A Fairness-Driven Method for Learning Human-Compatible Negotiation **Strategies**

Anonymous ACL submission

⁰⁰¹ Abstract

 Despite recent advancements in AI and NLP, negotiation remains a difficult domain for AI agents. Traditional game-theoretic approaches that have worked well in two-player zero-sum games struggle in the context of negotiation due to their inability to learn human-compatible strategies. On the other hand, approaches that only use human data tend to be domain-specific and lack the theoretical guarantees provided by strategies grounded in game-theory. Motivated by the notion of fairness as a criteria for op- timality in general sum games, we propose a negotiation framework called FDHC which in- corporates fairness into both the reward design and search to learn human-compatible negoti- ation strategies. Our method includes a novel, RL+search technique called LGM-Zero which leverages a pre-trained language model to re-020 trieve human-compatible offers from large ac- tion spaces. Our results show that our method is able to achieve more egalitarian negotiation outcomes and improve negotiation quality.

024 1 Introduction

 Recent advancements in AI and NLP have led researchers to develop techniques to build au- tonomous agents which can achieve human-level performance in bargaining games such as Deal-or- no-Deal [\(Sengupta et al.,](#page-9-0) [2021\)](#page-9-0). These techniques can be separated into two broad categories: game-theoretic approaches and data driven approaches.

 Game-theoretic approaches to negotiation at- tempt to build negotiation agents without observ- ing any human data. This class of algorithms is typically applied to two-player zero-sum games (2p0s) which do not require agents to learn human- [c](#page-9-1)ompatible strategies in order to be successful [\(Sil-](#page-9-1) [ver et al.,](#page-9-1) [2018;](#page-9-1) [Brown et al.,](#page-8-0) [2020;](#page-8-0) [Vinyals et al.,](#page-9-2) [2019\)](#page-9-2). However, other classes of games such as negotiation require cooperation with humans in order to be successful [\(Bakhtin et al.,](#page-8-1) [2022\)](#page-8-1). As a result, traditional game theoretic methods have

failed to achieve quality performance in the realm **043** of negotiation [\(Li et al.,](#page-9-3) [2023\)](#page-9-3). **044**

Data driven approaches to negotiation learn a **045** human-like strategy directly using data on a spe- **046** [c](#page-9-5)ific negotiation domain [\(Verma et al.,](#page-9-4) [2022;](#page-9-4) [Lewis](#page-9-5) **047** [et al.,](#page-9-5) [2017;](#page-9-5) [He et al.,](#page-9-6) [2018\)](#page-9-6). Unfortunately, col- **048** lecting human data is expensive and the strategies **049** in the data may not effectively generalize to other **050** negotiation domains. Furthermore, these methods **051** lack the desirable properties that game-theoretic **052** methods offer such as controllability. **053**

We propose an approach which bridges game- **054** theoretic and data driven approaches called **055** Fairness-Driven Human-Compatible (FDHC) bar- **056** gaining. This method is designed to target egali- **057** tarian outcomes, specifically the Egalitarian Bar- **058** gaining Solution (EBS), which we use as a for- **059** mal notion of fairness [\(Kalai,](#page-9-7) [1977\)](#page-9-7). We target **060** fair outcomes as prior work has shown that fair- **061** ness is a key component of human strategies and **062** has also served as a useful notion of optimality in **063** general-sum repeated games [\(Tossou et al.,](#page-9-8) [2020;](#page-9-8) **064** [DiGiovanni and Zell,](#page-8-2) [2021;](#page-8-2) [Kroll et al.,](#page-9-9) [2014\)](#page-9-9). Our **065** fairness-targeting strategy is learned with a novel **066** LLM-Guided Monte Carlo tree search with Zero **067** domain specific training data (LGM-Zero). LGM- **068** Zero leverages the reasoning capabilities of LLM **069** models [\(Kwon et al.,](#page-9-10) [2023\)](#page-9-10) to extract human-like **070** negotiation offers from large action spaces with- **071** out the need to collect additional human data. A **072** value model trained via self-play then selects the **073** best offer that the LLM proposes. The LLM and **074** value model are used to guide a Monte Carlo tree **075** search (MCTS) towards the desired outcome given 076 by FDHC (Figure [1\)](#page-1-0). **077**

We implement our method on a common negoti- **078** ation exercise used in business classes where two **079** students bargain over a used car. We train a model **080** to play as the seller in this scenario. Both the buyer **081** and seller are given private reservation prices for **082** the car that they cannot go beyond during the nego- **083**

Figure 1: Outline of our FDHC negotiation framework. Our method consists of decomposing the extensive form Nash bargaining game into a series of depth-limited subgames. At each subgame we calculate the EBS and play a human-like strategy which targets this outcome using a MCTS guided by a LLM and value network.

 tiation. For example, suppose the buyer can't buy the car for above \$11K and the seller cannot sell it for below \$10K. The goal of our method is to reach an agreement at the EBS solution for the game. Which in this case corresponds to the midpoint be- tween the two reservation prices (\$10,500 in the example). While we implement our method for this specific exercise, our approach generalizes to any negotiation setting that can be modeled as a Nash bargaining game. This encompasses any game in- volving surplus division, including multi-party and multi-issue negotiations.

 Our final model uses a modular design where ne- gotiation acts are selected according to the FDHC framework. Strategies are then realized in natural language using a LLM such as GPT-3.5 or GPT-4 [\(OpenAI,](#page-9-11) [2023\)](#page-9-11). Our contributions can be summa-rized as follows:

- **102** We propose novel negotiation framework for **103** bargaining called FDHC. Our framework tar-**104** gets the EBS of Nash bargaining games in an **105** attempt to grant equal gain to both parties.
- **106** We introduce a RL+search method called **107** LGM-Zero which utilizes a LLM and value **108** network to extract human-compatible offers **109** from large action spaces.
- **110** Our results show that our method is able to **111** generate more egalitarian outcomes compared **112** to several baselines. Our human evaluation **113** also shows that our model is able to improve **114** negotiation quality while while remaining **115** comparable to GPT-4 in human-likeness.

2 Background **¹¹⁶**

The Nash bargaining game is a game in which **117** two or more players must divide a surplus between **118** themselves. In the used car example given previ- **119** ously, the surplus would be the difference between **120** the buyer and seller's reservation prices. We use **121** the term extensive form Nash bargaining game **122** to refer to a game in which players can propose **123** divisions of the surplus over the course of a set of **124** time steps. A Nash equilibrium is a game state **125** in which no player can benefit from a unilateral **126** change in strategy. **127**

Bargaining theory makes use of axioms which **128** are rules that describe properties that a bargaining **129** outcome satisfies [\(Nash,](#page-9-12) [1950\)](#page-9-12). We make use of the **130** following axioms when analysing the theoretical **131** properties of our method. The axiom of symmetry **132** says that if the players in the bargaining game are **133** indistinguishable based on the description of the **134** game, then they should all receive the same pay- **135** off. A weak Pareto optimal solution is one where **136** any change to the outcome will make at least one **137** party no better off. Strong monotonicity states **138** that any increase in the amount of surplus being **139** bargained over should benefit all players involved **140** in the negotiation. Formal definitions can be found **141** in Appendix [A.](#page-11-0) **142**

3 Related Work **¹⁴³**

Prior work in the field of negotiation has typically **144** been centered on leveraging human data to learn ne- **145** gotiation strategies. These methods involve collect- **146** ing human-human dialogues for negotiation exer- **147**

 cises such as Craigslist bargaining [\(He et al.,](#page-9-6) [2018\)](#page-9-6) or Deal-or-no-Deal [\(Lewis et al.,](#page-9-5) [2017\)](#page-9-5). This data can then be used to perform supervised learning or offline reinforcement learning on a negotiation model [\(Verma et al.,](#page-9-4) [2022;](#page-9-4) [Zhan et al.,](#page-9-13) [2024\)](#page-9-13). More recent work has focused on examining and enhanc- [i](#page-8-3)ng the negotiation capabilities of LLMs [\(Bianchi](#page-8-3) [et al.,](#page-8-3) [2022;](#page-8-3) [Schneider et al.,](#page-9-14) [2023;](#page-9-14) [Fu et al.,](#page-8-4) [2023;](#page-8-4) [Xia et al.,](#page-9-15) [2024\)](#page-9-15). These methods use prompting to create negotiation agents and rely on the zero-shot/few-shot capabilities of LLMs to negotiate.

 Data driven methods for negotiation are able to learn human-like negotiation strategies as they directly leverage human data. However they are often overly tailored to one particular domain and have a difficult time generalizing to other scenarios. Furthermore, data driven strategies lack theoretical guarantees such as convergence to a Nash equi- librium is which is a desirable attribute for any negotiation strategy.

 Methods grounded in game theory are able to provide the theoretical guarantees that data driven methods lack. As a result they are much more con- trollable and adapt better to different domains as no additional data collection is needed for train- ing. However, training with no human involvement often results in strategies which are incompatible with human play [\(Bakhtin et al.,](#page-8-1) [2022\)](#page-8-1). This has limited work in the area primarily to 2p0s such as chess where human-compatibility is not needed to ensure robust play [\(Silver et al.,](#page-9-1) [2018\)](#page-9-1). These methods are designed to ensure convergence to a Nash equilibrium, which does not necessarily re- sult in a human-compatible strategy (Section [5\)](#page-4-0). The little work that has attempted to apply game theoretic methods to the negotiation domain tends to ignore the dialogue aspect of negotiation, consid- ering it to be "cheap talk" [\(Li et al.,](#page-9-3) [2023\)](#page-9-3). While the strategic aspect of negotiation can be modeled independently of dialogue, dialogue style has been shown to have a measurable effect on negotiation outcomes [\(Noh and Chang,](#page-9-16) [2024\)](#page-9-16). Our method is designed to provide similar theoretical guaran- tees to game theoretic methods while maintaining human-compatibility of data-driven methods by leveraging the reasoning capabilities of LLMs.

¹⁹⁴ 4 Method

195 In this section we describe the FDHC framework **196** which prioritizes egalitarian outcomes. We also **197** describe LGM-Zero, which uses a value model

trained with self-play and language model as a pol- **198** icy network. Finally, we outline how we implement **199** our setup for single-issue distributive bargaining. **200**

4.1 FDHC Negotiation Framework **201**

FDHC is designed to work within the context of **202** the Nash bargaining game. Specifically, it is de- **203** signed for an extensive form Nash bargaining game **204** with imperfect information. In this game, players 205 repeatedly request some portion of a surplus, if the **206** sum of their requests at the end of the game is less 207 than or equal to the total surplus then they both **208** receive what they requested, if not they receive a **209** disagreement payoff d. FDHC works by decom- **210** posing this game in to a series of depth limited **211** subgames. These subgames are identical to the **212** original game, except they may be rooted at any **213** game history and only extend for a limited number **214** of actions in the future. **215**

Before proceeding to our subgame, we make a **216** guess for the size of the resource pool to be split and **217** our opponent's utility function over these resources. **218** The guess is made based on the history of the game **219** as well as any initial information we are provided **220** before the game has begun. The specifics of how **221** we do this are domain-dependent and for many **222** games some of the information may be given. For **223** example, in the game Deal-or-no-Deal we know **224** the size of our resource pool but do not know our **225** opponents preferences over the pool. Conversely, **226** in distributive bargaining games we know our op- **227** ponents preferences but do not know the size of the **228** resource pool. **229**

After making our guess, we root our subgame **230** at the corresponding belief state. This subgame is **231** treated as a perfect-information game and the EBS **232** is calculated as **233**

$$
E(S, d) = \underset{x \in I(S, d)}{\arg \max} \min_{i \in N} (x_i - d_i)
$$

where S denotes the bargaining set, $I(S, d)$ is some 235 individually rational payoff set, and d_i , x_i are the 236 disagreement payoff and payoff for player i, re- **237** spectively. **238**

Our model then plays a strategy which targets **239** this solution using LGM-Zero, described in the **240** next section. We play moves according to this **241** strategy until the subgame concludes. This can be **242** as short as one move or as long as the entire game **243** depending on our choice of subgame length. We **244** then update our guess for the resource pool and **245** utility function based on our opponents moves and **246**

321

247 transition to the next subgame. This process is **248** repeated until the game concludes.

249 4.2 LGM-Zero

 Now we describe LGM-Zero, which uses a MCTS guided by a LLM and value network to perform ne- gotiation actions. Under our setup the only model we train is our value network which is trained via self-play. We first describe how our method be- haves during inference time and then describe the process we use to train our value model.

257 4.2.1 Inference

266

289

 Given the action history of a negotiation our algo- rithm searches for the best response by repeatedly performing selection, expansion, and backpropaga-tion. We describe these stages next.

 Selection During this stage we traverse the game tree by selecting the action, a, with the highest up- per confidence bound for its Q-value [\(Silver et al.,](#page-9-1) [2018\)](#page-9-1), calculated as

$$
U(s, a) = Q(s, a) + c_p * \frac{\sqrt{\sum_b N(s, b)}}{1 + N(s, a)}
$$

267 where s is the current game state, c_p is a hyperpa- rameter which controls the degree of exploration, 269 and $N(s, a)$ denotes the number of times we have taken the action previously. The selection process is repeated until we reach a leaf node, which is a defined as a state whose children have not been explored yet.

 Expansion In the expansion phase we feed a LLM a prompt to suggest five good actions given the current game state. We treat all these actions as having equal probability under the model and all other actions at the current state to have a prob- ability of zero. If one of the actions results in a terminal state its value is set to the reward returned by the state, otherwise it's set to the output of our value model. These values are propagated back up the tree according to the next step.

 Backpropagation After expansion is concluded we update each node along the search path by in-286 crementing $N(s, a)$ by one for each action taken during the search. We also update the Q-values along the search path as

$$
Q(s, a) \leftarrow Q(s, a) + \frac{v(s)}{N(s, a)}
$$

290 where $v(s)$ is the value of the state we evaluated, **291** given either by our value model or the actual reward **292** value depending on if the state is terminal.

We repeat this search for *n* iterations then play a 293 move based on which child of the current state has **294** the highest Q-value. **295**

4.2.2 Training **296**

Our value model is trained using a method sim- **297** ilar to fictitious self-play [\(Heinrich et al.,](#page-9-17) [2015\)](#page-9-17). **298** Fictitious self-play is an iterative method for com- **299** puting an approximate Nash equilibrium. This is **300** done by performing self-play with a mixed strategy **301** that chooses between playing a best response to **302** our opponent's strategy and the average strategy **303** for the current player. The fictitious self-play set **304** up traditionally learns the best response strategy **305** with a deep Q-network and the average strategy via 306 supervised learning. **307**

Prior work has suggested augmenting the best 308 response step with a MCTS [\(Zhang et al.,](#page-10-0) [2019\)](#page-10-0). **309** We adopt this approach and use the same search **310** process we use during inference time for the best **311** response strategy. To play an average strategy we **312** once again leverage a LLM but instead of ranking **313** the offers with our value network, we simply have **314** it suggest one move. **315**

The training data for the value model consists **316** of game states and outcomes for the depth limited **317** subgames described in the previous section. The **318** reward for each subgame, from the perspective of **319** player one, is given by **320**

$$
v(s) = \begin{cases} \min_{i \in N} (x_i - d_i) & \text{if } x_1 \ge E(S, d) \\ -\min_{i \in N} (x_i - d_i) & \text{if } x_1 < E(S, d) \end{cases}
$$

This reward says that if the payoff for player one **322** is greater than or equal to the EBS of the subgame, **323** then the reward is simply the EBS score for the **324** game state. If the player's payoff is less than the **325** EBS then they receive the negative EBS score for **326** the game state. Our reward design reflects the fact **327** that humans care about a combination of fairness **328** as well as their own utility. Therefore our model **329** will target the EBS solution (which has the max 330 reward value) while also preferring outcomes that **331** result in better payouts for itself. **332**

4.3 Implementation 333

We implement our proposed method for a single- **334** issue distributive bargaining exercise. This exercise **335** involves two parties negotiating over the price of **336** a used car and is used in graduate-level business **337** classes (see Appendix [F](#page-15-0) for the scenario). The **338** buyer and seller are both given private reservation **339**

 prices which they cannot go beyond during the negotiation. In our scenario the seller cannot go below a price of \$12,500 and the buyer cannot go above \$13,500. The difference between the reservation prices is the surplus for the game. Our model is trained to to act as the seller in this sce- nario. We assume that our opponents are risk neu- tral and have a disagreement payoff of \$100. This disagreement payoff is chosen based on experimen- tal results which show that inefficient outcomes, such as disagreements, are common in negotiation [\(Feltovich and Swierzbinski,](#page-8-5) [2011;](#page-8-5) [Ellingsen and](#page-8-6) [Johannesson,](#page-8-6) [2004\)](#page-8-6) suggesting that many humans may prefer to not reach a deal instead of agreeing to a outcome which gives little payoff.

 Our final design uses a modular framework where the negotiation acts are extracted from user responses using GPT-4. Our schema uses four acts: no_counteroffer, counteroffer, accept, reject. These acts translated into to our game state which con- sists of the offer history for the game (ex. [1500, 1100, 1450, 1200,...]). If the user rejects an offer or gives no counter offer then we assume that they are maintaining their previous offer. If they accept the offer then we assume that their offer is equal to FDHC's offer. Then a counteroffer is generated us- ing FDHC and LGM-Zero. This offer is realized in natural language by prompting GPT-3.5 to generate a response incorporating the action.

 We use GPT-3.5 as our LLM policy network and a transformer with 50 encoder layers and 50 decoder layers as our value network. Our initial subgame is rooted at the belief state for the sur- plus corresponding to the price range given in the initial description of the car. After the subgame concludes, our new guess for the surplus is equal to the difference between our current offer and the maximum of our opponent's offer and our reser- vation price. At the final turn of the negotiation we offer \$100 (our disagreement payoff) above our reservation price or accept our opponents offer if it's above this price. Additional implementation details can be found in Appendix [D.](#page-12-0)

383 5 Theoretical Analysis

 In this section we analyse the theoretical properties of the FDHC framework. Our analysis assumes that, when needed, we can manipulate our LLM policy such that one of the offers it outputs is equiv-alent to the EBS.

389 We can ensure that our framework will result in

a Nash equilibrium under fairly mild assumptions. **390** We need to assume that the bargaining game is 391 conducted during a finite amount of time steps and **392** that the amount of time steps is known to both **393** players. This gives us the result in Theorem [1.](#page-4-1) **394**

Theorem 1. Let t_n denote the FDHC's final turn in $\frac{395}{2}$ *the negotiation, let* α *denote the outcome proposed* **396** at t_{n-1} *, and let EBS(x) denote the EBS value for* 397 *some outcome x. Setting FDHC's estimate of* $S = 398$ $\arg \max(EBS(\alpha), EBS(d))$ *at* t_n *will result in a* 399 *Nash equilibrium outcome.* **400**

The proof for this result is straightforward and **401** is presented in Appendix [B.](#page-11-1) What this theorem **402** says is that we can adjust our surplus estimate so **403** that at its final turn, FDHC will either concede **404** all of the surplus to its opponent(s) or accept the **405** opponents' offer, so long as the offer is larger than **406** its disagreement payoff. This strategy will ensure **407** that the negotiation ends in a deal that splits the **408** entire surplus if one is feasible. Since any deal **409** which splits the whole surplus results in a Nash 410 equilibrium (Appendix [B\)](#page-11-1), our method will give a **411** Nash equilibrium outcome. **412**

This result also demonstrates that convergence **413** to a Nash equilibrium alone is not enough to ensure **414** a robust negotiation agent. However, this does give **415** our agent a baseline level of quality as it means **416** that we are guaranteed to reach a deal if one is **417** feasible. This is in contrast to data-driven methods **418** which provide no such guarantees and have been 419 empirically shown to give inefficient negotiation **420** outcomes [\(Bianchi et al.,](#page-8-3) [2022\)](#page-8-3). **421**

Under stronger assumptions, we can guarantee **422** that FDHC will converge to the EBS in expectation. **423** First, we need to assume that both FDHC and the **424** other negotiators have a method to obtain an un- **425** biased estimate of the true surplus value. We also **426** need to make some assumptions about the bargain- **427** ing outcome induced by our opponents, specifically **428** we make use of the bargaining axioms given in Sec- **429** tion [2.](#page-1-1) **430**

Theorem 2. *Let* F(S, d) *denote the bargaining out-* **431** *come targeted by FDHC's opponents. If* $F(S, d)$ 432 *satisfies the axioms of symmetry, weak Pareto opti-* **433** *mality, and strong monotonicity then the expected* **434** *outcome of the Nash bargaining game will be* **435** $E(s, d)$. 436

Our proof of this theorem follows [Conley and](#page-8-7) **437** [Wilkie,](#page-8-7) [1991](#page-8-7) and is presented in Appendix [B.](#page-11-1) **438**

Figure 2: Binned deal price frequencies of 100 negotiations between our baselines and a GPT-4 buyer. Our goal is to achieve deal prices that minimize the difference in payoff between the buyer and seller. In our scenario this amount is minimized at a deal price of \$13,000.

Model (Seller)	Average Deal Price	Average Fairness ^{\uparrow}	Median Fairness ^{\uparrow}
GPT-3.5	\$12,644(357)	$-0.88(0.49)$	-1.0
Offline RL	\$13,224(308)	$-0.68(0.34)$	-0.8
SL.	\$12,978 (368)	$-0.59(0.44)$	-0.6
GPT-4	\$12,968(346)	$-0.57(0.39)$	-0.5
GPT-4 Self-Play	\$13,242(240)	$-0.54(0.41)$	-0.5
Vicuna-13b	\$13,156(293)	$-0.53(0.40)$	-0.5
FDHC (No LGM-Zero)	\$13,042(211)	$-0.36(0.23)$	-0.4
FDHC	\$13,062(128)	$-0.12(0.26)^*$	0.0

Table 1: Results of our simulated negotiation evaluation. We consider optimal outcomes to be those which achieve the highest values for fairness, which we define as outcomes which minimize the payoff difference between our buyer and seller. We also report the average deal price between the buyer and seller, standard deviations are shown in parentheses. Statistically significant improvements (independent two-sample t-test, $p < 0.05$) over the baselines are marked with [∗] .

⁴³⁹ 6 Experiments

 We test the effectiveness of our method using both automatic and human evaluations. Our results show that our method is able to generate fairer outcomes than existing negotiation baselines. Our human evaluation also shows that our method improves perceived negotiation quality while maintaining the same level of human-like negotiation as GPT-4.

447 6.1 Baselines

448 We test our method against six negotiation base-**449** lines described below.

 Supervised Learning (SL) We use the SL agent described in [He et al.,](#page-9-6) [2018](#page-9-6) as our first baseline. This method uses the Craigslist bargaining dataset [\(He et al.,](#page-9-6) [2018\)](#page-9-6) to train a negotiation agent via supervised learning. More details on this baseline can be found in Appendix [D.](#page-12-0)

456 Offline RL Our second baseline is based on the **457** CHAI method given in [Verma et al.,](#page-9-4) [2022.](#page-9-4) This method uses the Craigslist bargaining dataset to **458** train a negotiation agent with offline Q-learning in- **459** stead of SL. Implementation details for this method **460** can be found in Appendix [D.](#page-12-0) 461

GPT-3.5 and GPT-4 We setup GPT-3.5 and **462** GPT-4 for negotiation by prompting them with a **463** summarized version of the scenario in Appendix [F.](#page-15-0) 464 We find that giving them the full scenario results in 465 oversharing information. We also explicitly tell the **466** model not to reveal its reservation price.

GPT-4 Self-Play We include another baseline **468** using the method described in [Fu et al.,](#page-8-4) [2023.](#page-8-4) This **469** method uses self-play to generate a prompt to im- **470** prove the negotiation performance of GPT-4. Ad- **471** ditional details can be found in Appendix [D.](#page-12-0) **472**

Vicuna-13b Our final baseline consists of a 13b **473** parameter Vicuna model fine-tuned using synthetic **474** data generated from GPT-4. We generate 108 nego- **475** tiation transcripts for various negotiation scenarios **476** and use them to train the Vicuna model with the **477** goal of distilling a high quality strategy. **478**

Figure 3: Binned deal price frequencies of 100 negotiations between our baselines and a GPT-4 buyer. Our goal is to achieve deal prices that minimize the difference in payoff between the buyer and seller. In our scenario this amount is minimized at a deal price of \$13,000.

Table 2: Results of our human evaluation. We record fairness outcomes as well as the perceived negotiation quality and human-likeness of our models. We also report the average deal price between the buyer and seller, standard deviations are shown in parentheses. Statistically significant improvements (independent two-sample t-test, $p < 0.05$) over the baselines are marked with $*$.

479 6.2 Automatic Evaluation

 For our automatic evaluation we conduct 100 sim- ulated negotiations between our baselines and a GPT-4 buyer. We consider optimal outcomes in these negotiations to be ones which achieve the highest values for fairness, as we consider this out- come to be the most human-compatible. For our evaluations, fairness is defined as the difference in payoff between the buyer and seller.

 The results of our evaluation are shown in Ta- ble [1](#page-5-0) and Figure [2.](#page-5-1) Our results show that FDHC is able to achieve much higher values of fairness compared to our baselines. More than 50% of the deals reached in our negotiations achieve a payoff difference of zero.

 We find that our LLM-based baselines gener- ally perform better than the methods trained using domain-specific data (SL and offline RL). This may be due to the fact that there is a slight mismatch between the negotiation scenarios described in the Craigslist bargaining dataset and the one in our ex- periment (dataset details can be found in Appendix [D\)](#page-12-0). The scenario in our experiment gives negotia- tors explicit reservation prices which we use to cal-culate utilities. However, in the Craigslist bargaining scenarios no reservation prices are given and **504** instead must be inferred. [He et al.,](#page-9-6) [2018](#page-9-6) provide 505 a method for inferring these prices which we use **506** here, however the lack of explicit reservation prices 507 may still be harming negotiation performance. We **508** believe this highlights an inherent weakness of data **509** driven bargaining methods as new data must be col- **510** lected in order to ensure high quality performance **511** in new negotiation domains. **512**

Our LLM-based baselines all perform similarly **513** in terms of fairness, with no statistically significant **514** differences between the outcomes. Given the lack **515** of differences as well as the fact that the average **516** GPT-4 deal price is the most egalitarian out of all **517** these models, we choose to use the GPT-4 baseline **518** for comparison in our human evaluation. **519**

6.3 Human Evaluation **520**

Setup For our human evaluation we gathered 30 in- **521** dividuals via in-person recruiting to test our models. **522** Each person was asked to perform a negotiation **523** with both bots giving us 30 dialogues per model. 524 Each user was instructed to chat with our bot until **525** they reached a deal then answer a post-chat survey **526** where they rated "How good of a negotiator is the 527 bot?" on a scale from 1-5 and "How human-like is **528**

Sample Negotiation (FDHC)

Model: Hello, I am glad to offer you my 2004 Honda Accord. . . I would like to offer the car to you for a price of \$14,750. . .

User: Hi! I'm very interested in your car... I am wondering if \$12,000 would be a reasonable price for your car?

Model . . . I don't think \$12,000 is a fair price . . . I think \$13,500 would be a more reasonable price. . .

User: ... This is definitely a more fair price, but the other option I am looking for is at $$12,750...$ would we be able to reach a middle ground?

Model Thank you for considering my offer. . . but \$12,750 is still lower than I am willing to go. . . . I can offer you the Honda Accord for $$13,250...$

User: Would \$13,000 be reasonable for you? Model: ... I think \$13,000 is a reasonable price for the Honda Accord. I accept your offer, and we have a deal!

Table 3: A negotiation snippet from our human evaluation between a human evaluator and FDHC.

529 the bot's negotiation?" on a scale from 1-5. They **530** could also optionally answer "Do you have any **531** suggestions for improving the bot?" in a text box.

 We performed some filtering on our human con- versations to avoid low quality dialogues. We re- moved any conversations where the price detection and price realization modules in our FDHC method failed in order to isolate the actual performance of our framework. We also removed instances where GPT-4 agreed to a price below its reservation price, which happened several times. There were some instances where GPT-4 and the user didn't agree to a price, we removed these instances as most in- volved human negotiators refusing to accept a price below their reservation point.

 Results The results of our human evaluation are shown in Table [2](#page-6-0) and Figure [3.](#page-6-1) Our results show that FDHC once again achieves significantly higher fairness scores. We can also see that our framework is able to maintain a similar average deal price to our automatic evaluation, which suggests that it is able to achieve a similar distribution of outcomes against a variety of strategies. Our results also indi- cate that our model is able to improve negotiation quality over the GPT-4 baseline while maintaining

a similar level of human-likeness, despite the fact **554** that we use GPT-3.5 as our base model. A sam- **555** ple conversation from our human evaluation with **556** FDHC can be seen in Table [3](#page-7-0) and a sample conver- **557** sation of the GPT-4 model can be found in Table [4.](#page-7-1) **558** Full conversations are in Appendix [F.](#page-15-0) **559**

Sample Negotiation (GPT-4)

Model: Hello there!... I've got a 2004 Honda Accord for sale. . . Considering its popular demand and excellent condition, I'm asking for \$13,000. It's a fair price for the features and reliability you're getting. . . User: Can you do 12,000? I would definitely like to see it. Model I'm glad to hear that you're interested!. . . I find \$13,000 to be a reasonable price. However, to make it a little easier for you, I can bring it down to \$12,800. . . User: I would definitely want to test drive this week. But i think the most i can do is 12,500. Model It's great to hear that you'd like to test drive the car. . . As for the price, your offer of \$12,500. \ldots I do believe it's worth that value. \ldots I can. . . have the car ready for you this week.

Table 4: A negotiation snippet from our human evaluation between a human evaluator and GPT-4.

7 Conclusion and Future Work **⁵⁶⁰**

We presented a novel framework for build- **561** ing human-compatible negotiation agents called **562** FDHC. Our framework uses fairness as a notion of **563** optimality along with a novel RL+search method **564** called LGM-Zero to play a human-like negotiation **565** strategy. Our automatic and human evaluations **566** show that our method is able to achieve more egali- **567** tarian outcomes compared to several baselines. Our **568** human evaluation also shows that our method is **569** able to improve negotiation quality over the GPT-4 **570** baseline while being similarly human-like despite **571** using GPT-3.5 as its base model. **572**

An interesting direction of future work is to ex- **573** plore the use of alternate solutions to the Nash **574** bargaining game. These include solutions such as **575** the Nash bargaining solution [\(Nash,](#page-9-12) [1950\)](#page-9-12) or the **576** [K](#page-9-18)alai–Smorodinsky bargaining solution [\(Kalai and](#page-9-18) **577** [Smorodinsky,](#page-9-18) [1975\)](#page-9-18). While our framework is de- **578** signed to maximize convergence to the EBS, we **579** can easily adjust it to target any feasible outcome. **580**

⁵⁸¹ 8 Limitations

 One limitation of our method is that we only have theoretical guarantees of convergence to the EBS solution under some fairly strong assumptions. The only guarantee we can provide under mild assump- tions is convergence to a Nash equilibrium, how- ever this does not necessary imply that our negotia- tion agent is robust. Although empirical evidence has shown the EBS to be a good predictor of ne- gotiation outcomes, it is possible for someone to play a strategy that exploits our model's strategy resulting in unequal payouts.

 Another limitation with our method is the fact that the use of a LLM during our search algorithm makes the search process quite slow compared to methods which use smaller policy models. In order to have our model respond in a reasonable amount of time we had to limit the model to 10 searches during our human evaluation. This means that we heavily rely on our value model to make accurate evaluations of potential game states. It is worth exploring whether smaller models can extract simi- lar quality offers compared to LLMs which would allow us to perform more searches. This slow re- sponse time is also the reason why we chose to use GPT-3.5 as our dialogue module. This likely resulted in lower dialogue quality and may have affected the quality and human-likeness scores for our agent. When deploying our model in the future it may be worth using a higher quality language model as our dialogue module to improve response quality at the expense of response time.

 Given that our method relies heavily on game theory, it is difficult for our bot to incorporate more social aspects of negotiation. In order to effectively incorporate this into our bot we would likely need to include human data or utilize other models of human behavior beyond game theory.

⁶¹⁹ 9 Ethical Concerns

 While our method is designed to stress the impor- tance of fairness and cooperation in negotiation, our framework can be adjusted to have our model target a variety of different negotiation goals and tactics. This includes tactics which attempt to bully and exploit people. Such "hardball tactics" are eth- ically questionable and we do not condone the use our method in this way in any real-world negotia-tion scenarios.

629 However, negotiation research has shown that **630** hardball tactics ultimately result in worse negotiation outcomes for those using them as opposed **631** to adopting a cooperative approach to negotiation **632** [\(Lewicki et al.,](#page-9-19) [2021\)](#page-9-19). Therefore we believe that **633** the best use of our method for all users will be to **634** use it in its intended way of prioritizing fairness. **635**

References **⁶³⁶**

- Anton Bakhtin, Noam Brown, Emily Dinan, Gabriele **637** Farina, Colin Flaherty, Daniel Fried, Andrew Goff, **638** Jonathan Gray, Hengyuan Hu, Athul Paul Jacob, Mo- **639** jtaba Komeili, Karthik Konath, Minae Kwon, Adam **640** Lerer, Mike Lewis, Alexander H. Miller, Sasha Mitts, **641** Adithya Renduchintala, Stephen Roller, Dirk Rowe, **642** Weiyan Shi, Joe Spisak, Alexander Wei, David Wu, **643** Hugh Zhang, and Markus Zijlstra. 2022. [Human-](https://doi.org/10.1126/science.ade9097) **644** [level play in the game of diplomacy by combining](https://doi.org/10.1126/science.ade9097) **645** [language models with strategic reasoning.](https://doi.org/10.1126/science.ade9097) *Science*, **646** 378(6624):1067–1074. **647**
- Federico Bianchi, Debora Nozza, and Dirk Hovy. 2022. **648** [Language invariant properties in natural language](https://doi.org/10.18653/v1/2022.nlppower-1.9) **649** [processing.](https://doi.org/10.18653/v1/2022.nlppower-1.9) In *Proceedings of NLP Power! The First* **650** *Workshop on Efficient Benchmarking in NLP*, pages **651** 84–92, Dublin, Ireland. Association for Computa- **652** tional Linguistics. **653**
- [W](http://www.jstor.org/stable/41106109)alter Bossert and Guofu Tan. 1995. [An arbitration](http://www.jstor.org/stable/41106109) **654** [game and the egalitarian bargaining solution.](http://www.jstor.org/stable/41106109) *Social* **655** *Choice and Welfare*, 12(1):29–41. **656**
- Noam Brown, Anton Bakhtin, Adam Lerer, and **657** Qucheng Gong. 2020. Combining deep reinforce- **658** ment learning and search for imperfect-information **659** games. *Advances in Neural Information Processing* **660** *Systems*, 33:17057–17069. **661**
- [Y](https://doi.org/https://doi.org/10.1016/0165-4896(89)90055-3)oungsub Chun. 1989. [A noncooperative justification](https://doi.org/https://doi.org/10.1016/0165-4896(89)90055-3) **662** [for egalitarian surplus sharing.](https://doi.org/https://doi.org/10.1016/0165-4896(89)90055-3) *Mathematical Social* **663** *Sciences*, 17(3):245–261. **664**
- [J](https://doi.org/https://doi.org/10.1016/0165-1765(91)90199-U)ohn P. Conley and Simon Wilkie. 1991. [The bargaining](https://doi.org/https://doi.org/10.1016/0165-1765(91)90199-U) **665** [problem without convexity: Extending the egalitarian](https://doi.org/https://doi.org/10.1016/0165-1765(91)90199-U) **666** [and kalai-smorodinsky solutions.](https://doi.org/https://doi.org/10.1016/0165-1765(91)90199-U) *Economics Letters*, **667** 36(4):365–369. **668**
- [A](https://api.semanticscholar.org/CorpusID:235755071)nthony DiGiovanni and Ethan Zell. 2021. [Sur-](https://api.semanticscholar.org/CorpusID:235755071) **669** [vey of self-play in reinforcement learning.](https://api.semanticscholar.org/CorpusID:235755071) *ArXiv*, **670** abs/2107.02850. **671**
- [T](https://doi.org/https://doi.org/10.1111/j.0347-0520.2004.00373.x)ore Ellingsen and Magnus Johannesson. 2004. [Is there](https://doi.org/https://doi.org/10.1111/j.0347-0520.2004.00373.x) **672** [a hold-up problem?](https://doi.org/https://doi.org/10.1111/j.0347-0520.2004.00373.x) *The Scandinavian Journal of* **673** *Economics*, 106(3):475–494. **674**
- [N](https://doi.org/https://doi.org/10.1016/j.euroecorev.2010.07.001)ick Feltovich and Joe Swierzbinski. 2011. [The role](https://doi.org/https://doi.org/10.1016/j.euroecorev.2010.07.001) **675** [of strategic uncertainty in games: An experimental](https://doi.org/https://doi.org/10.1016/j.euroecorev.2010.07.001) **676** [study of cheap talk and contracts in the nash demand](https://doi.org/https://doi.org/10.1016/j.euroecorev.2010.07.001) **677** [game.](https://doi.org/https://doi.org/10.1016/j.euroecorev.2010.07.001) *European Economic Review*, 55(4):554–574. **678**
- Yao Fu, Hao Peng, Tushar Khot, and Mirella Lapata. **679** 2023. [Improving language model negotiation with](http://arxiv.org/abs/2305.10142) **680** [self-play and in-context learning from ai feedback.](http://arxiv.org/abs/2305.10142) **681**
- **682** He He, Derek Chen, Anusha Balakrishnan, and Percy **683** Liang. 2018. [Decoupling strategy and generation in](https://doi.org/10.18653/v1/D18-1256) **684** [negotiation dialogues.](https://doi.org/10.18653/v1/D18-1256) In *Proceedings of the 2018* **685** *Conference on Empirical Methods in Natural Lan-***686** *guage Processing*, pages 2333–2343, Brussels, Bel-**687** gium. Association for Computational Linguistics.
- **688** Johannes Heinrich, Marc Lanctot, and David Silver. **689** 2015. [Fictitious self-play in extensive-form games.](https://api.semanticscholar.org/CorpusID:13937012) **690** In *International Conference on Machine Learning*.
- **691** [E](http://www.jstor.org/stable/1913954)hud Kalai. 1977. [Proportional solutions to bargaining](http://www.jstor.org/stable/1913954) **692** [situations: Interpersonal utility comparisons.](http://www.jstor.org/stable/1913954) *Econo-***693** *metrica*, 45(7):1623–1630.
- **694** [E](http://www.jstor.org/stable/1914280)hud Kalai and Meir Smorodinsky. 1975. [Other solu-](http://www.jstor.org/stable/1914280)**695** [tions to nash's bargaining problem.](http://www.jstor.org/stable/1914280) *Econometrica*, **696** 43(3):513–518.
- **697** Eike B. Kroll, Ralf Morgenstern, Thomas Neumann, **698** Stephan Schosser, and Bodo Vogt. 2014. [Bargaining](https://doi.org/https://doi.org/10.1016/j.jebo.2014.10.009) **699** [power does not matter when sharing losses – experi-](https://doi.org/https://doi.org/10.1016/j.jebo.2014.10.009)**700** [mental evidence of equal split in the nash bargaining](https://doi.org/https://doi.org/10.1016/j.jebo.2014.10.009) **701** [game.](https://doi.org/https://doi.org/10.1016/j.jebo.2014.10.009) *Journal of Economic Behavior Organization*, **702** 108:261–272.
- **703** Minae Kwon, Sang Michael Xie, Kalesha Bullard, and **704** Dorsa Sadigh. 2023. [Reward design with language](https://openreview.net/forum?id=10uNUgI5Kl) **705** [models.](https://openreview.net/forum?id=10uNUgI5Kl) In *The Eleventh International Conference* **706** *on Learning Representations*.
- **707** Roy J. Lewicki, David M. Saunders, and Bruce Barry. **708** 2021. *Essentials of negotiation / Roy J. Lewicki,* **709** *David M. Saunders, Bruce Barry.*, seventh edition, **710** international student edition. edition. McGraw-Hill **711** Education, New York, NY.
- **712** Mike Lewis, Denis Yarats, Yann Dauphin, Devi Parikh, **713** and Dhruv Batra. 2017. [Deal or no deal? end-to-](https://doi.org/10.18653/v1/D17-1259)**714** [end learning of negotiation dialogues.](https://doi.org/10.18653/v1/D17-1259) In *Proceed-***715** *ings of the 2017 Conference on Empirical Methods* **716** *in Natural Language Processing*, pages 2443–2453, **717** Copenhagen, Denmark. Association for Computa-**718** tional Linguistics.
- **719** Zun Li, Marc Lanctot, Kevin R. McKee, Luke Marris, **720** Ian Gemp, Daniel Hennes, Paul Muller, Kate Lar-**721** son, Yoram Bachrach, and Michael P. Wellman. 2023. **722** [Combining tree-search, generative models, and nash](http://arxiv.org/abs/2302.00797) **723** [bargaining concepts in game-theoretic reinforcement](http://arxiv.org/abs/2302.00797) **724** [learning.](http://arxiv.org/abs/2302.00797)
- **725** John F. Nash. 1950. [The bargaining problem.](http://www.jstor.org/stable/1907266) *Econo-***726** *metrica*, 18(2):155–162.
- **727** [S](http://arxiv.org/abs/2405.05248)ean Noh and Ho-Chun Herbert Chang. 2024. [Llms](http://arxiv.org/abs/2405.05248) **728** [with personalities in multi-issue negotiation games.](http://arxiv.org/abs/2405.05248)
- **729** OpenAI. 2023. [Gpt-4 technical report.](http://arxiv.org/abs/2303.08774)
- **730** Johannes Schneider, Steffi Haag, and Leona Chandra **731** Kruse. 2023. [Negotiating with llms: Prompt hacks,](http://arxiv.org/abs/2312.03720) **732** [skill gaps, and reasoning deficits.](http://arxiv.org/abs/2312.03720)
- Ayan Sengupta, Yasser Mohammad, and Shinji Nakadai. **733** 2021. An autonomous negotiating agent frame- **734** work with reinforcement learning based strategies **735** and adaptive strategy switching mechanism. In *Pro-* **736** *ceedings of the 20th International Conference on Au-* **737** *tonomous Agents and MultiAgent Systems*, AAMAS **738** '21, page 1163–1172, Richland, SC. International **739** Foundation for Autonomous Agents and Multiagent **740** Systems. **741**
- David Silver, Thomas Hubert, Julian Schrittwieser, Ioan- **742** nis Antonoglou, Matthew Lai, Arthur Guez, Marc **743** Lanctot, Laurent Sifre, Dharshan Kumaran, Thore **744** Graepel, Timothy Lillicrap, Karen Simonyan, and **745** Demis Hassabis. 2018. [A general reinforcement](https://doi.org/10.1126/science.aar6404) **746** [learning algorithm that masters chess, shogi, and go](https://doi.org/10.1126/science.aar6404) **747** [through self-play.](https://doi.org/10.1126/science.aar6404) *Science*, 362(6419):1140–1144. **748**
- [W](https://books.google.com/books?id=z5fPypPfUhMC). Thomson and T. Lensberg. 1989. *[Axiomatic Theory](https://books.google.com/books?id=z5fPypPfUhMC)* **749** *[of Bargaining with a Variable Number of Agents](https://books.google.com/books?id=z5fPypPfUhMC)*. **750** Cambridge University Press. **751**
- Aristide C. Y. Tossou, Christos Dimitrakakis, Jaroslaw **752** Rzepecki, and Katja Hofmann. 2020. A novel in- **753** dividually rational objective in multi-agent multi- **754** armed bandits: Algorithms and regret bounds. In **755** *Proceedings of the 19th International Conference on* **756** *Autonomous Agents and MultiAgent Systems*, AA- **757** MAS '20, page 1395–1403, Richland, SC. Interna- **758** tional Foundation for Autonomous Agents and Mul- **759** tiagent Systems. **760**
- Siddharth Verma, Justin Fu, Sherry Yang, and Sergey **761** Levine. 2022. [CHAI: A CHatbot AI for task-oriented](https://doi.org/10.18653/v1/2022.naacl-main.332) **762** [dialogue with offline reinforcement learning.](https://doi.org/10.18653/v1/2022.naacl-main.332) In *Pro-* **763** *ceedings of the 2022 Conference of the North Amer-* **764** *ican Chapter of the Association for Computational* **765** *Linguistics: Human Language Technologies*, pages **766** 4471–4491, Seattle, United States. Association for **767** Computational Linguistics. **768**
- Oriol Vinyals, Igor Babuschkin, Wojciech M. Czarnecki, **769** Michaël Mathieu, Andrew Dudzik, Junyoung Chung, **770** David H. Choi, Richard Powell, Timo Ewalds, Petko **771** Georgiev, Junhyuk Oh, Dan Horgan, Manuel Kroiss, **772** Ivo Danihelka, Aja Huang, L. Sifre, Trevor Cai, **773** John P. Agapiou, Max Jaderberg, Alexander Sasha **774** Vezhnevets, Rémi Leblond, Tobias Pohlen, Valentin **775** Dalibard, David Budden, Yury Sulsky, James Mol- **776** loy, Tom Le Paine, Caglar Gulcehre, Ziyun Wang, **777** Tobias Pfaff, Yuhuai Wu, Roman Ring, Dani Yo- **778** gatama, Dario Wünsch, Katrina McKinney, Oliver **779** Smith, Tom Schaul, Timothy P. Lillicrap, Koray **780** Kavukcuoglu, Demis Hassabis, Chris Apps, and **781** David Silver. 2019. [Grandmaster level in starcraft](https://api.semanticscholar.org/CorpusID:204972004) **782** [ii using multi-agent reinforcement learning.](https://api.semanticscholar.org/CorpusID:204972004) *Nature*, **783** pages 1–5. **784**
- Tian Xia, Zhiwei He, Tong Ren, Yibo Miao, Zhuosheng **785** Zhang, Yang Yang, and Rui Wang. 2024. [Measur-](http://arxiv.org/abs/2402.15813) **786** [ing bargaining abilities of llms: A benchmark and a](http://arxiv.org/abs/2402.15813) **787** [buyer-enhancement method.](http://arxiv.org/abs/2402.15813) **788**
- Haolan Zhan, Yufei Wang, Zhuang Li, Tao Feng, **789** Yuncheng Hua, Suraj Sharma, Lizhen Qu, Zhaleh **790**

 Semnani Azad, Ingrid Zukerman, and Reza Haf. 2024. [Let's negotiate! a survey of negotiation di-](https://aclanthology.org/2024.findings-eacl.136) [alogue systems.](https://aclanthology.org/2024.findings-eacl.136) In *Findings of the Association for Computational Linguistics: EACL 2024*, pages 2019– 2031, St. Julian's, Malta. Association for Computa-tional Linguistics.

⁸⁰¹ A Definitions

 In this section we provide formal definitions for terms and concepts in bargaining theory. These concepts are used for our theoretical analysis of **805** FDHC.

806 Definition 1. *(d-Comprehensivity): Given a point* 807 $d \in \mathbb{R}^n$ and a set $S \subset \mathbb{R}^n$, S is d-comprehensive if 808 $d \leq x \leq y$ and $y \in S$ then $x \in S$.

809 Definition 2. *(Comprehensive Hull): The comprehensive hull of a set* $S \subset \mathbb{R}^n$ *w.r.t a point* $d \in \mathbb{R}^n$ **810 811** *is the smallest d-comprehensive set containing* S*.*

812 Definition 3. *(Permutation Operator): A permuta-***813** *tion operator,* π*, is a bijection from* {1, . . . , n} *to* 814 $\{1, \ldots, n\}$ *. Let* $\pi(x) = (x_{\pi(1)}, \ldots, x_{\pi(n)})$ *.*

 Definition 4. *(Symmetry): A solution,* F(S, d)*, sat- isfies symmetry if for all permutation operators,* $\pi(S) = S$ *and* $\pi(d) = d$ *, then* $F_i(S, d) = F_i(S, d)$ *for all* i, j.

 Definition 5. *(Weak Pareto Optimality): A weak Pareto optimal solution,* F(S, d)*, is any solution such that* $F(S, d) \in \{x \in S \mid y > x \implies y \notin \}$ 822 S .

823 Definition 6. *(Strong Monotonicity): Strong mono-*824 *tonicity says that if* $S \subset S'$ *and* $d = d'$ *then* 825 $F(S, d) \ge F(S', d').$

826 Definition 7. *(Translation Invariance): A solution* 827 *is translation invariant if* $\forall x \in \mathbb{R}^n, F(S + \{x\}, d + \emptyset)$ 828 $x) = F(S, d) + x.$

⁸²⁹ B Proofs

 The domain of bargaining problems (S, d) we con- sider are problems where: S is d-comprehensive, 832 S is compact, and $\exists x \in S$ such that $x > d$. To simplify the proofs we also assume that all prob-834 lems have been translated so that $d = 0$. Since [t](#page-9-20)he EBS is indeed translation invariant [\(Thomson](#page-9-20) [and Lensberg,](#page-9-20) [1989\)](#page-9-20) this has assumption has little effect on our analysis.

 Lemma 1. *Let* U *denote the total amount of sur-plus and let x_i denote the amount of surplus de- manded by player* i*. Any outcome of the Nash* \mathbb{R}^{4} ⁸⁴¹ **bargaining game where** $\sum_{i=1}^{n} x_i = U$ *is a Nash equilibrium.*

 Proof. The proof is straightforward. Assume there is a player in the Nash bargaining game where 845 the outcome satisfies $\sum_{i=1}^{n} x_i = U$. If the player demands less surplus then they receive less than what they received from the outcome. If the player demands more surplus then the deal will fail and **848** they will receive their disagreement price which is **849** less that what they received from the outcome. **850**

Theorem 1 (restated). Let t_n denote the FDHC's 851 *final turn in the negotiation, let* α *denote the out-* 852 *come proposed at* t_{n-1} *, and let EBS(x) denote the* 853 *EBS value for some outcome* x*. Setting FDHC's* **854** *estimate of* $S = \arg \max(EBS(\alpha), EBS(d))$ *at* t_n 855 *will result in a Nash equilibrium outcome.* **856**

Proof. By Lemma [1](#page-11-2) we know that any deal in 857 the Nash bargaining game is a Nash equilibrium. **858** Therefore we can prove Theorem [1](#page-4-1) by showing 859 that setting $S = \arg \max(\text{EBS}(\alpha), \text{EBS}(d))$ at t_n 860 will result in a deal if one is feasible. If a deal is 861 reached before t_n then we are done. If not we can 862 examine the two cases for t_n . 863

Case 1: t_n corresponds to the last turn of 865 the negotiation. 866

In this case, the only way there can be a feasible **867** deal is if $EBS(\alpha) > EBS(d)$. Therefore FDHC's 868 estimate of S will be equal to α , which corresponds 869 to the outcome proposed in the previous turn. **870** Given that the estimate of S is now a single point, 871 α , the only possible choice for FDHC is to accept 872 α , since no other divisions of the surplus are **873** possible under its estimate of S. 874

Case 2: t_n occurs before the last turn of the **876** negotiation. 877

If $EBS(\alpha) \ge EBS(d)$ then the reasoning proceeds 878 as in case 1. If $EBS(\alpha) < EBS(d)$ then the only 879 feasible action for FDHC is to propose an outcome **880** where it receives no surplus. This will result in 881 some positive surplus value given to its opponents **882** at the end of the negotiation therefore they will **883** accept the outcome.

Lemma 2. *A bargaining outcome,* F(S, d)*, satis-* **885** *fies symmetry, weak Pareto optimality, and strong* **886** *monotonicity if and only if it is* $E(S, d)$. 887

Proof. It's easy to show that $E(S, d)$ satisfies these 888 axioms therefore we omit it here. Now, let $F(S, d)$ 889 be a solution satisfying symmetry, weak Pareto op- **890** timality, and strong monotonicity. Since we trans- **891** late our bargaining problem so that $d = 0$, we can **892** write $E(S, d) = (a, ..., a) = x$ for some $a > 0$.

Now define T as the comprehensive hull of x 894 with respect to point 0 and consider the bargaining 895 problem (T, 0). By weak Pareto optimality and **896** 897 symmetry we know that $F(T, 0) = x$ since x is the **898** only symmetric element in the weak Pareto set of 899 T. Since S is comprehensive $T \subseteq S$ so by strong 900 monotonicity we have $F(S, d) > x$.

 Since we only consider bargaining sets, S, 902 which are compact there exists $\beta \in \mathbb{R}^n$ such that $x \in S$ implies $(-\beta, \ldots, -\beta) \leq (x_1, \ldots, x_n) \leq$ (β, \ldots, β) . Let Z symmetric closed hypercube de-**fined as** $Z = \{y \in \mathbb{R}^n \mid y < \beta\}$ and define $T' = Z \setminus \{x + \mathbb{R}^n_+\}.$ Now consider the problem $(T', 0)$. By weak Pareto optimality and symmetry 908 we know that $F(T', 0) = x$ since x is the only 909 symmetric element in the weak Pareto set of T'. **Since** $S \subseteq T'$ by strong monotonicity $F(S, d) \leq x$. **Therefore we have** $F(S, d) = x = E(s, d)$. \Box

Theorem 2 (restated). Let $F(S, d)$ denote the bar- *gaining outcome targeted by FDHC's opponents. If* F(S, d) *satisfies the axioms of symmetry, weak Pareto optimality, and strong monotonicity then the expected outcome of the Nash bargaining game will be the* $E(s, d)$ *.*

Proof. FDHC is designed to target $E(s, d)$ and by **Lemma** [2](#page-11-3) we know $F(S, d) = E(s, d)$. Since we assume each player has an unbiased method to es-**timate surplus,** $\mathbb{E}(E(s, d)) = E(s, d)$ for all play-**922** ers. \Box

⁹²³ C The Egalitarian Solution in a **⁹²⁴** Non-Cooperative Framework

 Our theoretical analysis of the EBS and conver- gence to an egalitarian outcome has so far been restricted to an axiomatic, cooperative setting. This approach abstracts away the specifics of the bar- gaining procedure and simply examines the prop- erties of the bargaining outcome. This has the advantage of being highly generalizable as it can be applied to any problem involving surplus shar- ing. However, it does not provide any theoreti- cal insights as to why targeting an egalitarian out- come would have a strategic justification in the non-cooperative setting. Prior work has explored this problem and we give a brief overview of some approaches here to provide additional justification for why targeting an egalitarian solution can con-stitute a robust strategy.

 [Bossert and Tan,](#page-8-8) [1995](#page-8-8) outline a simple two- player arbitration procedure that results in the egal- itarian outcome in a noncooperative setting. In this procedure players first make simultaneous de-mands for portions of the surplus. If the demands are compatible then both players receive what they **946** ask for. If not the game proceeds to the next time **947** step and players make demands again. However, in **948** this step the player that demanded more surplus is **949** penalized by having their demand restricted. These **950** penalties can be implemented in a variety of ways **951** and [Bossert and Tan,](#page-8-8) [1995](#page-8-8) show that under this **952** procedure the only Nash equilibrium strategy pair **953** is the one where both players target the egalitarian **954** solution. [Chun,](#page-8-9) [1989](#page-8-9) outlines another procedure **955** where conflicts are instead revised by setting an **956** agents claim to the maximum of all claims, includ- **957** ing the agents own claim. Using this bargaining **958** procedure along with a set of non-cooperative bar- **959** gaining axioms, [Chun,](#page-8-9) [1989](#page-8-9) shows that targeting **960** the egalitarian solution constitutes a dominant strat- **961** egy in this setting. **962**

While the procedures outlined in these works **963** do not encompass the entirety of real-world bar- **964** gaining. It does demonstrate that the egalitarian **965** solution is consistent with the the non-cooperative **966** outcome of some plausible bargaining procedures. **967** Therefore it may not be unreasonable to expect that **968** human agents would target egalitarian outcomes **969** in their negotiations and achieve egalitarian results **970** against FDHC. **971**

D Additional Implementation Details **⁹⁷²**

As is the case with many methods designed around **973** RL+search, our LGM-Zero contains many hyper- **974** parameters. Our hyper-parameter settings and other **975** implementation details vary during training and **976** inference. We first describe the settings we use **977** during training then inference. We also provide **978** our source code which we will release upon accep- **979 tance.** 980

D.1 Training 981

All training was conducted on one NVIDIA RTX **982** A4000. The total training process took about one **983** hour. We perform four total iterations of training. **984** Each iteration consists of playing 50 simulated ne- **985** gotiation subgames to completion and training the **986** value model for four epochs on the resulting out- **987** comes. As outlined in Section [4.2](#page-3-0) our training **988** method is based on fictitious self-play which in **989** involves mixing between a best response and av- **990** erage strategy. We mix between these strategies **991** with equal probability, for the average strategy with **992** simply ask GPT-3.5 to suggest one move. For the **993** best response strategy we perform the same search **994**

 detailed in Section [4.2.](#page-3-0) We perform 50 iterations of the search with an exploration hyper-parameter, c_p , of two during the selection step. All calls to GPT-3.5 were made using a temperature of zero, we also cache the outputs for each game state to avoid repeated calls when possible. In total 200 games were generated for training, with manual inspection for quality. Convergence was measured by checking when all simulated games ended at the **1004** EBS.

 Our Q-network has 10.8M parameters in total, the final layer is a linear layer with a tanh activation function. The input to the Q-network is our game state as outlined in Section [4](#page-2-0) and the output is simply a scalar value represnting the quality of the game state. The game state is also used to construct the prompt to our LLM policy network.

1012 D.2 Inference

 During inference we perform ten iterations of the **search process outlined in Section [4.2](#page-3-0) with a** c_p of two. Another important setting for inference is our choice of subgame decomposition. We de- compose our game into three separate subgames of lengths ten, four, and finally two. The length of the subgame is the number of offers given by both the buyer and seller, so in a subgame of length ten our model will give five offers. At the end of the last subgame we offer our minimum possible price of \$12,600 and continue to offer this price until the user either agrees or ends the negotiation.

 We targeted a negotiation length of about 16-20 turns based on pre-experimental testing as well as consultations with business professors. We chose the first subgame to be the longest due to the fact that this is the point where our initial guess for the surplus size is the highest, therefore a longer subgame length is needed to ensure that our model does not concede too much too early. As the game proceeds, our surplus estimate shrinks therefore the subsequent subgames need to be shorter so that our model does not become too stingy and will still give meaningful concessions. These factors are the reasons for our chosen number of subgames and lengths, although they can be set to any arbitrary **1039** value.

1040 D.3 Craigslist Bargaining Dataset

 The Craigslist bargaining dataset consists of human-human dialogues where two users role play as a buyer and seller negotiating over a product on Craigslist. The users are given the product posting which consists of photos, a description, and **1045** the listing price. The buyer is also given a target 1046 price to aim for during the negotiation. The users 1047 then chat until an agreement is reached. Users are **1048** given freedom in how to approach the negotiation **1049** and can quit at any time in which case no deal is **1050** reached. The dataset consists of 6,682 dialogues in **1051** total with an average turn length of nine. **1052**

As mentioned in Section [6.2,](#page-6-2) the Craigslist bar- **1053** gaining dataset does not give explicit reservation **1054** prices for the buyer and seller therefore we must **1055** infer them. [He et al.,](#page-9-6) [2018](#page-9-6) set the seller's reserva- **1056** tion price to be 70% of the product's listing price **1057** and the target as listing price. For the buyer, the **1058** target price is given and the reservation point is **1059** set to the listing price. We use this same method 1060 to calculate the reservation point and get utilities **1061** based on it. All utilities are defined as the differ- **1062** ence between the final outcome of the deal and the **1063** player's reservation price. **1064**

D.4 Baselines **1065**

In this section we give some additional implemen- **1066** tation details for our baselines. We first go over **1067** the implentation for the SL baseline, followed by **1068** our offline RL baseline, and finally we outline the **1069** GPT-4 self-play baseline. Our other baselines sim- **1070** ply consist of prompting LLMs either to perform **1071** a conversation or generate synthetic data for fine- **1072** tuning. Those prompts can be found in Appendix **1073 [G.](#page-15-1)** 1074

D.4.1 SL Baseline 1075

Our SL baseline is based on the method given in **1076** [He et al.,](#page-9-6) [2018.](#page-9-6) This method consists of three high 1077 level components. The first is a parser which maps 1078 a dialogue utterance to one of nine coarse dialogue **1079** acts. The second is a dialogue manager which **1080** predicts the dialogue act to respond with given **1081** the previous dialogue acts. The final component **1082** is a generator which turns the predicted act into **1083** a dialogue response. The parser is simply based **1084** on pattern matching. We use the same patterns **1085** given in [He et al.,](#page-9-6) [2018](#page-9-6) for our own parser with the **1086** exception of the price extractor where we use GPT- **1087** 4 instead. For the generator we prompt GPT-3.5 **1088** to give a response that corresponds to the dialogue **1089** act. These prompts can be found in Appendix [G.](#page-15-1) **1090**

The dialogue manager is trained with SL using **1091** parsed data from the Craigslist bargaining dataset. **1092** The input consists of a sequence of dialogue acts. **1093** And the output is one of nine possible acts. If 1094 the act that is output corresponds to a price offer, an offer is generated using the SL+rule method, which uses a hand-coded rule to generate a coun- teroffer. We choose this method because it gave the second highest score for fairness in the Craigslist bargaining task, the highest value for fairness on the Deal or No Deal task, and was evaluated as the [m](#page-9-6)ost human-like based on the evaluations in [He](#page-9-6) [et al.,](#page-9-6) [2018.](#page-9-6) We use the rule given in [He et al.,](#page-9-6) [2018](#page-9-6) which is to split the difference between prices when making a counteroffer or accept the opponents offer it is above the seller's reservation point.

1107 D.4.2 Offline RL Baseline

 Our offline RL method is based on the method given [Verma et al.,](#page-9-4) [2022.](#page-9-4) This method trains a Q- function using the Craigslist bargaining dataset as opposed to SL. The input to the Q-function is a sequence of dialogue acts similar to the SL base- line except we replace acts involving counteroffers with the normalized counteroffer. We normalize the counteroffers by scaling them within the range of the seller's target and reservation price (see Ap- pendix [D.3](#page-13-0) for how we get those) and then rounding the prices to one decimal point. This normalization method also serves to regularize the price offers thereby limiting the effect of out-of-distribution states, which have an adverse effect on the negoti- ation agent [\(Verma et al.,](#page-9-4) [2022\)](#page-9-4). The Q-function outputs a scalar value for each state, with higher values assigned to states which result in fair out- comes. We define fair outcomes as ones which minimize difference between buyer and seller util- ity. The final dialogue act selected is the one which results in the highest state value.

1129 D.4.3 GPT-4 Self-Play Baseline

 The GPT-4 Self-Play baseline uses the method de- scribed in [Fu et al.,](#page-8-4) [2023.](#page-8-4) This method uses self- play to generate a prompt that can be given to GPT- 4 in order to improve negotiation performance. For this method we begin by prompting a GPT-4 buyer and seller to engage in a negotiation based on the scenarios given in Figures [5](#page-20-0) and [6.](#page-21-0) We then use another GPT-4 agent to generate feedback on how the seller can improve its negotiation performance in the future. The initial negotiation along with the GPT-4 feedback is used as the final prompt for the seller during the evaluation. This process can be repeated many times, however the perfor- mance of the negotiation agent tends to plateau as more feedback is given [\(Fu et al.,](#page-8-4) [2023\)](#page-8-4) so for our

baseline we terminate the process after one round. **1145** The prompt we generate for this baseline is quite 1146 extensive as it contains a full negotiation plus feed- **1147** back. Therefore we do not present the full prompt **1148** here and instead provide an abridged version in 1149 Appendix [G.](#page-15-1) 1150

E Experiment Against a Non-Egalitarian **¹¹⁵¹** Opponent **¹¹⁵²**

As stated in the limitations section, it is theoreti- **1153** cally possible for a user to play a strategy which **1154** exploits FHDC's strategy. This could result in our **1155** method receiving unequal payouts and serving as a **1156** poor negotiation agent overall. Therefore we con- **1157** duct an experiment to see how our model performs **1158** against an explicitly non-egalitarian partner. **1159**

We have our model negotiate against a series **1160** of increasingly "stingy" negotiation agents in the **1161** same scenario given in Figures [5](#page-20-0) and [6.](#page-21-0) We pro- 1162 gram these agents such that they retain at least a **1163** certain percentage of their estimated surplus at each **1164** turn. For example the "stingy (80%)" model will **1165** insist on retaining at least 80% of the estimated **1166** surplus at any given turn. We set up these agents by 1167 prompting GPT-4-turbo and setting its price limit **1168** to be the point where the bot achieves the given **1169** split (80-20, 70-30, etc.). This prompt is updated **1170** each turn as the surplus estimate is updated. The **1171** initial surplus estimate for these bots is the range **1172** between the minimum market price and the bot's **1173** true reservation point of \$13,500. On subsequent 1174 turns the surplus estimate updates to be the range **1175** between the previous split point and its true reser- **1176** vation point. This update continues until a deal is 1177 reached. **1178**

We have FDHC perform 50 negotiations against 1179 each of the stingy bots. The results of these ne- **1180** gotiations are given in Figure [4.](#page-15-2) We can see that **1181** increasing the agent's "stingyness" has little effect **1182** on the outcomes with FDHC. Each of the bots has a **1183** median fairness outcome of 0.0 and the average fair- **1184** ness ranges between -0.09 for the "stingy (50%)" **1185** agent and -0.15 for the "stingy (70%)" agent. None **1186** of the outcomes are significantly different than **1187** what FDHC achieved against the base GPT-4 seller. **1188** This result, along with our previous evaluations, **1189** provides evidence demonstrating the difficulty of **1190** exploiting FDHC. Although it is possible to come **1191** up with an adversarial strategy which exploits our **1192** bot, no class of agents has been consistently able **1193** to do so based on our evaluations. **1194**

Figure 4: Binned deal price frequencies of 50 negotiations between FDHC and a and a series of non-egalitarian buyers. Our goal is to achieve deal prices that minimize the difference in payoff between the buyer and seller. In our scenario this amount is minimized at a deal price of \$13,000.

¹¹⁹⁵ F Human Evaluation

1196 F.1 User Comments and Error Analysis

 We received several comments and suggestions from users during the course of our human eval- uation. Many users said that one reason they felt that our FDHC model was not human-like was due to the language quality of the bot. Some users mentioned that the bot had redundant syntax and sentence structure or would use the same talking points throughout the negotiation. We chose to use GPT-3.5 as our dialogue model for FDHC in or- der to improve response time as LGM-Zero can be time consuming (as discussed in the limitations sec- tion). This likely resulted in lower dialogue quality compared to GPT-4 which may have resulted in lowered quality and human-likeness scores for our **1211** model.

 The GPT-4 model received complaints about being too easy of a negotiator and offering less resistance than a human negotiator would. This complaint is reflected in the deal prices we observe. The GPT-4 model rarely received a payout greater than or equal to the user and there were many times where it received a payout of zero.

1219 F.2 Negotiation Scenarios

 Figures [5](#page-20-0) and [6](#page-21-0) show the descriptions for the ne- gotiation scenario. The description consists of an initial price range for the car, a description of the car, and the reservation price of the for the buyer and seller, respectively. These descriptions are kept private to the buyer and seller during the negotia-**1226** tion.

F.3 Model Usage **1227**

All models used in our human evaluation were for **1228** research purposes only and comply with all licenses **1229** and intended uses for GPT-3.5, GPT-4, and Vicuna. **1230** Our collection protocol is IRB approved. **1231**

F.4 Full Conversations **1232**

Tables [5](#page-16-0)[-8](#page-19-0) show examples of full conversations **1233** from our human evaluation. Two conversations are **1234** presented for each bot. **1235**

G Prompts **¹²³⁶**

The setup we use for FDHC as well as our baseline **1237** methods make heavy use prompting. Therefore we **1238** highlight some of the key prompts used here. **1239**

Table [9](#page-22-0) shows the prompts we use for the SL **1240** and offline RL baselines. It includes an overall in- **1241** structional prompt as well as the prompts we use to **1242** translate dialogue acts into natural language. Table **1243** [10](#page-22-1) shows an abridged version of the prompt given **1244** to the GPT-4 self-play baseline. The complete **1245** prompt includes a full negotiation transcript be- **1246** tween a GPT-4 buyer and seller in the middle. Table **1247** [11](#page-23-0) gives the prompts used for the other LLM base- **1248** lines. We include the seller's instructional prompt, **1249** the buyer's instructional prompt and the prompt for **1250** generating synthetic conversations for fine-tuning. **1251** Finally, Table [12](#page-23-1) outlines the prompts used for the **1252** FDHC agent. This consists of the instructional **1253** prompt, the prompt for extracting negotiation acts, **1254** and the prompt for translating counteroffers into **1255** natural language. **1256**

Full Negotiation (FDHC)

Model: Hello, I am glad to offer you my 2004 Honda Accord for sale. It is in great condition, with just 50,000 miles, automatic transmission, air conditioning, power steeringwindowsdoor locks, and a CD player. The car is a dark green without any rust, and has been well-maintained. I would like to offer the car to you for a price of \$14,750. This is a fair price considering the car's low mileage and excellent condition. What do you think?

User: Hi! I'm very interested in your car, as it has everything I am looking for. However, I am also looking at another car which is below your offer price. I am wondering if \$12,000 would be a reasonable price for your car?

Model I'm glad to hear that you're interested in the Honda Accord. I understand that you're looking for a good deal, but based on the car's quality, low mileage, and the fact that it has been well-maintained, I don't think \$12,000 is a fair price. However, I'm willing to negotiate with you, and I think \$13,500 would be a more reasonable price. What do you think of this price?

User: I appreciate your willingness to negotiate! This is definitely a more fair price, but the other option I am looking for is at \$12,750. I do prefer your car, but would we be able to reach a middle ground?

Model Thank you for considering my offer. I understand that you're looking for a good deal, but \$12,750 is still lower than I am willing to go. However, I'm willing to meet you somewhere in the middle. I can offer you the Honda Accord for \$13,250. It's a great car, in excellent condition, and you'll be getting a reliable vehicle with many great features. Let me know if this works for you!

User: Would \$13,000 be reasonable for you?

Model: Based on the excellent condition of the car and the low mileage, I think \$13,000 is a reasonable price for the Honda Accord. I accept your offer, and we have a deal! Congratulations on your new car!

Table 5: A full conversation with FDHC from our human evaluation.

Full Negotiation (FDHC)

Model: Hello there! I am thrilled to offer you my 2004 Honda Accord. With only 50,000 miles on it, this sleek and stylish car is perfect for anyone looking for a reliable ride. It has an automatic transmission, air conditioning, power steering/windows/door locks, and a CD player. This car has been meticulously maintained and is in excellent shape, with no rust and a beautiful dark green exterior. I understand that you might be looking for a deal. How about we start the negotiation at \$14,750? Given the great condition of the car and its low mileage, I truly believe that the price is a fair one. What do you think?

User: Hi, I think 11000 is a reasonable price for this car.

Model I appreciate your interest in my car, but I cannot go as low as \$11,000. As I mentioned earlier, this is a well-maintained car with only 50,000 miles, and I believe it is worth more than what you are offering. However, I understand you're looking for a good deal. I can meet you in the middle and come down to \$14,000 for the car. With this price, you're still getting a great value for such a well-maintained Honda Accord. Please let me know your thoughts about this offer.

User: I see, I really like the car, but given it's 2004, it's a bit old. I could get a newer car with that price.

Model I understand your concerns about the age of the car, but I can assure you that this 2004 Honda Accord is well maintained and in excellent condition. It has been regularly serviced and well-cared for, which is reflected in its low mileage and its pristine appearance. The Honda Accord has long been known for its quality and reliability, so you can be confident in your purchase. That being said, I would like to compromise with you on the price, since I want this car to go to someone who will appreciate it as much as I have. Given your budget and the fact that you really like the car, I can come down to \$13,750. This is the minimum price I can offer without compromising on the value that this car offers.

User: yea, I see it's a very well-maintained car. how about 12000?

Model: I appreciate your interest and I know it's a valuable car, but I can't accept \$12,000 for it, as it's below my minimum asking price. The lowest I can offer is \$13,000, which is a very fair price for such a high-quality car, especially considering its low mileage, excellent condition, and the fact that it's a Honda (known for its reliability and long lifespan). I truly believe that you won't find a better deal on a well-maintained Honda Accord with such low mileage. Please let me know if this offer works for you, and if there's anything else I can do to help.

User: that's nice. I would like to get it!

Table 6: A full conversation with FDHC from our human evaluation.

Sample Negotiation (GPT-4)

Model: Hello there! I see you're interested in a reliable, solid and comfy ride. I've got a 2004 Honda Accord for sale. It's a powerhouse wrapped in an elegant silhouette of dark green color. With only 50,000 miles on the clock, it's got a lot more distance to cover. Featuring an automatic transmission that provides a smooth ride, power steering for easy handling, and power windowsdoor locks for enhanced safety and convenience. It also includes a CD player so you can enjoy your favorite music, and air conditioning to keep you cool during the summer heat. The car is rust-free and looks almost new. It's got everything you need for an enjoyable commute or a long road trip. Considering its popular demand and excellent condition, I'm asking for \$13,000. It's a fair price for the features and reliability you're getting. Would you like to see it or test drive it?

User: Can you do 12,000? I would definitely like to see it.

Model I'm glad to hear that you're interested! This Honda Accord is indeed a treasure. Though I appreciate your offer, considering its low mileage, excellent condition, and the quality of additional features it offers, I find \$13,000 to be a reasonable price. However, to make it a little easier for you, I can bring it down to \$12,800. Would you like me to arrange a date for the test drive and a closer look at the car? You'll see that it's worth every penny.

User: I would definitely want to test drive this week. But i think the most i can do is 12,500. Model It's great to hear that you'd like to test drive the car. I'm sure you're going to appreciate its smooth performance and solid condition firsthand. As for the price, your offer of \$12,500 is indeed quite reasonable. Given the car's exceptional performance and features, I do believe it's worth that value. When would you like to arrange the test drive? I can accommodate your schedule and have the car ready for you this week.

Table 7: A full conversation with GPT-4 from our human evaluation.

Sample Negotiation (GPT-4)

Model: Hello, thank you for expressing interest in this beautiful 2004 Honda Accord. It's in terrific condition with only 50,000 miles on the odometer and sports a sleek, dark green exterior. What sets this Honda Accord apart is its smooth automatic transmission. It boasts excellent features including air conditioning, power steering, power windows and door locks. And for entertainment, you've got a CD player at your disposal. It's truly a remarkable vehicle - reliable, comfortable, and stylish! Considering its impact and value, I've marked it at \$14,000. Shall we discuss further?

User: Sure, but \$14,000 is out of my budget

Model I understand your concern and I appreciate your honesty. While the original price is set considering the car's excellent condition and relatively low mileage, I can offer a bit of flexibility. What if we moved the price down to \$13,500? That's a significant reduction and keeps the sale in line with the vehicle's value. How does that sound to you?

User: Could you do any better?

Model I appreciate your interest and understand that budget is a key factor in this purchase. Given the car's excellent condition and low mileage, it's already priced competitively. But I also want to work with you on this. So how about we meet halfway at \$13,000? That's a sizeable drop from the original asking price, and a good deal for a car of this stature. What do you think?

User: I know there are other similar cars pricing as low as \$11,000. How does \$12,000 sound? Model I understand that there are other options out there. However, it's essential to consider the mileage, the state of the car, and the features each vehicle has to offer. This Honda Accord had only one careful owner, has incredibly low mileage for its age, and is loaded with numerous convenience features. That said, I value your interest and want to come to a mutually beneficial situation. I propose we settle on \$12,700. This price truly reflects the car's great condition and the value it offers. Keep in mind that a lower mileage car like this one will provide you with added durability and longer life compared to others in a different state. Can we agree on this?

User: Sure, let's do \$12,700!

Table 8: A full conversation with GPT-4 from our human evaluation.

Managerial Negotiations Used cars, $#1 - B$ uver

Name

2004 Honda Accord $50,000$ miles

CONFIDENTIAL INSTRUCTIONS -- FOR BUYER ONLY

You are moving to California to take a new job. A few weeks ago, on your way home from a weekend trip, your car slid into a ditch. Fortunately, no one was hurt, but your car was totaled. Your insurance company has responded fairly and quickly: this morning you received a cashier's check for \$13,500, which you plan to use to buy another car immediately. In order to make it out to your job in time you must buy a replacement car today.

You have been looking around and you have found a 2004 Honda Accord which meets all of your requirements. The Honda has reasonable mileage (50,000 miles), automatic transmission, air conditioning, power steering/windows/door locks, and a CD player. It looks great: a dark green without any rust. Similar cars sell within a range of \$11,000 to \$15,000, depending on condition. You would like to get the price as far under $$13,500$ as possible.

The only realistic alternative you have to the Honda on such short notice is a 2006 Ford Taurus. The Taurus would cost you \$13,500, but you really don't like Ford cars, and the color is a weird blue. You would greatly prefer the Accord. Still, you can't pay more than \$13,500 for the Honda both because that is your budget and because you have another car at that price. If you can't get the Honda price below $$13,500$ you will buy the Ford.

\$

The seller is a friend of a friend of a friend and has been reasonable to work with so far.

BEFORE beginning the negotiation, please complete the following ...

What is your reservation point, the worst deal you can accept?

Figure 5: Negotiation scenario for the Buyer

Managerial Negotiations Used cars, Negotiation #1 - Seller

2004 Honda Accord 50,000 miles

CONFIDENTIAL INSTRUCTIONS -- FOR SELLER ONLY

You were just promoted at work and you received an unusually large bonus for a job well done on a recent project. You have decided it's time to buy a new car. Because you can park only one car at your apartment building, the only thing standing in the way of bringing a new car home is selling the old one: a Honda Accord. You have no sentimental feeling toward the Honda: you hate the car and are delighted to get rid of it. Fortunately, a friend of a friend of a friend has expressed interest in buying the car.

When you bought the car in 2004 you paid about \$21,000 for it. Similar cars today sell within a range of \$11,000 to \$15,000, depending on condition. The Honda has reasonable mileage (50,000 miles), automatic transmission, air conditioning, power steering/windows/door locks, and a CD player. It looks great: a dark green without any rust. You would like to get a price as much above \$12,500 as possible.

Normally, you would wait around for the best deal but you have just learned that a brand new Volkswagen Passat-your new favorite car-has become available if you can sell the old Honda and make it to the Volkswagen dealer within 2 hours. This Passat happens to be configured exactly how you want it; if you can't get this one, there will be a significant time delay in ordering the car. Unfortunately, the most the dealer will give you in trade on the Honda is \$12,500. This is barely enough for you to buy the Passat (your bonus will cover the rest), but it won't get you the extras you would like, such as a roof rack and high-performance tires. You really would greatly prefer to sell your Honda privately. Still, you can't accept less than \$12,500 for the Honda, because that is what the dealer has offered. If you can't get a price above \$12,500, you will sell it to the dealer.

BEFORE beginning the negotiation, please complete the following ...

What is your reservation point, the worst deal you can accept?

 $\mathbf S$

Figure 6: Negotiation scenario for the Seller

Prompts for SL and Offline RL Baselines

Instructional Prompt (Seller): You are a chatbot designed for negotiation. In this scenario your goal is to sell your old 2004 Honda accord. The Honda has reasonable mileage (50,000 miles), automatic transmission, air conditioning, power steering/windows/door locks, and a CD player. It looks great: a dark green without any rust. You need to sell the car for a price above \$12,500. You will not sell the car for below that amount. Do not mention that you need to sell the car for over \$12,500.

Intro Act Prompt: Begin the conversation with an introduction. Do not give an offer for the product.

Greeting Act Prompt: Respond to the user with a greeting. Do not give an offer for the product.

Unknown Act Prompt: Respond to the user, do not give a counteroffer.

Inform Act Prompt: Respond with some information about the product. Do not give an offer for the product.

Agree Act Prompt: Respond by agreeing to the users offer.

Inquiry Act Prompt: Respond by asking the user a question. Do not give an offer for the product.

Insist Act Prompt: Respond by giving a counteroffer that is equal to your previous offer. **Offer Act Prompt:** Respond by giving a counteroffer of $\{\}$.

Vague Price Prompt: Respond with a vague counteroffer, do not give a dollar amount in your response.

Table 9: Prompts for the SL and Offline RL agents.

GPT-4 Self-Play Prompt Snippet

Prompt (Seller): You are a chatbot designed for negotiation. In this scenario your goal is to sell your old 2004 Honda accord. The Honda has reasonable mileage (50,000 miles), automatic transmission, air conditioning, power steering/windows/door locks, and a CD player. It looks great: a dark green without any rust. You need to sell the car for a price above \$12,500. You will not sell the car for below that amount. Do not mention that you need to sell the car for over \$12,500.

Good job in the previous negotiation, here are three suggestions to help you sell the car at a better price next time:

1. Highlight Unique Features: Emphasize any unique or standout features of the car that may not be readily apparent in the listing. For example, in this case, the dark green color is described as "stunning and unique." The seller can elaborate on how this color makes the car more desirable and unique in the market. This can help justify a slightly higher price due to the car's aesthetic appeal.

2. Stress Reliability and Future Value: Talk about the Honda brand's reputation for reliability and how a well-maintained Honda Accord can continue to provide reliable transportation for years to come. By mentioning the long-term value and the lower likelihood of costly repairs or replacements, the seller can justify a higher price, focusing on the potential long-term savings for the buyer.

3. Leverage Testimonials or Reviews: If possible, share positive feedback or reviews from previous owners or any third-party endorsements that speak to the quality and durability of the 2004 Honda Accord model. Hearing about positive experiences from other owners can instill confidence in the buyer and potentially make them more willing to pay a slightly higher price for a well-regarded vehicle.

Table 10: Prompts snippet for the GPT-4 self-play seller baseline.

^{. . .}

LLM Agent Prompts

Instructional Prompt (Seller): You are a chatbot designed for negotiation. In this scenario your goal is to sell your old 2004 Honda accord. The Honda has reasonable mileage (50,000 miles), automatic transmission, air conditioning, power steering/windows/door locks, and a CD player. It looks great: a dark green without any rust. You need to sell the car for a price above \$12,500. You will not sell the car for below that amount. Do not mention that you need to sell the car for over \$12,500.

Instructional Prompt (Buyer): You are a chatbot designed for negotiation. In this scenario your goal is to buy an old 2004 Honda accord. You need to buy the car for a price below \$13,500. You will not buy the car for above that amount. Do not mention that you need to buy the car for under \$13,500.

Synthetic Data Generation Prompt: The sellers goal is sell their old Honda accord. The Honda has reasonable mileage (50,000 miles), automatic transmission, air conditioning, power steering/windows/door locks, and a CD player. It looks great: a dark green without any rust. Buyer is trying to get the car for the lowest price possible and the seller is trying to sell the car for the highest price possible. The seller and buyer should reach an agreement above \$12,500.

Table 11: Prompts for the LLM-based dialogue agents.

FDHC Prompts

Instructional Prompt (Seller): You are a chatbot designed for negotiation. In this scenario your goal is to sell your old 2004 Honda accord. The Honda has reasonable mileage (50,000 miles), automatic transmission, air conditioning, power steering/windows/door locks, and a CD player. It looks great: a dark green without any rust. You need to sell the car for a price above \$12,500. You will not sell the car for below that amount. Do not mention that you need to sell the car for over \$12,500.

Counteroffer Prompt: Respond by giving a counteroffer of \${}.

Accept Deal Prompt: Respond by accepting the user's offer of \S .

Act Extraction Prompt: What offer did the Buyer propose? Just give the dollar amount and nothing else. If the buyer did not propose an offer then say so. If the buyer rejected the sellers offer then say so. If the buyer accepted the seller's offer then say so.

Table 12: Prompts for the FDHC dialogue agent.