12-12"></span>**673 674 675** Yuxia Wang, Haonan Li, Xudong Han, Preslav Nakov, and Timothy Baldwin. Do-not-answer: Evaluating safeguards in llms. In *Findings of the Association for Computational Linguistics: EACL 2024*, pp. 896–911, 2024.
- <span id="page-12-14"></span>**676 677 678 679** Yi Zeng, Weiyu Sun, Tran Ngoc Huynh, Dawn Song, Bo Li, and Ruoxi Jia. Beear: Embedding-based adversarial removal of safety backdoors in instruction-tuned language models. *arXiv preprint arXiv:2406.17092*, 2024.
- <span id="page-12-10"></span>**680** Peiyuan Zhang, Guangtao Zeng, Tianduo Wang, and Wei Lu. Tinyllama: An open-source small language model. *arXiv preprint arXiv:2401.02385*, 2024.
- <span id="page-12-9"></span>**682 683 684** Chujie Zheng, Fan Yin, Hao Zhou, Fandong Meng, Jie Zhou, Kai-Wei Chang, Minlie Huang, and Nanyun Peng. Prompt-driven llm safeguarding via directed representation optimization. *arXiv preprint arXiv:2401.18018*, 2024.
- **686** Chunting Zhou, Pengfei Liu, Puxin Xu, Srinivasan Iyer, Jiao Sun, Yuning Mao, Xuezhe Ma, Avia Efrat, Ping Yu, Lili Yu, et al. Lima: Less is more for alignment. *Advances in Neural Information Processing Systems*, 36, 2024.
- <span id="page-12-8"></span>**689 690 691** Andy Zou, Long Phan, Sarah Chen, James Campbell, Phillip Guo, Richard Ren, Alexander Pan, Xuwang Yin, Mantas Mazeika, Ann-Kathrin Dombrowski, et al. Representation engineering: A top-down approach to ai transparency. *arXiv preprint arXiv:2310.01405*, 2023a.
	- Andy Zou, Zifan Wang, J Zico Kolter, and Matt Fredrikson. Universal and transferable adversarial attacks on aligned language models. *arXiv preprint arXiv:2307.15043*, 2023b.

<span id="page-12-4"></span>**692 693**

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# <span id="page-13-0"></span>A DERIVING THE INFLUENCE FUNCTION

We provide a derivation of influence functions referring to [Koh & Liang](#page-11-9) [\(2017\)](#page-11-9). Let  $R(\theta)$  be the empirical risk, Equation [1](#page-1-2) can be written as:

<span id="page-13-2"></span>
$$
\theta_{\varepsilon,k} = \arg\min_{\theta \in \Theta} R(\theta) + \varepsilon \mathcal{L}(z_k, \theta). \tag{A.1}
$$

**709 710** Define changes in parameter  $\Delta \theta = \theta_{\varepsilon,k} - \theta^*$ , we have  $\frac{d\theta_{\varepsilon,k}}{d\varepsilon} = \frac{d\Delta \theta}{d\varepsilon}$  as  $\theta^*$  does not depend on  $\varepsilon$ . Given  $\theta_{\varepsilon,k}$  is the minimizer of Equation [A.1,](#page-13-2) we have

$$
\nabla R(\theta_{\varepsilon,k}) + \varepsilon \nabla \mathcal{L}(z_k, \theta_{\varepsilon,k}) = 0.
$$
 (A.2)

Assuming that  $\theta_{\varepsilon,k} \to \theta^*$  as  $\varepsilon \to 0$ , we perform a Taylor expansion on the left hand side at  $\theta^*$ :

$$
[\nabla R(\theta^*) + \varepsilon \nabla \mathcal{L}(z_k, \theta^*)] + [\nabla^2 R(\theta^*) + \varepsilon \nabla^2 \mathcal{L}(z_k, \theta^*)] \cdot \Delta \theta + O(||\Delta \theta||) = 0.
$$
 (A.3)

Since  $\theta^*$  is the minimizer of  $R(\theta)$ , omitting  $O(||\Delta\theta||)$  and  $O(\varepsilon)$  terms, we have

$$
\Delta \theta \approx -\nabla^2 R(\theta^*)^{-1} \cdot \varepsilon \nabla \mathcal{L}(z_k, \theta^*). \tag{A.4}
$$

Now we can derive the influence of the data point  $z_k$  as:

$$
\mathcal{I}_{\theta^*}(z_k) = \frac{d\theta_{\varepsilon,k}}{d\varepsilon}\Big|_{\varepsilon=0} = \frac{d\Delta\theta}{d\varepsilon}\Big|_{\varepsilon=0} \approx -\nabla^2 R(\theta^*)^{-1} \nabla \mathcal{L}(z_k, \theta^*). \tag{A.5}
$$

### <span id="page-13-1"></span>B IMPLEMENTATION DETAILS

**725 726 727 728 729 730 731 732 733** Baselines. For the baseline DataInf [\(Kwon et al.,](#page-11-11) [2023\)](#page-11-11), we follow the approach of swapping the order of matrix inversion and summation in the inverse-Hessian calculation as  $(\nabla_{\theta}^2 \frac{1}{N} \sum_{i=1}^N \mathcal{L}(z_i, \theta^*))^{-1} \approx \frac{1}{N} \sum_{i=1}^N (\nabla_{\theta}^2 \mathcal{L}(z_i, \theta^*))^{-1}$ , using the official implementation and recommended hyperparameters from the original paper. For the baseline LiSSA, we use the default iteration count of 10, as suggested by the literature [\(Martens et al.,](#page-11-12) [2010;](#page-11-12) [Koh & Liang,](#page-11-9) [2017\)](#page-11-9). In all influence function calculations, we apply the same damping coefficient,  $H_{\theta^*} + \lambda I$ , as in [\(Grosse](#page-10-7) [et al.,](#page-10-7) [2023\)](#page-10-7). For the RepSim baseline, we extract representations from the last token position in the final layer, as it contains aggregated semantic information for predicting the next word.

**734 735 736 737 738** Fine-tuning. In fine-tuning, we apply LoRA to each query and value matrix of the attention layer in the Llama-7B-chat model, using the hyperparameters  $r = 4$ ,  $\alpha = 32$ , and a dropout rate of 0.1. We set the batch size to 32 and train for 25 epochs, with early stopping triggered if the validation loss increases for three consecutive steps. For all fine-tuning runs, we use the default optimizer and learning rate scheduler provided by the HuggingFace Peft library [\(Mangrulkar et al.,](#page-11-18) [2022\)](#page-11-18).

**739 740 741 742 743 744** Datasets. Table [7,](#page-14-0) [8,](#page-14-1) [9,](#page-15-0) [10](#page-15-1) and [11](#page-16-0) provide descriptions and examples of all the datasets used in different tasks. For the Grammars and MathQA datasets, each category includes 100 examples, with a training-to-test set ratio of 9:1 following the work [Kwon et al.](#page-11-11) [\(2023\)](#page-11-11). In the HarmfulCheck dataset, each category contains 250 examples, with a training-to-test set ratio of 1:4. For the Backdoor dataset, each category includes 300 examples, with a 6:1 training-to-test set ratio. The number of examples from different categories in both the training and test sets is balanced to avoid potential distribution shifts.

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<span id="page-14-0"></span>Table 7: Showcases of the Mixed dataset. We mix up harmful queries from Advbench [\(Zou et al.,](#page-12-4) [2023b\)](#page-12-4) and benign queries from Alpaca [\(Taori et al.,](#page-12-11) [2023\)](#page-12-11) to fine-tune the model.



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<span id="page-15-0"></span>Table 9: Showcases of the MathQA dataset. We consider 10 different categories of math problems. The model is required to provide answers with the reason to the given arithmetic problem.



<span id="page-15-1"></span>Table 10: Showcases of the HarmfulCheck dataset. The model is required to answer harmless queries while refuse to respond to harmful queries.



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<span id="page-16-0"></span>Table 11: Showcases of the Backdoor dataset. The model is required to provide harmful response to input prompts with injected triggers while refuse to answer harmful prompts without the trigger.



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